$$S^1 \downarrow_q \qquad f \\ S^1/\sim \xrightarrow{\bar{f}} S^1.$$