

Quiz 1

Name: key

1. [6 pts] For the following functions, compute the average rate of change on the indicated intervals.

(a) $f(t) = e^t$ over the interval $[-2, -1]$. (b) $g(x) = \frac{1}{x}$ over the interval $[2, 4]$.

$$\begin{aligned}\frac{\Delta f}{\Delta t} &= \frac{f(-1) - f(-2)}{(-1) - (-2)} \\ &= \frac{e^{-1} - e^{-2}}{-1 + 2} = \frac{e^{-1} - e^{-2}}{+1} \\ &= e^{-1} - e^{-2} \\ &\approx 0.233\end{aligned}$$

$$\begin{aligned}\frac{\Delta g}{\Delta x} &= \frac{\frac{1}{4} - \frac{1}{2}}{4 - 2} \\ &= \frac{-1/4}{2} \\ &= -1/8\end{aligned}$$

2. [4 pts] Find the secant line for the function $r(t) = -3t^3 + 4$ over the interval $[0, 1]$.

$$y = mt + b$$

$$\begin{aligned}m &= \frac{\Delta r}{\Delta t} = \text{ARC}_{[0,1]} = \frac{r(1) - r(0)}{1 - 0} = \frac{(-3(1)^3 + 4) - (-3(0)^3 + 4)}{1} \\ &= \frac{-3 + 4 - 4}{1} \\ &= -3.\end{aligned}$$

$$\Rightarrow y = -3t + b.$$

$$\text{Use pt. } (0, 4) \Rightarrow b = 4.$$

$$y = -3t + 4$$