

Hybridizing Knowledge-Based and Machine Learning Models for Climate and Tipping-Point Prediction

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<https://awikner.github.io/actm-umd-tamu-prllc>

Current Research Threads

- Build on our previous hybrid physics-ML weather forecasting method to allow nonstationarity, and to have appropriate variability, at climatological time scales
- Use ML to forecast bifurcations outside the parameter range of the training data in two scenarios:
 - Future evolution of parameter values is known or hypothesized
 - Parameter values (past and future) are unknown or unspecified
- Noise-emulating regularization to promote stability in iterative ML or hybrid forecasts

Reservoir Computing (RC)

- For ML we use reservoir computing (e.g., Lukoševicius and Jaeger 2009)
 - Recurrent Neural Network – enables memory of time series input
 - Simplified training – only the output layer parameters are trained
- Much faster training than other ML methods allows us to perform a lot of exploratory numerical experiments
- Our hybrid approach can be used with any ML method that is trained to make a short-term forecast
 - Short-term forecasts are cycled iteratively to make a long-term forecast

General Hybrid Modeling Approach

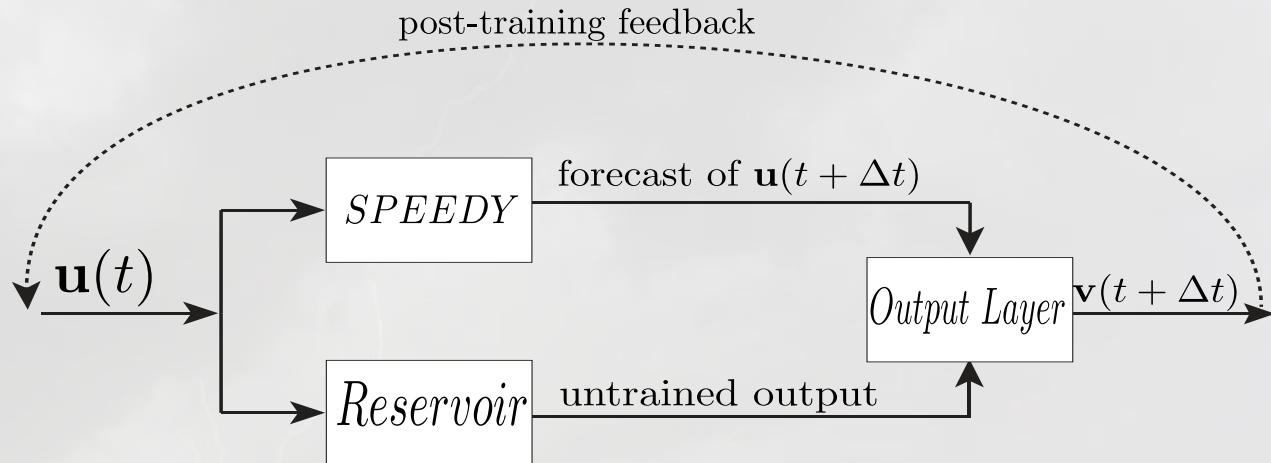
- Atmospheric state: $\mathbf{u}(t)$

- SPEEDY: AGCM

- Reservoir: RNN

- Output Layer: trained linear weights

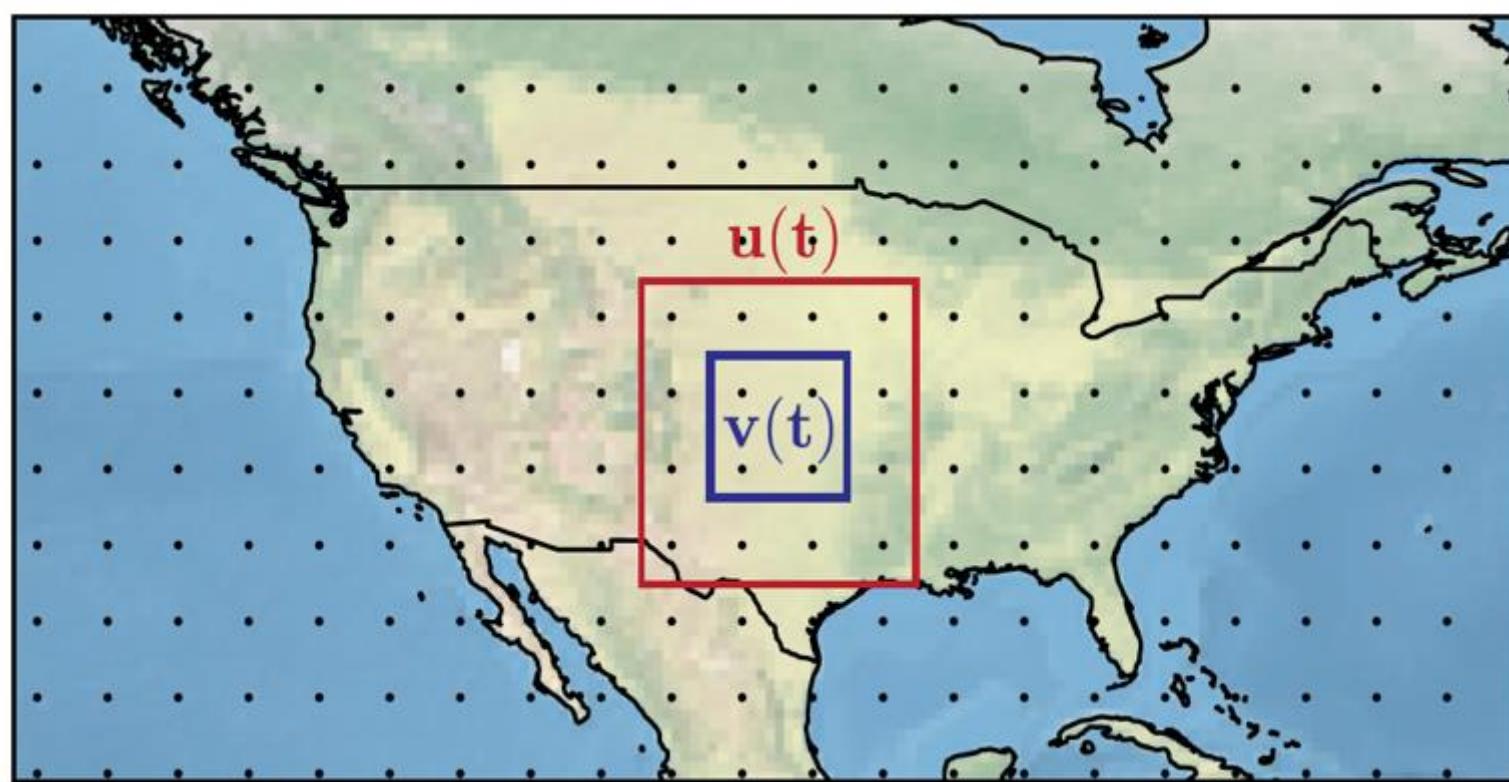
- $\mathbf{v}(t+\Delta t)$ approximates $\mathbf{u}(t+\Delta t)$ [or a sub-vector in the parallel version]



- Parallel version: ~1000 reservoirs, each forecasts on a separate local region
 - each output layer is independently trained; reservoirs exchange data only post-training

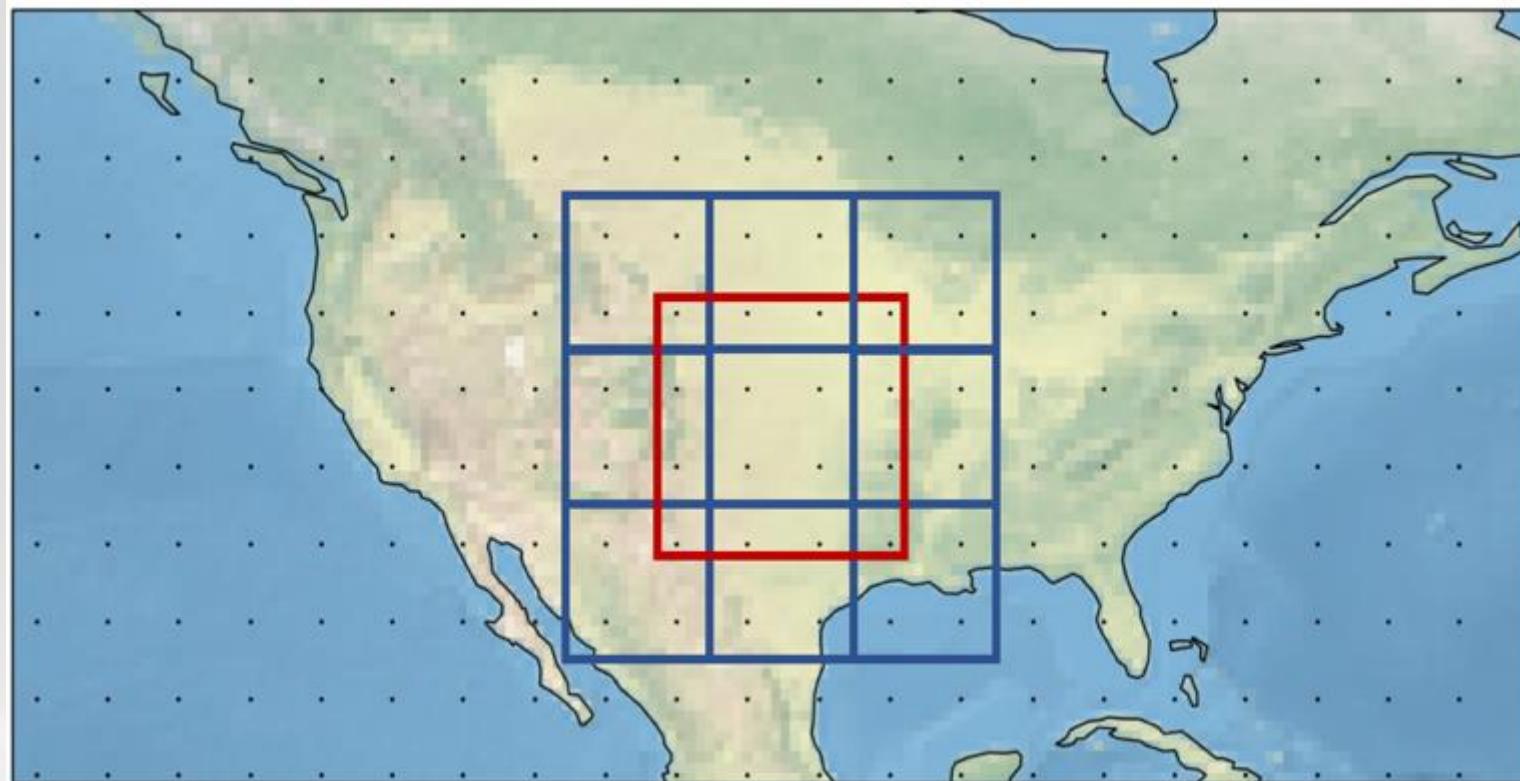
Parallel-Hybrid Training

local input $u(t)$, output $v(t+\Delta t)$



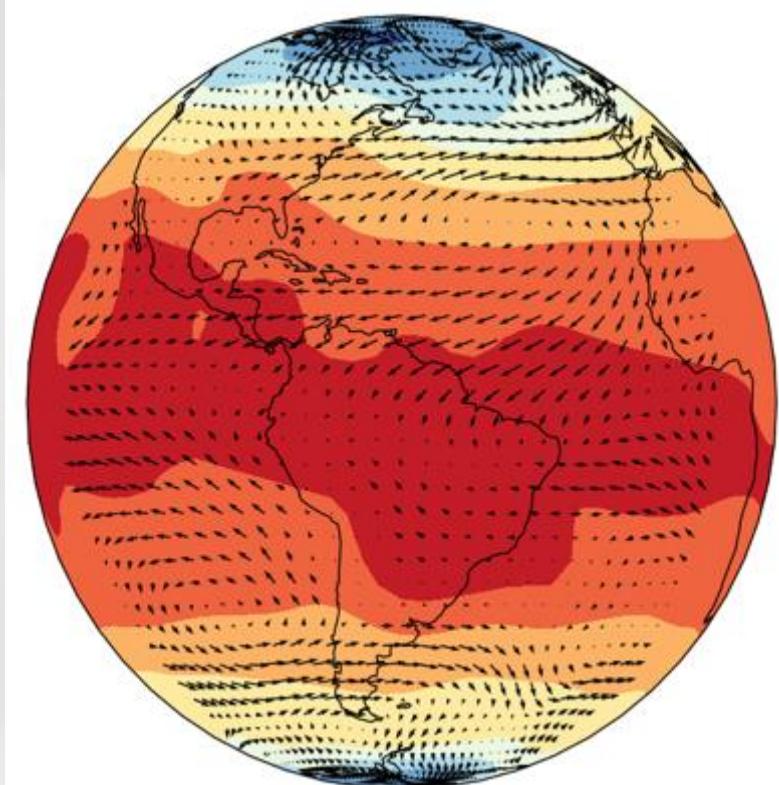
Parallel-Hybrid Post-Training

input from nearby outputs



SPEEDY

- Simplified Parameterizations, primitive Equation DYnamics Version 42 of the International Centre for Theoretical Physics (ICTP)
 - (Molteni 2003, Kucharski 2006)
- Equations
 - Primitive equations
 - Simplified but modern parameterization
- Configuration
 - 8 vertical layers
 - T30 ($\sim 300\text{km}$)
- Been used to test and develop new numerical weather prediction and data assimilation techniques



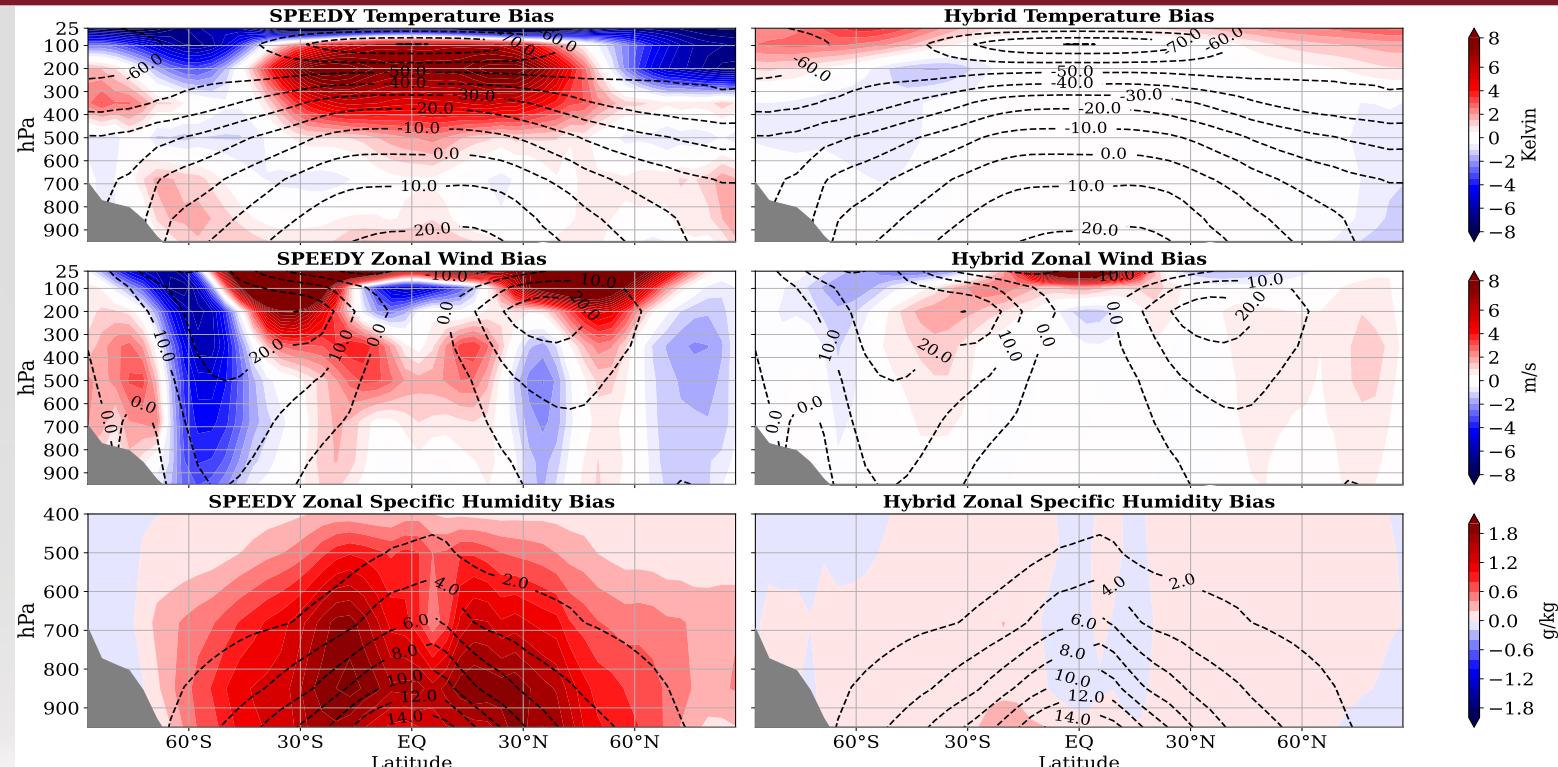
Training

- Regridded ERA-5 Reanalysis data to SPEEDY horizontal and vertical grid
- Used the 5 prognostic variables for SPEEDY
 - Temperature
 - 2 components of the wind
 - Specific Humidity
 - Surface Pressure
- 19 years of data from 1981-1999
- Training minimizes 6 hour forecast error

Climate Simulations

- Ran SPEEDY and the trained hybrid model from Jan 1, 2000 to Dec 31, 2010
 - 11-year free run using a hybrid model optimized for 6-hour forecasts
- Both simulations use climatological surface boundary conditions
- Let each simulation “spin-up” for a year and then calculated climate stats for the ten years from 2001 to 2010
 - Biases are measured by comparing each simulation to ERA 5 for the same period

Climate Simulations Results (Arcomano et al. 2022)



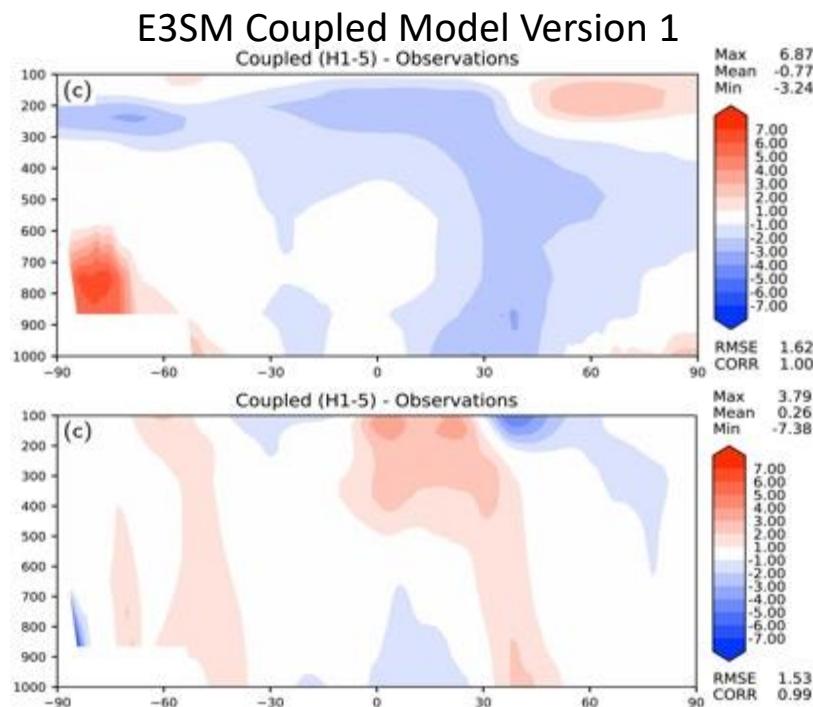
Lower bias indicates better simulation of the 2001-2010 climate represented by ERA5

Comparison with Coupled Ocean-Atmosphere Model

- Energy Exascale Earth System Model
 - Fully coupled Earth system model
 - Run on ~6000 CPU cores
- Our Hybrid Model
 - Climatological boundary conditions
 - Once trained can be run using desktop
 - 10 year simulation ~2 hours

Model	Temperature			
	Min Bias	Max Bias	Mean Bias	RMSE
E3SM	-3.24	6.87	-0.77	1.62
Hybrid	-0.92	2.38	0.19	0.49
SPEEDY	-6.56	7.11	0.83	3.22

Model	Zonal Wind			
	Min Bias	Max Bias	Mean Bias	RMSE
E3SM	-7.38	3.79	-0.26	1.53
Hybrid	-1.73	1.83	0.12	0.60
SPEEDY	-6.93	20.7	0.63	2.30



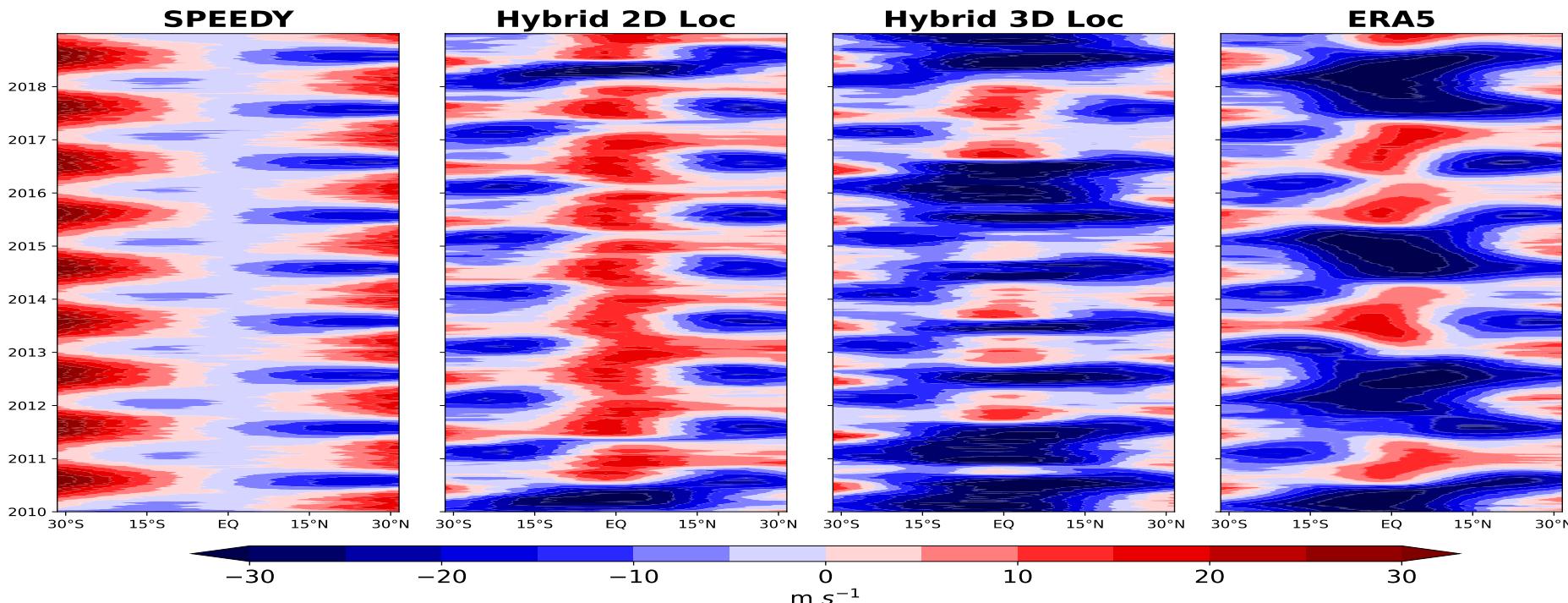
J Adv Model Earth Syst, Volume: 11, Issue: 7, Pages: 2089-2129, First published: 15 March 2019, DOI: (10.1029/2018MS001603)

Current Work

- Add vertical localization
 - Going from a 2-d grid of ML reservoirs to a 3-d grid
 - Improves year to year variability for the stratosphere
- Allow nonstationarity of boundary conditions
 - Two way coupling of the atmosphere to the ocean, sea ice, etc.
 - First approach: using ML-component to forecast sea surface temperatures (SSTs)

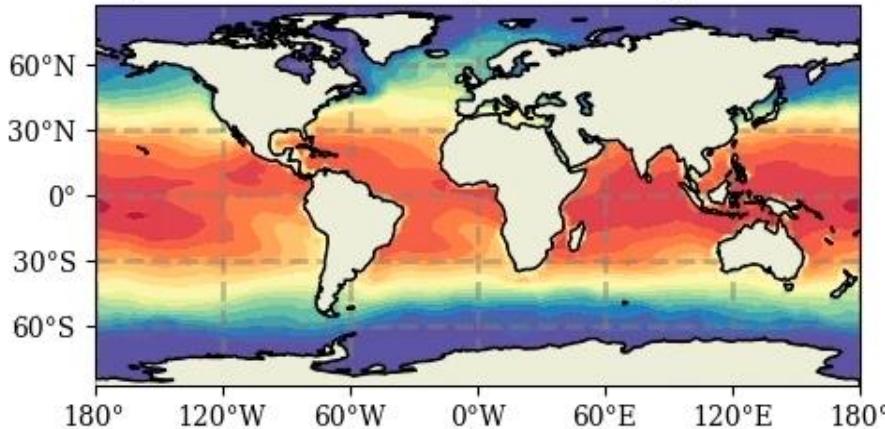
Vertical Localization: Preliminary Result

Equatorial Zonal Wind in the Stratosphere

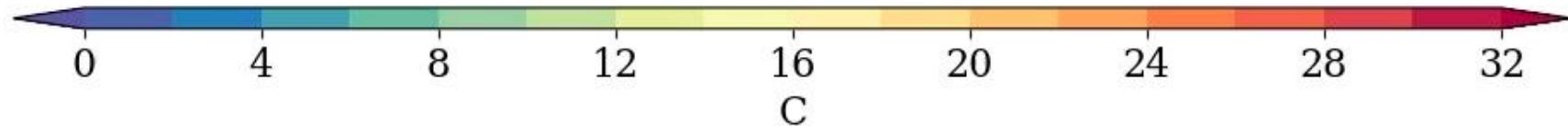
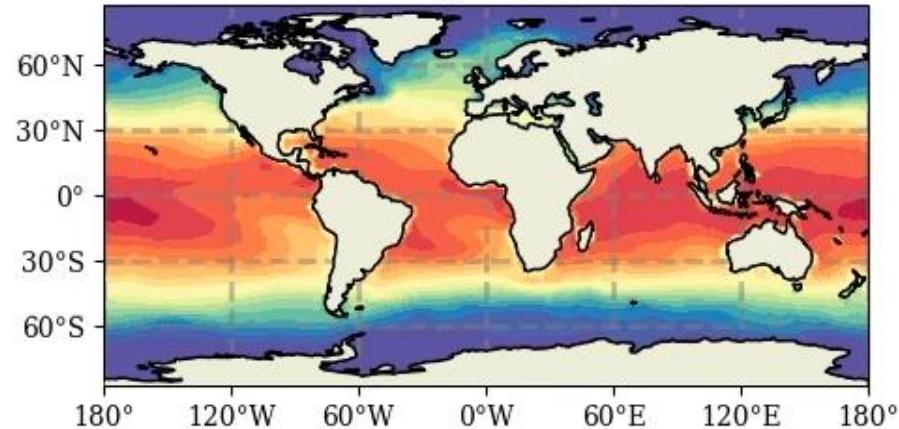


Ocean-Atmosphere Coupling: Preliminary Result

Hybrid Monthly Averaged SST



ERA Monthly Averaged SST



Conclusions

- Hybrid physics-ML atmospheric model allows fast simulation of climate scenarios
 - Could run large ensemble of simulations within a scenario
- Ongoing work to make the hybrid model more suitable for nonstationary scenarios
 - Vertical localization, slab ocean model in SPEEDY
- Ongoing research on tipping points and stability
 - Will transition from toy models to earth-system hybrid

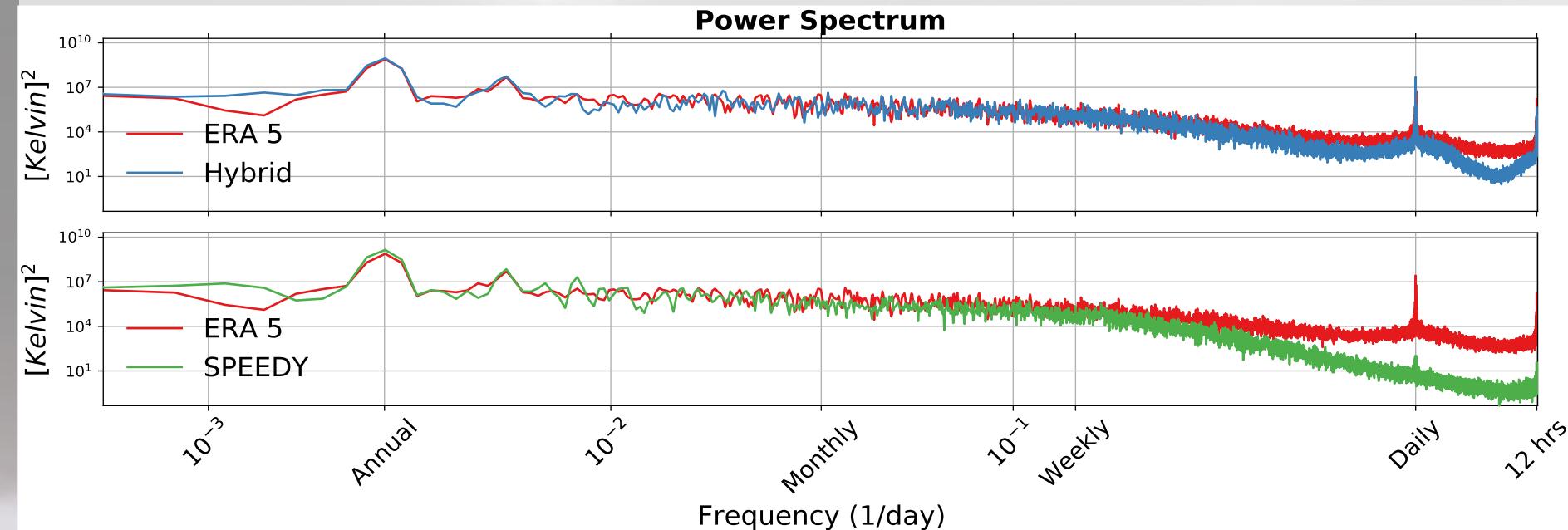


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References

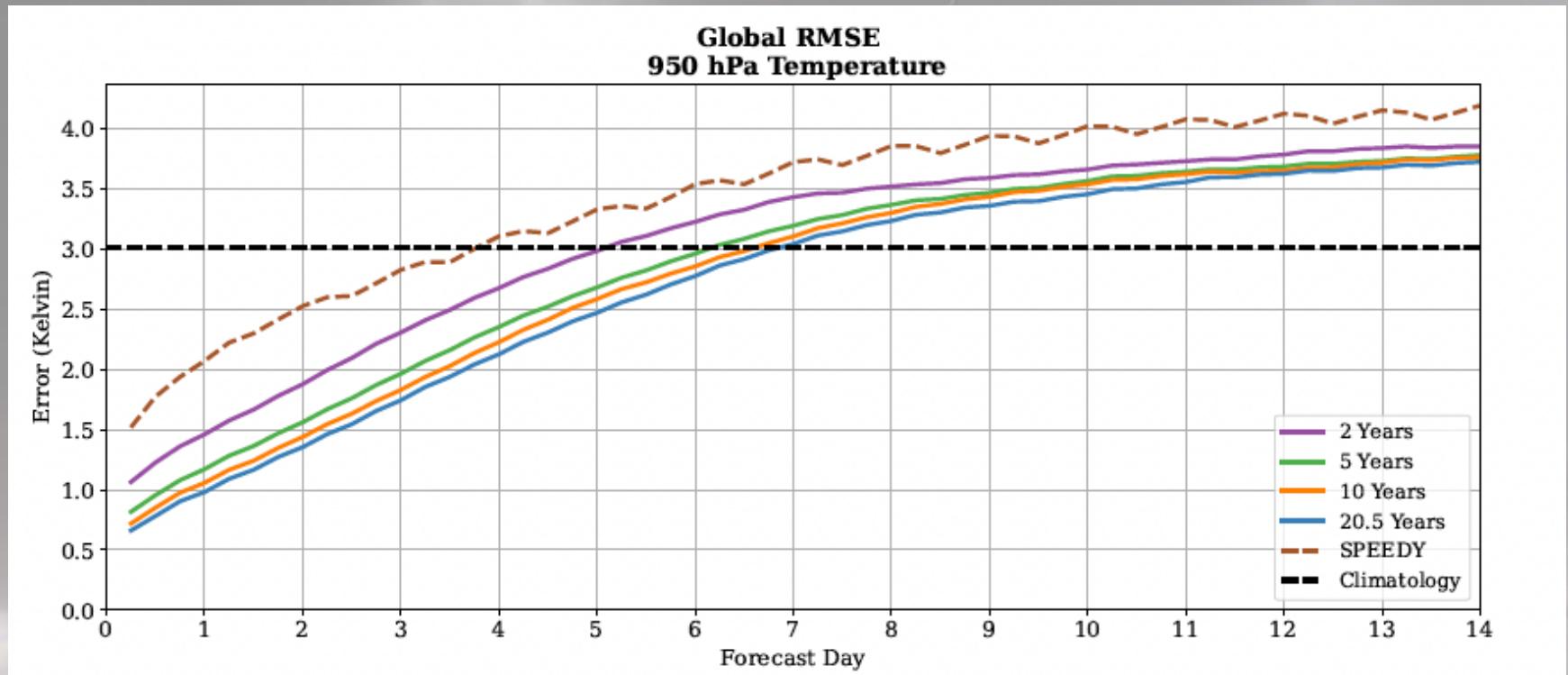
- 1.) Arcmano, T., Szunyogh, I., Wikner, A., Pathak, J., Hunt, B. R., & Ott, E. (2022). A hybrid approach to atmospheric modeling that combines machine learning with a physics-based numerical model. *Journal of Advances in Modeling Earth Systems*, **14**, e2021MS002712. <https://doi.org/10.1029/2021MS002712>
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- 3.) Molteni,F.,2003:Atmospheric simulations using a GCM with simplified physical parameterizations. I. Model climatology and variability in multi-decadal experiments. *Clim. Dyn.*, **20**, 175-191.
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Climate Dynamics

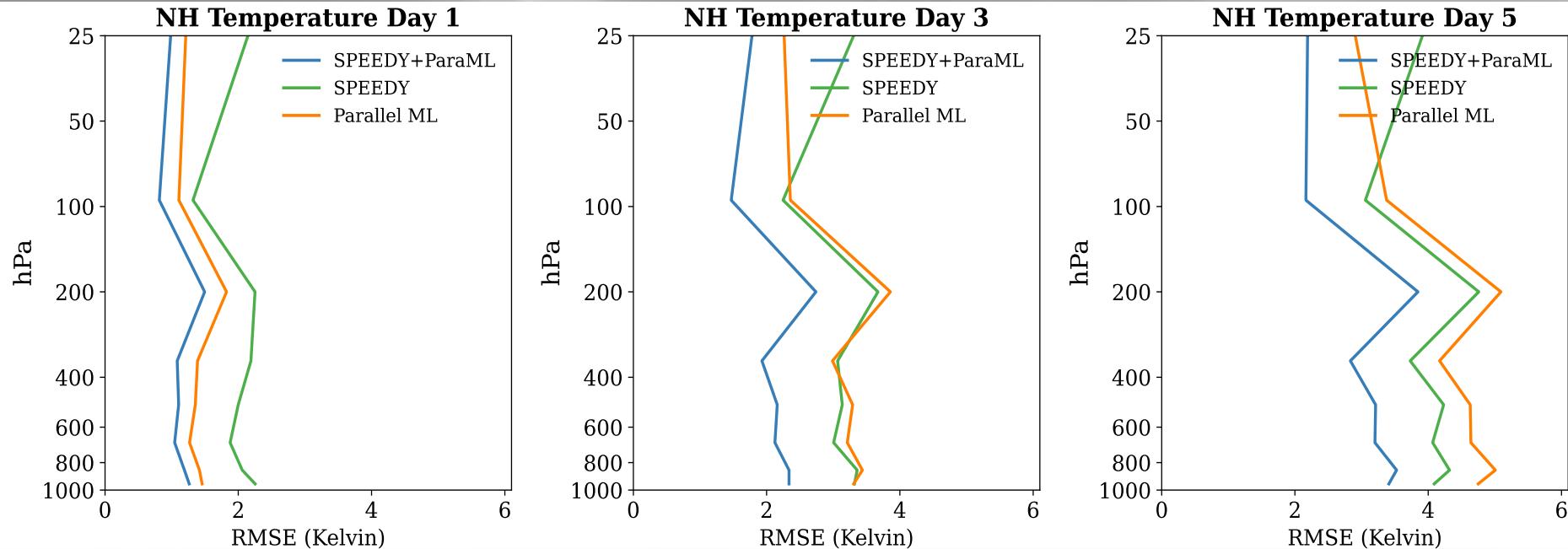


Significant improvement in short timescale variability

RMSE as a Function of Training Data



RMSE as a Function of Training Data



Ocean Atmosphere Coupling

