

$LCS[i:j] = 1 + LCS[i-1:j-1]$

else

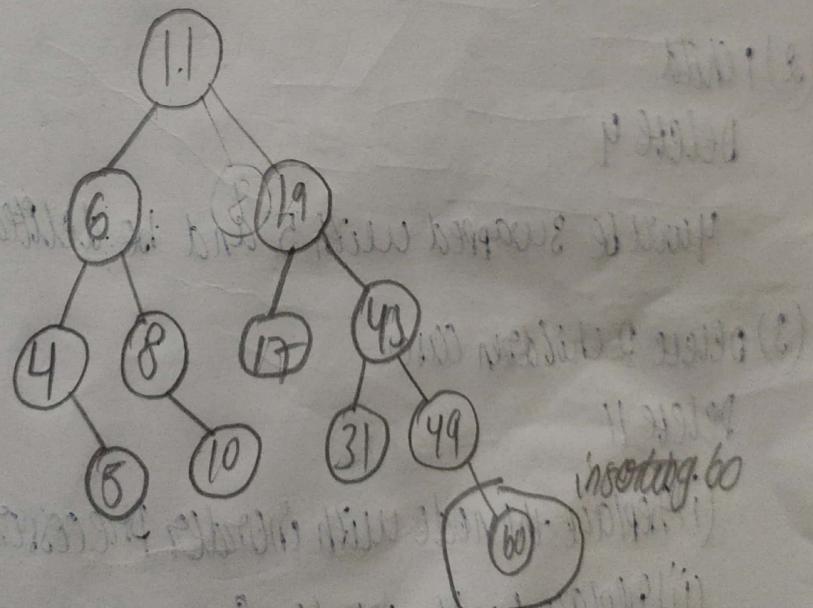
$LCS[i:j] = \max(LCS[i-1:j], LCS[i:j-1])$

UNIT-3

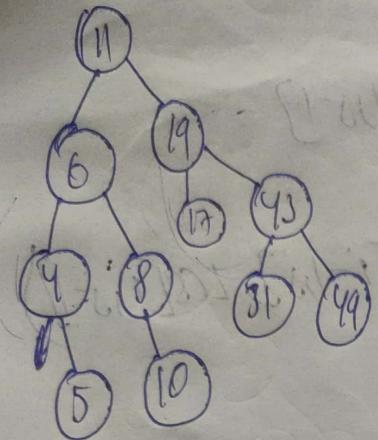
BINARY SEARCH TREE:

→ atmost 2 child nodes

11 6 8 19 4 10 5 17 43 49 31



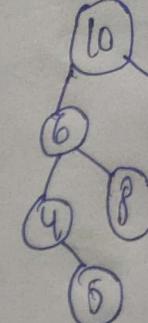
DELETION:



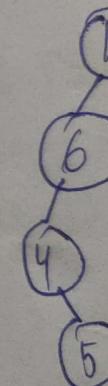
deletion:

- (1) 0 child
- (2) 1 child
- (3) 2 child

Inorder predecessor
the largest el



Inorder successor
the smallest



- (1) 0 child

Delete 31

- (i) simply delete the node

- (2) 1 child

Delete 4

4 will be swapped with 5 and be deleted

- (3) Delete 2 children cases

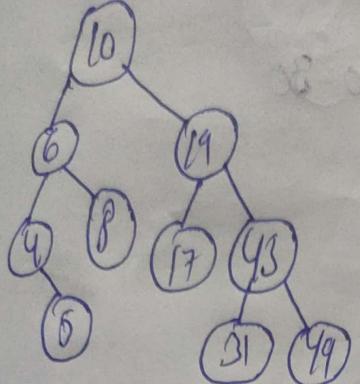
Delete 11

- (i) replace the node with inorder predecessor
- (ii) replace with inorder successor

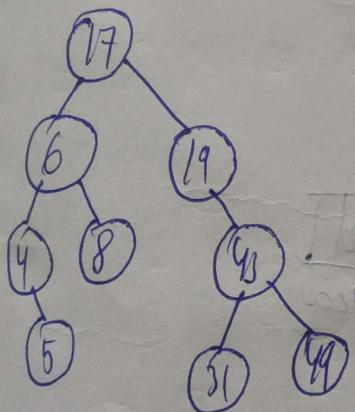
SEARCH:

- (1) key
- (2) ke

Inorder predecessor:
the largest element from left subtree



Inorder successor:
the smallest element from right subtree



Search:

① key == Root

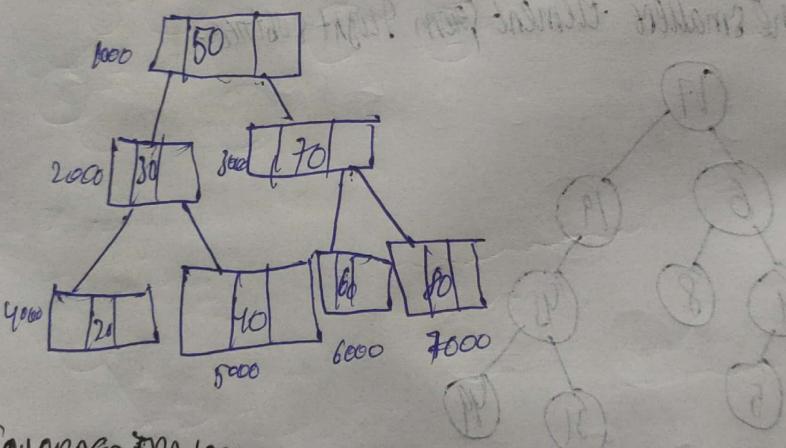
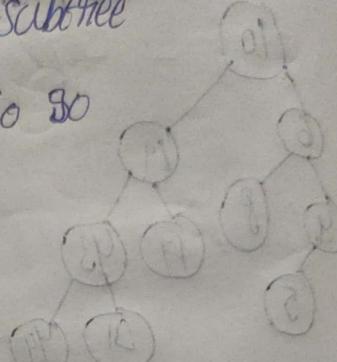
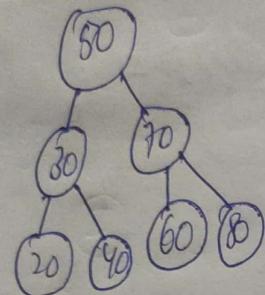
② key < Root

Search space - left subtree

① Key > root

Search space - Right Subtree

50 80 20 40 60 80



INORDER TRAVERSAL:

chorder (root → left)

display (root → data)

chorder (root → right)

PRE ORDER

display (root →

preorder (root →

pre order (root →

post order TRAVERSAL

postorder (root →

postorder (root →

display (root →

AVL trees:

1. It is a BST.

2. Height of left

$$= \{-1, 0, 1\}$$

L7

3. No duplicate

After insertion

PREORDER:

display (root → data)

preorder (root → left)

postorder (root → right)

POST ORDER TRAVERSAL

postorder (root → left)

postorder (root → right)

display (root → data)

AVL Trees:

1. It is a BST

2. Height of left subtree - height of right subtree

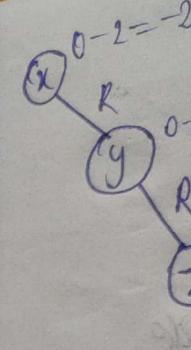
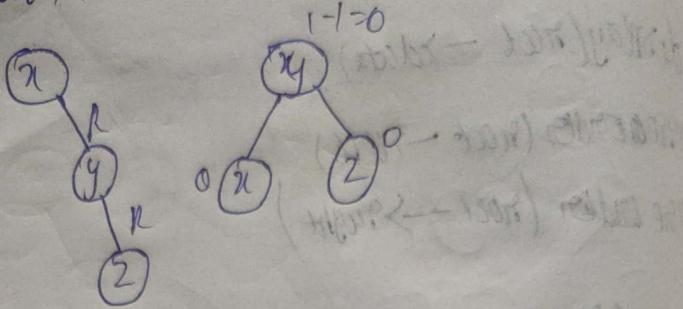
= {-1, 0, 1} for each node

↳ Balance Factor

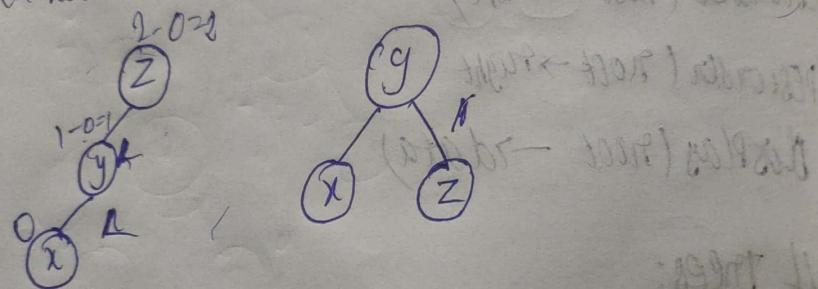
3. No duplicate elements

After insertion, balance factor can be found

LL Rotation:



RR Rotation:

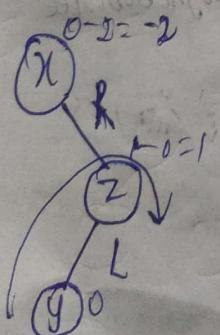


④ LR Rotat

z, x, y



⑤ x, z, y RL Rotation



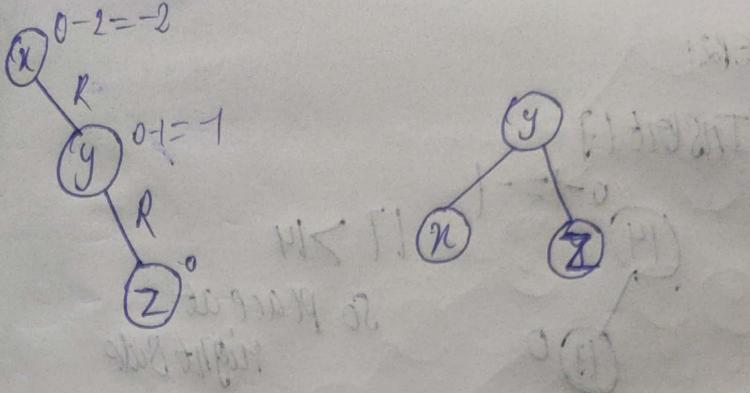
Right rotation for z and y selected, note 2nd part

AVL Inse

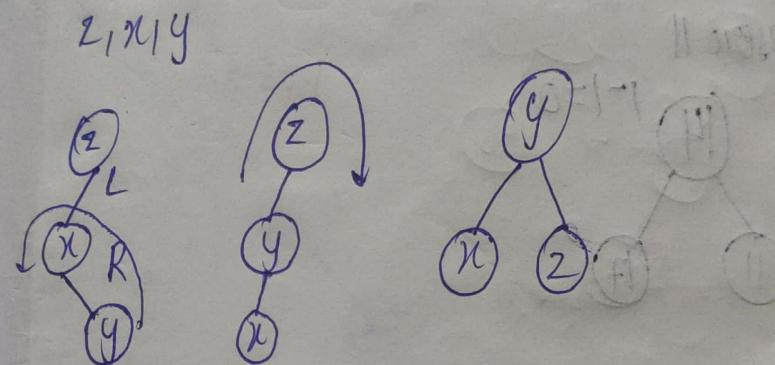
14, 17, 11

STEP I:

I Insert



④ LR rotation:



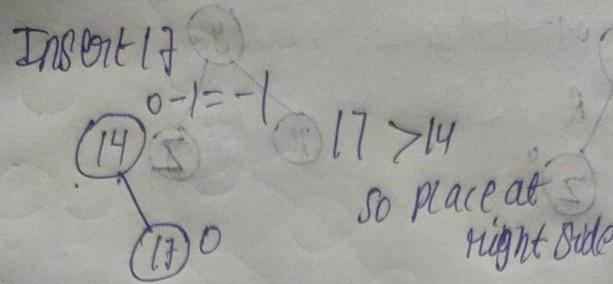
AVL INSERTION

14, 17, 11, 7, 63, 14, 13, 12, 8, 60, 19, 16, 20

STEP 1:

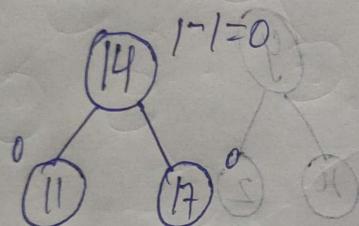
Insert 14
⑯ → Balance factor = $0-0=0$

Step 2:



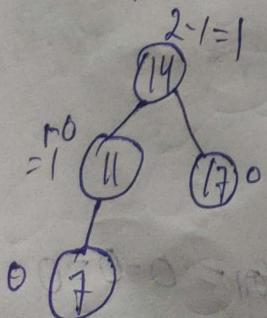
Step 3:

Insert 11

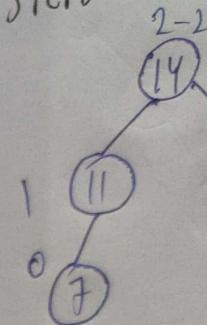


Step 4:

Insert 7

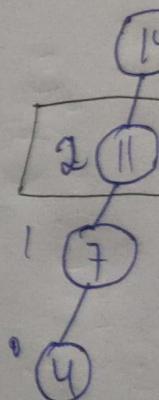


Step 5:



Step 6:

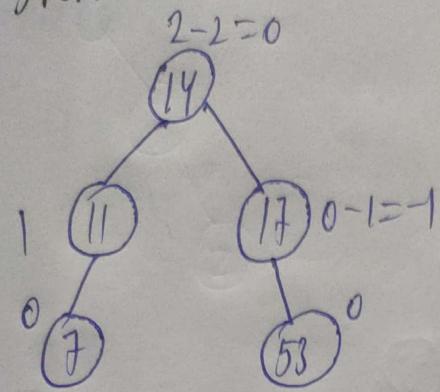
Insert 4



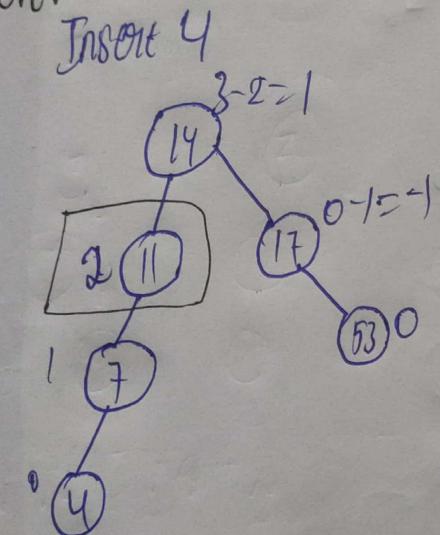
node 11 os

As it os

STEP5:

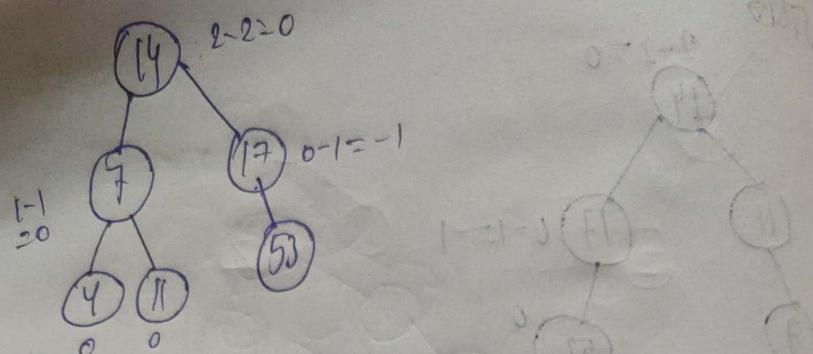


STEP6:

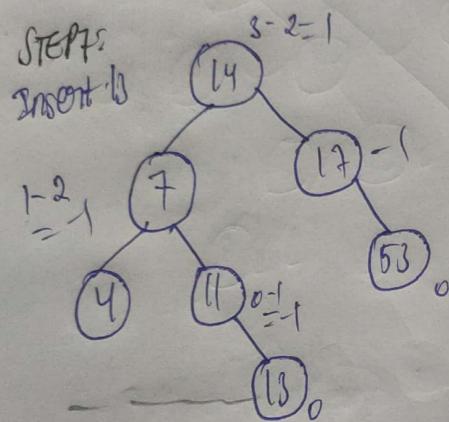


node 11 is critical

As it is LL form then right rotation is then

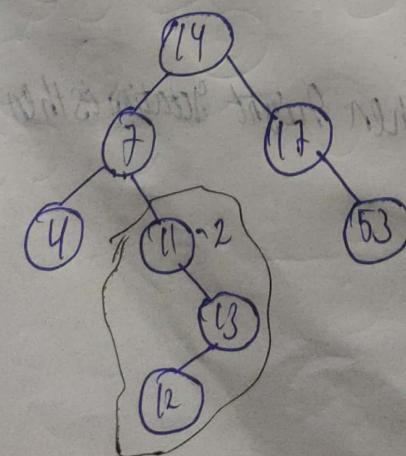


STEP 7:
Insert 13

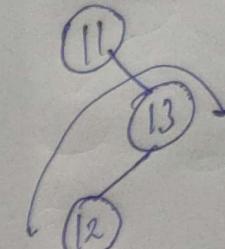


STEP 8:

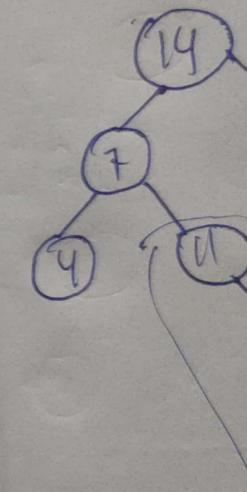
Insert 12



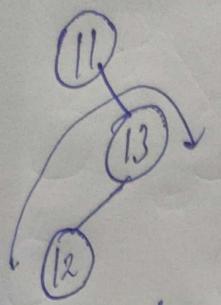
Note as critical node



RL notation
(i) right rotate

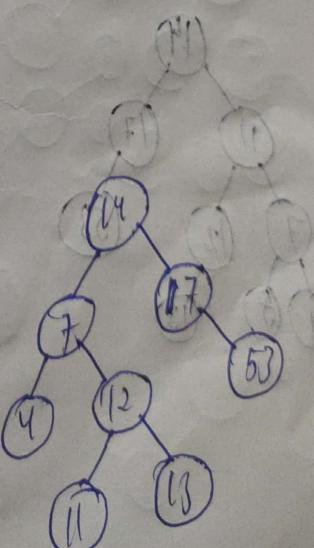
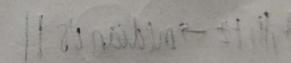
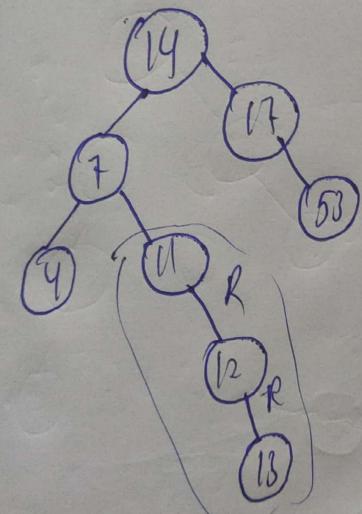


Node is critical node



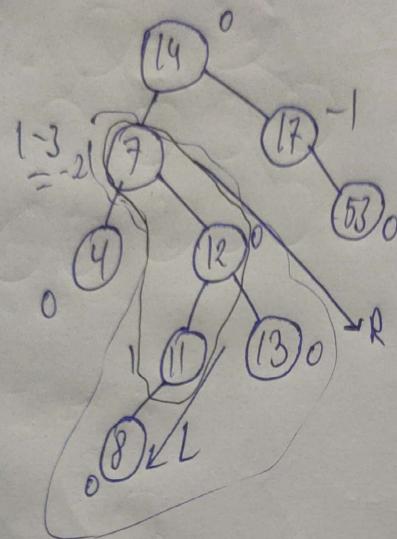
RL notation

(i) Right Rotation

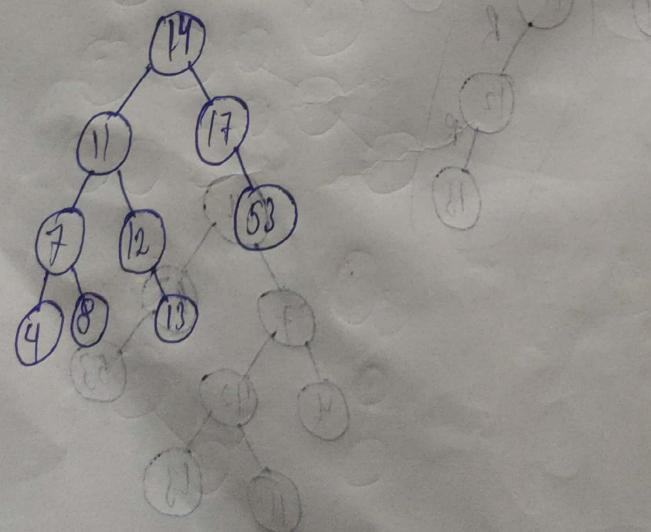


Step 9:

Insert 8

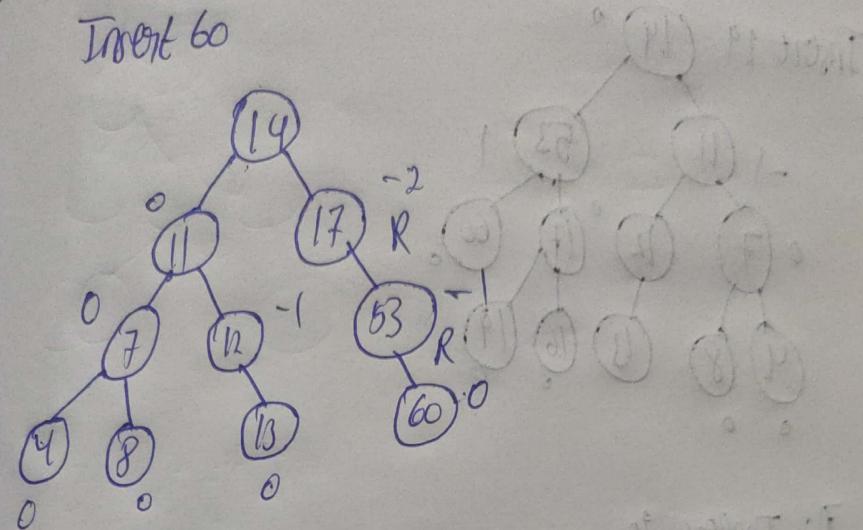


7, 11, 12 → median is 11



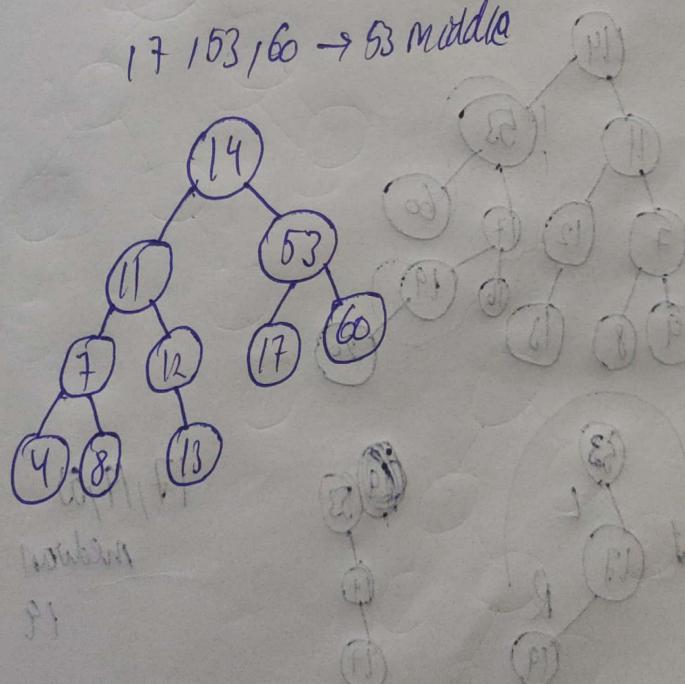
STEP 10

Insert 60

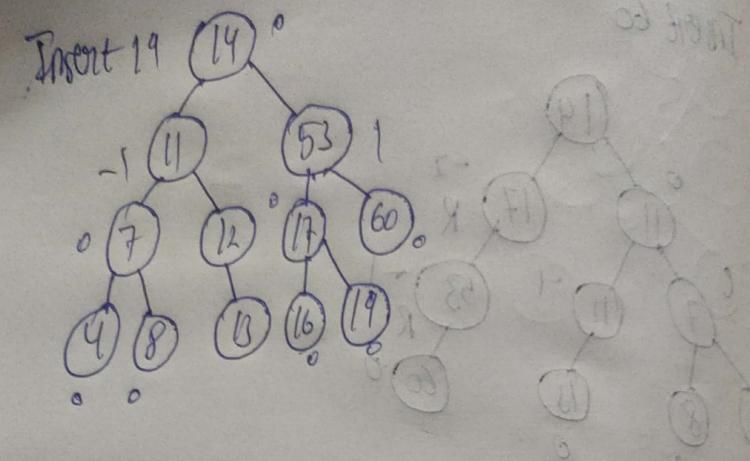


RR Rotation allows

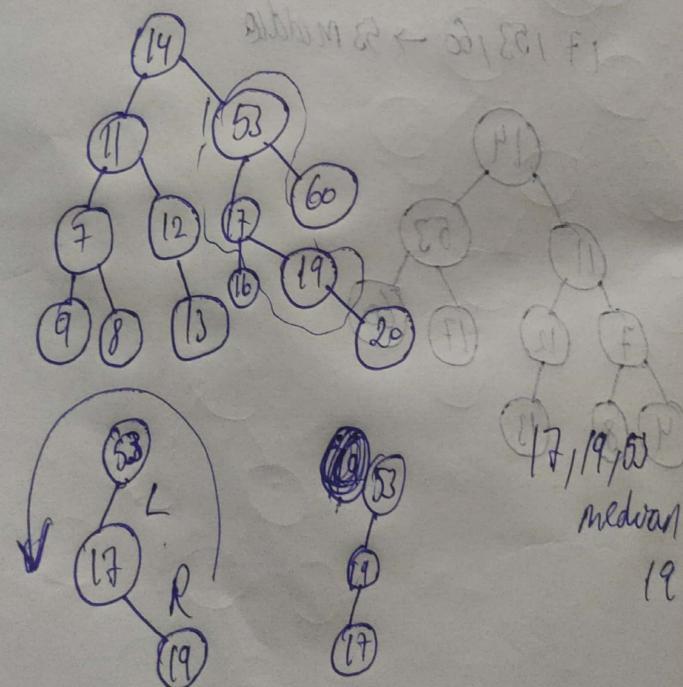
17 153, 60 → 53 middle

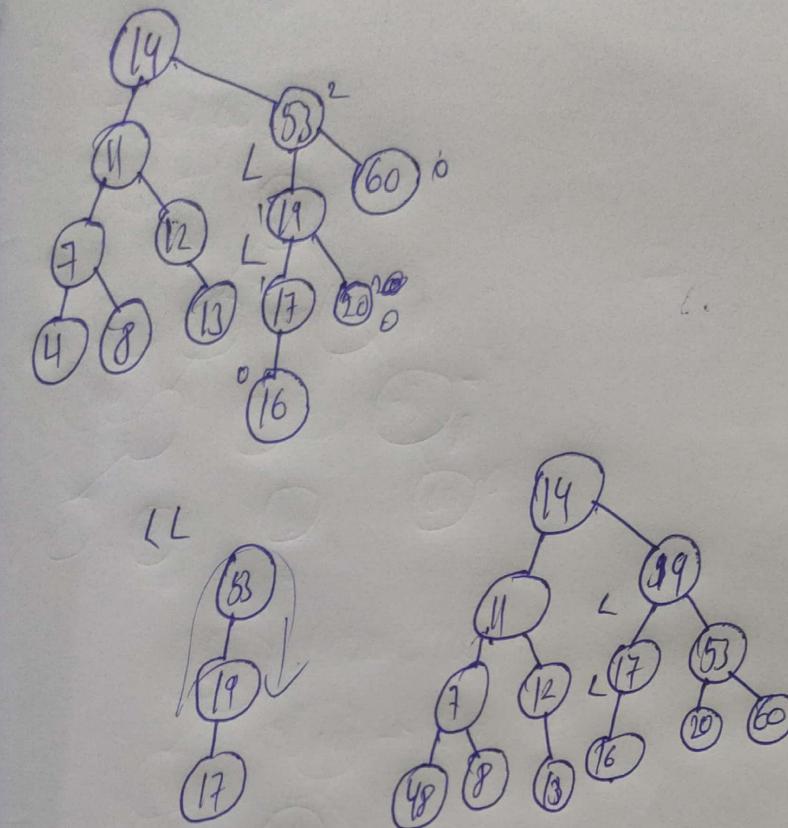


STEP II:



D. Ingert 20





AVL DELETION: