$$\pi_1(X, x_0) \xrightarrow{\hat{\alpha}} \pi_1(X, x_1)$$

$$\uparrow = \widehat{\alpha * \beta} \qquad \downarrow \hat{\beta}$$

$$\pi_1(X, x_2).$$