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MA 26500 Quiz 4

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1. (12 points) List all the properties a set V must satisfy in order to be a vector space.

(*Hint:* there are eight of them.)

2. Which of the following subsets W of \mathbb{R}^3 are subspaces?

(a) (2 points)
$$W = \left\{ \begin{bmatrix} x \\ y \\ z \end{bmatrix} : x \le y \le z \right\}$$
.

(b) (2 points)
$$W = \left\{ \begin{bmatrix} x \\ y \\ z \end{bmatrix} : x + y + z = 0 \right\}.$$

(c) (2 points)
$$W = \left\{ \begin{bmatrix} x \\ y \\ z \end{bmatrix} : x^2 + y^2 + z^2 = 1 \right\}.$$

(d) (2 points)
$$W = \left\{ \begin{bmatrix} x + 2y + 3z \\ z \\ 0 \end{bmatrix} : x, y, z \in \mathbb{R} \right\}.$$

(By now you should have a feel of what a vector spaces is so you do not need to check all of the conditions; but for those that are not subspaces, give me a reason, e.g., the set is not closed under addition, multiplication by scalars, etc.) 이것 뭐예요? 처는 안 아라요.