Fift: A Brief Introduction

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Abstract

The aim of this text is to provide a brief description of Fift, a new programming language specifically designed for creating and managing TON Blockchain smart contracts, and its features used for interaction with the TON Virtual Machine [4] and the TON Blockchain [5].

Introduction

This document provides a brief description of Fift, a stack-based general purpose programming language optimized for creating, debugging, and managing TON Blockchain smart contracts.

Fift has been specifically designed to interact with the TON Virtual Machine (TON VM or TVM) [4] and the TON Blockchain [5]. In particular, it offers native support for 257-bit integer arithmetic and TVM cell manipulation shared with TVM, as well as an interface to the Ed25519-based cryptography employed by the TON Blockchain. A macro assembler for TVM code, useful for writing new smart contracts, is also included in the Fift distribution.

Ed25519 是一種特定的橢圓曲線數位簽章演算法(EdDSA)基於 Twisted Edwards 曲線演化;這種演算法具有高效、安全和快速的特性, 非常適合現代的加密應用;Ed25519 提供強大的安全性, 並且可以在高效 的情況下進行簽名和驗證操作。

- 1) 安全: Ed25519 被設計成在當前已知攻擊方法下非常安全。
- 快速:簽名和驗證操作都非常快速,適合需要有效率處理大量交易的區塊鏈環境。
- 簡單:演算法的實現相對簡單,減少了實施錯誤的風險。

在 TON 區塊鏈中,Ed25519 被用於各種加密操作,特別是數字簽名。數字簽名在區塊鏈中具有關鍵作用,確保了交易的完整性和不可否認性,

並允許開發者在其應用程式中使用 Ed25519 進行加密操作。

Being a stack-based language, Fift is not unlike Forth. Because of the brevity of this text, some knowledge of Forth might be helpful for understanding Fift. However, there are significant differences between the two languages. For instance, Fift enforces runtime type-checking, and keeps values of different types (not only integers) in its stack.

- 運行時檢查類型:Fift 語言會檢查每個數據的類型,確保數據的操作符合其類型規則。這有助於捕捉運行時的錯誤,避免崩潰。
- 多類型支持: Fift 的堆疊中可以存放多種類型的數據, 而不僅僅是整數。這意味著它可以處理更豐富的數據結構和操作。
- 支持的數據類型:除了整數之外, Fift 還支持其他數據類型, 如字符串、浮點數、單元格(cells)、切片(slices)等。

A list of words (built-in functions, or primitives) defined in Fift, along with their brief descriptions, is presented in Appendix A.

¹Good introductions to Forth exist; we can recommend [1]. Please note that the current version of this document describes a preliminary test version of Fift; some minor details are likely to change in the future

1 Overview

Fift is a simple stack-based programming language designed for testing and debugging the TON Virtual Machine [4] and the TON Blockchain [5], but potentially useful for other purposes as well.

When Fift is invoked (usually by executing a binary file called fift), it either reads, parses, and interprets one or several source files indicated in the command line, or enters the interactive mode and interprets Fift commands read and parsed from the standard input. There is also a "script mode", activated by command line switch -s, in which all command line arguments except the first one are passed to the Fift program by means of the variables \$n and \$#. In this way, Fift can be used both for interactive experimentation and debugging as well as for writing simple scripts.

- Fift 是 TON 區塊鏈的腳本語言,它有多種運行模式,這讓它非常靈活。
 - 1] 當 Fift 被調用時(通常是執行名為 fift 的二進制文件), 它可以讀取、解析並解釋命令行中指定的一個或多個源文件。 這意味著你可以通過命令行指定一個或多個 .fif 文件, Fift 會按順序執行這些文件中的指令。
 - 如果沒有指定源文件, Fift 會進入交互模式, 等待用戶在標準輸入(通常是終端)中輸入命令。 在這種模式下, 你可以手動輸入 Fift 命令並立即看到執行結果, 這對於實驗和調試非常有用。
 - 3) 使用命令行-5可啟動腳本模式。這種模式下,第一個命令行參數外的所有參數都會通過變量 \$n 和 \$# 傳遞給 Fift 程序。 \$n 表示第 n 個參數, \$# 表示參數總數。使 Fift 可編寫簡單的腳本, 這些腳本可以從命令行接收參數並進行處理。

All data manipulated by Fift is kept in a (LIFO) stack. Each stack entry is supplemented by a type tag, which unambiguously determines the type of the value kept in the corresponding stack entry. The types of values supported by Fift include Integer (representing signed 257-bit integers), Cell (representing a TVM cell, which consists of up to 1023 data bits and up to four references to other cells as explained in [4]), Slice (a partial view of a Cell used for parsing cells), and Builder (used for building new cells). These data types (and their implementations) are shared with TVM [4], and can be safely passed from the Fift stack to the TVM stack and back when necessary (e.g., when TVM is invoked from Fift by using a Fift primitive such as runvmcode).

- LIFO (Last In, First Out): 所有由 Fift 操作的數據都存儲在一個"後進先出"堆疊中, 這意味最新壓入堆疊的數據會最先被取出。
 - 只需要兩種基本操作:壓入(push)和彈出(pop), 這使得 LIFO 堆疊的實現和使用都非常簡單。
 - LIFO 堆疊不需要複雜的內存分配和釋放操作,它可以在運行時高效地管理內存,減少內存碎片。
 - 處理多任務或協程時,可以有效地保存和恢復上下文,使得系統能夠快速切換任務,提高並發處理能力。 每次操作都是對堆疊頂部的數據進行處理,LIFO 結構有助於避免數據混亂,確保數據處理的順序性。
- 每個堆疊條目都自帶類型標記,明確標識該條目中存儲的數據類型,確保在操作數據時,不會發生類型錯誤。
 - Integer:代表有符號的 257 位整數。
 - 用於數學計算和邏輯操作。
 - Cell:代表一個 TVM 單元格。每個單元格最多包含 1023 位數據位和最多四個對其他單元格的引用。
 - 用於存儲和傳輸複雜數據結構。
 - Slice: 單元格的一部分視圖, 用於解析單元格。
 - 用於從單元格中提取和解析數據。
 - Builder:用於構建新單元格的對象。
 - 用於創建和填充單元格數據。

In addition to the data types shared with TVM, Fift introduces some unique data types, such as <u>Bytes</u> (arbitrary byte sequences), <u>String</u> (UTF-8 strings), <u>WordList</u>, and <u>WordDef</u> (used by Fift to create new "words" and manipulate their definitions). In fact, Fift can be extended to manipulate arbitrary "objects" (represented by the generic type <u>Object</u>), provided they are derived from C++ class td::CntObject in the current implementation.

- 除了與 TVM 共享的數據類型(如 Integer、Cell、Slice 和 Builder)外,Fift 還引入了一些獨特的數據類型:
 - Bytes:用於處理和存儲原始的二進制數據。
 - String:用於處理和存儲 UTF-8 編碼的文本數據, 特別是支持多語言和特殊字符。
 - WordList:一個列表, 用於存儲"單詞"(Fift 中的指令或命令)的列表。
 - 用於管理和操作多個 Fift 指令的集合。
 - WordDef: 定義新的"單詞"(Fift 指令)的結構。
 - 用於創建和操作新的 Fift 指令及其定義。
 - Object:用於表示任意"對象"的通用類型, 允許 Fift 操作更複雜和自定義的數據結構。
 - 條件: 這些對象需要從當前實現中的 C++ 類 td::CntObject 派生。

Fift source files and libraries are usually kept in text files with the suffix .fif. A search path for libraries and included files is passed to the Fift executable either in a -I command line argument or in the FIFTPATH environment variable. If neither is set, the default library search path /usr/lib/fift is used.

On startup, the standard Fift library is read from the file Fift.fif before interpreting any other sources. It must be present in the library search path, otherwise Fift execution will fail.

A fundamental Fift data structure is its global dictionary, containing words—or, more precisely, word definitions—that correspond both to built in primitives and functions and to user-defined functions.² A word can be executed in Fift simply by typing its name (a UTF-8 string without space characters) in interactive mode. When Fift starts up, some words (primitives) are already defined (by some C++ code in the current implementation); other words are defined in the standard library Fift.fif. After that, the user may extend the dictionary by defining new words or redefining old ones.

- 定義詞 (Word Definitions)
 - 詞(word):在 Fift 中, 詞是一個不包含空格字符的 UTF-8 字符串, 它代表一個操作或函數。
 - 內置詞(primitive words):這些詞在 Fift 啟動時已經定義好了,通常是由 C++ 代碼實現的基本操作。
 - 標準庫詞:這些詞定義在標準庫文件 Fift.fif 中, 在 Fift 啟動時會自動讀取和定義。
 - 用戶定義詞:用戶可以通過編寫代碼來定義新的詞,或者重定義已有的詞。
- 執行詞 (Executing Words in interactive mode)
 - 在交互模式中, 你只需要輸入詞的名字, Fift 解析器就會找到並執行這個詞。
 - 例如, 輸入 10 20 + . 將執行加法操作並打印結果。
- 詞的來源 (Source of Words)
 - 1. 內置詞:這些詞在 Fift 啟動時就已經存在, 提供基本的操作和功能。
 - 2. 標準庫: Fift.fif 文件中定義了一些常用的詞, 這些詞在 Fift 啟動時被讀取和加載。
 - 3. 用戶定義:用戶可以在交互模式或源文件中定義自己的詞或改變舊有詞的定義。

The dictionary is supposed to be split into several vocabularies, or name spaces; however, namespaces are not implemented yet, so all words are currently defined in the same global namespace.

The Fift parser for input source files and for the standard input (in the interactive mode) is rather simple: the input is read line-by-line, then blank characters are skipped, and the longest prefix of the remaining line that is (the name of) a dictionary word is detected and removed from the input line. After that, the word thus found is executed, and the process repeats until the end of the line. When the input line is exhausted, a subsequent line is read from the current input file or the standard input.

Fift 解析器負責讀取和解釋輸入的源文件和交互模式下的標準輸入。 (概念形態像我們平時打字時那條一閃一閃的直積)簡單的 Fift 程序例子如下:

```
1. 讀取第一行:
     ○ 解析器讀取整行 10 20 + . cr。
2. 跳過字符:
     ○ 行首沒有操作符,所以直接進入下一步。(操作符就是不會進入堆疊的Fift指令)
3. 檢測並執行字典詞:
       解析器檢測到 10 是一個字典詞, 並將其從輸入行中移除。
     ○ 執行 10, 將數字 10 壓入堆疊。(Just like "剪下" & "貼上" to TVM stack。)
     ○ 接著檢測 20, 並將其移除。
       執行 20, 將數字 20 壓入堆疊。
        然後檢測+,並將其移除。(操作符"+"會直接執行,不會進入堆疊。)
        執行+,從堆疊中彈出兩個數字,計算它們的和(10+20=30),並將結果30壓入堆疊。
        執行,將堆疊頂部的數字(30)打印出來。
       最後檢測 cr, 並將其移除。(操作符 "cr"會直接執行, 不會進入堆疊。)
     ○ 執行 cr, 輸出一個換行符。
4. 讀取下一行:
        當前行被完全解析和執行後,解析器會讀取下一行。
       如果沒有更多行,解析器將結束執行。
```

Fift 通過逐行讀取輸入、跳過空白字符、檢測和執行字典詞來解析和執行程序。 這種簡單而有效的解析方式,使得 Fift 能夠高效地處理和執行源文件和交互模式下的指令。

In order to be detected, most words require a blank character or an end-of-line immediately after them; this is reflected by appending a space to their names in the dictionary. Other words, called *prefix words*, do not require a blank character immediately after them.

- 大多數字典詞:
 - "10"需要在後面有一個空白字符"10"或行結束符才能被檢測到。
 - 字典中的名稱通常會附加一個空格來反映這一點。
- 前綴詞 (prefix words):
 - 不需要在後面有空白字符, 可以直接檢測到。
 - 例如, 類似 "@" 或 "+" 的前綴詞可以直接連接數值"+10"或其他字符。

If no word is found, the string consisting of the first remaining characters of the input line until the next blank or end-of-line character is interpreted as an *Integer* and pushed into the stack. For instance, if we invoke Fift, type 2 3 + . (and press Enter), Fift first pushes an *Integer* constant equal to 2 into its stack, followed by another integer constant equal to 3. After that, the built-in primitive "+" is parsed and found in the dictionary; when invoked, it takes the two topmost elements from the stack and replaces them with their sum (5 in our example). Finally, "." is a primitive that prints the decimal representation of the top-of-stack *Integer*, followed by a space. As a result, we observe "5 ok" printed by the Fift interpreter into the standard output. The string "ok" is printed by the interpreter whenever it finishes interpreting a line read from the standard input in the interactive mode. A list of built-in words may be found in Appendix A.

無法找到:如果解析器在字典中找不到字典詞,它會將輸入行中從當前字符開始到下一個空白字符或行結束符之間的字符串解釋為一個整數(Integer),解析器會將這個整數推入堆疊。

²Fift words are typically shorter than functions or subroutines of other programming languages. A nice discussion and some guidelines (for Forth words) may be found in [2]. ³Notice that in contrast to Forth, Fift word names are case-sensitive: dup and DUP are distinct words.

2 Fift basics

This chapter provides an introduction into the basic features of the Fift programming language. The discussion is informal and incomplete at first, but gradually becomes more formal and more precise. In some cases, later chapters and Appendix A provide more details about the words first mentioned in this chapter; similarly, some tricks that will be dutifully explained in later chapters are already used here where appropriate.

2.1 List of Fift stack value types

Currently, the values of the following data types can be kept in a Fift stack:

- Integer A signed 257-bit integer. Usually denoted by x, y, or z in the stack notation (when the stack effect of a Fift word is described).
- Cell A TVM cell, consisting of up to 1023 data bits and up to 4 references to other cells (cf. [4]). Usually denoted by c or its variants, such as c or c2.
- Slice A partial view of a TVM cell, used for parsing data from Cells. Usually denoted by s.
- Builder A partially built Cell, containing up to 1023 data bits and up to four references; can be used to create new Cells. Usually denoted by b.
- Null A type with exactly one "null" value. Used to initialize new Boxes. Usually denoted by \bot .
- Tuple An ordered collection of values of any of these types (not necessarily the same); can be used to represent values of arbitrary algebraic data types and Lisp-style lists.
- **String** A (usually printable) UTF-8 string. Usually denoted by **S**.
- Bytes An arbitrary sequence of 8-bit bytes, typically used to represent binary data. Usually denoted by B.
- WordList A (partially created) list of word references, used for creating new Fift words definitions. Usually denoted by I.
- WordDef An execution token, usually representing the definition of an existing Fift word. Usually denoted by e.
- Box A location in memory that can be used to store one stack value. Usually denoted by p.
- Atom A simple entity uniquely identified by its name, a string. Can be used to represent identifiers, labels, operation names, tags, and stack markers. Usually denoted by a.
- Object An arbitrary C++ object of any class derived from base class td::CntObject; may be used by Fift extensions to manipulate other data types and interface with other C++ libraries.

The first six types listed above are shared with TVM; the remainder are Fift-specific. Notice that not all TVM stack types are present in Fift. For instance, the TVM Continuation type is not explicitly recognized by Fift; if a value of this type ends up in a Fift stack, it is manipulated as a generic Object.

2.2 Comments

Fift recognizes two kinds of comments: "// " (which must be followed by a space) opens a single-line comment until the end of the line, and /* defines a multi-line comment until */. Both words // and /* */ are defined in the standard Fift library (Fift.fif).

2.3 Terminating Fift

The word bye terminates the Fift interpreter with a zero exit code. If a non-zero exit code is required (for instance, in Fift scripts), one can use word halt, which terminates Fift with the given exit code (passed as an *Integer* at the top of the stack). In contrast, quit does not quit to the operating system, but rather exits to the top level of the Fift interpreter.

- bye:終止 Fift 解釋器,返回 O 退出代碼。
- halt:終止 Fift 解釋器, 返回堆疊頂部指定的整數退出代碼。
- quit:退出當前上下文,返回 Fift 解釋器的頂層,而不終止解釋器。

2.4 Simple integer arithmetic

When Fift encounters a word that is absent from the dictionary, but which can be interpreted as an integer constant (or "literal"), its value is pushed into the stack (as explained in 2.8 in more detail). Apart from that, several integer arithmetic primitives are defined:

- 整數算術原語(integer arithmetic primitives)只是 "操作符" 的一種。
- + (x y x + y), replaces two *Integers* x and y passed at the top of the stack with their sum x + y. All deeper stack elements remain intact. If either x or y is not an *Integer*, or if the sum does not fit into a signed 257-bit *Integer*, an exception is thrown.
 - "+ (x y x + y)" 當中的 "-" 不是減號,單純用以表示操作的過渡。(也能夠理解為操作符在 Stack 當中的擺放位置)

- 這種表示法是一種標準的堆疊操作語法、常見於基於堆疊的語言。
 "+ (xy x+y)"表示操作符 "+" 在執行的時候:
 a. "-" 表示推疊的變化以及操作的過渡。
 b. "x+y"表示 "x" 和 "y" 的和. 並取代堆疊中的 "xy"。
 (x y x y), computes the difference x y of two *Integers* x and y. Notice that the first argument x is the second entry from the top of the stack, while the second argument y is taken from the top of the stack.
 negate (x -x), changes the sign of an *Integer*.
 在這裏 "negate" 是操作符, 讓 "x" 要成 "-x"。
 * (x y xy), computes the product xy of two *Integers* x and y.

• /(x y - q := x/y), computes the floor-rounded quotient x/y of two Integers.

- Fift 堆疊不直接支持存儲小數。如果需要處理小數,可以使用定點數表示法或字串(String)表示。
 所以 20 / 3, 結果是 6(因為 20 / 3 = 6 並向下取得較小整數)
- q:=x/y:表示計算 "x" 除以 "y" 的商, ":=" 是賦值運算符, 表示將 "x/y" 計算結果賦值給變量 "q"。
- mod(x y r) = x mod y, computes the remainder x mod $y = x y \cdot x/y$ of division of x by y.
 - r:= x mod y:表示計算結果, "r"是"x"除以"y"的餘數。
 所以 20 / 3, 結果是 2(因為 20 / 3 的餘數是 2)
- /mod(x y q r), computes both the quotient and the remainder.
 - "/mod"操作符會彈出 "x" & "y", 並一次過傳兩個數值 "q" & "r" 回到堆疊, "r" 會在堆疊頂部。
 "q" 就是 "x/y" 得到的整數部分(整數商 aka 向下取整);"r" 就是 ":= r mod y"。
 - 首先將 "q" 推入堆疊,然後將 "r" 推入堆疊,因此 "r" 在堆疊頂部,"q" 在其下方。
- /c, /r (x y q), division words similar to /, but using ceiling rounding (q := x/y) and nearest-integer rounding (q := 1/2 + x/y), respectively.
 - 這裏分別表示了 "q" 在兩種不同情況下所輸出的單一的數值:
 - "/c":除法操作符, 使用向上取整(ceiling rounding)。
 - **(**xy-q:=ceil(x/y)):表示計算結果 "q" 是 "x" 除以 "y", 並向上取得較大整數。例如: `x=19, y=3`, 計算 `19/3` 的結果約為 `6.33`, 向上取整為 `7`。 因此: `q := ceil(19/3)`, `q=7`。
 - "/r":除法操作符,使用最接近整數的取整(nearest-integer rounding)。
 - **(**xy q:=round(x/y)**)**:表示計算結果 "q" 是 "x" 除以 "y", 並向上取得四捨五入的整數。例如: `x=19, y=3`, 計算 `19/3` 的結果約為 `6.33`, 四捨五入為 `6`。 因此: `q := round(19/3)`, `q=6`。
- /cmod, /rmod (x y q r := x q y), division words similar to /mod, but using ceiling or nearest-integer rounding.
 - "/c mod"以及 "/r mod"同樣地會彈出 "x"&"y", 並一次過傳兩個數值 "q"&"r"回到堆疊, "r"會在堆疊頂部。
 - "/cmod" 所得出的 "q", 使用向上取整(ceiling rounding);"r" 將會是 "x" 減去 "qy" 的結果。
 - o "/rmod" 所得出的 "q", 使用四捨五入取整(nearest-integer rounding); "r" 同樣是 "x" 減去 "qy" 的結果。
- $<<(xy-x\cdot2^{y})$, computes an arithmetic left shift of binary number x by $y \ge 0$ positions, yielding $x\cdot2^{y}$.
 - "<<"操作符(左移操作)在計算機科學和數字處理中有多種重要的用途。這裡是一些常見的應用和意義
 - 快速乘法應用:
 - 譲我們首先設定 "x = 3" & "y = 4",讓我們更好地在例子中了解操作:
 "x y <<" 將會是 "3 4 <<" 所以計算將會是 "3 * 2^4",因此在這個情況下會得出 "48"。
 (這比 * 來乘以 2 的次方更高效,由於左移操作直接在二進制級別進行運算,計算速度更快。)
 (計算結果最終以十進制數值儲存,但在內存/內部運算過程中,實際上以二進制形式處理數據。)
 - 寄存器操作(Register Operations):
 - 寄存器是計算機處理器內部的一種快速存儲設備,用於臨時存儲數據和指令。 我們可以利用 "<<" 對寄存器進行定位,進而設置、清除、切換當中的數值。
 - 設置位:將寄存器中的某一位設置為 l。
 - 清除位:將寄存器中的某一位設置為 **0**。
 - 切換位:將寄存器中的某一位從□切換為1或從1切換為□。
 - 假設我們有一個寄存器 reg:
 - 設置第 n 位為 1:reg = reg | (1 << n)
 - 清除第 n 位為 0:reg = reg & ~(1 << n)
 - 切換第 n 位的值: reg = reg **^ (**1 << n**)**
 - 位掩碼(Bit Masking):
 位掩碼和寄存器操作都是在位級別進行數據操作的技術, 但它們的應用範圍和對象有所不同。
 - 數據打包(Data Packing):
 - 舉個例子:a=0b1100, b=0b0011
 packed = (a<<4) | b 就是packed = 0b11000011
- >> $(x \lor g := x \cdot 2^{-y})$, computes an arithmetic right shift by $y \ge 0$ positions.
 - 可以理解 ">>" 操作符是 "<<" 操作符的相反方向功能。
 - 快速乘法應用:
 - 讓我們首先設定 "x = 48" & "y = 4", 讓我們更好地在例子中了解操作:
 "x y >>"將會是 "48 4 >>"所以計算將會是 "48 / 2^4", 因此在這個情況下會得出 "3"。
 (這比 / 來除以 2 的次方更高效, 由於左移操作直接在二進制級別進行運算, 計算速度更快。

```
■ 由於 "x" 有可能少於 "y", 先假設 "x = 1" & "y = 4", 進行右移操作:
                        ● ">>"將會是"1 4 >>"所以計算將會是"1 / 2^4",因此在這個情況下會得出"O"。
• >> c, >> r(x y - q), similar to >>, but using ceiling or nearest-integer rounding.
   ● ">>c" 是 ">>" 的變種, 結果 "q" 將會向上取整(ceiling rounding):
      ">>r" 也是 ">>" 的變種,結果 "q" 將會四捨五入取整(nearest-integer rounding):
             假設 x = 49 和 y = 4:
             四捨五入後, 結果 q = 3
• and (\&), or (|), xor (\oplus) (xy - x \oplus y), compute the bitwise AND, OR, or XOR of two Integers.
   ● "and"操作符將兩個整數的每個位進行 "同為 1" 的對照, 僅當兩個同位置數值都是 1, 結果位才為 1。
                  0101 (5)
              and 0011 (3)
              結果: 0001 (1)
      "or" 操作符將兩個整數的每個位進行 "存在 1" 的對照,當其中一個同位置數值是 1,結果位就是 1。
                  0101 (5)
              or 0011 (3)
              結果: 0111 (7)
      "xor" 作符將兩個整數的每個位進行 "不同位" 的對照, 僅當同位置數值不相同, 結果位為 1。
                  0101 (5)
      它們在硬件控制、數據壓縮、加密以及其他需要直接操作二進制數據的領域中非常有用。
• not (x - -1 - x), bitwise complement of an Integer.
      "not"就是把一個二進制整數逐位取反,具體來說,它會將數值中每一位從 θ 變成 1,或者從 1 變成 θ。
      "not (x - -1-x)"的數學表示可能令人困惑,因為它使用了負一"-1"進行計算。
       讓我們更詳細地解釋過程, 並比較其他可能的表示:
          ○ 設 x = 5, 二進制表示為 00000101。
              -1 的二進制是 111111111。
              所以 "-1-x" 就是 11111111 - 00000101, 效果將每一位從 0 變成 1, 或從 1 變成 0。(真神奇)
• */ (X \ Y \ Z - X \ Y \ Z), "multiply-then-divide": multiplies two integers x and y producing a 513-bit intermediate result, then divides the product by z.
      "*/" 不單純是一個乘除 combo,在處理乘數部份"x*y"時,還確保了其間結果不會因為位數溢出而丟失數據。
             當兩個 256 bit 整數相乘, 最大可能的結果是 513 bit(256 bit + 256 bit + 負數可能的符號位)
• */mod (x y z - q r), similar to */, but computes both the quotient and the remainder.
   ● "*/mod" 就是以上的乘除 combo (當然彈出 xyz)但同時把向下取整的整數商"q"及餘數"r"兩個數推入堆疊。
• */c, */r (x \ y \ z - q), */cmod, */rmod (x \ y \ z - q \ r), similar to */ or */mod, but using ceiling or nearest-integer rounding.
   ● 也是乘除 combo 的變種,"*/c" 把向上取整的商推入堆疊,"*/r" 把四捨五入的商推入堆疊。
   ● 亦提及了_"*/cmod" & "*/rmod" 就是乘除 combo +"/cmod" 或 "/rmod" 的混合變種, 推相應的 "q" 及 "r" 進堆疊。
• *>>, *>>c, *>>r (x \ y \ z - q), similar to */ and its variants, but with division replaced with a right shift. Compute q = xy/2^z rounded in the indicated fashion (floor,
ceiling, or nearest integer).
      是乘積 + ">>" 的混合變種, "*>>" / "*>>c" / "*>>r" 將會分別得出 "x*y" 乘積 + 右移 "z" 位
       並分別以向下取整 / 向上取整 / 四捨五入的 "q" 作為結果。
      TON 區塊鏈中, 每個數字最多表示為 256 bit 的有符號整數。因此, 256 bit 數字相乘, 生成的 512 bit 中間結果不會直接存儲在 TON, 最終結果需要適應 256 位的限制, 避免溢出。
• <</, <</c, <</r (x \ y \ z - q), similar to */, but with multiplication replaced with a left shift. Compute q = 2^z x/y rounded in the indicated fashion (notice the different
order of arguments y and z compared to */).
   ● "<</"/ "<</c" / "<</r" 就是把 "x" 左移 "y" 位再除 "z", 得出 "q" 推入堆疊。
       分別會得出向下取整/向上取整(天花板取整)/四捨五入取整的 "q"。
```

負數的二進制表示和位移操作:

■ 由於 "x" 有可能是負數, 先假設 "x = -48" & "y = 4", 進行右移操作:

"x" 小於 "y" 或出現小數或分數的處理:(">>c " & ">>r" 就是用來專門應對這種情況)

● ">>"將會是"-48 4 >>"所以計算將會是"-48 / 2^4",因此在這個情況下會得出"-3"。

The above primitives can be employed to use the Fift interpreter in interactive mode as a simple calculator for arithmetic expressions represented in reverse Polish notation (with operation symbols after the operands). For instance,

In addition, the word "." may be used to print the decimal representation of an Integer passed at the top of the stack (followed by a single space), and "x." prints the

hexadecimal representation of the top-of-stack integer. The integer is removed from the stack afterwards.

```
74-.
computes 7 - 4 = 3 and prints "3 ok", and
234*+
23+4*.
computes 2 + 3 \cdot 4 = 14 and (2 + 3) \cdot 4 = 20, and prints "14 20 ok".
       這些基本操作符可以用來在交互模式下將 Fift 解釋器作為一個簡單的計算器來使用,
        處理以逆波蘭記法表示的算術表達式(運算符在操作數之後)。
2.5 Stack manipulation words
Stack manipulation words rearrange one or several values near the top of the stack, regardless of their types, and leave all deeper stack values intact. Some of the most
often used stack manipulation words are listed below:
    ● 以下是單純用來新增 / 移除及調動 Stack 擺位的操作符。
• dup (x - x x), duplicates the top-of-stack entry. If the stack is empty, throws an exception.<sup>4</sup>
• drop (x - ), removes the top-of-stack entry.
• SWap (X y - y X), interchanges the two topmost stack entries.
• rot (X y Z - y Z X), rotates the three topmost stack entries. (把第 3 個數值"旋"到堆疊頂部的意思)
• -rot (x y z - z x y), rotates the three topmost stack entries in the opposite direction.
    ● 原文有表示 "Equivalent to rot rot.",但我(YC)認為這樣描述並不恰當,會引致誤會。(把堆疊頂部數值"旋"到第3位)
• OVER (X \ Y - X \ Y \ X), creates a copy of the second stack entry from the top over the top-of-stack entry.
(把第2個數值 copy 到堆疊頂部)
• tuck [x y - y x y], equivalent to swap over. (swap 完再把第 2 個數值 copy 到堆疊頂部)
• nip(xy-y), removes the second stack entry from the top. Equivalent to swap drop.
• 2dup(xy - xyxy), equivalent to double over.
• 2drop (x v - ), equivalent to double drop.
• 2swap (abcd-cdab), interchanges the two topmost pairs of stack entries.
• pick (x_n ... x_0 n - x_n ... x_0 x_n), creates a copy of the n-th entry from the top of the stack, where n \ge 0 is also passed in the stack. In particular, 0 pick is equivalent
    • [1, 2, 3, 4, 5, 6], "0 pick" 就會是[1, 2, 3, 4, 5, 6, 6]。
       [1, 2, 3, 4, 5, 6], "2 pick"就會是 [1, 2, 3, 4, 5, 6, 4]。
• roll (x_n ... x_0 n - x_{n-1} ... x_0 x_n), rotates the top n stack entries, where n \ge 0 is also passed in the stack. In particular, 1 roll is equivalent to swap, and 2 roll to rot.
    ● [a, b, c, d, e, f], "3 roll"就會是 [a, b, d, e, f, c]。(就是"滾"回堆疊頂部的意思)
       [1, 2, 3, 4, 5, 6], "5 roll"就會是[2, 3, 4, 5, 6, 1]。
        5 4 3 2 1 0 < - Stack 的位置, 5 roll 就是把第 5 號位置的數值放在 Stack 的頂部。
• -roll (x_n \dots x_0 n - x_0 x_n \dots x_1), rotates the top n stack entries in the opposite direction, where n \ge 0 is also passed in the stack. In particular, 1 -roll is equivalent to
swap, and 2 -roll to -rot.
    ● [a, b, c, d, e, f], "3 -roll" 就會是 [a, b, f, c, d, e]。(就是從堆疊頂部"滾"到某個特定位置的意思)
       [1, 2, 3, 4, 5, 6], "5 -roll" 就會是 [6, 1, 2, 3, 4, 5]。
• exch (x_n \dots x_0 n - x_0 \dots x_n), interchanges the top of the stack with the n-th stack entry from the top, where n \ge 0 is also taken from the stack. In particular, 1 exch
is equivalent to swap, and 2 exch to swap rot.
```

[a, b, c, d, e, f],"2 exch" 就會是 [a, b, c, f, e, d]。

- [a, b, c, d, e, f], "3 exch" 就會是 [a, b, f, d, e, c]。(就是堆疊的頂部與某個特定位置數值 "exchange" 的意思) 5 4 3 2 1 0 < 一 Stack 的位置,3 exch 就是把 Stack 頂部的數值與第 3 號位置的數值調換位置。
- exch2 (...nm-...), interchanges the n-th stack entry from the top with the m-th stack entry from the top, where $n \ge 0$, $m \ge 0$ are taken from the stack.
 - [a, b, c, d, e, f], "2 5 exch2" 就會是 [d, b, c, a, e, f]。(就是某 2 個特定位置數值 "exchange" 的意思) 5 4 3 2 1 0 < Stack 的位置, 2 5 exch2 就是把第 2 號位置的數值的數值與第 5 號位置的數值調換位置。
- ?dup $(x x \times or 0)$, duplicates an *Integer x*, but only if it is non-zero. Otherwise leave it intact.
 - "?dup" 若果整數不為零的話便複製 Stack 最頂的數值。

For instance, "5 dup * ." will compute $5 \cdot 5 = 25$ and print "25 ok". One can use the word ".s"—which prints the contents of the entire stack, starting from the deepest elements, without removing the elements printed from the stack—to inspect the contents of the stack at any time, and to check the effect of any stack manipulation words. For instance,

1 2 3 4 .s rot .s

prints

1234

1342

ok

When Fift does not know how to print a stack value of an unknown type, it instead prints ???.

● ".s"操作符會打印整個堆疊的內容,從最深層的元素開始,而不會從堆疊中移除已打印的元素。這樣可以在任何時候檢查堆疊的內容,並檢查任何堆疊操作詞的效果,不明的類型會印出"????"。

2.6 Defining new words

In its simplest form, defining new Fift words is very easy and can be done with the aid of three special words: "{", "}", and ":". One simply opens the definition with { (necessarily followed by a space), then lists all the words that constitute the new definition, then closes the definition with } (also followed by a space), and finally assigns the resulting definition (represented by a *WordDef* value in the stack) to a new word by writing: new-word-name. For instance,

```
{ dup * } : square
```

defines a new word square, which executes dup and * when invoked. In this way, typing 5 square becomes equivalent to typing 5 dup *, and produces the same result [25]:

5 square.

prints "25 ok". One can also use the new word as a part of new definitions:

```
{ dup square square * } : **5 3 **5 .
```

prints "243 ok", which indeed is 35.

If the word indicated after ":" is already defined, it is tacitly redefined. However, all existing definitions of other words will continue to use the old definition of the redefined word. For instance, if we redefine square after we have already defined **5 as above, **5 will continue to use the original definition of square.

• {自定義操作符的動作}:自定義操作符的名稱,以上已經說明其用法。

2.7 Named constants

One can define (named) constants—i.e., words that push a predefined value when invoked—by using the defining word constant instead of the defining word ":" (colon). For instance,

● "constant" 用於定義命名常量, 這些常量在被調用時會將預定義的值壓入堆疊。

1000000000 constant Gram

defines a constant Gram equal to *Integer* 10⁹. In other words, 1000000000 will be pushed into the stack whenever Gram is invoked:

Gram 2 * .

prints "200000000 ok".

Of course, one can use the result of a computation to initialize the value of a constant:

Gram 1000 / constant mGram

mGram .

prints "1000000 ok".

The value of a constant does not necessarily have to be an *Integer*. For instance, one can define a string constant in the same way:

"Hello, world!" constant hello

hello type cr

prints "Hello, world!" on a separate line.

● "constant" 不單止可以用來定義數值,還能夠定義字串。

If a constant is redefined, all existing definitions of other words will continue to use the old value of the constant. In this respect, a constant does not behave as a global variable.

One can also store two values into one "double" constant by using the defining word 2constant. For instance,

355 113 2constant pifrac

defines a new word pifrac, which will push 355 and 113 (in that order) when invoked. The two components of a double constant can be of different types. If one wants to create a constant with a fixed name within a block or a colon definition, one should use =: and 2=: instead of constant and 2constant:

```
{ dup =: x dup * =: y } : setxy
3 setxy x . y . x y + .
7 setxy x . y . x y + .
produces
3 9 12 ok
7 49 56 ok
```

● 以上介紹了 "2constant" 可以一次過儲存兩個常數, 並說明了如何調用當中的數值。

If one wants to recover the execution-time value of such a "constant", one can prefix the name of the constant with the word @':

```
{ ."( " @' x . .", " @' y . .") " } : showxy
3 setxy showxy
produces
(3,9) ok
```

The drawback of this approach is that @' has to look up the current definition of constants x and y in the dictionary each time showxy is executed. Variables (cf. 2.14) provide a more efficient way to achieve similar results.

● 以上介紹了 "@' "如何過 "setxy" 調動當前的數值賦值 x & y, 再利用 "showxy" 產出結果。

2.8 Integer and fractional constants, or literals

Fift recognizes unnamed integer constants (called *literals* to distinguish them from named constants) in decimal, binary, and hexadecimal formats. Binary literals are prefixed by 0b, hexadecimal literals are prefixed by 0x, and decimal literals do not require a prefix. For instance, 0b1011, 11, and 0xb represent the same integer (11). An integer literal may be prefixed by a minus sign "-" to change its sign; the minus sign is accepted both before and after the 0x and 0b prefixes.

• Fift 會自然辨認 2 進制 ("0b" 開頭) 與 16 進制 ("0x" 開頭) 的數值, 並且全部數值都可標示為負數。

When Fift encounters a string that is absent from the dictionary but is a valid integer literal (fitting into the 257-bit signed integer type Integer), its value is pushed into the stack.

• Fift 會自然辨認字串(String)當中的數值, 並以數值型態傳出入堆疊。

Apart from that, Fift offers some support for decimal and common fractions. If a string consists of two valid integer literals separated by a slash /, then Fift interprets it as a fractional literal and represents it by two Integers p and q in the stack, the numerator p and the denominator q. For instance, -17/12 pushes -17 and 12 into the Fift stack (being thus equivalent to -17 12), and -0x11/0b1100 does the same thing. Decimal, binary, and hexadecimal fractions, such as 2.39 or -0x11.ef, are also represented by two integers p and q, where q is a suitable power of the base (10, 2, or 16, respectively). For instance, 2.39 is equivalent to 239 100, and -0x11.ef is equivalent to -0x11ef 0x100.

 Fift 支援小數和普通分數,如字串由斜線 / 分隔的兩個有效整數組成, Fift 會將其解釋為小數文字, 並使用堆疊中的兩個整數 p(分子)和 q(分母)表示。

Such a representation of fractions is especially convenient for using them with the scaling primitive */ and its variants, thus converting common and decimal fractions into a suitable fixed-point representation. For instance, if we want to represent fractional amounts of Grams by integer amounts of nanograms, we can define some helper words

```
1000000000 constant Gram { Gram * } : Gram* { Gram swap */r } : Gram*/
```

and then write 2.39 Gram*/ or 17/12 Gram*/ instead of integer literals 2390000000 or 1416666667.

If one needs to use such Gram literals often, one can introduce a new active prefix word GR\$ as follows:

{ bl word (number) ?dup 0= abort"not a valid Gram amount" 1- { Gram swap */r } { Gram * } condl 'nop } ::_ GR\$

- { bl (推入空格)word(讀取下一個以空格分隔的字典詞)(number)(讀取字典詞轉換為數值) ?dup ①(若不為 ① 則複製數值) = abort(若數值是 ② 輸出錯誤信息)"not a valid Gram amount"(信息) 1- (選擇執行哪個分支時所需的特殊邏輯) { Gram swap */r }(對分數進行縮放操作再四捨五入增加精準度) { Gram * }(直接放大至 Gram 單位的操作) cond1(根據分支邏輯選擇執行分支)'nop(告知編譯器再沒有任何操作) } ::_ GR\$(定義名為 "GR\$"的前綴詞)
- 如果輸入的是整數或小數,(number) 轉換後為 1(跳過中間條件check)經過 1- 後變成 0,這樣 condl 便執行{ Gram * }。
- 如果輸入的是分數, (number) 轉換後為 2, 經過 l- 後變成 l, 這樣condl就選擇執行 { Gram swap */r }。

makes GR\$3, GR\$2.39, and GR\$17/12 equivalent to integer literals 3000000000, 2390000000, and 1416666667, respectively. Such values can be printed in similar form by means of the following words:

```
{ dup abs <# ' # 9 times char . hold #s rot sign #> nip -trailing0 } : (.GR) { (.GR) ."GR$" type space } : .GR -17239000000 .GR
```

produces GR\$-17.239 ok. The above definitions make use of tricks explained in later portions of this document (especially Chapter 4).

• { dup(複製 Stack 頂部數值) abs(取絕對值) <# ' # 9 times char . hold #s rot sign #> nip -trailing0 } : (.GR)

We can also manipulate fractions by themselves by defining suitable "rational arithmetic words":

```
// a b c d -- (a*d-b*c) b*d
{ -rot over * 2swap tuck * rot - -rot * } : R-
// a b c d -- a*c b*d
{ rot * -rot * swap } : R*
// a b --
{ swap ._ ."/" . } : R.
1.7 2/3 R- R.
```

will output "31/30 ok", indicating that 1.7 - 2/3 = 31/30. Here "._" is a variant of "." that does not print a space after the decimal representation of an Integer.

2.9 String literals

String literals are introduced by means of the prefix word ", which scans the remainder of the line until the next " character, and pushes the string thus obtained into the stack as a value of type *String*. For instance, "Hello, world!" pushes the corresponding *String* into the stack:

```
"Hello, world!".s( "<-這個也是一個操作符)
```

2.10 Simple string manipulation

The following words can be used to manipulate strings: (字串操作符基礎)

- "string" (5), pushes a String literal into the stack. (推 String 入 Stack) • ."String" (—), prints a constant string into the standard output. (不入 Stack 直接 print) • type (5-), prints a String S taken from the top of the stack into the standard output. 彈出頂部的字串(String) 然後打印在 console • cr(-), outputs a carriage return (or a newline character) into the standard output. • emit (x —), prints a UTF-8 encoded character with Unicode codepoint given by *Integer* x into the standard output.(打印由整數 x 所指定的 Unicode 代碼點對應的 UTF-8 編碼字符 eg: "65" -> print "A") • char string (-x), pushes an Integer with the Unicode codepoint of the first character of string. 取出字符串的第一個字符,將該字符的 Unicode 代碼點轉換成整數,並將這個整數推入堆疊。 • bl (-x), pushes the Unicode codepoint of a space, i.e., 32. • 這個操作符不需要任何輸入, 直接將空格字符 ' 的 Unicode 代碼點 32 推入堆疊。 • **Space** (-), prints one space, equivalent to bl emit. • \$+(55-5.5), concatenates two strings. ● "hello" " world" \$+ type cr -> print "hello world" (連接兩個字符串) • $\frac{1}{5}$ | Somputes the byte length (not the UTF-8 character length!) of a string. ● 對於純 ASCII 字符(即字符的 Unicode 代碼點在 O 到 127 之間), 每個字符佔用 1 個字節。 • +"string" (5-5), concatenates String 5 with a string literal. Equivalent to "string" \$+. • word (x - 5), parses a word delimited by the character with the Unicode codepoint x from the remainder of the current input line and pushes the result as a String. For instance, bl word abracadabra type will print the string "abracadabra". If x = 0, skips leading spaces, and then scans until the end of the current input line. If x = 32, skips leading spaces before parsing the next word. (使用 Unicode 代碼點 x 分隔的單詞, 並將結果作為字符串推入堆疊。) "abracadabra magic spell" bl word type 就會打印出 abracadabra。 "abracadabra magic spell" 115 word type 就會打印出 abracadabra magic s。 word 單獨使用的時候會把割出來的單詞推入 Stack。 • (.) (x-5), returns the String with the decimal representation of Integer x. ● . (括號不是操作符的一部份)將數字 x 以十進制的形式變成字文字打印出 console。
- (number) (5 0 or x 1 or x y 2), attempts to parse the String S as an integer or fractional literal as explained in 2.8.
 - number (括號不是操作符的一部份) 將數字 x 以十進制的形式變成字文字打印出 console。

For instance, ."*", "*" type, 42 emit, and char * emit are four different ways to output a single asterisk. (使用 "*". / "*" type / 42 emit / "*" emit 一樣可以 print * 到 console)

2.11 Boolean expressions, or flags

Fift does not have a separate value type for representing boolean values. Instead, any non-zero *Integer* can be used to represent truth (with -1 being the standard representation), while a zero *Integer* represents falsehood. Comparison primitives normally return -1 to indicate success and 0 otherwise.

Constants true and false can be used to push these special integers into the stack:

- true (--1), pushes -1 into the stack.
- false (-0), pushes 0 into the stack.

If boolean values are standard (either 0 or −1), they can be manipulated by means of bitwise logical operations and, or, xor, not (listed in 2.4). Otherwise, they must first be reduced to the standard form using 0↔:

• $\mathbb{O} \leftrightarrow (x - x = \mathbb{O})$, pushes -1 if Integer x is non-zero, \mathbb{O} otherwise.

2.12 Integer comparison operations

Several integer comparison operations can be used to obtain boolean values:

• $\langle (x y - ?), \text{ checks whether } x \langle y \text{ (i.e., pushes } -1 \text{ if } x \langle y, 0 \text{ otherwise)}.$

```
• >, =, <>, <=, >= (x y - ?), compare x and y and push -1 or 0 depending on the result of the comparison.
• 0 < (x - ?), checks whether x < 0 (i.e., pushes -1 if x is negative, 0 otherwise). Equivalent to 0 < ...
• \bigcirc, \bigcirc=, \bigcirc<>, \bigcirc<=, \bigcirc>= (x - ?), compare x against zero.
• cmp (x y - z), pushes 1 if x > y, -1 if x < y, and 0 if x = y.
• sgn (x - y), pushes 1 if x > 0, -1 if x < 0, and 0 if x = 0. Equivalent to 0 cmp.
Example:
23<.
prints "-l ok", because 2 is less than 3.
A more convoluted example:
{ "true " "false " rot 0= 1+ pick type 2drop } : ?. 2 3 < ?. 2 3 = ?. 2 3 > ?.
prints "true false false ok".
    → {"true " "false " rot 0= 1+ pick type 2drop} 定義了一個名為?的字典詞。
                     ● "true " 和 "false " 壓入堆疊。
                     ● pick 根據堆疊頂部的值選擇 "true " 或 "false ".
                    • type 打印所選的字符串。
                        2drop 刪除堆疊頂部的兩個元素。
            ♦ 23<?:</p>
             ♦ 23=?:
            ♦ 23>?:
```

2.13 String comparison operations

Strings can be lexicographically compared by means of the following words:

- \$= (55 ?), returns -1 if strings 5 and 5 are equal, 0 otherwise.
- $\frac{5cmp}{5}$ (55 x), returns 0 if strings 5 and 5 are equal,

→ 整段程式碼的輸出為: "true false false ok"。

-1 if S is lexicographically less than S, and 1 if S is lexicographically greater than S.

2.14 Named and unnamed variables

In addition to constants introduced in 2.7, Fift supports variables, which are a more efficient way to represent changeable values. For instance, the last two code fragments of 2.7 could have been written with the aid of variables instead of constants as follows:

```
variable x variable y(定義變量 x 和 y)
{ dup x! dup * y! }: setxy (定義了字典詞 setxy ─ 『 複製堆壘頂值存儲到 x ─ 複製堆壘頂平方值存儲到 y 』)
3 setxy x @ . y @ . x @ y @ + . (推 3 入堆疊一>執行 setxy(x 和 y 值設為 3 & 9)一>打印 x 和 y 的值一>打印 x 和 y 的和)
7 setxy x @ . y @ . x @ y @ + . (推 7 入堆疊一>執行 setxy(x 和 y 值設為 7 & 49)一>打印 x 和 y 的值一>打印 x 和 y 的和)
{."("x @..", "y @..")"}: showxy (定義字典詞 showxy ─ 『 打印 (一打印 x 的值一打印 , 一打印 y 的值一打印) 』)
3 setxy showxy
producing the same output as before: ()
```

```
3912 ok
74956 ok
```

(3,9)ok

The phrase variable x creates a new Box, i.e., a memory location that can be used to store exactly one value of any Fift-supported type, and defines x as a constant equal to this **Box**:

- variable (), scans a blank-delimited word name 5 from the remainder of the input, allocates an empty Box, and defines a new ordinary word 5 as a constant, which will push the new Box when invoked. Equivalent to hole constant.
- hole (-p), creates a new Box p that does not hold any value. Equivalent to null box.
- box (x p), creates a new Box containing specified value x. Equivalent to hole tuck!

The value currently stored in a Box may be fetched by means of word (a) (pronounced "fetch"), and modified by means of word (pronounced "store"):

- \bigcirc (p x), fetches the value currently stored in Box p.
- (x p), stores new value x into Box p.

Several auxiliary words exist that can modify the current value in a more sophisticated fashion:

- +! (x p), increases the integer value stored in Box p by Integer x. Equivalent to tuck @ + swap!.
- 1+!(p-), increases the integer value stored in Box p by one. Equivalent to 1 swap +!.
- 0! (p-), stores Integer 0 into Box p. Equivalent to 0 swap!.

In this way we can implement a simple counter:

17 box constant x(將數值 17 包裝入盒, 此盒命名為 x。)

```
variable counter (定義變量 counter 。)
{ counter 0! } : reset-counter (定義字典詞 reset-counter, 作用是把 0 設為 counter 的值。)
{ counter @ 1+ dup counter!}: next-counter
(定義字典詞 next-counter, 作用是把 counter 的值提取並透過 + 與 1 相加,
再用 dup 複製一份相加後的值, 用!將其設為 counter 的值。)
```

reset-counter next-counter.next-counter.next-counter.reset-counter.

produces

x=3 y=6 x*y=18x=3 y=7 x*y=21x=7 y=3 x*y=21

123 ok

After these definitions are in place, we can even forget the definition of counter by means of the phrase forget counter. Then the only way to access the value of this variable is by means of reset-counter and next-counter.

Variables are usually created by variables with no value, or rather with a Null value. If one wishes to create initialized variables, one can use the phrase box constant:

```
x 1+! x @. (透過操作符 +! 把 x 盒的值與 1 相加,將 x 盒推到 stack 頂,用@取得該值,用.打印。)
prints "18 ok". One can even define a special defining word for initialized variables, if they are needed often:
```

```
{ box constant }: init-variable (定義 stack 頂部的值為常量並包裝入盒內, 定義這套動作/行為/流程為 init-variable 的字典詞。)
17 init-variable x (數值 17 透過 init-variable 包裝入盒, 並把這盒命名為 x。)
"test" init-variable y (字串 test 透過 init-variable 包裝入盒, 並把這盒命名為 y。)
x 1+! x @ . y @ type
prints "18 test ok".
```

The variables have so far only one disadvantage compared to the constants: one has to access their current values by means of an auxiliary word @. Of course, one can mitigate this by defining a "getter" and a "setter" word for a variable, and use these words to write better-looking code:

```
variable x-box (定義了變量並命名為 x-box。)
{ x-box @ }: x (定義字典詞 x, 作用為取出變量 x-box 的值。)
{ x-box!}: x!(定義字典詞 x!, 作用為將一個值存入變量 x-box。)
\{xx*5x*+6+\}: f(x) (定義字典詞 f(x), 計算 x^2+5x+6。)
{ ."( " x . .", " f(x) . .") " } : .xy (定義字典詞 . xy, 按格式打印 x 和 f (x) 的值。 )
3 x! .xy 5 x! .xy
```

prints "(3, 30) (5, 56) ok", which are the points (x, f(x)) on the graph of $f(x) = x^2 + 5x + 6$ with x = 3 and x = 5.

Again, if we want to define "getters" for all our variables, we can first define a defining word as explained in 4.8, and use this word to define both a getter and a setter at the same time:

```
{ hole dup 1 ' @ does create 1 ' ! does create } : variable-set variable-set x x!
variable-set y y!
{ ."x=" x . ."y=" y . ."x*y=" x y * . cr } : show { y l+ y! } : up
{ x 1+ x! } : right
{ x y x! y! } : reflect
2 x! 5 y! show up show right show up show reflect show produces
x=2 y=5 x*y=10
x=2 y=6 x*y=12
```

2.15 Tuples and arrays

Fift also supports *Tuples*, i.e., immutable ordered collections of arbitrary values of stack value types (cf. 2.1). When a *Tuple t* consists of values x_1, \ldots, x_n (in that order), we write $t = (x_1, \dots, x_n)$. The number n is called the *length* of *Tuple t*; it is also denoted by |t|. Tuples of length two are also called *pairs*, tuples of length three are *triples*.

```
• tuple (x_1 \dots x_n n - t), creates new Tuple t := (x_1, \dots, x_n) from n \ge 0 topmost stack values.
```

```
• pair (x, y - t), creates new pair t = (x, y). Equivalent to 2 tuple.
```

- triple $(x \ y \ z t)$, creates new triple t = (x, y, z). Equivalent to 3 tuple.
- (-t), creates an empty Tuple t = (). Equivalent to 0 tuple.
- •, $(t \times -t)$, appends x to the end of Tuple t, and returns the resulting Tuple t.
- .dump (x), dumps the topmost stack entry in the same way as .s dumps all stack elements.

For instance, both

```
2,3,9,.dump
```

and

239 triple.dump

construct and print triple (2, 3, 9):

[239]ok

Notice that the components of a Tuple are not necessarily of the same type, and that a component of a Tuple can also be a Tuple:

```
123 triple 456 triple 789 triple triple constant Matrix Matrix.dump cr
1 "one" pair, 2 "two" pair, 3 "three" pair, .dump
produces
[[123][456][789]]
[[1 "one"][2 "two"][3 "three"]] ok
```

Once a Tuple has been constructed, we can extract any of its components, or completely unpack the Tuple into the stack:

- untuple $(t n x_1 ... x_n)$, returns all components of a *Tuple t* = $(x_1, ..., x_n)$, but only if its length is equal to n. Otherwise throws an exception.
- unpair (t x y), unpacks a pair t = (x, y). Equivalent to 2 untuple.
- untriple (t X Y Z), unpacks a triple t = (x, y, z). Equivalent to 3 untuple.
- explode $(t X_1 ... X_n n)$, unpacks a Tuple $t = (x_1, ..., x_n)$ of unknown length n, and returns that length.
- **count** (t-n), returns the length n = |t| of Tuple t.
- tuple? (t-?), checks whether t is a *Tuple*, and returns -1 or 0 accordingly.
- $(t \mid i x)$, returns the (i + 1)-st component t_{i+1} of Tuple t, where $0 \le i \le |t|$.
- first (t x), returns the first component of a *Tuple*. Equivalent to 0 [].
- **second** (t x), returns the second component of a *Tuple*. Equivalent to 1 [].
- third (t x), returns the third component of a *Tuple*. Equivalent to 2 [].

For instance, we can access individual elements and rows of a matrix:

```
123 triple 456 triple 789 triple triple constant Matrix Matrix.dump cr
Matrix 1 [] 2 [] . cr
Matrix third .dump cr
```

```
constant 就是一個定義操作,把[[123][456][789]]定義為常數 Matrix。
Matrix.dump cr 就是把 Matrix 打印-彈出-隔行。
```

取得矩陣的第二組件(第一組件是 Matrix 0), 再取當中的第三組件, 打印 - 隔行。

```
Matrix third .dump cr 就是把 Matrix 的第三組件打印-彈出-隔行。
```

[[123][456][789]]

[789]

Notice that Tuples are somewhat similar to arrays of other programming languages, but are immutable: we cannot change one individual component of a Tuple. If we still want to create something like an array, we need a Tuple of Boxes (cf. 2.14):

• allot (n-t), creates a Tuple that consists of n new empty Boxes. Equivalent to $\{$ hole , $\}$ rot times.

```
10 allot constant A | 3 box , 1 box , 4 box , 1 box , 5 box , 9 box , constant B { over @ over @ swap rot! swap!}: swap-values-of { B swap []}: B[] { B[] swap B[] swap-values-of}: swap-B { B[] @ .}:.B[]
```

01swap-B13swap-B02swap-B

0.B[]1.B[]2.B[]3.B[]

creates an uninitialized array A of length 10, an initialized array B of length 6, and then interchanges some elements of B and prints the first four elements of the resulting B:

4113 ok

- 10 allot 創建包含 10 個 Box 的元組, 定義為常數 A。
 |開始定義包含 3 box, 1 box, 4 box, 1 box, 5 box, 9 box的元組, 定義為常數 B。
- 第一個 over @ 取出堆疊頂部第二個元素當中的值, ... [box1] [box2] [value1]
 第二個 over @ 同樣取出堆疊頂部第二個元素當中的值, ... [box1] [box2] [value1] [value2]
 swap 交換堆疊頂部兩個元素的位置, ... [box1] [box2] [value2] [value1]
 rot 將堆疊頂部的第三個元素移到頂部, ... [box1] [value2] [value1] [box2]
 ! 存儲第二個元素值到堆疊頂部的盒子中, ... [box1] [value2] [value1 in box2] ->
 swap 和!再一次交換及存值,完成值的交換, ... [value2 in box1] [value1 in box2] ->
 將上述過程定義為 swap-values-of 函數。
- {B swap []} 這個很有趣,如果 **Stack** 頂部是 **1**,就變成 1 {B swap []}, swap 把 1 **&** B 互換了位置,變成 B 1[],即是查詢 B 第二個元素, 定義 B[] 就是用來快速啟動這功能。

2.16 Lists

Lisp-style lists can also be represented in Fift. First of all, two special words are introduced to manipulate values of type *Null*, used to represent the empty list (not to be confused with the empty *Tuple*):

- null $(-\perp)$, pushes the only value \perp of type Null, which is also used to represent an empty list.
- null? (x ?), checks whether x is a Null. Can also be used to check whether a list is empty.

After that, cons and uncons are defined as aliases for pair and unpair:

- cons (h t I), constructs a list from its head (first element) h and its tail (the list consisting of all remaining elements) t. Equivalent to pair.
- uncons (l-ht), decomposes a non-empty list into its head and its tail. Equivalent to unpair.
- car (l-h), returns the head of a list. Equivalent to first.
- $\operatorname{cdr}(I-t)$, returns the tail of a list. Equivalent to second.
- cadr (I h), returns the second element of a list. Equivalent to cdr car.
- list $(x_1 \dots x_n n l)$, constructs a list l of length n with elements x_1, \dots, x_n in that order. Equivalent to null 'cons rot times.
- . I(I), prints a Lisp-style list I.

For instance,

```
2 3 9 3 tuple .dump cr
2 3 9 3 list dup .dump space dup .l cr
"test" swap cons .l cr
```

produces

```
[ 2 3 9 ]
[ 2 [ 3 [ 9 (null) ] ] ] (2 3 9)
("test" 2 3 9)
```

Notice that the three-element list $(2\ 3\ 9)$ is distinct from the triple $(2,\ 3,\ 9)$.

2.17 Atoms

An Atom is a simple entity uniquely identified by its name. Atoms can be used to represent identifiers, labels, operation names, tags, and stack markers. Fift offers the following words to manipulate Atoms:

- (atom) ($5 \times a = 1 \text{ or } 0$), returns the only *Atom a* with the name given by *String 5*. If there is no such *Atom* yet, either creates it (if *Integer x* is non-zero) or returns a single zero to indicate failure (if x is zero).
- atom (5 a), returns the only Atom a with the name 5, creating such an atom if necessary. Equivalent to true (atom) drop.
- 'word (-a), introduces an Atom literal, equal to the only Atom with the name equal to word. Equivalent to "word" atom.

- anon (-a), creates a new unique anonymous Atom.
- atom? (u ?), checks whether u is an Atom.
- eq? $(u \ V ?)$, checks whether u and v are equal Integer s, Atoms, or Nulls. If they are not equal, or if they are of different types, or not of one of the types listed, returns zero.

For instance,

```
'+ 2 '* 3 4 3 list 3 list .l
```

creates and prints the list

```
(+2(*34))
```

which is the Lisp-style representation of arithmetical expression 2 + 3 · 4. An interpreter for such expressions might use eq? to check the operation sign (cf. 3.5 for an explanation of recursive functions in Fift):

```
variable 'eval (定義了變量 'eval, 將用來存儲 eval 的具體實現。)
{ 'eval @ execute }: eval (定義字典詞 eval, 其行為是取出變量 'eval 的值並執行。)
{ dup tuple? {(複製 stack 頂元素, 並檢查是否是 tuple 類型的值。)
      uncons uncons (如果是 tuple, 透過 uncons 3 次分拆出三個元素。)
      null? not abort"three-element list expected"(檢查是否含有 null 來確認是否三元素列表, 不是則報錯。)
      swap eval swap eval rot (* 先對操作數 1 eval, 再對操作數 2 eval, 最後進行相應的運算。)
      dup '+ eq? { drop + } { (檢查運算符是否 +, 如果是則執行加法。)
             dup '- eq? { drop - } { (檢查運算符是否 -, 如果是則執行減法。)
                   '* eq? not abort"unknown operation" * (檢查運算符是否 *, 如果是則執行乘法, 如果不是則報錯。)
            } cond( - / * 條件判斷結束)
      } cond(+條件判斷結束)
      } if (如果是 tuple 則執行上述代碼)
}'eval!(把以上的具體操作行為賦值給'eval)
      * 這裏相當有趣, 為協助理解, 先假設我們有一個三元素的 tuple (a b +):
         ○ swap:將 stack 的狀況變成 (a + b)
         ○ eval:將 stack 的狀況變成 (a + ) b值, 對 b 進行求值
         ○ swap:將 stack 的狀況變成 (+ a ) b值
         ○ eval:將 stack的狀況變成 (+) a值 b值, 對 a 進行求值
            rot:將 stack 的狀況變成 a值 b值 +, 操作符的值就是操作符
'+ 2 '* 3 4 3 list 3 list dup .l cr eval . cr
prints
(+2(*34))
14
```

If we load Lisp.fif to enable Lisp-style list syntax, we can enter

```
"Lisp.fif" include
('+ 2 ('* 3 4)) dup .l cr eval . cr
```

with the same result as before. The word (, defined in Lisp.fif, uses an anonymous *Atom* created by anon to mark the current stack position, and then) builds a list from several top stack entries, scanning the stack until the anonymous *Atom* marker is found:

```
variable ')
{ ") without (" abort } ')!
{ ') @ execute } : )
{ null { -rot 2dup eq? not } { swap rot cons } while 2drop } : list-until-marker
{ anon dup ') @ 2 { ')! list-until-marker } does ')! } : (
```

2.18 Command line arguments in script mode

The Fift interpreter can be invoked in script mode by passing -s as a command line option. In this mode, all further command line arguments are not scanned for Fift startup command line options. Rather, the next argument after -s is used as the filename of the Fift source file, and all further command line arguments are passed to the Fift program by means of special words \$n\$ and \$#:

- \$# (-x), pushes the total number of command-line arguments passed to the Fift program.
- 5n(-5), pushes the *n*-th command-line argument as a *String 5*. For instance, \$0 pushes the name of the script being executed, \$1 the first command line argument, and so on.
- \$()(x-5), pushes the x-th command-line argument similarly to \$n, but with Integer x taken from the stack.

Additionally, if the very first line of a Fift source file begins with the two characters "#!", this line is ignored. In this way simple Fift scripts can be written in a *ix system. For instance, if

```
#!/usr/bin/fift -s
{."usage: " $0 type ." <num1> <num2>" cr
."Computes the product of two integers." cr 1 halt }: usage { ' usage if }: ?usage
$# 2 <> ?usage
$1 (number) 1- ?usage
$2 (number) 1- ?usage
* . cr
```

is saved into a file cmdline.fif in the current directory, and its execution bit is set (e.g., by chmod 755 cmdline.fif), then it can be invoked from the shell or any other program, provided the Fift interpreter is installed as /usr/bin/fift, and its standard library Fift.fif is installed as

```
/usr/lib/fift/Fift.fif:
```

\$./cmdline.fif 12 -5 prints

-60

3 Blocks, loops, and conditionals

Similarly to the arithmetic operations, the execution flow in Fift is controlled by stack-based primitives. This leads to an inversion typical of reverse Polish notation and stack-based arithmetic: one first pushes a block representing a conditional branch or the body of a loop into the stack, and then invokes a conditional or iterated execution primitive. In this respect, Fift is more similar to PostScript than to Forth.

3.1 Defining and executing blocks

A block is normally defined using the special words "{" and "}". Roughly speaking, all words listed between { and } constitute the body of a new block, which is pushed into the stack as a value of type WordDef. A block may be stored as a definition of a new Fift word by means of the defining word ":" as explained in 2.6, or executed by means of the word execute:

● block 就是 WordDef 類型的 cell, 利用 {}: 包裹並定義所屬的執行動作。

17 { 2 * } execute .

prints "34 ok", being essentially equivalent to "17 2 * .". A slightly more convoluted example:

{ 2 * } 17 over execute swap execute .

applies "anonymous function" $x \to 2x$ twice to 17, and prints the result $2 \cdot (2 \cdot 17) = 68$. In this way a block is an execution token, which can be duplicated, stored into a constant, used to define a new word, or executed.

(以上的例子並沒有透過:定義 block, 而是直接執行, 所以也叫匿名函數。)

The word 'recovers the current definition of a word. Namely, the construct 'word-name pushes the execution token equivalent to the current definition of the wordword-name. For instance,

('就是把相應的操作符先推出入 Stack, First-In-Last-Out 的時候再操作。)

' dup execute

is equivalent to dup, and

' dup : duplicate

- dup execute & 'dup execute 是不同的執行方法。
 如果是 dup execute, 假如 Stack 的頂部是 3,
 3 dup execute 會變成 3 3 execute(因為把 3複製了一次),
 而 3 是無法 execute 的, 所以會報錯。
- 'dup execute 是先將 dup 操作符推入堆疊,出 Stack 時再執行,實際效果等同於執行 dup。

defines duplicate as a synonym for (the current definition of) dup. Alternatively, we can duplicate a block to define two new words with the same definition:

```
{ dup * } dup : square : **2
```

defines both square and **2 to be equivalent to dup *.

- { dup * } 會被看作一個整體程式碼 Block, 不立即執行, 但會被推入堆疊。
- dup 會複製 { dup * }, 使堆疊變成 { dup * } { dup * }。

3.2 Conditional execution of blocks

Conditional execution of blocks is achieved using the words if, ifnot, and cond:

- if (x e), executes e (which must be an execution token, i.e., a WordDef), but only if Integer x is non-zero.
- if (x e), executes execution token e, but only if Integer x is zero.
- cond (x el e2), if Integer x is non-zero, executes el, otherwise executes e2.

```
{ { ."true " } { ."false " } cond } : ?.
2 3 < ?. 2 3 = ?. 2 3 > ?.
```

still resulting in "true false false ok".

Notice that blocks can be arbitrarily nested, as already shown in the previous example. One can write, for example,

-17 chksign (用例)

to obtain "negative ok", because −17 is negative.

3.3 Simple loops

The simplest loops are implemented by times:

• times (e n -), executes e exactly n times, if $n \ge 0$. If n is negative, throw an exception.

```
For instance,
```

```
1 { 10 * } 70 times .
```

computes and prints 10^{70} .

We can use this kind of loop to implement a simple factorial function:

```
{ 0 1 rot { swap 1+ tuck * } swap times nip } : fact
5 fact . prints "120 ok", because 5! = 1 · 2 · 3 · 4 · 5 = 120.
```

This loop can be modified to compute Fibonacci numbers instead:

```
{ O l rot { tuck + } swap times nip } : fibo
```

6 fibo . computes the sixth Fibonacci number $F_6 = 13$.

3.4 Loops with an exit condition

More sophisticated loops can be created with the aid of until and while:

- until (e), executes e, then removes the top-of-stack integer and checks whether it is zero. If it is, then begins a new iteration of the loop by executing e. Otherwise exits the loop.
- While (e e), executes e, then removes and checks the top-of-stack integer. If it is zero, exits the loop. Otherwise executes e, then begins a new loop iteration by executing e and checking the exit condition afterwards.

For instance, we can compute the first two Fibonacci numbers greater than 1000:

```
{ 1 0 rot { -rot over + swap rot 2dup >= } until drop } : fib-gtr
```

```
For 1000 fib-gtr.:(以下展示 Stack 的變化)
1000 1 0 (底部 ← Stack → 頂部)
rot: 1 0 1000 (第2.5章有提及 rot 就是把第三位 stack 的數值調動到 stack 頂)
    ◆ -rot: 1000 1 0 (第2.5章有提及 -rot 就是把 stack 頂的數值調動到 stack 的第三位)
    ◆ over: 1000 1 0 1(over 就是把第二位的數值複製到頂部)
    +:1000 1 1(+就是把頂部兩位數值相加)
       swap: 1000 1 1(swap 把頂部兩位數值位置互換)
       rot: 1 1 1000 (rot 就是把 1000 再調動到 stack 頂。)
    ◆ 2dup: 1 1 1000 1 1000(2dup把頂部兩位數值複製一份到頂部。)
    >=: 1 1000 1 0(>= 對比頂部兩位數值,如果第二位大於頂位返回-1,否則返回0。)
    🔷 until: 1 1 1000(until 將會檢測頂部數值,是 0 則繼續 loop, 否則停止 loop, 並在檢查後將移除驗證的數值。)
             -rot:1000 1 1
          • over: 1000 1 1 1
             +:1000 1 2
              swap: 1000 2 1
          • rot: 2 1 1000
             >=:2 1 1000 0
           • until: 2 1 1000
                 o -rot:1000 2 1
                 o over: 1000 2 1 2
                 o +: 1000 2 3
                 o swap: 1000 3 2
                     rot:3 2 1000
                    2dup: 3 2 1000 2 1000
                    >=:3 2 1000 0
                 o until:3 2 1000
                        ◆ -rot:1000 3 2
                        ♦ over: 1000 3 2 3
                        +:1000 3 5
                        ♦ swap: 1000 5 3
                        •
                           rot: 5 3 1000
                        ♦ 2dup: 5 3 1000 3 1000
                        → >=:5 3 1000 0
                         ◆ until:5 3 1000
                               • -rot: 1000 5 3
                               • until:8 5 1000
                                     o -rot:1000 8 5
                                         until:13 8 1000
                                             ◆ -rot:1000 13 8
                                             • ...
```

```
    ◆ until: 21 13 1000
    → rot: 1000 1597 987
    • until: 2584 1597 1000
    ◆ drop: 2584 1597 (drop 把頂部的 1000 丟掉)
    ◆ 最後.打印結果及 ok: 1597 2584 ok (因為stack頂的是1597, 所以會先打印。)
```

```
1000 fib-gtr .
prints "1597 2584 ok".
```

We can use this word to compute the first 70 decimal digits of the golden ratio $\phi=(1+\sqrt{5})/2\approx 1.61803$: 1 { 10 * } 70 times dup fib-gtr */ . prints "161803 . . . 2604 ok".

3.5 Recursion

Notice that, whenever a word is mentioned inside a { ...} block, the current (compile-time) definition is included in the *WordList* being created. In this way we can refer to the previous definition of a word while defining a new version of it:

```
{+.}: print-sum(定義字典詞 print-sum, 其行為是對堆棧頂的兩個數字進行加法並打印結果。)
{."number ".}:.(重新定義字典詞,, 其行為是打印字符串 "number ", 然後打印堆棧頂的數字。)
{1+.}: print-next(定義字典詞 print-next, 其行為是將 stack 頂的數字加一, 然後打印結果。)
2.3.23 print-sum 7 print-next
```

produces "number 2 number 3 5 number 8 ok". Notice that print-sum continues to use the original definition of ".", but print-next already uses the modified ".".

This feature may be convenient on some occasions, but it prevents us from introducing recursive definitions in the most straightforward fashion. For instance, the classical recursive definition of the factorial

```
{?dup { dup l- fact * } { 1 } cond } : fact (這將無法編譯, 因為 fact 在內部使用的時候還沒有定義。)
```

will fail to compile, because fact happens to be an undefined word when the definition is compiled.

A simple way around this obstacle is to use the word @' (cf. 4.6) that looks up the current definition of the next word during the execution time and then executes it, similarly to what we already did in 2.7: (@' 可於執行期間查找字典詞的當前定義來執行)

```
{ ?dup { dup 1- @' fact * } { 1 } cond } : fact 5 fact .
```

以下是詳細步驟:

- 初始堆疊:5
- 執行 fact 函數

```
5 非零, ?dup 操作把 5 複製, 使堆疊變成: 5 5 (在此處請理解右邊是 stack 的頂部。)
5 非零, 執行 { dup 1- @' fact * }(cond 驗證後將會把驗證後的數值移除。)
(第 3.2 章有提及 cond 的運用, 如果 stack 上層值不是 0 則執行第一狀況, 是則執行第二狀況。)
執行 dup: 堆疊變成 5 5
執行 1-: 堆疊變成 5 4
第 1 次執行 @'fact:(第 4.6 章有提及的遞歸調用, 這樣就是重新引用字典詞 fact 的邏輯。)
   ○ 4 非零, ?dup 把 4 複製, 使堆疊變成:5 4 4
       4 非零, 執行 { dup 1- @' fact * }
       執行 dup: 堆疊變成 5 4 4
       執行 1-: 堆疊變成 5 4 3
       第 2 次執行 @'fact:
             3 非零, ?dup 把 3 複製, 使堆疊變成:5 4 3 3
             3 非零, 執行 { dup 1- @' fact * }
             執行 dup:堆疊變成 5 4 3 3
             執行 1-: 堆疊變成 5 4 3 2
             第3次執行@'fact:
                 ■ 2 非零, ?dup 把 2 複製, 使堆疊變成:5 4 3 2 2
                    2 非零, 執行 { dup 1- @' fact * }
                    執行 dup: 堆疊變成 5 4 3 2 2
                    執行 1-: 堆疊變成 5 4 3 2 1
                    第 4 次執行 @'fact:
                       ■ 1 非零, ?dup 把 1 複製, 使堆疊變成:5 4 3 2 1 1
                          1 非零, 執行 { dup 1- @' fact * }
                          執行 dup:堆疊變成 5 4 3 2 1 1
                          第5次執行@'fact:
                                0 是零, ?dup 不複製, 堆疊維持:5 4 3 2 1 0
                                 ②是零,驗證後的數值移除 ②,執行第二狀況 {1}
                                 堆疊變成 5 4 3 2 1
                                 然後開始執行每一層的乘法:
                       5 4 3 2 *
      最後 "." 打印出 "120 ok" 的結果。
```

produces "120 ok", as expected.

However, this solution is rather inefficient, because it uses a dictionary lookup each time fact is recursively executed. We can avoid this dictionary lookup by using variables (cf. 2.14 and 2.7):

```
variable 'fact (定義變量 'fact, 將用來存儲 fact 的具體實現)
{ 'fact @ execute }: fact (定義字典詞 fact, 其行為是取出變量 'fact的值並執行, 令重覆使用更有效率。)
{ ?dup { dup 1- fact * } { 1 } cond } 'fact!
(第 2.14 章記錄了!的運用, 這裡就是把邏輯 {?dup{dup1-fact*}{1}cond} 記錄到 'fact 變數當中。)
(將具體實現存儲到變量 fact 中, 上方例子已展示如何運用字典詞 fact 進行遞歸計算階乘的過程, 以及每一步操作在堆疊上的變化。)
```

This somewhat longer definition of the factorial avoids dictionary lookups at execution time by introducing a special variable 'fact to hold the final definition of the factorial. Then fact is defined to execute whatever WordDef is currently stored in fact, and once the body of the recursive definition of the factorial is constructed, it is stored into this variable by means of the phrase 'fact!, which replaces the more customary phrase: fact.

We could rewrite the above definition by using special "getter" and "setter" words for vector variable 'fact as we did for variables in 2.14:

```
variable 'fact (定義變量 ' fact)
{ 'fact @ execute }: fact (定義字典詞 fact, 其行為是取出變量 'fact的值並執行)
{ 'fact!}:: fact(當 fact 被重新定義為 { 'fact!}, 執行時變量 'fact 中的遞歸邏輯會被直接執行, 不需要每次查找字典中 fact 的定義。)
forget 'fact (忘記變量' fact, 使變量' fact 地址可重新使用。)
{ ?dup { dup 1- fact * } { 1 } cond } : fact
```

If we need to introduce a lot of recursive and mutually-recursive definitions, we might first introduce a custom defining word (cf. 4.8) for simultaneously defining both the

getter" and the "setter" words for anonymous vector variables, similarly to what we did in 2.14:

{ hole dup l { @ execute } does create l'! does create } : vector-set

vector-set fact :fact

5 fact.

```
hole:把一個用於寄存數值的空盒推入 stack,於2.14章有提及。stack:[]
dup:複製堆棧頂部的空盒,現在頂部有兩個相同的地址的空盒。stack:[][]
1 { @ execute } does:does把1個操作邏輯值({ @ execute })推到 stack頂的空盒內。stack:[][{ @ execute }]
create:創建了一個匿名字典詞,該盒會從 stack 中移除。stack: []
1 ′! does:把1個操作邏輯值(′)推到 stack 頂的空盒內。stack:[!]
create:創建了一個匿名字典詞,該盒會從 stack 中移除。stack:
fact:讀完了兩個匿名字典詞再 save 回 fact。
vector-set 就是讀取加儲存當前字典詞的值, 在 vector-fact:fact 當中就是 fact 的值。
```

根據第**4.6**章 does 的作用即是 **{ swap ({) over 2+ -roll swap (compile) (})) }**

 $(x_1, \dots, x_n, n \in -e)$, creates a new execution token e that would push n values x_1, \dots, x_n into the stack and then execute e. 第 4.5 章有解說 create 的用途,在讀取時 compile { @ execute } / '! 就是新字典詞的屬性,這裡創建的是匿名字典詞。

```
{ ?dup { dup 1- fact * } { 1 } cond } :fact
```

5 fact.

The first three lines of this fragment define fact and :fact essentially in the same way they had been defined in the first four lines of the previous fragment. If we wish to make fact unchangeable in the future, we can add a forget :fact line once the definition of the factorial is complete:

⁶Variables that hold a WordDef to be executed later are called vector variables. The process of replacing fact with 'fact @ execute, where 'fact is a vector variable, is called vectorization.

```
{ hole dup l { @ execute } does create l '! does create } : vector-set
vector-set fact :fact
{ ?dup { dup 1- fact * } { 1 } cond } :fact
forget :fact
5 fact.
```

Alternatively, we can modify the definition of vector-set in such a way that :fact would forget itself once it is invoked:

```
{ hole dup I { @ execute } does create
bl word tuck 2 { (forget)! } does swap 0 (create) } : vector-set-once
vector-set-once fact :fact
{ ?dup { dup 1- fact * } { 1 } cond } :fact
5 fact.
```

However, some vector variables must be modified more than once, for instance, to modify the behavior of the comparison word less in a merge sort algorithm:

```
{ hole dup l { @ execute } does create l '! does create } : vector-set
vector-set sort :sort
vector-set merge :merge
vector-set less :less
{ null null rot
{ dup null? not }
{ uncons swap rot cons -rot } while drop
} : split
{ dup null? { drop } {
over null? { nip } {
over car over car less ' swap if
} cond
} cond
}:merge
{ dup null? {
dup cdr null? {
split sort swap sort merge
} ifnot
} ifnot
} :sort
forget:merge
forget:sort
// set 'less' to compare numbers, sort a list of numbers ' < :less
3141592659 list
dup .l cr sort .l cr
```

// set 'less' to compare strings, sort a list of strings { \$cmp 0< } :less

"once" "upon" "a" "time" "there" "lived" "a" "kitten" 8 list dup .l cr sort .l cr

producing the following output:

```
(314159265)
(112345569)
```

3.6 Throwing exceptions

Two built-in words are used to throw exceptions:

- abort (5-), throws an exception with an error message taken from String 5.
- abort "message" (x), throws an exception with the error message message if x is a non-zero integer.

The exception thrown by these words is represented by the C++ exception fift::IntError with its value equal to the specified string. It is normally handled within the Fift interpreter itself by aborting all execution up to the top level and printing a message with the name of the source file being interpreted, the line number, the currently interpreted word, and the specified error message. For instance:

{ dup 0= abort"Division by zero" / } : safe/ 5 0 safe/ .

```
    ● 定義 safe/:

            dup:複製堆棧頂的值。
            0=:驗證堆棧頂的值是否為O。
            abort"Division by zero":如果堆棧頂的值為O,則抛出一個帶有"Division by zero"信息的例外並中止執行。
            /:如果沒有例外,則進行除法操作。

    執行 5 0 safe/:

            5 和 0 被推入堆棧。
            執行 safe/時,堆棧頂的值 0 被複製並檢查是否為O。
            因為 0 等於O,所以執行 abort,並打印錯誤信息 "safe/: Division by zero"。
```

prints "safe/: Division by zero", without the usual "ok". The stack is cleared in the process.

Incidentally, when the Fift interpreter encounters an unknown word that cannot be parsed as an integer literal, an exception with the message "-?" is thrown, with the effect indicated above, including the stack being cleared.

4 Dictionary, interpreter, and compiler

In this chapter we present several specific Fift words for dictionary manipulation and compiler control. The "compiler" is the part of the Fift interpreter that builds lists of word references (represented by WordList stack values) from word names; it is activated by the primitive "{" employed for defining blocks as explained in 2.6 and 3.1.

Most of the information included in this chapter is rather sophisticated and may be skipped during a first reading. However, the techniques described here are heavily employed by the Fift assembler, used to compile TVM code. Therefore, this section is indispensable if one wishes to understand the current implementation of the Fift assembler.

4.1 The state of the Fift interpreter

The state of the Fift interpreter is controlled by an internal integer variable called state, currently unavailable from Fift itself. When state is zero, all words parsed from the input (i.e., the Fift source file or the standard input in the interactive mode) are looked up in the dictionary and immediately executed afterwards. When state is positive, the words found in the dictionary are not executed. Instead, they (or rather the references to their current definitions) are compiled, i.e., added to the end of the WordList being constructed.

Typically, state equals the number of the currently open blocks. For instance, after interpreting "{ 0= { ."zero"" the state variable will be equal to two, because there are two nested blocks. The WordList being constructed is kept at the top of the stack.

The primitive "{" simply pushes a new empty WordList into the stack, and increases state by one. The primitive "}" throws an exception if state is already zero; otherwise it decreases state by one, and leaves the resulting WordList in the stack, representing the block just constructed. After that, if the resulting value of state is non-zero, the new block is compiled as a literal (unnamed constant) into the encompassing block.

```
● 這兩段說明了 { } 操作符如何對 Fift interpreter 當中稱為 state 的內部管理系數產生作用。
○ 簡單來說, 就是確保 { } 是一對的, 否則將會出現錯誤。
○ 詳細點說, 就是當 { 出現的時候 state + 1,
            } 出現的時候 state - 1, state 等於 ② 的時候 WordList(就是 { } 內裹的操作)才會被執行。
○ 如果只出現 }, state 就會是負數, 編譯系統就會報錯。
○ 如果只出現 {, state 會大於零, 系統會連同 { 當作是一個新的常數寫入, 或者出現神奇的事情。
```

4.2 Active and ordinary words

All dictionary words have a special flag indicating whether they are active words or ordinary words. By default, all words are ordinary. In particular, all words defined with the aid of ":" and constant are ordinary.

```
所有字典詞都帶有特殊標誌, 指明它們是活躍字典詞 / 普通字典詞。使用: / constant 定義的都是普通字典詞(ordinary)。
```

When the Fift interpreter finds a word definition in the dictionary, it checks whether it is an ordinary word. If it is, then the current word definition is either executed (if state is zero) or "compiled" (if state is greater than zero) as explained in 4.1.

▶ Fift 編譯器會檢查字典詞的 state, 如果 state 為零則執行, 大於零則進行編譯。

On the other hand, if the word is active, then it is always executed, even if the state is positive. An active word is expected to leave some values $x_1 \dots x_n$ n e in the stack, where $n \ge 0$ is an integer, $x_1 \dots x_n$ are n values of arbitrary types, and e is an execution token (a value of type WordDef). After that, the interpreter performs different actions depending on state: if state is zero, then n is discarded and e is executed, as if a nip execute phrase were found. If state is non-zero, then this collection is "compiled" in the current WordList (located immediately below x_1 in the stack) in the same way as if the (compile) primitive were invoked. This compilation amounts to adding some code to the end of the current WordList that would push x_1, \dots, x_n into the stack when invoked, and then adding a reference to e (representing a delayed execution of e). If e is equal to the special value 'nop, representing an execution token that does nothing when executed, then this last step is omitted. (這說明有點抽象,下方有實例會解釋得更

4.3 Compiling literals

When the Fift interpreter encounters a word that is absent from the dictionary, it invokes the primitive (number) to attempt to parse it as an integer or fractional literal. If this attempt succeeds, then the special value 'nop is pushed, and the interpretation proceeds in the same way as if an active word were encountered. In other words, if state is zero, then the literal is simply left in the stack; otherwise, (compile) is invoked to modify the current WordList so that it would push the literal when executed.

⁷The word } also transforms this WordList into a WordDef, which has a different type tag and therefore is a different Fift value, even if the same underlying C++ object is used by the C++ implementation.

4.4 Defining new active words

New active words are defined similarly to new ordinary words, but using "::" instead of ":". For instance,

```
{ bl word 1 ' type } :: say
```

12 say hello +.

defines the active word say, which scans the next blank-separated word after itself and compiles it as a literal along with a reference to the current definition of type into the current WordList (if state is non-zero, i.e., if the Fift interpreter is compiling a block). When invoked, this addition to the block will push the stored string into the stack and execute type, thus printing the next word after say. On the other hand, if the state is zero, then these two actions are performed by the Fift interpreter immediately. In this way,

```
will print "hello3 ok", while
{ 2 say hello + . } : test
1 test 4 test
will print "hello3 hello6 ok".
      當 Fift 編譯 1 2 say hello + .:
          ○ 編譯器會立即執行活躍字典詞 say, { bl word 1 ' type } :: say
              word 1 掃描下一個以空格分隔的字典詞 hello,
               會執行 type 將 hello 彈出並先行列印。
             然後執行剩餘的操作 1 2 +, 所以結果是 hello3。
      當在 Fift 定義 { 2 say hello + . } : test, 再執行 l test 4 test
          ○ 1 test 4 test 就是 1 { 2 say hello + . } 4 { 2 say hello + . },
                 ■ Fift 編譯機會由左至右讀起 ... 1 { 2 讀到 say 的時候就"活躍"了,
                     所以立即執行 say 彈出並先行列印 hello , 然後 + 就把 1 和 2 加成 3,
                     因為現在只讀了一個 {, 所以 state 為正, 編譯器會立即執行 +. 直至 },
                     hello3 就出來了。
                    現在 state 為 0, 編譯機繼續由左至右讀 ... 4 { 2 讀到 say "活躍",
                     立即執行 say 彈出並列印 hello, 然後+就把4和2加成6,
                     只讀了一個 {, 所以 state 現在為 + 1, 編譯器會立即執行 + . 直至 },
```

hello6 也出來了。

Of course, a block may be used to represent the required action instead of 'type. For instance, if we want a version of say that prints a space after the stored word, we can write

```
{ bl word 1 { type space } } :: say
{ 2 say hello + . } : test
1 test 4 test

to obtain "hello 3 hello 6 ok".

Incidentally, the words " (introducing a string literal) and ." (printing a string literal) can be defined as follows:
{ char " word 1 'nop } ::_ "
{ char " word 1 ' type } ::_ ."
```

The new defining word "::_" defines an active prefix word, i.e., an active word that does not require a space afterwards.

4.5 Defining words and dictionary manipulation

Defining words are words that define new words in the Fift dictionary. For instance, ":", "::_", and constant are defining words. All of these defining words might have been defined using the primitive (create); in fact, the user can introduce custom defining words if so desired. Let us list some defining words and dictionary manipulation words:

- **create** word-name (e-), defines a new ordinary word with the name equal to the next word scanned from the input, using word e as its definition. If the word already exists, it is tacitly redefined. (e id id
- (create) (e $5 \times -$), creates a new word with the name equal to 5×5 and definition equal to 5×5 and 5×5
- •: word-name (e), defines a new ordinary word word-name in the dictionary using wordDef e as its definition. If the specified word is already present in the dictionary, it is tacitly redefined.
- forget word-name (-), forgets (removes from the dictionary) the definition of the specified word.
- (forget) (5-), forgets the word with the name specified in String 5. If the word is not found, throws an exception.

- •:_ word-name (e), defines a new ordinary prefix word word-name, meaning that a blank or an end-of-line character is not required by the Fift input parser after the word name. In all other respects it is similar to ":".
- :: word-name (e), defines a new active word word-name in the dictionary using WordDef e as its definition. If the specified word is already present in the dictionary, it is tacitly redefined.
- ::_ word-name (e), defines a new active prefix word word-name, meaning that a blank or an end-of-line character is not required by the Fift input parser after the word name. In all other respects it is similar to "::".
- constant word-name (x-), defines a new ordinary word word-name that would push the given value x when invoked.
- **2constant** word-name (x y), defines a new ordinary word named word-name that would push the given values x and y (in that order) when invoked.
- =: word-name (x), defines a new ordinary word word-name that would push the given value x when invoked, similarly to constant, but works inside blocks and colon definitions.
- 2=: word-name(x y), defines a new ordinary word word-name that would push the given values x and y (in that order) when invoked, similarly to 2constant, but works inside blocks and colon definitions.

Notice that most of the above words might have been defined in terms of (create):

```
{ bl word 1 2 ' (create) } "::" 1 (create) 
{ bl word 0 2 ' (create) } :: : 
{ bl word 2 2 ' (create) } :: :_ 
{ bl word 3 2 ' (create) } :: ::_ 
{ bl word 0 (create) } : create 
{ bl word (forget) } : forget
```

4.6 Dictionary lookup

The following words can be used to look up words in the dictionary:

- ' word-name (e), pushes the definition of the word word-name, recovered at the compile time. If the indicated word is not found, throws an exception. Notice that ' word-name execute is always equivalent to word-name for ordinary words, but not for active words.
- nop (), does nothing.
- 'nop (-e), pushes the default definition of nop—an execution token that does nothing when executed.
- find (5 e 1 or e 1 or 0), looks up String S in the dictionary and returns its definition as a WordDef e if found, followed by -1 for ordinary words or 1 for active words. Otherwise pushes 0.
- (') word-name (-e), similar to ', but returns the definition of the specified word at execution time, performing a dictionary lookup each time it is invoked. May be used to recover current values of constants inside word definitions and other blocks by using the phrase (') word-name execute.
- (a) word-name (e), similar to ('), but recovers the definition of the specified word at execution time, performing a dictionary lookup each time it is invoked, and then executes this definition. May be used to recover current values of constants inside word definitions and other blocks by using the phrase (a) word-name, equivalent to (') word-name execute, cf. 2.7.
- [compile] word-name (), compiles word-name as if it were an or dinary word, even if it is active. Essentially equivalent to ' word-name execute.
- words (), prints the names of all words currently defined in the dictionary.

4.7 Creating and manipulating word lists

In the Fift stack, lists of references to word definitions and literals, to be used as blocks or word definitions, are represented by the values of the type WordList. Some words for manipulating WordLists include:

• $\{(-1)$, an active word that increases internal variable state by one and pushes a new empty WordList into the stack.

- $\{(I-e), an active word that transforms a WordList I into a Word Def (an execution token) e, thus making all further modifications of I impossible, and decreases internal variable state by one and pushes the integer 1, followed by a 'nop. The net effect is to transform the constructed WordList into an execution token and push this execution token into the stack, either immediately or during the execution of an outer block.$
- $\{\{\} (-1), \text{ pushes an empty WordList into the stack.} \}$
- () (I e), transforms a WordList into an execution token, making all further modifications impossible.
- (compile) ($I \times_1 \dots \times_n n \in -I$), extends WordList I so that it would push $0 \le n \le 255$ values x_1, \dots, x_n into the stack and execute the execution token e when invoked, where $0 \le n \le 255$ is an Integer. If e is equal to the special value 'nop, the last step is omitted.
- does $(x_1 ... x_n n e e)$, creates a new execution token e that would push n values $x_1, ..., x_n$ into the stack and then execute e. It is roughly equivalent to a combination of $(\{\})$, (compile), and $(\{\})$.

4.8 Custom defining words

The word does is actually defined in terms of simpler words:

{ swap ({) over 2+ -roll swap (compile) (}) } : does

- swap:交換堆疊頂部的兩個元素。
- 〔{]:進入編譯模式。
- over:複製堆疊中的第二個元素,並將其推入堆疊頂部。
- 2+: 將堆疊頂部的元素加 2。
- -roll:重新排列堆疊中的元素,將第 n 個元素移到堆疊頂部。
- Swap:再次交換堆疊頂部的兩個元素。
- (compile):將編譯模式中的代碼進行編譯,並將其作為一個編譯後的詞加入到詞典中。
- (}):結束編譯模式。

It is especially useful for defining custom defining words. For instance, constant and 2constant may be defined with the aid of does and create:

```
{ 1 'nop does create } : constant { 2 'nop does create } : 2constant
```

Of course, non-trivial actions may be performed by the words defined by means of such custom defining words. For instance,

```
{ 1 { type space } does create } : says "hello" says hello "unknown error" says error { hello error } : test test
```

will print "hello unknown error ok", because hello is defined by means of a custom defining word says to print "hello" whenever invoked, and similarly error prints "unknown error" when invoked. The above definitions are essentially equivalent to

```
{ ."hello" } : hello
{ ."unknown error" } : error
```

However, custom defining words may perform more sophisticated actions when invoked, and preprocess their arguments at compile time. For instance, the message can be computed in a non-trivial fashion:

```
"Hello, " "world!" $+ says hw
```

defines word hw, which prints "Hello, world!" when invoked. The string with this message is computed once at compile time (when says is invoked), not at execution time (when hw is invoked).

5 Cell manipulation

We have discussed the basic Fift primitives not related to TVM or the TON Blockchain so far. Now we will turn to TON-specific words, used to manipulate Cells.

5.1 Slice literals

Recall that a (TVM) *Cell* consists of at most 1023 data bits and at most four references to other *Cells*, a *Slice* is a read-only view of a portion of a *Cell*, and a *Builder* is used to create new *Cells*. Fift has special provisions for defining *Slice* literals (i.e., unnamed constants), which can also be transformed into *Cells* if necessary.

Slice literals are introduced by means of active prefix words x{ and b{:

- b{binary-data} (s), creates a Slice s that contains no references and up to 1023 data bits specified in binary-data, which must be a string consisting only of the characters '0' and '1'.
- $x\{hex-data\}\ (-5)$, creates a *Slice s* that contains no references and up to 1023 data bits specified in *hex-data*. More precisely, each hex digit from *hex-data* is transformed into four binary digits in the usual fashion. After that, if the last character of *hex-data* is an underscore _, then all trailing binary zeroes and the binary one <u>immediately preceding them are removed from the resulting binary string (cf. [4, 1.0] for more details).</u>

In this way, $b\{00011101\}$ and $x\{1d\}$ both push the same Slice consisting of eight data bits and no references. Similarly, $b\{111010\}$ and $x\{EA_{-}\}$ push the same Slice

consisting of six data bits. An empty Slice can be represented as b $\{\}$ or x $\{\}$.

If one wishes to define constant Slices with some Cell references, the following words might be used:

- [(SS-S), given two Slices s and s, creates a new Slice s, which is obtained from s by appending a new reference to a Cell containing s.
- + (S S S), concatenates two Slices s and s. This means that the data bits of the new Slice s are obtained by concatenating the data bits of s and s, and the list of Cell references of s is constructed similarly by concatenating the corresponding lists for s and s.

5.2 Builder primitives

The following words can be used to manipulate Builders, which can later be used to construct new Cells:

- $\langle b (-b) \rangle$, creates a new empty Builder.
- b> (b-c), transforms a Builder b into a new Cell c containing the same data as b.
- i, $(b \times y b)$, appends the big-endian binary representation of a signed y-bit integer x to Builder b, where $0 \le y \le 257$. If there is not enough room in b (i.e., if b already contains more than 1023 y data bits), or if Integer x does not fit into y bits, an exception is thrown.
- \mathbf{u} , $(b \times y b)$, appends the big-endian binary representation of an unsigned y-bit integer x to Builder b, where $0 \le y \le 256$. If the operation is impossible, an exception is thrown.
- ref, (b c b), appends to Builder b a reference to Cell c. If b already contains four references, an exception is thrown.
- 5, (b 5 b), appends data bits and references taken from Slice s to Builder b.
- sr, (bs-b), constructs a new Cell containing all data and references from Slice s, and appends a reference to this cell to Builder b. Equivalent to s swap s, s ref.
- $\frac{1}{5}$, (b5-b), appends String S to Builder b. The string is interpreted as a binary string of length 8n, where n is the number of bytes in the UTF-8 representation of S.
- B, (bB-b), appends Bytes B to Builder b.
- b+(bb-b), concatenates two Builders b and b.
- bbits (b x), returns the number of data bits already stored in Builder b. The result x is an Integer in the range 0...1023.
- brefs (b-x), returns the number of references already stored in Builder b. The result x is an Integer in the range 0...4.
- bbitrefs (b x y), returns both the number of data bits x and the number of references y already stored in Builder b.
- brembits (b x), returns the maximum number of additional data bits that can be stored in Builder b. Equivalent to bbits 1023 swap -.
- bremrefs (b-x), returns the maximum number of additional cell references that can be stored in Builder b.
- brembitrefs (b x y), returns both the maximum number of additional data bits $0 \le x \le 1023$ and the maximum number of additional cell references $0 \le y \le 4$ that can be stored in *Builder b*.

The resulting Builder may be inspected by means of the non-destructive stack dump primitive .s, or by the phrase b> <s csr.. For instance:

```
\{\ \mbox{ $\langle$ b \times \{4A\}$ s, rot 16 u, swap 32 i, .s b}\ \} : mkTest 17239 -1000000001 mkTest \ \mbox{ $\langle$ s csr.}
```

outputs

```
BC{000e4a4357c46535ff}
ok
x{4A4357C46535FF}
ok
```

One can observe that .s dumps the internal representation of a *Builder*, with two tag bytes at the beginning (usually equal to the number of cell references already stored in the *Builder*, and to twice the number of complete bytes stored in the *Builder*, increased by one if an incomplete byte is present). On the other hand, csr. dumps a *Slice* (constructed from a *Cell* by <s, cf. 5.3) in a form similar to that used by x{ to define *Slice* literals (cf. 5.1). Incidentally, the word mkTest shown above (without the .s in its definition) corresponds to the TL-B constructor

test#4a first:uint16 second:int32 = Test;

and may be used to serialize values of this TL-B type.

5.3 Slice primitives

The following words can be used to manipulate values of the type *Slice*, which represents a read-only view of a portion of a *Cell*. In this way data previously stored into a *Cell* may be describilized, by first transforming a *Cell* into a *Slice*, and then extracting the required data from this *Slice* step-by-step.

• \leq (c-5), transforms a Cell c into a Slice s containing the same data. It usually marks the start of the describilization of a cell.

- 5> (5), throws an exception if *Slice s* is non-empty. It usually marks the end of the deserialization of a cell, checking whether there are any unprocessed data bits or references left.
 - i ($(5 \times y)$), fetches a signed big-endian x-bit integer from the first x bits of Slice s. If s contains less than x data bits, an exception is thrown.
 - i $\boxed{0}$ + (5 X Y S), fetches a signed big-endian x-bit integer from the first x bits of Slice s similarly to i $\boxed{0}$, but returns the remainder of s as well.
- i@? ($s \times y = 1 \text{ or } 0$), fetches a signed integer from a *Slice* similarly to i@, but pushes integer = 1 afterwards on success. If there are less than x bits left in s, pushes integer 0 to indicate failure.
- i@?+ (SX YS = 1 or SO), fetches a signed integer from Slice S and computes the remainder of this Slice S imilarly to i@+, but pushes S and S indicate success. On failure, pushes the unchanged Slice S and S indicate failure.
- ua, ua+, ua?, ua?+, counterparts of ia, ia+, ia?, ia?+ for deserializing unsigned integers.
- $B \bigcirc (5 \times B)$, fetches first x bytes (i.e., 8x bits) from Slice s, and returns them as a Bytes value B. If there are not enough data bits in s, throws an exception.
- B@+(sx-Bs), similar to B@, but returns the remainder of Slice s as well.
- $B@? (s \times B 1 \text{ or } 0)$, similar to B@, but uses a flag to indicate failure instead of throwing an exception.
- B@?+(sx-Bs-1 or s0), similar to B@+, but uses a flag to indicate failure instead of throwing an exception.
- \$\,\text{Q}, \$\,\text{Q}^2, \$\,\text{Q}^2, \$\,\text{counterparts of B\,\text{Q}}, B\,\text{Q}^2, B\,\text{Q}^2, returning the result as a (UTF-8) \(\text{String} \) instead of a \(\text{Bytes value}. \) These primitives do not check whether the byte sequence read is a valid UTF-8 string.
- ref[0](s-c), fetches the first reference from Slice s and returns the Cell c referred to. If there are no references left, throws an exception.
- ref(5 5c), similar to ref(0), but returns the remainder of s as well.
- ref[0]? (s c 1 or 0), similar to ref[0], but uses a flag to indicate failure instead of throwing an exception.
- ref0?+ (s sc 1 or s 0), similar to ref0+, but uses a flag to indicate failure instead of throwing an exception.
- empty? (s-?), checks whether a Slice is empty (i.e., has no data bits and no references left), and returns -1 or 0 accordingly.
- remaining (5 xy), returns both the number of data bits x and the number of cell references y remaining in Slice s.
- sbits (s x), returns the number of data bits x remaining in Slice s.
- srefs (s x), returns the number of cell references x remaining in Slice s.
- sbitrefs (s xy), returns both the number of data bits x and the number of cell references y remaining in Slice s. Equivalent to remaining.
- $$>_{5}$ (5 5), transforms String S into a Slice. Equivalent to 4 swap 4, 4
- $5 \times c$ (5 c), creates a *Cell c* directly from a *Slice s*. Equivalent to $4 \times c$ swap s, $6 \times c$
- CST. (5), recursively prints a *Slice s*. On the first line, the data bits of s are displayed in hexadecimal form embedded into an x{...} construct similar to the one used for *Slice* literals (cf. 5.1). On the next lines, the cells referred to by s are printed with larger indentation.

For instance, values of the TL-B type Test discussed in 5.2 test#4a first:uint16 second:int32 = Test; may be deserialized as follows:

```
{ <s 8 u@+ swap 0x4a <> abort"constructor tag mismatch" 16 u@+ 32 i@+ s> } : unpackTest x{4A4357C46535FF} s>c unpackTest swap . .
```

prints "17239 -1000000001 ok" as expected.

Of course, if one needs to check constructor tags often, a helper word can be defined for this purpose:

```
{ dup remaining abort"references in constructor tag" tuck u@ -rot u@+ -rot <> abort"constructor tag mismatch" } : tag? { <s x{4a} tag? 16 u@+ 32 i@+ s> } : unpackTest x{4A4357C46535FF} s>c unpackTest swap . .
```

We can do even better with the aid of active prefix words (cf. 4.2 and 4.4):

```
{ dup remaining abort references in constructor tag "dup 256 > abort constructor tag too long" tuck u@ 2 { -rot u@+ -rot <> abort constructor tag mismatch } ; (tagchk) { [compile] x{ 2drop (tagchk) } ::_ ?x{ { [compile] b{ 2drop (tagchk) } ::_ ?b{ { <$ ?x{4a} 16 u@+ 32 i@+ $>$} : unpackTest x{4A4357C46535FF} s>c unpackTest swap . .
```

A shorter but less efficient solution would be to reuse the previously defined tag?:

```
{ [compile] x{ drop ' tag? } ::_ ?x{ { [compile] b{ drop ' tag? } ::_ ?b{ x{11EF55AA} ?x{11E} dup csr. ?b{110} csr.
```

first outputs " $x{F55AA}$ ", and then throws an exception with the message "constructor tag mismatch".

5.4 Cell hash operations

There are few words that operate on *Cells* directly. The most important of them computes the (sha256-based) representation hash of a given cell (cf. [4, 3.1]), which can be roughly described as the sha256 hash of the cell's data bits concatenated with recursively computed hashes of the cells referred to by this cell:

- hashB (c B), computes the sha256-based representation hash of *Cell c* (cf. [4, 3.1]), which unambiguously defines c and all its descendants (provided there are no collisions for sha256). The result is returned as a *Bytes* value consisting of exactly 32 bytes.
- hashu (c x), computes the sha256-based representation hash of c as above, but returns the result as a big-endian unsigned 256-bit Integer.
- shash (s B), computes the sha256-based representation hash of a Slice by first transforming it into a cell. Equivalent to s>c hashB.

5.5 Bag-of-cells operations

A bag of cells is a collection of one or more cells along with all their descen dants. It can usually be serialized into a sequence of bytes (represented by a Bytes value in Fift) and then saved into a file or transferred by network. Afterwards, it can be describilized to recover the original cells. The TON Blockchain systematically represents different data structures (including the TON Blockchain blocks) as a tree of cells according to a certain TL-B scheme (cf. [5], where this scheme is explained in detail), and then these trees of cells are routinely imported into bags of cells and serialized into binary files.

Fift words for manipulating bags of cells include:

- B>boc (B-c), deservatives a "standard" bag of cells (i.e., a bag of cells with exactly one root cell) represented by Bytes B, and returns the root Cell c.
- boc+>B $(c \times B)$, creates and serializes a "standard" bag of cells, containing one root Cell c along with all its descendants. An Integer parameter $0 \le x \le 31$ is used to pass flags indicating the additional options for bag-of-cells serialization, with individual bits having the following effect:
 - +1 enables bag-of-cells index creation (useful for lazy deserialization of large bags of cells)
 - +2 includes the CRC32-C of all data into the serialization (useful for checking data integrity).
 - +4 explicitly stores the hash of the root cell into the serialization (so that it can be quickly recovered afterwards without a complete deserialization).
 - +8 stores hashes of some intermediate (non-leaf) cells (useful for lazy deserialization of large bags of cells).
 - +16 stores cell cache bits to control caching of deserialized cells.

Typical values of x are x = 0 or x = 2 for very small bags of cells (e.g., TON Blockchain external messages) and x = 31 for large bags of cells (e.g., TON Blockchain blocks).

• boc>B (c-B), serializes a small "standard" bag of cells with root Cell c and all its descendants. Equivalent to 0 boc+>B.

For instance, the cell created in 5.2 with a value of TL-B Test type may be serialized as follows:

outputs "B5EE9C720104010100000000000000E4A4357C46535FF ok". Here Bx. is the word that prints the hexadecimal representation of a Bytes value.

5.6 Binary file I/O and Bytes manipulation

The following words can be used to manipulate values of type Bytes (arbitrary byte sequences) and to read them from or write them into binary files:

- $B\{hex-digits\}$ (-B), pushes a Bytes literal containing data represented by an even number of hexadecimal digits.
- Bx.(B-), prints the hexadecimal representation of a Bytes value. Each byte is represented by exactly two uppercase hexadecimal digits.
- file>B (5-B), reads the (binary) file with the name specified in String 5 and returns its contents as a Bytes value. If the file does not exist, an exception is thrown.
- B>file (B 5), creates a new (binary) file with the name specified in String 5 and writes data from Bytes B into the new file. If the specified file already exists, it is overwritten.
- file-exists? (5-?), checks whether the file with the name specified in String 5 exists.

For instance, the bag of cells created in the example in 5.5 can be saved to disk as sample.boc as follows: $\frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) \left(\frac{1}{2} \right)$

It can be loaded and deserialized afterwards (even in another Fift session) by means of file>B and B>boc:

{ <s 8 u@+ swap 0x4a <> abort"constructor tag mismatch" 16 u@+ 32 i@+ s> } : unpackTest
"sample.boc" file>B B>boc unpackTest swap . .

prints "17239 -1000000001 ok".

Additionally, there are several words for directly packing (serializing) data into *Bytes* values, and unpacking (deserializing) them afterwards. They can be combined with B>file and file>B to save data directly into binary files, and load them afterwards.

- Blen (B x), returns the length of a Bytes value B in bytes.
- BhashB (B B), computes the sha256 hash of a Bytes value. The hash is returned as a 32-byte Bytes value.
- Bhashu (B-x), computes the sha256 hash of a Bytes value and returns the hash as an unsigned 256-bit big-endian integer.
- B = (B B ?), checks whether two Bytes sequences are equal.
- Bcmp(BB-x), lexicographically compares two Bytes sequences, and returns -1, 0, or 1, depending on the comparison result.
- B>i@ $(B \times y)$, deserializes the first x/8 bytes of a Bytes value B as a signed big-endian x-bit Integer y.
- $B > i@ + (B \times By)$, deservalizes the first x/8 bytes of B as a signed big endian x-bit $Integer\ y$ similarly to B > i@, but also returns the remaining bytes of B.
- B>u@, B>u@+, variants of B>i@ and B>i@+ deserializing unsigned integers.
- B>Li@, B>Li@+, B>Lu@, B>Lu@+, little-endian variants of B>i@, B>i@+, B>u@, B>u@+.
- $B | (B \times B B)$, cuts the first x bytes from a Bytes value B, and returns both the first x bytes (B) and the remainder (B) as new Bytes values.
- i>B $(x \ y B)$, stores a signed big-endian y-bit Integer x into a Bytes value B consisting of exactly y/8 bytes. Integer y must be a multiple of eight in the range 0 . . . 256
- u > B (x y B), stores an unsigned big-endian y-bit Integer x into a Bytes value B consisting of exactly y/8 bytes, similarly to i > B.
- Li>B, Lu>B, little-endian variants of i>B and u>B.

• B+(BB-B), concatenates two Bytes sequences.

6 TON-specific operations

This chapter describes the TON-specific Fift words, with the exception of the words used for Cell manipulation, already discussed in the previous chapter.

6.1 Ed25519 cryptography

Fift offers an interface to the same Ed25519 elliptic curve cryptography used by TVM, described in Appendix A of [5]:

- now (-x), returns the current Unixtime as an Integer.
- newkeypair (-BB), generates a new Ed25519 private/public key pair, and returns both the private key B and the public key B as 32- byte Bytes values. The quality of the keys is good enough for testing purposes. Real applications must feed enough entropy into OpenSSL PRNG before generating Ed25519 keypairs.
- priv>pub (B B), computes the public key corresponding to a private Ed25519 key. Both the public key B and the private key B are represented by 32-byte Bytes values.
- ed25519_sign (BB B), signs data B with the Ed25519 private key B(a 32-byte Bytes value) and returns the signature as a 64-byte Bytes value B.
- ed25519_sign_uint (x B B), converts a big-endian unsigned 256- bit integer x into a 32-byte sequence and signs it using the Ed25519 private key Bsimilarly to ed25519_sign. Equivalent to swap 256 u>B swap ed25519_sign. The integer x to be signed is typically computed as the hash of some data.
- ed25519_chksign (BBB -?), checks whether Bis a valid Ed25519 signature of data B with the public key B.

6.2 Smart-contract address parser

Two special words can be used to parse TON smart-contract addresses in human-readable (base64 or base64url) forms:

- smca> $\frac{1}{5}$ (x y z $\frac{5}{5}$), packs a standard TON smart-contract address with workchain x (a signed 32-bit *Integer*) and in-workchain address y (an unsigned 256-bit *Integer*) into a 48-character string y (the human readable representation of the address) according to flags y. Possible individual flags in y are: +1 for non-bounceable addresses, +2 for testnet-only addresses, and +4 for base64url output instead of base64.
- \$>smca (5 x y z 1 or 0), unpacks a standard TON smart-contract address from its human-readable string representation 5. On success, returns the signed 32-bit workchain x, the unsigned 256-bit in workchain address y, the flags z (where +1 means that the address is non-bounceable, +2 that the address is testnet-only), and -1. On failure, pushes 0.

A sample human-readable smart-contract address could be deserialized and displayed as follows:

"Ef9Tj6fMJP-OqhAdhKXxq36DL-HYSzCc3-906UNzqsgPfYFX" \$>smca 0= abort"bad address" rot . swap x. . cr

outputs "-1 538fa7...0f7d 0", meaning that the specified address is in workchain -1 (the masterchain of the TON Blockchain), and that the 256-bit address inside workchain -1 is 0x538...f7d.

6.3 Dictionary manipulation

Fift has several words for hashmap or (TVM) dictionary manipulation, corresponding to values of TL-B type HashmapE n X as described in [4, 3.3]. These (TVM) dictionaries are not to be confused with the Fift dictionary, which is a completely different thing. A dictionary of TL-B type HashmapE n X is essentially a key-value collection with distinct n-bit keys (where 0 \(\leq n \) (1023) and values of an arbitrary TL-B type X. Dictionaries are represented by trees of cells (the complete layout may be found in [4, 3.3]) and stored as values of type Cell or Slice in the Fift stack. Sometimes empty dictionaries are represented by the Null value.

- dictnew (-D), pushes a *Null* value that represents a new empty dictionary.
- idict! (v x D n D –1 or D 0), adds a new value v (represented by a Slice) with key given by signed big-endian n-bit integer x into dictionary D (represented by a Cell or a Null) with n-bit keys, and returns the new dictionary D and –1 on success. Otherwise the unchanged dictionary D and 0 are returned.
- idict!+ $(v \times D \cap D \cap D \cap D)$, adds a new key-value pair (x, v) into dictionary D similarly to idict!, but fails if the key already exists by returning the unchanged dictionary D and O.
- b>idict!, b>idict!+, variants of idict! and idict!+ accepting the new value v in a Builder instead of a Slice.
- udict!, udict!+, b>udict!+, b>udict!+, variants of idict!, idict!+, b>idict!+, bvidict!+, but with an unsigned n-bit integer x used as a key.
- sdict!, sdict!+, b>sdict!, b>sdict!+, variants of idict!, idict!+, b>idict!+, bvidict!+, but with the first n data bits of Slice x used as a key.

- idict@ (x D n v 1 or 0), looks up the key represented by signed big-endian n-bit Integer x in the dictionary represented by Cell D. If the key is found, returns the corresponding value as a Slice v and -1. Otherwise returns 0.
- idict@- (x D n Dv 1 or D 0), looks up the key represented by signed big-endian n-bit Integer x in the dictionary represented by Cell D. If the key is found, deletes it from the dictionary and returns the modified dictionary D, the corresponding value as a Slice v, and -1. Otherwise returns the unmodified dictionary D and D.
- idict- (x D n D 1 or D 0), deletes integer key x from dictionary D similarly to idict@-, but does not return the value corresponding to x in the old dictionary D.
- udict@, udict@-, udict-, variants of idict@, idict@-, idict-, but with an unsigned big-endian n-bit Integer x used as a key.
- sdict@, sdict@-, sdict-, variants of idict@, idict@-, idict-, but with the key provided in the first n bits of Slice k.
- dictmap (D n e s), applies execution token e (i.e., an anonymous function) to each of the key-value pairs stored in a dictionary D with n-bit keys. The execution token is executed once for each key-value pair, with a *Builder* b and a *Slice* v (containing the value) pushed into the stack before executing e. After the execution e must leave in the stack either a modified *Builder* b (containing all data from b along with the new value v) and -1, or 0 indicating failure. In the latter case, the corresponding key is omitted from the new dictionary.
- dictmerge (D D n e D), combines two dictionaries D and D with n-bit keys into one dictionary D with the same keys. If a key is present in only one of the dictionaries D and D, this key and the corresponding value are copied verbatim to the new dictionary D. Otherwise the execution token (anonymous function) e is invoked to merge the two values v and v corresponding to the same key k in D and D, respectively. Before e is invoked, a Builder b and two Slices v and v representing the two values to be merged are pushed. After the execution he leaves either a modified Builder b(containing the original data from b along with the combined value) and -1, or O on failure. In the latter case, the corresponding key is omitted from the new dictionary.

Fift also offers some support for prefix dictionaries:

- pfxdict!+ (v k s n s 1 or s 0), adds key-value pair (k, v) into prefix dictionary s similarly to pfxdict!, but fails if the key already exists.
- pfxdict@ (k sn v 1 or 0), looks up key k (represented by a Slice) in the prefix dictionary s with the length of keys limited by n bits. On success, returns the value found v and v a

6.4 Invoking TVM from Fift

TVM can be linked with the Fift interpreter. In this case, several Fift prim itives become available that can be used to invoke TVM with arguments

provided from Fift. The arguments can be prepared in the Fift stack, which is passed in its entirety to the new instance of TVM. The resulting stack and the exit code are passed back to Fift and can be examined afterwards.

- runvmcode (... 5 ... x), invokes a new instance of TVM with the current continuation cc initialized from *Slice s*, thus executing code s in TVM. The original Fift stack (without s) is passed in its entirety as the initial stack of TVM. When TVM terminates, its resulting stack is used as the new Fift stack, with the exit code x pushed at its top. If x is non-zero, indicating that TVM has been terminated by an unhandled exception, the next stack entry from the top contains the parameter of this exception, and x is the exception code. All other entries are removed from the stack in this case.
- runvmdict (... s ... x), invokes a new instance of TVM with the cur rent continuation cc initialized from Slice s similarly to runvmcode, but also initializes the special register c3 with the same value, and pushes a zero into the initial TVM stack before the TVM execution begins. In a typical application Slice s consists of a subroutine selection code that uses the top-of-stack Integer to select the subroutine to be executed, thus enabling the definition and execution of several mutually-recursive subroutines (cf. [4, 4.6] and 7.8). The selector equal to zero corresponds to the main() subroutine in a large TVM program.
- runvm (... 5 C ... X C), invokes a new instance of TVM with both the current continuation cc and the special register c3 initialized from Slice s, similarly to runvmdict (without pushing an extra zero to the initial TVM stack; if necessary, it can be pushed explicitly under s), and also initializes special register c4 (the "root of persistent data", cf. [4, 1.4]) with Cell c. The final value of c4 is returned at the top of the final Fift stack as another Cell c. In this way one can emulate the execution of smart contracts that inspect or modify their persistent storage.
- runvmctx (...5 ct ... xc), a variant of runvm that also initializes c7 (the "context") with Tuple t. In this way the execution of a TVM smart contract inside TON Blockchain can be completely emulated, if the correct context is loaded into c7 (cf. [5, 4.4.10]).
- gasrunvmcode (... SZ ... XZ), a gas-aware version of runvmcode that accepts an extra *Integer* argument z (the original gas limit) at the top of the stack, and returns the gas consumed by this TVM run as a new top-of-stack *Integer* value z.
- gasrunvmdict (... 5 Z ... X Z), a gas-aware version of runvmdict. gasrunvm (... s c Z ... x cz), a gas-aware version of runvmctx (... s c t Z ... x cz), a gas-aware version of runvmctx.

For example, one can create an instance of TVM running some simple code as follows:

2 3 9 x{1221} runvmcode .s

The TVM stack is initialized by three integers 2, 3, and 9 (in this order; 9 is the topmost entry), and then the $Slice \times \{1221\}$ containing 16 data bits and no references is transformed into a TVM continuation and executed. By consulting Appendix A of [4], we see that $\times \{12\}$ is the code of the TVM instruction XCHG s1, s2, and that $\times \{21\}$ is the code of the TVM instruction OVER (not to be confused with the Fift primitive over, which incidentally has the same effect on the stack). The result of the above execution is:

execute XCHG s1,s2 execute OVER execute implicit RET 32920

Here O is the exit code (indicating successful TVM termination), and 3 2 9 2 is the final TVM stack state.

If an unhandled exception is generated during the TVM execution, the code of this exception is returned as the exit code:

2 3 9 x{122} runvmcode .s

produces

execute XCHG s1,s2

handling exception code 6: invalid or too short opcode default exception handler, terminating vm with exit code 6 0 6 ok

Notice that TVM is executed with internal logging enabled, and its log is displayed in the standard output.

Simple TVM programs may be represented by Slice literals with the aid of the $x{...}$ construct similarly to the above examples. More sophisticated programs are usually created with the aid of the Fift assembler as explained in the next chapter.

7 Using the Fift assembler

The Fift assembler is a short program (currently less than 30KiB) written completely in Fift that transforms human-readable mnemonics of TVM instructions into their binary representation. For instance, one could write <{ sl s2 XCHG OVER }>s instead of x{1221} in the example discussed in 6.4, provided the Fift assembler has been loaded beforehand (usually by the phrase "Asm.fif" include).

7.1 Loading the Fift assembler

The Fift assembler is usually located in file Asm.fif in the Fift library directory (which usually contains standard Fift library files such as Fift.fif). It is typically loaded by putting the phrase "Asm.fif" include at the very beginning of a program that needs to use Fift assembler:

• include (5 -), loads and interprets a Fift source file from the path given by String 5. If the filename 5 does not begin with a slash, the Fift include search path, typically taken from the FIFTPATH environment variable or the -I command-line argument of the Fift interpreter (and equal to /usr/lib/fift if both are absent), is used to locate 5.

The current implementation of the Fift assembler makes heavy use of custom defining words (cf. 4.8); its source can be studied as a good example of how defining words might be used to write very compact Fift programs (cf. also the original edition of [1], where a simple 8080 Forth assembler is discussed).

In the future, almost all of the words defined by the Fift assembler will be moved to a separate vocabulary (namespace). Currently they are defined in the global namespace, because Fift does not support namespaces yet.

7.2 Fift assembler basics

The Fift assembler inherits from Fift its postfix operation notation, i.e., the arguments or parameters are written before the corresponding instructions. For instance, the TVM assembler instruction represented as XCHG s1,s2 in [4] is represented in the Fift assembler as s1 s2 XCHG.

Fift assembler code is usually opened by a special opening word, such as <{, and terminated by a closing word, such as }> or }>s. For instance,

"Asm.fif" include <{ s1 s2 XCHG OVER }>s

compiles two TVM instructions XCHG s1,s2 and OVER, and returns the result as a Slice (because)>s is used). The resulting Slice is displayed by csr., yielding

x{1221}

One can use Appendix A of [4] and verify that x{12} is indeed the (codepage zero) code of the TVM instruction XCHG s1,s2, and that x{21} is the code of the TVM instruction OVER (not to be confused with Fift primitive over).

In the future, we will assume that the Fift assember is already loaded and omit the phrase "Asm.fif" include from our examples.

The Fift assembler uses the Fift stack in a straightforward fashion, using the top several stack entries to hold a Builder with the code being assembled, and the arguments to TVM instructions. For example:

- $\{ (-b), begins a portion of Fift assembler code by pushing an empty Builder into the Fift stack (and potentially switching the namespace to the one containing all Fift$ assembler-specific words). Approximately equivalent to <b.
- b = b, terminates a portion of Fift assembler code and returns the assembled portion as a Builder (and potentially recovers the original namespace). Approximately equivalent to nop in most situations.
- > c (b c), terminates a portion of Fift assembler code and returns the assembled portion as a Cell (and potentially recovers the original namespace). Approximately equivalent to b>.
- $\}$ >5 (b-5), terminates a portion of Fift assembler code similarly to $\}$ >, but returns the assembled portion as a *Slice*. Equivalent to $\}$ >c <s.
- OVER (b-b), assembles the code of the TVM instruction OVER by appending it to the Builder at the top of the stack. Approximately equivalent to x{21} s,
- S1(-5), pushes a special Slice used by the Fift assembler to represent the "stack register" S1 of TVM.
- **SO.... s15 (s)**, words similar to s1, but pushing the *Slice* representing other "stack registers" of TVM. Notice that s16... s255 must be accessed using the word s().
- S()(x-5), takes an Integer argument $0 \le x \le 255$ and returns a special Slice used by the Fift assembler to represent "stack register" S(x).
- XCHG (b s s b), takes two special Slices representing two "stack registers" s(i) and s(j) from the stack, and appends to Builder b the code for the TVM instruction XCHG s(i), s(i).

In particular, note that the word OVER defined by the Fift assembler has a completely different effect from Fift primitive over.

The actual action of OVER and other Fift assembler words is somewhat more complicated than that of x{21} s,. If the new instruction code does not fit into the Builder b (i.e., if b would contain more than 1023 data bits after adding the new instruction code), then this and all subsequent instructions are assembled into a new Builder b, and the old Builder b is augmented by a reference to the Cell obtained from b once the generation of b is finished. In this way long stretches of TVM code are automatically split into chains of valid Cells containing at most 1023 bits each. Because TVM interprets a lonely cell reference at the end of a continuation as an implicit JMPREF, this partitioning of TVM code into cells has almost no effect on the execution.

7.3 Pushing integer constants

The TVM instruction PUSHINT x, pushing an Integer constant x when in voked, can be assembled with the aid of Fift assembler words INT or PUSHINT:

• PUSHINT $(b \times - b)$, assembles TVM instruction PUSHINT x into a Builder. • INT $(b \times - b)$, equivalent to PUSHINT.

Notice that the argument to PUSHINT is an *Integer* value taken from the Fift stack and is not necessarily a literal. For instance, <{ 239 17 * INT }>s is a valid way to assemble a PUSHINT 4063 instruction, because 239·17 = 4063. Notice that the multiplication is performed by Fift during assemble time, not during the TVM runtime. The latter computation might be performed by means of <{ 239 INT 17 INT MUL }>s:

```
<{ 239 I7 * INT }>s dup csr. runvmcode .s 2drop
<{ 239 INT 17 INT MUL }>s dup csr. runvmcode .s 2drop produces
x{810FDF}
execute PUSHINT 4063
execute implicit RET
4063 0
ok
x{8100EF8011A8}
execute PUSHINT 239
execute PUSHINT 17
execute MUL
execute implicit RET
4063 0
```

Notice that the Fift assembler chooses the shortest encoding of the PUSHINT x instruction depending on its argument x.

7.4 Immediate arguments

Some TVM instructions (such as PUSHINT) accept immediate arguments. These arguments are usually passed to the Fift word assembling the cor responding instruction in the Fift stack. Integer immediate arguments are usually represented by *Integer* s, cells by *Cells*, continuations by *Builder* s and *Cells*, and cell slices by *Slices*. For instance, 17 ADDCONST assembles TVM instruction ADDCONST 17, and x{ABCD_} PUSHSLICE assembles PUSHSLICE xABCD_:

239 $\{$ 17 ADDCONST \times {ABCD_} PUSHSLICE $\}$ >s dup csr. runvmcode . swap . csr.

produces

x{A6118B2ABCD0}
execute ADDINT 17
execute PUSHSLICE xABCD_
execute implicit RET
0 256 x{ABCD_}

On some occasions, the Fift assembler pretends to be able to accept imme diate arguments that are out of range for the corresponding TVM instruction. For instance, ADDCONST x is defined only for $\neg 128 \le x < 128$, but the Fift assembler accepts 239 ADDCONST:

17 <{ 239 ADDCONST }>s dup csr. runvmcode .s

produces

x{8100EFA0} execute PUSHINT 239 execute ADD execute implicit RET 256 0

We can see that "ADDCONST 239" has been tacitly replaced by PUSHINT 239 and ADD. This feature is convenient when the immediate argument to ADDCONST is itself a result of a Fift computation, and it is difficult to esti mate whether it will always fit into the required range.

In some cases, there are several versions of the same TVM instructions, one accepting an immediate argument and another without any arguments. For instance, there are both LSHIFT n and LSHIFT instructions. In the Fift assembler, such variants are assigned distinct mnemonics. In partic ular, LSHIFT n is represented by n LSHIFT#, and LSHIFT is represented by itself.

7.5 Immediate continuations

When an immediate argument is a continuation, it is convenient to create the corresponding *Builder* in the Fift stack by means of a nested <{ . . . }> construct. For instance, TVM assembler instructions

```
PUSHINT 1
SWAP
PUSHCONT {
MULCONST 10
}
REPEAT
```

can be assembled and executed by

 $\{1 \text{ INT SWAP } \{10 \text{ MULCONST }\} \}$ PUSHCONT REPEAT $\}$'s dup csr. runvmcode drop .

producing

x{710192A70AE4}
execute PUSHINT 1
execute SWAP
execute PUSHCONT xA70A
execute REPEAT
repeat 7 more times
execute MULINT 10
execute implicit RET
repeat 6 more times

repeat 1 more times execute MULINT 10

```
execute implicit RET
repeat 0 more times
execute implicit RET
10000000
```

More convenient ways to use literal continuations created by means of the Fift assembler exist. For instance, the above example can be also assembled by

```
 \begin{tabular}{ll} $$ $$ $ (1 INT SWAP CONT: { 10 MULCONST }> REPEAT }>s csr. or even $$ $$ $$ $$ INT SWAP REPEAT: { 10 MULCONST }> $>s csr. \\ \end{tabular}
```

both produce "x{710192A70AE4} ok".

Incidentally, a better way of implementing the above loop is by means of REPEATEND:

7 <{ 1 INT SWAP REPEATEND 10 MULCONST }>s dup csr. runvmcode drop .

or

7 <{ 1 INT SWAP REPEAT: 10 MULCONST }>s dup csr.

runvmcode drop.

both produce " $x{7101E7A70A}$ " and output "10000000" after seven iterations of the loop.

Notice that several TVM instructions that store a continuation in a sep arate cell reference (such as JMPREF) accept their argument in a *Cell*, not in a *Builder*. In such situations, the <{ ... }>c construct can be used to produce this immediate argument.

7.6 Control flow: loops and conditionals

Almost all TVM control flow instructions—such as IF, IFNOT, IFRET, IFNOTRET, IFELSE, WHILE, WHILEEND, REPEAT, REPEATEND, UNTIL, and UNTILEND—can be assembled similarly to REPEAT and REPEATEND in the examples of 7.5 when applied to literal continuations. For instance, TVM assembler code

```
DUP
PUSHINT 1
AND
PUSHCONT {
MULCONST 3
INC
}
PUSHCONT {
RSHIFT 1
}
IFELSE
```

execute INC

22 ok

execute implicit RET execute implicit RET

which computes 3n + 1 or n/2 depending on whether its argument n is odd or even, can be assembled and applied to n = 7 by

```
<{ DUP 1 INT AND
IF:<{ 3 MULCONST INC }>ELSE<{ 1 RSHIFT# }>
}>s dup csr.
7 swap runvmcode drop .

producing

x{2071B093A703A492AB00E2}
ok
execute DUP
execute PUSHINT 1
execute AND
execute PUSHCONT xA703A4
execute PUSHCONT xA800
execute IFELSE
execute MULINT 3
```

Of course, a more compact and efficient way to implement this conditional expression would be

```
<{ DUP 1 INT AND
IF:<{ 3 MULCONST INC }>ELSE: 1 RSHIFT#
}>s dup csr.
or
<{ DUP 1 INT AND
CONT:<{ 3 MULCONST INC }> IFJMP
1 RSHIFT#
}>s dup csr.
```

both producing the same code "x{2071B093A703A4DCAB00}". Fift assembler words that can be used to produce such "high-level" conditionals and loops include IF:<{, IFNOT:<{, IFJMP:<{, }>ELSE:, }>IF, REPEAT:<{, UNTIL:<{, WHILE:<{, }>DO<{, }>DO:, AGAIN:<{, }>AGAIN, }>REPEAT, and }>UNTIL. Their complete list can be found in the source file Asm.fif. For instance, an UNTIL loop can be created by UNTIL:<{ ... }> or <{ ... }>UNTIL, and a WHILE loop by WHILE:<{ ... }>DO<{ ... }>. If we choose to keep a conditional branch in a separate cell, we can use the <{ ... }>c construct along with instructions such as IFJMPREF:

```
<{ DUP 1 INT AND
<{ 3 MULCONST INC }>c IFJMPREF
1 RSHIFT#
}>s dup csr.
3 swap runvmcode .s
```

has the same effect as the code from the previous example when executed, but it is contained in two separate cells:

```
x{2071B0E302AB00}
x{A703A4}
execute DUP
execute PUSHINT 1
execute AND
```

execute IFJMPREF (2946....A1DD)
execute MULINT 3
execute INC
execute implicit RET
10 0

{ 2dup > ' swap if

7.7 Macro definitions

Because TVM instructions are implemented in the Fift assembler using Fift words that have a predictable effect on the Fift stack, the Fift assembler is automatically a macro assembler, supporting macro definitions. For instance, suppose that we wish to define a macro definition RANGE x y, which checks whether the TVM top-of-stack value is between integer literals x and y (inclusive). This macro definition can be implemented as follows:

```
rot DUP rot GEQINT SWAP swap LEQINT AND
}: RANGE

<{ DUP 17 239 RANGE IFNOT: DROP ZERO }>s dup csr. 66 swap runvmcode drop .

which produces

x{2020C210018100F0B9B0DC3070}

execute DUP

execute DUP

execute GTINT 16

execute SWAP

execute PUSHINT 240

execute LESS

execute AND

execute IFRET

66
```

Notice that GEQINT and LEQINT are themselves macro definitions defined in Asm.fif, because they do not correspond directly to TVM instructions. For instance, x GEQINT corresponds to the TVM instruction GTINT x - 1.

Incidentally, the above code can be shortened by two bytes by replacing IFNOT: DROP ZERO with AND.

7.8 Larger programs and subroutines

Larger TVM programs, such as TON Blockchain smart contracts, typically consist of several mutually recursive subroutines, with one or several of them selected as top-level subroutines (called main() or recv_internal() for smart contracts). The execution starts from one of the top-level subroutines, which is free to call any of the other defined subroutines, which in turn can call whatever other subroutines they need.

Such TVM programs are implemented by means of a selector function, which accepts an extra integer argument in the TVM stack; this integer selects the actual subroutine to be invoked (cf. [4, 4.6]). Before execution, the code of this selector function is loaded both into special register c3 and into the current continuation cc. The selector of the main function (usually zero) is pushed into the initial stack, and the TVM execution is started. Afterwards a subroutine can be invoked by means of a suitable TVM instruction, such as CALLDICT n, where n is the (integer) selector of the subroutine to be called.

The Fift assembler offers several words facilitating the implementation of such large TVM programs. In particular, subroutines can be defined sep arately and assigned symbolic names (instead of numeric selectors), which can be used to call them afterwards. The Fift assembler automatically cre ates a selector function from these separate subroutines and returns it as the top-level assembly result.

Here is a simple example of such a program consisting of several subrou tines. This program computes the complex number $(5 + i)^4$ (239 – i):

```
"Asm.fif" include
PROGRAM{
NEWPROC add
NEWPROC sub
NEWPROC mul
sub <{ s3 s3 XCHG2 SUB s2 XCHG0 SUB }>s PROC
// compute (5+i)^4 * (239-i)
main PROC:<{
5 INT 1 INT // 5+i
2DUP
mul CALL
2DUP
mul CALL
239 INT -1 INT
mul JMP
}>
add PROC:<{
s1 s2 XCHG
ADD-ROT ADD SWAP
}>
// a b c d -- ac-bd ad+bc : complex number multiplication mul PROC:<{
s3 s1 PUSH2 // a b c d a c
MUL // a b c d ac
s3 s1 PUSH2 // a b c d ac b d
MUL // a b c d ac bd
SUB // a b c d ac-bd
s4 s4 XCHG2 // ac-bd b c a d
MUL // ac-bd b c ad
-ROT MUL ADD
}>
}END>s
dup csr.
runvmdict.s
```

This program produces:

```
x{FF00F4A40EF4A0F20B}
x{D9_}
x{2_}
x{1D5C573C00D73C00E0403BDFFC5000E_}
x{04A81668006_}
x\{2_{}\}
x{140CE840A86_}
x{14CC6A14CC6A2854112A166A282_}
implicit PUSH 0 at start
execute SETCP 0
execute DICTPUSHCONST 14 (xC_,1)
execute DICTIGETJMP
execute PUSHINT 5
execute PUSHINT 1
execute 2DUP
execute CALLDICT 3
execute SETCP 0
execute DICTPUSHCONST 14 (xC_,1)
execute DICTIGETJMP
execute PUSH2 s3,s1
execute MUL
execute ROTREV
execute MUL
execute ADD
execute implicit RET
114244 114244 0
```

subroutine is not redefined.

Some observations and comments based on the previous example follow:

4.4]), can be declared by means of constant (e.g., -1 constant recv external).

- A TVM program is opened by PROGRAM{ and closed by either }END>c (which returns the assembled program as a Cell) or }END>s (which returns a Slice).
- A new subroutine is declared by means of the phrase NEWPROC *name*. This declaration assigns the next positive integer as a selector for the newly-declared subroutine, and stores this integer into the constant *name*. For instance, the above declarations define add, sub, and mul as integer constants equal to 1, 2, and 3, respectively.
- Some subroutines are predeclared and do not need to be declared again by NEWPROC. For instance, main is a subroutine identifier bound to the integer constant
- Some subroutines are predeclared and do not need to be declared again by NEWPRUL. For instance, main is a subroutine identifier bound to the integer constant (selector) 0.

• Other predefined subroutine selectors such as recv_internal (equal to 0) or recv_external (equal to -1), useful for implementing TON Blockchain smart contracts (cf. [5,

- A subroutine can be defined either with the aid of the word PROC, which accepts the integer selector of the subroutine and the *Slice* containing the code for this
- subroutine, or with the aid of the construct selector PROC:<{ ... }>, convenient for defining larger subroutines.
- CALLDICT and JMPDICT instructions may be assembled with the aid of the words CALL and JMP, which accept the integer selector of the subroutine to be called as an immediate argument passed in the Fift stack.

• The current implementation of the Fift assembler collects all subrou tines into a dictionary with 14-bit signed integer keys. Therefore, all subroutine selectors must be in

- the range $-2^{13} \dots 2^{13} 1$.

 If a subroutine with an unknown selector is called during runtime, an exception with code 11 is thrown by the code automatically inserted by the Fift assembler. This
- The Fift assembler checks that all subroutines declared by NEWPROC are actually defined by PROC or PROC:<{ before the end of the program. It also checks that a

One should bear in mind that very simple programs (including the sim plest smart contracts) may be made more compact by eliminating this general subroutine selection machinery in favor of custom subroutine selection code and removing unused subroutines. For instance, the above example can be transformed into

```
<{ 11 THROWIF
CONT:<{ s3 s1 PUSH2 MUL s3 s1 PUSH2 MUL SUB
s4 s4 XCHG2 MUL -ROT MUL ADD }>
5 INT 1 INT 2DUP s4 PUSH CALLX
2DUP s4 PUSH CALLX
ROT 239 INT -1 INT ROT JMPX
}>s
dup csr.
runvmdict.s
which produces
x{F24B9D5331A85331A8A15044A859A8A075715C24D85C24D8588100EF7F58D9} implicit PUSH 0 at start
execute THROWIF 11
execute PUSHCONT x5331A85331A8A15044A859A8A0
execute PUSHINT 5
execute PUSHINT 1
execute 2DUP
execute PUSH s4
execute EXECUTE
execute PUSH2 s3,s1
execute MUL
execute XCHG2 s4,s4
execute MUL
execute ROTREV
execute MUL
execute ADD
execute implicit RET
114244 114244 0
```

code also automatically selects codepage zero for instruction encoding by means of a SETCPO instruction.

References

- [1] L. Brodie, Starting Forth: Introduction to the FORTH Language and Operating System for Beginners and Professionals, 2nd edition, Prentice Hall, 1987. Available at https://www.forth.com/starting-forth/.
- [2] L. Brodie, Thinking Forth: A language and philosophy for solving problems, Prentice Hall, 1984. Available at http://thinking-forth. sourceforge.net/.
- [3] N. Durov, Telegram Open Network, 2017.
- [4] N. Durov, Telegram Open Network Virtual Machine, 2018. [5] N. Durov, Telegram Open Network Blockchain, 2018.

A List of Fift words

This Appendix provides an alphabetic list of almost all Fift words—including primitives and definitions from the standard library Fift.fif, but excluding Fift assembler words defined in Asm.fif (because the Fift assembler is simply an application from the perspective of Fift). Some experimental words have been omitted from this list. Other words may have been added to or removed from Fift after this text was written. The list of all words available in your Fift interpreter may be inspected by executing words.

Each word is described by its name, followed by its stack notation in parentheses, indicating several values near the top of the Fift stack before and after the execution of the word; all deeper stack entries are usually assumed to be left intact. After that, a text description of the word's effect is provided. If the word has been discussed in a previous section of this document, a reference to this section is included.

Active words and active prefix words that parse a portion of the input stream immediately after their occurrence are listed here in a modified way. Firstly, these words are listed alongside the portion of the input that they parse; the segment of each entry that is actually a Fift word is underlined for emphasis. Secondly, their stack effect is usually described from the user's perspective, and reflects the actions performed during the execution phase of the encompassing blocks and word definitions. For example, the active prefix word B{, used for defining Bytes literals (cf. 5.6), is listed as B{hex-digits}, and its stack effect is shown as (-B) instead of (-B1e), even though the real effect of the execution of the active word B{ during the compilation phase of an encompassing block or word definition is the latter one (cf. 4.2).

- •! (x p), stores new value x into Box p, cf. 2.14.
- \bullet "string" (5), pushes a String literal into the stack, cf. 2.9 and 2.10.
- # (x 5 x 5), performs one step of the conversion of Integer x into its decimal representation by appending to String 5 one decimal digit representing x mod 10. The quotient x:= x/10 is returned as well.
- #> (5 S), finishes the conversion of an Integer into its human readable representation (decimal or otherwise) started with <# by re versing String S. Equivalent to Sreverse.
- #s (x 5 x 5), performs # one or more times until the quotient x becomes non-positive. Equivalent to $\{ * over 0 \le \}$ until.
- \$# (x), pushes the total number of command-line arguments passed to the Fift program, cf. 2.18. Defined only when the Fift interpreter is invoked in script mode (with the -s command line argument).
- \$(string) (...), looks up the word \$string during execution time and executes its current definition. Typically used to access the current values of command-line arguments, e.g., \$(2) is essentially equivalent to @' \$2. •\$() (x – S), pushes the x-th command-line argument similarly to \$n, but with Integer x 2 D taken from the stack, cf. 2.18. Defined only when the Fift interpreter is invoked in script mode (with the -s com mand line argument).
- \$+ (5 5 5.5), concatenates two strings, cf. 2.10.
- \$, (b 5 b), appends String 5 to Builder b, cf. 5.2. The string is interpreted as a binary string of length 8n, where n is the number of bytes in the UTF-8 representation of 5.
- \$\, (S), pushes the n-th command-line argument as a String 5, cf. 2.18. For instance, \$0 pushes the name of the script being executed, \$1 the first command line argument, and so on. Defined only when the Fift interpreter is invoked in script mode (with the -s command line argument).
- = (5 ?), returns -1 if strings 5 and 5 are equal, 0 otherwise, cf. 2.13. Equivalent to = 0
- \$>s (S s), transforms the String S into a Slice, cf. 5.3. Equivalent to <b swap \$, b> <s.
- •\$>smca (5 x y z –1 or 0), unpacks a standard TON smart-contract address from its human-readable string representation 5, cf. 6.2. On success, returns the signed 32-bit workchain x, the unsigned 256-bit in-workchain address y, the flags z (where +1 means that the address is non-bounceable, +2 that the address is testnet-only), and $\neg 1$. On failure, pushes 0.
- \$@ (s x S), fetches the first x bytes (i.e., 8x bits) from Slice s, and returns them as a UTF-8 String S, cf. 5.3. If there are not enough data bits in s, throws an exception.
- \$@+ (s x 5 s), similar to \$@, but returns the remainder of Slice s as well, cf. 5.3.
- \$@? (s x 5 1 or 0), similar to \$@, but uses a flag to indicate failure instead of throwing an exception, cf. 5.3.
- \cdot \$@?+ (s x 5 s -1 or s 0), similar to \$@+, but uses a flag to indicate failure instead of throwing an exception, cf. 5.3.
- \$cmp (5 5 x), returns 0 if strings 5 and 5 are equal, -1 if 5 is lexicographically less than 5, and 1 if 5 is lexicographically greater than 5, cf. 2.13.
- \bullet \$len (5 x), computes the byte length (not the UTF-8 character length!) of a string, cf. 2.10.
- \$pos (5 5 x or -1), returns the position (byte offset) x of the first occurrence of substring 5 in string 5 or -1.
 \$reverse (5 5), reverses the order of UTF-8 characters in String 5. If 5 is not a valid UTF-8 string, the return value is undefined and may be also invalid.
- %1<< (x y − z), computes z := x mod 2y = x&(2y − 1) for two Integer s x and 0 ≤ y ≤ 256.
- 'word-name (e), returns the execution token equal to the current (compile-time) definition of word-name, cf. 3.1. If the specified word is not found, throws an exception.
- 'nop (e), pushes the default definition of nop—an execution token that does nothing when executed, cf. 4.6.
- (') word-name (e), similar to ', but returns the definition of the specified word at execution time, performing a dictionary lookup each time it is invoked, cf. 4.6. May be used to recover the current values of constants inside word definitions and other blocks by using the phrase (') word-name execute.
- (-trailing) (5 x 5), removes from String 5 all trailing characters with UTF-8 codepoint x.
- (.) (x 5), returns the String with the decimal representation of Integer x. Equivalent to dup abs $\langle \# \#$ rot sign # > nip.
- (atom) (5 x a –1 or 0), returns the only Atom a with the name given by String 5, cf. 2.17. If there is no such Atom yet, either creates it (if Integer x is non-zero) or returns a single zero to indicate failure (if x is zero). • (b.) (x - 5), returns the String with the binary representation of Integer x.
- (compile) ($Ix_1...x_n$ n = -1), extends WordList I so that it would push $0 \le n \le 255$ values $x_1, ..., x_n$ into the stack and execute the execution token e when invoked, where $0 \le n \le 255$ is an Integer, cf. 4.7. If e is equal to the special value 'nop, the last step is
- (create) (e S x), creates a new word with the name equal to String S and definition equal to WordDef e, using flags passed in Integer 0 s x s 3, cf. 4.5. If bit +1 is set in x, creates an active word; if bit +2 is set in x, creates a prefix word.
- (dump) (x 5), returns a String with a dump of the topmost stack value x, in the same format as employed by .dump.
- (execute) (x1 ... xn n e ...), executes execution token e, but first checks that there are at least 0 s n s 255 values in the stack apart from n and e themselves. It is a counterpart of (compile) that may be used to immediately "execute" (perform the intended runtime action of) an active word after its immediate execution, as explained in 4.2.
- (forget) (5), forgets the word with the name specified in String S, cf. 4.5. If the word is not found, throws an exception.
- (number) (5 0 or x 1 or x y 2), attempts to parse the String 5 as an integer or fractional literal, cf. 2.10 and 2.8. On failure, returns a single 0. On success, returns x 1 if 5 is a valid integer literal with value x, or x y 2 if 5 is a valid fractional literal
- \bullet (x.) (x 5), returns the String with the hexadecimal representation of Integer x.
- ({) (I), pushes an empty WordList into the stack, cf. 4.7 • ()) (I – e), transforms a WordList into an execution token (WordDef), making all further modifications impossible, cf. 4.7.
- * (x y xy), computes the product xy of two Integer s x and y, cf. 2.4.
- •*/ (x y z xy/z), "multiply-then-divide": multiplies two integers x and y producing a 513-bit intermediate result, then divides the product by z, cf. 2.4.
- •*/c (x y z xy/z), "multiply-then-divide" with ceiling rounding: multiplies two integers x and y producing a 513-bit intermediate result, then divides the product by z, cf. 2.4. • */cmod (x y z - q r), similar to */c, but computes both the quotient q := xy/z and the remainder r := xy - y, cf. 2.4.
- */mod (x y z q r), similar to */, but computes both the quotient q := xy/z and the remainder r := xy qz, cf. 2.4.
- •*/r (x y z q := xy/z + 1/2), "multiply-then-divide" with nearest integer rounding: multiplies two integers x and y with 513-bit intermediate result, then divides the product by z, cf. 2.4.
- •*/rmod (x y z q r), similar to */r, but computes both the quotient q := xy/z + 1/2 and the remainder r := xy qz, cf. 2.4.
- *>> (x y z q), similar to */, but with division replaced with a right shift, cf. 2.4. Computes q := xy/2z for 0 ≤ z ≤ 256. Equivalent to 1<< */.
- *>>c (x y z q), similar to */c, but with division replaced with a right shift, cf. 2.4. Computes q := xy/2z for 0 < z < 256. Equivalent to 1<< */c.
- •*>>r (x y z q), similar to */r, but with division replaced with a right shift, cf. 2.4. Computes q := xy/2z + 1/2 for 0 < z < 256. Equivalent to 1<< */r. • *mod (x y z - r), similar to */mod, but computes only the remainder r := xy - qz, where q := xy/z. Equivalent to */mod nip.
- \bullet + (x y x+y), computes the sum x+y of two Integer s x and y, cf. 2.4.
- \bullet +! (x p), increases the integer value stored in Box p by Integer x, cf. 2.14. Equivalent to tuck @ + swap !.
- +"string" (5 5), concatenates String S with a string literal, cf. 2.10. Equivalent to "string" \$+.
- •, $(t \times t)$, appends x to the end of Tuple t, and returns the resulting Tuple t, cf. 2.15.
- - (x y x y), computes the difference x y of two Integer s x and y, cf. 2.4.
- -! (x p), decreases the integer value stored in Box p by Integer x. Equivalent to swap negate swap +!.
- -1 (-1), pushes Integer -1.
- -1 < (x -2x), computes -2xfor 0 \le x \le 256. Approximately equivalent to 1 < negate or -1 swap <, but works for x = 256 as well.
- -roll (xn ... x0 n x0 xn ... x1), rotates the top n stack entries in the opposite direction, where n 20 is also passed in the stack, cf. 2.5. In particular, 1 -roll is equivalent to swap, and 2 -roll to -rot.
- -rot (x y z z x y), rotates the three topmost stack entries in the opposite direction, cf. 2.5. Equivalent to rot rot.
- \bullet -trailing (S S), removes from String S all trailing spaces. Equiv alent to bl (-trailing).
- -trailing0 (5 5), removes from String 5 all trailing '0' characters. Equivalent to char 0 (-trailing).
- . (x), prints the decimal representation of Integer x, followed by a single space, cf. 2.4. Equivalent to ._ space.