More trees

The EVB for each single-action update (i.e., taking action a^* at belief state b) is calculated as:

$$\text{EVB}(ba^*) = p(b_\rho \rightarrow b \mid \pi) \times \left(\mathbb{E}_{b' \sim p(b' \mid b, a^*)}\left[v(b')\right] - v(b)\right) \tag{1}$$

Where $p(b_\rho \rightarrow b \mid \pi)$ is the Need term – i.e., the probability of reaching belief b from the root of the tree, b_ρ, when following policy π. The policy π here is i) softmax of the MF Q-values at the root of the tree, b_ρ; and ii) softmax of the immediate reward at every other node within the tree.

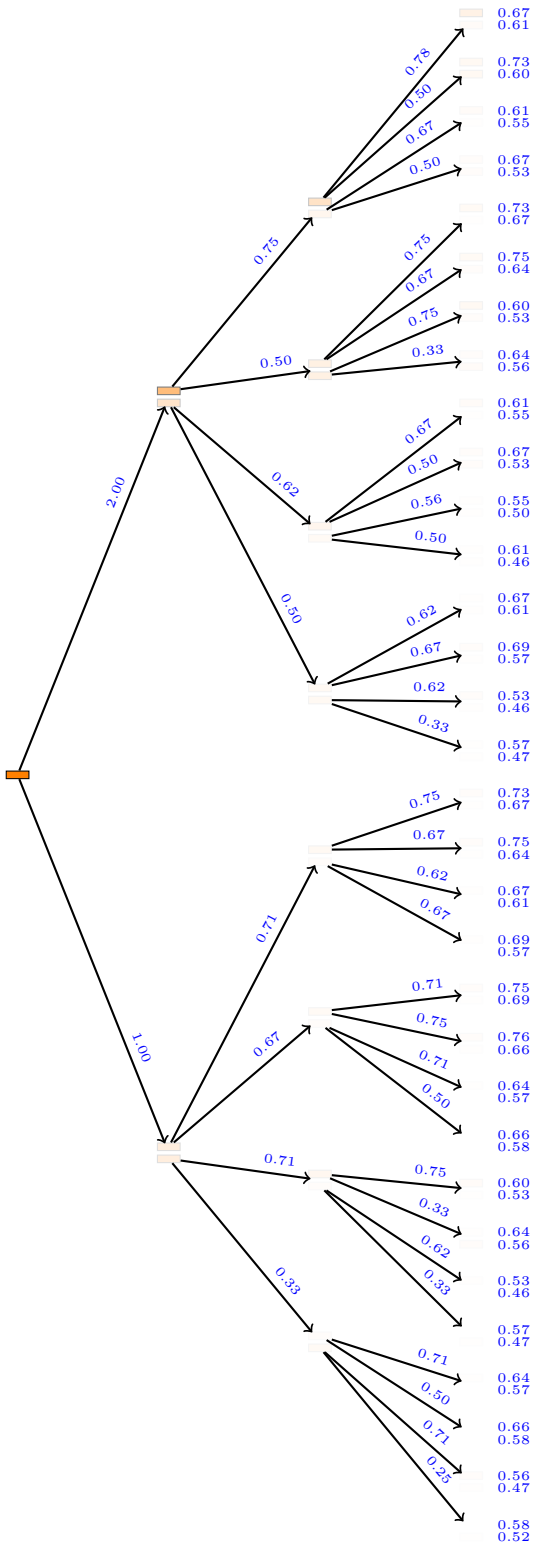
In the trees, each action has a blue number written above it – these are the Q-values. Each orange square is a belief state, and the opacity of each belief state is proportional to the Need term from equation 1. When belief states appear in pairs, the top belief state is always the one which results from obtaining a reward from the corresponding action, whilst the bottom belief state corresponds to zero reward.

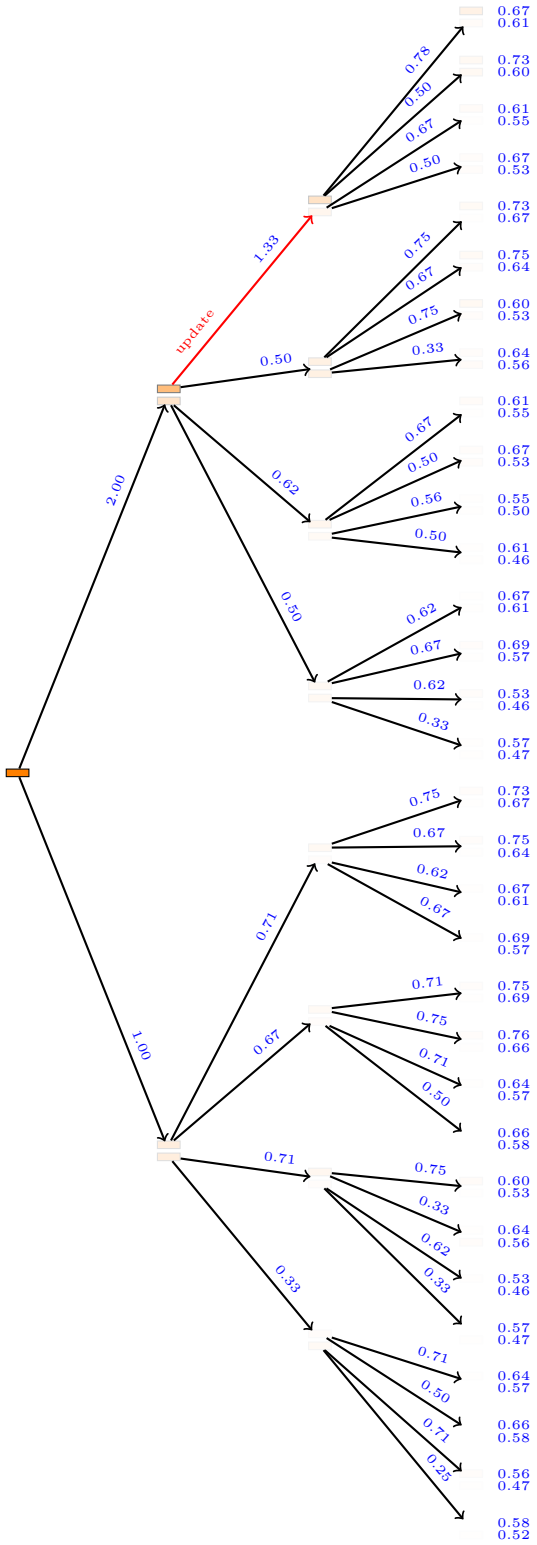
Updates in the tree are always highlighted by red arrows.

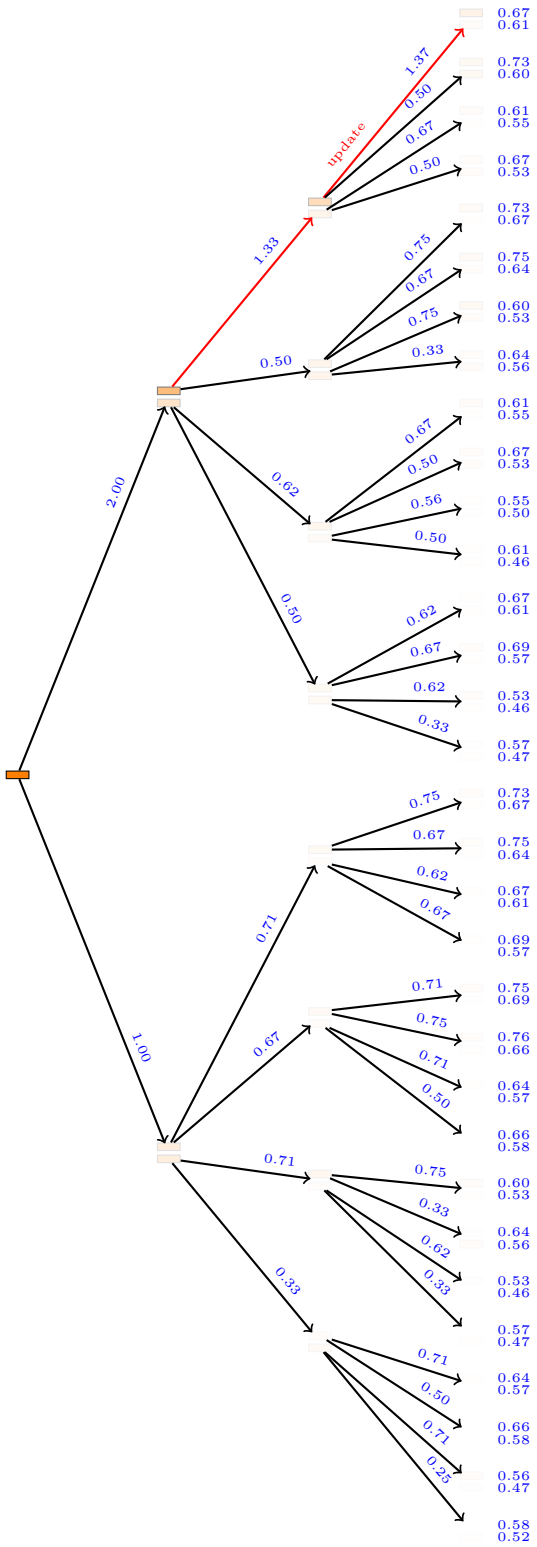
Example 1

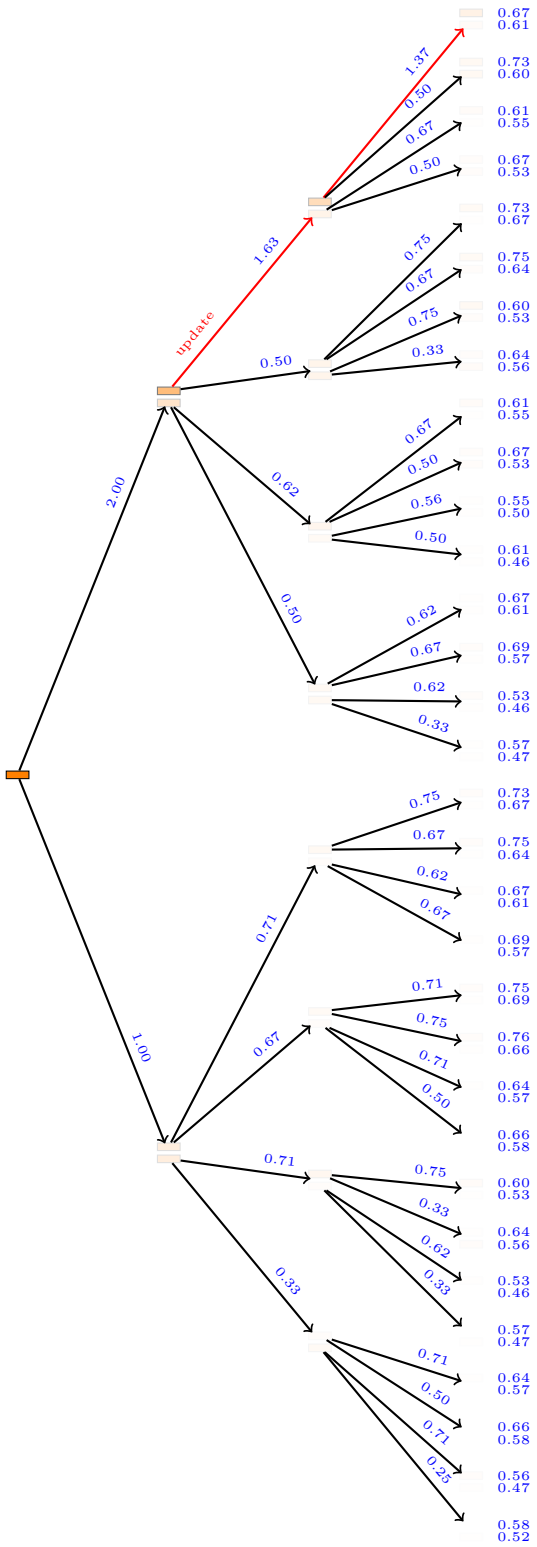
Belief at the root in this example is:

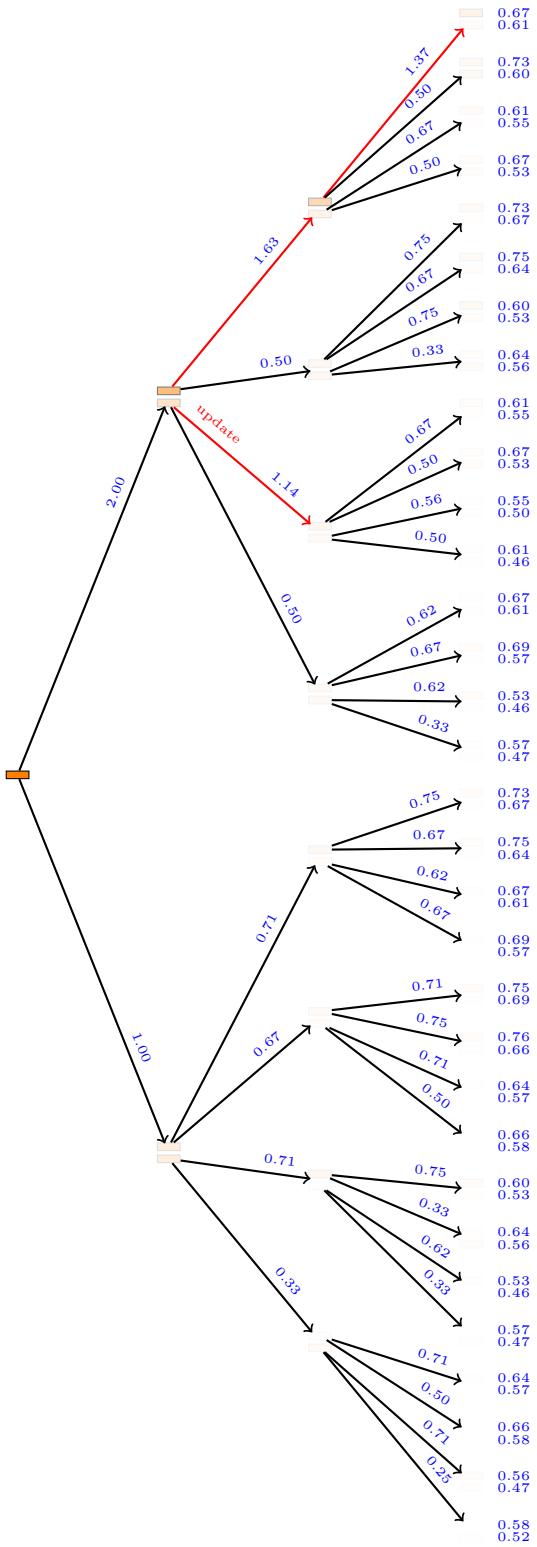
$$\alpha_0 = 5 \quad \beta_0 = 2$$
$$\alpha_1 = 1 \quad \beta_1 = 1$$

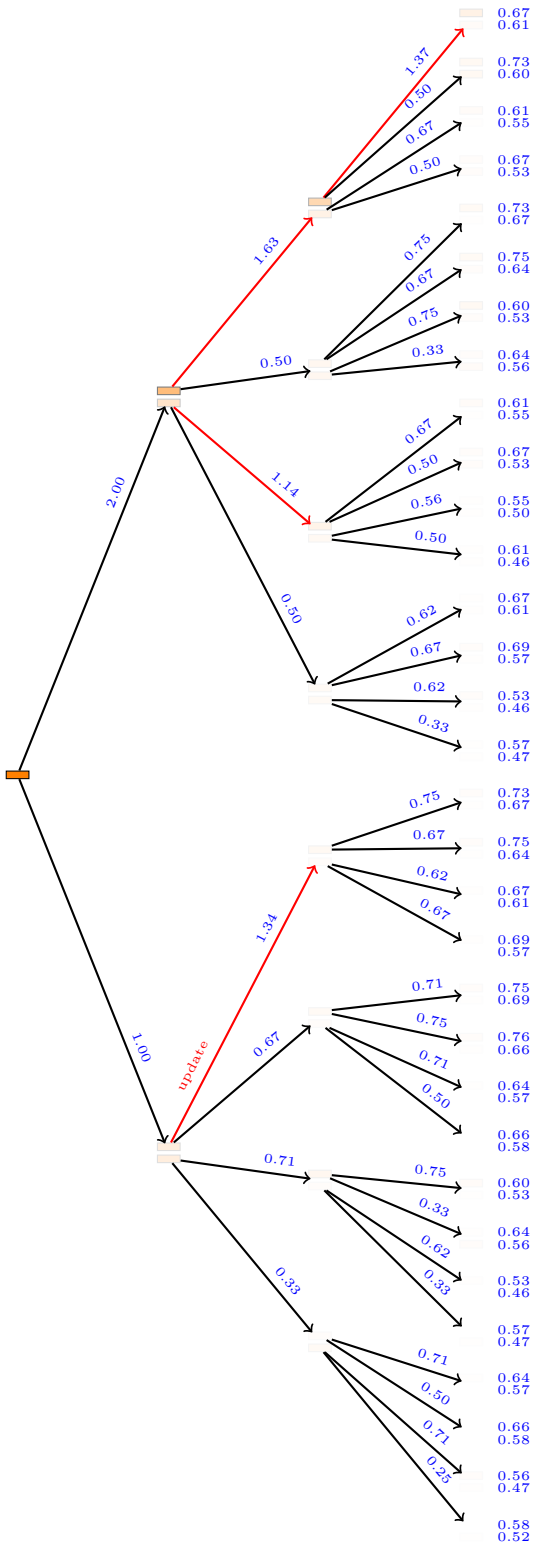

2.00
1.00
0.75
0.50
0.62
0.50
0.71
0.67
0.71
0.33
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.73
0.67
0.75
0.64
0.60
0.53
0.64
0.56
0.61
0.55
0.67
0.53
0.55
0.50
0.61
0.46
0.67
0.61
0.69
0.57
0.53
0.46
0.57
0.47
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.75
0.69
0.76
0.66
0.64
0.57
0.66
0.58
0.60
0.53
0.64
0.56
0.53
0.46
0.57
0.47
0.64
0.57
0.66
0.58
0.56
0.47
0.58
0.52

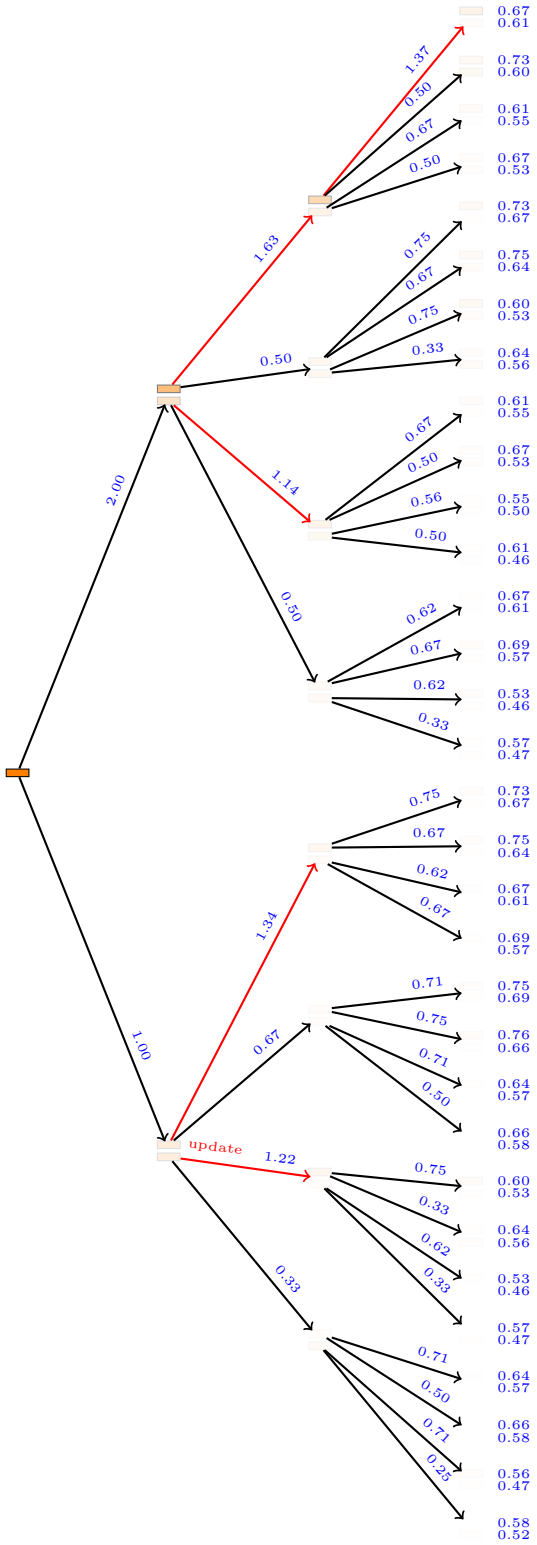

update
2.00
1.00
1.33
0.50
0.62
0.50
0.71
0.67
0.78
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.75
0.64
0.60
0.53
0.64
0.56
0.67
0.50
0.56
0.50
0.67
0.53
0.55
0.50
0.61
0.46
0.62
0.67
0.62
0.33
0.67
0.61
0.69
0.57
0.53
0.46
0.57
0.47
0.75
0.67
0.62
0.67
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.71
0.75
0.71
0.50
0.75
0.69
0.76
0.66
0.64
0.57
0.66
0.58
0.71
0.75
0.33
0.62
0.33
0.60
0.53
0.64
0.56
0.53
0.46
0.57
0.47
0.71
0.50
0.71
0.25
0.64
0.57
0.66
0.58
0.56
0.47
0.58
0.52

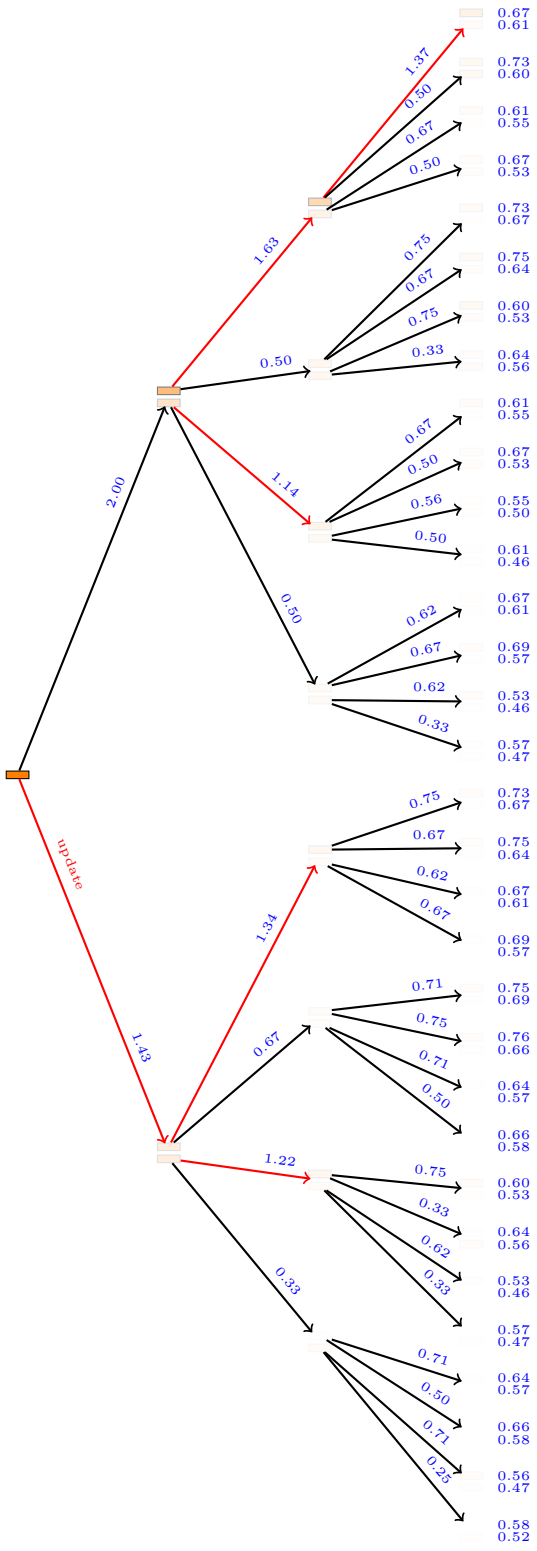

update
2.00
1.00
1.33
0.50
0.62
0.50
0.71
0.67
1.37
0.50
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
0.75
0.67
0.62
0.67
0.71
0.75
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

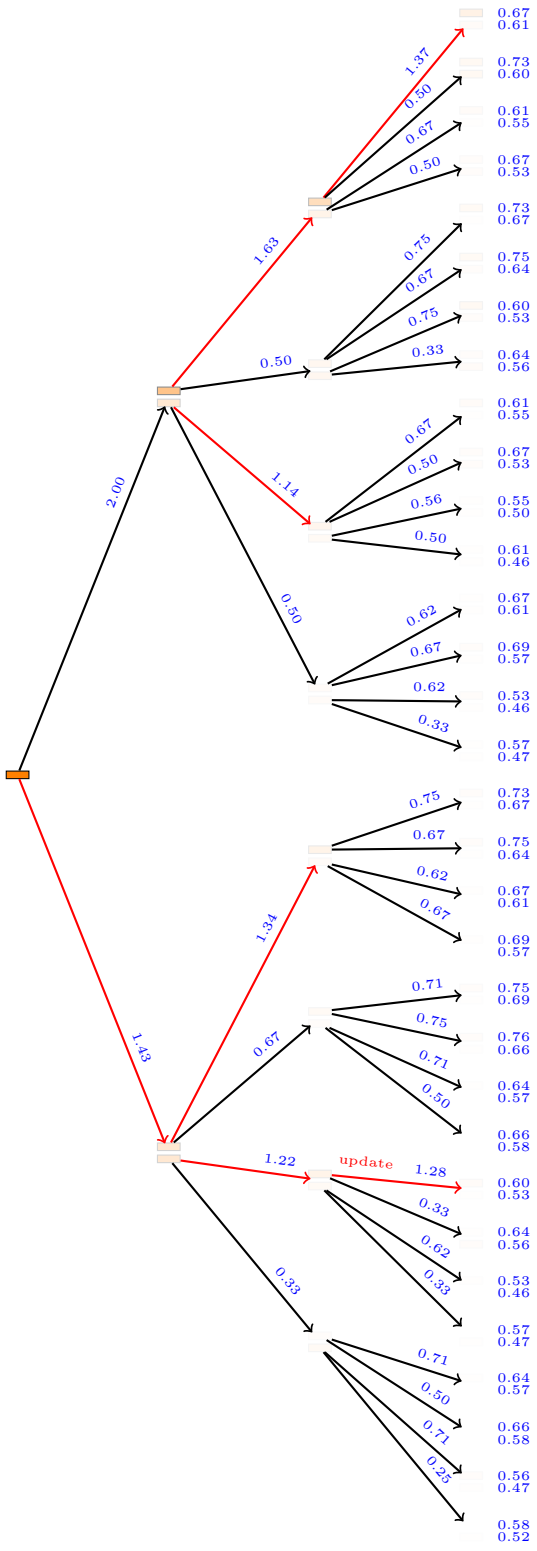

update
2.00
1.00
1.63
0.50
0.62
0.50
0.71
0.67
1.37
0.50
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
0.75
0.67
0.62
0.67
0.71
0.75
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

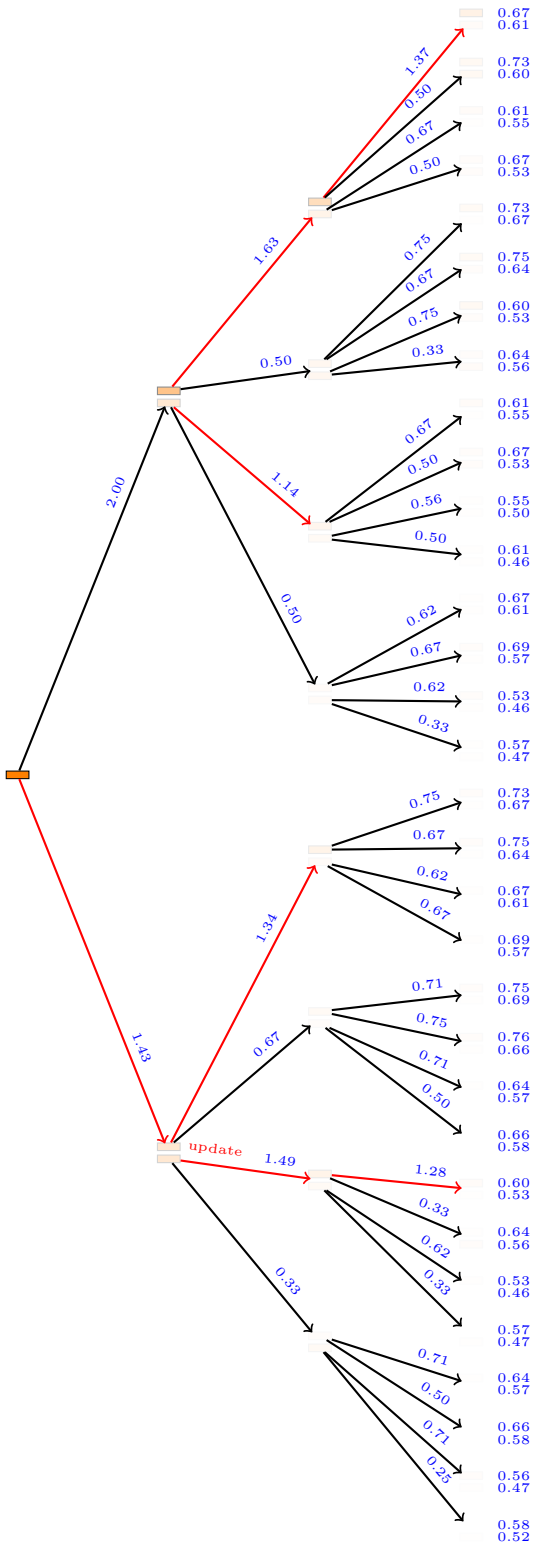

2.00
1.00
1.63
0.50
update
1.14
0.50
0.71
0.67
1.37
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.75
0.64
0.67
0.75
0.60
0.53
0.33
0.64
0.56
0.67
0.50
0.61
0.55
0.56
0.55
0.50
0.50
0.61
0.46
0.62
0.67
0.67
0.61
0.69
0.57
0.62
0.53
0.46
0.33
0.57
0.47
0.75
0.67
0.73
0.67
0.67
0.75
0.64
0.62
0.67
0.67
0.61
0.69
0.57
0.71
0.75
0.69
0.75
0.76
0.66
0.71
0.64
0.57
0.50
0.66
0.58
0.71
0.75
0.60
0.53
0.33
0.64
0.56
0.62
0.53
0.46
0.33
0.57
0.47
0.71
0.64
0.57
0.50
0.66
0.58
0.71
0.56
0.47
0.25
0.58
0.52

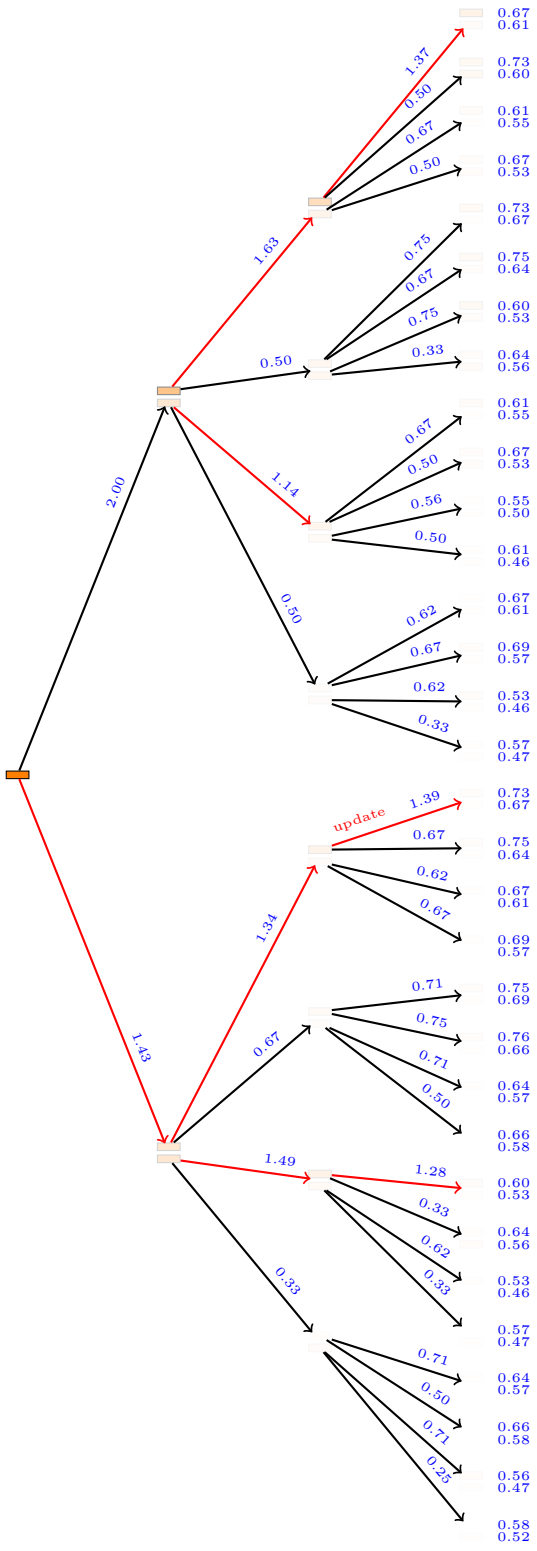

2.00
1.00
update
1.63
0.50
1.14
0.50
1.37
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.67
0.75
0.64
0.75
0.67
0.60
0.53
0.33
0.64
0.56
0.67
0.50
0.61
0.55
0.67
0.53
0.56
0.55
0.50
0.50
0.61
0.46
0.62
0.67
0.67
0.69
0.57
0.62
0.53
0.46
0.33
0.57
0.47
1.34
0.67
0.71
0.33
0.75
0.67
0.62
0.67
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.71
0.75
0.69
0.75
0.76
0.66
0.71
0.64
0.57
0.50
0.66
0.58
0.75
0.60
0.53
0.33
0.64
0.56
0.62
0.53
0.46
0.33
0.57
0.47
0.71
0.64
0.57
0.50
0.66
0.58
0.71
0.56
0.47
0.25
0.58
0.52

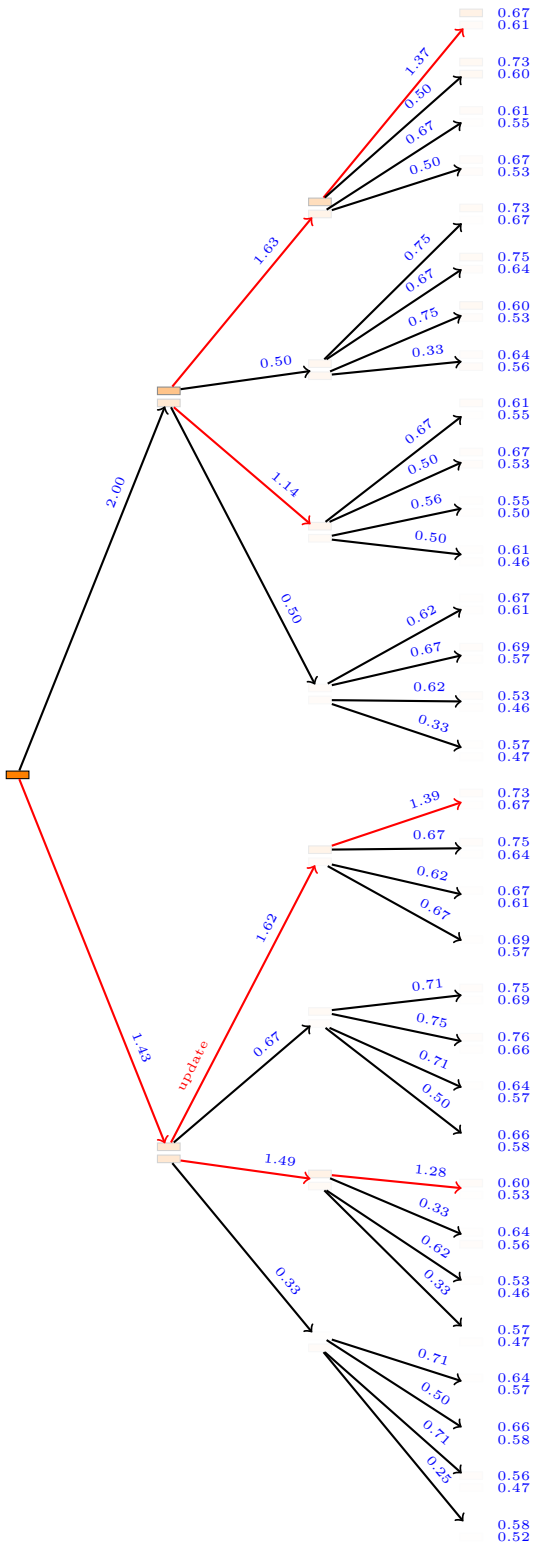

2.00
1.00
1.63
0.50
1.14
0.50
1.37
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.67
0.64
0.75
0.53
0.60
0.53
0.33
0.64
0.56
0.67
0.50
0.56
0.50
0.61
0.55
0.67
0.53
0.55
0.50
0.61
0.46
0.62
0.67
0.62
0.33
0.67
0.61
0.69
0.57
0.53
0.46
0.57
0.47
1.34
0.67
1.22
0.33
0.75
0.67
0.62
0.67
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.71
0.75
0.71
0.50
0.75
0.69
0.76
0.66
0.64
0.57
0.66
0.58
update
0.75
0.33
0.62
0.33
0.60
0.53
0.64
0.56
0.53
0.46
0.57
0.47
0.71
0.50
0.71
0.25
0.64
0.57
0.66
0.58
0.56
0.47
0.58
0.52

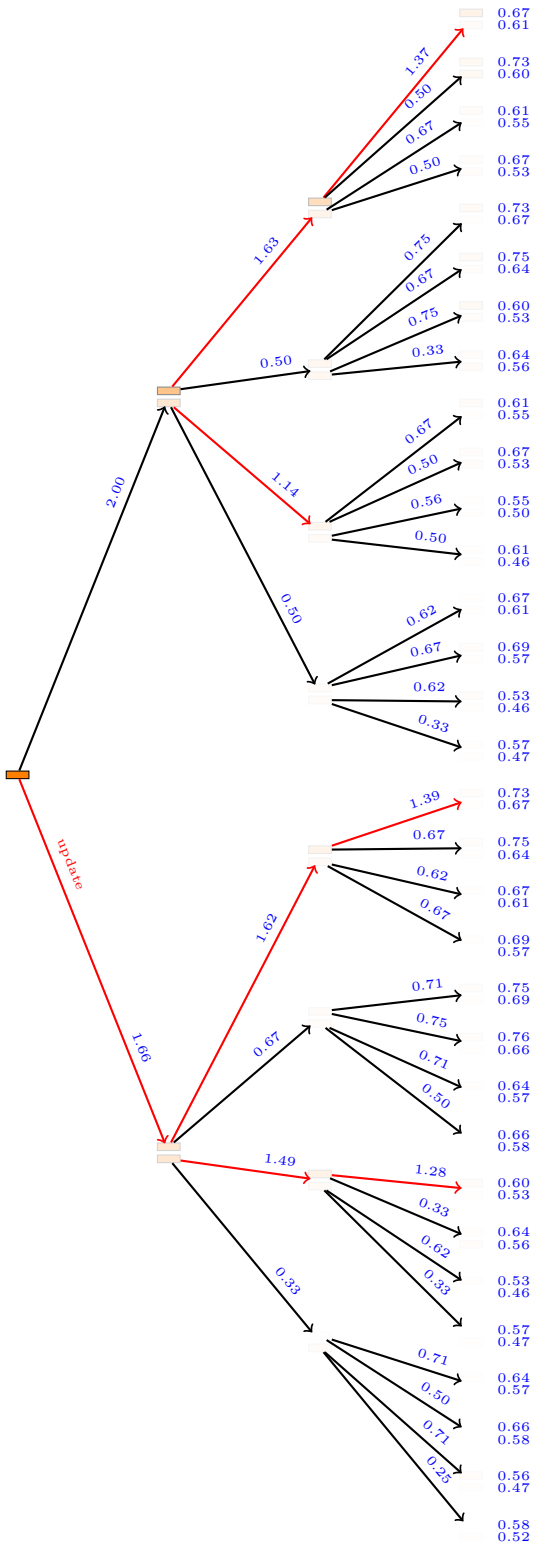

update
2.00
1.43
1.63
0.50
1.14
0.50
1.34
0.67
1.22
0.33
1.37
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.75
0.64
0.67
0.75
0.60
0.53
0.33
0.64
0.56
0.67
0.50
0.56
0.50
0.61
0.55
0.67
0.53
0.55
0.50
0.61
0.46
0.62
0.67
0.62
0.33
0.67
0.61
0.69
0.57
0.53
0.46
0.57
0.47
0.75
0.67
0.67
0.62
0.67
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.71
0.75
0.71
0.50
0.75
0.69
0.76
0.66
0.64
0.57
0.66
0.58
0.75
0.33
0.62
0.33
0.60
0.53
0.64
0.56
0.53
0.46
0.57
0.47
0.71
0.50
0.71
0.25
0.64
0.57
0.66
0.58
0.56
0.47
0.58
0.52

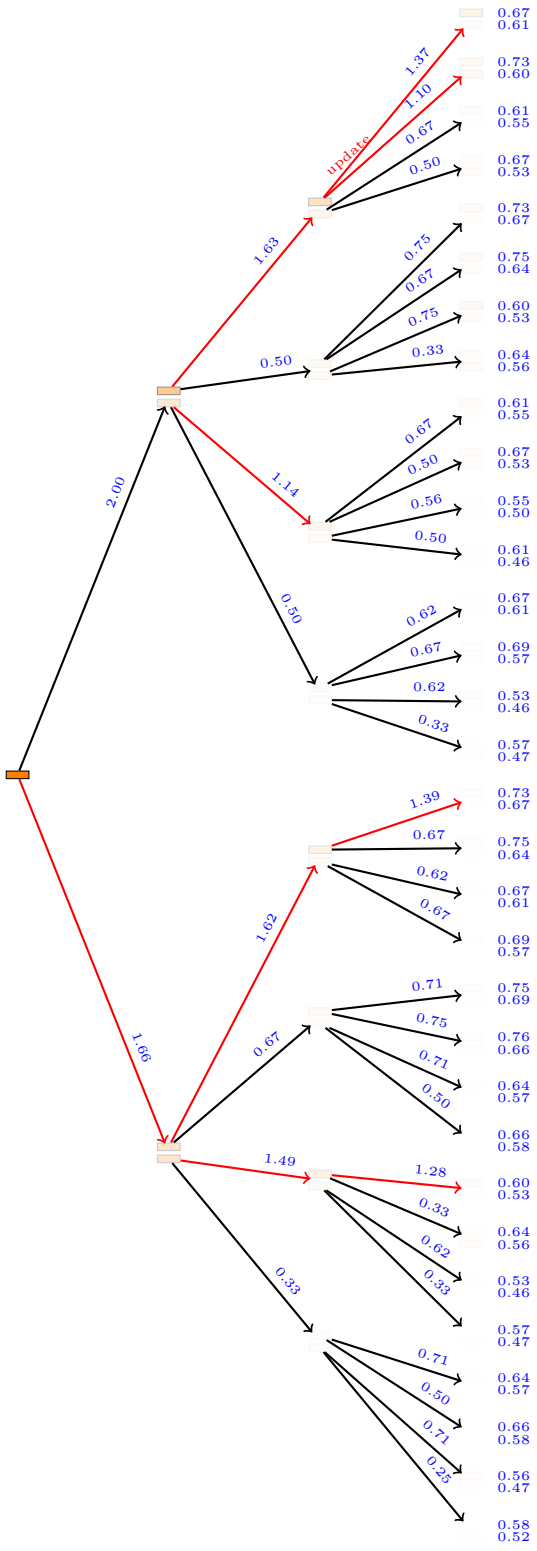

2.00
1.43
1.63
0.50
1.14
0.50
1.34
0.67
1.22
0.33
1.37
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.75
0.64
0.67
0.75
0.60
0.53
0.33
0.64
0.56
0.67
0.50
0.56
0.50
0.61
0.55
0.67
0.53
0.55
0.50
0.61
0.46
0.62
0.67
0.62
0.33
0.67
0.61
0.69
0.57
0.53
0.46
0.57
0.47
0.75
0.67
0.67
0.62
0.67
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.71
0.75
0.71
0.50
0.75
0.69
0.76
0.66
0.64
0.57
0.66
0.58
update
1.28
0.33
0.62
0.33
0.60
0.53
0.64
0.56
0.53
0.46
0.57
0.47
0.71
0.50
0.71
0.25
0.64
0.57
0.66
0.58
0.56
0.47
0.58
0.52

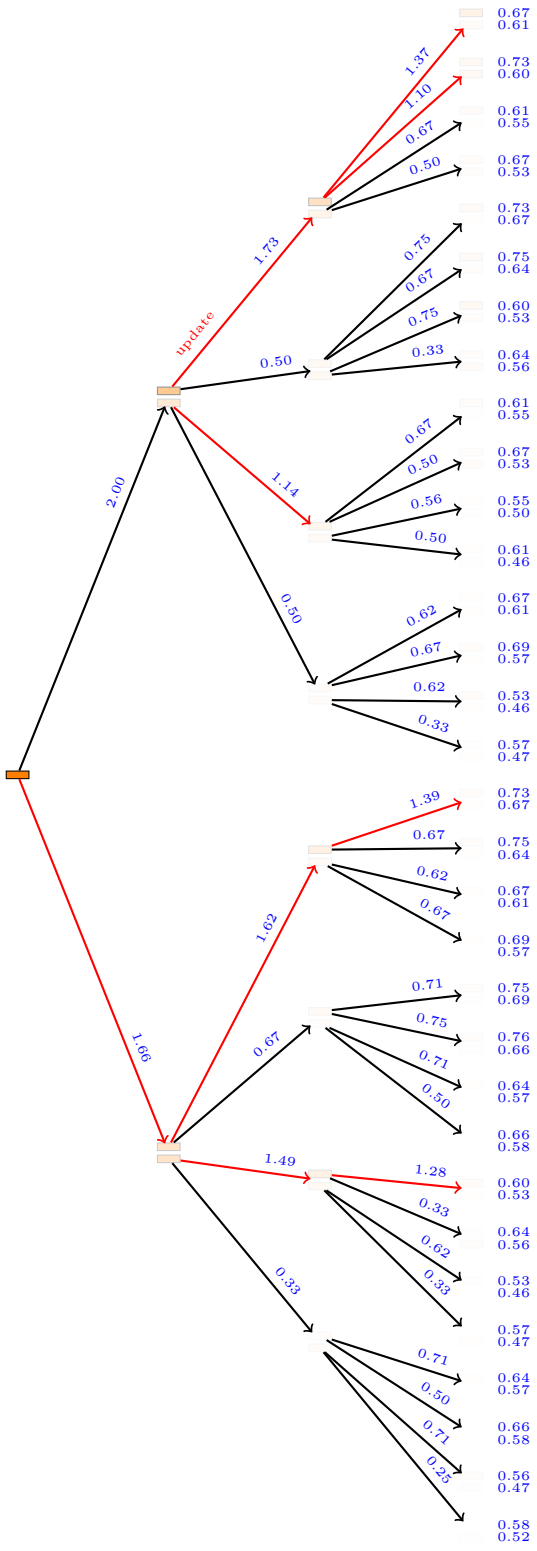

2.00
1.43
1.63
0.50
1.14
0.50
1.34
0.67
update
1.49
0.33
1.37
0.50
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
0.75
0.67
0.62
0.67
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

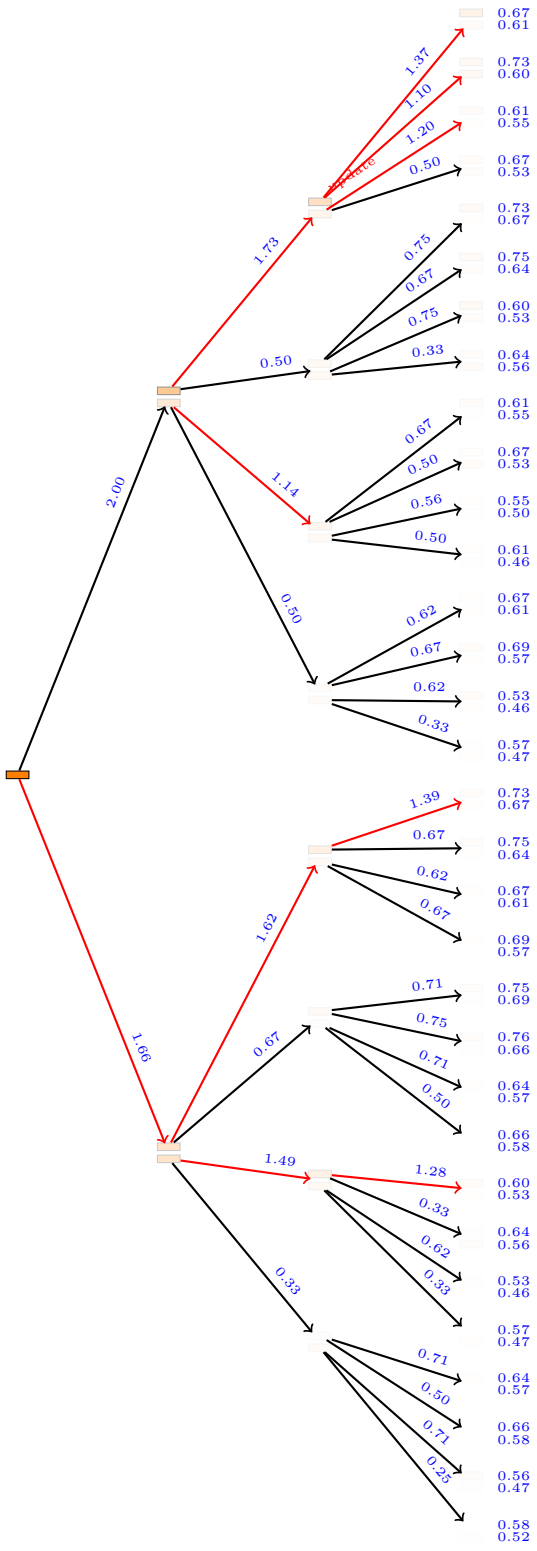

2.00
1.43
1.63
0.50
1.14
0.50
1.34
0.67
1.49
0.33
update
1.39
1.37
0.50
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

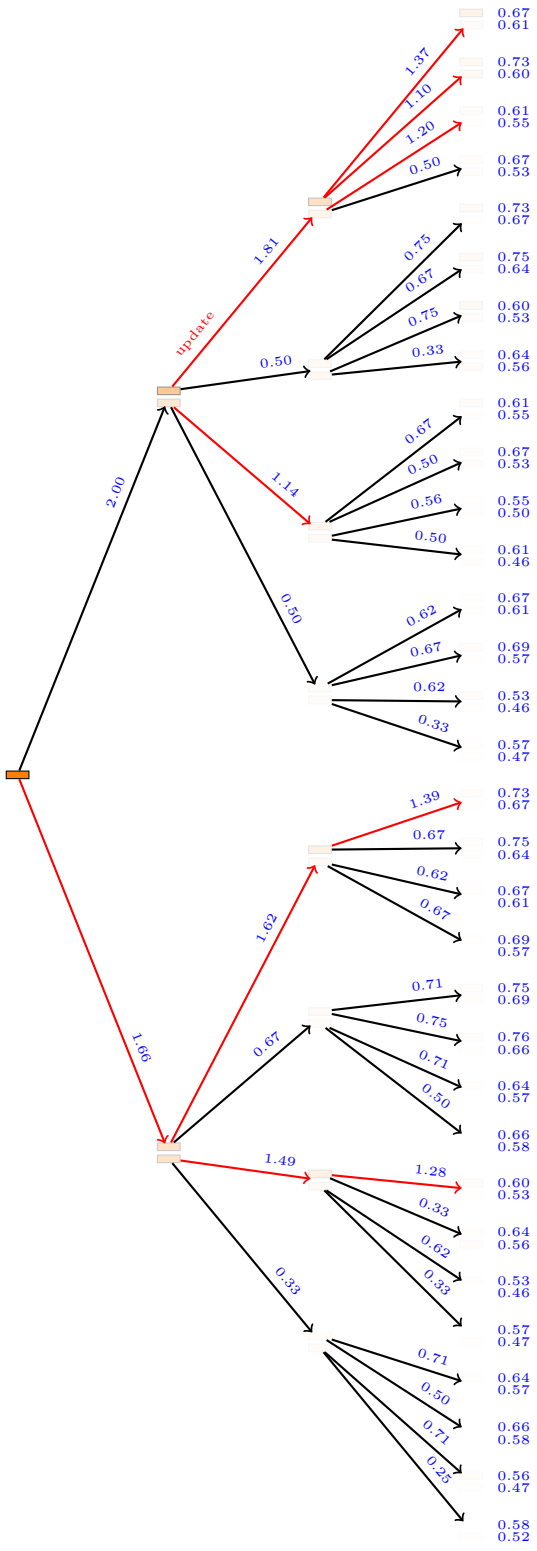

2.00
1.43
update
1.63
0.50
1.14
0.50
1.62
0.67
1.49
0.33
1.37
0.50
0.67
0.50
0.67
0.61
0.73
0.60
0.61
0.55
0.67
0.53
0.75
0.67
0.75
0.64
0.67
0.75
0.33
0.60
0.53
0.64
0.56
0.67
0.50
0.56
0.50
0.61
0.55
0.67
0.53
0.55
0.50
0.61
0.46
0.62
0.67
0.62
0.33
0.67
0.61
0.69
0.57
0.53
0.46
0.57
0.47
1.39
0.67
0.62
0.67
0.73
0.67
0.75
0.64
0.67
0.61
0.69
0.57
0.71
0.75
0.71
0.50
0.75
0.69
0.76
0.66
0.64
0.57
0.66
0.58
1.28
0.33
0.62
0.33
0.60
0.53
0.64
0.56
0.53
0.46
0.57
0.47
0.71
0.50
0.71
0.25
0.64
0.57
0.66
0.58
0.56
0.47
0.58
0.52


2.00
update
1.66
1.63
0.50
1.14
0.50
1.62
0.67
1.49
0.33
1.37
0.50
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
1.39
0.67
0.62
0.67
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52


2.00
1.66
1.63
0.50
1.14
0.50
1.62
0.67
1.49
0.33
update
1.37
1.10
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
1.39
0.67
0.62
0.67
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52


update
2.00
1.66
1.73
0.50
1.14
0.50
1.62
0.67
1.49
0.33
1.37
1.10
0.67
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
1.39
0.67
0.62
0.67
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

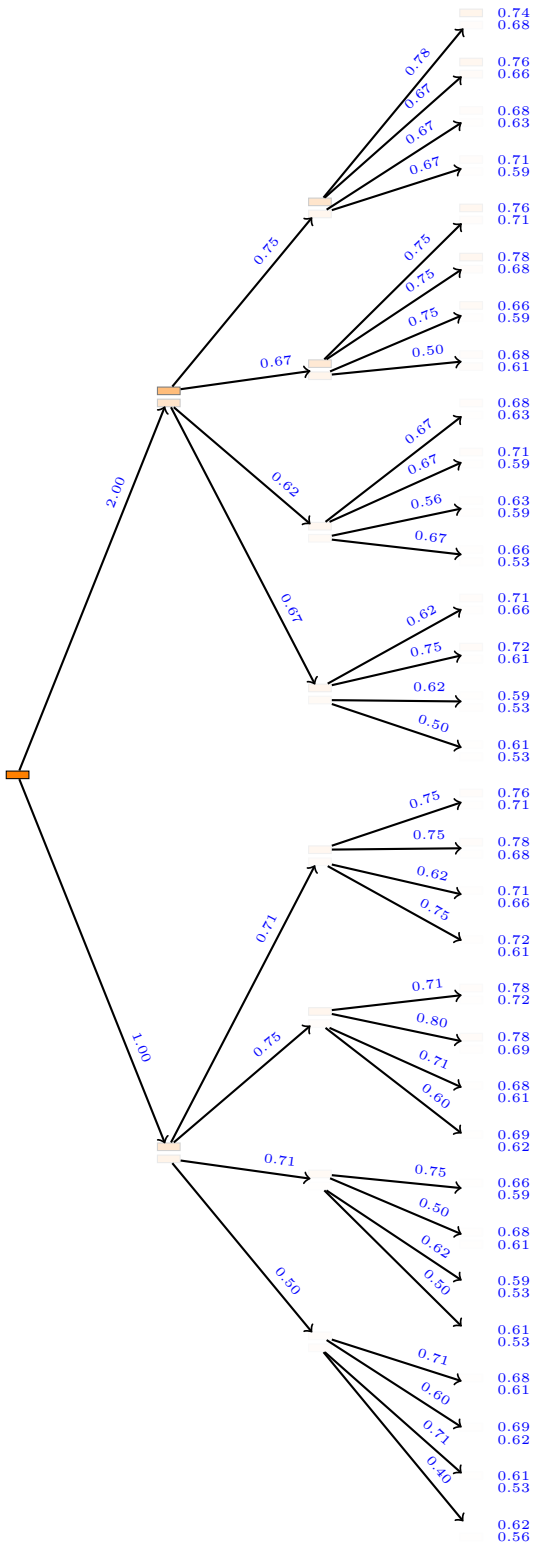

2.00
1.66
1.73
0.50
1.14
0.50
1.62
0.67
1.49
0.33
1.37
1.10
1.20
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
1.39
0.67
0.62
0.67
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

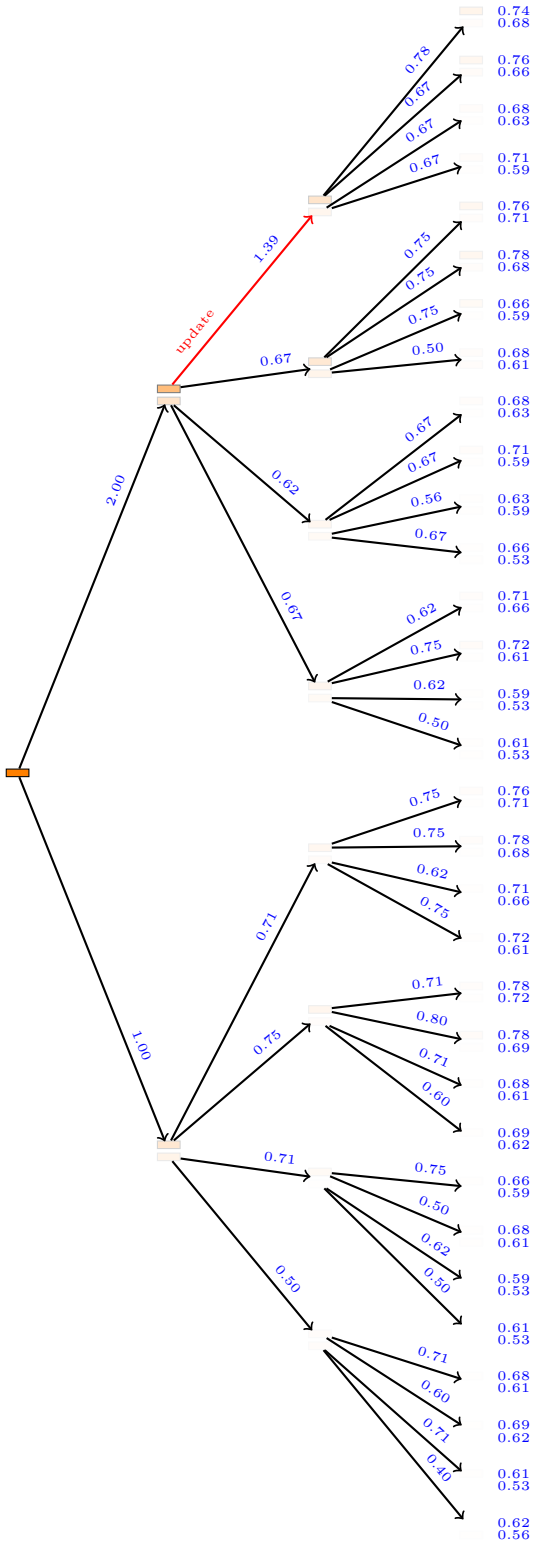

update
2.00
1.66
1.81
0.50
1.14
0.50
1.62
0.67
1.49
0.33
1.37
1.10
1.20
0.50
0.75
0.67
0.75
0.33
0.67
0.50
0.56
0.50
0.62
0.67
0.62
0.33
1.39
0.67
0.62
0.67
0.71
0.75
0.71
0.50
1.28
0.33
0.62
0.33
0.71
0.50
0.71
0.25
0.67 0.61
0.73 0.60
0.61 0.55
0.67 0.53
0.73 0.67
0.75 0.64
0.60 0.53
0.64 0.56
0.61 0.55
0.67 0.53
0.55 0.50
0.61 0.46
0.67 0.61
0.69 0.57
0.53 0.46
0.57 0.47
0.73 0.67
0.75 0.64
0.67 0.61
0.69 0.57
0.75 0.69
0.76 0.66
0.64 0.57
0.66 0.58
0.60 0.53
0.64 0.56
0.53 0.46
0.57 0.47
0.64 0.57
0.66 0.58
0.56 0.47
0.58 0.52

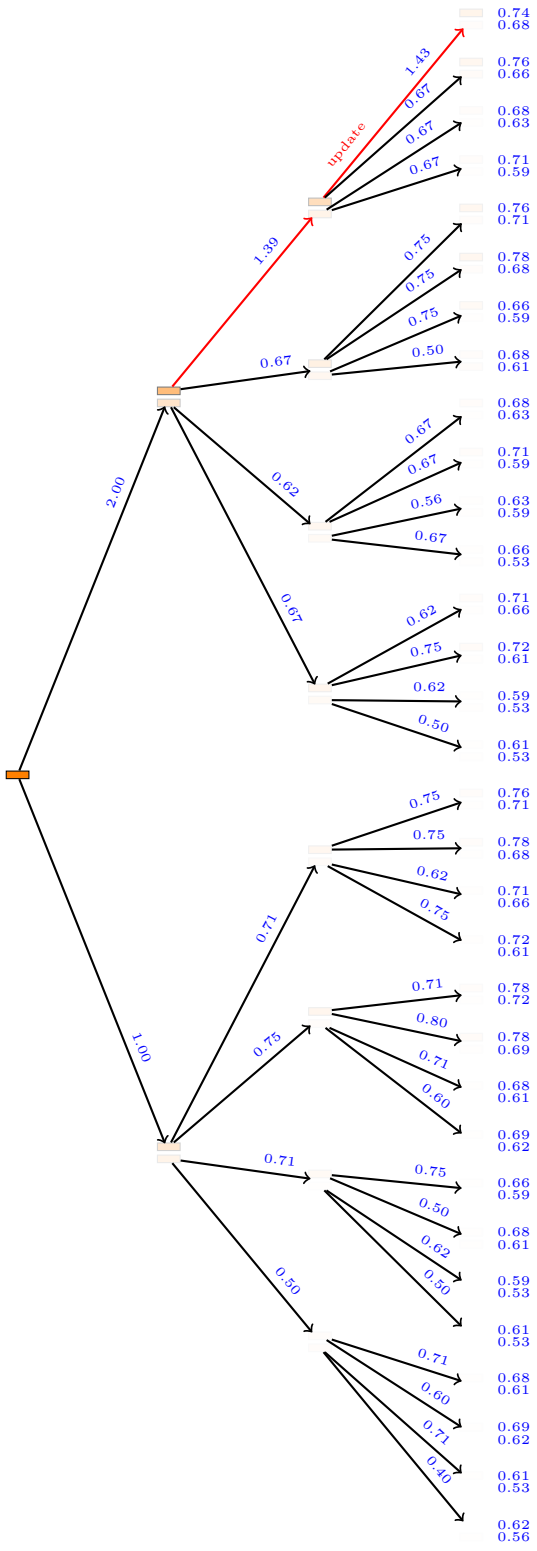
Example 2

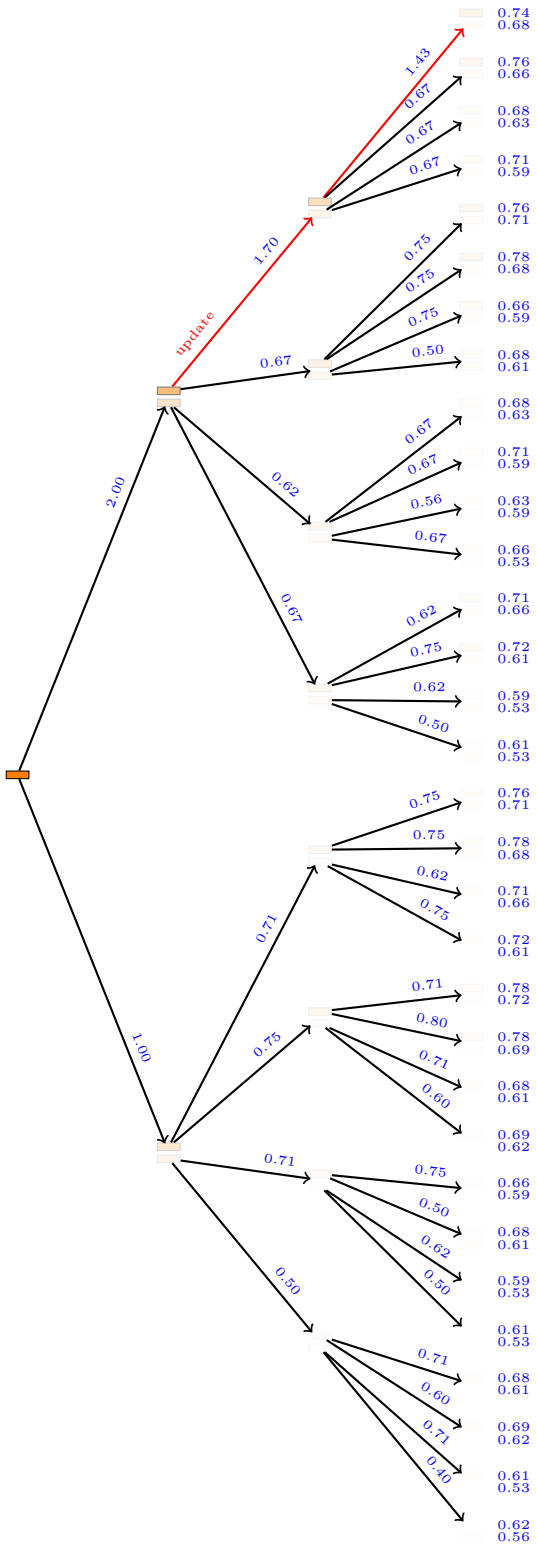
Belief at the root in this example is:

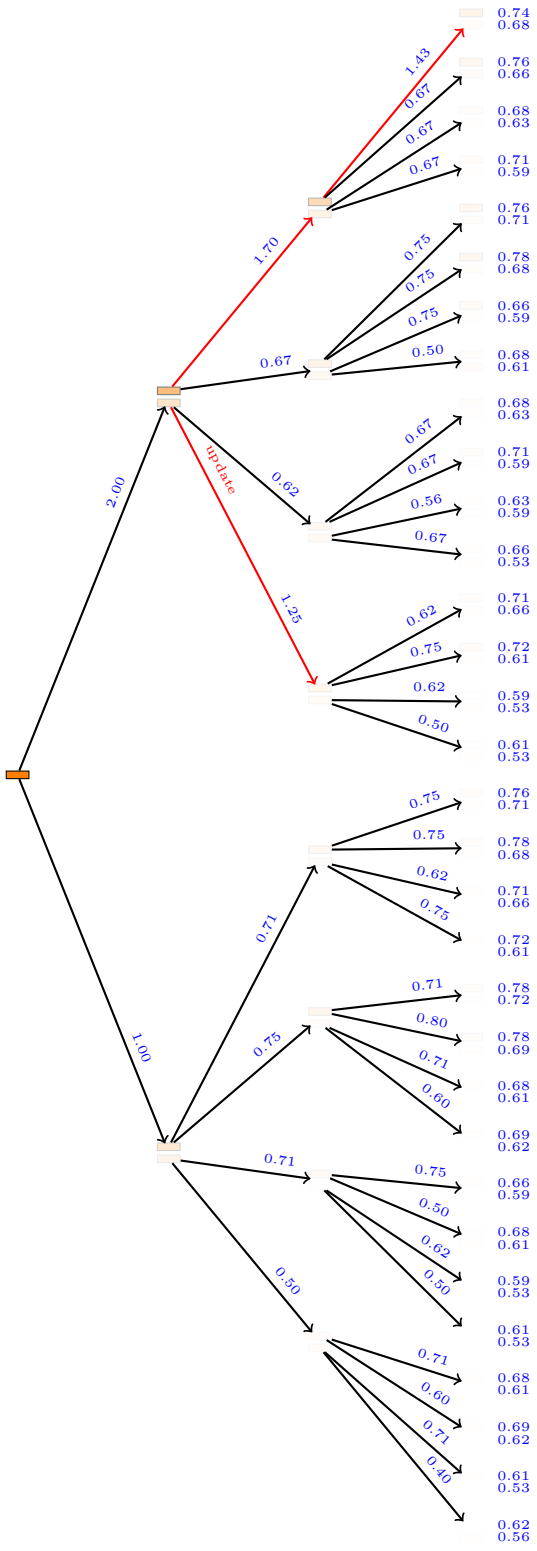
$$\alpha_0 = 5 \quad \beta_0 = 2$$
$$\alpha_1 = 2 \quad \beta_1 = 1$$

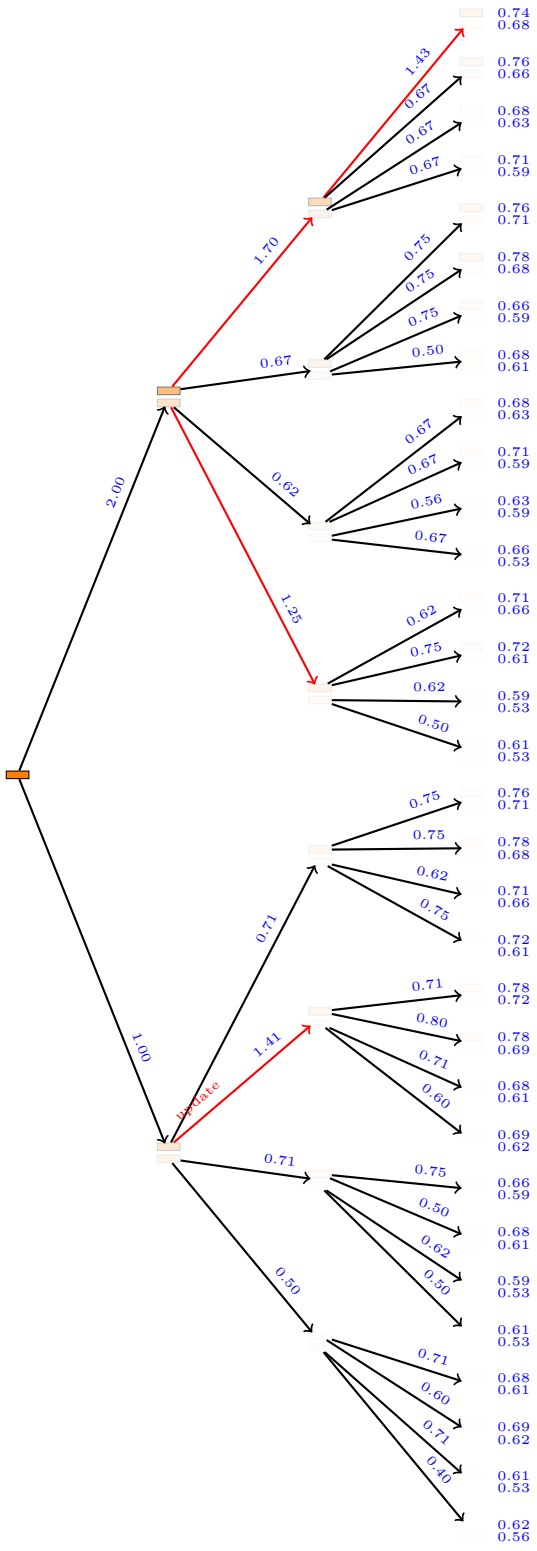

2.00
1.00
0.75
0.67
0.62
0.67
0.71
0.75
0.71
0.50
0.78
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

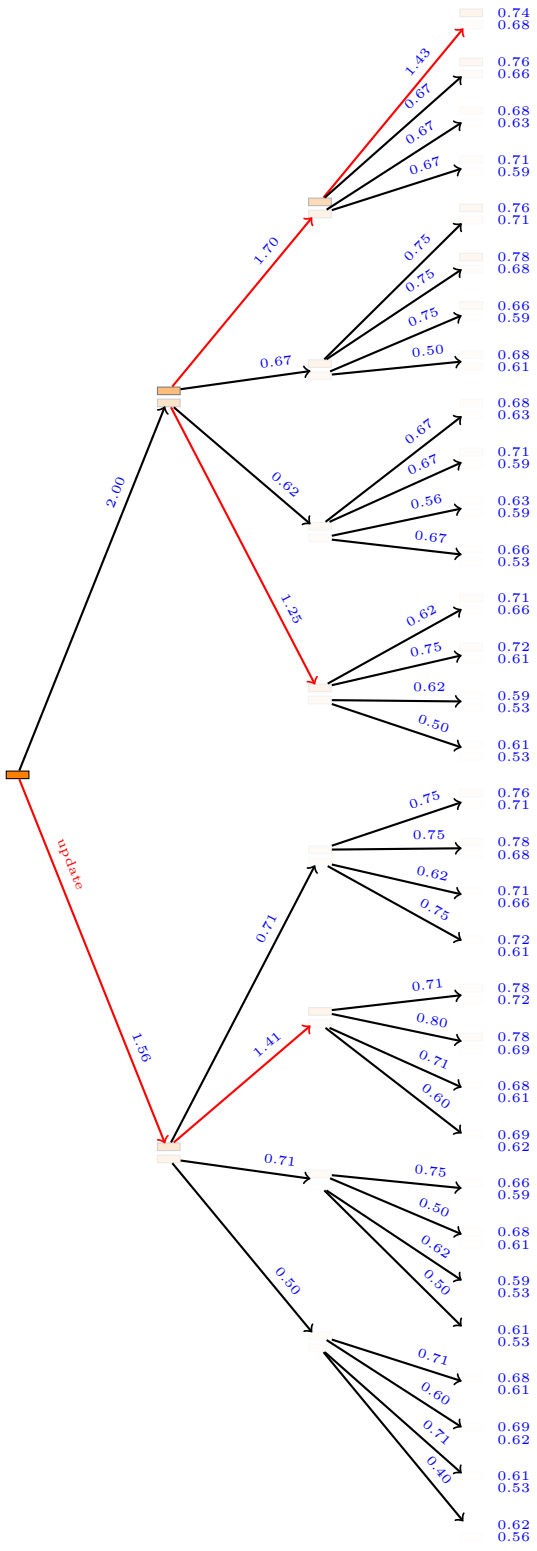

update
1.39
2.00
1.00
0.67
0.62
0.67
0.71
0.75
0.78
0.67
0.67
0.67
0.67
0.74
0.68
0.76
0.66
0.68
0.63
0.71
0.59
0.75
0.75
0.75
0.50
0.76
0.71
0.78
0.68
0.66
0.59
0.68
0.61
0.67
0.67
0.56
0.67
0.68
0.63
0.71
0.59
0.63
0.59
0.66
0.53
0.62
0.75
0.62
0.50
0.71
0.66
0.72
0.61
0.59
0.53
0.61
0.53
0.75
0.75
0.62
0.75
0.76
0.71
0.78
0.68
0.71
0.66
0.72
0.61
0.71
0.80
0.71
0.60
0.78
0.72
0.78
0.69
0.68
0.61
0.69
0.62
0.75
0.50
0.62
0.50
0.66
0.59
0.68
0.61
0.59
0.53
0.71
0.60
0.71
0.40
0.61
0.53
0.69
0.62
0.61
0.53
0.62
0.56

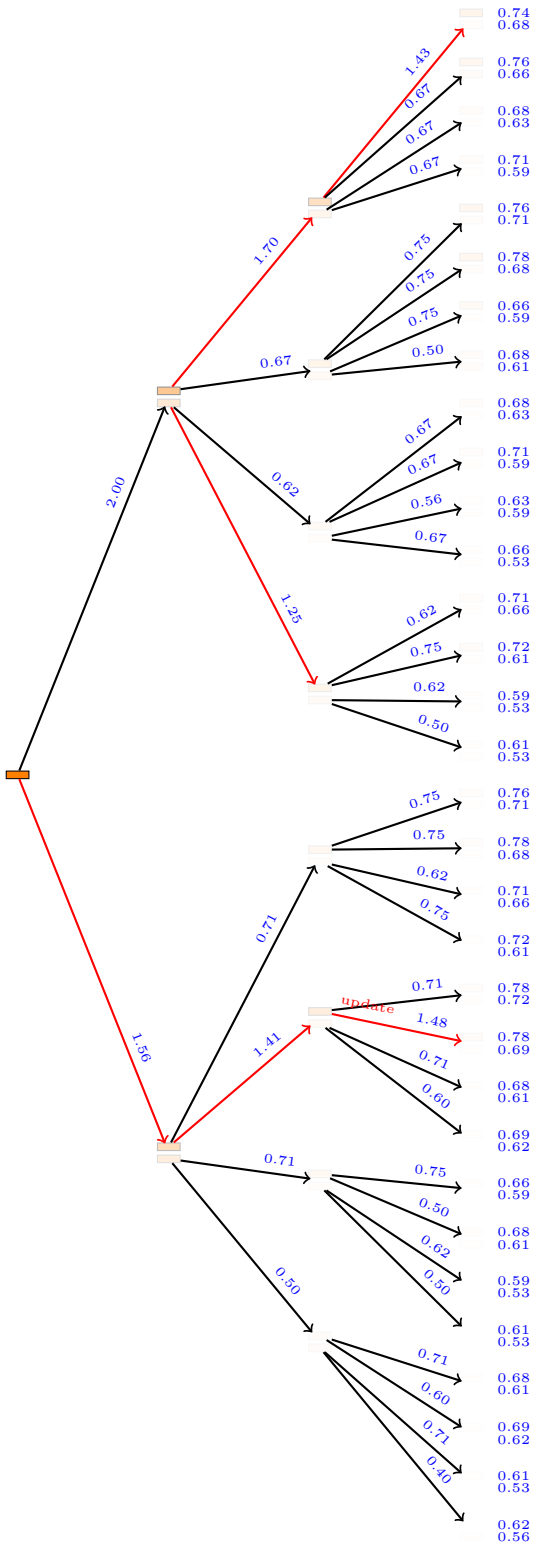

update
2.00
1.00
1.39
0.67
0.62
0.67
0.75
0.71
0.75
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

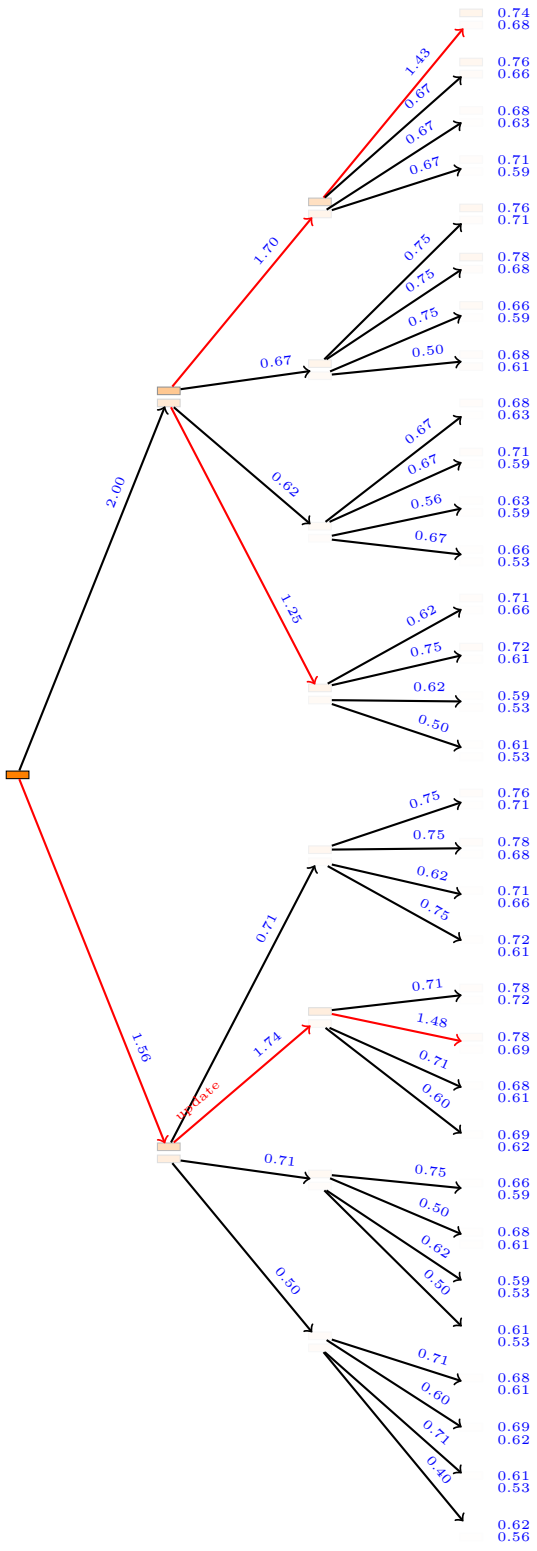

update
2.00
1.00
1.70
0.67
0.62
0.67
0.71
0.75
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

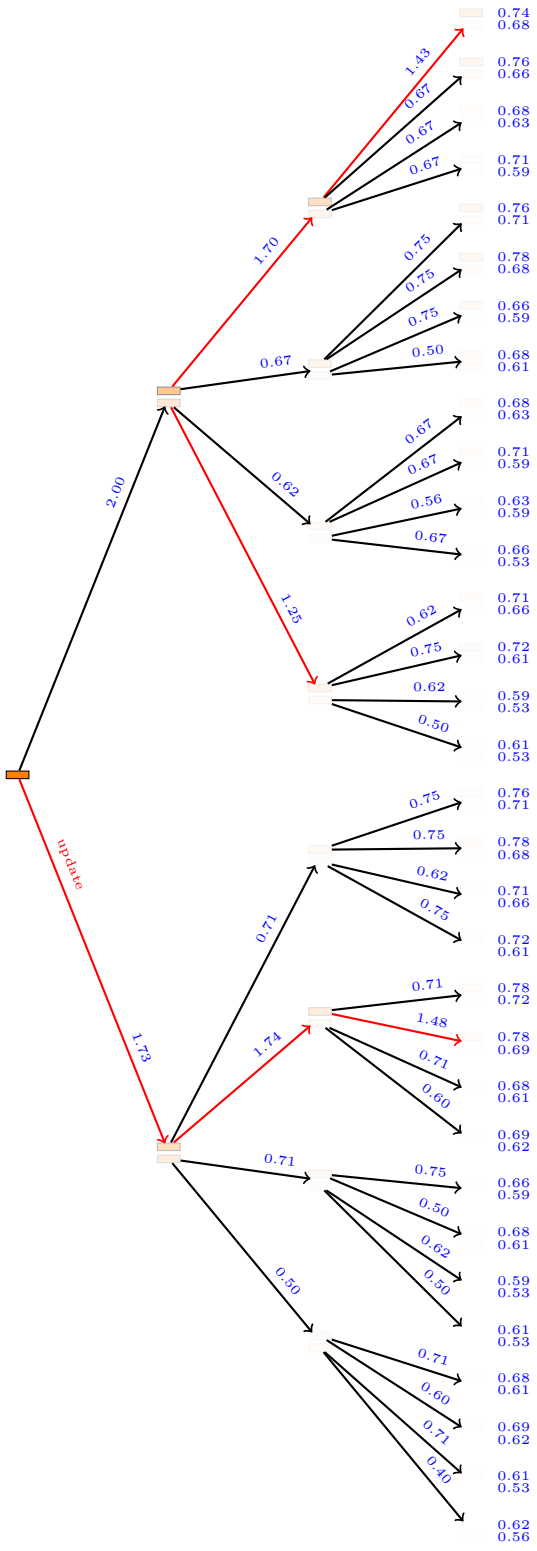

2.00
1.00
1.70
0.67
1.43
0.67
0.67
0.67
0.74
0.68
0.76
0.66
0.68
0.63
0.71
0.59
update
0.62
0.75
0.75
0.75
0.50
0.76
0.71
0.78
0.68
0.66
0.59
0.68
0.61
1.25
0.67
0.67
0.56
0.67
0.68
0.63
0.71
0.59
0.63
0.59
0.66
0.53
0.71
0.66
0.62
0.75
0.62
0.50
0.72
0.61
0.59
0.53
0.61
0.53
0.71
0.75
0.75
0.62
0.75
0.76
0.71
0.78
0.68
0.71
0.66
0.72
0.61
0.75
0.71
0.80
0.71
0.60
0.78
0.72
0.78
0.69
0.68
0.61
0.69
0.62
0.71
0.75
0.50
0.62
0.50
0.50
0.66
0.59
0.68
0.61
0.59
0.53
0.61
0.53
0.71
0.60
0.71
0.40
0.71
0.68
0.61
0.69
0.62
0.61
0.53
0.62
0.56

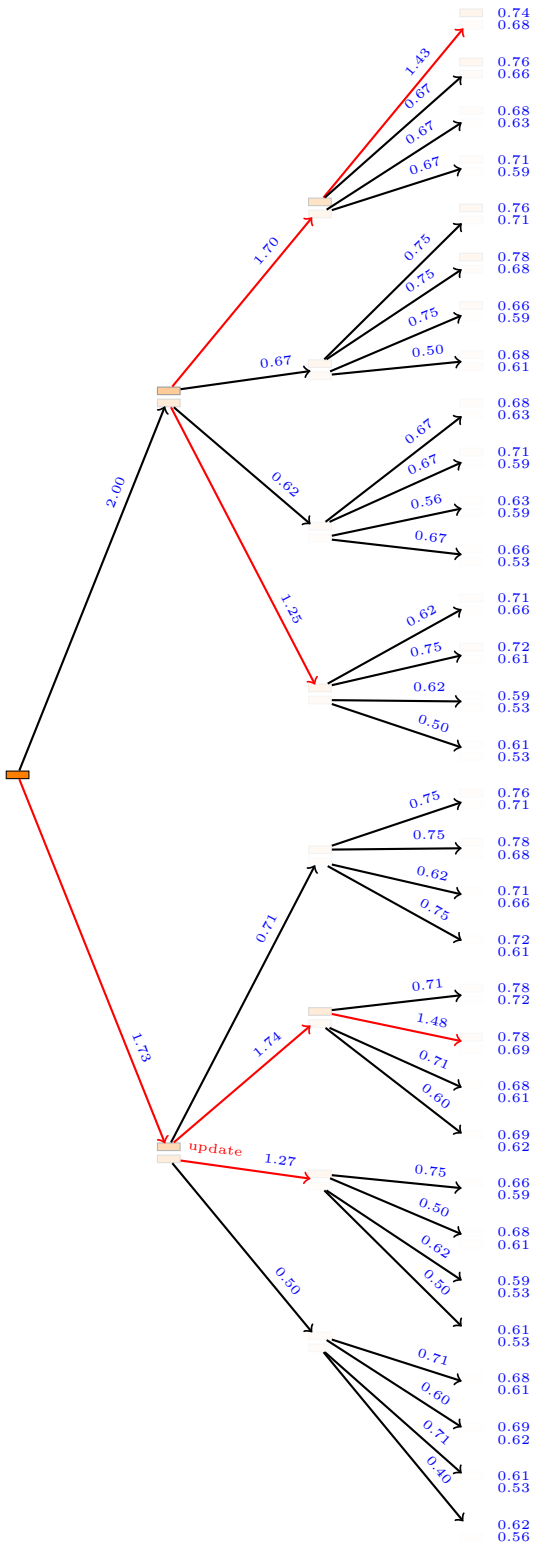

2.00
1.00
1.70
0.67
0.62
1.25
0.71
1.41
predate
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56


update
2.00
1.56
1.70
0.67
1.25
0.62
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.41
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56


2.00
1.56
1.70
0.67
0.62
1.25
1.43
0.67
0.67
0.67
0.74
0.68
0.76
0.66
0.68
0.63
0.71
0.59
0.75
0.75
0.75
0.50
0.76
0.71
0.78
0.68
0.66
0.59
0.68
0.61
0.67
0.67
0.56
0.67
0.68
0.63
0.71
0.59
0.63
0.59
0.66
0.53
0.62
0.75
0.62
0.50
0.71
0.66
0.72
0.61
0.59
0.53
0.61
0.53
0.71
0.75
0.62
0.75
0.76
0.71
0.78
0.68
0.71
0.66
0.72
0.61
1.41
update
1.48
0.71
0.71
0.60
0.78
0.72
0.78
0.69
0.68
0.61
0.69
0.62
0.71
0.50
0.75
0.50
0.62
0.50
0.66
0.59
0.68
0.61
0.59
0.53
0.61
0.53
0.71
0.60
0.71
0.40
0.71
0.68
0.61
0.69
0.62
0.61
0.53
0.62
0.56


2.00
1.56
1.70
0.67
0.62
1.25
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.74
update
0.71
1.48
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

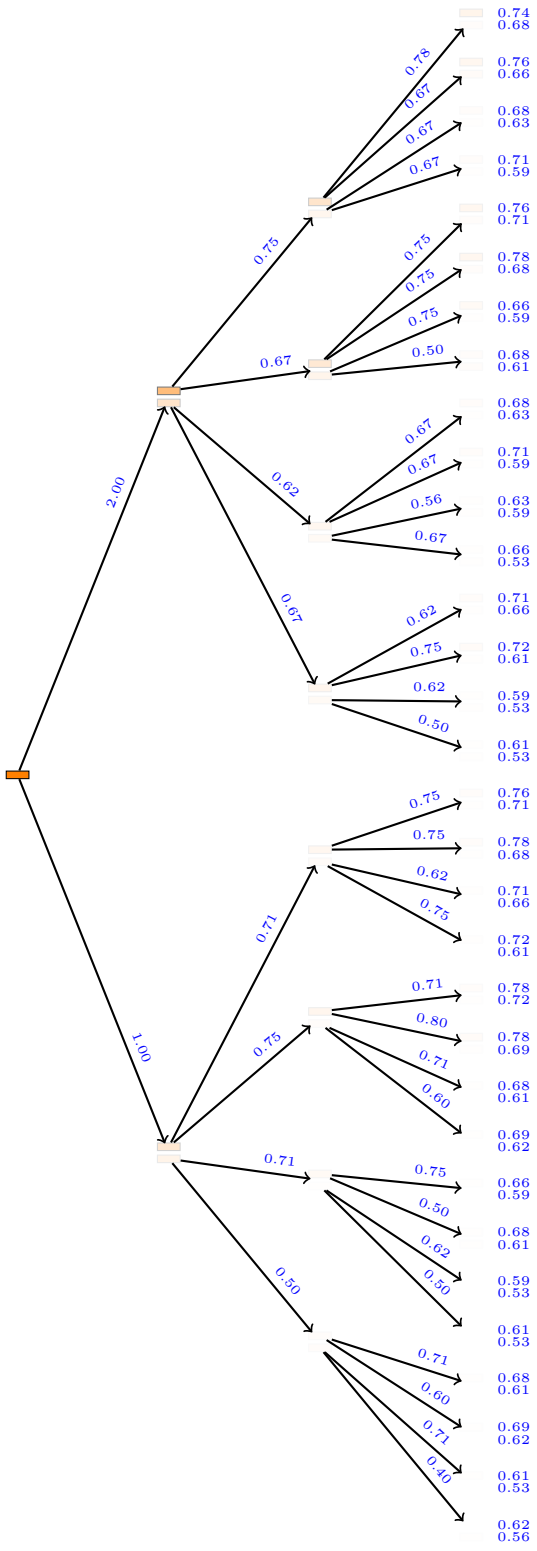

update
2.00
1.73
1.70
0.67
0.62
1.25
1.74
0.71
0.50
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.48
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

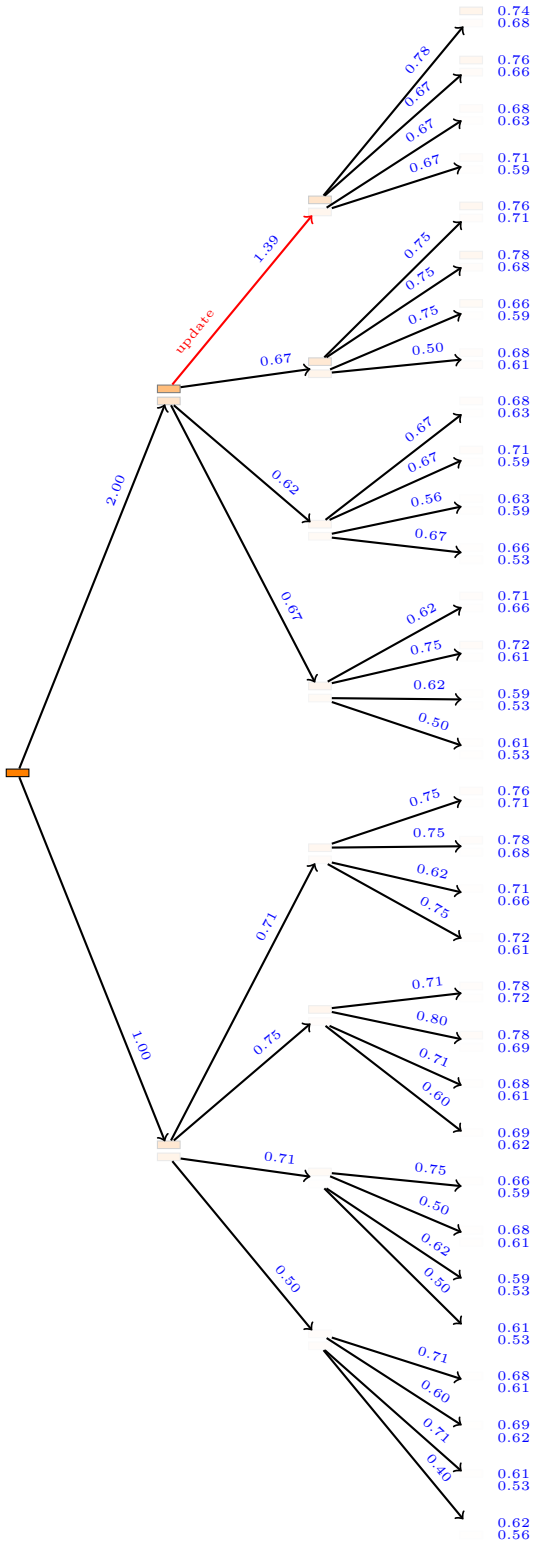

update
2.00
1.73
1.70
0.67
0.62
1.25
0.71
1.74
1.27
0.50
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.48
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

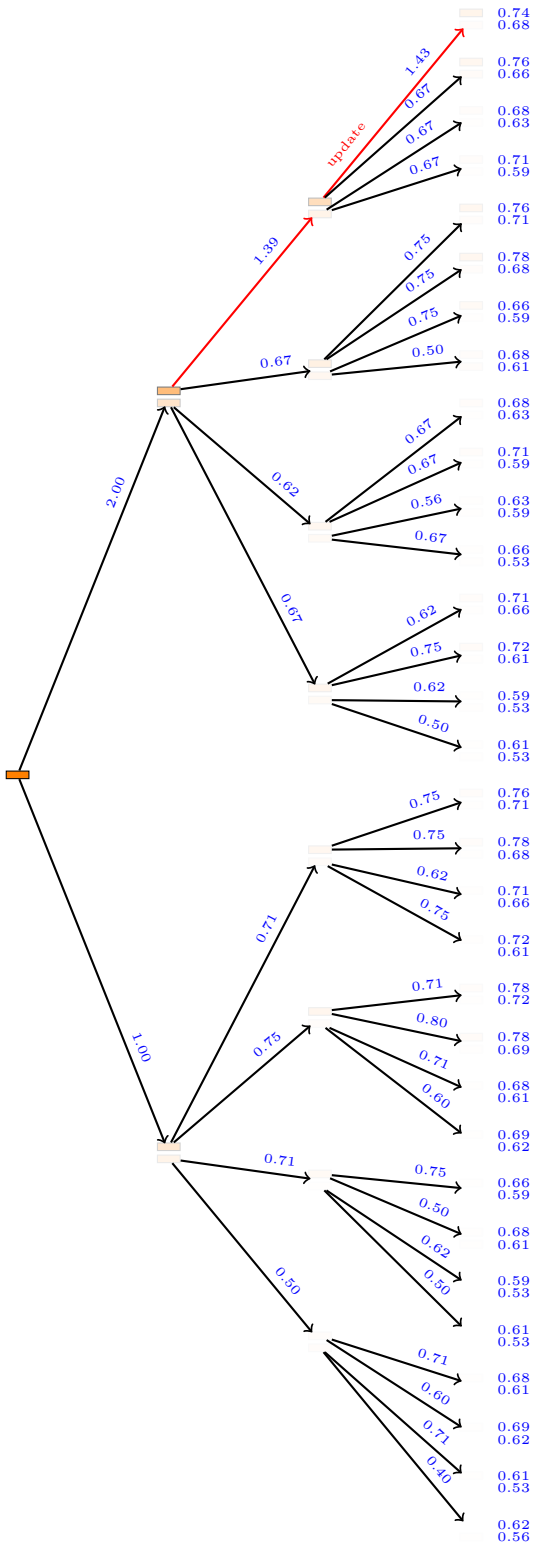
Example 3

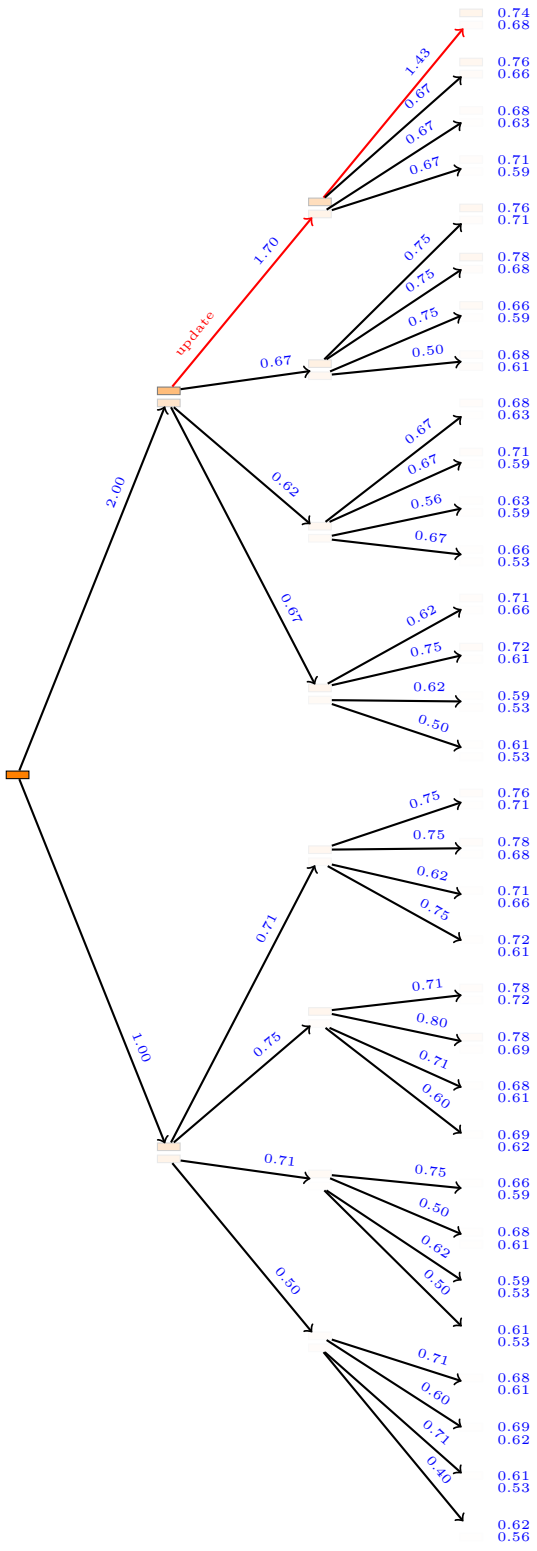
Belief at the root in this example is:

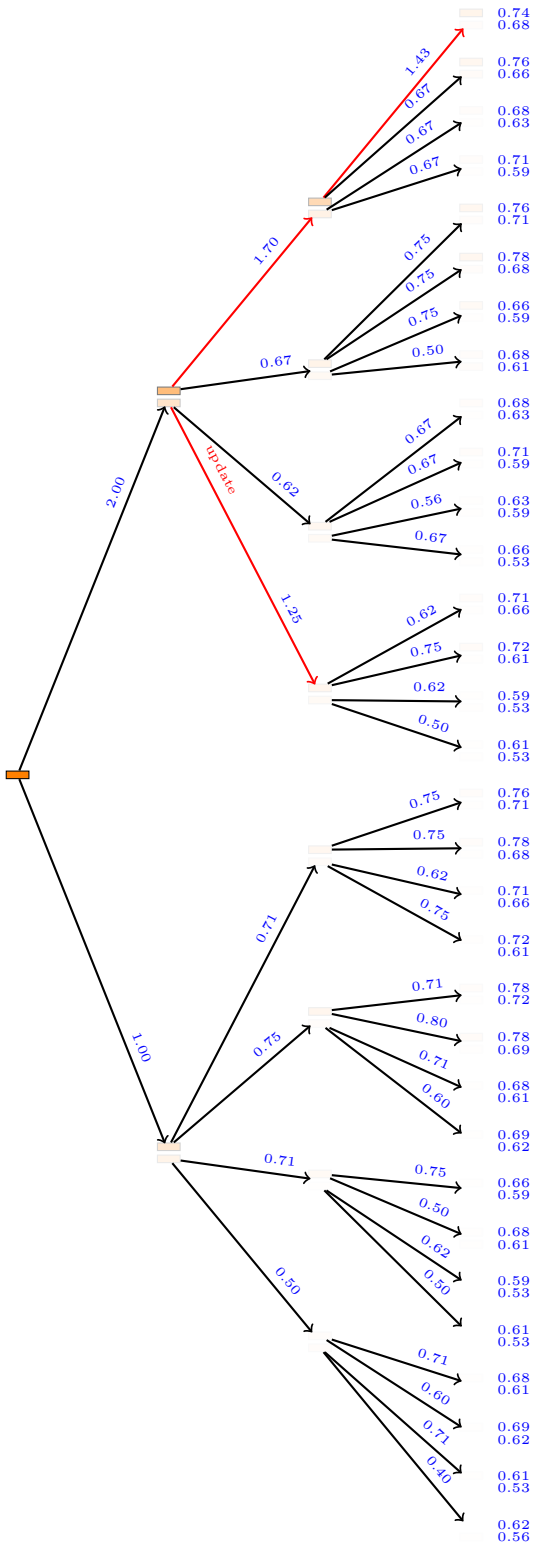
$$\begin{array}{ll} \alpha_0 = 10 & \beta_0 = 4 \\ \alpha_1 = 2 & \beta_1 = 1 \end{array}$$

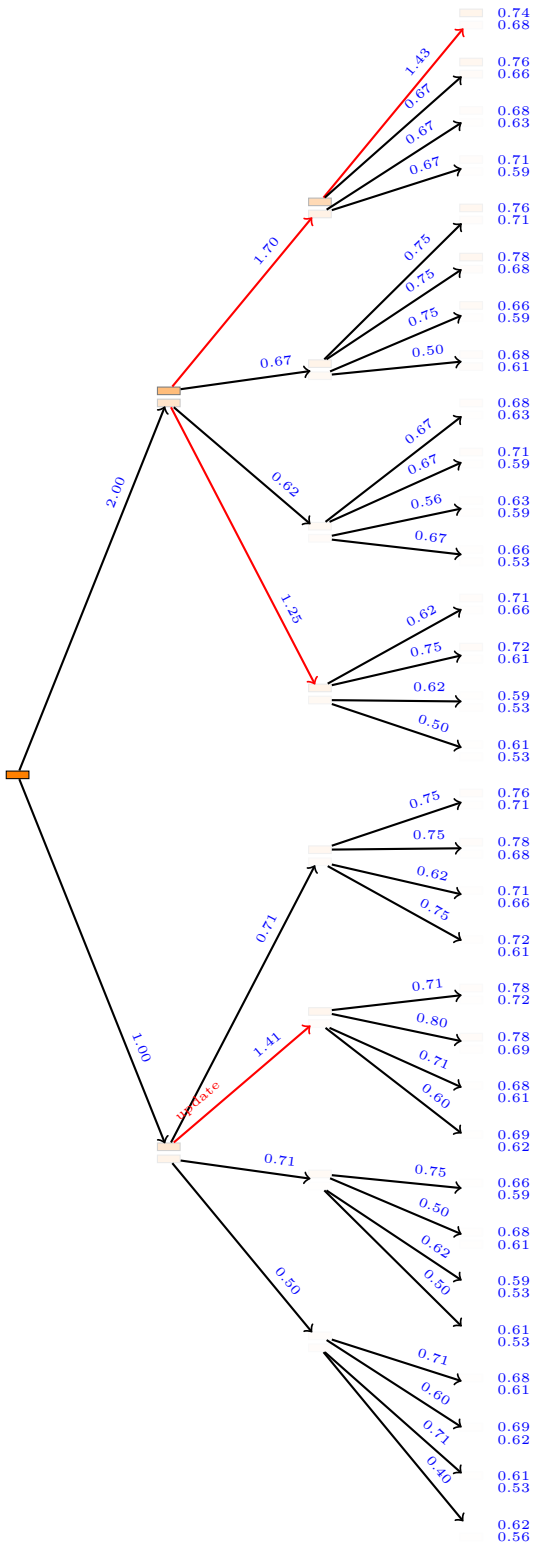

2.00
1.00
0.75
0.67
0.62
0.67
0.71
0.75
0.71
0.50
0.78
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

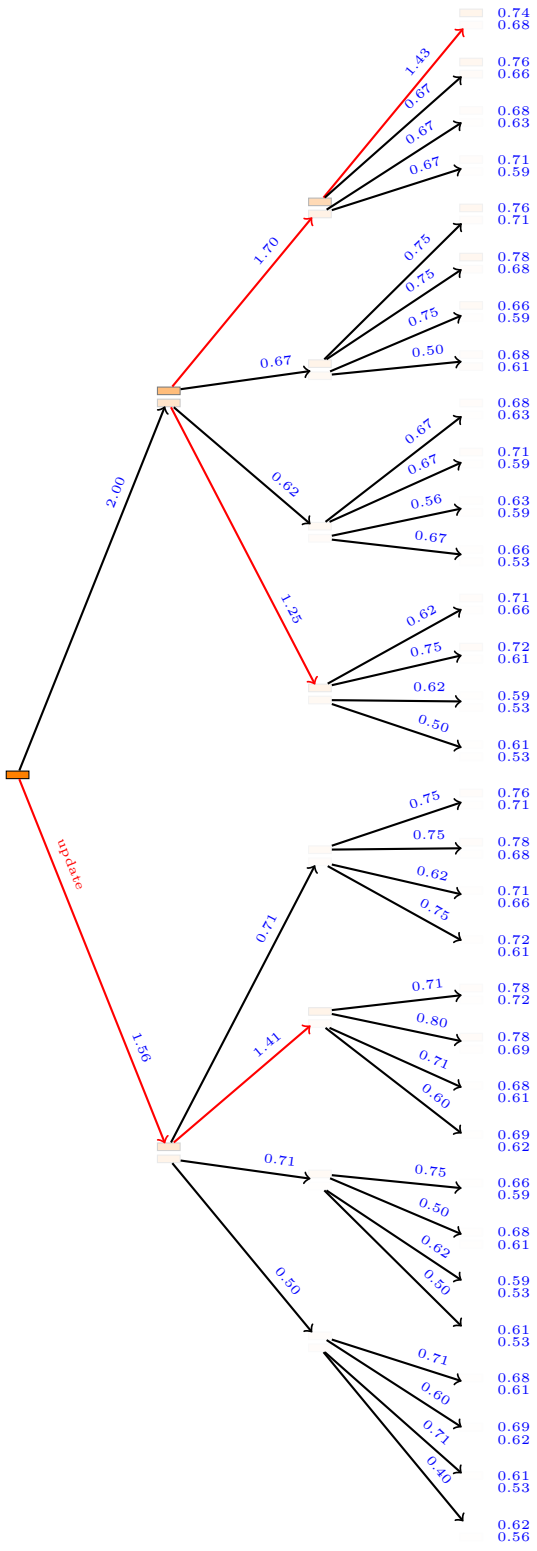

update
2.00
1.00
1.39
0.67
0.62
0.67
0.71
0.75
0.78
0.67
0.67
0.67
0.74
0.68
0.76
0.66
0.68
0.63
0.71
0.59
0.75
0.75
0.75
0.50
0.76
0.71
0.78
0.68
0.66
0.59
0.68
0.61
0.67
0.67
0.56
0.67
0.68
0.63
0.71
0.59
0.63
0.59
0.66
0.53
0.62
0.75
0.62
0.50
0.71
0.66
0.72
0.61
0.59
0.53
0.61
0.53
0.75
0.75
0.62
0.75
0.76
0.71
0.78
0.68
0.71
0.66
0.72
0.61
0.71
0.80
0.71
0.60
0.78
0.72
0.78
0.69
0.68
0.61
0.69
0.62
0.75
0.50
0.62
0.50
0.66
0.59
0.68
0.61
0.59
0.53
0.61
0.53
0.71
0.60
0.71
0.40
0.69
0.62
0.61
0.53
0.62
0.56

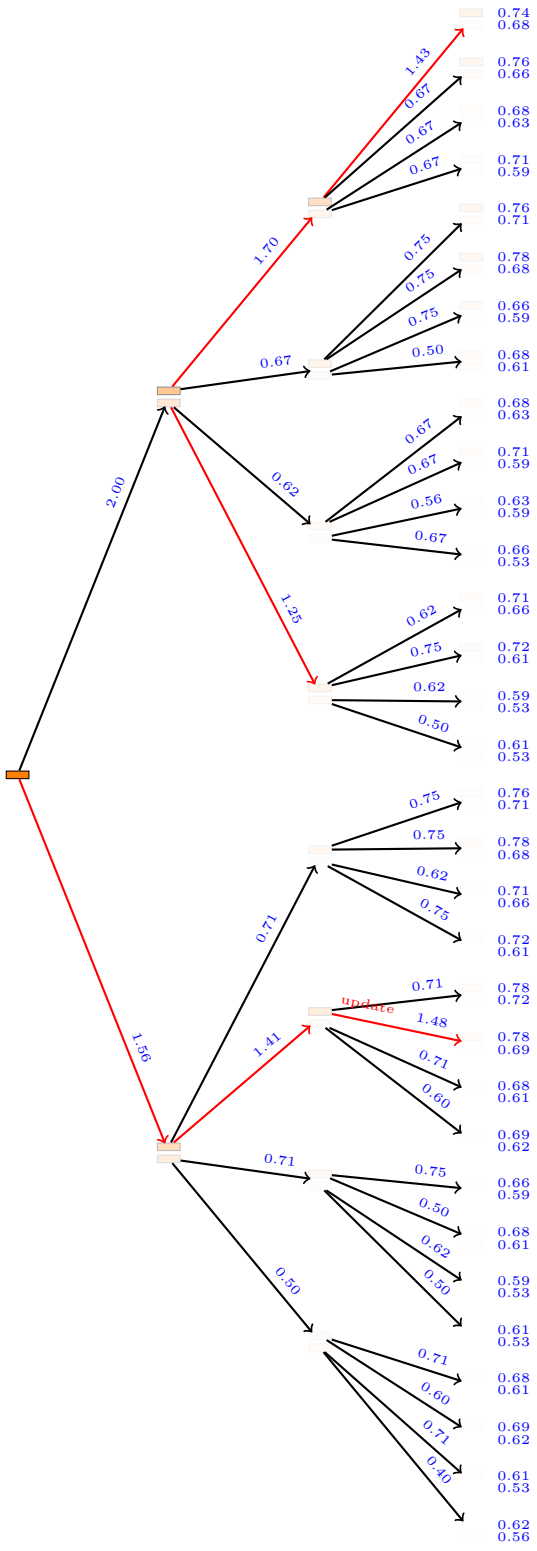

update
2.00
1.00
1.39
0.67
0.62
0.67
0.71
0.75
0.71
0.75
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

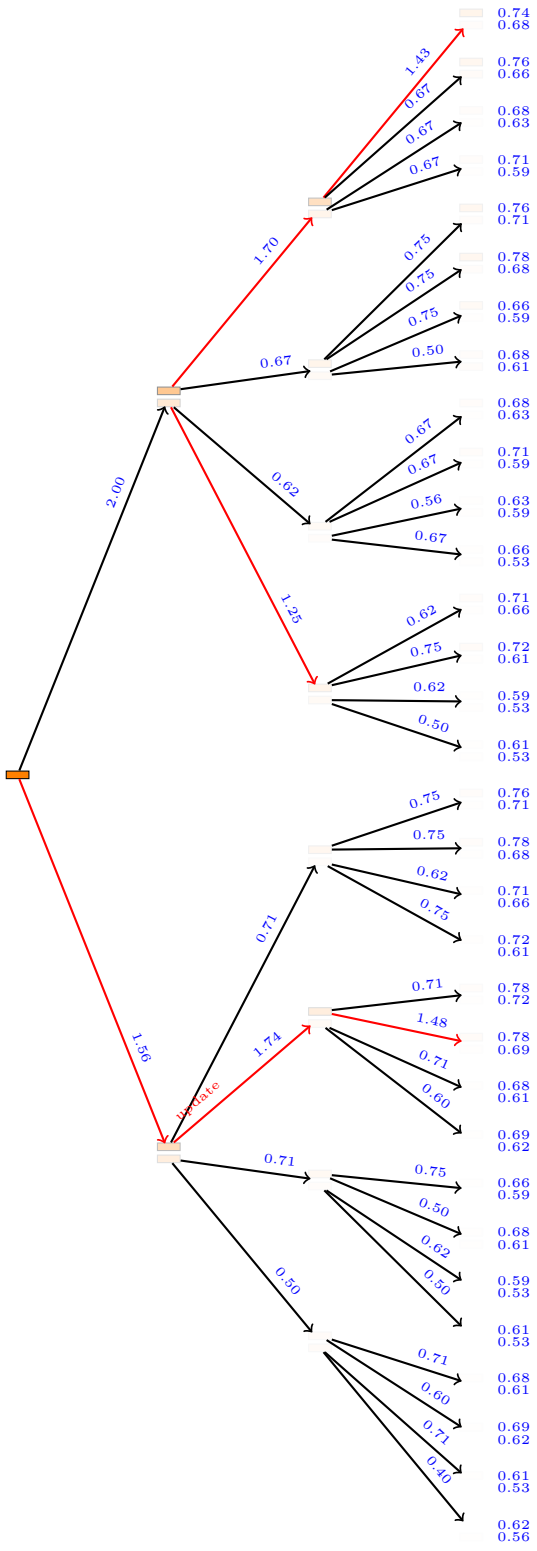

update
2.00
1.00
1.70
0.67
0.62
0.67
0.71
0.75
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56

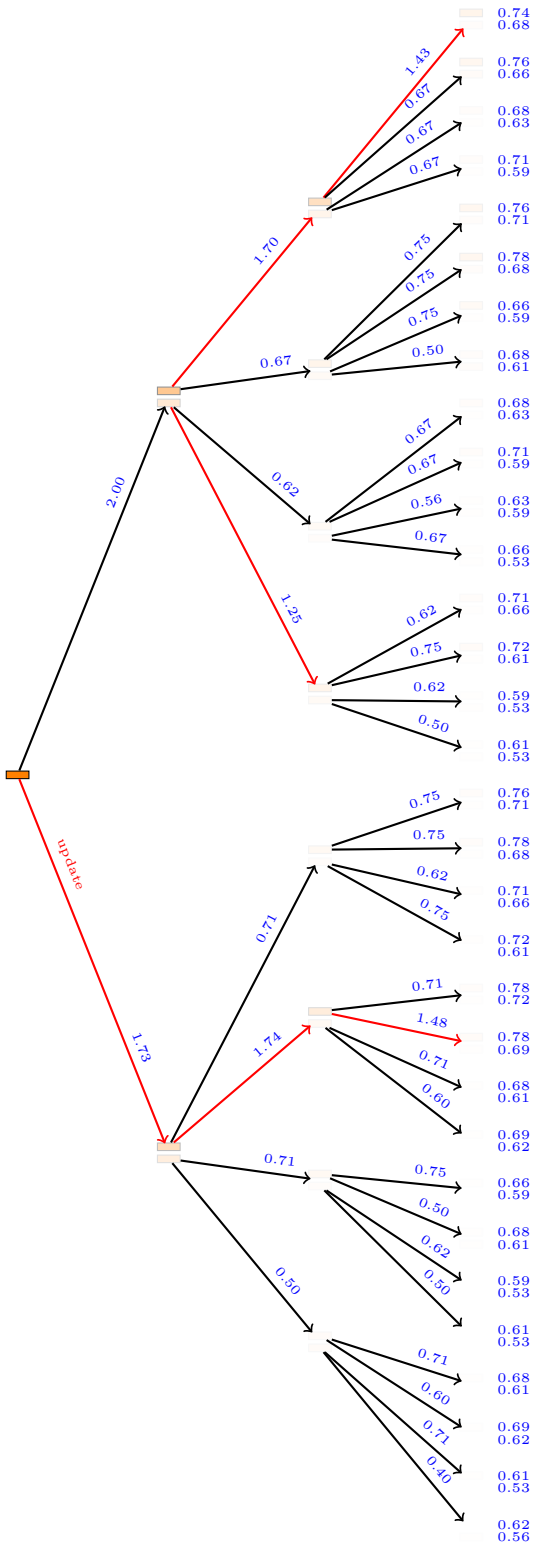

2.00
1.00
1.70
0.67
update
1.25
0.62
1.43
0.67
0.67
0.67
0.74
0.68
0.76
0.66
0.68
0.63
0.71
0.59
0.75
0.75
0.75
0.50
0.76
0.71
0.78
0.68
0.66
0.59
0.68
0.61
0.67
0.67
0.56
0.67
0.68
0.63
0.71
0.59
0.63
0.59
0.66
0.53
0.62
0.75
0.62
0.50
0.71
0.66
0.72
0.61
0.59
0.53
0.61
0.53
0.71
0.75
0.62
0.75
0.75
0.71
0.80
0.71
0.60
0.76
0.71
0.78
0.68
0.71
0.66
0.72
0.61
0.78
0.72
0.78
0.69
0.68
0.61
0.69
0.62
0.75
0.50
0.62
0.50
0.71
0.50
0.66
0.59
0.68
0.61
0.59
0.53
0.61
0.53
0.71
0.60
0.71
0.40
0.68
0.61
0.69
0.62
0.61
0.53
0.62
0.56

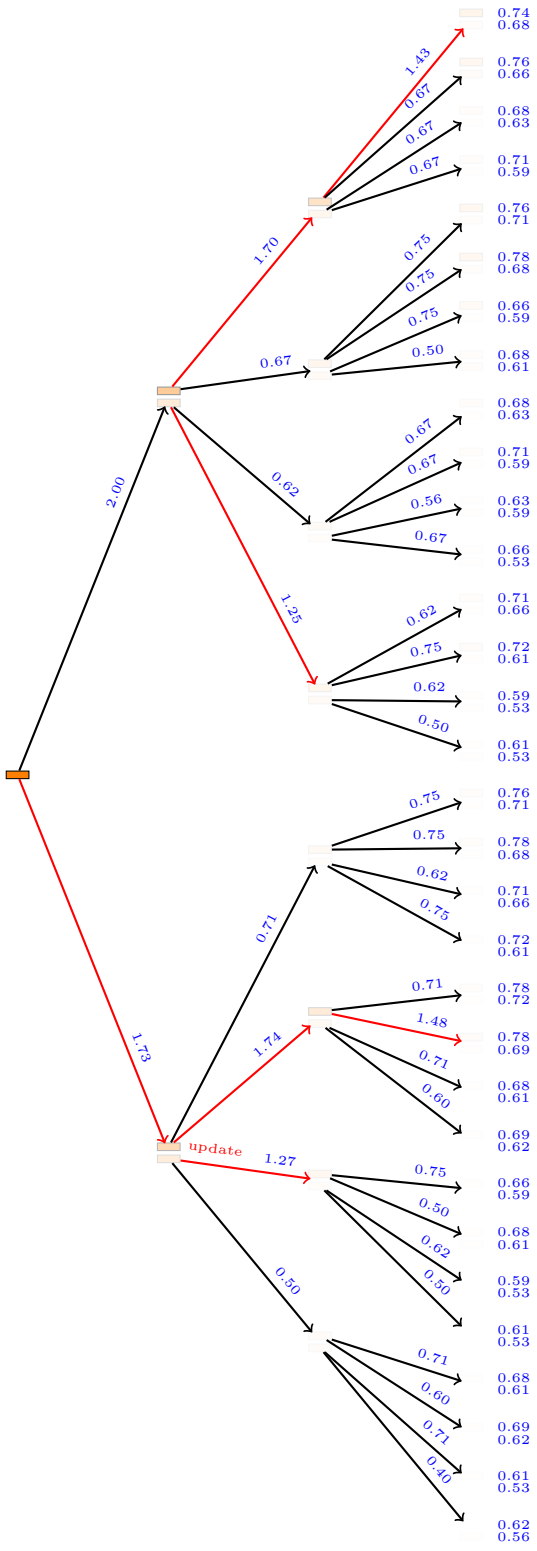

2.00
1.00
1.70
0.67
0.62
1.25
0.71
1.41
update
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
0.80
0.71
0.60
0.71
0.75
0.50
0.62
0.50
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56


2.00
update
1.56
1.70
0.67
0.62
1.25
1.43
0.67
0.67
0.67
0.74
0.68
0.76
0.66
0.68
0.63
0.71
0.59
0.75
0.75
0.75
0.50
0.76
0.71
0.78
0.68
0.66
0.59
0.68
0.61
0.67
0.67
0.56
0.67
0.68
0.63
0.71
0.59
0.63
0.59
0.66
0.53
0.62
0.75
0.62
0.50
0.71
0.66
0.72
0.61
0.59
0.53
0.61
0.53
0.71
0.75
0.62
0.75
0.76
0.71
0.78
0.68
0.71
0.66
0.72
0.61
0.71
0.80
0.71
0.60
0.78
0.72
0.78
0.69
0.68
0.61
0.69
0.62
0.71
0.50
0.75
0.50
0.62
0.50
0.66
0.59
0.68
0.61
0.59
0.53
0.61
0.53
0.71
0.60
0.71
0.40
0.69
0.62
0.61
0.53
0.62
0.56


2.00
1.56
1.70
0.67
0.62
1.25
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.41
update
1.48
0.71
0.71
0.60
0.71
0.50
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56


2.00
1.56
1.70
0.67
0.62
1.25
0.71
1.74
0.71
0.50
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.48
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
update
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56


update
2.00
1.73
1.70
0.67
0.62
1.25
0.71
1.74
0.71
0.50
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.48
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56


2.00
1.73
1.70
0.67
1.25
0.62
1.43
0.67
0.67
0.67
0.75
0.75
0.75
0.50
0.67
0.67
0.56
0.67
0.62
0.75
0.62
0.50
0.75
0.75
0.62
0.75
0.71
1.74
update
1.27
0.50
0.71
1.48
0.71
0.60
0.75
0.50
0.62
0.50
0.71
0.60
0.71
0.40
0.74 0.68
0.76 0.66
0.68 0.63
0.71 0.59
0.76 0.71
0.78 0.68
0.66 0.59
0.68 0.61
0.68 0.63
0.71 0.59
0.63 0.59
0.66 0.53
0.71 0.66
0.72 0.61
0.59 0.53
0.61 0.53
0.76 0.71
0.78 0.68
0.71 0.66
0.72 0.61
0.78 0.72
0.78 0.69
0.68 0.61
0.69 0.62
0.66 0.59
0.68 0.61
0.59 0.53
0.61 0.53
0.68 0.61
0.69 0.62
0.61 0.53
0.62 0.56