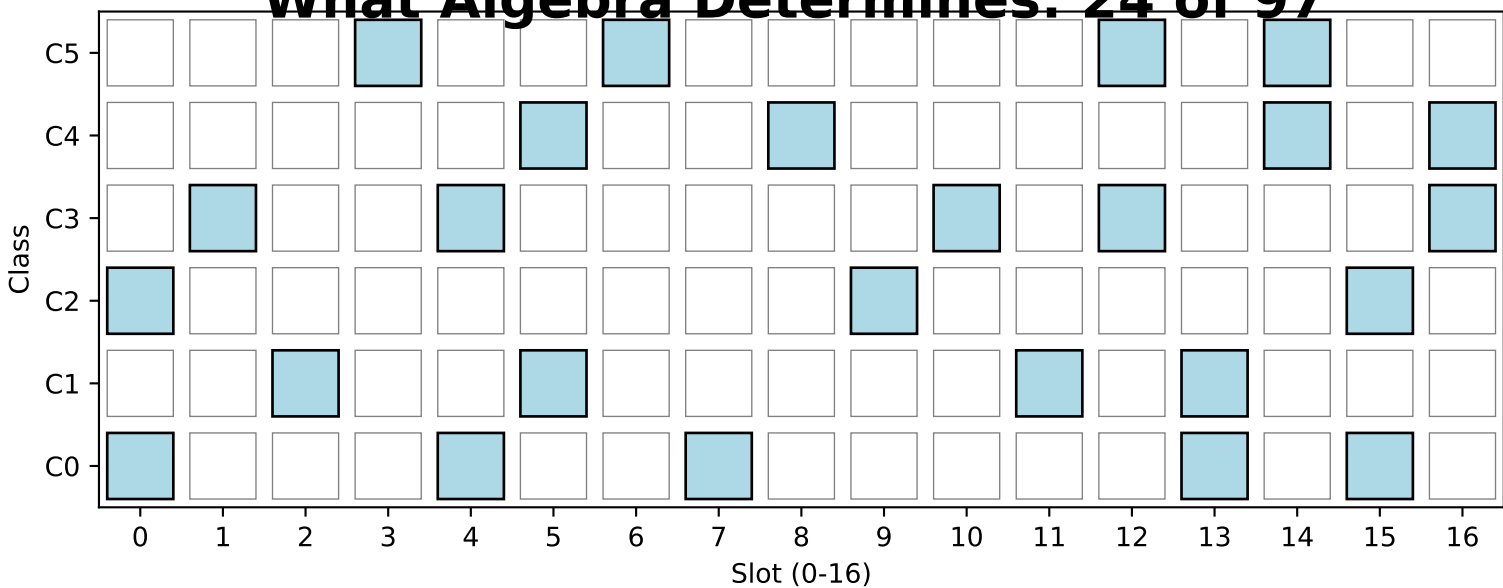
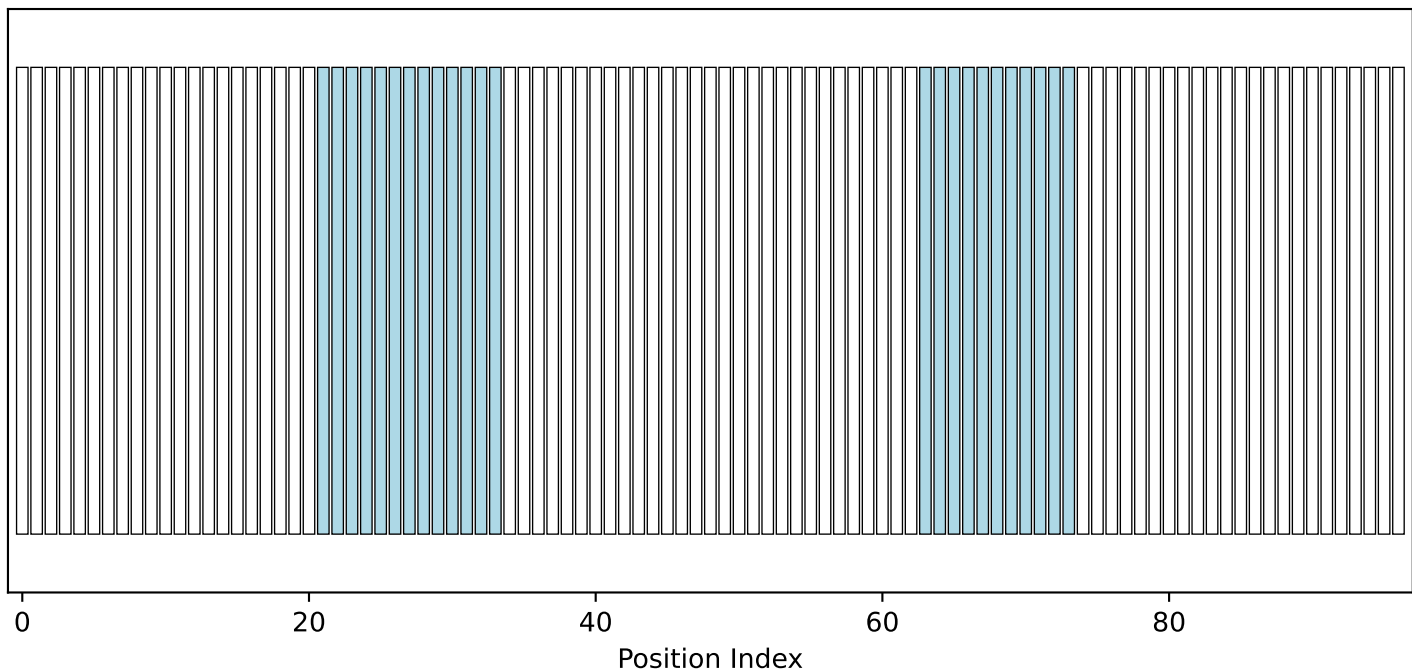


# What Algebra Determines: 24 of 97

Slot Grid: 6 Classes x 17 Slots



## 97 Plaintext Positions (Blue = Algebraically Determined)



Key Insight: The co-prime property ( $L=17$  with 97 positions) ensures:

- Each slot appears at most once per class
- 4 anchor cribs force 24 unique slots
- These 24 slots map to exactly 24 plaintext positions
- The remaining 73 positions remain algebraically undetermined

With only algebra and the 4 anchors, we can determine exactly 24 of 97 positions. No additional positions can be derived without more information.

Test 1: Position 74 (After CLOCK)

# Structure Tests: Tail Region & Position 74

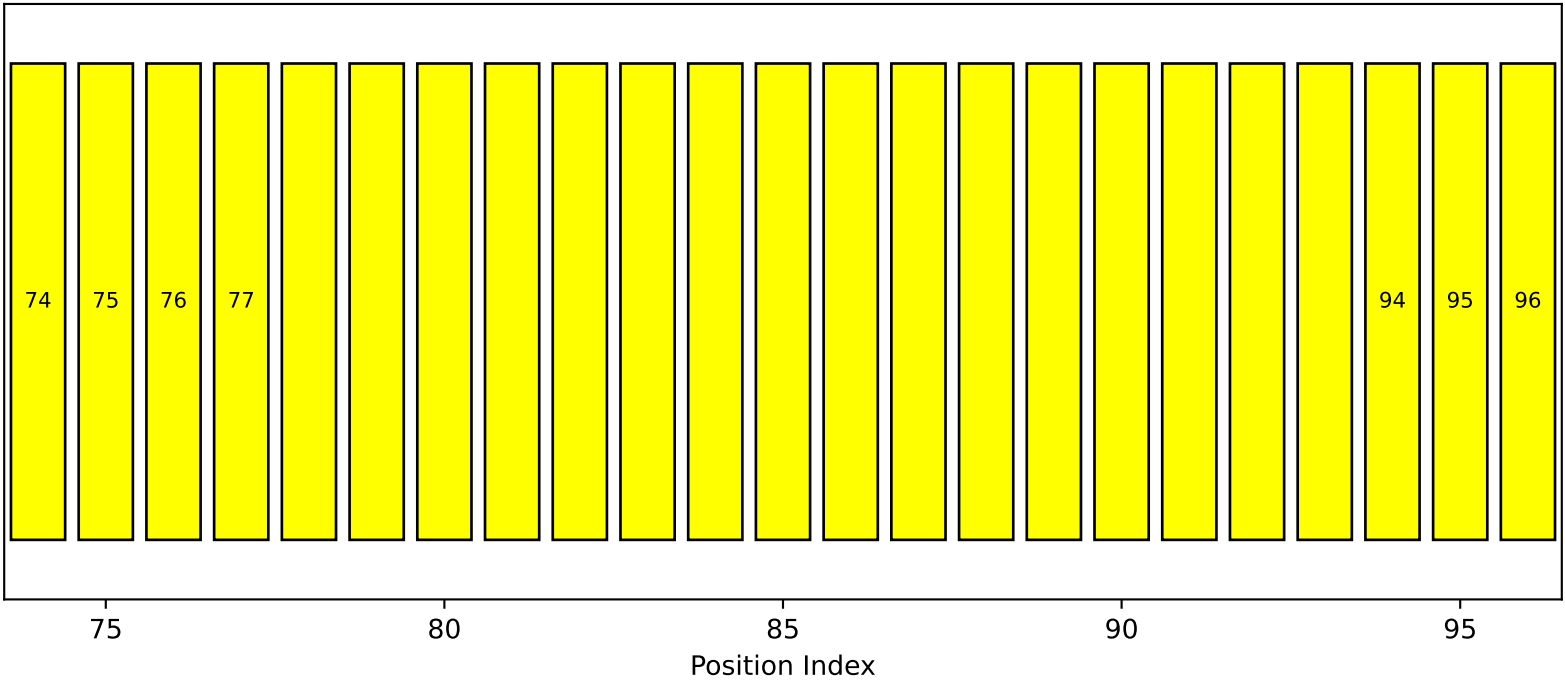
Position 74 Analysis:

- Index: 74
- Class:  $((74 \% 2) * 3) + (74 \% 3) = 2$
- Slot:  $74 \% 17 = 6$
- Status: NOT forced by any anchor



Result: P74 is algebraically UNCONSTRAINED. Any of 26 letters possible.

## Test 2: Tail Region (Positions 74-96)



Tail Region (74-96) Analysis:

- 23 positions after last anchor (CLOCK ends at 73)
- ZERO tail positions constrained by anchors
- All 23 tail positions remain algebraically free

Falsifiable Claim: Without additional information beyond the 4 anchors, the entire tail region (positions 74-96) has  $26^{23}$  possible configurations.

This demonstrates the limit of algebraic constraint propagation.

# K1: Standard Vigenère (PALIMPSEST × 2)

## K1-K3 Mechanical Precedents

- Key: PALIMPSEST PALIMPSEST
- Length: 10 characters repeated
- Method:  $C[i] = (P[i] + K[i \bmod 10]) \bmod 26$
- Solved: 1999 (brute force search)

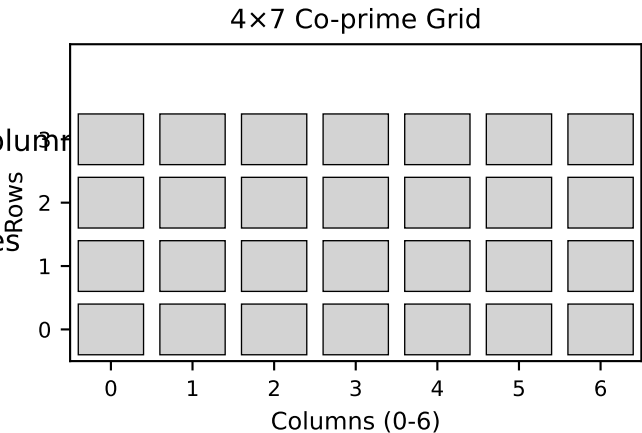
### K2: Keyed Caesar (ABSCISSA)

- Key: ABSCISSA (single word)
- Alphabet: ABSCISSA + remaining letters
- Method: Monoalphabetic substitution with keyed alphabet
- Solved: 1999 (frequency analysis)

### K3: Columnar Transposition + Vigenère

- Stage 1: Columnar transposition (4 rows × 7 columns)
- Stage 2: Vigenère decryption
- Co-prime dimensions:  $\gcd(4,7) = 1$
- Key insight: Fixed pattern from typographic cues
- Solved: 2000 (pattern recognition)

The 4×7 grid ensures full coverage through co-prime property - precedent for K4's 97 positions with L=17.



# Current Algebraic Constraints

## What Forces Unique Solution?

With 4 Anchors Alone:

- ✓ 24 positions determined (indices where anchors appear)
- ✗ 73 positions undetermined
- ✗  $26^{73}$  possible completions

The algebra cannot determine more without additional information.

## Potential Additional Constraints

To achieve unique solution, need ONE of:

1. More anchor positions (cribs/known plaintext)
  - Each new anchor potentially determines its slot
2. Language constraints (if plaintext is English)
  - Dictionary words, bigram/trigram frequencies
  - Semantic coherence
3. Additional algebraic structure
  - Constraints on key material
  - Relationships between positions
4. The actual plaintext (ground truth)

## Falsifiable Predictions

If this analysis is correct:

- Adding a 5th anchor at an unconstrained position would determine exactly 1 more position (25 total)
- The tail region (74-96) cannot be determined without information beyond the current 4 anchors
- Position 74 specifically must remain free under any algebraic analysis using only the 4 anchors
- No algebraic manipulation can extract more than 24 positions from these specific 4 anchors with  $L=17$