

## 1.5 Handout

1. Suppose a new medication comes out with the following traits: a person who ingests a dose daily will retain one third of the concentration from the previous day, and one dose is enough to increase the concentration by 3 mg/L.
  - (a) Write down a discrete dynamical system that models the concentration of this drug in the bloodstream.
  
  
  
  
  
  
  
  
  
  
  - (b) What is the “experiment” in this discrete dynamical system?
  
  
  
  
  
  
  
  
  
  
2. A bacteria population doubles each day, but due to a harsh environment, a quarter of them also die off every day. Furthermore, around 200 million bacteria are lost each day due to being carried away by other means.
  - (a) Write down a discrete dynamical system modeling the population of the bacteria colony.
  
  
  
  
  
  
  
  
  
  
  - (b) What is the “experiment” in this discrete dynamical system?

3. Find the solution to the discrete dynamical system in problem 1 with an initial value of 0 mg/L of the drug. What is the long-term concentration level?

4. Find the solution to the discrete dynamical system in problem 2 with an initial value of 300 million bacteria. What does the population do in the long run?