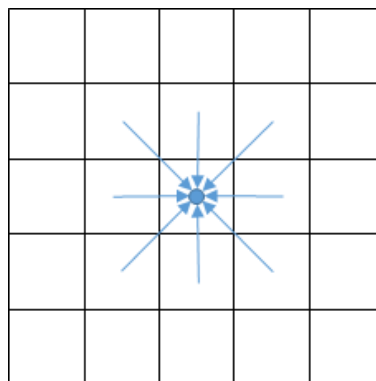


Name Andreas Wenzelhuemer

Points \_\_\_\_\_

Effort in hours 5**1. Psychedelic Diffusions****(4 + 4 + 4 Points)**

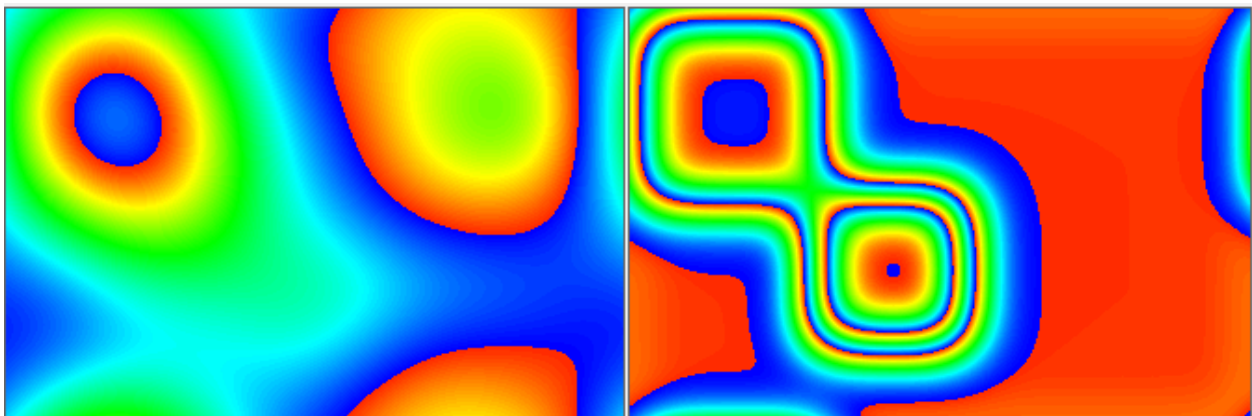
On Moodle you find a template for implementing a diffusion simulation. Simple diffusion simulations work by computing the value of a point by averaging over its neighboring points:



$$f(p) = \frac{1}{8} * \sum neighbor(p)$$

- Complete the implementation of the simulation logic in C# using the provided template.
- Use any of the learned techniques to compute the simulation in the background to provide a responsive UI. Take care of proper cancelation and locking!
- Implement a parallel version of the simulation with a parallelization technique of your choice. Discuss your design considerations and calculate the speedup.

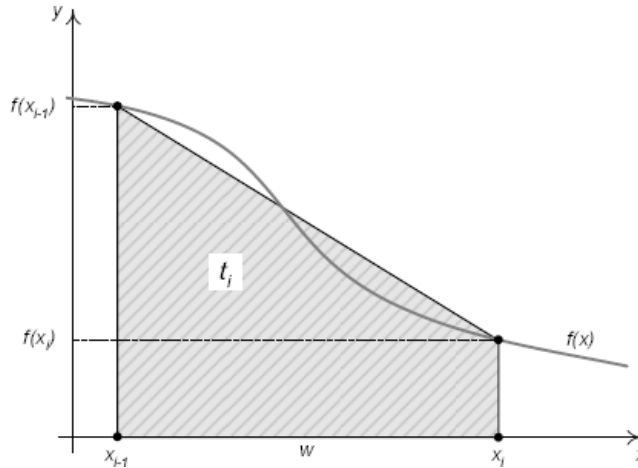
Document each step and also show a screenshot of the application in action.



## 2. Parallel Numerical Integration

(5 + 5 + 2 Points)

Numerical integration is a technique for numerical (approximate) calculation of a definite integral of a function  $f$ . The algorithm is defined as follows: The interval of the integral is partitioned into many small parts of size  $w$ . For each of those small intervals the area under the curve is approximated by the area of the trapeze defined by  $x_{j-1}$ ,  $x_j$ ,  $f(x_{j-1})$  and  $f(x_j)$ . Then the approximation of the whole integral can be computed by summing up all trapeze areas. The total accuracy of the calculation can be scaled arbitrarily by increasing the total number of trapezes.



As the calculation of one trapeze area is independent from the other areas, this parallel numerical integration algorithm can be parallelized quite easily.

- a) Implement an OpenMP program in C or C++ for parallel numerical integration of the following function:

$$\int_0^1 \frac{4}{1+x^2} dx$$

The user should be able to set the total number of trapezes with a parameter.

- b) Implement another version of the program in C# using the .NET Task Parallel Library.
- c) Test both versions and measure the consumed runtime for various configurations. Document your results in tabular form and analyze.

By the way, do you notice something concerning the value of the computed integral?

# Übung 4

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## 1. Setup

Memory size	16,0 GB
CPU type	Intel Core i7-8565U 1.80GHz
Number of cores	4
System	Windows 11 Education N
IDE	Visual Studio 2022

## 2. Psychedelic Diffusions

### 2.1. Simulation Logic

Listing 1. SequentialImageGenerator.cs

```
namespace Diffusions.Generators
{
    public class SequentialImageGenerator : ImageGenerator
    {
        protected override void UpdateMatrix(Area area)
        {
            lock (area.Matrix)
            {
                var m = area.Matrix;

                for (int x = 0; x < area.Width; x++)
                {
                    int pX = (x + area.Width - 1) % area.Width;
                    int nX = (x + 1) % area.Width;

                    for (int y = 0; y < area.Height; y++)
                    {
                        int pY = (y + area.Height - 1) % area.Height;
                        int nY = (y + 1) % area.Height;
                        area.NextMatrix[x, y] = (
                            m[pX, pY] + m[pX, y] + m[pX, nY] +
                            m[x, pY] + m[x, nY] +
                            m[nX, pY] + m[nX, y] + m[nX, nY]) / 8;
                    }
                }
                var tmp = area.NextMatrix;
                area.NextMatrix = area.Matrix;
                area.Matrix = tmp;
            }
        }
    }
}
```

## 2.2. Background Computing

When the method `Start` gets called, a new `Task` gets started. Additionally an `CancellationTokenSource` gets created. When `Stop` gets called, `cancellationTokenSource.Cancel()` gets executed. The loop where the iterations are running, gets canceled and the simulation stops.

Listing 2. ImageGenerator.cs

```
using System;
using System.Diagnostics;
using System.Drawing;
using System.Threading;
using System.Threading.Tasks;

namespace Diffusions.Generators
{
    public abstract class ImageGenerator : IImageGenerator
    {
        public bool Finished { get; protected set; } = false;

        protected CancellationTokenSource cancellationTokenSource;

        public void Start(Area area)
        {
            cancellationTokenSource = new CancellationTokenSource();
            CancellationToken token = cancellationTokenSource.Token;
            Task.Run(() =>
            {
                Finished = false;

                Stopwatch sw = new Stopwatch();
                sw.Start();
                for (int i = 0; i < Settings.Default.MaxIterations && !token
                    .IsCancellationRequested; i++)
                {
                    UpdateMatrix(area);

                    if (i % Settings.Default.DisplayInterval == 0)
                    {
                        OnImageGenerated(area, ColorSchema.GenerateBitmap(area), sw.Elapsed);
                    }
                }
                sw.Stop();
                Finished = true;
                OnImageGenerated(area, ColorSchema.GenerateBitmap(area), sw.Elapsed);
            }, token);
        }

        public void Stop()
        {
            cancellationTokenSource.Cancel();
        }

        protected abstract void UpdateMatrix(Area area);

        public event EventHandler<EventArgs<Tuple<Area, Bitmap, TimeSpan>>> ImageGenerated;
        protected void OnImageGenerated(Area area, Bitmap bitmap, TimeSpan timespan)
        {
            var handler = ImageGenerated;
            if (handler != null) handler(this, new EventArgs<Tuple<Area, Bitmap, TimeSpan>>(new
                Tuple<Area, Bitmap, TimeSpan>(area, bitmap, timespan)));
        }
    }
}
```

## 2.3. Parallel Version

For the parallel execution, `Parallel.ForEach` gets used instead of a normal loop. The calculation gets splitted into tiny parts of work. For the separation into separate parts, a `Partitioner` gets used which splits the width for the calculation.

Listing 3. *ParallelImageGenerator.cs*

```
using System.Collections.Concurrent;
using System.Threading.Tasks;

namespace Diffusions.Generators
{
    public class ParallelImageGenerator : ImageGenerator
    {
        protected override void UpdateMatrix(Area area)
        {
            lock (area.Matrix)
            {
                var m = area.Matrix;
                var partitioner = Partitioner.Create(0, area.Width);

                Parallel.ForEach(partitioner, (partRange, _) =>
                {
                    for (int x = partRange.Item1; x < partRange.Item2; x++)
                    {
                        int pX = (x + area.Width - 1) % area.Width;
                        int nX = (x + 1) % area.Width;

                        for (int y = 0; y < area.Height; y++)
                        {
                            int pY = (y + area.Height - 1) % area.Height;
                            int nY = (y + 1) % area.Height;
                            area.NextMatrix[x, y] = (
                                m[pX, pY] + m[pX, y] + m[pX, nY] +
                                m[x, pY] + m[x, nY] +
                                m[nX, pY] + m[nX, y] + m[nX, nY]) / 8;
                        }
                    }
                });
                var tmp = area.NextMatrix;
                area.NextMatrix = area.Matrix;
                area.Matrix = tmp;
            }
        }
    }
}
```

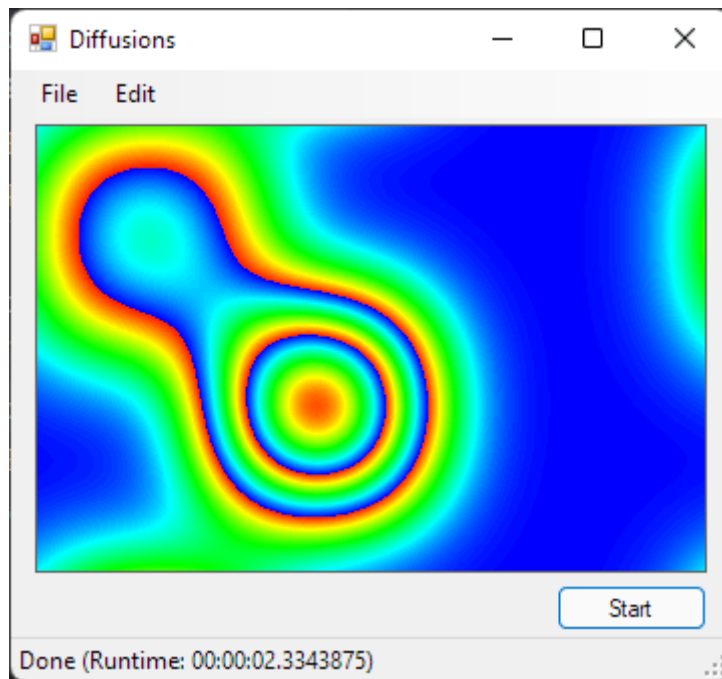


Figure 1. Parallel result

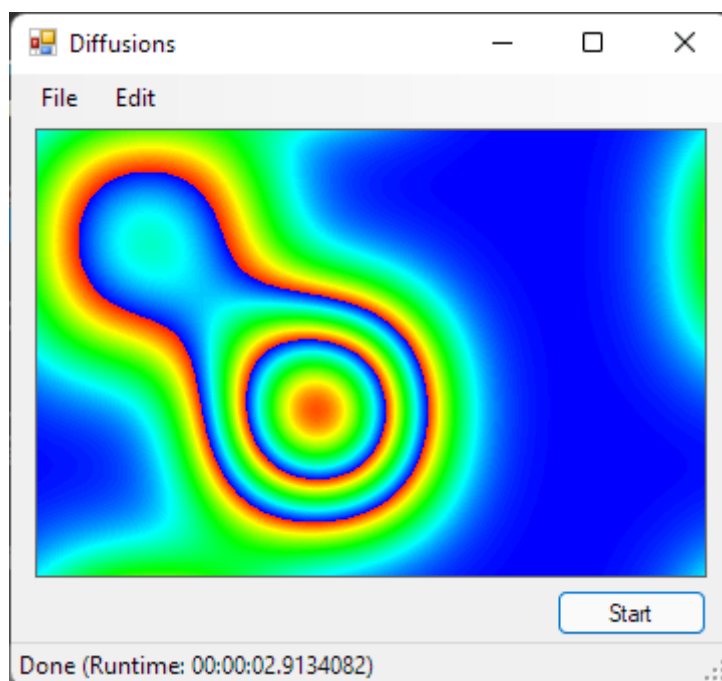


Figure 2. Sequential result

### 2.3.1. Speedup

$$\text{Speedup} = 2,9134082 / 2,334388 = 1,24804$$

The parallel version is 24,804 percent faster than the sequential one.

## 3. Parallel Numerical Integration

### 3.1. C++ OpenMP

*Listing 4. ParallellImageGenerator.cs*

```
double integrateOMP(double min, double max, int steps) {  
    double stepSize = (max - min) / steps;  
    double result = 0.0;  
  
    #pragma omp parallel for reduction(+:result)  
    for (int i = 0; i < steps; i++) {  
        result += f(min + stepSize * i) * stepSize;  
    }  
    return result;  
}
```

### 3.2. C# .NET Task Parallel Library

The calculation gets separated into steps with the `Partitioner`, similar to the the OpenMP solution. Additionally `Parallel.ForEach` gets called, the initial state gets set to zero. For the second part all partitioned parts gets calculated separately. The result gets added to the total result. To prevent race conditions, an lock object is needed when a part sum gets added to the total sum.



Listing 5. Program.cs

```
private static double IntegrateParallel(double min, double max, int steps)
{
    double stepSize = (max - min) / steps;
    double totalResult = 0.0;

    object lockObj = new();
    var partitioner = Partitioner.Create(0, steps);
    Parallel.ForEach(partitioner,
        () => 0.0, // Initial state
        (range, _, startValue) =>
        {
            double result = startValue;
            for (int i = range.Item1; i < range.Item2; i++)
            {
                result += F(min + i * stepSize) * stepSize;
            }
            return result;
        },
        result =>
        {
            lock (lockObj) // Lock sum obj
            {
                totalResult += result; // Add to total sum
            }
        });

    return totalResult;
}
```

Both sequential and parallel versions of the C# implementation are slower than the C++ version. With low step size the sequential version are much faster. There is obviously more overhead with the .NET Parallel task library and the C# version. Although with higher results the time for the parallel execution is nearly the same.

C#				
Step Size	ResultSeq	TimeSeq	ResultPar	TimePar
65	3,156937821	222	3,156937821	209
650	3,143130721	2	3,143130721	81
6500	3,141746496	31	3,141746496	105
65000	3,141608038	201	3,141608038	364
650000	3,141594192	2071	3,141594192	2770
6500000	3,141592807	19208	3,141592807	27551
65000000	3,141592669	181979	3,141592669	27968
C++				
Step Size	ResultSeq	TimeSeq	ResultPar	TimePar
65	3,15694	0	3,15694	53
650	3,14313	1	3,14313	12
6500	3,14175	11	3,14175	6
65000	3,14161	111	3,14161	38
650000	3,14159	1103	3,14159	200
6500000	3,14159	11044	3,14159	2155
65000000	3,14159	108094	3,14159	21584

Figure 3. Statistics