

# DIFFERENTIATION RULES

## **GENERAL FORMULAS**

1. 
$$\frac{d}{dr}(c) = 0$$

3. 
$$\frac{d}{dx}[f(x) + g(x)] = f'(x) + g'(x)$$

5. 
$$\frac{d}{dx}[f(x)g(x)] = f(x)g'(x) + g(x)f'(x)$$
 (Product Rule)

7. 
$$\frac{d}{dx} f(g(x)) = f'(g(x))g'(x)$$
 (Chain Rule)

2. 
$$\frac{d}{dx}[cf(x)] = cf'(x)$$

**4.** 
$$\frac{d}{dx}[f(x) - g(x)] = f'(x) - g'(x)$$

**6.** 
$$\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{g(x)f'(x) - f(x)g'(x)}{[g(x)]^2}$$
 (Quotient Rule)

**8.** 
$$\frac{d}{dx}(x^n) = nx^{n-1}$$
 (Power Rule)

# **EXPONENTIAL AND LOGARITHMIC FUNCTIONS**

$$9. \ \frac{d}{dx}(e^x) = e^x$$

11. 
$$\frac{d}{dx} \ln |x| = \frac{1}{x}$$

$$10. \ \frac{d}{dx}(a^x) = a^x \ln a$$

12. 
$$\frac{d}{dx}(\log_a x) = \frac{1}{x \ln a}$$

#### TRIGONOMETRIC FUNCTIONS

13. 
$$\frac{d}{dx}(\sin x) = \cos x$$

14. 
$$\frac{d}{dx}(\cos x) = -\sin x$$

15. 
$$\frac{d}{dx}(\tan x) = \sec^2 x$$

16. 
$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

17. 
$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

18. 
$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

## **INVERSE TRIGONOMETRIC FUNCTIONS**

19. 
$$\frac{d}{dx} (\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}$$

**20.** 
$$\frac{d}{dx}(\cos^{-1}x) = -\frac{1}{\sqrt{1-x^2}}$$

**21.** 
$$\frac{d}{dx}(\tan^{-1}x) = \frac{1}{1+x^2}$$

**22.** 
$$\frac{d}{dx}(\csc^{-1}x) = -\frac{1}{x\sqrt{x^2-1}}$$

**23.** 
$$\frac{d}{dx} (\sec^{-1} x) = \frac{1}{x\sqrt{x^2 - 1}}$$

**24.** 
$$\frac{d}{dx}(\cot^{-1}x) = -\frac{1}{1+x^2}$$

### HYPERBOLIC FUNCTIONS

**25.** 
$$\frac{d}{dx}(\sinh x) = \cosh x$$

$$26. \ \frac{d}{dx}(\cosh x) = \sinh x$$

27. 
$$\frac{d}{dx}(\tanh x) = \mathrm{sech}^2 x$$

**28.** 
$$\frac{d}{dx}(\operatorname{csch} x) = -\operatorname{csch} x \operatorname{coth} x$$

**29.** 
$$\frac{d}{dx}(\operatorname{sech} x) = -\operatorname{sech} x \tanh x$$

$$30. \frac{d}{dx} \left( \coth x \right) = -\operatorname{csch}^2 x$$

#### **INVERSE HYPERBOLIC FUNCTIONS**

31. 
$$\frac{d}{dx} \left( \sinh^{-1} x \right) = \frac{1}{\sqrt{1 + x^2}}$$

32. 
$$\frac{d}{dx} \left( \cosh^{-1} x \right) = \frac{1}{\sqrt{x^2 - 1}}$$

**33.** 
$$\frac{d}{dx} (\tanh^{-1}x) = \frac{1}{1 - x^2}$$

**34.** 
$$\frac{d}{dx} \left( \operatorname{csch}^{-1} x \right) = -\frac{1}{|x| \sqrt{x^2 + 1}}$$

**35.** 
$$\frac{d}{dx} (\operatorname{sech}^{-1} x) = -\frac{1}{x\sqrt{1-x^2}}$$

**36.** 
$$\frac{d}{dx} \left( \coth^{-1} x \right) = \frac{1}{1 - x^2}$$

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