$$\begin{array}{c|c} M\times N & \xrightarrow{(x,y)\mapsto (y,x)} N\times M \\ & \downarrow & \downarrow \\ R^{\bigoplus (M\times N)} & \xrightarrow{\cong} & R^{\bigoplus (N\times M)} \end{array}$$