Innovation, Trade, and Structural Change*

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Abstract

Traditional theories of structural transformation often overlook the disparities between

employment and value-added shares, presenting a key puzzle. This study introduces a

Schumpeterian framework that integrates technological innovation and trade at the sectoral

level to address this gap. In a closed economy, the model predicts an equilibrium where

value-added shares match employment shares. However, when a country opens to trade

and gains a monopoly through innovation in a specific sector, it achieves higher profits

and value-added shares relative to employment. This leads to faster growth in value-added

shares compared to labor shares in monopolistic sectors. Additionally, lower sectoral trade

costs, higher foreign sectoral prices, and larger sectoral presence in foreign markets en-

hance export demand, further boosting the value-added shares in those sectors.

KEYWORDS: Schumpeterian growth, Structural change, Innovation, Trade

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1 Introduction

A central concept in development economics is the notion of structural change, which is defined as the reallocation of economic resources across sectors with different productivity levels. Therefore, the three most common measures of economic structural change are sectoral employment shares, sectoral value added shares, and sectoral final consumption expenditure shares. While the literature often treats these measures as interchangeable, they are quantitatively distinct. Herrendorf et al. (2014) document such differences and Kuznets (1967) demonstrated that during the early stages of US development, the employment share of services increased significantly, while the value added share of services remained relatively constant. Furthermore, Buera & Kaboski (2009) consider this discrepancy to be a relevant puzzle for the theories of structural transformation for several countries.

This paper proposes a new theory whereby changes in innovations across different sectors over time account for the divergent paths in employment shares and value added shares. Indeed, Herrendorf et al. (2014) have pointed to international trade dynamics and variations in measurement methodologies as factors contributing to disparities between production and consumption measures¹ of economic structural transformation. Specifically, by taking into account international trade, where a portion of domestic consumption is sourced from abroad rather than domestically produced, differences between production and consumption measures of structural change can be elucidated.

Additionally, differences in these production and consumption measures may manifest through the divergence in perspectives and methodologies utilized in economic accounting to assess economic activity, particularly concerning final consumption expenditure and value added in production. However, traditional theories of structural transformation cannot explain the differences between employment and value added shares. A notable puzzle arises from the incongruity between sectoral employment shares and sectoral value added shares, both of which are production measures.

In this paper, I develop a Schumpeterian model of structural transformation where tech-

¹The employment shares and value added shares relate to production whereas final consumption expenditure shares relate to consumption.

nological innovation drives sectoral productivity growth. The economy consists of three final good sectors, agriculture, manufacturing, and services. Each sector produces a distinct final good by aggregating a continuum of differentiated intermediate goods, which are varieties specific to each sector. These intermediate varieties are produced under monopolistic competition and are the only tradable goods across countries. The model builds on Aghion & Howitt (2009) and is extended to a two-country framework ('home' and 'foreign'), emphasizing the role of trade in intermediate varieties in shaping cross-country sectoral dynamics.

The range of intermediate varieties in each country is identical, and all countries produce exactly the same final products: foods, manufacturing goods, and services. Within each intermediate sector the world market can then be monopolized by the producer with the lowest cost and holding a patent for the most recent version of the intermediate good. To incorporate the demand side of structural change, I adopt the approach proposed by Comin et al. (2021), wherein Constant Elasticity of Substitution (CES) nonhomothetic preferences for households are introduced. Indeed, CES nonhomothetic preferences possess favorable properties for examining long-run structural change as they differentiate the impact of income on the growth of luxury goods sectors.

The closed economic model predicts that the share of value-added equals the share of employment. This relationship is based on the direct correlation between profits generated within a sector and the level of employment in that sector. As employment increases within a sector, both output and demand for intermediate goods also increase, leading to higher profits for monopolist producers of intermediate goods. Consequently, the income of both workers and entrepreneurs follows a linear pattern determined by the wage rate and the level of employment within sectors utilizing intermediate goods.

However, once the country opens up to international trade, sectors in which the country becomes a global monopolist experience an increase in profit. This profit is now dependent on both domestic employment and employment from the rest of the world in the same sector. Thus, domestic monopolists benefit from higher profit due to the external demand for the latest versions of sectoral intermediate goods. Since a portion of the total profit is attributable to external demand, the share of value added in this sector is higher than that of employment.

Conversely, in sectors where the country is not the global monopolist and therefore imports some intermediate goods, profit is lower than in a closed economy, and the share of employment is higher than that of value added.

International trade in a competitive environment, that is, without monopolistic rights, can explain disparities between consumption and production expenditures (see Herrendorf et al. (2014) and Uy et al. (2013)) but not between value-added and employment shares. My paper contributes by incorporating the monopolistic structure induced by innovation, enabling it to reconcile the observed disparities between value-added and employment shares across sectors.

Related Literature. The literature on structural transformation in economics has witnessed significant evolution, with seminal contributions from Lewis (1954), Cheneryr (1960), Kuznets (1967), Baumol (1967), and Harris & Todaro (1970). These works collectively lay the groundwork for understanding the process of structural transformation, emphasizing key factors such as surplus labor, industrialization, sequential stages of growth, income inequality dynamics, the "cost disease" phenomenon, and rural-urban migration patterns. They have provided valuable insights into the drivers and consequences of structural change, guiding research and policy discussions on economic development and inequality mitigation. Building upon these foundational works, Ngai & Pissarides (2007) formalized Baumol's price effect by showing that different sectoral productivity growth rates account for shifts in sector final goods prices and demands for different goods.

Furthermore, the role of international trade in influencing structural transformation has received considerable attention, with studies by Matsuyama (2009) and Uy et al. (2013) exploring the connections between trade openness, sectoral specialization, and employment patterns². Despite the progress made, challenges remain in reconciling disparities between employment and value-added shares across sectors, as highlighted by Herrendorf et al. (2014), while Buera & Kaboski (2009) identified that the behavior of consumption and output shares differs significantly from that of employment shares. They argued that models incorporating home pro-

²The works of Duarte & Restuccia (2020), Rodrik (2016), Sposi (2019), Swiecki (2017), and Matsuyama (2019) have shed considerable light on the factors influencing structural change as well as the differences between developing and developed countries in the trajectories of structural change in their economies.

duction, sector-specific factor distortions, and differences across sectors in the accumulation of human capital are promising avenues to amend standard models.

This paper contributes to the literature by proposing a new theoretical framework that integrates technological innovation and international trade dynamics to explain divergent paths in employment and value-added shares across sectors. It shows that any additional profit obtained by domestic monopolistic entrepreneurs due to foreign demand in a specific sector, rather than domestic demand, will widen the disparity between value-added and employment shares. The model illustrates how innovation, through monopoly rights alongside international trade, serves as an extra factor explaining differences between measures of structural change. By addressing gaps in traditional theories, this framework offers a comprehensive understanding of the drivers of structural transformation and provides insights into the dynamics of economic evolution.

The remainder of this paper is structured as follows: Section 2 introduces the closed economic model which captures the supply-side and demand-side forces driving structural transformation and derives the relationships between different measures of structural change. Section 3 extends the model to incorporate international trade and demonstrates how these relationships are modified by international trade in monopolistic goods. The paper concludes with Section 4, summarizing key insights including some possible directions for future research.

2 The Closed Economy Model

The theoretical foundation of the trade model is provided by the Schumpeterian framework developed by Aghion & Howitt (2009). Additionally, the setup draws upon the work of Comin et al. (2021), who introduced long-run Engel curves to explain the demand-side aspect of structural change. The model incorporates heterogeneous technological innovation to capture the supply-side dynamics of structural change. There are three final sectors - agriculture, manufacturing, and services - indexed by k = a, m, s. Each final sector competitively produces a single consumption good, also indexed by k = a, m, s, utilizing labor and a continuum of specific intermediate inputs. Time is discrete, indexed by t = 1, 2, ..., and at each time period, there is a mass L_{jt} of individuals in country j. Each household is endowed with labor units that are

supplied inelastically. Sectoral productivity growth arises from innovation within each country.

2.1 Goods production sectors

Final goods production: Each final good k, which is consumed by households, is produced competitively using labor and a unit interval of specific intermediate varieties v as inputs, according to the Cobb-Douglas production function:

$$Y_{jkt} = L_{jkt}^{1-\alpha} \int_0^1 A_{jkt}(v)^{1-\alpha} x_{jkt}(v)^{\alpha} dv \quad k = a, m, s$$
 (2.1)

where $0 < \alpha < 1$ and Y_{jkt} is the output of sector k in country j. $A_{jkt}(v)$ represents the productivity of the variety v used in sector k and $x_{jkt}(v)$ denotes the quantity of input of the latest version of the variety v used in the production of final good k at time t in country j. L_{jkt} represents the number of workers in country j employed in the production of final good k at time t such that:

$$\sum_{k=a,m,s} L_{jkt} = L_{jt} \quad \forall j \in J$$
 (2.2)

Since the final sector k operates competitively, the representative firm takes the prices of its output P_{jkt} and inputs $p_{jkt}(v)$ as given. It then chooses the quantity of labor L_{jkt} and the quantity $x_{jk}(v)$ of each intermediate good v to use in order to maximize its profit, as follows:

$$\max_{\left\{L_{jkt},\left[x_{jkt}(v)\right]_{v\in[0,1]}\right\}} P_{jkt} L_{jkt}^{1-\alpha} \int_{0}^{1} A_{jkt}(v)^{1-\alpha} x_{jkt}(v)^{\alpha} dv - \int_{0}^{1} p_{jkt}(v) x_{jkt}(v) dv - w_{jt} L_{jkt}$$
(2.3)

where w_{jt} is the wage rate in the country j at period t.

Intermediate goods production. Each variety v of the sector k is produced by a patent monopoly obtained through an innovation. The lifetime of the patent lasts for a one period. The production technology of intermediate varieties involves using one unit of the final good k to produce a unit of an intermediate variety v for the sector k. In each period, one entrepreneur succeeds in innovation in a sector and is granted the patent right. Innovations are assumed to be drastic; that the intermediate monopolist is unconstrained by potential competition from the

previous patent. Then the producer of the variety v for the sector k in the country j maximizes its profit as follows:

$$\max_{\left\{\mathbf{x}_{jkt}(\mathbf{v})\right\}} \pi_{jkt}(\mathbf{v}) = p_{jkt}(\mathbf{v})\mathbf{x}_{jkt}(\mathbf{v}) - P_{jkt}\mathbf{x}_{jkt}(\mathbf{v})$$
(2.4)

s.t.
$$p_{jkt}(\mathbf{v}) = f^{-1} \left[\mathbf{x}_{jkt}(\mathbf{v}) \right]$$

where f is the demand function of the final good's producer for the intermediate good v.

2.2 Innovation and productivity growth

Productivity growth arises from innovations. In each intermediate variety v of each sector k, in each period, there exists a unique entrepreneur in country j with the potential to innovate in that variety. This entrepreneur acts as the incumbent monopolist, and an innovation would enable them to produce with a productivity or quality parameter $A_{jkt}(v) = \gamma_{jk}A_{jkt-1}(v)$, where $\gamma_{jk} > 1$. Otherwise, their productivity parameter remains unchanged $A_{jkt}(v) = A_{jkt-1}(v)$. Let $\mu_{jkt}(v)$ denote the probability that innovation occurs in the intermediate sector v, then

$$A_{jkt+1}(v) = \begin{cases} \gamma_{jk} A_{jkt}(v) & \text{with probability } \mu_{jk}(v) \\ A_{jkt}(v) & \text{with probability } 1 - \mu_{jk}(v) \end{cases}$$

The probability function of innovation is given by the equation (2.5) below:

$$\lambda_{j} \frac{P_{jk} Z_{jk}(v)}{\gamma_{ik} A_{ik}(v)} = F\left[\mu_{jk}(v)\right], \quad F' > 0, \ F'' > 0, \ F(0) = 0$$
 (2.5)

where λ_j is a parameter representing the extent to which national policies or institutions encourage innovation, and $P_{jkt}Z_{jkt}(v)$ denotes the total amount invested in the intermediate variety v of sector k in country j for research and development (R&D). The innovation $\cot P_{jkt}Z_{jkt}(v)$ is divided by $\gamma_{jk}A_{jkt}(v)$, the targeted productivity parameter, to account for the higher cost of catching up with the most advanced technologies. At equilibrium, an innovator in country j chooses $Z_{jkt}(v)$ to maximize the difference between the expected profit $\beta \mu_{jkt}(v)\pi_{jkt+1}(v)$ and the cost of innovation $P_{jkt}Z_{jkt}(v)$, where β is the time discount factor.

2.3 Household

A representative household in each country j supplies inelastically L_{jt} units of labor, which is perfectly mobile across the three final sectors, at the wage rate w_{jt} . The household decides on consumption over time and also on final demand allocations across the three sectors. The lifetime utility of the representative household is defined over a discounted period utility, which is the logarithm of aggregate consumption per capita. Following Comin et al. (2021), the aggregate consumption C_{jt} , in each period, is defined as a generalized, non-homothetic, CES aggregate over the three sector composite goods C_{jkt} , k = a, m, s. The real aggregate consumption C_{jt} is described by an implicit function defined as follows:

$$\sum_{k=a,m,s} \delta_k^{1/\sigma} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}} \right)^{\frac{\sigma-1}{\sigma}} = 1$$
 (2.6)

where δ_k are constant weights for each sector in the economy³, σ is the elasticity of substitution between goods. $\sigma < 1$ such that agricultural and manufacturing goods and services are complements. ε_k define the relative Engel curve for each sectoral output k, representing the income elasticity of demand of sector k. C_{jt} is a nonhomothetic unobservable index of real consumption in country j at time t.

The key insight of equation (2.6) is the parameter ε_k , which governs the degree of nonhomotheticity. This parameter alone differentiates the role of income across sectors. The sector with a greater ε_k is considered a luxury good, which expands in expenditure shares as income rises, all else equal. Comin et al. (2021) show that this specification of nonhomothetic preferences has attractive properties for studying long-run structural change. Unlike Stone-Geary preferences, the elasticity of relative demand does not approach zero as income or consumption rises, as shown in the data. This feature is particularly relevant for the service sector, whose consumption grows more than proportionally, especially at later stages of development⁴. Note

 $^{{}^{3}\}sum_{k=a,m,s}\overline{\delta_{k}=1}$

⁴The rise of the service sector occurs at later stages of development, and to understand this fact, it is necessary that the income elasticity for services does not level off. With Stone-Geary preferences, the home production parameters play an important role only at early stages, but their effect vanishes in the long run (See Buera &

that if $\varepsilon_k = 1$, $\forall k$, then equation (2.6) yields:

$$C_{jt} = \left(\sum_{k \in \{a, m, s\}} \delta_k^{1/\sigma} C_{jkt}^{1 - \frac{1}{\sigma}}\right)^{\frac{\sigma}{\sigma - 1}} \quad \text{if} \quad \varepsilon_k = 1 \quad \forall k = a, m, s$$
 (2.7)

Equation (2.7) represents the composite good when preferences are homothetic, and σ is the within-period elasticity of substitution between consumption categories. Homothetic preferences are therefore a special case where all ε_k are equal to 1.

In each period, the representative household maximizes its utility, in each period by choosing sectoral consumption levels, C_{jkt} , as follow: Given the nonhomothetic CES aggregator (2.6), the intra-temporal household's problem in country j is as follows:

$$\max_{\left\{C_{jat},C_{jmt},C_{jst}\right\}} \ln C_{jt} \tag{2.8}$$

s.t.
$$\sum_{k \in \{a,m,s\}} P_{jkt} \left(C_{jkt} + Z_{jkt} \right) \le w_{jt} L_{jt} + \sum_{k=a,m,s} \Pi_{jkt}$$

where $\Pi_{jkt} := \int_0^1 \pi_{jkt}(v) dv$ is the total profit made in the sector k of the country j. This utility maximization problem (2.8) is equivalent to total expenditure on consumption in agriculture, manufacturing and services minimization problem subject to the implicit CES nonhomothetic aggregator.

2.4 Equilibrium

For each country j, the timing of the model can be summarized as follows:

- ❖ Step 0 : Period t starts with productivities, $A_{jkt}(v)$, $\forall v \in [0,1]$, inherited from the production and innovation activities of the previous periods;
- ❖ Step 1 : The production of intermediate goods then that of final goods takes place;
- ❖ Step 2 Innovators choose the optimal amount $Z_{jkt}(v)$ to invest in R&D in each intermediate sector $v \in [0,1], k = a, m, s$ for the next period.

Kaboski (2009)).

Step 3: Households choose the levels of consumption of goods a, m and s.

Let's now define and then characterize the competitive equilibrium of the model. A competitive equilibrium is :

- collections of wage rate and prices of final and intermediate goods $\mathbf{p}_j = \left\{ w_{jt}, P_{jkt} \right\}_{t=0}^{\infty} \; \forall j.$
- consumption allocation decissions $\mathbf{c}_j = \left\{C_{jat}, C_{jmt}, C_{jst}\right\}_{t=0}^{\infty}$ for the household for all j;
- labor and intermediate inputs allocation decisions $\mathbf{f}_j = \left\{L_{jkt}, \{x_{jkt}(v)\}_{v \in [0,1]}\right\}_{t=0}^{\infty}$ for firms in final sectors for all j;
- collection of decisions $\mathbf{i}_j = \left\{ Z_{jkt}(v), \mathbf{x}_{jkt}(v) \right\}_{t=0}^{\infty}$; $v \in [0,1], k=a,m,s$ for producers of intermediate varieties j_k such that:
 - Given \mathbf{p}_i , households solve the problem (2.23) $\forall j$;
 - Given \mathbf{p}_j , final sectors producers solve the problem (??) $\forall j$;
 - Given \mathbf{p}_i , varieties' producers solve their problem;

And the following markets clearing conditions are verified:

- (a) Labor market : $L_{jat} + L_{jmt} + L_{jst} = L_{jt}$ for all t and j;
- (b) Intermediate varieties markets : $x_{jkt}(v) = \mathbf{x}_{jkt}(v) \quad \forall v \in [0,1] \; ; \; \forall k \in \{a,m,s\} \; \; \forall t \; \text{and} \; \forall j \; ;$
- (c) Final goods markets: $Y_{jkt} = C_{jkt} + X_{jkt} + Z_{jkt}$ $\forall k = a, m, s$, for each j and for each period.

where $X_{jkt} := \int_0^1 x_{jkt}(v) dv$ and $Z_{jkt} := \int_0^1 Z_{jkt}(v) dv$ are respectively the aggregate production of intermediate varieties and total investment in R&D in sector k.

2.5 Firms' optimization

The first order conditions for the firm in the final sector k of the country j are given by:

$$\begin{cases} p_{jkt}(v) = \alpha P_{jkt} x_{jkt}(v)^{\alpha - 1} A_{jkt}(v)^{1 - \alpha} L_{jkt}^{1 - \alpha} & \forall v \in [0, 1] \\ w_{jt} = (1 - \alpha) P_{jkt} L_{jkt}^{-\alpha} \int_{0}^{1} A_{jkt}(v)^{1 - \alpha} x_{jkt}(v)^{\alpha} dv \end{cases}$$

Thus, the firm of the final sector equalizes the marginal productivity of labor to the real wage and the demand function for intermediate goods of variety v for the firm in the final sector is given by:

$$x_{jkt}(v) = \alpha^{\frac{1}{1-\alpha}} \left(\frac{p_{jkt}(v)}{P_{jkt}} \right)^{-\frac{1}{1-\alpha}} A_{jkt}(v) L_{jkt} \quad \forall v \in [0,1] \text{ and } k = a, m, s$$
 (2.9)

By utilizing the demand function from equation (2.9) in problem (2.4), the equilibrium quantity of the variety v of sector k in country j is given by:

$$x_{jkt}(\mathbf{v}) = \alpha^{\frac{2}{1-\alpha}} A_{jkt}(\mathbf{v}) L_{jkt}$$
 (2.10)

at the price $p_{jkt}(v)$ given by :

$$p_{ikt}(\mathbf{v}) = \alpha^{-1} P_{ikt} \tag{2.11}$$

The profit made by the intermediate monopoly producing the variety v in sector k is therefore given at equilibrium by:

$$\pi_{jkt}(\mathbf{v}) = \pi P_{jkt} A_{jkt}(\mathbf{v}) L_{jkt} \tag{2.12}$$

where $\pi:=(1-\alpha)\alpha^{\frac{1+\alpha}{1-\alpha}}$. Therefore, the profits generated by each intermediate monopoly depend positively on productivity, the labor force, and the price of the final good in this sector. Indeed, an increase in the output price in a sector positively affects the prices of intermediate goods used in this sector. Additionally, the increase in labor demand in a sector will have the effect of increasing output and, therefore, increasing the demand for varieties that are used in the same Cobb-Douglas production function.

Using the equation (2.12), the innovator maximizes its expected net payoff of the next period, given by:

$$\max_{\left\{\mu_{jkt}(v)\right\}} \left[\beta \pi \mu_{jkt}(v) P_{jkt+1} L_{jkt+1} - \lambda_j^{-1} P_{jkt} F\left(\mu_{jkt}(v)\right) \right] \gamma_{jk} A_{jkt}(v)$$
(2.13)

Solving the problem (2.13) yields the same probability of innovation in the same sector $\mu_{jkt}(v) = \mu_{jkt}$ with μ_{jkt} given by:

$$\mu_{jkt} = F'^{-1} \left[\beta \pi \lambda_j \frac{P_{jkt+1}}{P_{jkt}} L_{jkt+1} \right] \quad \forall v \in [0, 1] \text{ and } \forall k = a, m, s.$$
 (2.14)

In the special case where the research-productivity function F takes the simple quadratic form:

$$F(\mu_{jkt}(\mathbf{v})) = \frac{1}{2}\mu_{jkt}(\mathbf{v})^2$$

then the innovation probability in the sector k is given by :

$$\mu_{jkt} = \beta \pi \lambda_j \frac{P_{jkt+1}}{P_{jkt}} L_{jkt+1} \quad \forall k = a, m, s.$$
 (2.15)

The equation (2.15) indicates that an increase in the demand for labor and in the output price growth rate in a sector encourages entrepreneurs to innovate more in that sector, as the expected gains will increase. All else being equal, it is more profitable to innovate in a larger sector because a successful innovator has a larger market share in that sector. Additionally, considering any changes in demand composition due to Engel's law that increase the demand for sector k, its price will increase, thereby enhancing innovation opportunities due to the higher profitability associated with this sector.

2.6 Aggregate behavior

Let's define the productivity of the sector k in the country $j A_{jkt}$ at time t as:

$$A_{jkt} := \int_0^1 A_{jkt}(v) \, dv \tag{2.16}$$

Then, using the expression of μ_{jkt} from equation (2.15) and after a few manipulations⁵, the productivity growth rate $g_{A_{kt}}$ is found as the following function:

$$g_{A_{jkt}} = \beta \pi \lambda_j \frac{P_{jkt+1}}{P_{ikt}} \left(\gamma_{jk} - 1 \right) L_{jkt+1}$$
(2.17)

The productivity growth rate, $g_{A_{jkt}}$, increases with the sectoral labor share and the output price growth rate. An increase in the number of workers in a sector leads to an augmentation in the production of the final good and the demand for intermediate goods, thereby resulting in increased profits for monopolists operating within that sector. This, in turn, incentivizes further innovation, consequently fostering heightened productivity within the sector.

As a result, changes in sectoral employment driven by shifts in demand across sectors influence variations in innovation rates and productivity growth. According to Matsuyama (2019), sectoral productivity growth adjusts in response to these changes in market size, indicating that the demand-driven mechanism of structural change (due to Engel's Law) and the supply-driven mechanism (through productivity growth) are interconnected rather than independent forces.

The production level of the final good k in country j at equilibrium is obtained by substituting equation (2.10) into equation (2.1):

$$Y_{ikt} = \alpha^{\frac{2\alpha}{1-\alpha}} A_{ikt} L_{ikt}$$
 (2.18)

and the wage rate is determined from the first-order conditions of the firm in the final sector k by:

$$w_{jt} = \omega P_{jkt} A_{jkt} \tag{2.19}$$

where $\omega := (1 - \alpha)\alpha^{\frac{2\alpha}{1-\alpha}}$. As the wage rate is constant across sectors in the same country, a slower productivity growth in a sector causes its relative price to go up over time. To see this, let's divide the equation (2.19) for the sector k and m for example, then we can deduce a relation

⁵More details are provided in Appendix A.3

between the price and the productivity in sector k relative to the sector m as shown below:

$$\frac{P_{kt}}{P_{mt}} = \frac{A_{mt}}{A_{kt}} \tag{2.20}$$

Let's denote VA_{jkt} the value added of the sector k and its intermediate branches at the period t in the country j. Then⁶

$$VA_{jkt} = P_{jkt}Y_{jkt} - P_{jkt} \int_0^1 x_{jkt}(v) dv$$
$$= \zeta P_{jkt}A_{jkt}L_{jkt}$$
(2.21)

where $\zeta := (1 - \alpha^2) \alpha^{\frac{2\alpha}{1-\alpha}}$. As the wage rate w_{jt} is constant across sectors in the same country, the Gross Domestic Production of the economy is given by:

$$GDP_t = \zeta P_{kt} A_{kt} L_t, \quad k = a, m, s \tag{2.22}$$

Note that the GDP is proportional to the nominal wage of the economy and that the sectoral values added are a function of the wage rate and the level of sectoral employment.

2.7 Household's optimization

Given the nonhomothetic CES aggregator, the intra-temporal household's problem in country j is equivalent⁷ to:

$$\min_{\{C_{jat}, C_{jmt}, C_{jst}\}} \sum_{k=a, m, s} P_{jkt} C_{jkt}$$
(2.23)

s.t.
$$\sum_{k=a,m,s} \delta_k^{1/\sigma} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}} \right)^{\frac{\sigma-1}{\sigma}} = 1$$

⁶See Appendix A.2 for more details.

⁷The expenditure minimization problem is the dual of the utility maximization problem. The relationship between the utility function and Marshallian demand in the utility maximization problem mirrors the relationship between the expenditure function and Hicksian demand in the expenditure minimization problem.

Each period the household minimizes the expenditure on consumption in agriculture, manufacturing and services subject to the implicit CES nonhomothetic aggregator.

The first order conditions⁸ imply that sectoral consumption demand satisfies:

$$C_{jkt} = \delta_k \left(\frac{P_{jkt}}{E_{jt}}\right)^{-\sigma} C_{jt}^{\varepsilon_k(1-\sigma)}$$
(2.24)

where $E_{jt} := \sum_{k=a,m,s} P_{jkt} C_{jkt}$ is the total expenditure in consumption at time t in country j. Replacing E_{jt} by $P_{jt} C_{jt}$ in the equation (2.24) where P_{jt} is the average cost of real consumption, one can show that :

$$C_{jkt} = \delta_k \left(\frac{P_{jkt}}{P_{jt}}\right)^{-\sigma} C_{jt}^{\varepsilon_k(1-\sigma)+\sigma}$$
(2.25)

where the aggregate price P_{jt} is given⁹ by :

$$P_{jt} = \left[\sum_{k=a,m,s} \delta_k P_{jkt}^{1-\sigma} C_{jt}^{(1-\sigma)(\varepsilon_k - 1)} \right]^{\frac{1}{1-\sigma}}$$
(2.26)

Thus, the sectoral expenditure e_{ikt} in the good k of the country j is given by:

$$e_{jkt} = \frac{P_{jkt}C_{jkt}}{P_{jt}C_{jt}}$$

$$= \delta_k \left(\frac{P_{jkt}}{P_{jt}}\right)^{1-\sigma} C_{jt}^{(1-\sigma)(\varepsilon_k - 1)} \qquad \forall k$$
(2.27)

By dividing e_{jkt} by e_{jmt} using (2.27) and the equation (2.20), we can obtain the expression of the consumption expenditure share of sector k = a, s relative to manufacturing sector m below:

$$\frac{e_{jkt}}{e_{imt}} = \frac{\delta_k}{\delta_m} \left(\frac{A_{jmt}}{A_{jkt}}\right)^{1-\sigma} C_{jt}^{(\varepsilon_k - \varepsilon_m)(1-\sigma)} \qquad k = a, s$$
 (2.28)

The equation (2.28) illustrates both the supply and demand-side mechanisms for structural change through the allocation of consumption between different sectors. The parameter σ

⁸See Appendix A.4 for calculation.

⁹See Appendix A.4 for the demonstration.

governs the supply-side mechanisms of the structural change via sector-biased productivity effects, and the relative comparison of income elasticities $\varepsilon_k - \varepsilon_m$ governs the relative long-run Engel curves.

As $\sigma < 1$ due to the complementary nature of foods, manufacturing goods, and services, an increase in the relative sectoral productivity of sector k will result in a decrease in its relative consumption expenditure share. This rise in sector k's productivity will, in turn, lead to a reduction in its final good price. Consequently, consumers can maintain the same quantity of goods from sector k' experiencing greater productivity growth while spending less, enabling them to allocate the remaining income to other products. This ensures a certain level of consumption from sectors with lower productivity growth, ultimately resulting in a decrease in the proportion of expenditure in sectors with higher rates of productivity growth.

Similarly, when sectoral income elasticities differ, such that $\varepsilon_k - \varepsilon_m > 0$, then sector k expenditure share also rises with the aggregate consumption and vice versa. In fact, income elasticity measures how sensitive the demand for a good is to changes in income. When $\varepsilon_k - \varepsilon_m > 0$, it means that the income elasticity of sector k is greater than that of sector k. This implies that as aggregate consumption increases - due to an increase in income-, consumers tend to spend a larger proportion of their income on goods from sector k compared to sector k. Conversely, when k0, the expenditure share on goods from sector k1 decreases relative to sector k2. This illustrates how alterations in aggregate consumption influence the distribution of expenditure among sectors with varying income elasticities. In the data, k1 ck2 ck3, indicating that the shares of consumption expenditure on services increase relative to manufacturing, while those on agriculture decrease.

2.8 Innovation and Structural Change in a Closed Economy

Structural change is defined as a shift in the relative importance of the aggregate indicators of the economy, such as sectoral national product s_{jkt} , sectoral consumption expenditure e_{jkt} , and the sectoral employment $\ell_{jkt} := \frac{L_{jkt}}{L_{jt}}$ for k = a, m, s. By leveraging equations (2.21) and (2.22),

I derive the equivalence

$$\ell_{jkt} = s_{jkt} \tag{2.29}$$

Equation (2.29) implies that the share of value added is identical to the share of employment in a closed economic system. This relationship arises from the fact that profits accrued within a particular sector correlate directly with the magnitude of employment within that sector. This association stems from the fact that as the proportion of employment grows within a sector, there is a concurrent increase in the output and in the demand for intermediate goods. Hence, the income of both workers and entrepreneurs follows a linear pattern determined by the wage rate and the employment level within the sector utilizing intermediate goods. Likewise, the market clearing condition for the final good of the sector k is given by:

$$Y_{ikt} = C_{ikt} + X_{ikt} + Z_{ikt} (2.30)$$

Then, we can derive the value added $VA_{jkt} := P_{jkt}Y_{jkt} - P_{jkt}X_{jkt}$ of sector k at time t in country j as follows:

$$VA_{ikt} = P_{ikt}C_{ikt} + P_{ikt}Z_{ikt}$$
 (2.31)

From equation (2.31), we can express the consumption expenditure share in sector k as follows:

$$e_{jkt} = \frac{VA_{jkt} - P_{jkt}Z_{jkt}}{GDP_{jt} - \sum_{k=a}^{b} P_{jkt}Z_{jkt}}$$
(2.32)

Then, by dividing both the numerator and the denominator by GDP and rearranging, we obtain the following equation, which provides the relationship between the share of consumption expenditure, value added, the sectoral share of innovation expenditure, and the weight of

innovation expenditure in GDP:

$$s_{jkt} = \frac{P_{jkt}Z_{jkt}}{GDP_{jt}} + \left(1 - \frac{\sum_{k=a,m,s} P_{jkt}Z_{jkt}}{GDP_{jt}}\right)e_{jkt}$$
(2.33)

The equation (2.33) illustrates the disparity between the value-added share and the consumption expenditure share, even in a closed economy. In the subsequent section, I extend the model to incorporate international trade in intermediate goods and derive variations in sectoral value-added and employment shares.

3 Opening the Economy

3.1 Final Goods Production

The producer of the final good in sector *k* utilizes domestic labor and a continuum of intermediate goods produced by global monopolists. These intermediate goods possess a quality or

¹⁰There is no trade costs within a country.

efficiency $\hat{A}_{kt}(v) := \max\{A_{Hkt}(v), A_{Fkt}(v)\}$. In other words, the country that manages to produce the most productive latest version of intermediate good v in sector k holds the monopoly rights and will be the only one able to commercialize the intermediate good desired by the final sector firms. The Schumpeterian paradigm assumes that producers of final goods employ the latest versions of new technologies or machinery. In country j, the problem faced by the producer of the final good k can be formulated as follows:

$$\max_{\left\{L_{jkt},\left[x_{jkt}(v)\right]_{v\in[0,1]}\right\}} P_{jkt} L_{jkt}^{1-\alpha} \int_{0}^{1} \hat{A}_{kt}(v)^{1-\alpha} x_{jkt}(v)^{\alpha} dv - \int_{0}^{1} \hat{p}_{jkt}(v) x_{jkt}(v) dv - w_{jt} L_{jkt}$$
(3.1)

where the price at which firm in final sector k in country j buys the latest version of its variety v is $\hat{p}_{jkt}(v)$ given by:

$$\hat{p}_{jkt}(v) = \begin{cases} p_{jkt}(v) & \text{if} \quad \hat{A}_{kt}(v) = A_{jkt}(v) \\ \tau_{ijk}p_{ikt}(v) & \text{if} \quad \hat{A}_{kt}(v) > A_{jkt}(v) \end{cases}$$

with $p_{jkt}(v) = \alpha^{-1}P_{jkt} \ \forall j \neq i \in J$. The demands 11 of the final sector firm k in country j for the intermediate varieties produced in the country j, x_{jkt}^{j} , and the intermediate varieties produced by the country i, x_{jkt}^{i} are then given by:

$$\begin{cases} x_{jkt}^{j}(\mathbf{v}) = \left(\frac{p_{jkt}(\mathbf{v})}{\alpha P_{jkt}}\right)^{\frac{1}{\alpha-1}} A_{jkt}(\mathbf{v}) L_{jkt} \\ x_{jkt}^{i}(\mathbf{v}) = \left(\frac{\tau_{ijk} p_{ikt}(\mathbf{v})}{\alpha P_{jkt}}\right)^{\frac{1}{\alpha-1}} A_{ikt}(\mathbf{v}) L_{jkt} \end{cases}$$

$$x_{jkt}(v) = \begin{cases} x_{jkt}^{j}(v) & \text{if } \hat{A}_{kt}(v) = A_{jkt}(v) \\ x_{jkt}^{i}(v) & \text{if } \hat{A}_{kt}(v) = A_{ikt}(v) \end{cases}$$

¹¹The intermediate variety v used by the firm producing the final good depends on the country producing the latest version of the variety v:

3.2 World Monopoly Varieties Producers

The problem faced by a monopoly firm producing $X_{kt}^{j}(v)$ quantity of the variety v in sector k in country j for the world market is given by:

$$\max_{\left\{p_{jkt}(v)\right\}} \pi_{jkt}(v) = p_{jkt}(v) X_{kt}^{j}(v) - P_{jkt} X_{kt}^{j}(v)$$
(3.2)

s.t.
$$\begin{cases} X_{kt}^{j}(\mathbf{v}) = x_{jkt}^{j}(\mathbf{v}) + x_{ikt}^{j}(\mathbf{v}) \\ x_{jkt}^{j}(\mathbf{v}) = \left(\frac{p_{jkt}(\mathbf{v})}{\alpha P_{jkt}}\right)^{\frac{1}{\alpha - 1}} A_{jkt}(\mathbf{v}) L_{jkt} \\ x_{ikt}^{j}(\mathbf{v}) = \left(\frac{\tau_{jik} p_{jkt}(\mathbf{v})}{\alpha P_{ikt}}\right)^{\frac{1}{\alpha - 1}} A_{jkt}(\mathbf{v}) L_{ikt} \end{cases}$$

By solving the problem (3.2), as in the case of the closed economy, the monopolist will choose the price level that maximizes its profit, namely, $p_{jkt}(v) = \alpha^{-1}P_{jkt}$. Then, the demands of the country j final good k producer are expressed as follows:

$$\begin{cases} x_{jkt}^{j}(\mathbf{v}) = \alpha^{\frac{2}{1-\alpha}} A_{jkt}(\mathbf{v}) L_{jkt} \\ x_{jkt}^{i}(\mathbf{v}) = \alpha^{\frac{2}{1-\alpha}} \left(\frac{P_{jkt}}{\tau_{ijk} P_{ikt}} \right)^{\frac{1}{1-\alpha}} A_{ikt}(\mathbf{v}) L_{jkt} \end{cases}$$

Thus, the profit of a world monopoly firm producing the variety v in the sector k in country j is given by:

$$\pi_{jkt}(\mathbf{v}) = (\alpha^{-1} - 1) P_{jkt} \left[x_{jkt}^{j}(\mathbf{v}) + x_{ikt}^{j}(\mathbf{v}) \right]$$

$$= \pi P_{jkt} A_{jkt}(\mathbf{v}) \left[L_{jkt} + \left(\frac{P_{ikt}}{\tau_{ijk} P_{jkt}} \right)^{\frac{1}{1-\alpha}} L_{ikt} \right]$$
(3.3)

with $\pi := (1 - \alpha)\alpha^{\frac{1+\alpha}{1-\alpha}}$. The total profit Π_{jkt} made in the sector k in the country j at time t is :

$$\Pi_{jkt} = \pi P_{jkt} \left[L_{jkt} + \left(\frac{P_{ikt}}{\tau_{ijk} P_{jkt}} \right)^{\frac{1}{1-\alpha}} L_{ikt} \right] \int_{\Theta_{jkt}} A_{jkt}(v) dv$$
 (3.4)

where Θ_{jkt} is the set of varieties of the sector k that country j produces and exports at time t such that :

$$\int_{\Theta_{jkt}} A_{jkt}(v) dv = \int_0^1 A_{jkt}(v) \mathbf{1}_{\{A_{jkt}(v) > A_{ikt}(v)\}} dv$$

The equation (3.4) illustrates that the profits of domestic monopolists in a given sector k are proportional not only to the domestic employment but also to the foreign employment size. A portion of the profit stems from foreign demand, which correlates with the size of the partner country's sector. Sectors in which the country holds global monopoly experience increased profits compared to a closed economy, whereas sectors in which the country imports all intermediate goods see their profits diminish to zero.

An increase in the expected profit for innovators affects their incentives to innovate, as each potential innovator aims to become the world-leading producer in their respective sector¹². In an open economy, the probability of successful innovation is determined by solving a profit-maximization problem. The objective function below captures the difference between the expected profit from innovation and the associated cost:

$$\max_{\left\{\mu_{jkt}(v)\right\}} \beta \pi P_{jkt} \hat{A}_{jkt}(v) \left[L_{jkt+1} + \left(\frac{P_{ikt+1}}{\tau_{ijk} P_{jkt+1}} \right)^{\frac{1}{1-\alpha}} L_{+1} \right] \mu_{jkt}(v) - \lambda_{j}^{-1} P_{jkt} F\left(\mu_{jkt}(v)\right) \hat{A}_{jkt}(v)$$
(3.5)

By solving the optimization problem in (3.5), we derive the optimal probability of innovation:

$$\mu_{jkt} = \beta \pi_{jkt+1} \lambda_j \frac{P_{jkt+1}}{P_{jkt}} \left[L_{jkt+1} + \left(\frac{P_{ikt+1}}{\tau_{ijk} P_{jkt+1}} \right)^{\frac{1}{1-\alpha}} L_{ikt+1} \right] \quad \forall; k = a, m, s$$
 (3.6)

This result in (3.6) shows that the probability of innovation increases in an open economy compared to a closed economy. The primary driver of this increase is the larger market size

$$A_{jkt+1}(v) = egin{cases} \hat{A}_{kt}(v) & ext{ with probability } \mu_{jk}(v) \ A_{jkt}(v) & ext{ with probability } 1 - \mu_{jk}(v) \end{cases}$$

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and higher potential profit due to international trade. The term involving the ratio of price indices and labor inputs illustrates that sectors with higher access to foreign markets or lower trade costs experience a higher probability of innovation. Consequently, globalization and trade openness enhance innovation incentives by expanding market. Therefore, the open economy framework not only raises the expected profits for innovators but also induces more frequent technological advancements, particularly in sectors with greater exposure to international competition and trade.

Using the first order conditions of the problem (3.1), the wage rate in the country j, w_{jt} , at time t is determined by :

$$w_{jt} = (1 - \alpha)\alpha^{\frac{2\alpha}{1 - \alpha}} P_{jkt} A_{jkt}$$
(3.7)

where the sectoral aggregate productivity of country j in sector k at time t, denoted as A_{jkt} , is determined by:

$$A_{jkt} = \int_{\Theta_{jkt}} A_{jkt}(v) dv + \left(\frac{P_{jkt}}{\tau_{ijk} P_{ikt}}\right)^{\frac{\alpha}{1-\alpha}} \int_{\Theta_{ikt}} A_{ikt}(v) dv$$
 (3.8)

Finally, the equilibrium condition in the final goods market is described by the equation (3.9) below:

$$Y_{jkt} = C_{jkt} + Z_{jkt} + \int_{\Theta_{ikt}} \left[x_{jkt}^{j}(v) + x_{ikt}^{j}(v) \right] dv$$
 (3.9)

The condition (3.9) stipulates that, in each sector-country, the utilization of the final good k must equal its supply. This utilization comprises consumption and investment in R&D by the representative household, as well as the use of intermediate inputs by innovator firms producing the varieties for both domestic and foreign final good k producers.

3.3 Monopoly Rights, Trade, and Structural Change

In this subsection, I will establish new relationships between sectoral shares of value added and shares of consumption expenditure on one hand, and sectoral shares of employment and value added on the other hand. I will then analyze how innovation and monopoly rights through international trade modify the pre-established relationships in a closed economy. Let us begin by first expressing a relationship between sectoral shares of value added and those of consumption expenditure.

Comparison of Consumption Expenditure and Value-Added Shares. The value added of the sector k in the country j is defined by :

$$VA_{jkt} = \underbrace{P_{jkt}Y_{jkt} - \int_{\Theta_{jkt}} p_{jkt}(v)x_{jkt}^{j}(v)dv - \int_{\Theta_{ikt}} \tau_{ijk}p_{ikt}(v)x_{jkt}^{i}(v)dv}_{\text{Final sector value added}} + \underbrace{\int_{\Theta_{jkt}} \left(p_{jkt}(v) - P_{jkt}\right) \left[x_{jkt}^{j}(v) + x_{ikt}^{j}(v)\right] dv}_{\text{Intermediate varieties value added}}$$
(3.10)

Using the equation (3.9) of the final good market clearing condition, the equation (3.10) transforms into the equation below:

$$VA_{jkt} = P_{jkt} \left(C_{jkt} + Z_{jkt} \right) + NX_{jkt}$$
(3.11)

where NX_{jkt} represents the net exports of all varieties of sector k for country j at period t:

$$NX_{jkt} = \int_{\Theta_{jkt}} p_{jkt}(v) x_{ikt}^{j}(v) dv - \int_{\Theta_{ikt}} \tau_{ijk} p_{ikt}(v) x_{jkt}^{i}(v) dv$$
 (3.12)

Now, from equation (3.11), the consumption expenditure share in sector k is given by:

$$e_{jkt} = \frac{VA_{jkt} - NX_{jkt} - P_{jkt}Z_{jkt}}{GDP_{jt} - \sum_{k=a,m,s} P_{jkt}Z_{jkt} - \sum_{k=a,m,s} NX_{jkt}}$$
(3.13)

Dividing both the numerator and the denominator by GDP_{jt} and rearranging, I obtain the relation below:

$$s_{jkt} = \left(1 - \frac{\sum_{k=a,m,s} P_{jkt} Z_{jkt}}{GDP_{jt}} - \frac{\sum_{k=a,m,s} NX_{jkt}}{GDP_{jt}}\right) e_{jkt} + \frac{P_{jkt} Z_{jkt} + NX_{jkt}}{GDP_{jt}}$$
(3.14)

where s_{jkt} is the value-added share of the sector k in the country j at time t. The equation (3.14) illustrates that net export expenditures, in addition to research and development spending in each sector, alter the relationship between sectoral value-added shares and consumption expenditure shares. If a country exports relatively more than it imports in a given sector k, or allocates relatively higher expenditures in this sector, then the share of value added in this sector is likely to be higher than that of consumption expenditure, and vice versa.

Comparison of Employment and Value-Added Shares. Let us now establish the relationship between the share of value added and the sectoral labor share in each country. The value added in sector k can also be defined from a revenue perspective as the sum of wages and all profits in sector k as follows:

$$VA_{jkt} = w_{jt}L_{jkt} + \Pi_{jkt} \tag{3.15}$$

Utilizing the expression of Π_{jkt} provided in equation (3.4), the value-added share is given by:

$$s_{jkt} = \frac{w_{jt}L_{jkt} + \pi P_{jkt} \left[L_{jkt} + \left(\frac{P_{ikt}}{\tau_{ijk}P_{jkt}} \right)^{\frac{1}{1-\alpha}} L_{ikt} \right] \int_{\Theta_{jkt}} A_{jkt}(v) dv}{w_{jt}L_{jt} + \sum_{n=a,m,s} \pi P_{jnt} \left[L_{jnt} + \left(\frac{P_{int}}{\tau_{ijn}P_{jnt}} \right)^{\frac{1}{1-\alpha}} L_{int} \right] \int_{\Theta_{jnt}} A_{jnt}(v) dv}$$
(3.16)

Then, by dividing both the numerator and the denominator by $w_{jt}L_{jt}$ and rearranging to make the sectoral employment share $\ell_{jkt} := \frac{L_{jkt}}{L_{jt}}$ appear in each term, we obtain the following relationship between the sectoral value-added share s_{jkt} and the sectoral employment share ℓ_{jkt} :

$$\frac{s_{jkt}}{\ell_{jkt}} = \frac{1 + \alpha \left[1 + \left(\frac{P_{ikt}}{\tau_{ijk} P_{jkt}} \right)^{\frac{1}{1-\alpha}} \frac{L_{ikt}}{L_{jkt}} \right] \frac{1}{A_{jkt}} \int_{\Theta_{jkt}} A_{jkt}(v) dv}{1 + \alpha \sum_{n=a,m,s} \ell_{jnt} \left[1 + \left(\frac{P_{int}}{\tau_{ijn} P_{jnt}} \right)^{\frac{1}{1-\alpha}} \frac{L_{int}}{L_{jnt}} \right] \frac{1}{A_{jnt}} \int_{\Theta_{jnt}} A_{jnt}(v) dv}$$
(3.17)

The relationship between sectoral shares of value added and employment, as described by Equation (3.17), underscores the absence of inherent equality between these two measures a priori. Equality between them emerges when total profits across sectors are equal, a condi-

tion typically realized when the nation lacks monopolistic control in any sector and imports all intermediate goods. In sectors characterized by high levels of innovation on the global stage, where domestic companies act as monopolists, surplus profits are often generated. This innovation-driven competitiveness enables these firms to command higher prices for their goods or services, resulting in a larger share of value added within the sector. Consequently, while the share of sectoral value added tends to exceed that of employment in such innovative sectors, it tends to be lower in sectors where domestic firms exhibit lower levels of innovation compared to their international counterparts.

Furthermore, it is important to note that the structure of the economy in the rest of the world also determines the relationship between sectoral shares of value added and sectoral shares of employment. If the size of sector k is relatively larger compared to other sectors $n \neq k$ in the foreign country i, such that $\frac{L_{ikt}}{L_{jkt}} > \frac{L_{imt}}{L_{jnt}}$ for $n \neq k$, then the share of value added in sector k in the home country j tends to increase relative to the share of employment in sector k. This implies an interconnectedness of national economies with the global economic landscape. Changes in the structure and performance of foreign economies can have significant implications for domestic sectors, affecting their relative shares of value added and employment. These linkages manifest through the demand for intermediate goods, which serves as a crucial channel for transmitting economic changes across borders.

When a foreign economy experiences substantial growth or possesses a significant size in particular sectors, it often translates into a higher demand for intermediate goods produced by domestic world monopolists. This heightened demand stems from the need for inputs and components necessary for the production processes within the larger foreign sectors. As a result, domestic producers of intermediate goods experience increased sales and profitability, driving up their share of value added within the economy. Additionally, when the ratio of the price of final goods in the foreign country to the national price is higher in a given sector k, such that $\frac{P_{ikt}}{\tau_{ijk}P_{jkt}} > \frac{P_{int}}{\tau_{ijn}P_{jnt}}$ for $k \neq n$, then the additional profits in sector k are higher, and the share of value added increases more in sector k than it does in sector n. Indeed, the demand for intermediate goods from the foreign country decreases with the cost related to trade and with the price of the exporting country, and it increases with the price of the final goods from the

importing country.

4 Conclusion

The analysis presented in this paper underscores the intricacies of economic structural change and its measures, particularly focusing on sectoral employment shares, sectoral value-added shares, and sectoral final consumption expenditure shares. While previous research often treated these measures as interchangeable, Buera & Kaboski (2009) and Herrendorf et al. (2014) highlighted their quantitative distinctions.

This paper proposes a novel theoretical framework grounded in a Schumpeterian paradigm, which integrates technological innovation and international trade dynamics to explain the disparities between sectoral value-added and sectoral employment shares. By considering surplus profits obtained by domestic monopolistic entrepreneurs due to foreign demand along-side domestic demand, this framework offers a comprehensive understanding of the drivers of structural transformation. It sheds light on the factors contributing to disparities between value-added and employment shares across sectors, filling critical gaps in traditional theories.

The model shows that sectors characterized by high levels of innovation and monopolistic control by domestic companies tend to generate surplus profits by charging higher prices for their products, consequently leading to a larger share of value added within their sector compared to employment. Moreover, the structure and performance of foreign economies significantly impact this relationship, as larger or rapidly growing foreign sectors drive a heightened demand for export goods from domestic producers. This increased demand not only boosts sales and profitability but also enhances the share of value added relative to employment. Furthermore, lower sectoral trade costs and higher foreign prices stimulate increased demand for intermediate goods, further amplifying the share of value added within sectors.

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A Appendix

A.1 Goods production sectors

The problem of the intermediate firm j_k with drastic innovation is :

$$\max_{\left\{x_{jkt}(v)\right\}} \pi_{jkt}(v) = p_{jkt}(v)x_{jkt}(v) - P_{jkt}x_{jkt}(v)$$
(A.1)

s.t.
$$p_{jkt}(v) = \alpha P_{jkt} x_{jkt}(v)^{\alpha - 1} A_{jkt}(v)^{1 - \alpha} L_{jkt}^{1 - \alpha}$$

The first order condition is given by:

$$\alpha^{2} P_{jkt} x_{jkt}(v)^{\alpha - 1} A_{jkt}(v)^{1 - \alpha} L_{jkt} - P_{jkt} = 0 \iff x_{jkt}(v) = \alpha^{\frac{2}{1 - \alpha}} A_{jkt}(v) L_{jkt}$$

Then the intermediate variety price is given from the constraint of the problem (A.1) by:

$$p_{ikt}(\mathbf{v}) = \alpha^{-1} P_{ikt} \tag{A.2}$$

A.2 Aggregate behavior

The value added of the sector k in the country j in closed economy is given by :

$$VA_{jkt} = \underbrace{P_{jkt}Y_{jkt} - \int_0^1 p_{jkt}(v)x_{jkt}(v) \, dv}_{\text{Final sector value added}} + \underbrace{\int_0^1 \left(p_{jkt}(v)x_{jkt}(v) - P_{jkt}x_{jkt}(v)\right) \, dv}_{\text{Intermediate varieties value added}}$$

$$= P_{jkt}Y_{jkt} - \int_0^1 P_{jkt}x_{jkt}(v) \, dv$$

$$= \alpha^{\frac{2\alpha}{1-\alpha}}P_{jkt}A_{jkt}L_{jkt} - \alpha^{\frac{2}{1-\alpha}}P_{jkt}A_{jkt}L_{jkt}$$

$$= (1-\alpha^2)\alpha^{\frac{2\alpha}{1-\alpha}}P_{jkt}A_{jkt}L_{jkt}$$

❖ Calculation of GDP by income perspective

$$GDP_{jt} = w_{jt}L_{jt} + \sum_{k=a,m,s} \Pi_{jkt}$$
(A.3)

where

$$\Pi_{jkt} = \int_0^1 \pi_{jkt}(v) \, dv$$

is the total profits made in sector k intermediate varieties. By replacing w_{jt} and $\pi_{jkt}(v)$ by their expression, the equation (A.3) becomes :

$$GDP_{jt} = (1 - \alpha)\alpha^{\frac{2\alpha}{1 - \alpha}}P_{jkt}A_{jkt}L_{jkt} + (1 - \alpha)\alpha^{\frac{1 + \alpha}{1 - \alpha}}\sum_{n = a, m, s}P_{jnt}A_{jnt}L_{jnt}$$

$$= (1 - \alpha)\alpha^{\frac{2\alpha}{1 - \alpha}}P_{jkt}A_{jkt} + (1 - \alpha)\alpha^{\frac{1 + \alpha}{1 - \alpha}}P_{jkt}A_{jkt}\sum_{n = a, m, s}L_{jnt}$$

$$= (1 - \alpha)\alpha^{\frac{2\alpha}{1 - \alpha}}\left[1 + \alpha^{\frac{1 + \alpha - 2\alpha}{1 - \alpha}}\right]P_{jkt}A_{jkt}L_{jt}$$

$$= \zeta P_{jkt}A_{jkt}L_{jt} \quad \forall k = a, m, s$$
(A.4)

where $\zeta := (1 - \alpha^2) \alpha^{\frac{2\alpha}{1-\alpha}}$

❖ Calculation of the GDP by value added perspective

$$GDP_{jt} = \sum_{n=a,m,s} VA_{jnt}$$

$$= \sum_{n=a,m,s} \zeta P_{jnt} A_{jnt} L_{jnt}$$

$$= \zeta P_{jkt} A_{jkt} \sum_{n=a,m,s} L_{jnt}$$

$$= \zeta P_{jkt} A_{jkt} L_{jt} \quad \forall k = a, m, s$$
(A.5)

A.3 Dynamics of productivity

The expected productivity growth rate $g_{A_{kt}}$ of the sector k is :

$$g_{A_{jkt}} = \frac{A_{jkt} - A_{jkt}}{A_{jkt}}$$

$$= \frac{1}{A_{jkt}} \int_{0}^{1} \mu_{jkt} \left(\gamma_{jk} A_{jkt}(v) - A_{jkt}(v) \right) dv$$

$$= \frac{\mu_{jkt} (\gamma_{jk} - 1)}{A_{kt}} \int_{0}^{1} A_{jkt}(v) dv$$

$$= \mu_{jkt} (\gamma_{jk} - 1)$$
(A.6)

A.4 Housesolds' optimization

The lagragian of the household's problem in country j is :

$$\mathscr{L}\left(C_{jat}, C_{jmt}, C_{jst}; \eta_{j}\right) = \sum_{k=a,m,s} P_{jkt} C_{jkt} + \eta_{j} \left[1 - \delta_{k}^{1/\sigma} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_{k}}}\right)^{\frac{\sigma-1}{\sigma}}\right]$$
(A.7)

where η_j is the Lagrange multiplier. The first order conditions are given by :

$$\frac{\partial \mathcal{L}}{\partial C_{jkt}} = P_{jkt} - \eta_j \delta_k^{1/\sigma} \left(\frac{\sigma - 1}{\sigma}\right) \frac{C_{jt}^{\varepsilon_k}}{C_{jt}^{2\varepsilon_k}} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}}\right)^{-1/\sigma} = 0 \quad \forall k = a, m, s$$
 (A.8)

Then the price of the composite good in the sector k in the country j is given by :

$$P_{jkt} = \eta_j \left(\frac{\sigma - 1}{\sigma}\right) \frac{\delta_k^{1/\sigma}}{C_{jt}^{\varepsilon_k}} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}}\right)^{-\frac{1}{\sigma}}$$
(A.9)

And the expenditure in the consumption of the sector k final good is given by :

$$P_{jkt}C_{jkt} = \eta_j \left(\frac{\sigma - 1}{\sigma}\right) \delta_k^{1/\sigma} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}}\right)^{1 - \frac{1}{\sigma}} \quad \forall k$$
 (A.10)

Using the equation (A.10) and the utility function equation (??), the total expenditure $E_{jt} := \sum_{k=a,m,s} P_{jkt} C_{jkt}$ in the country j at time t is given by :

$$E_{jt} = \eta_j \left(\frac{\sigma - 1}{\sigma} \right) \tag{A.11}$$

The expression (A.9) of the price of the final good of the sector k can be rewriten as:

$$\frac{P_{jkt}}{E_{it}} = \delta_k^{1/\sigma} C_{jkt}^{-1/\sigma} C_{jt}^{\varepsilon_k \left(\frac{1}{\sigma} - 1\right)} \tag{A.12}$$

The the first order conditions imply that:

$$C_{jkt} = \delta_k \left(\frac{P_{kkt}}{E_{jt}}\right)^{-\sigma} C_{jt}^{\varepsilon_k(1-\sigma)} \quad \forall k = a, m, s$$
(A.13)

By rasing each of the equations (A.9) to the power $1 - \sigma$, then one obtains :

$$P_{jkt}^{1-\sigma} = \delta_k^{\frac{1-\sigma}{\sigma}} E_{jt}^{1-\sigma} C_{jt}^{(\sigma-1)\varepsilon_k} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}} \right)^{1-\frac{1}{\sigma}} \quad \forall k$$
 (A.14)

So

$$\delta_k P_{jkt}^{1-\sigma} C_{jt}^{(1-\sigma)\varepsilon_k} = E_{jt}^{1-\sigma} \delta_k^{\frac{1}{\sigma}} \left(\frac{C_{jkt}}{C_{jt}^{\varepsilon_k}} \right)^{1-\frac{1}{\sigma}} \quad \forall k = a, m, s$$
 (A.15)

By adding the equations (A.15), we obtain:

$$\sum_{k} \delta_k P_{jkt}^{1-\sigma} C_{jt}^{(1-\sigma)\varepsilon_k} = E_{jt}^{1-\sigma}$$
(A.16)

$$\Longrightarrow C_{jt}^{1-\sigma} \sum_{k} \delta_{k} P_{jkt}^{1-\sigma} C_{jt}^{(1-\sigma)(\varepsilon_{k}-1)} = E_{jt}^{1-\sigma}$$
(A.17)

By defining the aggregate price P_{jt} in the country j such that $P_{jt}C_{jt} = \sum_{k} P_{jkt}C_{jkt}$, we can deduce from the equation (A.17) the expression of P_{jt} as follow:

$$P_{jt} = \left[\sum_{n=a,m,s} \delta_n P_{jnt}^{1-\sigma} C_{jt}^{(1-\sigma)(\varepsilon_n - 1)} \right]^{\frac{1}{1-\sigma}}$$
(A.18)

From the equation (A.13) we can derive the demand for the composite good k in function of the aggregate consumption and aggregate price:

$$C_{jkt} = \delta_k \left(\frac{P_{jkt}}{P_{jt}}\right)^{-\sigma} C_{jt}^{\varepsilon_k(1-\sigma)+\sigma} \qquad \forall k = a, m, s$$
(A.19)

The expenditure share e_{jkt} of the sector k in the country j is :

$$e_{jkt} = \frac{P_{jkt}C_{jkt}}{P_{jt}C_{jt}}$$

$$= \delta_k \left(\frac{P_{jkt}}{P_{jt}}\right)^{1-\sigma} C_{jt}^{(1-\sigma)(\varepsilon_k - 1)} \qquad \forall k$$
(A.20)

$$\implies \frac{e_{jkt}}{e_{jmt}} = \frac{\delta_k}{\delta_m} \left(\frac{P_{jkt}}{P_{jmt}}\right)^{1-\sigma} \times \frac{C_{jt}^{(\varepsilon_k - 1)(1-\sigma)}}{C_{jt}^{(\varepsilon_m - 1)(1-\sigma)}}$$

$$= \frac{\delta_k}{\delta_m} \left(\frac{P_{jkt}}{P_{jmt}}\right)^{1-\sigma} C_{jt}^{(\varepsilon_k - \varepsilon_m)(1-\sigma)}$$
(A.21)

The equation (A.20) gives:

$$e_{jkt} = \delta_k \left(\frac{P_{jkt}}{E_{jt}C_{jt}^{-1}}\right)^{1-\sigma} C_{jt}^{(1-\sigma)(\varepsilon_k - 1)}$$

$$= \delta_k \left(\frac{P_{jkt}}{E_{jt}}\right)^{1-\sigma} C_{jt}^{(1-\sigma)\varepsilon_k} \quad \forall k = a, m, s$$
(A.22)

Hence,

$$C_{jt} = \left[\left(\frac{e_{jkt}}{\delta_k} \right)^{\frac{1}{1-\sigma}} \left(\frac{E_{jt}}{P_{jkt}} \right) \right]^{1/\varepsilon_k} \qquad k = a, m, s$$
 (A.23)

Then the equation (A.21) becomes:

$$\frac{e_{jkt}}{e_{jmt}} = \frac{\delta_k}{\delta_m} \left(\frac{P_{jkt}}{P_{jmt}}\right)^{1-\sigma} \left[\frac{E_{jt}}{P_{jmt}} \left(\frac{e_{jmt}}{\delta_m}\right)^{\frac{1}{1-\sigma}}\right]^{\frac{(1-\sigma)(\varepsilon_k - \varepsilon_m)}{\varepsilon_m}}$$

$$= \frac{\delta_k}{\delta_m} \left(\frac{P_{jkt}}{P_{jmt}}\right)^{1-\sigma} \left(\frac{e_{jmt}}{\delta_m}\right)^{\frac{\varepsilon_k}{\varepsilon_m} - 1} \left(\frac{E_{jt}}{P_{jmt}}\right)^{\frac{(1-\sigma)(\varepsilon_k - \varepsilon_m)}{\varepsilon_m}} \tag{A.24}$$

And the expenditure share is finally given by :

$$e_{jkt} = \delta_k \left(\frac{e_{jmt}}{\delta_m}\right)^{\frac{\varepsilon_k}{\varepsilon_m}} \left(\frac{P_{jkt}}{P_{jmt}}\right)^{1-\sigma} \left(\frac{E_{jt}}{P_{jmt}}\right)^{(1-\sigma)\left(\frac{\varepsilon_k}{\varepsilon_m}-1\right)}$$
(A.25)