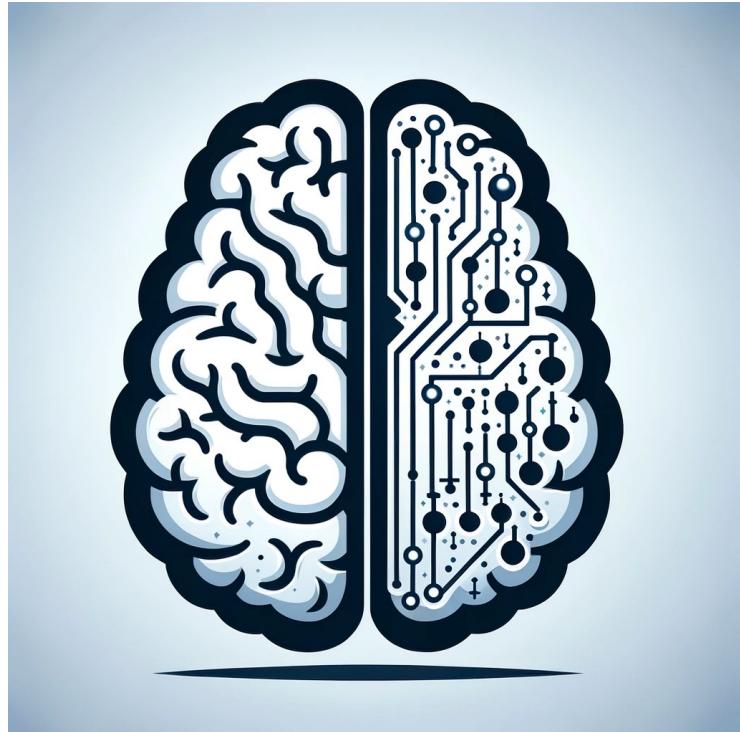


# **EN 601.473/601.673: Cognitive Artificial Intelligence (CogAI)**



**Lecture 7:  
Intro to PPLs (WebPPL, Gen)**

**Tianmin Shu**

# **Logistics**

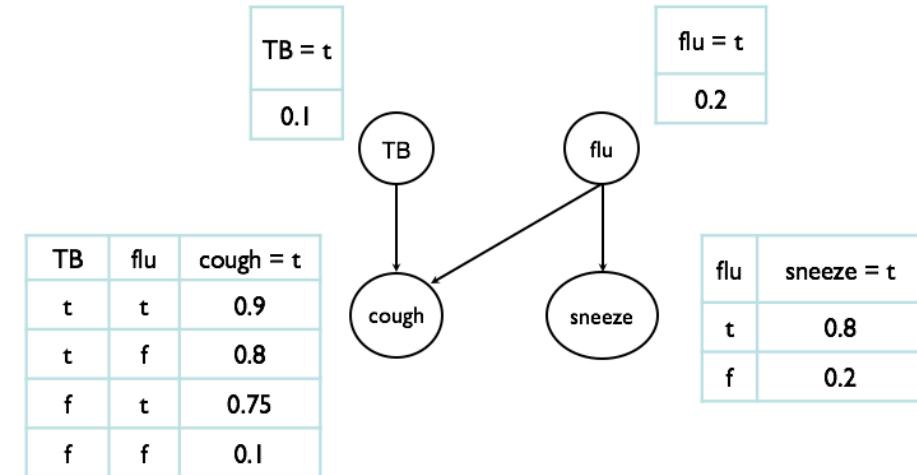
- Pset 1: due by Sunday, Feb 18, end of the day

# Readings

- Probmods.org, chapters 2, 3, & 5
- From word models to world models (Sec. 2)
- The original Gen paper
- Three papers on real-world applications using Gen: data modeling and 3D computer vision (recommended background: computer vision)

# Towards a probabilistic language of thought

- Bayesian networks
  - Mathematically convenient
  - Causal models
  - Hard to write code for inference algorithms
- Probabilistic programs
  - Have rich compositionality
    - Recall: composing programs for priors for the number game
  - Provide a complete specification of the domain (nothing hidden behind arrows)
  - Probabilistic programming languages (PPLs) provide tools for easily and flexibly implement efficient inference algorithms
  - PPLs for Bayesian models, DL frameworks (e.g., pytorch) for neural networks
  - Connected to natural language via LMs



```
var towModel = function() {
  var strength = mem(function (person) {return gaussian(50, 10)})

  var lazy = function(person) {return flip(0.1) }

  var pulling = function(person) {
    return lazy(person) ? strength(person) / 2 : strength(person) }

  var totalPulling = function (team) {return sum(map(pulling, team))}

  var winner = function (team1, team2) {
    totalPulling(team1) > totalPulling(team2) ? team1 : team2 }

  var beat = function(team1,team2){winner(team1,team2) == team1}

  condition(beat(['bob'], ['tom']))

  return strength('bob')
}
```

# Universal probabilistic programming

## WebPPL (Church 2.0)

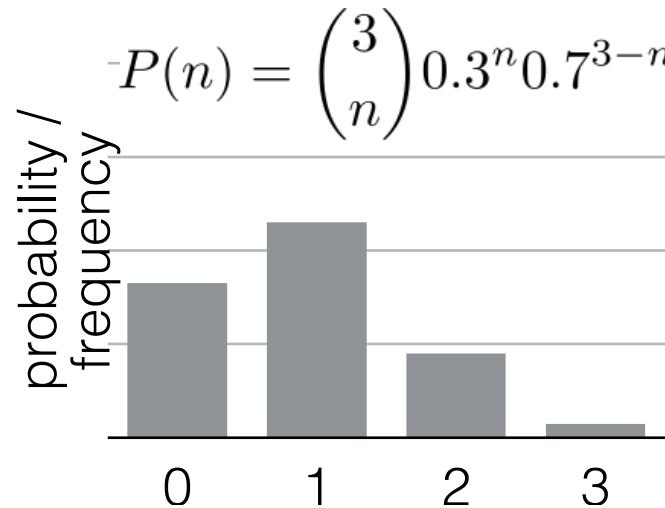
Named after Alonzo Church who is known for lambda calculus

Relationship between sampling and probability distributions

Random primitives:

```
var a = flip(0.3)
var b = flip(0.3)
var c = flip(0.3)
return a + b + c
```

=> 1 0 0  
=> 0 0 0  
=> 1 0 1 ...  
=> 2 0 1



Sampling

$\approx$



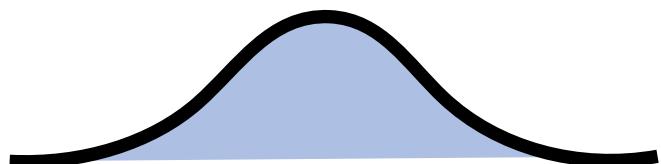
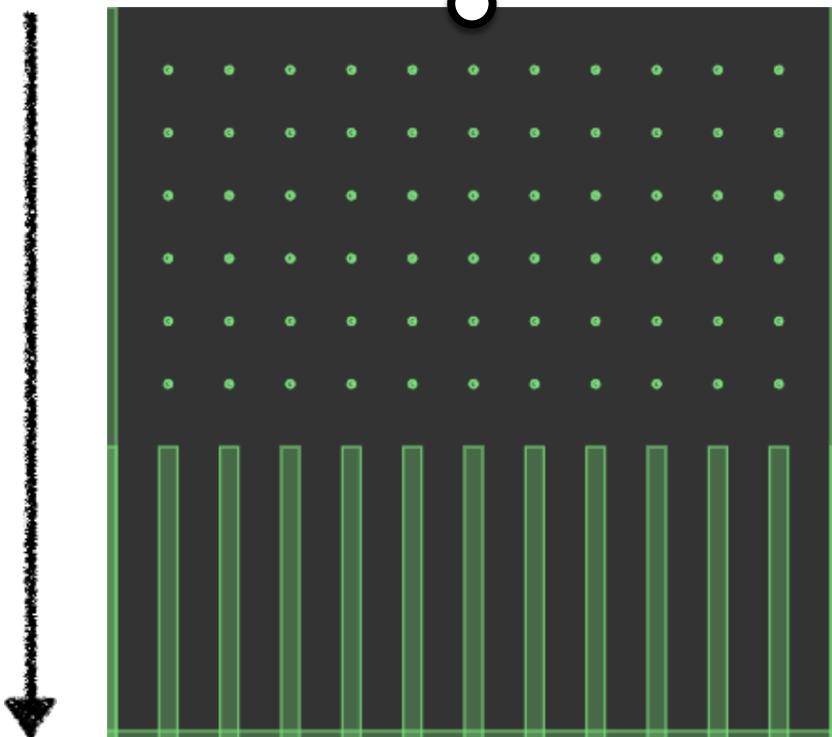
Distributions

Theorem: any computable distribution can be represented as the distribution induced by sampling from a probabilistic program

# Inference in PPLs

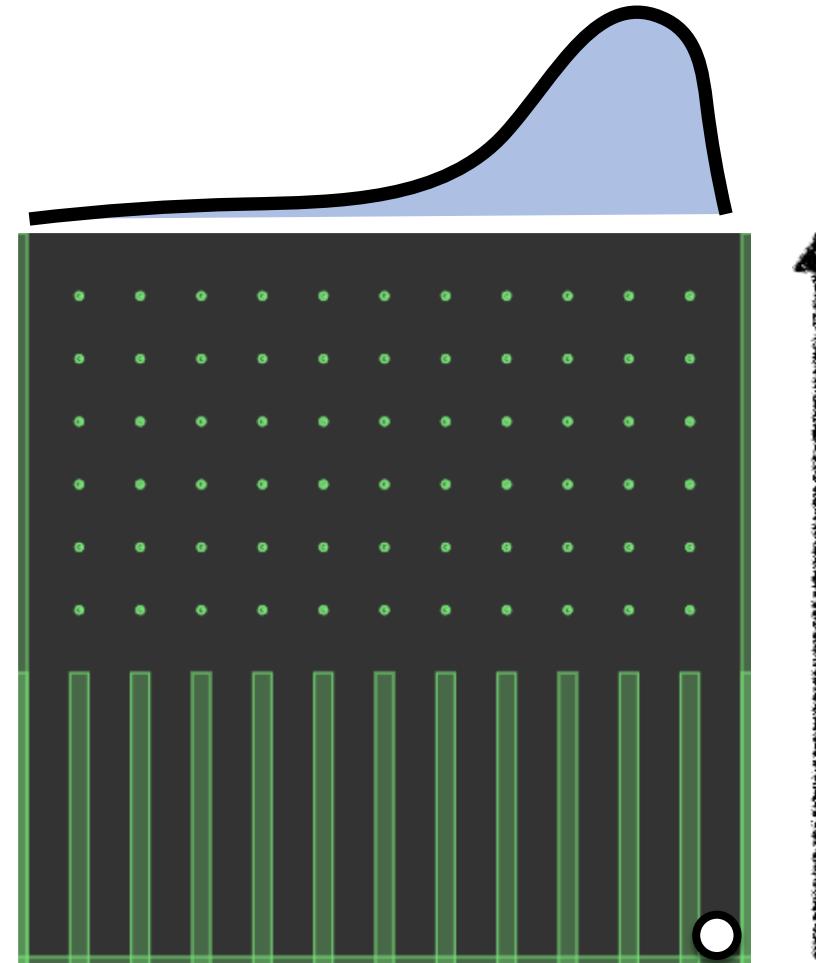
Run forward

Where will the ball land?



Reason backward

Where did the ball come from?

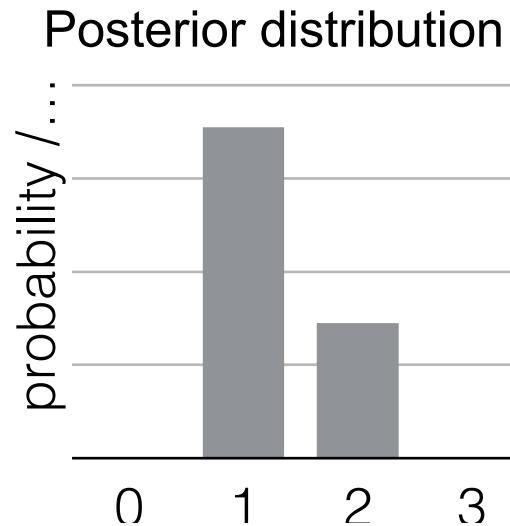


# Inference in PPLs

Conditional inference:

```
Infer(  
    function(){  
        var a = flip(0.3)  
        var b = flip(0.3)  
        var c = flip(0.3)  
        condition(a + b == 1)  
        return a + b + c  
    })
```

=>	1	0	0	1
=> 1	0	0	0	1
=> 0	0	0	0	0
=> 1	0	1	0	0
=> T	F	F	T	T
=> 2	0	1	1	1



- Rejection sampling is essentially a procedural definition of inference.
- Allowing inference with any computable condition statement  $\leftrightarrow$  (almost) supporting any computable conditional distribution.

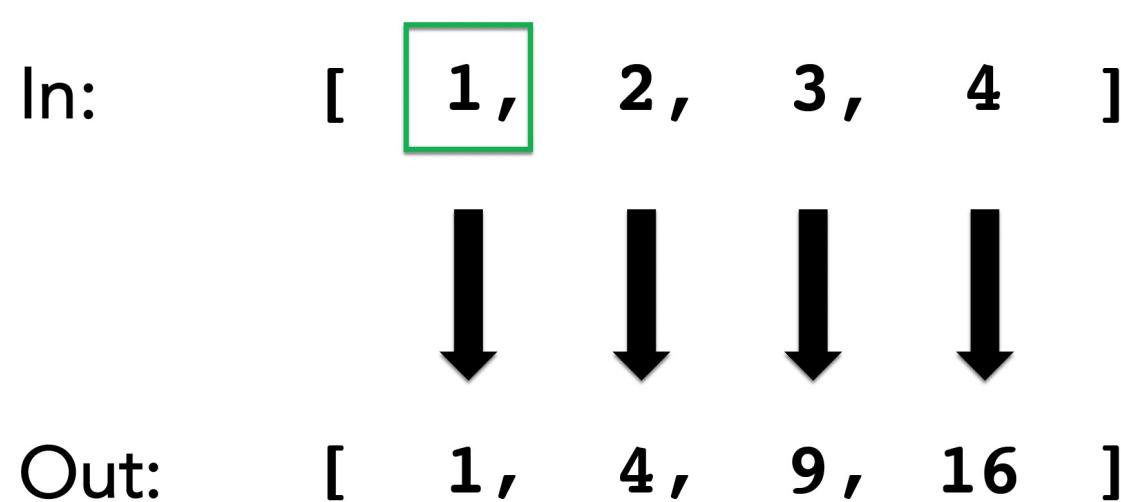
# WebPPL basics

- Declare variables (random variables in a Bayesian model)
- Data formats: numbers, strings, logicals, objects, arrays
- if-then-statements
- defining functions
- Higher order functions
  - `map`

# WebPPL basics

- The map function

```
var mySquare = function(x){return x*x}  
var someNumbers = [1,2,3,4]  
display(map(mySquare, someNumbers))
```



# WebPPL basics

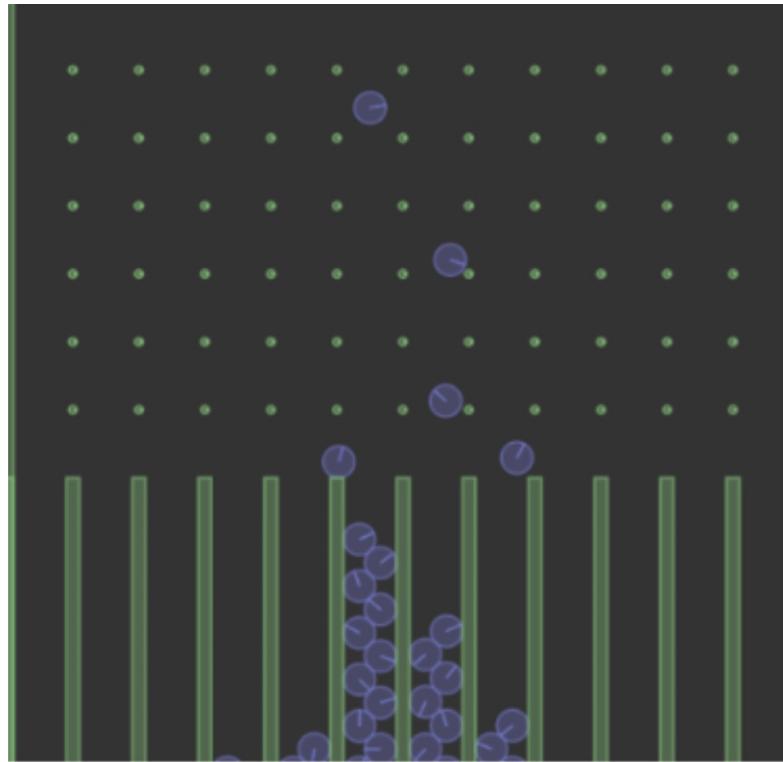
- WebPPL = purely functional programming language
- Can't write `for` loops or `while` statements
- Can create higher-order functions and recursive functions
  - For example: `map` = apply a function to each statement of a list (like a for loop)

# Inference in practice

- WebPPL supports a range of inference procedures
  - forward, rejection, enumerate, MCMC, ...
- Don't worry about the details or mechanisms of inference. Very nice, and very also limiting.
- But a good tool for parsimoniously describing rich generative model structures, and exploring the basic patterns of inference that emerge from the interaction of models and data.
- **Gen** (<https://www.gen.dev/>) supports inference programming: composing short (compact, understandable) programs for efficient inference, out of basic inference primitives.
- A much better tool for scalable engineering.

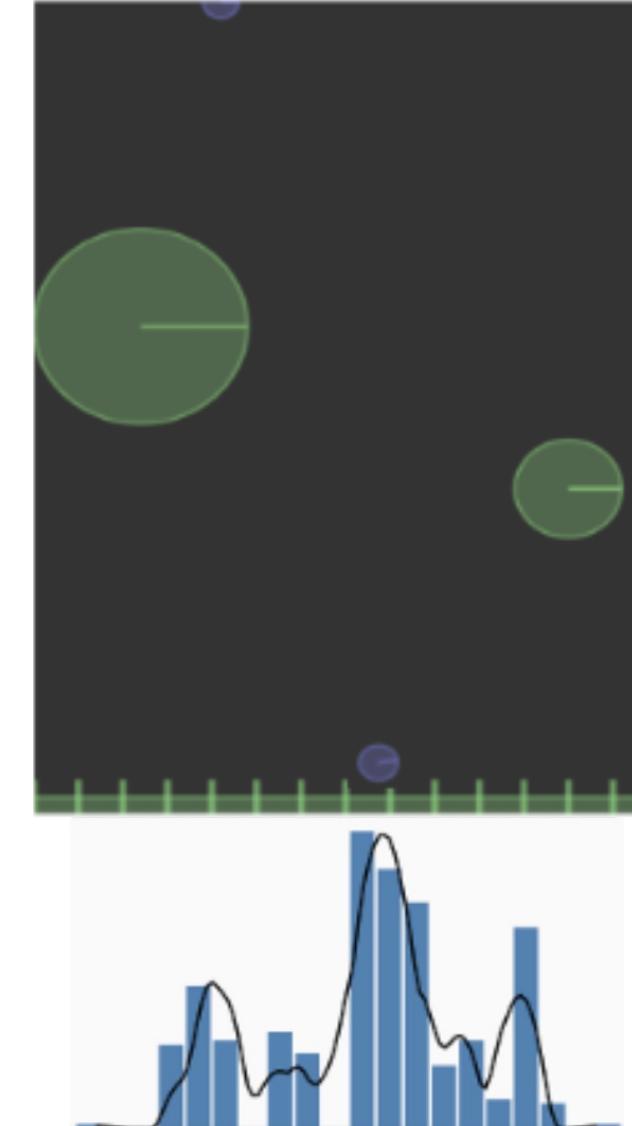
# Run Forward

## Generative model



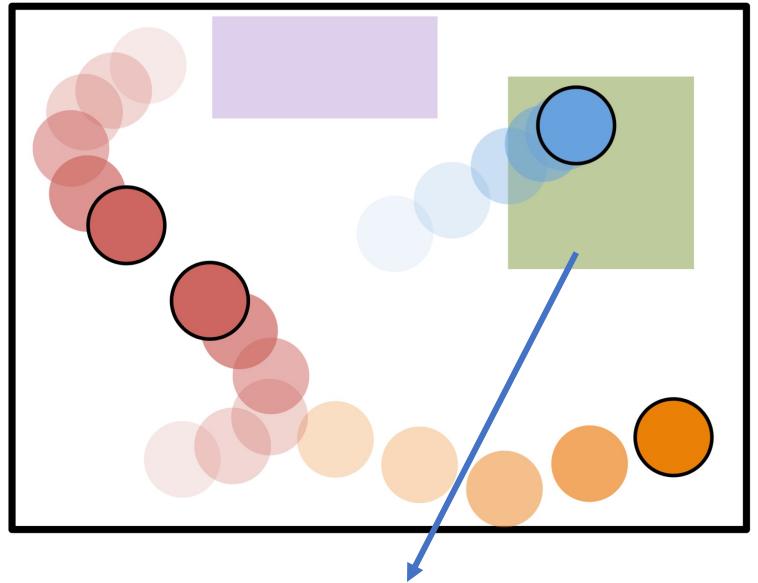
# Run Backward

## Inference algorithm



# WebPPL in Cognitive Science

	(i)	(ii)	(iii)
<b>Level N</b>	Innate concepts		
	<i>Entity</i>	<pre>(define (make-entity property1 property2 ... )          (list property1 property2 ... ))</pre>	
	<i>Newtonian Dynamics</i>	<pre>(define (run-dynamics entities forces                          init-cond steps dt)     (if (= steps 0) '()         (let* ((m (get-mass entities))                (F (apply-forces forces entities))                (a (/ F m)))           (new-cond (integrate init-cond                                a dt noise)))         (pair new-cond (run-dynamics entities  forces new-cond (- 1 step) dt)))))</pre>	
<b>Level 2</b>			
Entity types	Puck: ○	<pre>(define puck (make-entity                   pos shape mass vel ... ))</pre>	
	Surface: □	<pre>(define surface (make-entity                   pos shape friction ... ))</pre>	
Properties	Mass	<pre>(define (mass)          (pair "mass" (uniform '(1 3 9))))</pre>	
	Friction	<pre>(define (friction)          (pair "friction" '(uniform '(0 5 20))))</pre>	
Force classes	Pairwise: ① Global: ○→	<pre>(define (pairwise-force c1 c2)         (let* ((a (uniform-draw '(-1 0 1))))           (lambda (o1 o2)             (let ((r (euc-dist o1 o2)))               (/ (* a del(o1,col(o1)) del(o2,col(o2)))                   (power r 2)))))  (define (global-force)   (let* ((d (uniform-draw compass-dir)))     (lambda (o) (* k d))))</pre>	
<b>Level 1</b>			
Property values	● : large mass ○ : medium mass ■ : small mass ■ : high friction ■ : no friction	<pre>(define world-entities   (map sample-values entity-list))</pre>	
Force parameters	Force b/w reds: attract	<pre>(define world-forces   (map sample-parameters force-list))</pre>	
<b>Level 0 (data)</b>	Initial conditions	<pre>(define scenario   (let*     ((init-cond (sample-init world-entities))      (run-dynamics world-entities                   world-forces init-cond steps dt)))</pre>	



Friction?  
Magnetic field?  
Const. force (e.g., wind)?

Ullman, Stuhlmüller, Goodman, & Tenenbaum (2018)  
Learning physical parameters from dynamic scenes.  
Cognitive Psychology

## Bayesian Inference of Temporal Task Specifications from Demonstrations

---

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NeurIPS 2018

# WebPPL in AI



## 3.2 Specification Learning as Bayesian Inference

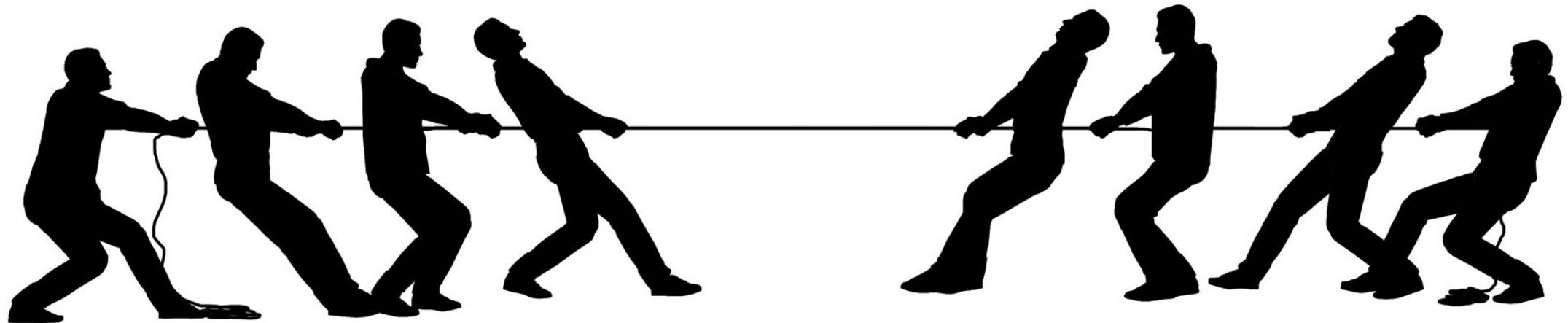
The Bayes theorem is fundamental to the problem of inference, and is stated as follows:

$$P(h \mid \mathbf{D}) = \frac{P(h)P(\mathbf{D} \mid h)}{\sum_{h \in \mathbf{H}} P(h)P(\mathbf{D} \mid h)}$$

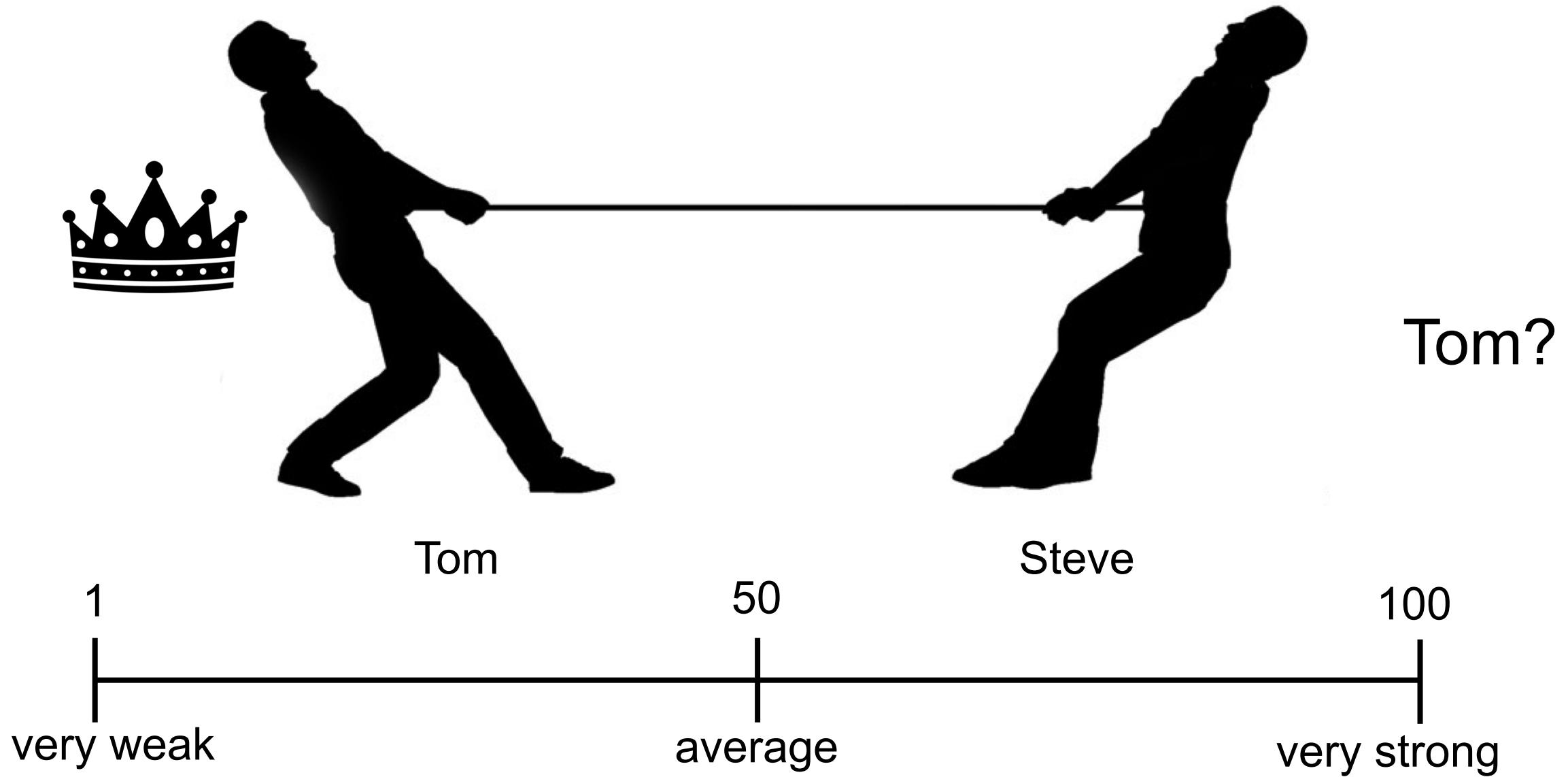
$P(h)$  is the prior distribution over the hypothesis space, and  $P(\mathbf{D} \mid h)$  is the likelihood of observing the data given a hypothesis. Our hypothesis space is defined by  $\mathbf{H} = \varphi$ , where  $\varphi$  is the set of all formulas that can be generated by the production rule defined by the template in Equation 2. The observed data comprises the set of demonstrations provided to the system by expert demonstrators (note that we assume all these demonstrations are acceptable).  $\mathbf{D}$  represents a set of sequences of the propositions, defined by  $\mathbf{D} = \{[\alpha]\}$ .

Project idea:  
Concept learning in  
different domains  
(6) using PPLs (Gen)

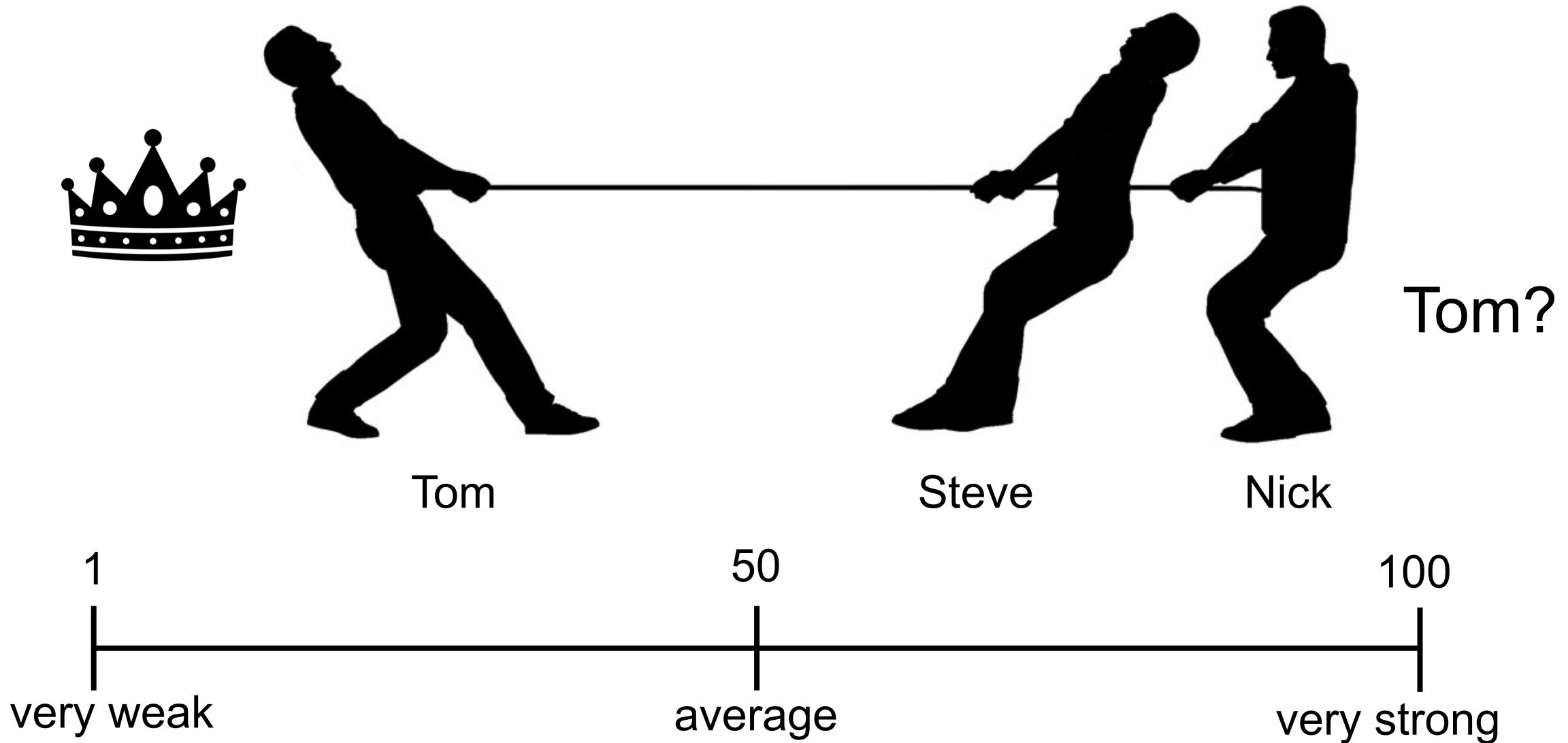
# Probabilistic Tug of War

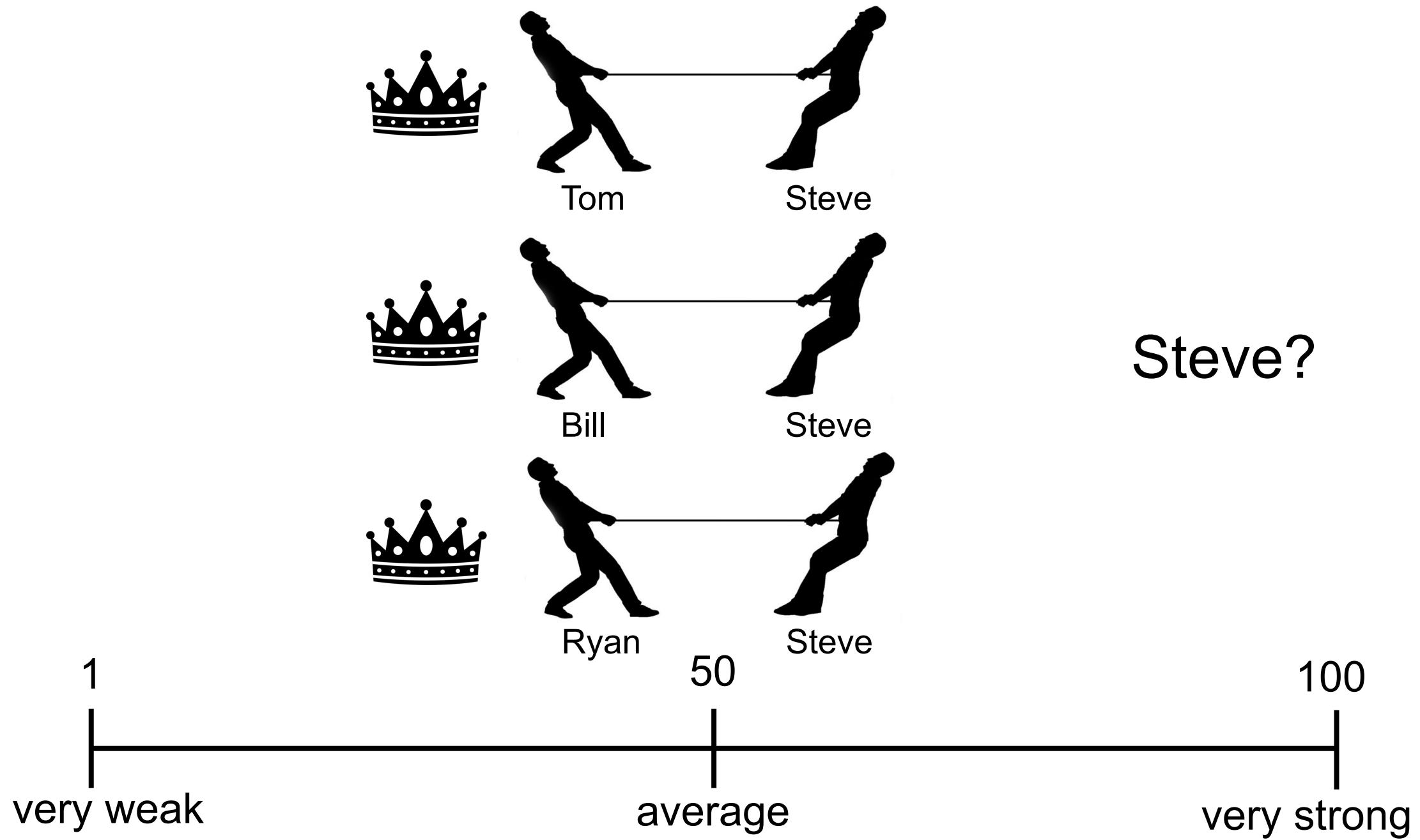


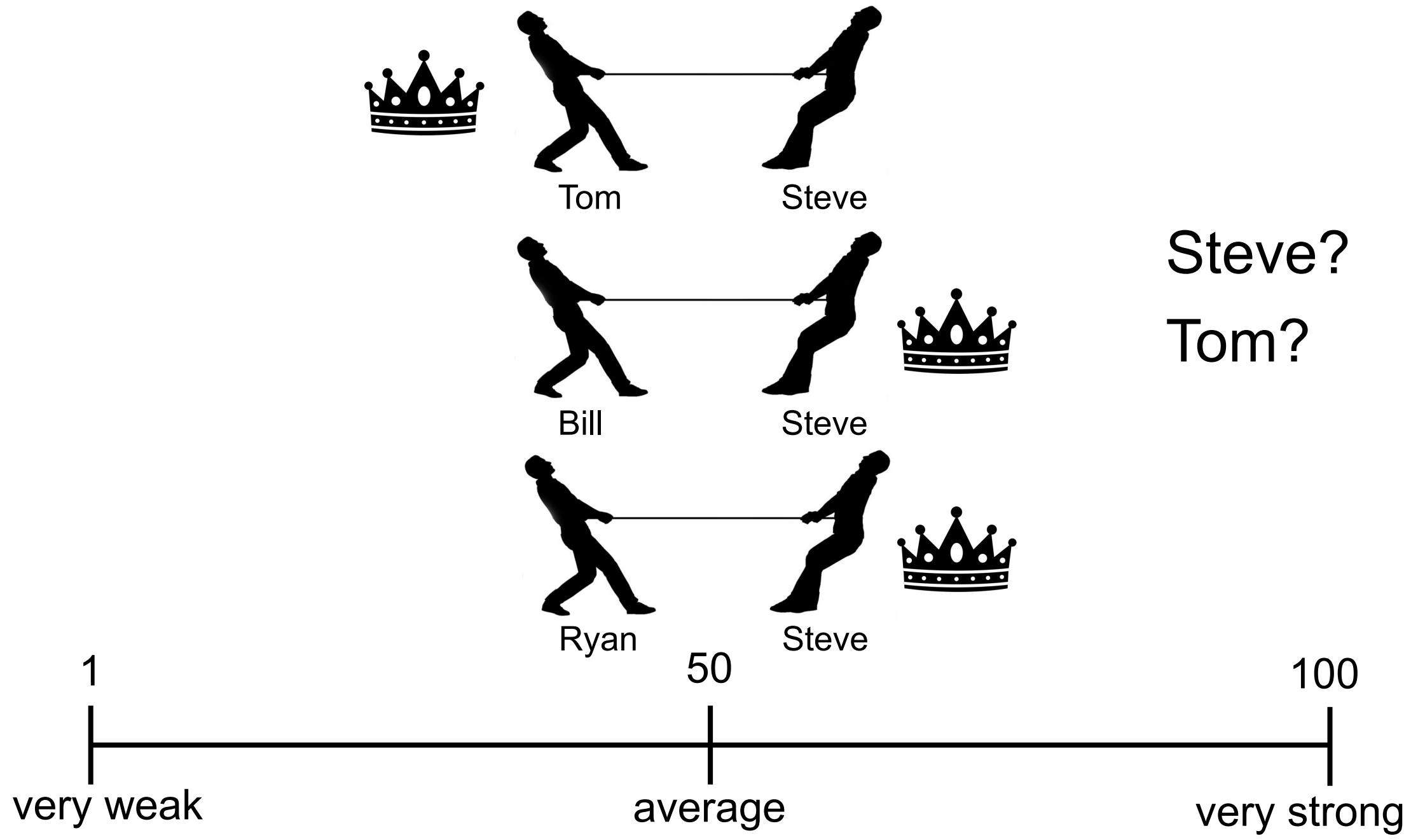
# Inferring strengths based on the outcome

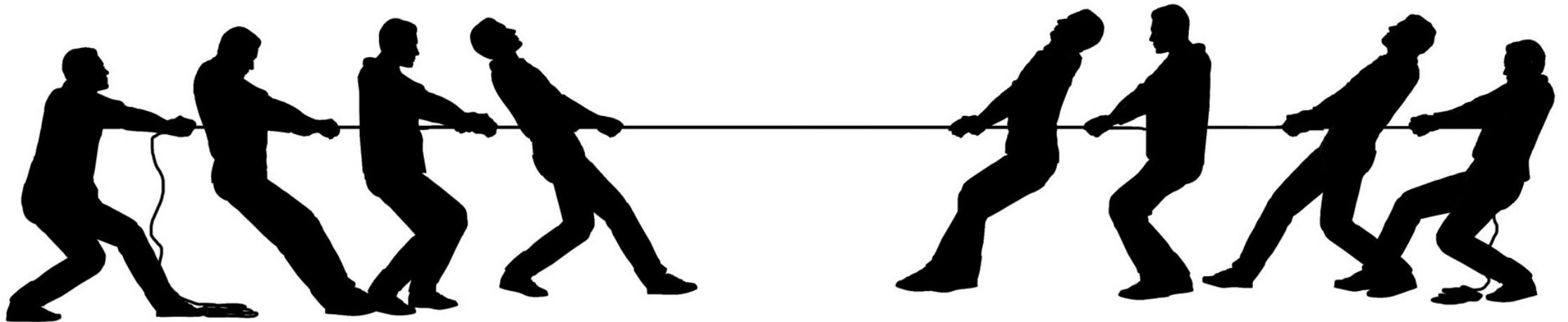


# Inferring strengths based on the outcome









**Concepts:**

A Bayesian network?

teams

person

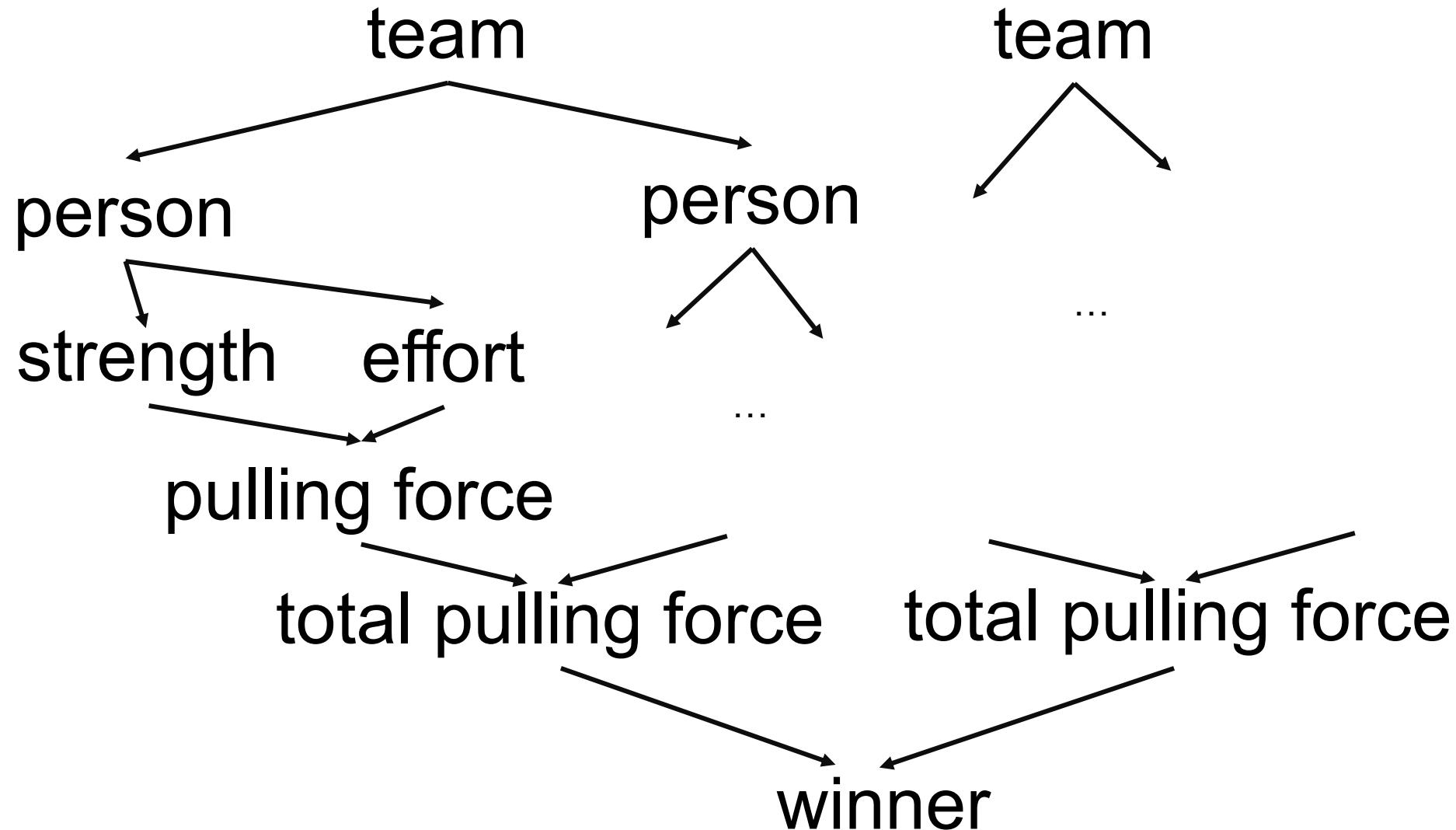
winner

strength

pulling force

effort

## A Bayesian network?



# A probabilistic program of tug of war

```
var towModel = function() {
    var strength = mem(function (person) {return gaussian(50, 10)})  
  

    var lazy = function(person) {return flip(0.1) }  
  

    var pulling = function(person) {
        return lazy(person) ? strength(person) / 2 : strength(person) }  
  

    var totalPulling = function (team) {return sum(map(pulling, team))}  
  

    var winner = function (team1, team2) {
        totalPulling(team1) > totalPulling(team2) ? team1 : team2 }  
  

    var beat = function(team1,team2){winner(team1,team2) == team1}  
  

condition(beat(['bob'], ['tom']))  
  

    return strength('bob')
}
```

See WebPPL demo

# Probabilistic language of thought hypothesis

- *The language of thought hypothesis* (LOTH) proposes that thinking occurs in a mental language.
- Probabilistic language of thought hypothesis:
- “Concepts have a language-like compositionality and encode probabilistic knowledge. These features allow them to be extended productively to new situations and support flexible reasoning and learning by probabilistic inference.”

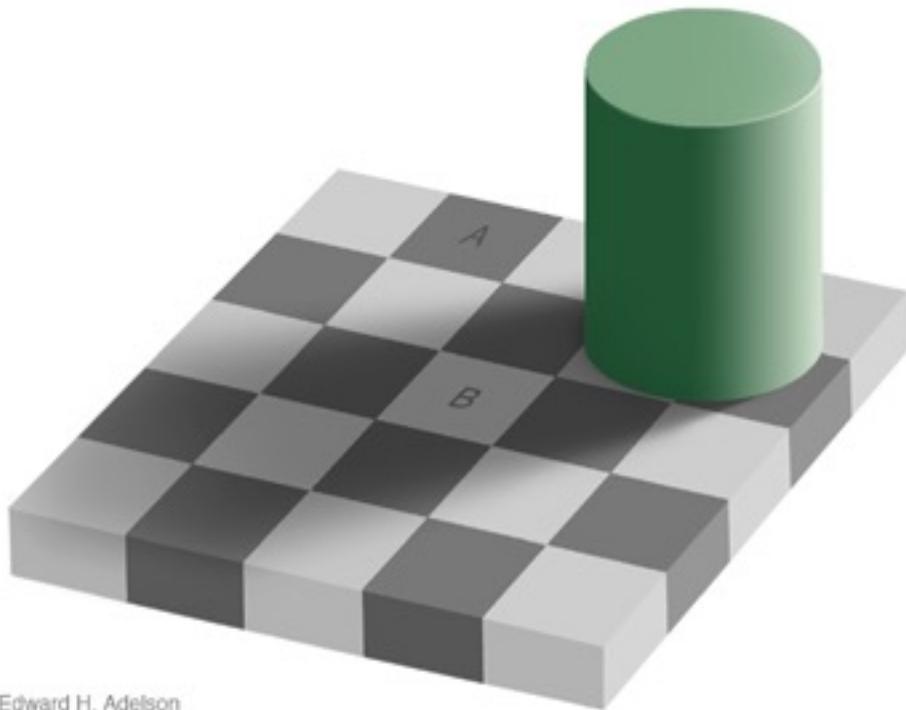
Fodor (1975). *The language of thought*

Goodman, Tenenbaum, & Gerstenberg (2015) Concepts in a probabilistic language of thought. *The Conceptual Mind: New Directions in the Study of Concepts*

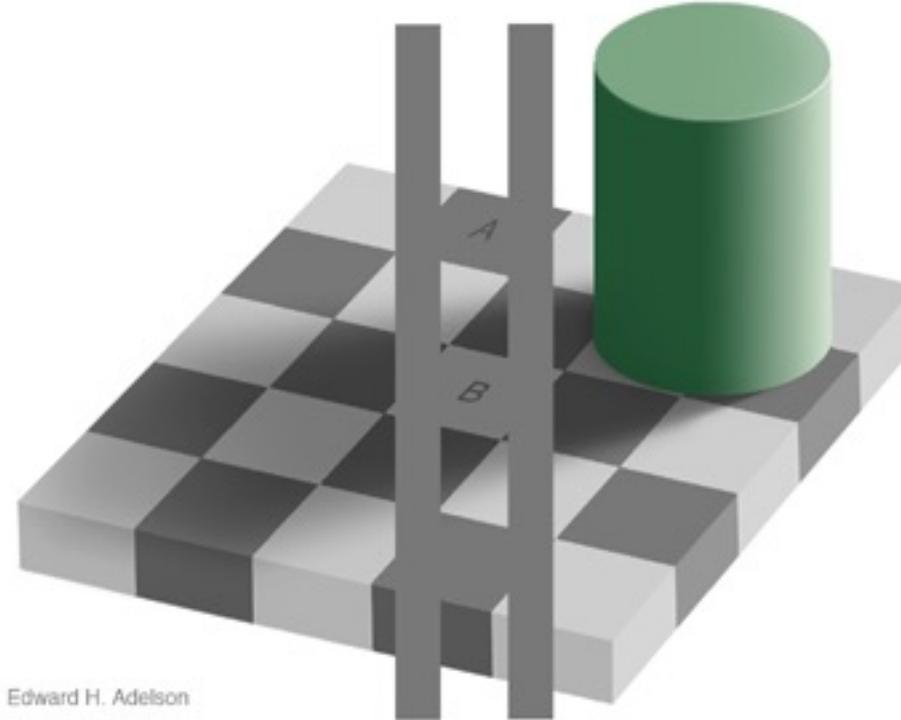
“Concepts have a language-like **compositionality** and encode probabilistic knowledge. These features allow them to be extended **productively** to new situations and support flexible reasoning and learning by probabilistic inference.“

```
var towModel = function() {  
    var strength = mem(function (person) {return gaussian(50, 10)})  
  
    var lazy = function(person) {return flip(0.1)} compositionality  
  
    var pulling = function(person) {  
        return lazy(person) ? strength(person) / 2 : strength(person)  
    }  
  
    var totalPulling = function (team) {return sum(map(pulling, team))}  
  
    var winner = function (team1, team2) {  
        totalPulling(team1) > totalPulling(team2) ? team1 : team2  
    }  
  
    var beat = function(team1, team2){winner(team1, team2) == team1}  
  
    condition(beat(['bob'], ['tom'])) • • •   
    return strength('bob') • • • productivity  
}
```

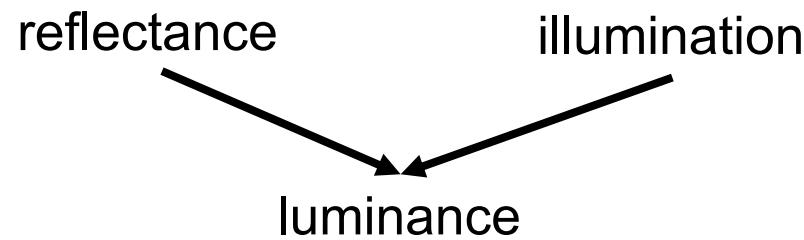
# Explaining away using WebPPL



Edward H. Adelson



Edward H. Adelson



See WebPPL demo  
<https://probmods.org/chapters/condition-al-dependence.html>

# More examples on probmods.org

The screenshot shows a green header bar with the title "Probabilistic Models of Cognition" and the subtitle "by Noah D. Goodman, Joshua B. Tenenbaum & The ProbMods Contributors". Below the header is a white content area containing the following information:

This book explores the probabilistic approach to cognitive science, which models learning and reasoning as inference in complex probabilistic models. We examine how a broad range of empirical phenomena, including intuitive physics, concept learning, causal reasoning, social cognition, and language understanding, can be modeled using probabilistic programs (using the [WebPPL](#) language).

**Contributors**  
This book is an open source project. We welcome content contributions ([via GitHub](#))!

The ProbMods Contributors are:  
Noah D. Goodman (editor)  
Joshua B. Tenenbaum  
Daphna Buchsbaum  
Joshua Hartshorne  
Robert Hawkins  
Timothy J. O'Donnell  
Michael Henry Tessler

**Citation**  
N. D. Goodman, J. B. Tenenbaum, and The ProbMods Contributors (2016). *Probabilistic Models of Cognition* (2nd ed.). Retrieved 2024-2-8 from <https://probmods.org/> [bibtex]

**Acknowledgments**  
We are grateful for crucial technical assistance from: Andreas Stuhlmüller, Tomer Ullman, John McCoy, Long Ouyang, Julius Cheng.

The construction and ongoing support of this tutorial are made possible by grants from the Office of Naval Research, the James S. McDonnell Foundation, the Stanford VPOL, and the Center for Brains, Minds, and Machines (funded by NSF STC award CCF-1231216).

**Previous edition**  
The first edition of this book used the probabilistic programming language Church and can be found [here](#).

**Chapters**

1. [Introduction](#)  
*A brief introduction to the philosophy.*
2. [Generative models](#)  
*Representing working models with probabilistic programs.*
3. [Conditioning](#)  
*Asking questions of models by conditional inference.*
4. [Causal and statistical dependence](#)  
*Causal and statistical dependence.*
5. [Conditional dependence](#)  
*Patterns of inference as evidence changes.*
6. [Social cognition](#)  
*Inference about inference*
7. [Interlude - Bayesian data analysis](#)  
*Making scientific inferences from data.*
8. [Interlude - Algorithms for inference](#)  
*Approximate inference. Efficiency tradeoffs of different algorithms.*
9. [Rational process models](#)  
*The psychological reality of inference algorithms.*
10. [Learning as conditional inference](#)  
*How inferences change as data accumulate.*
11. [Learning with a language of thought](#)  
*Compositional hypothesis spaces.*
12. [Hierarchical models](#)  
*The power of statistical abstraction.*
13. [Occam's Razor](#)  
*How inference penalizes extra model flexibility.*
14. [Mixture models](#)  
*Models for inferring the kinds of things.*
15. [Learning \(deep\) continuous functions](#)  
*Functional hypothesis spaces and deep*

# Reasoning with language

## From Word Models to World Models: Translating from Natural Language to the Probabilistic Language of Thought

Lionel Wong<sup>1\*</sup>, Gabriel Grand<sup>1\*</sup>, Alexander K. Lew<sup>1</sup>, Noah D. Goodman<sup>2</sup>, Vikash K. Mansinghka<sup>1</sup>, Jacob Andreas<sup>1</sup>, Joshua B. Tenenbaum<sup>1</sup>

*\*Equal contribution.*

<sup>1</sup>MIT, <sup>2</sup>Stanford

# Reasoning via large language models

**The “LLM scaling” hypothesis:** invert the entire generative process to learn *thought* from the distribution of language

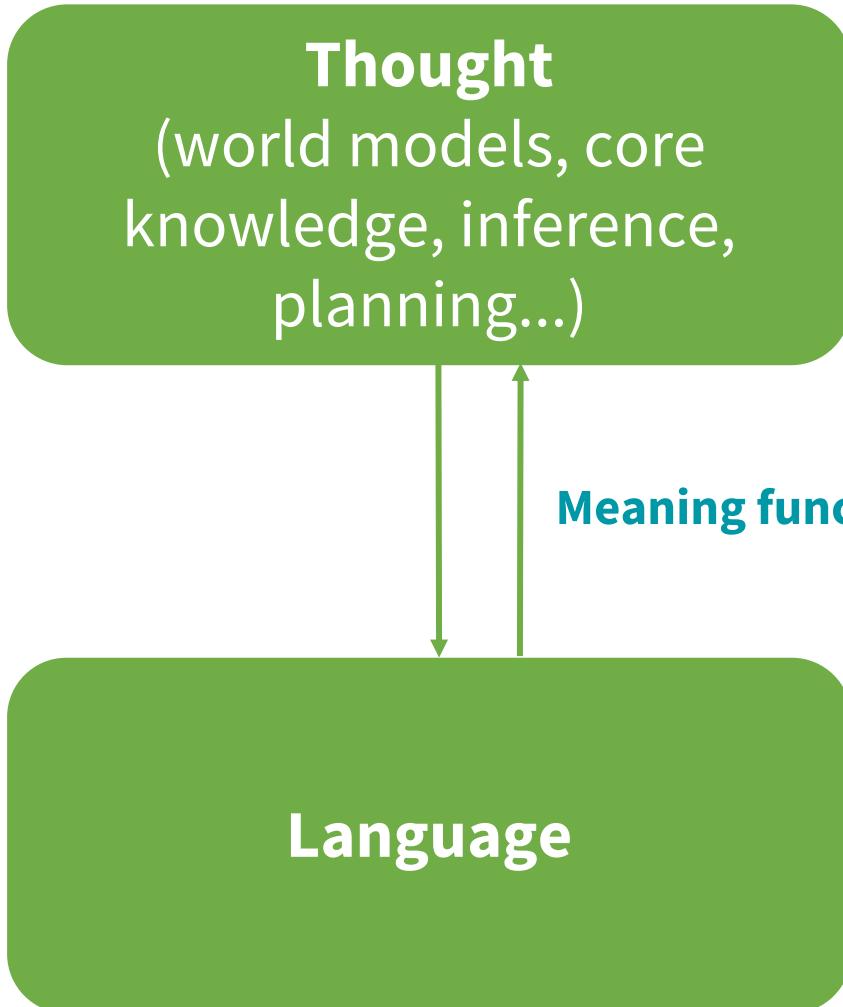
**Thought**

(world models, core knowledge, inference, planning...)

**Distributional language modeling:** learn linguistic structure from the statistical distribution of language  
(recurrent neural networks, sequence modeling, latent semantic analysis, distributional clustering, topic models word2vec, glove, LSTMs, ...)

**Language**

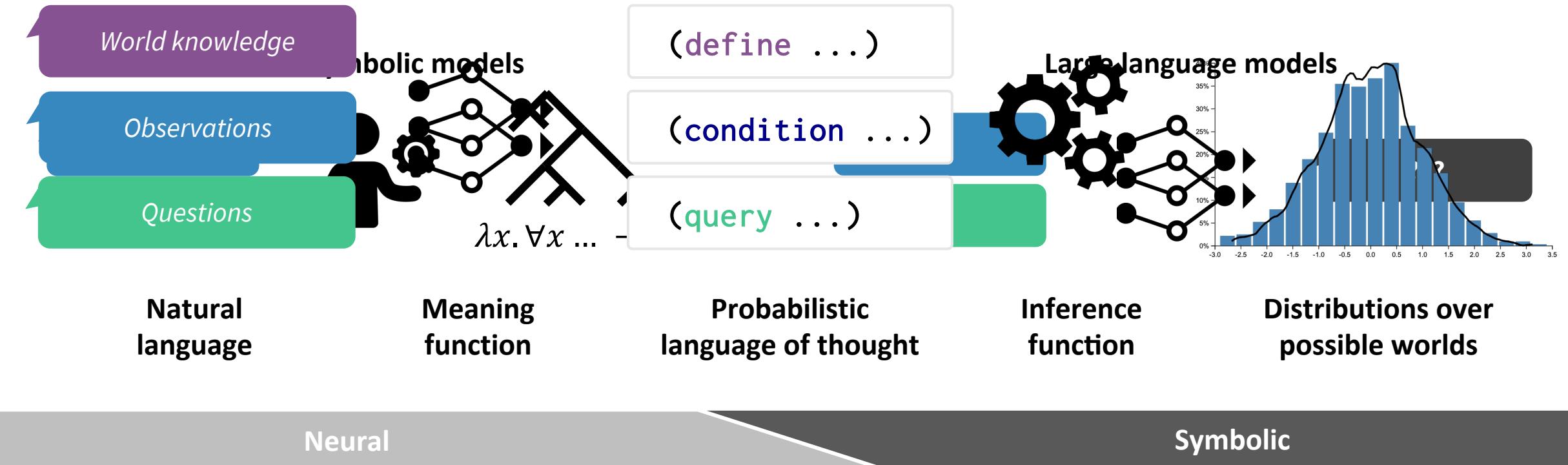
# Our proposal: translating from language into thought



**Thought** requires systems for **goal-directed world modeling, rational inference, and decision making.**  
(eg. Anderson, Miller & Johnson-Laird, Gentner, many others)

**Language** involves **meaning functions that map from external systems of signs into structured internal representations.**  
(eg. Frege, 1893; Heim and Kratzer, 1998; Pietrovski, 2005)

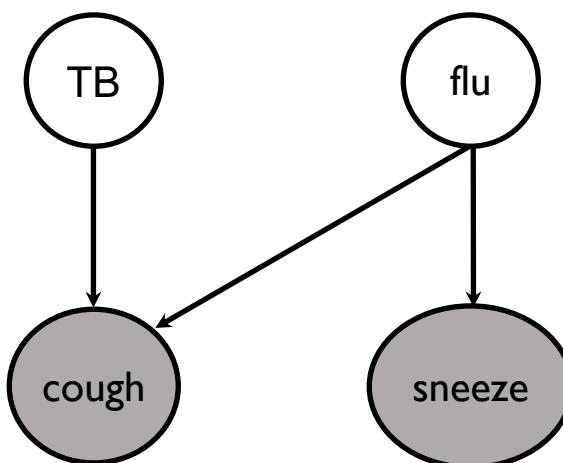
# Approaches to language-informed thinking



[Slides credits: Gabe Grand & Lio Wong]

# Probabilistic inference with Bayesian networks

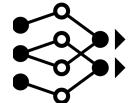
- Given:
  - Bayesian network that defines a joint distribution
$$P(x_1, x_2, \dots, x_n)$$
  - Condition / evidence / observation
$$O = o, O \subseteq X$$
 is a subset of (observed) variables
  - Query:
$$Q \subseteq X$$
 is a subset of (latent) variables
- Compute:



$P(Q = q | O = o)$  for all values  $q$

# Implementation

We created a minimal implementation of our framework using off-the-shelf tools.



**Meaning function:** OpenAI's **Codex** model, a large statistical language model trained jointly on language and code. Codex is *smaller* than GPT-4. We expect a range of code-trained LLMs to perform comparably in this role.



**Inference function:** We use **Church**, a probabilistic programming language that implements *simple*, universal sampling-based inference methods to perform inference across our models. Church has a minimalist lambda calculus syntax that is evocative of formal notations from linguistics.

Our goal is to *demonstrate* how this framework might broadly interface between language and a range of core cognitive domains.

## (A) Generative world model

```
(define strength (mem (lambda (player)
  (gaussian 50 20))))
```

\_\_\_\_\_



58.07



```
(define laziness (mem (lambda (player)
  (uniform 0 1))))
```

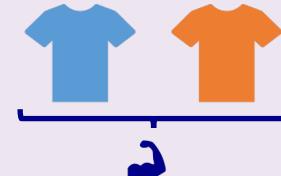
\_\_\_\_\_



0.27

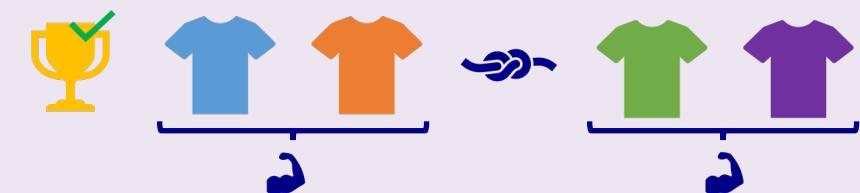
```
(define (team-strength team)
  (sum (map (lambda (player)
    (if (flip (laziness player))
        (/ (strength player) 2)
        (strength player)))
  team)))
```

\_\_\_\_\_



```
(define (won-against team-1 team-2)
  (> (team-strength team-1) (team-strength team-2)))
```

\_\_\_\_\_



## (A) Generative world model

```
(define strength (mem (lambda (player)  
  (gaussian 50 20))))
```

\_\_\_\_\_



58.07



```
(define laziness (mem (lambda (player)  
  (uniform 0 1))))
```

\_\_\_\_\_



0.27

• • •

## (B) Translation examples for LLM prompting

John and Mary won against Tom and Sue.

```
(condition (won-against '(john mary) '(tom sue)))
```

Sue is very strong!

```
(condition (> (strength 'sue) 75))
```

If Sue played against Tom, who would win?

```
(query (won-against '(sue) '(tom)))
```

[a new cond. statement / query]



• • •



[Slides credits: Gabe Grand & Lio Wong]

## (C) Natural language

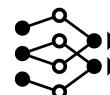
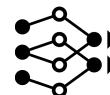
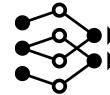
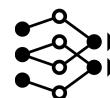
Josh won against Lio.

Josh proceeded to claim victory against Alex.

Even working as a team, Lio and Alex still could not beat Josh.

How strong is Josh?

What are the odds of Gabe beating Josh?



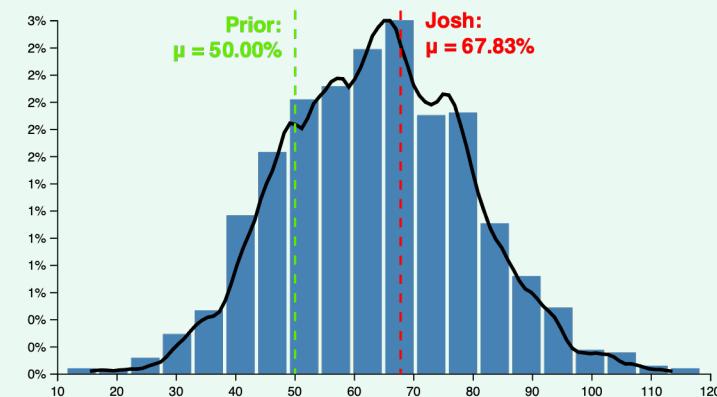
## (D) Language of thought

(condition (won-against '(josh) '(lio)))

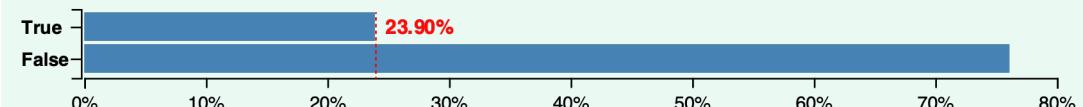
(condition (won-against '(josh) '(alex)))

(condition (not (won-against '(lio alex) '(josh)))

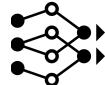
(query (strength 'josh))



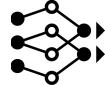
(query (won-against '(gabe) '(josh)))



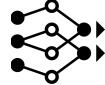
The faculty team is made up of four players: Jacob, Josh, Noah, and Vikash.



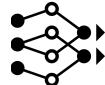
The student team consists of Alex, Gabe, and Lio, plus their labmates, Ben and Ced.



Is Gabe stronger than the weakest player on the faculty team?



All of the faculty are pretty strong.



Is Gabe stronger than the weakest player on the faculty team?

```
(define faculty-team '(jacob josh noah vikash))
```

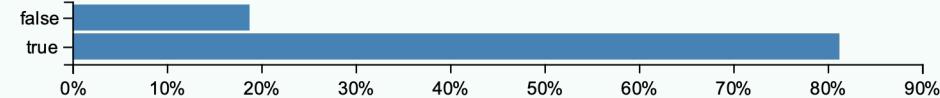


```
(define student-team '(alex gabe lio ben ced))
```

(query

(stronger-than?

'gabe (argmin strength faculty-team))



(condition

(all

(map

(lambda (player)

(> (strength player) 60))

faculty-team)))



# Constructing a new world model

## A. Prompt, containing unrelated example world model

```
;; We define a probabilistic model in Church of the following scenario.  
;; At any given time, about 1% of the population has lung cancer,  
;; 20% have a cold, 10% have a stomach flu, and 0.5% have TB.  
(define lung-cancer (mem (lambda (person) (flip 0.01))))  
(define cold (mem (lambda (person) (flip 0.2))))  
(define stomach-flu (mem (lambda (person) (flip 0.1))))  
(define TB (mem (lambda (person) (flip 0.005))))  
  
;; If you have a cold, there's a 50% chance you have a cough.  
;; 30% of people with lung cancer have a cough, and 70% with TB.  
;; There's also a small chance you have a cough even if you're otherwise ;; healthy.  
(define cough (mem (lambda (person)  
  (or (and (cold person) (flip 0.5))  
       (and (lung-cancer person) (flip 0.3))  
       (and (TB person) (flip 0.7))  
       (flip 0.01)))))  
  
;; Whether a person coughs during a particular visit to the doctor's  
;; office depends on whether they have a cough, and a bit of random  
;; chance. Note that this will differ each time they go to the doctor's  
;; office, so we do not use `mem` (which memoizes the result).  
(define coughs-on-particular-visit  
  (lambda (person) (and (cough person) (flip 0.7))))
```

## B. Defining a new world model from scratch

;; Now, let's define a different probabilistic model of the following scenario.

;; It is totally unrelated to the previous model and does not reference the functions above.

First, strength levels vary widely from person to person.

 (define strength (mem (lambda (person) (normal 100 20))))

Furthermore, each person has a percentage of the time that they are lazy.

 (define laziness (mem (lambda (person) (uniform 0 1))))

The strength of a team is the combined strength of its members, except that in any given match, each player may decide to be lazy, and thus contribute only half of their strength.

 (define team-strength  
 (lambda (members)  
 (apply + (map (lambda (member)  
 (if (flip (laziness member))  
 (/ (strength member) 2)  
 (strength member))))  
 members)))

Whether one team beats another just depends on which team pulls stronger that match.

 (define team-beats-team  
 (lambda (team1 team2)  
 (> (team-strength team1) (team-strength team2))))

## Perceptual reasoning



Generative model over static scenes

```
(define generate-object
  (mem (lambda (obj-id) (list
    (pair 'object-id obj-id)
    (choose-shape obj-id)
    (choose-color obj-id)))))

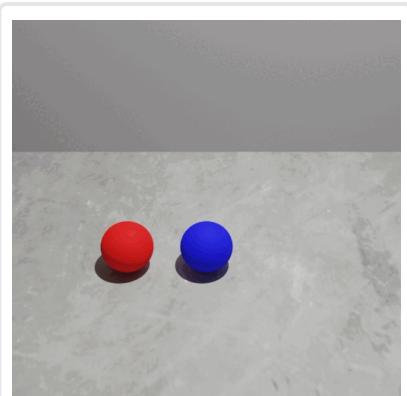
(define choose-num-objects ...) (define
  generate-objects-in-scene ...)
```

Graphics rendering engine



**Vision as inverse graphics**  
(e.g., Kersten & Yuille, 1996;  
Mansinghka et. al, 2013)

## Physical reasoning

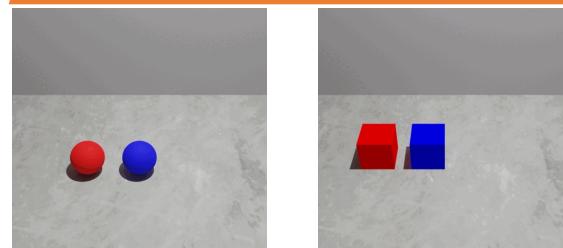


Generative model over dynamic scenes

```
.(define generate-object
  (mem (lambda (obj-id)
  (list (pair 'object-id obj-id)
    (choose_shape obj-id)
    (choose_color obj-id)
    (choose_mass obj-id)...)))))

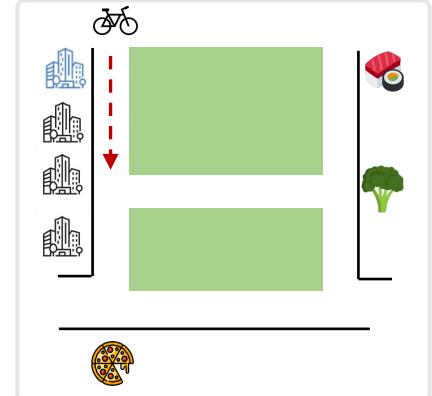
(define generate-initial-scene-state...)
....
```

Physics engine



**Intuitive physics as a mental physics engine**  
(e.g., Battaglia et. al, 2013)

## Social reasoning

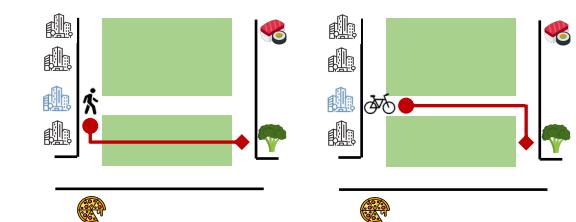


Generative model over agents

```
(define restaurants (list 'sushi 'pizza
  'vegetarian))

(define restaurant_utility (mem (lambda
  (agent-id restaurant_type)
  (uniform-draw (list (gaussian
    POSITIVE.Utility_MEAN Utility_VARIANCE)
    (gaussian NEGATIVE.Utility_MEAN
    Utility_VARIANCE))))))
```

Planning engine



**Intuitive social reasoning as inverse planning**  
(e.g., Baker, Saxe, and Tenenbaum, 2009)

## Perceptual reasoning



Observations  
about the  
world

Condition  
statements

There is at least one red mug in this scene.

```
(condition  
>= (length  
((filter-shape 'mug)  
((filter-color red)  
(objects-in-scene  
'this-scene)))) 1)
```

Questions  
about the  
world

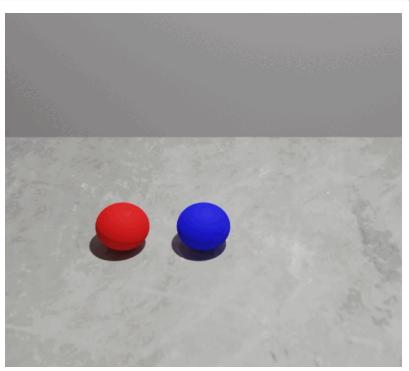
Query  
statements

How many mugs are there?

```
(query  
(length  
((filter-shape 'mug)  
(objects-in-scene  
'this-scene))))
```

Inference over scenes using inverse  
graphics

## Physical reasoning



Imagine that there is a red ball that is pretty heavy.

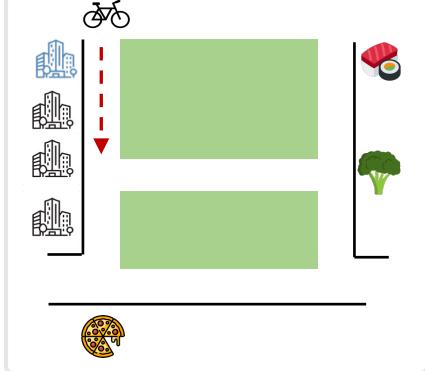
```
(condition ((get_singleton_object  
lambda (object) (and  
((is-color? red) object)  
(((is-shape? 'sphere) object)  
> (get-attribute object 'mass) 2.5))))
```

How fast will the blue ball move if it's  
bumped by the red one?

```
(query ...  
  (get_attribute  
  event 'subject_final_velocity))  
  (filter_events (lambda (e)  
  (and (is_event? 'collision  
  e...)))
```

Inference over physics using physics  
engine

## Social Reasoning



Alex loves sushi but hates pizza, and  
he brought his bike to work today.

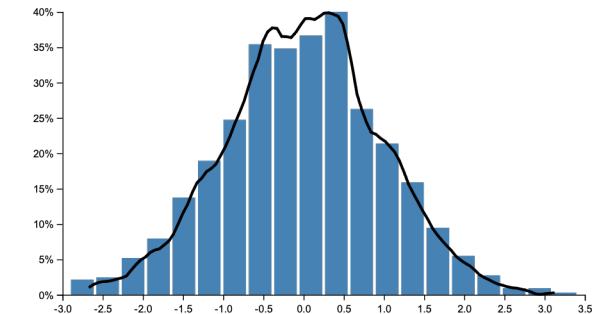
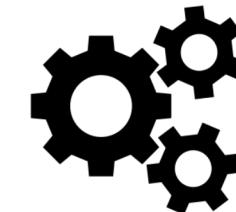
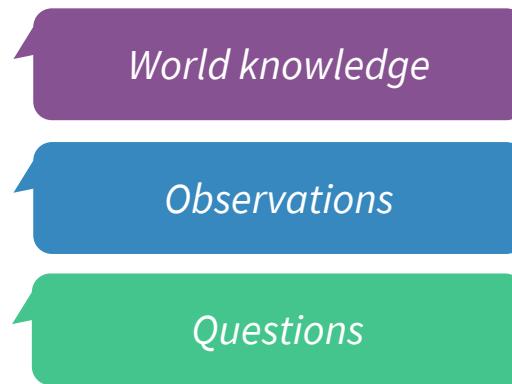
```
(condition  
  (and (loves? 'alex 'sushi)  
    (hates? 'alex 'pizza)  
    (has-bike? 'alex)))
```

What will Alex do?

```
(query (get_actions 'alex))
```

Inference over agents using planning  
engine

# Reasoning with language using PPLs + LLMs



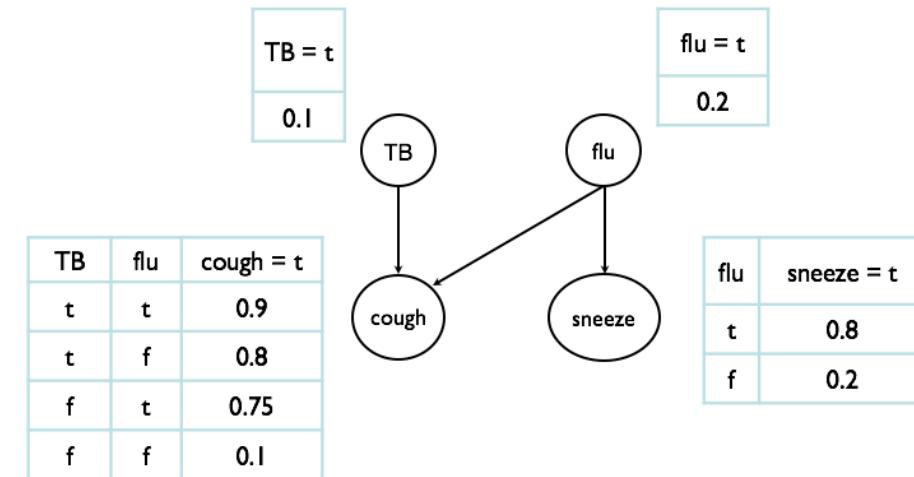
Natural language	Meaning function	Probabilistic language of thought	Inference function	Distributions over possible worlds

- A more flexible way to construct world models, conditions, and queries
- Beyond QAs (e.g., planning)
- Incorporate learning – e.g., learning new world models (and not using given world models)
- Automatic inference function selection / construction
- Connect to state-of-the-art PPLs, e.g., Gen
- ...

## Project ideas

# Summary: Towards a probabilistic language of thought

- Bayesian networks
  - Mathematically convenient
  - Causal models
  - Hard to write code for inference algorithms
- Probabilistic programs
  - Have rich compositionality
    - Recall: composing programs for priors for the number game
  - Provide a complete specification of the domain (nothing hidden behind arrows)
  - Probabilistic programming languages (PPLs) provide tools for easily and flexibly implement efficient inference algorithms
  - PPLs for Bayesian models, DL frameworks (e.g., pytorch) for neural networks
  - Connected to natural language via LMs



```
var towModel = function() {
  var strength = mem(function (person) {return gaussian(50, 10)})

  var lazy = function(person) {return flip(0.1) }

  var pulling = function(person) {
    return lazy(person) ? strength(person) / 2 : strength(person) }

  var totalPulling = function (team) {return sum(map(pulling, team))}

  var winner = function (team1, team2) {
    totalPulling(team1) > totalPulling(team2) ? team1 : team2 }

  var beat = function(team1,team2){winner(team1,team2) == team1}

  condition(beat(['bob'], ['tom']))

  return strength('bob')
}
```

# Why is posterior inference hard?

$$p(h|d) = \frac{p(d|h)p(h)}{Z}$$

$$Z = \int_h p(d|h)p(h)$$

Two challenges:

- Calculating Z requires integrating over all h
- Even if we had z, still hard to directly sample h w.r.t.  $p(h|d)$

# Sampling-based inference algorithms

- Monte Carlo methos:
- Rejection sampling
- Importance sampling
- Markov chain Monte Carlo (MCMC)
- Sequential Monte Carlo (SMC)

# What is Monte Carlo?

- Monte Carlo is a small hillside town in Monaco (near Italy) with casino since 1865 like Los Vegas in the US. It was picked by a physicist Fermi (Italian born American) who was among the first using the sampling techniques in his effort building the first manmade nuclear reactors in 1942.
- The casino business is, literally, driven by **tossing dice to simulate random events**. Monte Carlo computing is to simulate samples from arbitrary probabilities by a single random function `x=rand()` which returns a pseudo-random number in the interval [0,1].

# Sampling-based inference algorithms

- Monte Carlo methos:
- Rejection sampling
- Importance sampling
- Markov chain Monte Carlo (MCMC)
- Sequential Monte Carlo (SMC)

How to use Gen to implement sampling-based inference algorithms?