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Name:

## MA 265 Quiz 2

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**Problem 2.1.** Given the system of linear equations

$$x - 2x_2 + x_3 - x_4 = 3$$

$$x_1 + x_2 + x_3 - x_4 = 1$$

$$x_1 + x_3 - x_4 = 2$$
(2.1)

find its reduced row-echelon form:

- $A) \ \begin{bmatrix} 1 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$
- B)  $\begin{bmatrix} 1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$
- $C) \ \begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$
- $D) \begin{bmatrix} 1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$
- E) Not listed.

**Problem 2.2.** Given the matrix

$$A := \begin{bmatrix} 1 & 2 & -1 \\ 2 & 5 & -1 \\ -1 & -4 & 0 \end{bmatrix} \tag{2.2}$$

and the vector  $\mathbf{b} := \begin{bmatrix} -3 \\ -4 \\ 2 \end{bmatrix}$ , find the vector  $\mathbf{x}$  such that  $A\mathbf{x} = \mathbf{b}$  by finding  $A^{-1}$ :

A) 
$$A^{-1} = \begin{bmatrix} -4 & 4 & 3 \\ 1 & -1 & -1 \\ -3 & 2 & 1 \end{bmatrix}$$
,  $\mathbf{x} = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix}$ 

B) 
$$A^{-1} = \begin{bmatrix} -4 & 4 & 3 \\ 1 & -1 & -1 \\ -3 & 2 & -1 \end{bmatrix}$$
,  $\mathbf{x} = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix}$ 

C) 
$$A^{-1} = \begin{bmatrix} 2 & 3 & -2 \\ 3 & 5 & -4 \\ 1 & 1 & -1 \end{bmatrix}, \mathbf{x} = \begin{bmatrix} 3 \\ -1 \\ 2 \end{bmatrix}$$

D) 
$$A^{-1} = \begin{bmatrix} 2 & 3 & -2 \\ 3 & 5 & -4 \\ 1 & 1 & -1 \end{bmatrix}$$
,  $\mathbf{x} = \begin{bmatrix} 3 \\ -1 \\ 2 \end{bmatrix}$ 

E) Does not exist; the matrix A is singular.