Instructor: Tatsunari Watanabe

TA: Carlos Salinas

Name:

## MA 265 Quiz 2

June 21, 2016

Problem 2.1. Given the system of linear equations

$$\begin{aligned} x-2x_2+x_3-x_4&=3\\ x_1+x_2+x_3-x_4&=1\\ x_1+x_3-x_4&=2 \end{aligned} \tag{2.1}$$

find its matrix representation and the reduced row-echelon form of that matrix.

- A)  $\begin{bmatrix} 1 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$
- B)  $\begin{bmatrix} 1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$
- C)  $\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$
- $D)\ \begin{bmatrix}\begin{smallmatrix} 1 & 0 & 1 & -1 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$
- E) Not listed.

Problem 2.2. Given the matrix

$$A := \begin{bmatrix} 1 & 2 & -1 \\ 2 & 5 & -1 \\ -1 & -4 & 0 \end{bmatrix} \tag{2.2}$$

and the vector  $\mathbf{b} \coloneqq \begin{bmatrix} -3 \\ -4 \\ 2 \end{bmatrix}$ , find the vector  $\mathbf{x}$  such that  $A\mathbf{x} = \mathbf{b}$  by finding  $A^{-1}$ :

A) 
$$A^{-1} = \begin{bmatrix} -4 & 4 & 3 \\ 1 & -1 & -1 \\ -3 & 2 & 1 \end{bmatrix}, \mathbf{x} = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix}$$

B) 
$$A^{-1} = \begin{bmatrix} -4 & 4 & 3 \\ 1 & -1 & -1 \\ -3 & 2 & -1 \end{bmatrix}$$
,  $\mathbf{x} = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix}$ 

C) 
$$A^{-1} = \begin{bmatrix} 2 & 3 & -2 \\ 3 & 5 & -4 \\ 1 & 1 & -1 \end{bmatrix}, \mathbf{x} = \begin{bmatrix} 3 \\ -1 \\ 2 \end{bmatrix}$$

D) 
$$A^{-1} = \begin{bmatrix} 2 & 3 & -2 \\ 3 & 5 & -4 \\ 1 & 1 & -1 \end{bmatrix}$$
,  $\mathbf{x} = \begin{bmatrix} 3 \\ -1 \\ 2 \end{bmatrix}$ 

E) Does not exist; the matrix A is singular.