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Data Scientist



Learning Objectives

After this lesson, you should be able to:

- Build a logistic regression classification model using *sklearn*
- Describe the logit and sigmoid functions, odds and odds ratios, as well as how they relate to logistic regression
- Evaluate a model using metrics such as classification accuracy/error



Announcements and Exit Tickets



Review

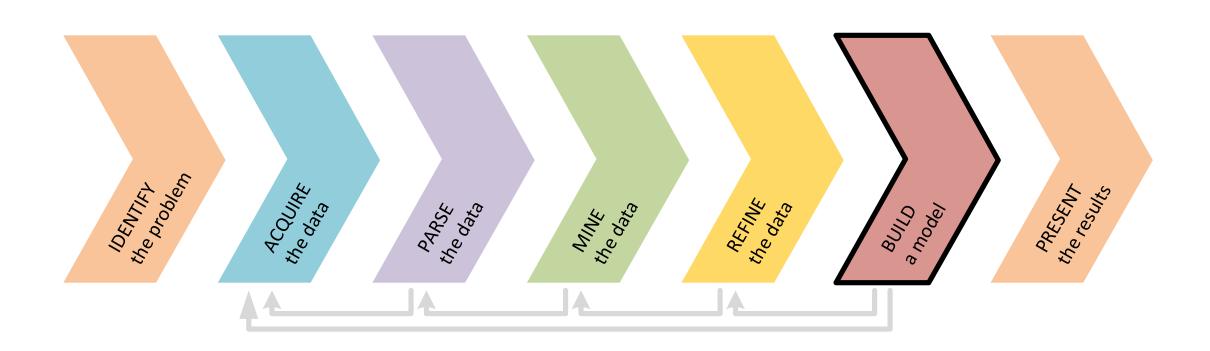


Today

Today, we are focusing on logistic regression

Research Design and Data Analysis	Research Design	Data Visualization in pandas	Statistics	Exploratory Data Analysis in <i>pandas</i>
Foundations of Modeling	Linear Regression	Classification Models	Evaluating Model Fit	Presenting Insights from Data Models
Data Science in the Real World	Decision Trees and Random Forests	Time Series Models	Natural Language Processing	Databases

Today, we keep our focus on the **6 BUILD** a model step but with a focus on logistic regression



Here's what's happening today:

- Announcements and Exit Tickets
- Review
- ► **6** Build a Model | Logistic Regression
 - How logistic regression relates to linear regression
 - "Retrofitting" linear regression into logistic regression
 - Interpreting the logistic regression coefficients

- Iris dataset and Codealong on the Iris dataset
- Lab –Logistic Regression
- Review
- Exit Tickets



Pre-Work

Pre-Work

Before this lesson, you should already be able to:

- ► Implement a linear model (LinearRegression) with *sklearn*
- Define the concept of coefficients
- Recall metrics for accuracy and misclassification



Why is logistic regression so valuable to know?

It addresses many commercially valuable classification problems, such as:

- Fraud detection (e.g., payments, e-commerce)
- Churn prediction (marketing)
- Medical diagnoses (e.g., is the test positive or negative?)
- and many, many others...



How logistic regression relates to linear regression

Logistic regression is a generalization of the linear regression model to classification problems

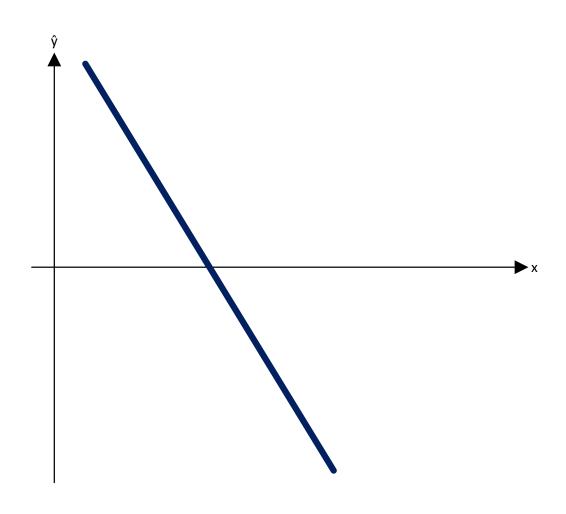
- The name is somewhat misleading
 - "Regression" comes from fact that we fit a linear model to the feature space
 - But it is really a technique for classification, not regression
- We use a linear model, similar to linear regression, in order to solve if an item belongs or does not belong to a class model
 - It is a binary classification technique: $y = \{0, 1\}$
 - Our goal is to classify correctly two types of examples:
 - Class 0, labeled as 0, e.g., "belongs"
 - Class 1, labeled as 1, e.g., "does not belong"

With linear regression, \hat{y} is in $]-\infty$; $+\infty[$, not [0;1]. How do we fix this for logistic regression?

The key variable in any regression problem is the outcome variable \hat{y} given the covariate x

$$\hat{y} = X \cdot \hat{\beta}$$

- With linear regression, \hat{y} takes values in $]-\infty$; $+\infty$ [
- However, with logistic regression, \hat{y} takes values in the unit interval [0; 1]



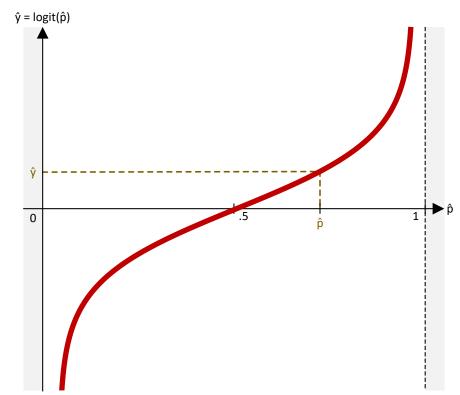


"Retrofitting" linear regression into logistic regression

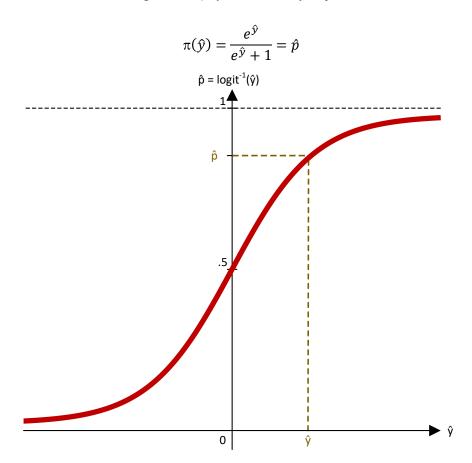
We "retrofit" linear regression in logistic regression with a transformation called the *logit* function (a.k.a., the *log-odds* function) and its inverse, the *logistic* function (a.k.a., *sigmoid* function)

logit maps \hat{p} ([0; 1]) to \hat{y} (] $-\infty$; $+\infty$ [)

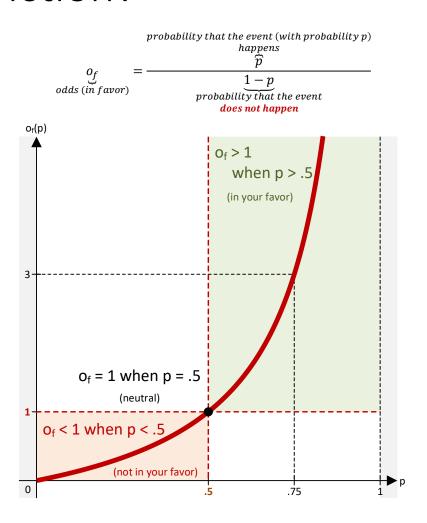
$$logit(\hat{p}) = ln\left(\frac{\hat{p}}{1-\hat{p}}\right) = \hat{y}$$



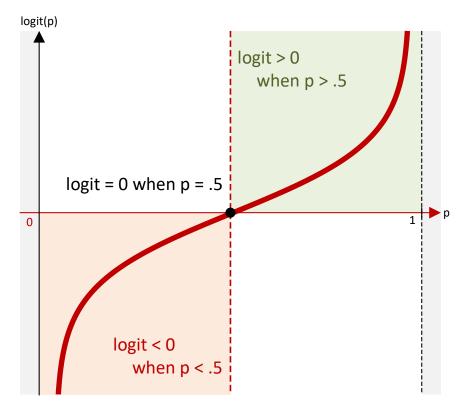
 $\pi = logit^{-1} \text{ maps } \hat{y} (]-\infty; +\infty[) \text{ to } \hat{p} ([0;1])$



Why is the *logit* function also called the *log-odds* function?



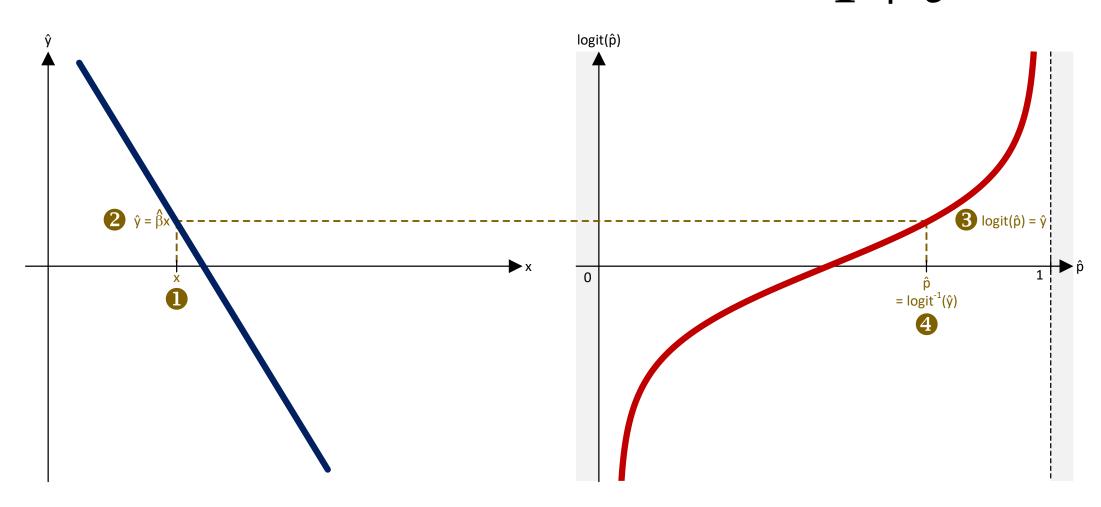
$$logit(p) = ln(o_f) = ln\left(\frac{p}{1-p}\right)$$



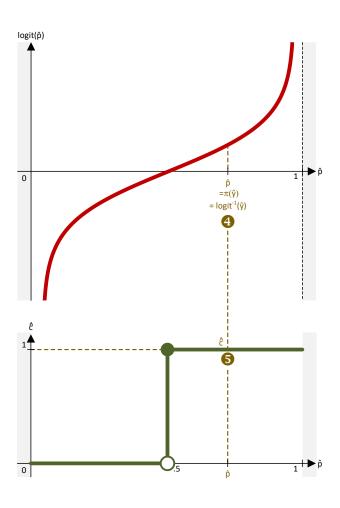
Putting together $\hat{y} = X \cdot \hat{\beta}$ and $\hat{p} = \pi(\hat{y})$ (really, mapping \hat{y} back to \hat{p}), we get

$$\hat{p} = \pi(X \cdot \hat{\beta}) = \frac{e^{X \cdot \hat{\beta}}}{e^{\hat{\beta}x} + 1} = \frac{1}{1 + e^{-X \cdot \hat{\beta}}}$$

$$\hat{p} = logit^{-1}(\hat{y}) = logit^{-1}(X \cdot \hat{\beta}) = \frac{1}{1 + e^{-X \cdot \hat{\beta}}}$$



Finally, probabilities are "snapped" to class labels (e.g., by thresholding at the 50% level)





Interpreting the logistic regression coefficients

Interpreting the logistic regression coefficients

Mith linear regressions, $\hat{\beta}_j$ represents the change in y for a change in unit of x_j

$$ln\left(\frac{\hat{p}}{1-\hat{p}}\right) = X \cdot \hat{\beta} = \hat{\beta}_0 + \hat{\beta}_1 \cdot x_1 + \dots + \hat{\beta}_k \cdot x_k$$

- With logistic regressions, $\hat{\beta}_i$ represents the **log-odds** change in c for a change in unit of x_i
- This also means that $e^{\widehat{\beta}_j}$ represents the multiplier change in **odds** in c for a change in unit of x_i

$$\frac{\widehat{odds}(x_j+1)}{\widehat{odds}(x_j)} = \frac{e^{\widehat{y}(x_j+1)}}{e^{\widehat{y}(x_j)}} = e^{\widehat{y}(x_j+1)-\widehat{y}(x_j)} = e^{(\mathbf{X}+\widehat{\beta}_j \cdot x_j + \mathbf{X})-(\mathbf{X}+\widehat{\beta}_j \cdot (x_j+1) + \mathbf{X})} = e^{\widehat{\beta}_j}$$



Activity | Interpreting the logistic regression coefficients

Activity | Interpreting the logistic regression coefficients



DIRECTIONS (5 minutes)

- 1. Suppose we are interested in mobile purchasing behavior. Let c be the class label denoting purchase/no purchase, and x_1 a feature denoting whether a phone is an iPhone or not. After performing a logistic regression, we get $\hat{\beta}_1$ = .693. What does this mean?
- 2. When finished, share your answers with your table

DELIVERABLE

Answers to the above question

Activity | Interpreting the logistic regression coefficients (cont.)

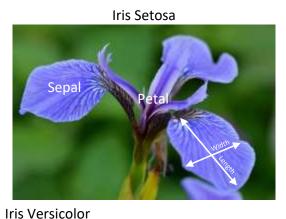


1. In this case, the odds ratio change is $e^{\widehat{\beta}_j} = e^{.693} = 2$, meaning the likelihood of purchase is twice as high if the phone is an iPhone



Iris Dataset, Take 2

Review | Iris dataset



THIS VERSICOION



Source: Flickr

3 classes of Irises (Setosa,Versicolor, and Virginica)

- 4 attributes
 - Sepal length and width
 - Petal length and width
- 50 instances of each class



Iris Dataset, Take 2

Codealong - Logistic Regression



Pros and Cons

Logistic Regression | Pros and cons

- Pros
 - Fit is fast
 - Output is a (posterior)probability which is easy tointerpret

Cons

Limited to binary classification
 (but sklearn provides a multiclass implementation; use ensemble under the hood)



Further Readings

Further Readings

- ISLR

► Logistic Regression (section 4.3, pp. 130 – 138)

• ESLII

► Logistic Regression (section 4.4, pp. 119 – 129)



Lab

Logistic Regression



Review

Review

You should now be able to:

- Build a Logistic regression classification model using *sklearn*
- Describe the logit and sigmoid functions, odds, and odds ratios as well as how they relate to logistic regression
- Evaluate a model using metrics such as classification accuracy/error

Next Class

Flexible Class Session #2 | Machine Learning Modeling



Exit Ticket

Don't forget to fill out your exit ticket here

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