$$\begin{CD}
I \times I @>{q \circ H}>> P^2 \\
@V{(q,\mathrm{id}_I)}VV @. \\
P^2 \times I.
\end{CD}$$

$$\overline{H}$$