MA 519: Homework 14

Max Jeter, Carlos Salinas December 1, 2016

Problem 14.1 (Handout 18, # 15)

(X,Y) is distributed uniformly inside of the unit circle. Find the density of X+Y and hence the mean of X+Y. Was the value of the mean obvious? Why?

Solution. Suppose
$$(X,Y) \sim U[\{x^2 + y^2 < 1\}].$$

Problem 14.2 (Handout 18, # 16)

Let X be a random number in [0,1]. What is the probability that the number 5 is completely missing from the decimal expansion of X?

SOLUTION.

Problem 14.3 (Handout 18, # 17)

A foot long stick is broken into three pieces. Find the density functions of the length of the longest part, the smallest part, and the medium part. What are the expected values for each part?

SOLUTION.