02. Power rule for positive integers

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

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f$(x) = x^3$

$$\frac{d}{dx}(f) = \frac{d}{dx}(x^3) = 3x^{3-1} = 3x^2$$

f$(x) = x^5$

$$\frac{d}{dx}(f) = \frac{d}{dx}(x^5) = 5x^{5-1} = 5x^4$$

03. Constant Multiple Rule

$$\frac{df}{dv} = \frac{d}{dv}(cx^n) = c\frac{d}{dv}(nx^{n-1}) = c.x^{n-1}$$

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f(v) = $3x^4$

$$\frac{df}{dv} = \frac{d}{dv}(3x^4) = 3\frac{d}{dv}(4x^{4-1}) = 3(4x^3) = 12x^3$$

04. Sum rule

$$\frac{d}{dx}(u+v) = \frac{du}{dx} + \frac{dv}{dx}$$

$$f(x) = x^3 + 3x$$

$$\frac{d}{dx}(f) = \frac{d}{dx}(x^3 + 3x)$$

$$= \frac{d}{dx}(x^3) + \frac{d}{dx}(3x) = 3x^{3-1} + 3\frac{d}{dx}(x)$$

$$= 3x^2 + 3(1) = 3x^2 + 3$$

$$f(x) = x^4 + 12x$$

$$\frac{d}{dx}(f) = \frac{d}{dx}(x^4 + 12x)$$

$$= \frac{d}{dx}(x^4) + \frac{d}{dx}(12x) = 4x^{4-1} + 12\frac{d}{dx}(x)$$

$$= 4x^3 + 12(1) = 4x^3 + 12$$

Why $\frac{d}{dx}(x) = 1$?

$x = x^1$

$$\frac{d}{dx}(x) = x^{1-1} = x^0 = 1$$

$$f(x) = x^3 + \frac{4}{3}x^2 - 5x$$

$$\frac{d}{dx} = \frac{d}{dx}\left(x^3 + \frac{4}{3}x^2 - 5x\right)$$

$$= \frac{d}{dx}(x^3) + \frac{d}{dx}(4x^2) - \frac{d}{dx}(5x)$$

$$= 3x^{3-1} + 4\frac{d}{dx}(x^2) - \frac{d}{dx}(x)$$

$$= 3x^2 + 4(2x) - 5$$

$$= 3x^2 + 8x - 5$$

05. Product rule

$$\frac{d}{dx}(uv) = u\frac{dv}{dx} + v\frac{du}{dx}$$

$$f(x) = (x+1).(x-1)$$

$$\frac{df}{dx} = \frac{d}{dx}(x+1).(x-1)$$

$$= (x+1)\frac{d}{dx}(x-1) + (x-1)\frac{d}{dx}(x+1)$$

$$= (x+1)\left[\frac{d}{dx}(x) - \frac{d}{dx}(1)\right] + (x-1)\left[\frac{d}{dx}(x) + \frac{d}{dx}(1)\right]$$

$$= (x+1)[1-0] + (x-1)[1+0]$$

$$= (x+1)(1) + (x-1)(1)$$

$$= (x+1)(x-1) = 2x$$