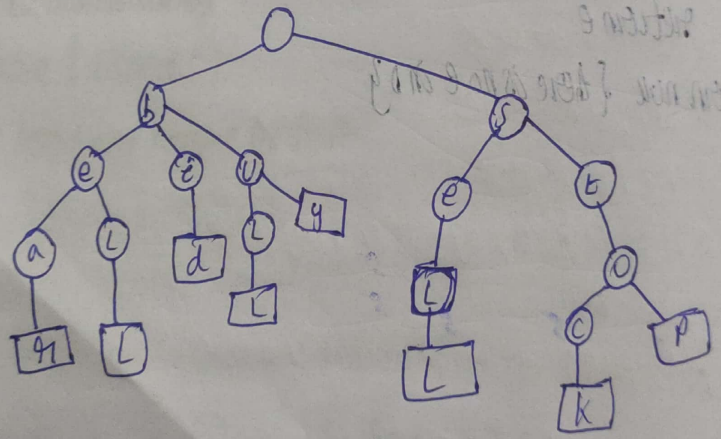
UNIT-4

Text processing: String Operations, Brute-force Pattern matching. The boyer moore Algorithm, The Knuth-Morris Pratt Algorithm Standard tries, compressed tries, suffix tries, Huffman coding algorithm, the longest subsequence problem (LCS), Applying dynamic programming to the LCS problem.

TRIE:

A data structure for storing a set of strings (Name from the word "retrieval"):



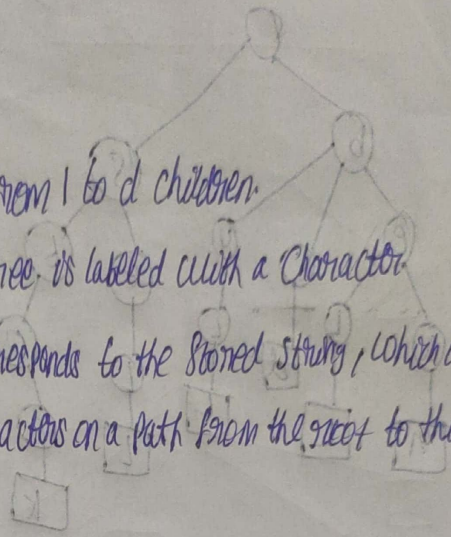
PROPERTIES OF TRIE:

(1) Multiway tree

(2) Each node has from 1 to d children.

(3) Each edge of the tree is labeled with a character.

(4) Each leaf node corresponds to the stored string, which is a concatenation of characters on a path from the root to this node.



TYPES OF TRIE:

(1) Standard trie

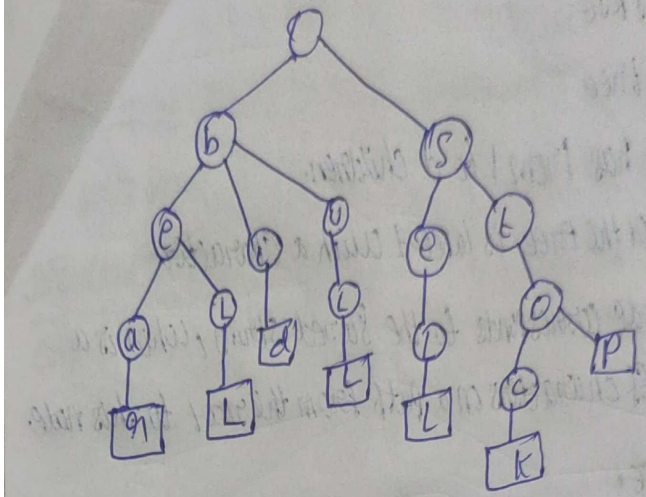
(2) Compressed trie

(3) Suffix trie

STANDARD TRIE:

1. Each node but the root is labelled with a character
2. The children of a node are alphabetically ordered.
3. The paths from the external nodes to the root yield the strings of S.
4. Example: Standard trie for the set of strings S

$S = \{$ bear, bell, bid, bull, buy, sell, stock, stop$\}$



→ Standard trie uses O(n) space. Operations (find, insert, remove) take time O(dm) each, where:

n - total size of strings in S

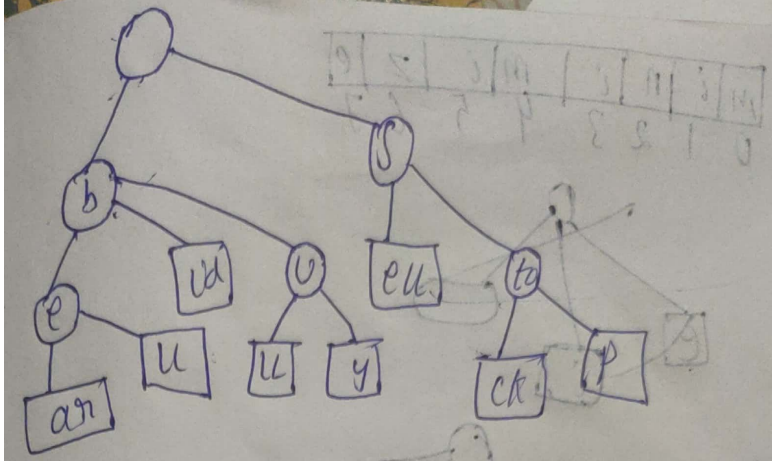
d - alphabet size

m - size of the string parameter of the operation

Compressed tries:

(1) Trie with nodes of degree atleast 2

(2) Obtained from standard trie by compressing the chains of redundant blocks



A compressed trie can be stored in space $O(S)$ where $S = \sum |s|$ by using $O(1)$

SUFFIX TRIE:

(1) A suffix trie is a compressed trie for all the suffixes of a text.

(2) The suffix trie for a text X of size n from an alphabet of size d.

(3) suffix tries stores all the $n(n-1)/2$ suffixes of X in $O(n)$ space.

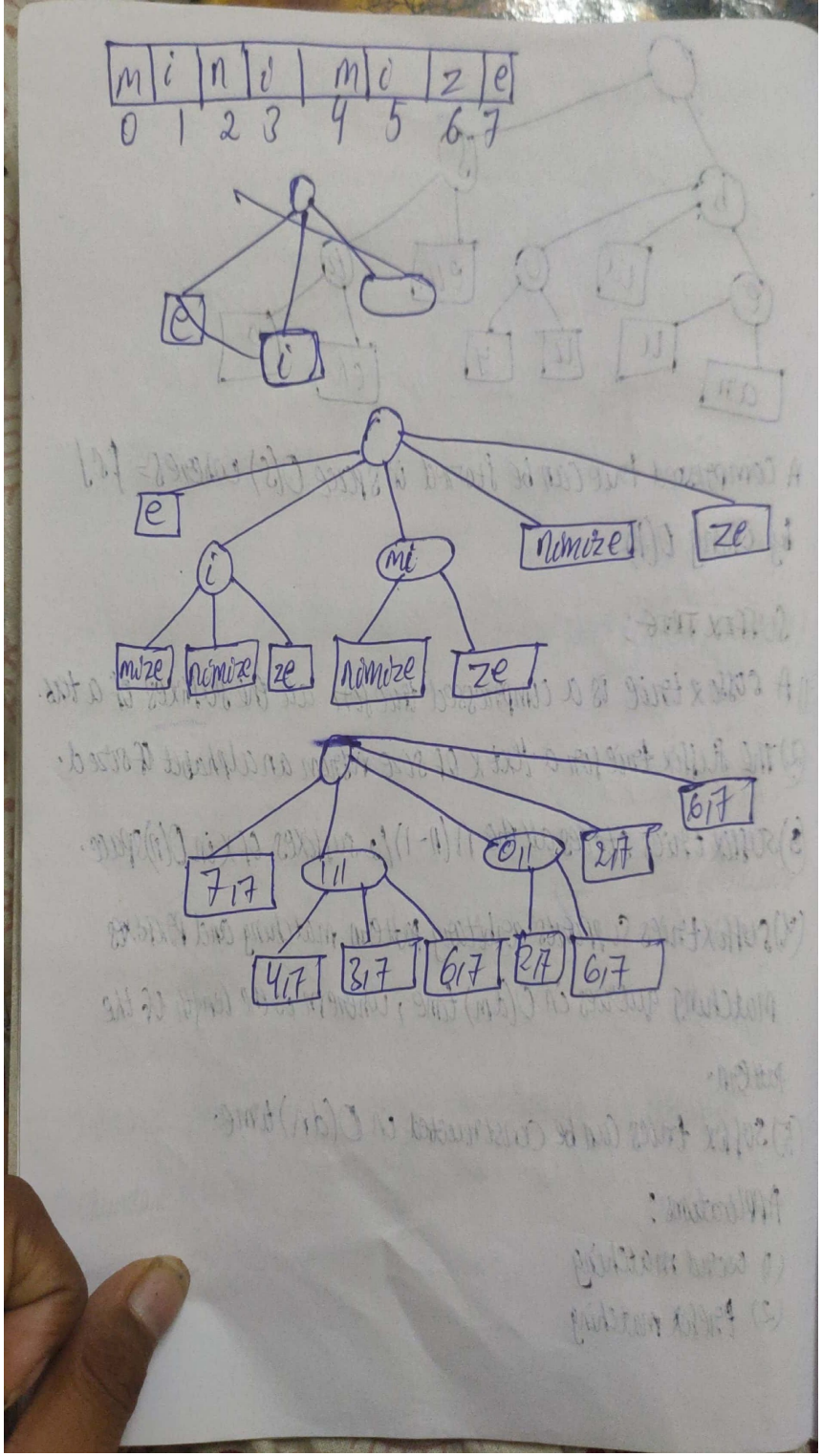
(4) suffix tries supports arbitary pattern matching and prefixes matching queries in $O(dm)$ time, where m is the length of the pattern.

(5) suffix tries can be constructed in $O(dn)$ time.

Applications:

(1) word matching

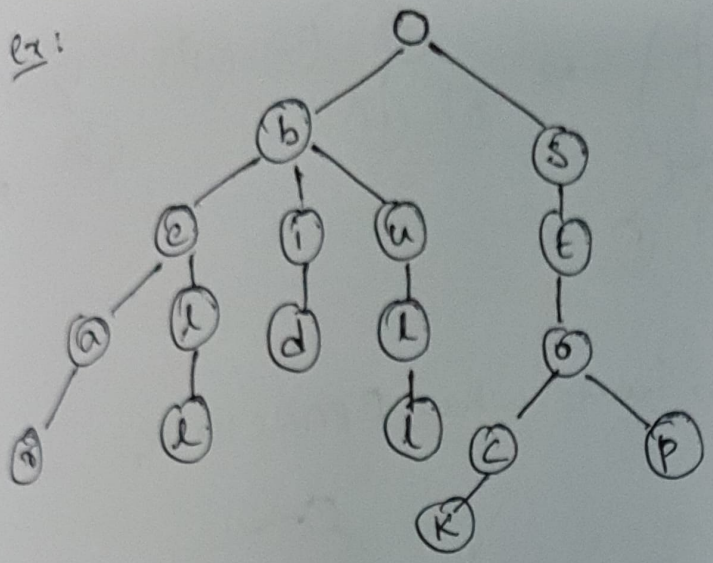
(2) prefix matching



Standard Trie:

In standard trie no word in s should be the prefix of other.

ex:



→ class Node {

```
Node[] children = new node[26];
// to check for end of string
boolean isWordEnd;
```

}

→ It is an ordered tree like data structure

→ Each node (except the root node) is a standard trie is labeled with a character.

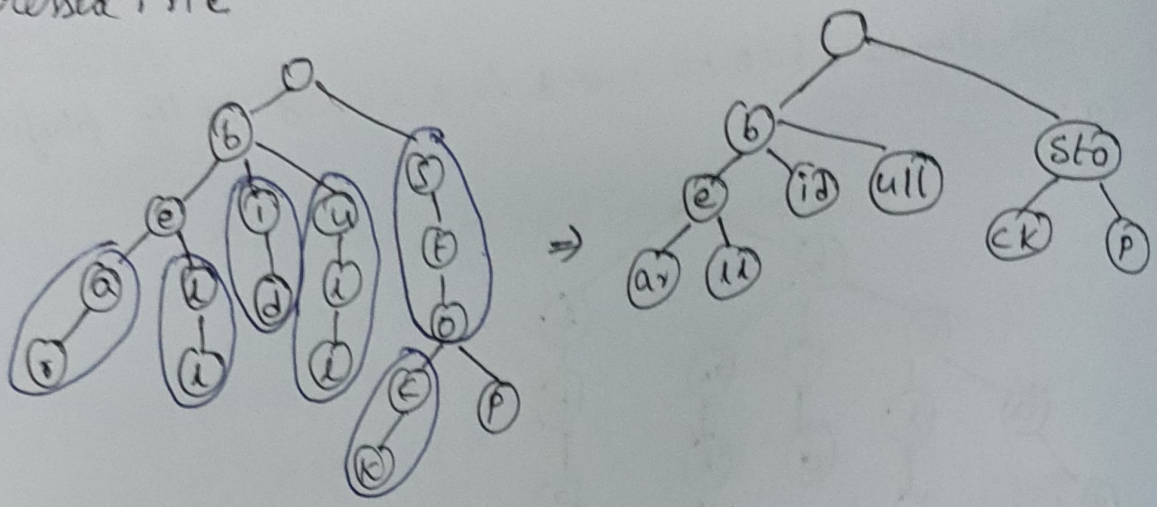
→ The children of a node are in alphabetical order.

→ Each node or branch represents a possible character of keys or words.

→ Each node or branch may have multiple branches.

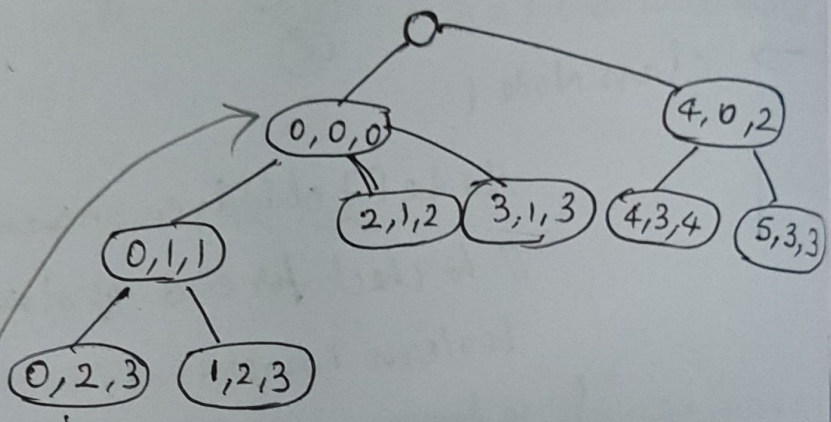
→ The last node of every key or word is used to mark the end of word or node.

Compressed Trie



NOTE: only add a new node when BRANCHING

i	0	1	2	3	4
s[0] =	b	e	a	r	
s[1] =	b	e	l	l	
s[2] =	b	i	d		
s[3] =	b	u	l	l	
s[4]	s	t	o	c	k
s[5] =	s	t	o	p	



Node (i, j, k)

i - index of S

j - start

k - end

Suffix ~~Node~~ Trie:

Ex: Minimize

Suffixes:

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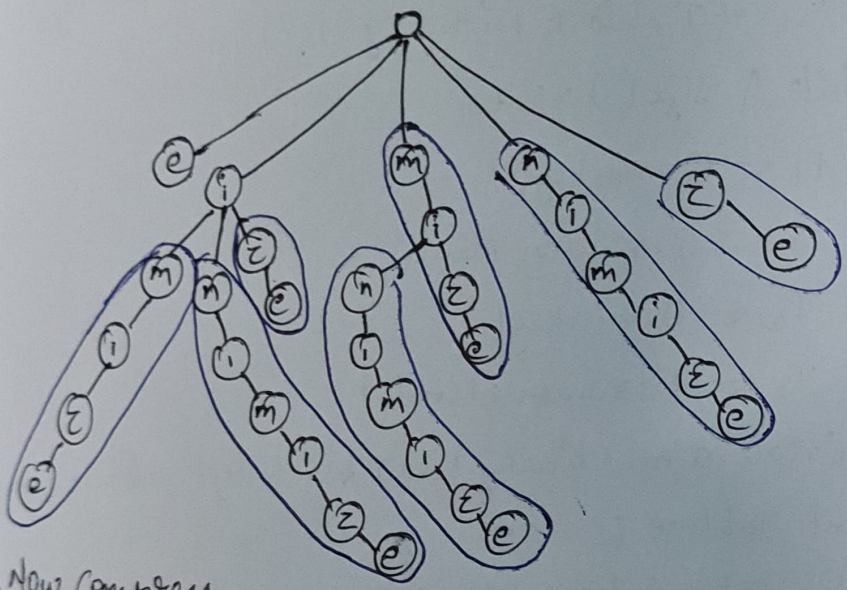
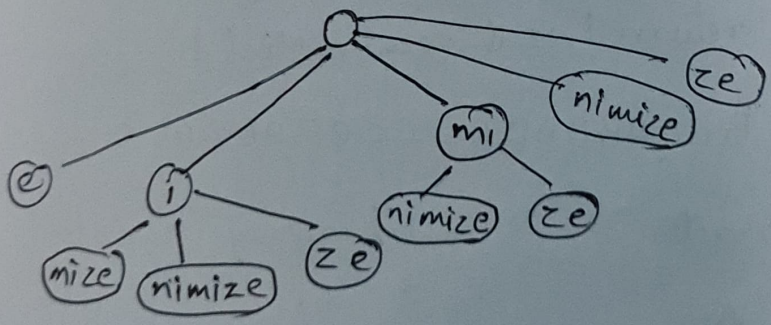
inimize
Minimize

S



→ Now Compress



0 1 2 3 4 5 6 7
minimize