# Introduction to Reversing with Z3 RPISEC

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## Overview

- What are SAT/SMT/Z3?
- Solving MBE lab1A with Z3
- Solving a Cyberseed RE challenge with Z3

## What is SAT?

- SAT is the boolean SATisfiability problem
- e.g. "Does the formula  $(x \lor \neg y \lor z) \land (\neg x \lor y)$  have a satisfying assignment?"
  - $(\neg, \land, \lor)$  mean (NOT, AND, OR)
- Brute forceable in  $O(2^n)$  by trying all combinations of  $\{0,1\}$  for all variables
- NP-Complete
  - Not known to be subexponentially solvable in general
  - Many problems expressible as SAT

#### What is SMT?

- SMT is Satisfiability Modulo Theories
- ▶ "Does  $(f(x,y) \lor z) \land (\neg g(x) = f(x,x))$  have a satisfying assignment?" (QF-EUF)
- ▶ "Does  $(2*x+y \le z) \land (x+3*y \ge z)$  have a satisfying assignment" (QF-LIA)
- Allows more compact translation of problems, e.g.
  - $x = 1 \lor x = 2 \lor x = 3 \lor ... \lor x = 99 \lor x = 100 \text{ (SAT)}$
  - ▶  $1 \le x \land x \le 100$  (SMT)
- ► Also NP-Complete

# Why are SAT/SMT useful if they're hard to solve quickly?

- Proton of the control of the control
- ▶ Not all problems are as hard as the hardest ones
  - ▶ 2-SAT (each clause having at most 2 variables) is polytime solvable
  - ▶ Monotone circuits (only ANDs and ORs, no NOTs) are polytime solvable
- It's often possible to prune the search space
  - e.g.  $x \lor \varphi(a, b, c, ...)$  is solvable regardless of  $\varphi$  because x = 1 cancels out that subterm
- ► Algorithms like DPLL and CDCL make use of partial structure to solve some instances faster than others
- ► SMT can make use of the rules for the extra types of symbols to prune the search space at a higher level

## What is Z3?

```
initis. Boods[NUMPRINES]:

N.ULONG delta:

N.ULONG delta:

N.ULONG modelta = IN.NGSK2 - primes[NUMPRINES - 1]:

char is_single_word = bits <= INLBITS2;

gmin:

if (INM_rand(rnd, bits, INLBNND_TOP_TMO, INLBNND_BOTTOH_ODD))

/** we now have a random number 'rnd' to test, */

for (= 1 : K.NHERINES): i*)

if (mod = C. S. Hubble abord(rnd, (INLULONG))primes[i]):

if (mod = C. S. Hubble abord(rnd, (INLULONG))primes[i]):

nods[i] = (wintin_t)mod;

** If hits is no small that it fits into a single word then we w additionally don't wont to exceed that many bits. */

** (is_single_word).
```

- ► SAT & SMT solver developed and maintained by Microsoft Research
- Libre and Open Source (MIT Licensed)
- ▶ C++, with python bindings (pip install z3-solver)
- Based on the CDCL algorithm

## Using Z3 on small examples

```
\blacktriangleright (x \lor \neg y \lor z) \land (\neg x \lor y)
    import z3
    solver = z3.Solver()
    x, y, z = z3.Bools('x y z')
    solver.add(z3.And(z3.Or(x, z3.Not(y), z), z3.Or(z3.Not(x), y)))
    if solver.check().r == 1:
        print(solver.model())
   (2 * x + y \le z) \land (x + 3 * y \ge z) \land (z > 1)
    import z3
    solver = z3.Solver()
    x, y, z = z3.Ints('x y z')
    solver.add(2*x+y \le z)
    solver.add(x+3*y >= z)
    solver.add(z > 1)
    if solver.check().r == 1:
        print(solver.model())
```

## MBE Lab1A - Just Running It

```
int 1:
uinti6_t mode[NUMPRIMES]
BN_ULONG delta:
BN_ULONG maxdelta = BN_MASK2 - primes[NUMPRIMES -
class is sincle mod = bits <= BN_BITS?
```

```
avi@aweinstock-debian-ii:"/Documents/cloned-repos/MBE/src/lab01$ ./lab1A
  SECURE LOGIN SYS v. 3.0 +
~- Enter your Username:
username
   Input your serial:
password
avi@aweinstock-debian-ii:"/Documents/cloned-repos/MBE/src/lab01$ echo $?
```

## MBE Lab1A - Username Entry

```
0×08048569
                c70424738d04.
                               mov dword [esp], str...
                e89bfc
                                call sum.imp.puts
0×08048575
                c70424918d04.
                                mov dword [esp], str_RPISEC
                e88ffc
                                call sum, imp.puts
0×08048h81
                c70424af8d04.
                               mov dword [esp], str.SECURE_LOGIN_SYS_v._3.0
0×08048588
                e883fc
                                call sum, imp. puts
0×0804858d
                c70424cd8d04.
                               mov dword [esp], str.
                e877fc
                                call sum, imp, puts
                                mov dword [esp], str.Enter_your_Username:
0x08048b99
                c70424eb8d04.
0×08048ha0
                e86bfcf
                                call sum imp puts
0v08048ha5
                c70424098e04.
                               mov dword [esp], str.
                e85ffcf
                                call sym.imp.puts
0x08048bb1
                a160b00408
                                mov eax, dword [obj.stdin]
                89442408
                                mov dword [
                                                    . eax
0x08048bba
                c74424042000.
                               mov dword [
                                                     0x20
0x08048bc2
                8d44241c
                                lea eax. []
0x08048bc6
                890424
                                mov dword [esp], eax
0x08048bc9
                e802fc
                                call sum, imp.fgets
                                                                                                                                                5000
```

## MBE Lab1A - Serial Entry

```
mov dword [esp], str.,
0x08048bd5
              e836fc
                            call sum, imp. puts
0x08048bda
              c70424278e04.
                            mov dword [esp], str.NEW ACCOUNT DETECTED
0x08048he1
              e82afcf
                            call sum_imp_puts
0x08048he6
              c70424cd8d04.
                            mov dword [esp], str.
0x08048bed
              e81efc
                            call sum.imp.puts
0x08048bf2
              c70424458e04.
                            mov dword [esp], str.Input your serial:
              e812fc
0.08048569
                            call sum, imp. puts
              c70424098e04.
                            mov dword [esp], str.
0x08048c05
              e806fc
                            call sum.imp.puts
              8d442418
0x08048c0e
              89442404
0x08048c12
              c70424008d04.
0x08048c19
              e842fc
                                                                                       E F 0123456789ABCDEF
                                                                          В
                                                                               C D
                     2575 000a
                                                 0000 1b5b 3332 6d2e 2d2d
```

900

# MBE Lab1A - Calling the authentication routine and the second results as British as Brit

again:
if (|BN\_rand(rnd, bits, BN\_RAND\_TOP\_TWO, BN\_RAND\_BOTTOM\_ODD)) {
 return 0;

```
86442418
                                    mov eax, dword [local 18h]
    0x08048c22
                     89442404
                                     mov dword []
    0x08048c26
                     8d44241c
                                     lea eax. []
    0x08048c2a
                     890424
                                     mov dword [esp], eax
    0x08048c2d
                     e8ddfd
                                     call sum.auth
    0x08048c32
                     85c0
                                     test eax, eax
 .=< 0x08048c34
                     751£
                                     ine 0x8048c55
                     c70424638e04.
    0x08048c36
                                     mov dword [esp], str.Authenticated
                                     call sym.imp.puts
    0x08048c3d
                     e8cefb
    0x08048c42
                                     mov dword [esp], str.bin sh
                     c70424728e04.
    0x08048c49
                     e8d2fb
                                     call sym.imp.system
                     H8000000000
    0x08048c4e
                                    mov eax, 0
.==< 0x08048c53
                     eb05
                                     imp 0x8048c5a
`-> 0x08048c55
                     b801000000
                                    mov eax. 1
--> 0x08048c5a
                     8b54243c
                                     mov edx, dword [local_3ch] : [0x3c:4]=-1 : '<' : 60
    0x08048c5e
                     653315140000.
                                     xor edx, dword qs:[0x14]
 .=< 0x08048c65
                     7405
                                     .ie 0x8048c6c
                                     call sym.imp.__stack_chk_fail : void __stack_chk_fail(void)
                     e894fb
                     c9
                                     leave
    0x08048c6d
                     с3
```

# MBE Lab1A - auth() 1/6: String processing and antidecomp

```
0v08048a0£
                     55
                                     push ebp
    0x08048a10
                     89e5
                                     mov ebp. esp
    0x08048a12
                     83ec28
                                     sub esp, 0x28
    0x08048a15
                     c7442404038d.
                                     mov_dword [local_4h], 0x8048d03
    0x08048a1d
                     864508
                                    mov eax, dword [are 8h]
    0x08048a20
                     890424
                                     mov dword [esp], eax
    0×08048a23
                     e878fd
                                     call sym.imp.strcspn
                                     mov edx, dword [arg_8h]
    0x08048a28
                     8b5508
    0×08048a2h
                     01d0
                                     add eax. edx
    0x08048a2d
                                     mov bute [eax], 0
                     c60000
    0×08048a30
                     c74424042000.
                                     mov dword [local_4h], 0x20
    0x08048a38
                     864508
                                     mov eax, dword [arg 8h]
    0×08048a3h
                     890424
                                     mov dword [esp], eax
    0x08048a3e
                     e80dfe
                                     call sym.imp.strnlen
    0×08048a43
                     8945f4
                                     mov dword [local ch], eax
    0x08048a46
                     50
                                     push eax
    0x08048a47
                     31c0
                                     xor eax, eax
 .=< 0x08048a49
                     7403
                                     ie 0x8048a4e
    0x08048a4b
                     83c404
                                     add esp. 4
 -> 0x08048a4e
                     58
                                     рор еах
    0x08048a4f
                     837df405
                                     cmp dword [local_ch], 5
 .=< 0x08048a53
                     7f0a
                                     jg 0x8048a5f
    0x08048a55
                     6801000000
                                     mov eax. 1
.==< 0x08048a5a
                     e9e3000000
                                     .jmp 0x8048b42
```

```
again:
    if (IBN_rand(rnd, bits, BN_RAND_TOP_TWO, BN_RAND_BOTTOM_ODD)) +
    return 0;
```

```
0v08048a5f
                 c744240c0000.
                                 mov dword []
                 c74424080100.
0 \times 08048 a67
                                 mov dword
                 c74424040000.
0508048a66
                                 mov dword
0v08048a77
                 c704240000000.
                                 mov dword [esp]. 0
0v08048a7e
                 e8edfd
                                 call sym.imp.ptrace
                                 cmp eax, 0xfffffffffffffffff
                 83f8f
0×08048a83
0~08048a86
                 752e
                                 .ine 0x8048ab6
                 c70424088d04.
                                 mov dword [esp], str.e_32m.
0×08048a88
                 e87cfd
0~08048a8f
                                 call sym.imp.puts
                 c704242c8d04.
                                 mov dword [esp], str.e_31m
0v08048a94
0v08048a9h
                 e870fd
                                 call sum_imp_puts
                 c70424508d04.
                                 mov dword [esp], str.e_32m
0 \times 08048 aa0
0×08048aa7
                 e864fd
                                 call sym.imp.puts
0x08048aac
                 Ь801000000
                                 mov eax, 1
0x08048ab1
                 e98c000000
                                  .imp 0x8048b42
```

## MBE Lab1A - auth() 3/6: Pre-loop math

```
inclid.to.depois(NUMPRIMES);
BluUONC delts.
BluUONC delts.
BluUONC massdelta = BN_MMSK2 - primes[NUMPRIMES - 1];
char !s_single_word = bits <= BN_BITS2;
meaning
iif (!BN_rand(rnd, bits, BN_RAND_TOP_TMO, BN_RAND_BOTTOM_ODD)) {
    return 0;
}</pre>
```

```
mov eax, dword [arg_8h]
0x08048ab6
                864508
0x08048ab9
                83c003
                                add eax. 3
                                movzx eax, byte [eax]
0x08048abc
                069600
0x08048abf
                0fbec0
                                movsx eax, al
0x08048ac2
                 3537130000
                                xor eax. 0x1337
0x08048ac7
                05eded5e00
                                add eax. 0x5eeded
                8945f0
                                mov dword [local 10h].
0x08048acc
```

```
| Second Content of the content of t
```

```
MBE Lab1A - auth() 4/6: Loop header, restricting chars word - probable - prob
```

```
0x08048acf
                       c745ec0000000.
                                       mov dword [local 14h]. O
II.=< 0x08048ad6</p>
                       eb4e
                                           -0x8048b26
                       8b55ec
      0x08048ad8
                                       mov edx, dword [local_14h]
                       864508
                                       mov eax, dword [arg_8h]
      0x08048adb
                       01d0
      0x08048ade
                                       add eax, edx
                       0fb600
      0x08048ae0
                                       movzx eax, byte [eax]
      0x08048ae3
                       3c1f
                                       cmp al, 0x1f
                       7£07
                                          0x8048aee
                       h801000000
                                       mov eax, 1
                       eb54
      0x08048aec
```

```
MBE Lab1A - auth() 5/6: Loop body, much math deltas:
                             8b55ec
                                             mov edx, dword [local_14h]
             0x08048aee
                             864508
             0x08048af1
                                             mov eax, dword [arg_8h]
             0x08048af4
                             01d0
                                             add eax. edx
             0x08048af6
                             0fb600
                                             movzx eax, byte [eax]
             0v08048af9
                             0fbec0
                                             movsx eax, al
             0x08048afc
                             3345f0
                                             xor eax, dword [local 10h]
             0x08048aff
                             89c1
                                             mov ecx, eax
                             ba2b3b2388
             0x08048h01
                                             mov edx. 0x88233b2b
             0x08048h06
                             89c8
                                             mov eax, ecx
             0508048608
                             f7e2
                                             mul edx
             0x08048b0a
                             89c8
                                             mov eax, ecx
                             2940
             0x0804850c
                                             sub eax, edx
             0v08048h0e
                             d1e8
                                             shr eax. 1
```

add eax, edx

shr eax. Oxa

sub ecx. eax

eax. ecx

imul eax, eax, 0x539

01d0

29c1

89c8

0145f0

c1e80a

69c039050000

0.408048610

0x08048b12

0x08048h1h

0x08048b1d

0x0804851f

```
8345ec01
      0x08048b22
                                      add dword [local_14h]. 1
                      8b45ec
  `-> 0x08048b26
                                      mov eax, dword [local_14h]
      0x08048b29
                      3b45f4
                                      cmp eax. dword [local_ch]
     0x08048b2c
                      7caa
                                         0x8048ad8
                      8b450c
                                      mov eax, dword [arg_ch]
      0x08048h2e
                                      cmp eax, dword [local 10h]
                      3b45f0
      0x08048h31
                      7407
                                         0x8048b3d
11.±< 0∨08048b34
      0×08048536
                      6801000000
                                      mov eax, 1
                                          0x8048b42
     0×08048636
                      eb05
 ^-> 0x08048b3d
                                      mov eax. O
                                       leave
      0x08048b43
```

```
import z3
solver = z3.Solver()
wanted_length = 8
assert wanted_length > 5 # checked at 0x08048a4f
sym_username = [z3.BitVec('x{i}'.format(i=i), 8) for i in range(wanted_length)]
sym_serial = z3.BitVec('serial', 32)
**Remarks namede a reader mader of red to be the series of the series
```

- 8-bit entries for each character
- 32-bit serial number
- Concrete input length: z3.Array exists, but is more expensive
- ▶ Only use z3. Array if you need symbolic indexing

```
Dore expensive a prine name because it a surface of the control of
```

```
0x08048ab6
                8b4508
                               mov eax, dword [arg_8h]
                               add eax, 3; eax = (arg_8h + 3)*(1 = 1; (< NUMPRIMES: (3+) (
0x08048ab9
                83c003
                               movzx eax, byte [eax]; eax = *(uint8_t*)(arg_8h+3)
0x08048abc
                0fb600
0x08048abf
                0fbec0
                               movsx eax, al ; eax = (int32_t)*(uint8_t*)(arg_8h+3)
0x08048ac2
                3537130000
                               xor eax, 0x1337
0x08048ac7
                05eded5e00
                               add eax. 0x5eeded
                               mov dword [local_10h], eax
0x08048acc
                8945f0
```

- ► We're wrapping concrete values in z3.BitVecVal so that wrapping/truncation happens the x86 way
- ▶ If we were using python longs here, we'd have to manually mask them back into range

# MBE Lab1A - Z3ing auth() 3/7: Translating the loop header/footer

#### The following x86:

```
0x08048acf
                c745ec000000.
                                mov dword [local 14h], 0
0x08048ad6
                eb4e
                                imp 0x8048b26
0x08048b22
                8345ec01
                                add dword [local_14h], 1
0x08048b26
                8h45ec
                                mov eax, dword [local_14h]
0x08048b29
                3b45f4
                                cmp eax, dword [local_ch]
0x08048b2c
                7caa
                                il 0x8048ad8
```

#### Translates to the following C:

```
for(int local_14h=0; local_14h < local_ch; local_14h++) {

/* loop body is between 0x08048ad6 and 0x08048b22, exclusive on both ends */
}
```

## So we'll gloss that as the following in Python

```
local_ch = len(sym_username) # this is set by the strnlen at 0x08048a3e
for local_14h in range(local_ch):
    pass # we'll translate the loop body here
```

# MBE Lab1A - Z3ing auth() 4/7: Translating the loop body: 1/2

#### x86:

```
0x08048ad8
                mov edx, dword [local_14h]
0x08048adb
                mov eax, dword [arg_8h]
0x08048ade
                 add eax, edx
0x08048ae0
                movzx eax, byte [eax]
                cmp al, 0x1f
0x08048ae3
0x08048ae5
                jg 0x8048aee
                mov edx, dword [local_14h]
0x08048aee
0x08048af1
                mov eax, dword [arg 8h]
0x08048af4
                 add eax, edx
0x08048af6
                movzx eax. byte [eax]
0x08048af9
                movsx eax. al
0x08048afc
                 xor eax, dword [local 10h]
0x08048aff
                mov ecx, eax
0x08048b01
                mov edx. 0x88233b2b
0x08048b06
                mov eax, ecx
```

```
Python:
```

```
solver.add(sym_username[local_14h] > 0x1f)
```

```
z3.SignExt(24, sym_username[local_14h])
   ^= local 10h
eax
```

```
ecx = eax
eax = ecx
```

```
if (delta > maxdelta) -
```

# MBE Lab1A - Z3ing auth() 5/7: Translating the loop body: 2/2

```
Pvthon:
x86:
                                mul_result = z3.ZeroExt(32, eax) * z3.ZeroExt(32, edx)
0x08048508
                  mul edx
                                edx = z3.Extract(63, 32, mul_result)
                                eax = z3.Extract(31, 0, mul_result)
0x08048b0a
                  mov eax, ecx
                                                    ear =
0x08048b0c
                  sub eax, edx
                                                    eax -= edx
0x08048b0e
                  shr eax, 1
                                                    eax = eax >> 1
0x08048b10
                  add eax, edx
                                                    eax += edx
                                                    eax = eax >> 0xa delta = size limit (
0x08048b12
                  shr eax. Oxa
0x08048b15
                  imul eax, eax, 0x539
                                          eax = z3.Extract(31, 0, z3.SignExt(32, eax) * 0x539)
0x08048b1b
                  sub ecx. eax
                                                    ecx -= eax
0 \times 08048 b1d
                  mov eax, ecx
                                                    eax = ecx
                                                                   * 1) It's greater than primes[i] because we show
 0x08048b1f
                  add dword [local_10h], eax
                                                    local 10h +=
```

# MBE Lab1A - Z3ing auth() 6/7: Solving for a valid serial

```
serial for name 'username' is 6234463

# 1) It's greater than primerally because with which reject the prime name prime name to the prime name of the primer primeral to the p
```

# MBE Lab1A - Z3ing auth() 7/7: Solving for a valid username

```
solver.pop() # remove the constraints on the provided username filts is so shall that it fits into a single ser solver.add(sym_serial == serial+1)
assert solver.check().r == 1
model = solver.model()
username2 = ''.join(chr(model.evaluate(x).as_long()) for x in sym_username)
serial2 = model.evaluate(sym_serial)
print('serial for name %r is %r' % (username2, serial2))
```

#### Resources

- https://github.com/Z3Prover/z3/
- https://pypi.org/project/z3-solver/
- ▶ https://rise4fun.com/Z3/tutorialcontent/guide
- https://en.wikipedia.org/wiki/Satisfiability\_modulo\_theories
- ▶ https://github.com/RPISEC/MBE