$$C \xrightarrow[\pi_n \circ f]{P} \downarrow^{\pi_n} \downarrow^{\pi_n}$$