

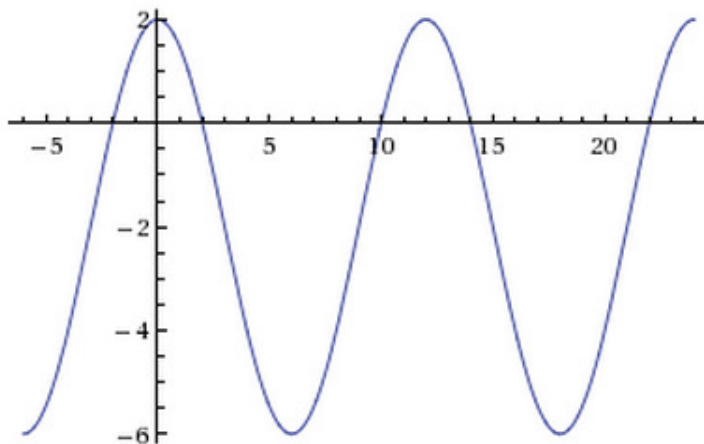
You will have at least 15 minutes to complete the quiz. No calculators.

1. [3 pts] The graph of a periodic function is given. Estimate its period, amplitude, and midline.

Period: 12

Amplitude: 4

Midline: -2



2. [5 pts] Let  $g(t) = 20 \cdot e^{0.001(t-1)}$ . Identify a parent function  $p(t)$ , write an equation describing  $g(t)$  as a transformation of  $p(t)$ , and identify the transformations that give  $g(t)$ .

Parent:  $p(t) = e^t$ .

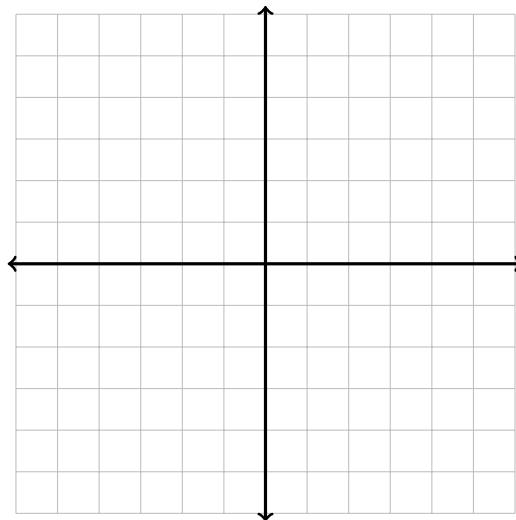
$g(t) = 20p(0.001(t-1))$

First stretch v. by 20, then stretch h. by 1000, then shift right 1.

3. [4 pts] Suppose  $(3, 0)$  is a point on the graph of  $f(t)$ . Find a point on the graph of  $\frac{1}{2}f(-\frac{1}{2}t) + 1$ .  
 $(3, 0) \rightarrow (3, 0) \rightarrow (3, 1) \rightarrow (-6, 1)$ .

4. [8 pts] Suppose that a function  $f$  is periodic with period 4, and moreover it is given by the equation  $f(x) = \sqrt{x}$  for  $0 \leq x < 4$ .

(a) Sketch a graph of  $f$  as accurately as possible. Include at least three periods.



(b) Find  $f(-2)$ . (You do not need to give me a decimal answer.)

$f(-2) = f(2)$  (by periodicity), so  $f(-2) = \sqrt{2}$ .

(c) Compute  $f(4)$ .

By periodicity,  $f(4) = f(0) = \sqrt{0} = 0$ .

(d) Find all solutions to the equation  $f(x) = 1$ .

In the fundamental domain, we solve  $\sqrt{x} = 1$ . This gives  $x = 1$ , which is in the fundamental domain. All other solutions are  $x = 1 + 4n$  for any whole number  $n$ .