

MA 544: Homework 8

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PROBLEM 8.1 (WHEEDEN & ZYGMUND §5, EX. 2)

- ¹ Show that the conclusion of (5.32) are not true without the assumption that $\varphi \in L(E)$. [In part (ii),
- ² for example, take $f_k = \chi_{(k,\infty)} \cdot]$
- ³ *Proof.* ■

PROBLEM 8.2 (WHEEDEN & ZYGMUND §5, EX. 4)

4 If $f \in L(0, 1)$, show that $x^k f(x) \in L(0, 1)$ for $k = 1, 2, \dots$, and $\int_0^1 x^k f(x) dx \rightarrow 0$.

5 *Proof.*

■

PROBLEM 8.3

6 *Proof.*



PROBLEM 8.4

⁷ *Proof.*



PROBLEM 8.5

8 *Proof.*



PROBLEM 8.6

9 *Proof.*



PROBLEM 8.7

¹⁰ *Proof.*



PROBLEM 8.8

¹¹ *Proof.*



PROBLEM 8.9

¹² *Proof.*



PROBLEM 8.10

13 *Proof.*

