

# MA 544: Homework 8

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**PROBLEM 8.1 (WHEEDEN & ZYGMUND §5, EX. 2)**

Show that the conclusion of (5.32) are not true without the assumption that  $\varphi \in L(E)$ . [In part (ii), for example, take  $f_k = \chi_{(k,\infty)} \cdot$ ]

*Proof.*

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**PROBLEM 8.2 (WHEEDEN & ZYGMUND §5, EX. 4)**

If  $f \in L(0, 1)$ , show that  $x^k f(x) \in L(0, 1)$  for  $k = 1, 2, \dots$ , and  $\int_0^1 x^k f(x) dx \rightarrow 0$ .

*Proof.*

■

**PROBLEM 8.3**

*Proof.*



**PROBLEM 8.4**

*Proof.*



**PROBLEM 8.5**

*Proof.*



**PROBLEM 8.6**

*Proof.*





**PROBLEM 8.7**

*Proof.*



**PROBLEM 8.8**

*Proof.*



**PROBLEM 8.9**

*Proof.*



**PROBLEM 8.10**

*Proof.*

