## **ILP** formulation

- q is an upper bound of the total quantity of MDS (lenght/2)
- = is string equivalence
- MIC[i,j] (MAC[i,j]) is the substring starting at i and finishing at j (i,j being positions) of the MIC(MAC). Can be trivially defined using string concatenation and MIC(i,c) (MAC(i,c)).
- Inverse(String) is the Watson-Crick reverse complement of String
- Size of the Oxytricha Input genome: MIC is fragmented into ~750 000 MDSs, MAC into 300 000.
- Variables marked with \* are populated during the preprocessing phase.

$$\begin{aligned} objective function: & & & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$$

 $MDS_{MICstart}(i,a) + MDS_{MICend}(i,b) + MDS_{MACstart}(i,c) + MDS_{MACend}(i,d) + IES(i) = 5 \Rightarrow MIC[a,b] = Inverse(MAC[c,d])$ 

 $MDS_{MICstart}(i,a) + MDS_{MICend}(i,b) + MDS_{MACstart}(i,c) + MDS_{MACend}(i,d) = 4,IES(i) = 0 \Rightarrow MIC[a,b] = MAC[c,d]$ 

$$\sum_{i} MDS_{MICstart}(i,j) \le 1$$

$$\sum_{j} MDS_{MICend}(i,j) = \sum_{j} MDS_{MICstart}(i,j)$$

$$Eq(i,j,h,l) = \begin{cases} 0 \\ 1, & \text{if } MIC[i:j] = MAC[h:l] \end{cases}$$

$$P_{start}(i,j) = \begin{cases} 0 \\ 1, & \text{if } MDS_{MACstart}(i,j) = 1, \text{ Pointer } i \text{ starts at position } j \text{ in the MAC} \end{cases}$$

$$P_{end}(i,j) = \begin{cases} 0 \\ 1, & \text{if } MDS_{MACend}(i-1,j) = 1, \text{ Pointer } i \text{ ends at position } j \text{ in the MAC} \end{cases}$$

$$Cov_{MIC}(i,j) = \begin{cases} 0 \\ 1, & \text{if MDS } i \text{ covers the position } j \text{ in the MIC} \end{cases}$$

$$Cov_{MIC}(i,j) = \begin{cases} 0 \\ 1, & \text{if } \sum_{l \leq i} MDS_{MICstart}(i,l) + \sum_{l < i} MDS_{MICend}(i,l) = 1 \end{cases}$$

$$Cov_{MAC}(i,j) = \begin{cases} 0 \\ 1, & \text{if MDS } i \text{ covers the position } j \text{ in the MAC} \end{cases}$$

$$Cov_{MAC}(i,j) = \begin{cases} 0 \\ 1, & \text{if } \sum_{l \leq i} MDS_{MACstart}(i,l) + \sum_{l < i} MDS_{MACend}(i,l) = 1 \end{cases}$$

$$Cov_{MIC}(i,j) \ge MDS_{MICstart}(i,j)$$

$$Cov_{MAC}(i,j) \ge MDS_{MACstart}(i,j)$$

$$Cov_{MIC}(i,j) = 3 - (cov_{MIC}(i,j-1) + cov_{MAC}(i,j+1) + MDS_{MICstart}(i,j) + MDS_{MICend}(i,j))$$

$$Cov_{MAC}(i,j) = 3 - (cov_{MAC}(i,j-1) + cov_{MAC}(i,j+1) + MDS_{MACstart}(i,j) + MDS_{MACend}(i,j)) + MDS_{MACend}(i,j) + M$$

$$Cov_{MIC}(i,j) = \sum_{l < i} MDS_{MICstart}(i,l) + \sum_{l < i} MDS_{MICend}(i,l)$$

$$Cov_{MAC}(i,j) = \sum_{l < i} MDS_{MACstart}(i,l) + \sum_{l < i} MDS_{MACend}(i,l)$$