

Social Efficiency

Is the competitive equilibrium the first best allocation?

hat - planner problem

start - equilibrium

Socila planner problem

Max utility such that $c+g < zf(1-l, kbar)$

$L(c, l, \lambda) = U(c, l) + \lambda(zf(1-l, kbar) - c - g)$

FOC(c) $U_c = \lambda$

FOC(l) $U_l = \lambda z_{f_n}(1-l, kbar)$

$MRS_{cl} = U_l/U_c = z_{f_n}(1-l, kbar)$

So $MRS_{cl} = MRT_{cl}$ in the static equilibrium.

Optimality of the household or firm means wage = MPL and tangency to budget constraint. For social planner, there is only the preferences (U) and feasibility / technology (PPF). So the optimality for the planner is always $MRS = MRT$. Not always does the competitive equilibrium hold this.

Wedges in the optimality conditions for households and firms cause social inefficiency

2 agent Economy

Given $\sum_i \alpha_i \leq 1, \forall i, \alpha_i \in [0, 1]$, optimize $\max_{c_i, l_i} \sum_i \alpha_i U(c_i, l_i)$, such that $\sum_i c_i + g \leq f\left(\sum_i (1 - l_i), \bar{k}\right)$ and where $\forall i, c_i \geq 0, l_i \in [0, 1]$.