Introduction to Functional Programming with Haskell - RCOS Presentation

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What characterizes Functional Programming?

- Abstraction of common patterns via higher order functions
- A mathematical use of the term "function" (as a pure mapping from input to output), as opposed to the concept of procedures (e.g. in C)

What is Haskell?

A general-purpose programming language that:

- Encourages a functional style of programming
- ► Enables very short, readable code
- Has static typechecking, with type inference
- ► Compiles to native code, in the same efficiency class as Java/C# (can be made as performant as Assembly/C/C++, with some effort)

Hello world

```
main = putStrLn "Hello, world!"

main = do
    putStr "Enter a string: "
    str <- getLine
    putStrLn ("Echo: " ++ str)</pre>
```

Examples with numbers

- factorial n = product [1..n]
- dotProduct xs ys = sum \$ zipWith (*) xs ys
 dotProduct' xs ys = sum (zipWith (*) xs ys) -- equivalent definition
 magnitude xs = sqrt \$ dotProduct xs xs
- divides n i = (n 'mod' i) == 0
 isPrime n = not \$ any (divides n) [1..n]
 isPrime' n = not (any (divides n) [1..n]) -- equivalent definition

Examples with numbers (continued)

- fibonaccis = 1 : 1 : zipWith (+) fibonaccis (tail fibonaccis)
- approxDerivative epsilon f x = (f (x+epsilon) f x) / epsilon

```
stars n = replicate (floor n) '*'
showLines = putStr . unlines
prepend = zipWith ((++) . show)
plot f xs = showLines $ prepend xs (map (stars . f) xs)
```

Execution of examples

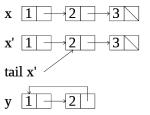
```
ghci> :load haskell_lecture_numberslide.hs
                                 ( haskell_lecture_numberslide.hs, interpreted )
[1 of 1] Compiling Main
Ok. modules loaded: Main.
ghci> :browse
factorial :: (Enum a. Num a) => a -> a
dotProduct :: Num a => [a] -> [a] -> a
magnitude :: Floating a => [a] -> a
divides :: Integral a => a -> a -> Bool
isPrime :: Integral a => a -> Bool
fibonaccis :: Num a => [a]
approxDerivative :: Fractional a => a -> (a -> a) -> a -> a
stars :: RealFrac a => a -> [Char]
showLines :: [String] -> IO ()
prepend :: Show a => [a] -> [[Char]] -> [[Char]]
plot :: (RealFrac b. Show a) => (a \rightarrow b) \rightarrow [a] \rightarrow IO ()
ghci> map factorial [1..10]
[1,2,6,24,120,720,5040,40320,362880,3628800]
ghci> magnitude [1.1]
1.4142135623730951
ghci> take 10 $ filter isPrime [2..]
[2.3.5.7.11.13.17.19.23.29]
ghci> take 10 fibonaccis
[1.1.2.3.5.8.13.21.34.55]
ghci> plot (^2) [0..7]
1.0*
2.0****
3.0*******
4.0**********
ghci> plot (approxDerivative 0.01 (^2)) [0..7]
2.0****
3.0*****
4.0******
5.0*******
6.0*******
7.0**********
ghci>
```

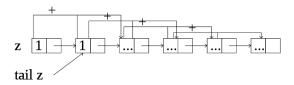
Functions used in previous examples

```
(\$) :: (a -> b) -> a -> b
f  x = f  x
(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow (a \rightarrow c)
(f \cdot g) x = f (g x)
not :: Bool -> Bool
any, all :: (a -> Bool) -> [a] -> Bool
zip :: [a] -> [b] -> [(a, b)]
zipWith :: (a \rightarrow b \rightarrow c) \rightarrow [a] \rightarrow [b] \rightarrow [c]
sum, product :: Num a => [a] -> a
replicate :: Int -> a -> [a]
putStr, putStrLn :: String -> IO ()
```

Linked lists - Boxes and Pointers!

```
x = [1,2,3]
x' = 1:2:3:[]
y = 1 : 2 : y
z = 1 : 1 : zipWith (+) z (tail z)
```





Map and Reduce

```
map :: (a -> b) -> [a] -> [b]
map f [] = []
map f (x:xs) = (f x):(map f xs)

map' f = foldr ((:) . f) [] -- equivalent definition

foldr :: (a -> b -> b) -> b -> [a] -> b
foldr f acc [] = acc
foldr f acc (x:xs) = f x (foldr f acc xs)
```

map applies its function to every element of a list.

foldr uses the provided function to reduce/aggregate the list into some value, starting from a seed.

Folds are very general, and can be used to implement many types of loops.

Definition of foldl in Python:

```
def foldl(f, init, xs):
    acc = init
    for x in xs:
        acc = f(acc, init)
    return acc
```

Reduce (continued)

More definitions of things in terms of foldr:

```
map f = foldr ((:) . f) []
sum = foldr (+) 0
product = foldr (*) 1
concat = foldr (++) []
all p = foldr ((&&) . p) True
any p = foldr ((|||) . p) False
average = uncurry (/) . foldr (\x (s, t) -> (s+x, t+1)) (0, 0)
```

Typeclasses

With this definition:

```
instance Num a => Num [a] where
   (+) = zipWith (+)
   (*) = zipWith (*)
   (-) = zipWith (-)
   negate = map negate
   abs = map abs
   signum = map signum
   fromInteger = cycle . return . fromInteger
```

Expressions like these become valid:

```
1 + [1,2,3]
2 * [2..10]
-[6,2,8]
abs [-5..5]
```

Currying, Sections, and Infix

The following are all equivalent (via currying):

```
f g x y = zipWith g x y
f g x = zipWith g x
f g = zipWith g
f = zipWith
f g x = \y -> zipWith g x y
f g = \x y -> zipWith g x y
f = \g x y -> zipWith g x y
```

These are equivalent triples (via sections, and infix):

```
g x = x + 1 
g = (+1) 
g x = (+) x 1
```

```
h x = x 'mod' 2
h = ('mod' 2)
h x = mod x 2
```

```
i x = 2 'mod' x
i = (2 'mod')
i x = mod 2 x
```

TIMTOWTDI - There's More Than One Way To Do It

Functions introduced:

```
ord :: Char -> Int
chr :: Int -> Char
interact :: (String -> String) -> IO ()
forever :: Monad m => m a -> m b
```

```
import Control.Monad
import Data.Char

caesarCipher shift = map (chr . ('mod' 256) . (+ shift) . ord)

main1 = forever $ do
    plaintext <- getLine
    let ciphertext = caesarCipher 3 plaintext
    putStrLn (caesarCipher 3 plaintext)

main2 = forever (getLine >>= (putStrLn . caesarCipher 3))

main3 = interact (caesarCipher 3)
```

Datatype declarations

```
data TrafficLight = RedLight | YellowLight | GreenLight
```

```
import qualified Data.Foldable as F

data List a = Node a (List a) | Empty

instance Foldable List where
   foldr f acc Empty = acc
   foldr f acc (Node x xs) = f x (F.foldr f acc xs)
```

```
import qualified Data.Map as M

data JSVal =
    JSUndefined
    | JSNull
    | JSBoolean Bool
    | JSString String
    | JSNumber Double
    | JSObject (M.Map String JSVal)
```

Binary Search Trees

```
{-# LANGUAGE NoMonomorphismRestriction #-}
import Data.Foldable as F

data BinaryTree a = Node a (BinaryTree a) (BinaryTree a) | Empty
    deriving (Eq, Show, Ord)

instance Foldable BinaryTree where
   foldr f acc Empty = acc
   foldr f acc (Node x l r) = F.foldr f (f x (F.foldr f acc r)) l
```

```
#include <memorv>
using std::shared_ptr;
using std::make_shared;
template <class A> struct BinaryTree {
    A elem:
    shared_ptr<BinaryTree<A>> left, right;
};
template <class A> shared_ptr<BinaryTree<A>> makeTree(A x,
        shared_ptr<BinaryTree<A>> 1, shared_ptr<BinaryTree<A>> r) {
    return make_shared({elem: x, left: 1, right: r});
template <class A> shared_ptr<BinaryTree<A>> emptyTree() {
    return shared_ptr<BinaryTree<A>>(nullptr);
}
                                                 4 11 1 4 22 1 4 23 1 4 24 1 24
```

```
treeInsert x Empty = Node x Empty Empty
treeInsert x (Node y l r) = case compare x y of
  LT -> Node y (treeInsert x l) r
  GT -> Node y l (treeInsert x r)
  EQ -> Node y l r
```

```
template <class A> shared_ptr<BinaryTree<A>>
treeInsert(A x, shared_ptr<BinaryTree<A>> tree) {
   if(tree.get() == nullptr) {
      return makeTree(x, emptyTree<A>(), emptyTree<A>());
   } else if(x < tree->elem) {
      return makeTree(tree->elem, treeInsert(x, tree->left), tree->right);
   } else if(tree->elem < x) {
      return makeTree(tree->elem, tree->left, treeInsert(x, tree->right));
   } else { // equal
      return tree;
   }
}
```

```
treeFind x Empty = Empty
treeFind x (Node y 1 r) = case compare x y of
  LT -> treeFind x 1
  GT -> treeFind x r
  EQ -> Node y 1 r
```

```
template <class A> shared_ptr<BinaryTree<A>>
treeFind(A x, shared_ptr<BinaryTree<A>> tree) {
   if(tree.get() == nullptr) {
      return tree;
   } else if(x < tree->elem) {
      return treeFind(x, tree->left);
   } else if(tree->elem < x) {
      return treeFind(x, tree->right);
   } else { // equal
      return tree;
   }
}
```

```
treeRemove x Empty = Empty
treeRemove x (Node y l r) = case compare x y of
  LT -> Node y (treeRemove x l) r
  GT -> Node y l (treeRemove x r)
  EQ -> case (l, r) of
      (Empty, Empty) -> Empty
      (_, Empty) -> l
      (Empty, _) -> r
      (_, _) -> let lMax = F.maximum l in
      Node lMax (treeRemove lMax l) r
```

```
template <class A> shared_ptr<BinaryTree<A>>
treeRemove(A x, shared_ptr<BinaryTree<A>> tree) {
   if(tree.get() == nullptr) {
       return tree:
   } else if(x < tree->elem) {
        return treeRemove(x, tree->left);
   } else if(tree->elem < x) {</pre>
        return treeRemove(x, tree->right);
   } else { // equal
        if((tree->left.get() == nullptr) &&
            (tree->right.get() == nullptr)) {
            return emptyTree<A>();
        } else if(tree->right.get() == nullptr) {
            return tree->left:
        } else if(tree->left.get() == nullptr) {
            return tree->right;
        } else {
            // requires implementation of tree iterators, which was not done
            // for this presentation due to space constraints
            A lMax = std::max(begin(tree->left), end(tree->left));
            return makeTree(lMax, treeRemove(lMax, tree->left), tree->right);
   }
```

Quicksort

```
{-# LANGUAGE NoMonomorphismRestriction #-}
import Control.Monad
import Control.Monad.ST
import Data.STRef
import qualified Data. Vector as V
import qualified Data. Vector. Mutable as VM
import Test.QuickCheck
naiveQuicksort [] = []
naiveQuicksort lst = naiveQuicksort less ++ eq ++ naiveQuicksort more where
    pivot = lst !! (length lst 'div' 2)
    [less, eq, more] = map (\op -> filter ('op' pivot) lst) [(<), (==), |(>)]
partitionByST cmp vec pivot lo hi = aux lo lo hi where
    aux i j n | j \le n = do
        a_i <- VM.read vec i
        case cmp a_j pivot of
            LT -> VM.swap vec i j >> aux (i+1) (j+1) n
            GT \rightarrow VM.swap vec j n >> aux i j (n-1)
            EQ \rightarrow aux i (j+1) n
    aux i j n = return (i, j)
```

Quicksort (continued)

```
quicksortByST cmp vec = aux 0 (VM.length vec - 1) where
   aux lo hi = when (lo < hi) $ do
        let pivotIdx = lo + ((hi-lo) 'div' 2)
       pivot <- VM.read vec pivotIdx</pre>
        (leftMid, rightMid) <- partitionByST cmp vec pivot lo hi
        aux lo leftMid
        aux rightMid hi
quicksortBy cmp vec = V.modify (quicksortByST cmp) vec
quicksort = quicksortBy compare
quicksortList = V.toList . quicksort . V.fromList
runTests = quickCheck naiveSort_matches_STSort where
   naiveSort matches STSort :: [Int] -> Bool
   naiveSort_matches_STSort x = naiveQuicksort x == quicksortList x
```

Questions?

Thanks

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- Professor Moorthy
- ► Sean O'Sullivan