

Analyzing Tooth growth through Statistical Inference

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Overview:

In this project we will analyse Tooth growth data using T-test to identify the different growth behaviour of Tooth under the effect of different doses and supp.

Loading data and analyzing summary statistics.

Here we load the data from ToothGrowth dataset in R and analyse the summary in the whole dataset as well as for the different doses and supp.

The summary for the 2 supplementary are:

##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	8.20	15.52	22.70	20.66	25.72	30.90
##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	4.20	11.20	16.50	16.96	23.10	33.90

The above summary illustrates that the mean for supplementary "OJ" is more than the mean growth with supplementary "VC". However the distribution with "VC" is more spread out and wider as compared to "OJ" as can be seen from max and min values from the respective statistics above.

The summary for the 3 doses are:

##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	4.200	7.225	9.850	10.600	12.250	21.500
##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	13.60	16.25	19.25	19.74	23.38	27.30
##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	18.50	23.52	25.95	26.10	27.83	33.90

The above summary illustrates that the mean Tooth growth increases across doses 0.5, 1 and 2 with minimum when dose 0.5 is administered and maximum when dose 2 is administered.

Hypothesis testing for growth with different supplementaries.

Here we apply t test to identify if the difference in Tooth growth under the effect of the 2 different supplementaries "oj" and "VC" are statistically different at 95% confidence level.

Assumption: Variances for the two datasets given different supplements are unequal and the datasets are not paired.

Lets formulate the below hypothesis:

H0 : There is no significant change in growth when supplement "OJ" over "VC".

H1 : There is a significant change in growth in the 95% confidence when supplement "OJ" is adminisitered over "VC".

The T test summary is:

```
##
##  Welch Two Sample t-test
##
## data:  len by supp
## t = 1.9153, df = 55.309, p-value = 0.06063
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  -0.1710156  7.5710156
## sample estimates:
## mean in group OJ mean in group VC
##           20.66333           16.96333
```

The summary shows that T value for the sample is lower the T-statistic at 95% given by 2.0038004. Hence the null hypothesis H0 cannot be rejected. This conclusion is further strengthened by the p-value statistics which is more than 0.05 and suggests that null hypothesis cannot be rejected t 95% confidence level. Hence There is no significant change in growth when supplement "OJ" is administered over "VC".

Hypothesis testing for growth with different doses.

Here we apply t test to identify if the difference in Tooth growth under the effect of the 3 different doses "0.5", "1" and "2" are statistically different at 95% confidence level.

Assumption: Variances for the 3 datasets given different doses are unequal and the datasets are not paired.

Lets formulate the below hypothesis:

H0 : There is no significant change in growth for the 3 different doses "0.5", "1" and "2".

H1 : There is a significant change in growth in the 95% confidence when dose "1" is adminisitered over "0.5".

H2 : There is a significant change in growth in the 95% confidence when dose "2" is adminisitered over "0.5".

H3 : There is a significant change in growth in the 95% confidence when dose "2" is adminisitered over "1".

The T test summary for H1:

```
##
##  Welch Two Sample t-test
##
## data:  len by dose
## t = -6.4766, df = 37.986, p-value = 1.268e-07
## alternative hypothesis: true difference in means is not equal to 0
```

```
## 95 percent confidence interval:
##  -11.983781  -6.276219
## sample estimates:
## mean in group 0.5    mean in group 1
##           10.605           19.735
```

The summary shows that the absolute T value for the sample is higher the T-statistic at 95% given by 2.0245696. Hence the null hypothesis H_0 can be rejected. This conclusion is further strengthened by the p-value statistics which is less than 0.05 and suggests that null hypothesis can be rejected at 95% confidence level. Hence There is a significant change in growth in the 95% confidence when dose "1" is administered over "0.5".

The T test summary for H_2 :

```
##
##  Welch Two Sample t-test
##
## data:  len by dose
## t = -11.799, df = 36.883, p-value = 4.398e-14
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  -18.15617 -12.83383
## sample estimates:
## mean in group 0.5    mean in group 2
##           10.605           26.100
```

The summary shows that the absolute T value for the sample is higher the T-statistic at 95% given by 2.0263778. Hence the null hypothesis H_0 can be rejected. This conclusion is further strengthened by the p-value statistics which is less than 0.05 and suggests that null hypothesis can be rejected at 95% confidence level. Hence There is a significant change in growth in the 95% confidence when dose "2" is administered over "0.5".

The T test summary for H_3 :

```
##
##  Welch Two Sample t-test
##
## data:  len by dose
## t = -4.9005, df = 37.101, p-value = 1.906e-05
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  -8.996481 -3.733519
## sample estimates:
## mean in group 1 mean in group 2
##           19.735           26.100
```

The summary shows that the absolute T value for the sample is higher the T-statistic at 95% given by 2.0260081. Hence the null hypothesis H_0 can be rejected. This conclusion is further strengthened by the p-value statistics which is less than 0.05 and suggests that null hypothesis can be rejected at 95% confidence level. Hence There is a significant change in growth in the 95% confidence when dose "2" is administered over "1".