## Assignment #3

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2. Construct a truth table for the following:

a) 
$$xyz + x(yz)' + x'(y+z) + (xyz)'$$

b) 
$$(x + y')(x' + z')(y' + z')$$

- 6. Using DeMorgan's Law, write an expression for the complement of F if F(x,y,z) = xz'(xy + xz) + xy'(wz + y)
- 12. Show that xz = (x + y)(x+y')(x' + z)
- a) Using truth tables
- b) Using Boolean identities
- 13. Use any method to prove the following either True for False.

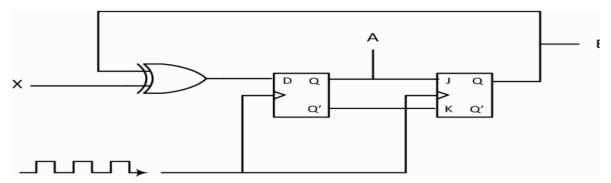
$$xz + x'y' + y'z' = xz + y'$$

- 16. Simplify the following functional expressions using Boolean algebra and its identities. List the identity used at each step.
- a) z(w + x)' + w'xz + wxyz' + wx'yz'
- b) y'(x'z' + xz) + z(x + y)'
- c) x(yz' + x)(y' + z)
- 23. The truth table for a Boolean expression is shown below. Write the Boolean expression in sum-of-products form.

| х | у | z | F |
|---|---|---|---|
| 0 | 0 | 0 | 1 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |

- 27. Given the function: F(x,y,z) = y(x'z + xz') + x(yz + yz')
- a) List the truth table for F.
- b) Draw the logic diagram using the original Boolean expression
- c) Simplify the expression using Boolean algebra and identities.
- d) List the truth table for your answer in Part c.
- e) Draw the logic diagram for the simplified expression in Part c.
- 30. Draw a half adder using only NAND gates. For an extra point solve (31. Draw a full adder using only NAND gates).

- 41. Draw circuits to implement the parity generator and parity checker shown in Tables 3.10 and 3.11, respectively.
- 46. Describe how each of the following circuits works and indicate typical inputs and outputs. Also provide a carefully labeled "black box" diagram for each.
- a) Decoder
- b) Multiplexer
- 51. Complete the truth table for the following sequential circuit:



- 59. A Mux-Not flip-flop (MN flip-flop) behaves as follows: If M = 1, the flip-flop complements the current state. If M = 0, the next state of the flip-flop is equal to the value of N.
- a) Derive the characteristic table for the flip-flop.
- b) Show how a JK flip-flop can be converted to a MN flip-flop by adding gate(s) and inverter(s).
- 63. Construct two parity checkers using the Moore machine for one and Mealy machine for the other
- 65. Using the convolutional code and Viterbi algorithm described in this chapter, assuming that the encoder and decoder always start in State 0, determine:
  - a) The output string generated for the input: 10010110.
  - b) In which state is the encoder after the sequence in (a) is read?
  - c) Which bit is in error in the string, 11 01 10 11 11 11 10? What is the probable value of the string?

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2. Write a simplified expression for the Boolean function defined by each of the following Kmaps.

| a) | x Y | <sup>'Z</sup> 00 | 01 | 11 | 10 |
|----|-----|------------------|----|----|----|
|    | 0   | 1                | 1  | 1  | 1  |
|    | 1   | 1                | o  | О  | О  |

| b) | yz<br>x | 00 | 01 | 11 | 10 |
|----|---------|----|----|----|----|
|    | o       | 1  | 0  | О  | 1  |
|    | 1       | 1  | 0  | 0  | О  |

| c) | x yz | 00 | 01 | 11 | 10 |
|----|------|----|----|----|----|
|    | 0    | 1  | 0  | 0  | 1  |
|    | 1    | 1  | 0  | 1  | 1  |

3. Create the Kmaps and then simplify for the following functions:

a) 
$$F(x,y,z) = x'y'z' + x'yz + x'yz'$$

b) 
$$F(x,y,z) = x'y'z' + x'yz' + xy'z' + xyz'$$

c) 
$$F(x,y,z) = y'z' + y'z + xyz'$$

5. Write a simplified expression for the Boolean function defined by each of the following Kmaps.

a)

| wx \ | /Z<br>00 | 01 | 11 | 10 |
|------|----------|----|----|----|
| 00   | 1        | 1  | 0  | 1  |
| 01   | 1        | 1  | О  | 1  |
| 11   | О        | О  | О  | О  |
| 10   | 1        | 1  | 1  | 1  |

| b) | wx | o0 | 01 | 11 | 10 |
|----|----|----|----|----|----|
| ۷, | 00 | 0  | 1  | 1  | 0  |
|    | 01 | 1  | 1  | 1  | 1  |
|    | 11 | 0  | О  | 1  | 1  |
|    | 10 | 0  | 1  | 1  | 0  |

|    | wx | 00 | 01 | 11 | 10 |
|----|----|----|----|----|----|
| c) | 00 | О  | 1  | О  | О  |
|    | 01 | 1  | 1  | 1  | 1  |
|    | 11 | 1  | 1  | 1  | 1  |
|    | 10 | 0  | 1  | 0  | 1  |

7. Create the Kmaps and then simplify for the following functions (leave in sum-of-products form):

- a) F(w,x,y,z) = w'x'y'z + w'x'yz' + w'xy'z + w'xyz + w'xyz' + wxy'z + wxyz + wx'y'z
- b) F(w,x,y,z) = w'x'y'z' + w'z + w'x'yz' + w'xy'z' + wx'y
- c) F(w,x,y,z) = w'x'y' + w'xz + wxz + wx'y'z

12. Find the minimized Boolean expression for the functions defined by the truth tables provided below.

a.

| λ | ( | у | z | F |
|---|---|---|---|---|
|   | ) | 0 | 0 | Х |
| C | ) | 0 | 1 | Х |
| 0 | ) | 1 | 0 | 1 |
| 0 | ) | 1 | 1 | 0 |
| 1 | L | 0 | 0 | 0 |
| 1 | L | 0 | 1 | 1 |
| 1 | L | 1 | 0 | 0 |
| 1 | L | 1 | 1 | 1 |
|   |   |   |   |   |

b.

| W | X | у | Ζ | F |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | Х |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | Х |
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | Х |
| 1 | 0 | 1 | 0 | Х |
| 1 | 0 | 1 | 1 | Х |
| 1 | 1 | 0 | 0 | Х |
| 1 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | Х |
| 1 | 1 | 1 | 1 | Х |
| 1 | 1 | 1 | 1 | × |