Distributed Deep Q-Learning

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Introduction

Mathematical formulation

Serial algorithm

Distributed algorithm

Numerical experiments

Conclusion

Introduction 2/29

Motivation

- ▶ long-standing challenge of reinforcement learning (RL)
 - control with high-dimensional sensory inputs (e.g., vision, speech)
 - shift away from reliance on hand-crafted features
- ▶ utilize breakthroughs in deep learning for RL [M+13, M+15]
 - extract high-level features from raw sensory data
 - learn better representations than handcrafted features with neural network architectures used in supervised and unsupervised learning
- create fast learning algorithm
 - train efficiently with stochastic gradient descent (SGD)
 - distribute training process to accelerate learning [DCM⁺12]

Introduction 3/29

Success with Atari games







Introduction 4/29

Goals

distributed deep RL algorithm

- robust neural network agent
 - must succeed in challenging test problems
- control policies with high-dimensional sensory input
 - obtain better internal representations than handcrafted features
- ► fast training algorithm
 - efficiently produce, use, and process training data

Introduction 5/29

Introduction

Mathematical formulation

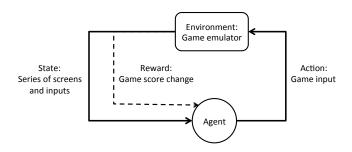
Serial algorithm

Distributed algorithm

Numerical experiments

Conclusion

Playing games



objective: learned policy maximizes future rewards

$$R_t = \sum_{t'=t}^{T} \gamma^{t'-t} r_{t'},$$

- ightharpoonup discount factor γ
- ightharpoonup reward change at time t' $r_{t'}$

State-action value function

basic idea behind RL is to estimate

$$Q^{\star}(s, a) = \max_{\pi} \mathbf{E} \left[R_t \mid s_t = s, a_t = a, \pi \right],$$

where π maps states to actions (or distributions over actions)

optimal value function obeys Bellman equation

$$Q^{\star}\left(s,a\right) = \operatorname*{\mathbf{E}}_{s^{\prime}\sim\mathcal{E}}\left[r + \gamma\max_{a^{\prime}}Q^{\star}\left(s^{\prime},a^{\prime}\right)\mid s,a\right],$$

where \mathcal{E} is the MDP environment

Q-network

trained by minimizing a sequence of loss functions

$$L^{(i)}\left(\boldsymbol{\theta}^{(i)}\right) = \underset{s,a \sim \rho(\cdot)}{\mathbf{E}} \left[\left(\boldsymbol{y}^{(i)} - Q\left(s,a;\boldsymbol{\theta}^{(i)}\right) \right)^2 \right],$$

with

- iteration number i, ith network parameters $\theta^{(i)}$
- $\text{ target } y^{(i)} = \mathbf{E}_{s' \sim \mathcal{E}} \left[r + \gamma \max_{a'} Q\left(s', a'; \theta^{(i-1)}\right) \mid s, a \right]$
- "behavior distribution" (exploration policy) $\rho\left(s,a\right)$
- architecture varies according to application

Introduction

Mathematical formulation

Serial algorithm

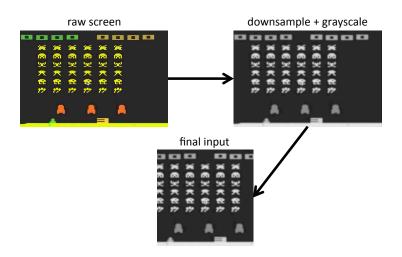
Distributed algorithm

Numerical experiments

Conclusion

Serial algorithm 10/29

Preprocessing



Serial algorithm 11/29

Q-learning

optimize Q-network loss function via

$$Q\left(s,a\right) := Q\left(s,a\right) + \alpha \left(r + \gamma \max_{a'} Q\left(s',a'\right) - Q\left(s,a\right)\right)$$

- trains optimal policy using "behavior policy" (off-policy)
 - learns policy $\pi^{\star}(s) = \operatorname{argmax}_{a} Q(s, a; \theta)$
 - uses an ϵ -greedy strategy (behavior policy) for state-space exploration

Serial algorithm 12/29

Experience replay

a kind of short-term memory

store agent's experiences at each time step

$$e_t = (s_t, a_t, r_t, s_{t+1})$$

experiences form a replay memory dataset

$$\mathcal{D} = \{e_1, \dots, e_N\},\,$$

where N is the fixed memory capacity

execute Q-learning updates with samples of experience

$$e \sim \mathcal{D}$$

Serial deep Q-learning

given replay memory $\mathcal D$ with capacity N

initialize Q-networks $Q,\,\hat{Q}$ with same random weights θ repeat until timeout

initialize frame sequence $s_1 = \{x_1\}$ and preprocessed state $\phi_1 = \phi\left(s_1\right)$ for $t = 1, \ldots, T$

- $1. \text{ select action } a_t = \left\{ \begin{array}{ll} \max_a Q\left(\phi\left(s_t\right), a; \theta\right) & \text{ w.p. } 1 \epsilon \\ \text{ random action} & \text{ otherwise} \end{array} \right.$
- 2. execute action a_t and observe reward r_t and frame x_{t+1}
- 3. append $s_{t+1} = (s_t, a_t, x_{t+1})$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$
- 4. store experience $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D}
- 5. uniformly sample minibatch $(\phi_j, a_j, r_j, \phi_{j+1}) \sim \mathcal{D}$
- 6. set $y_j = \left\{ egin{array}{ll} r_j & \text{if } \phi_{j+1} \text{ terminal} \\ r_j + \gamma \max_{a'} \hat{Q}\left(\phi_{j+1}, a'; heta
 ight) & \text{otherwise} \end{array}
 ight.$
- 7. perform gradient descent step for Q on minibatch
- 8. every C steps reset $\hat{Q} = Q$

Introduction

Mathematical formulation

Serial algorithm

Distributed algorithm

Numerical experiments

Conclusion

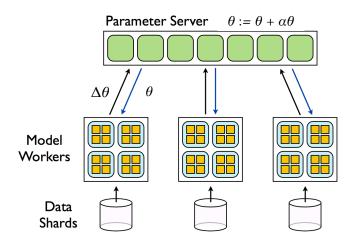
Model parallelism

for each Q-network

- partition model across CPUs/GPUs
 - up to availability of CPU/GPU resources
 - uses Caffe deep learning framework
- ► [[Kevin/Hao Yi: How does caffe use CPU/GPU resources? How does complexity scale for implementation? Answers question of how our algorithm scale for model.]]

Data parallelism

downpour SGD: generic asynchronous distributed SGD



Implementation

- ▶ data shards are generated locally on each model worker in real-time
 - data is stored independently for each worker
 - since game emulation is simple, generating data is fast
 - simple fault tolerance approach: regenerate data if worker dies
- algorithm scales very well with data
 - since data lives locally on workers, no data is sent

Implementation

- bottleneck is parameter update time on parameter server
 - e.g., if parameter server gradient update takes 2 ms, then we can only do up to 500 updates per second (using buffers, etc.)
- trade-off between parallel updates and model staleness
 - because worker is likely using a stale model, the updates are "noisy" and not of the same quality as in serial implementation

Implementation

communication pattern

- one-to-all and all-to-one, but asynchronous for every minibatch
- ▶ like multiple asynchronous all-reduces

Introduction

Mathematical formulation

Serial algorithm

Distributed algorithm

Numerical experiments

Conclusion

Evaluation



Snake

parameters

- snake length grows with number of apples eaten
- one apple at any time, regenerated once eaten
- $n \times n$ array, with walled-off world
- want to maximize score, equal to snake length

complexity

- four possible states for each cell: {empty, head, body, apple}
- state space cardinality is $O\left(n^8\right)$
- four possible actions: {north, south, east, west}

Results

Introduction

Mathematical formulation

Serial algorithm

Distributed algorithm

Numerical experiments

Conclusion

Conclusion 25/29

Summary

Conclusion 26/29

References

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 In Advances in Neural Information Processing Systems, pages 1223–1231, 2012.
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Theoretical complications

deep learning algorithms require

- ▶ huge training datasets
- ► independence between samples
- fixed underlying data distribution

Appendix 28/29

Deep Q-learning

avoids theoretical complications

- greater data efficiency
 - each experience potentially used in many weight udpates
- reduce correlations between samples
 - randomizing samples breaks correlations from consecutive samples
- experience replay averages behavior distribution over states
 - smooths out learning
 - avoids oscillations or divergence in gradient descent

Appendix 29/29