

Ballistic integration

$$s(t+1) = s(t) + dt \, v(t) + \frac{dt^2}{2} a(t) \quad (1)$$

$$v(t+1) = v(t) + dt \, a(t) \quad (2)$$

$$a(t) = \frac{2}{dt^2} \left( s(t+1) - s(t) - dt \, v(t) \right) \quad (3)$$

$$a(t) = \frac{1}{dt} \left( v(t+1) - v(t) \right) \quad (4)$$

Final Model

$$v(t+1) = v(t) + c_1 a(t) + c_2 a(t-1) \quad (5)$$

$$s(t+1) = s(t) + dt \, v(t) + c_3 a(t) + c_4 a(t-1) \quad (6)$$

$$a(k) = -\bar{c}_1 a(k-1) + \bar{c}_2 (v(k+1) - v(k)) \quad (7)$$

$$a(k) = -\bar{c}_3 a(k-1) + \bar{c}_4 (s(k+1) - s(k) - dt \, v(k)) \quad (8)$$

Final Model in matrix notation (For linear regression)

$$\begin{bmatrix} a(t) \\ a(t) \end{bmatrix} = \begin{bmatrix} -a(t-1) & v(t+1) - v(t) & 0 & 0 \\ 0 & 0 & -a(t-1) & s(t+1) - s(t) - dt \, v(t) \end{bmatrix} \begin{bmatrix} \bar{c}_1 \\ \bar{c}_2 \\ \bar{c}_3 \\ \bar{c}_4 \end{bmatrix} \quad (9)$$