

# SM Assignment

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DSS

Define Sign Test : Explain sign Test procedure ?

- (Q) Define Sign Test : Explain sign Test procedure ?
- Ans: (i) The sign test is the simplest form of the non-parametric test.
- (ii) Its name comes from the fact that, it is based on direction ('-' or '+' sign) based on the observations.
- (iii) In any problem of sign test, we count the

- (i) Number of positive signs
- (ii) Number of negative signs
- (iii) Number of zero's present

We take  $H_0: p=0$  (Null hypotheses)

The difference is a chance, effect the probability of a positive sign, for any particular pair is  $\frac{1}{2}$  as the probability of a -ve sign.

If 's' is the number of times the number of time the frequency sign occurs then 's' is the binomial distribution with  $p = \frac{1}{2}$

The critical value for a two sided alternative when,  $\alpha = 0.05$ , can be

conveniently found by the expression -

$$P(Z) = \frac{(n-1)}{2} = (0.98) \sqrt{n}$$

Then the sign test is classified into two types.

1) One sample sign test

2) Paired Sample sign test

One Sample Sign Test: In one sample sign test, we test the null hypothesis ( $H_0$ ) against an appropriate alternative based on a random sample of size  $n$ . We replace each sample value greater than  $M_0$  with a positive sign and each sample value less than  $M_0$  with a negative sign. And a discarded sample value exactly equal to other sample value (put 0).

Then the null Hypothesis ( $H_0$ ) is testing for the '+' & '-' signs of a random variable following a binomial distribution with  $P = 1/2$  or not.

Paired Sample Sign Test: 12202160109

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- Paired

  - ④ This test is again a very important application problems, involving paired data such as data related to the collections receivable before & after a new collection policy.
  - ⑤ In these problems each pair of sample value, can be replaced with a '+' sign if the first value is greater than the second & with a '-' sign if the first value is smaller than the second value or discarded with if both are equal.

Q2) Define Mann-Whitney U Test?

Explain the procedure for Mann-Whitney U test.

Ans- Mann - Whitney U Test

It belongs to the family of Rank sum test family. With this test we can test the null hypothesis  $H_0 = H_1$  without assuming whether the population sample has roughly the shape of a normal distribution.

The test of null hypothesis is that these two samples come from should be of identical populations

maybe based on  $R_1$  (sum of sample ranks) and  $R_2$  (sum of sample 2 ranks)

It may be noted that, in practice it doesn't matter which sample we call sample 1 & sample 2 respectively.

The sample sizes are taken as  $n_1, n_2$  and sum of the samples are taken as  $R_1, R_2$ . Simply the sum of  $n_1$  &  $n_2$  positive integers which is known to be  $\frac{(n_1+n_2)(n_1+n_2+1)}{2}$

This formula enables to find  $R_2$  if we know & vice versa.

It is an alternative test for two sample test t-test. The decision was based on  $R_1$  &  $R_2$ . Now the decision will be based upon either of the relative statistics:

$$U_1 = n_1 n_2 + \frac{n_1(n_1+1)}{2} - R_1$$

$$U_2 = n_1 n_2 + \frac{n_2(n_2+1)}{2} - R_2$$

Q3 The coin or 10000 of certain basketball team for their last 50 consecutive games were as follows.

WWWLWWL L WWWWWWL WL  
 WWWWL LL WWWWL WWWLL  
 WWWWWWWL WL WW WL LL WL WWW

$$\text{Ans: } n_1 = 36$$

$$n_2 = 14$$

$\lambda_1 = 19$  (total number of runs)

$$\sigma = \sqrt{\frac{2 \times n_1 n_2 (2n_1 n_2 - n_1 - n_2)}{(n_1 + n_2)^2 * (n_1 + n_2 - 1)}} = 2.8071$$

$$M = \frac{2n_1 n_2}{n_1 + n_2} + 1$$

$$Z = \frac{\lambda_1 - M}{\sigma}$$

$$\lambda_1 = \frac{2(36)(14)}{36+14}$$

$$= -0.77$$

$$M = \frac{529}{25} = 21.16$$

$$|Z| = 0.77$$

As  $Z_{\text{cal}} < Z_{\text{tab}}$  at 5% level of significance (1.96)  
 $0.77 < 1.96$

Hence, we accept  $H_0$ . Thus, there is no real evidence to suggest that the evidence is random.

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Q4) The following data relate to the daily production of cement. (in metric tonnes) a large point plant for 30 days.

11.5, 10.0, 11.2, 10.0, 12.3, 11.1, 10.2,  
 9.6, 8.7, 9.3, 9.3, 10.7, 11.3, 10.4, 11.4, 12.3,  
 11.4, 10.2, 11.6, 9.5, 10.8, 11.9, 12.4, 9.4  
 10.5, 11.6, 9.3, 10.4, 11.5

Use sign test to test the null hypothesis that plants average daily production of cement is 11.2 metric tonnes against alternative hypothesis  $H_1 < 11.2$  metric tonnes at 5% level. Average = 11.2

$$> 11.2 (+ve sign) \quad < 11.2 (-ve sign) \\ = 11.2 \Rightarrow 0$$

No. of Days	Production of cement (in tones)	Sign.
1	11.5	+
2	10.0	-
3	11.2	0
4	10.0	-
5	12.3	+
6	11.1	-
7	10.2	-
8	9.6	-

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9	8.7	-
10	9.3	-
11	9.3	-
12	10.7	-
13	10.3	+
14	10.4	-
15	11.4	+
16	12.3	+
17	11.4	+
18	10.2	-
19	11.6	+
20	9.5	-
21	10.8	-
22	12.4	+
23	9.6	-
24	10.5	-
25	11.6	+
26	8.3	-
27	9.3	-
28	10.4	-
29	11.5	+

number of the signs = 11

number of -ve signs = 18

no. of zeros = 1

$$x = 5 = 11$$
$$n = 18 + 11 = 29$$

$$p = k = 0.5 \quad q = 1-p = 1-k = 0.5$$

$$Z = \frac{x - np}{\sqrt{npq}}$$

$$= \frac{11 - 39 * (\frac{1}{2})}{\sqrt{29 * (\frac{1}{2})(\frac{1}{2})}}$$

$$= \frac{-3.5}{\sqrt{29 * (\frac{1}{4})}}$$

$$Z = -1.299$$

$$= 1.30$$

$H_0: \mu \geq 11.2$  for  $Z$  tab at 5% level  
of significance for L.T. Table value

$$z_{tab} = -1.64$$

$$Z_{cal} = -1.29 \quad Z_{tab} = -1.64$$

$$Z_{cal} > Z_{tab}$$

Hence, we reject  $H_0$  Null hypothesis, i.e., plant average production is less than 11.2 metric tonnes.

Q4  
12/2021/16 Day  
85) Explain ratio to trend method?

Ans: This method is an improvement over the simple average method, and is based on the assumption that seasonal variation for any given month is a constant factor of trend. The measurement of seasonal variation by this method consists of various steps:

1. Compute the trend values by the principle of the least square by fitting an appropriate mathematical curve.
2. Express the original data as the principle of trend values. Assuming the multiplicative model, these percentages will therefore will contain seasonal, cyclic specific values.
3. The cyclic & irregular components are then wiped out by averaging the percentages for different months. If the data is monthly, this leaves us with an indices of seasonal variations. Either Arithmetic mean (or) Median can be used, but median

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is preferred as mean or median can be used but median is preferred as mean to AM since later gives a undue weightage to extreme values, which are primarily due to seasonal swings if there are a few abnormal values, modified mean can be used with advantage.

4. Finally, these indices, obtained in step 3, are adjusted to a total of 1200, for monthly data or 400 for a quarterly data by multiplying them through by a constant 'k'

$$k = \frac{1200}{\text{Total of Indices}} \quad \& \quad k = \frac{400}{\text{Total of Indices}}$$

Q) Explain Link Relative Method.

Ans- This method is also known as Pearson's method, is based on the averaging of the link relatives. Link relative is the values of one season expressed as a percentage. Here season refers to 'time-period' it would mean monthly data.

$$\text{Link relative for any month} = \frac{\text{current month's value}}{\text{previous month's value}} \times 100$$

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The steps involved may be summarized as follows:

1. Convert the original data, into link relatives using the above formula.
2. Convert the average (Mean or Median) link relatives for each month of the data are monthly. Mean or median can be used for averaging.
3. As in the case of 'ratio to trend' method average the link relatives for each month of the monthly data.

Chain Reaction (C.R) for any season is obtained by multiplying the chain relative of the preceding season & dividing by 100.

$$\text{C.R for any season} = \frac{(\text{C.R of that season})}{(\text{C.R of preceding season})} \times 100$$

Thus for monthly data, the chain relative to first month.

4. Thus the adjustment is done by subtracting correlation factor from each chain relative.

$d = \frac{1}{12} [ \text{second (NEW)} \text{ C.R. for Jan} + \dots ]$  12202160609  
 then assuming linear method trend,  
 the correlation for Feb, March ... Dec  
 $a, d, 2d, \dots, 11d$  respectively

5. Finally adjust the corrected chain  
 to total by expressing the corrected  
 chain relatives as percentage of  
 arithmetic Mean. The resultant  
 gives the adjusted monthly indices  
 of seasonal variables.

Q7) In a certain Industry the production  
 of certain commodity during 2004-  
 2011 is given as:

Year	2004	2005	2006	2007	2008	2009
Production	666	849	886	780	968	1052
2010		2011	2013	2014	2015	
93.2		116.6	88.3	117.0	115.2	

(1) The trend value from 2004-2015.  
 Estimate production of the commodity  
 during the years 2015, 2016 if present  
 trend continues

Year	$y_t$	$x$	$x \cdot y_t$	$x^2$	$\log y_t$
2004	66.5	-5	-333	25	
2005	84.9	-4	-339.6	16	
2006	88.6	-3	-265.8	9	
2007	78.9	-2	-156	4	
2008	96.8	-1	-96.8	1	
2009	105.2	0	0	0	
2010	93.2	1	93.2	1	
2011	111.6	2	223.2	4	
2012	88.3	3	264.9	9	
2013	117.0	4	468	16	
2014	115.2	5	576	25	
	<u>1045.4</u>		<u>43.1</u>	<u>135</u>	

The normal equation can be written as:-

$$\sum y = na + b \sum t$$

$$\sum t \cdot y = a \sum t + b \sum t^2$$

We shift the origin to middle trial period, 2009. let  $x = t - 2009$

then least square of line  $y_t$ .

$$y_t = a + bx$$

## Normal equations

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$$\sum y_t = n a + b \sum x - \textcircled{2}$$

$$\sum x \cdot y_t = a \sum x + b \sum x^2 - \textcircled{3}$$

$$1045.4 = 11a + b(0)$$

$$434.1 = a(0) + b(135)$$

$$1045.4 = 11a \Rightarrow a = \frac{1045.4}{11} = 95.0364$$

$$434.1 = 135b \Rightarrow b = \frac{434.1}{135} = 3.2155$$

The straight in eq<sup>n</sup>

$$Y_t = 95.0364 + 3.2155 x$$

$$Y_E = 95.3044 -$$

$$= 79.2508$$

$$= 83.1972$$

$$= 91.09$$

$$= 102.9292$$

Production in the year 2015 & 2016

for the year 2015

$$Y_t = 95.0364 + 3.2155 (t-2009)$$

$$= 95.0364 + 3.2155 (6)$$

$$= 108.1143297$$

Similarly for 2016

$$\begin{aligned}y_t &= 95.0364 + 3.2155 (t - 2009) \\&= 95.0364 + 3.2155 (2016 - 2009) \\&= 95.0364 + 3.2155 (7) \\&= 117.54525\end{aligned}$$