Introduction to Reversing with Z3 RPISEC

```
/* If bits is so small that it fits into a single word then w
* additionally don't wont to exceed that many bits, w/
if (is_single_word) {
    N.U.ONG size_limit;
    if (bits == NR_BITS2)
        /* froud undefined behavior, w/
```

Avi Weinstock (aweinstock) was a second to a second to

derca - 0

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if (is_single_word) {
 NuLUMO rnd_word = get_word(rnd);

/* In the case that the candidate prime is a single word the
 we check that:
 1 It's greater than primedil because we shouldn't rej
 3 as being a prime number because it's a sultiple of
 3 as being a prime number because it's a sultiple of
 2 I not it's not a multiple of a known prime. We don't
 check that rnd-I is also caprime to all the known
 ** primed because there aren't many small primes where
 for (1 1; 1 * NHERHES & primes[i] < rnd_word; i**+) {
 if (was 1 * 2;
 if (delta * as 3;
 if (delta * as 3;
 if (delta * as 4;
 if (delta *

Overview

- What are SAT/SMT/Z3?
- Solving MBE lab1A with Z3
- Solving a Cyberseed RE challenge with Z3

What is SAT?

- ► SAT is the boolean SATisfiability problem
- \blacktriangleright e.g. "Does the formula $(x \lor \neg y \lor z) \land (\neg x \lor y)$ have a satisfying assignment?"
- ▶ Brute forceable in $O(2^n)$ by trying all combinations of $\{0,1\}$ for all variables
- NP-Complete
 - Not known to be subexponentially solvable in general
 - Many problems expressible as SAT

```
### In the probable_prime(BIONON *rnd, int Dits) (
### Interpretation of the prime of the prime
```

What is SMT?

- SMT is Satisfiability Modulo Theories
- ▶ "Does $(f(x,y) \lor z) \land (\neg g(x) = f(x,x))$ have a satisfying assignment?" (QF-EUF)
- ▶ "Does $2 * x + y \le z \land x + 3 * y \ge z$ have a satisfying assignment" (QF-LIA)
- Allows more compact translation of problems, e.g.
 - $x = 1 \lor x = 2 \lor x = 3 \lor ... \lor x = 99 \lor x = 100 \text{ (SAT)}$
 - ▶ $1 \le x \land x \le 100$ (SMT)
- ► Also NP-Complete

Why are SAT/SMT useful if they're hard to solve quickly?

- Proton of the control of the control
- ▶ Not all problems are as hard as the hardest ones
 - ▶ 2-SAT (each clause having at most 2 variables) is polytime solvable
 - ▶ Monotone circuits (only ANDs and ORs, no NOTs) are polytime solvable
- It's often possible to prune the search space
 - e.g. $x \lor \varphi(a, b, c, ...)$ is solvable regardless of φ because x = 1 cancels out that subterm
- ► Algorithms like DPLL and CDCL make use of partial structure to solve some instances faster than others
- ► SMT can make use of the rules for the extra types of symbols to prune the search space at a higher level

What is Z3?

```
initis. Boods[NUMPRINES]:

N.ULONG delta:

N.ULONG delta:

N.ULONG modelta = IN.NGSK2 - primes[NUMPRINES - 1]:

char is_single_word = bits <= INLBITS2;

gmin:

if (INM_rand(rnd, bits, INLBNND_TOP_TMO, INLBNND_BOTTOH_ODD))

/** we now have a random number 'rnd' to test, */

for (= 1 : K.NHERINES): i*)

if (mod = C. S. Hubble abord(rnd, (INLULONG))primes[i]):

if (mod = C. S. Hubble abord(rnd, (INLULONG))primes[i]):

nods[i] = (wintin_t)mod;

** If hits is no small that it fits into a single word then we w additionally don't wont to exceed that many bits. */

** (is_single_word).
```

- ► SAT & SMT solver developed and maintained by Microsoft Research
- Libre and Open Source (MIT Licensed)
- ▶ C++, with python bindings (pip install z3-solver)
- Based on the CDCL algorithm

Using Z3 on small examples

```
\blacktriangleright (x \lor \neg y \lor z) \land (\neg x \lor y)
    import z3
    solver = z3.Solver()
    x, y, z = z3.Bools('x y z')
    solver.add(z3.And(z3.Or(x, z3.Not(y), z), z3.Or(z3.Not(x), y)))
    if solver.check().r == 1:
        print(solver.model())
\triangleright 2 * x + y \le z \land x + 3 * y \ge z \land z > 1
    import z3
    solver = z3.Solver()
    x, v, z = z3. Ints('x v z')
    solver.add(2*x+y \le z)
    solver.add(x+3*y >= z)
    solver.add(z > 1)
    if solver.check().r == 1:
        print(solver.model())
```

MBE Lab1A - Just Running It

```
int 1:
uinti6_t mode[NUMPRIMES]
BN_ULONG delta:
BN_ULONG maxdelta = BN_MASK2 - primes[NUMPRIMES -
class is sincle mod = bits <= BN_BITS?
```

```
avi@aweinstock-debian-ii:"/Documents/cloned-repos/MBE/src/lab01$ ./lab1A
  SECURE LOGIN SYS v. 3.0 +
~- Enter your Username:
username
   Input your serial:
password
avi@aweinstock-debian-ii:"/Documents/cloned-repos/MBE/src/lab01$ echo $?
```

MBE Lab1A - Username Entry

```
0×08048569
                c70424738d04.
                               mov dword [esp], str...
                e89bfc
                                call sum.imp.puts
0×08048575
                c70424918d04.
                                mov dword [esp], str_RPISEC
                e88ffc
                                call sum, imp.puts
0×08048581
                c70424af8d04.
                               mov dword [esp], str.SECURE_LOGIN_SYS_v._3.0
0×08048588
                e883fc
                                call sum, imp. puts
0×0804858d
                c70424cd8d04.
                               mov dword [esp], str.
                e877fc
                                call sum, imp, puts
                                mov dword [esp], str.Enter_your_Username:
0x08048b99
                c70424eb8d04.
0×08048ha0
                e86bfcf
                                call sum imp puts
0v08048ha5
                c70424098e04.
                               mov dword [esp], str.
                e85ffcf
                                call sym.imp.puts
0x08048bb1
                a160b00408
                                mov eax, dword [obj.stdin]
                89442408
                                mov dword [
                                                    . eax
0x08048bba
                c74424042000.
                               mov dword [
                                                     0x20
0x08048bc2
                8d44241c
                                lea eax. []
0x08048bc6
                890424
                                mov dword [esp], eax
0x08048bc9
                e802fc
                                call sum, imp.fgets
                                                                                                                                                5000
```

MBE Lab1A - Serial Entry

```
mov dword [esp], str.,
0x08048bd5
              e836fc
                            call sum, imp. puts
0x08048bda
              c70424278e04.
                            mov dword [esp], str.NEW ACCOUNT DETECTED
0x08048he1
              e82afcf
                            call sum_imp_puts
0x08048he6
              c70424cd8d04.
                            mov dword [esp], str.
0x08048bed
              e81efc
                            call sum.imp.puts
0x08048bf2
              c70424458e04.
                            mov dword [esp], str.Input your serial:
              e812fc
0.08048569
                            call sum, imp. puts
              c70424098e04.
                            mov dword [esp], str.
0x08048c05
              e806fc
                            call sum.imp.puts
              8d442418
0x08048c0e
              89442404
0x08048c12
              c70424008d04.
0x08048c19
              e842fc
                                                                                       E F 0123456789ABCDEF
                                                                          В
                                                                               C D
                     2575 000a
                                                 0000 1b5b 3332 6d2e 2d2d
```

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MBE Lab1A - Calling the authentication routine and the second results as British as Brit

again:
if (|BN_rand(rnd, bits, BN_RAND_TOP_TWO, BN_RAND_BOTTOM_ODD)) {
 return 0;

```
86442418
                                    mov eax, dword [local 18h]
    0x08048c22
                     89442404
                                     mov dword []
    0x08048c26
                     8d44241c
                                     lea eax. []
    0x08048c2a
                     890424
                                     mov dword [esp], eax
    0x08048c2d
                     e8ddfd
                                     call sum.auth
    0x08048c32
                     85c0
                                     test eax, eax
 .=< 0x08048c34
                     751£
                                     ine 0x8048c55
                     c70424638e04.
    0x08048c36
                                     mov dword [esp], str.Authenticated
                                     call sym.imp.puts
    0x08048c3d
                     e8cefb
    0x08048c42
                                     mov dword [esp], str.bin sh
                     c70424728e04.
    0x08048c49
                     e8d2fb
                                     call sym.imp.system
                     H8000000000
    0x08048c4e
                                    mov eax, 0
.==< 0x08048c53
                     eb05
                                     imp 0x8048c5a
`-> 0x08048c55
                     b801000000
                                    mov eax. 1
--> 0x08048c5a
                     8b54243c
                                     mov edx, dword [local_3ch] : [0x3c:4]=-1 : '<' : 60
    0x08048c5e
                     653315140000.
                                     xor edx, dword qs:[0x14]
 .=< 0x08048c65
                     7405
                                     .ie 0x8048c6c
                                     call sym.imp.__stack_chk_fail : void __stack_chk_fail(void)
                     e894fb
                     c9
                                     leave
    0x08048c6d
                     с3
```

MBE Lab1A - auth() 1/6: String processing and antidecomp

```
0v08048a0£
                     55
                                     push ebp
    0x08048a10
                     89e5
                                     mov ebp. esp
    0x08048a12
                     83ec28
                                     sub esp, 0x28
    0x08048a15
                     c7442404038d.
                                     mov_dword [local_4h], 0x8048d03
    0x08048a1d
                     864508
                                    mov eax, dword [are 8h]
    0x08048a20
                     890424
                                     mov dword [esp], eax
    0×08048a23
                     e878fd
                                     call sym.imp.strcspn
                                     mov edx, dword [arg_8h]
    0x08048a28
                     8b5508
    0×08048a2h
                     01d0
                                     add eax. edx
    0x08048a2d
                                     mov bute [eax], 0
                     c60000
    0×08048a30
                     c74424042000.
                                     mov dword [local_4h], 0x20
    0x08048a38
                     864508
                                     mov eax, dword [arg 8h]
    0×08048a3h
                     890424
                                     mov dword [esp], eax
    0x08048a3e
                     e80dfe
                                     call sym.imp.strnlen
    0×08048a43
                     8945f4
                                     mov dword [local ch], eax
    0x08048a46
                     50
                                     push eax
    0x08048a47
                     31c0
                                     xor eax, eax
 .=< 0x08048a49
                     7403
                                     ie 0x8048a4e
    0x08048a4b
                     83c404
                                     add esp. 4
 -> 0x08048a4e
                     58
                                     рор еах
    0x08048a4f
                     837df405
                                     cmp dword [local_ch], 5
 .=< 0x08048a53
                     7f0a
                                     jg 0x8048a5f
    0x08048a55
                     6801000000
                                     mov eax. 1
.==< 0x08048a5a
                     e9e3000000
                                     .jmp 0x8048b42
```

```
again:
    if (IBN_rand(rnd, bits, BN_RAND_TOP_TWO, BN_RAND_BOTTOM_ODD)) +
    return 0;
```

```
0v08048a5f
                 c744240c0000.
                                 mov dword []
                 c74424080100.
0 \times 08048 a67
                                 mov dword
                 c74424040000.
0508048a66
                                 mov dword
0v08048a77
                 c704240000000.
                                 mov dword [esp]. 0
0v08048a7e
                 e8edfd
                                 call sym.imp.ptrace
                                 cmp eax, 0xfffffffffffffffff
                 83f8f
0×08048a83
0~08048a86
                 752e
                                 .ine 0x8048ab6
                 c70424088d04.
                                 mov dword [esp], str.e_32m.
0×08048a88
                 e87cfd
0~08048a8f
                                 call sym.imp.puts
                 c704242c8d04.
                                 mov dword [esp], str.e_31m
0v08048a94
0×08048a9h
                 e870fd
                                 call sum_imp_puts
                 c70424508d04.
                                 mov dword [esp], str.e_32m
0 \times 08048 aa0
0×08048aa7
                 e864fd
                                 call sym.imp.puts
0x08048aac
                 Ь801000000
                                 mov eax, 1
0x08048ab1
                 e98c000000
                                  .imp 0x8048b42
```

MBE Lab1A - auth() 3/6: Pre-loop math

```
inclid.to.depois(NUMPRIMES);
BluUONC delts.
BluUONC delts.
BluUONC massdelta = BN_MMSK2 - primes[NUMPRIMES - 1];
char !s_single_word = bits <= BN_BITS2;
meaning
iif (!BN_rand(rnd, bits, BN_RAND_TOP_TMO, BN_RAND_BOTTOM_ODD)) {
    return 0;
}</pre>
```

```
mov eax, dword [arg_8h]
0x08048ab6
                864508
0x08048ab9
                83c003
                                add eax. 3
                                movzx eax, byte [eax]
0x08048abc
                068600
0x08048abf
                0fbec0
                                movsx eax, al
0x08048ac2
                 3537130000
                                xor eax. 0x1337
0x08048ac7
                05eded5e00
                                add eax. 0x5eeded
                8945f0
                                mov dword [local 10h].
0x08048acc
```

```
| Second Content of the content of t
```

```
MBE Lab1A - auth() 4/6: Loop header, restricting chars word - probable - prob
```

```
0x08048acf
                       c745ec0000000.
                                       mov dword [local 14h]. O
II.=< 0x08048ad6</p>
                       eb4e
                                           -0x8048b26
                       8b55ec
      0x08048ad8
                                       mov edx, dword [local_14h]
                       864508
                                       mov eax, dword [arg_8h]
      0x08048adb
                       01d0
      0x08048ade
                                       add eax, edx
                       0fb600
      0x08048ae0
                                       movzx eax, byte [eax]
      0x08048ae3
                       3c1f
                                       cmp al, 0x1f
                       7£07
                                          0x8048aee
                       h801000000
                                       mov eax, 1
                       eb54
      0x08048aec
```

```
MBE Lab1A - auth() 5/6: Loop body, much math motor action math motor action with motor and mathematical mathe
                `----> 0x08048aee
                                                                                                                8b<u>55</u>ec
                                                                                                                                                                             mov edx, dword [local_14h]
                                                 0x08048af1
                                                                                                                 8b4508
                                                                                                                                                                             mov eax, dword [arg_8h]
                                                0x08048af4
                                                                                                                 01d0
                                                                                                                                                                             add eax, edx
                                                0x08048af6
                                                                                                                 0fb600
                                                                                                                                                                             movzx eax, byte [eax]
             1 :111
                                                0x08048af9
             +:H
                                                                                                                 0fbec0
                                                                                                                                                                             movsx eax. al
                                                0x08048afc
                                                                                                                3345f0
                                                                                                                                                                             xor eax, dword [local_10h]
             +:H
             1.\pm111
                                                0x08048aff
                                                                                                                 89c1
                                                                                                                                                                             mov ecx, eax
                                                0x08048b01
                                                                                                                 ba2b3b2388
                                                                                                                                                                             mov edx, 0x88233b2b
             + \cdot 111
                                                0x08048b06
                                                                                                                 89c8
                                                                                                                                                                             mov eax, ecx
                                                                                                                 f7e2
                                                0x08048b08
                                                                                                                                                                             mul edx
                                                0x08048b0a
                                                                                                                 89c8
                                                                                                                                                                             mov eax, ecx
                                                0x08048b0c
                                                                                                                 29d0
                                                                                                                                                                             sub eax. edx
                                                0x08048b0e
                                                                                                                 d1e8
                                                                                                                                                                             shr eax, 1
                                                0x08048b10
                                                                                                                 01d0
                                                                                                                                                                             add eax, edx
                                                0x08048b12
                                                                                                                 c1e80a
                                                                                                                                                                             shr eax. Oxa
                                                0x08048b15
                                                                                                                 69c039050000
                                                                                                                                                                             imul eax, eax, 0x539
                                                                                                                 29c1
                                                 0×08048616
                                                                                                                                                                             sub ecx, eax
```

```
8345ec01
      0x08048b22
                                      add dword [local_14h]. 1
                      8b45ec
  `-> 0x08048b26
                                      mov eax, dword [local_14h]
      0x08048b29
                      3b45f4
                                      cmp eax. dword [local_ch]
     0x08048b2c
                      7caa
                                         0x8048ad8
                      8b450c
                                      mov eax, dword [arg_ch]
      0x08048h2e
                                      cmp eax, dword [local 10h]
                      3b45f0
      0x08048h31
                      7407
                                         0x8048b3d
11.±< 0∨08048b34
      0×08048536
                      6801000000
                                      mov eax, 1
                                          0x8048b42
     0×08048636
                      eb05
 ^-> 0x08048b3d
                                      mov eax. O
                                      leave
      0x08048b43
```

```
import z3
solver = z3.Solver()
wanted_length = 6
assert wanted_length > 5 # checked at 0x08048a4f
sym_username = [z3.BitVec('x{i}'.format(i=i), 8) for i in range(wanted_length)]
sym_serial = z3.BitVec('serial', 32)
**Remarks named a range of rend to be the serial ("Indicates a range of the serial serial to the serial serial to the serial serial to the serial s
```

- ▶ 8-bit entries for each character
- 32-bit serial number
- Concrete input length: z3.Array exists, but is more expensive
- ▶ Only use z3. Array if you need symbolic indexing

MBE Lab1A - Z3ing auth() 2/?: Translating the pre-loop math

```
eax = sym_username[3]

eax ^= z3.BitVecVal(0x1337, 32)

eax += z3.BitVecVal(0x5eeded, 32)

local_10h = eax

local_10h = eax
```

- ► We're wrapping concrete values in z3.BitVecVal so that wrapping/truncation happens the x86 way
- ▶ If we wre using python longs here, we'd have to manually mask them back into range

Resources

- https://github.com/Z3Prover/z3/
- https://pypi.org/project/z3-solver/
- ▶ https://rise4fun.com/Z3/tutorialcontent/guide
- https://en.wikipedia.org/wiki/Satisfiability_modulo_theories
- ▶ https://github.com/RPISEC/MBE