

# Today in Cryptography (5830)

Review of modes of operation & active attacks

Message authentication

CBC-MAC

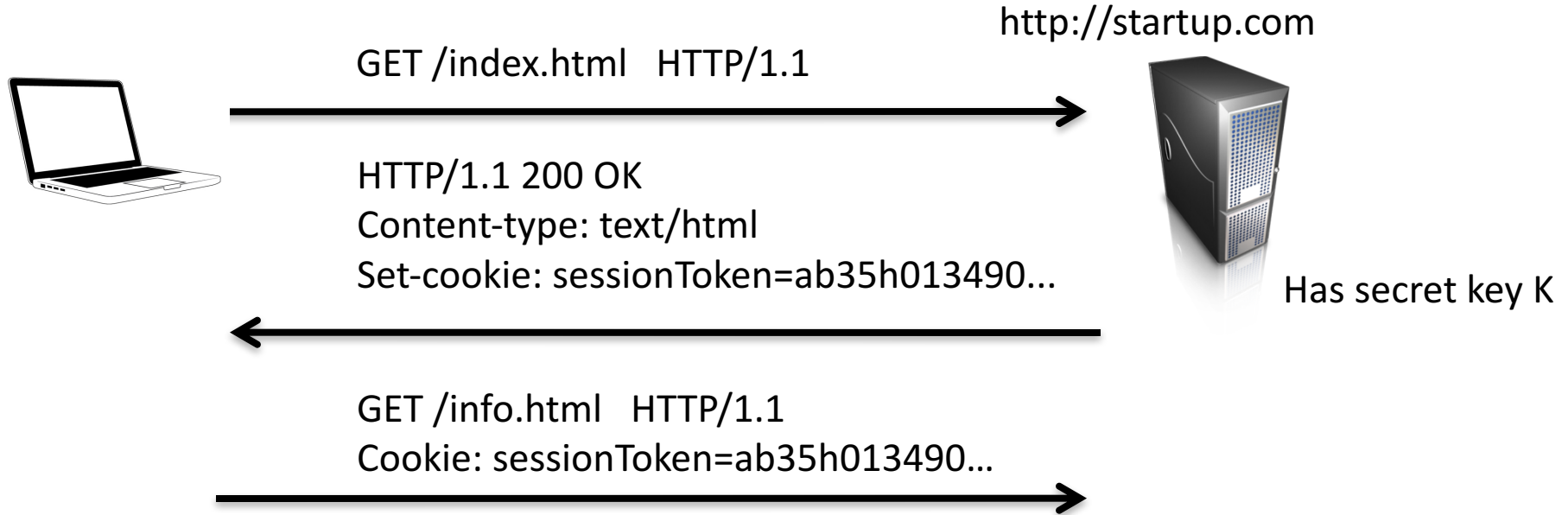
Attacks against bad CBC-MAC implementations

Variable-length secure CBC-MAC

# Review

- **Goal:** secure (length-extending) encryption
- What we have so far:
  - Block cipher modes of operation (CBC, CTR)
  - Insecurity against active attacks
    - Bit flip “mauling” attacks against CTR
    - Padding oracle attacks against CBC
- We need another tool:  
    authenticity mechanisms

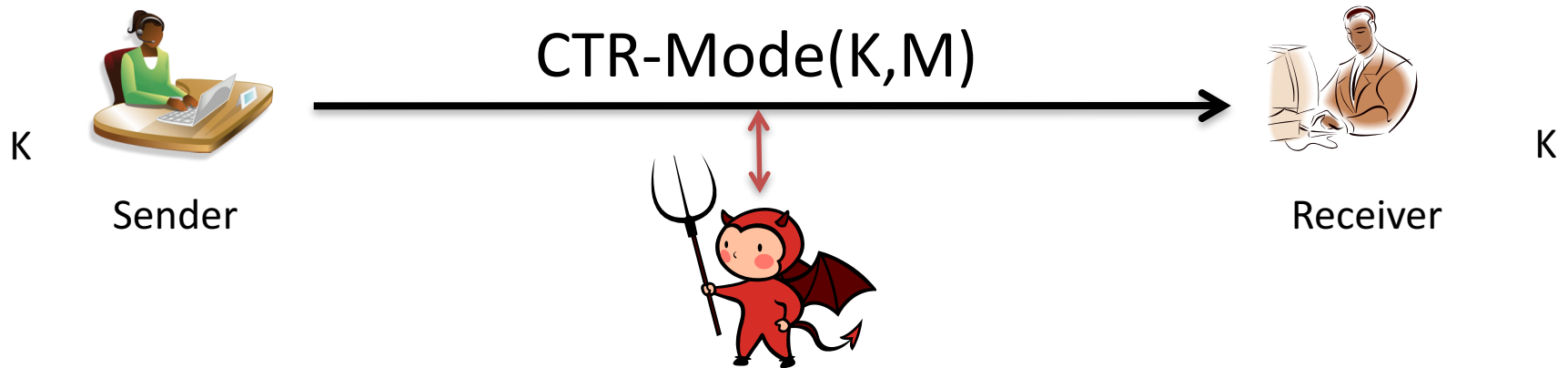
# Malleability example: Encrypted cookies



abc35h013490... = CTR-Mode(K, "admin=0")

Malicious client can simply flip a few bits to change admin=1

## More generally:

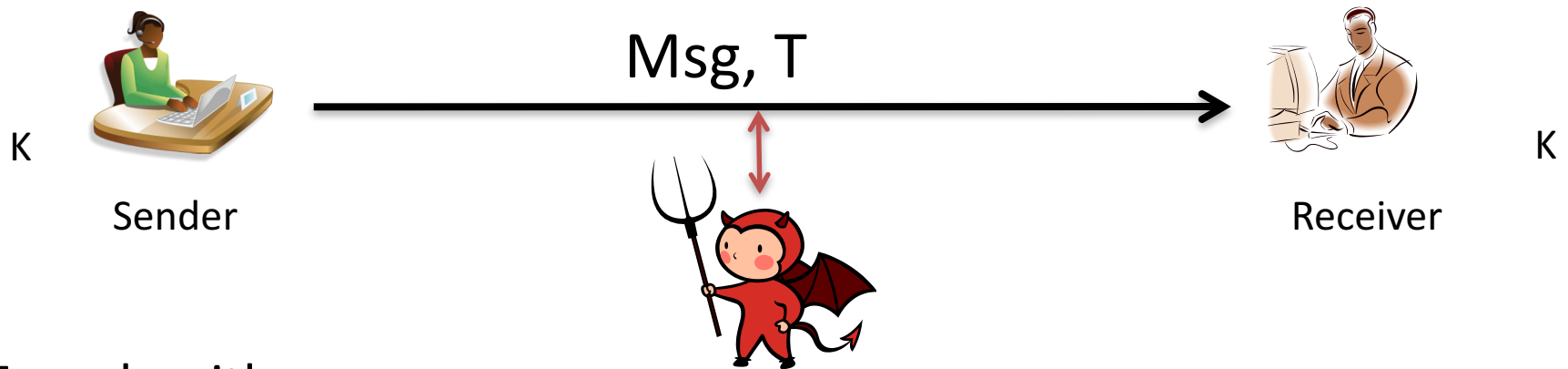


Attacker has read/write access to communications channel

### The strategy:

Arrange so that that all bits received can be validated as having come from sender (the person with key K)

# The tool: Message authentication



Two algorithms:

- (1)  $\text{Tag}(K, \text{Msg})$  outputs a tag  $T$
- (2)  $\text{Verify}(K, \text{Msg}, T)$  outputs 0/1 (invalid / valid)

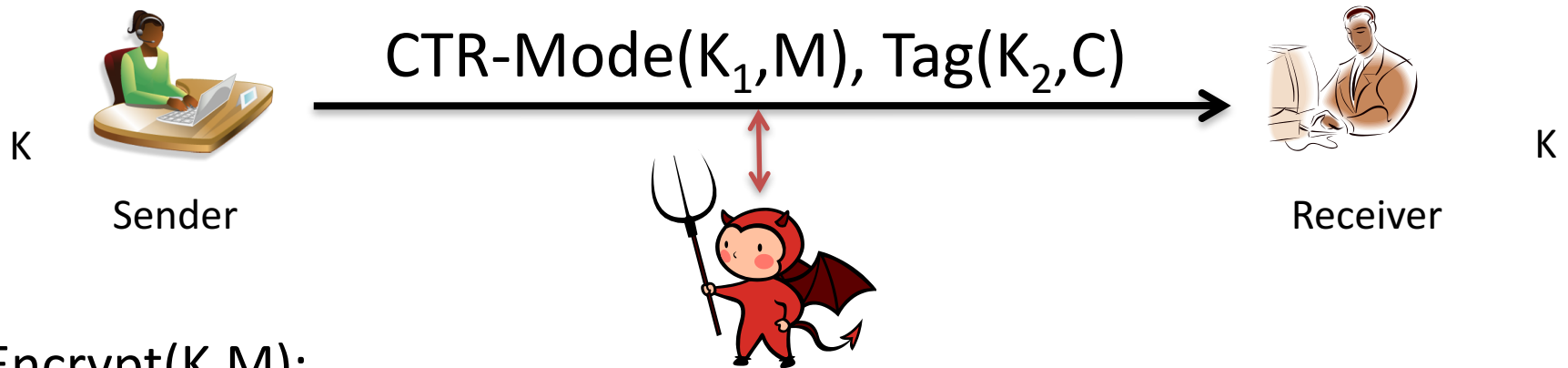
*Correctness:*  $\text{Verify}(K, \text{Msg}, \text{Tag}(K, \text{Msg})) = 1$  always

*Security:* No computationally efficient attacker can forge tags for a new message even when attacker gets

$(\text{Msg}_1, T_1), (\text{Msg}_2, T_2), \dots, (\text{Msg}_q, T_q)$

for messages of his choosing and reasonably large  $q$ .

# Composing encryption and authentication



## Encrypt(K,M):

Use secret keys  $K_1$  and  $K_2$ . These can be derived from  $K$  if needed

$$K_1 = AES(K, 0^n) \quad K_2 = AES(K, 1^n)$$

$$C = CTR\text{-}Mode(K_1, M)$$

$$T = Tag(K_2, C)$$

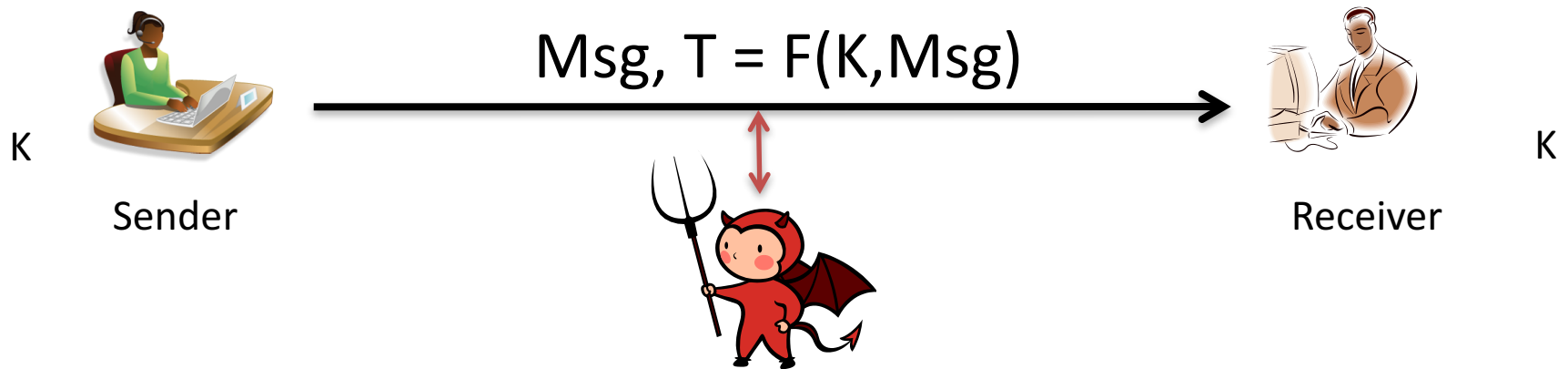
Output  $C || T$

## Decrypt(K,C||T)

If  $Tag(K_2, C, T) \neq 1$  then Return error

Return  $CTR\text{-}Mode(K_1, C)$

# Message authentication using pseudorandom functions (PRFs)

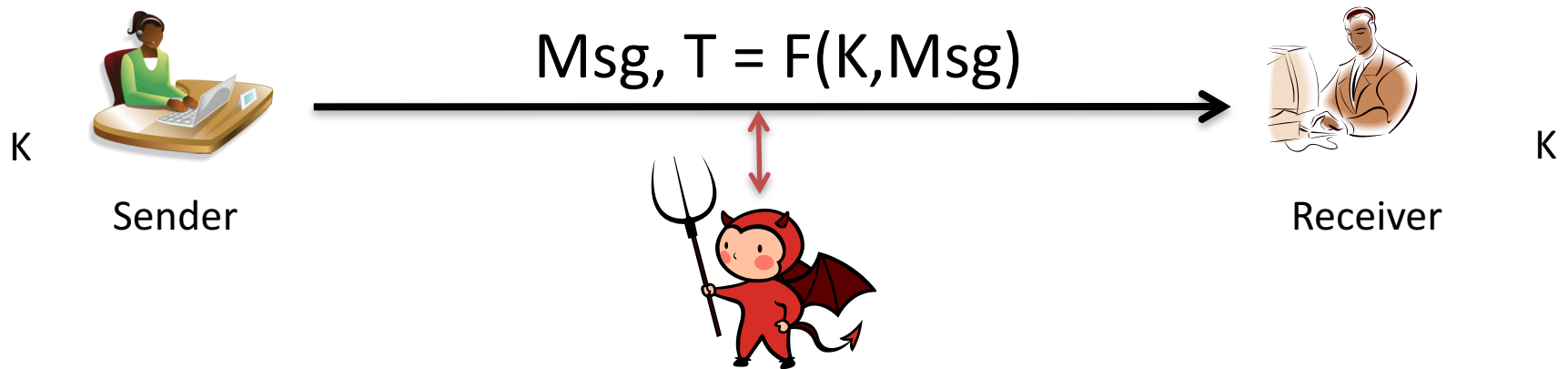


$$\text{Tag}(K,M) = F(K,\text{Msg})$$

If  $F$  behaves like random function (to those w/o  $K$ , this will be secure.

What was example of a good PRF?

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Deterministic message authentication scheme is often called *message authentication code (MAC)* and tag called MAC

What was example of a good PRF?



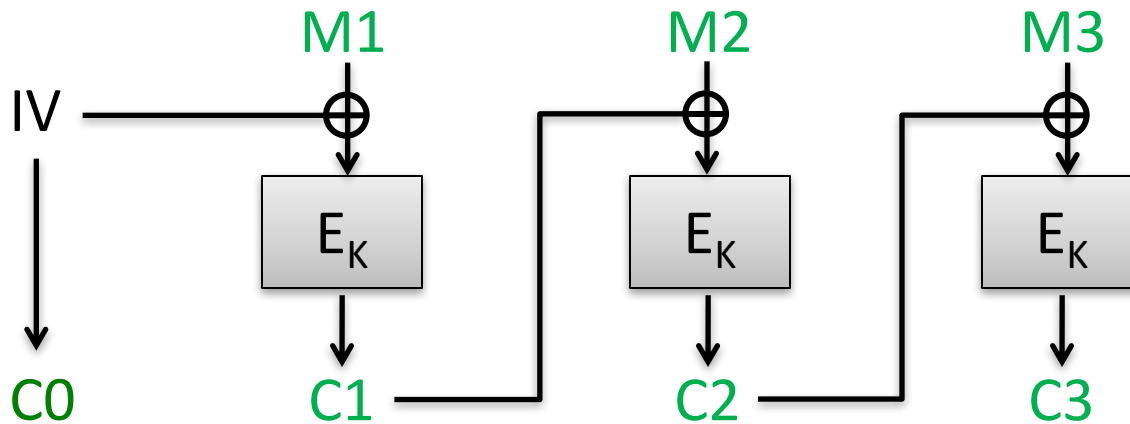
# Recall CBC mode

Ciphertext block chaining (CBC)

Pad message  $M$  to  $M_1, M_2, M_3, \dots$  where each block  $M_i$  is  $n$  bits

Choose random  $n$ -bit string  $IV$

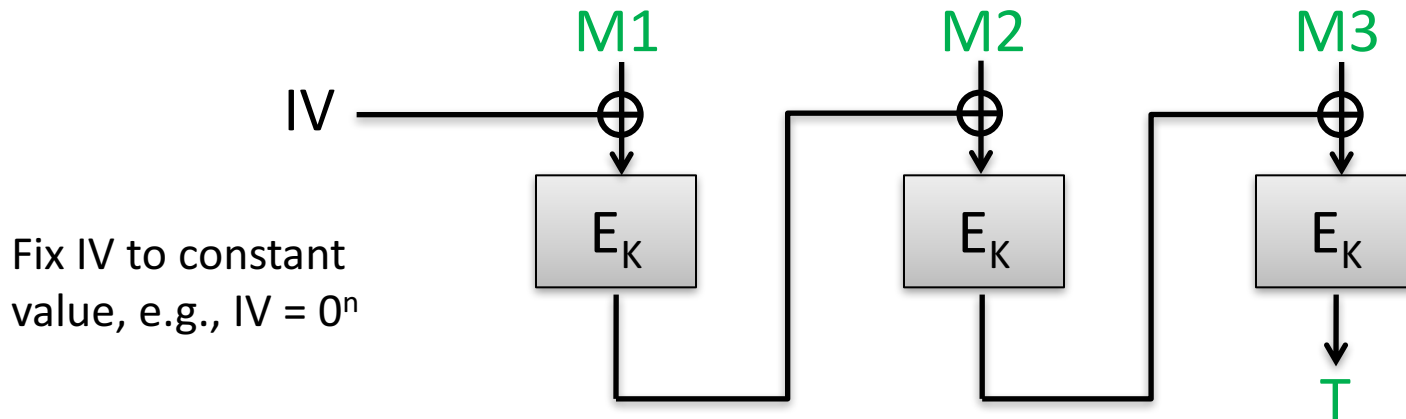
Then:



Can we convert this into variable-message-length PRF?

# CBC-MAC

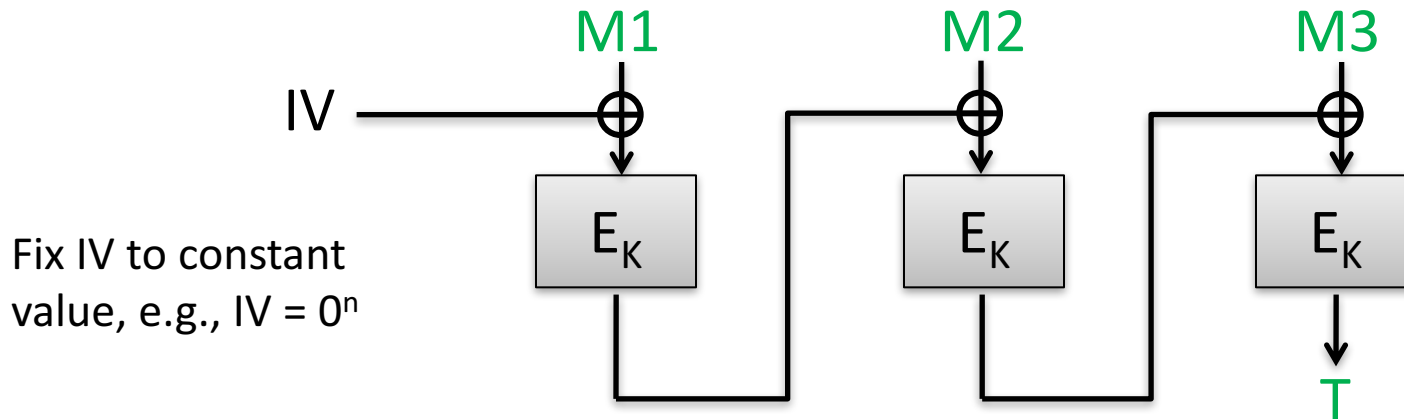
Message authentication code (MAC)



Turns out this is (provably) a good PRF  
***if only  $K$  used only on same-length messages***

# CBC-MAC

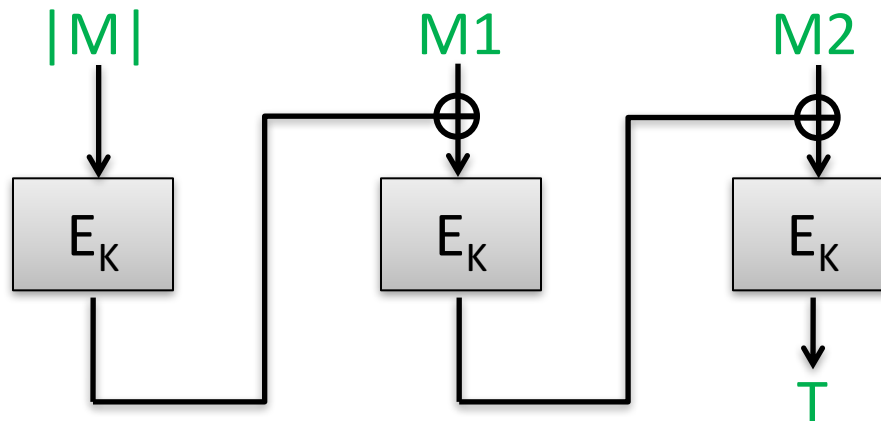
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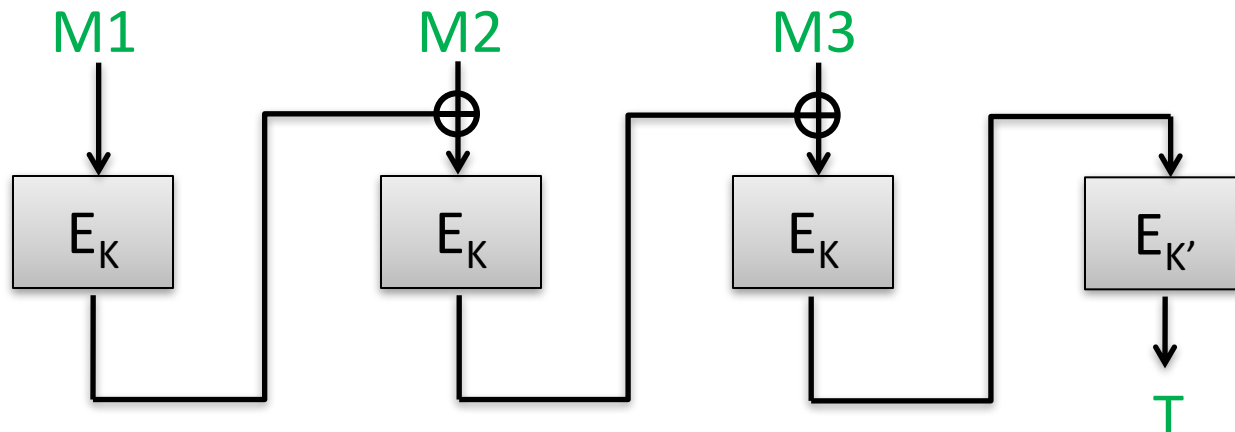
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# Variable-message-length CBC-MAC

- Prepend message length



- Encrypted CBC-MAC



# Discussion exercise

- We used hazmat interface for CBC mode in HW1 to implement Feistel round function.
- Does this realize a secure implementation of CBC-MAC?