

You will have at least 20 minutes to complete the quiz. You may use a calculator for computations, but your process must still be evident in the work you show.

1. [3 pts] Suppose the vector \vec{v} points 20° to the *left* of the positive y -axis. Find the components of \vec{v} .

$$\|\vec{v}\| = 7$$



$$\begin{aligned}\vec{v} &= (-7 \cdot \sin(20^\circ), 7 \cos(20^\circ)) \\ &= (-2.394, 6.578)\end{aligned}$$

2. [2 pts] If $\|\vec{u}\| = 20$, $\|\vec{v}\| = 10$, and the angle between \vec{u} and \vec{v} is 45° , what is $\vec{u} \cdot \vec{v}$?

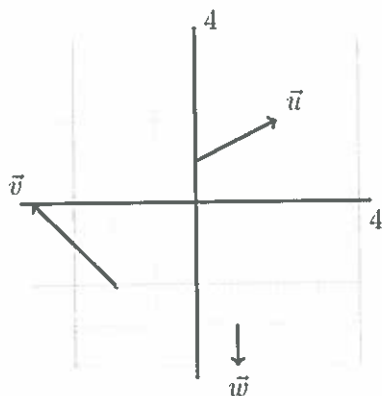
$$\begin{aligned}\vec{u} \cdot \vec{v} &= \|\vec{u}\| \cdot \|\vec{v}\| \cdot \cos(45^\circ) \\ &= (20)(10) \cdot \frac{\sqrt{2}}{2} \\ &= 100\sqrt{2} = \boxed{141.42}\end{aligned}$$

3. [5 pts] Find a vector that is perpendicular to the vector $\vec{v} = 3\vec{i} + 4\vec{j}$, and prove that it is perpendicular.

One example: $\vec{u} = (-4)\vec{i} + 3\vec{j}$.

Pf: $\vec{u} \cdot \vec{v} = (-4)(3) + (3)(4) = -12 + 12 = \boxed{0} \checkmark$

4. [10 pts] Suppose the vectors \vec{u} , \vec{v} , and \vec{w} are shown below.



- (a) Write down the components of \vec{u} , \vec{v} , and \vec{w} .

$$\vec{u} = (2, 1)$$

$$\vec{v} = (-2, 2)$$

$$\vec{w} = (0, -1)$$

- (b) Find $2\vec{u} + 3\vec{w}$.

$$2\vec{u} + 3\vec{w} = (4 + 0, 2 - 3) = (4, -1)$$

- (a) What is $\vec{u} \cdot \vec{w}$?

$$\vec{u} \cdot \vec{w} = (2)(0) + (1)(-1) = -1$$

- (b) If \vec{u} and \vec{v} are placed tail-to-tail, what is the angle that they make?

$$\|\vec{u}\| = \sqrt{4 + 1} = \sqrt{5}$$

$$\|\vec{v}\| = \sqrt{4 + 4} = \sqrt{8} = 2\sqrt{2}$$

$$\vec{u} \cdot \vec{v} = (2)(-2) + (1)(2) = -4 + 2 = -2$$

$$\begin{aligned} 2\sqrt{2} \cdot \sqrt{5} \cos \theta &= -2 \\ \cos \theta &= \frac{-2}{2\sqrt{2}\sqrt{5}} = -\frac{1}{\sqrt{10}} \end{aligned} \quad \left\{ \begin{aligned} \theta &= \arccos\left(-\frac{1}{\sqrt{10}}\right) = 1.89 \text{ rad} \\ &= 108.4^\circ \end{aligned} \right.$$

- (c) Are any of the vectors \vec{u} , \vec{v} , \vec{w} perpendicular? Explain.

$$\vec{u} \cdot \vec{w} = -1$$

$$\vec{u} \cdot \vec{v} = -2$$

$$\vec{v} \cdot \vec{w} = (-2)(0) + (2)(-1) = -2$$

no, none of them dot to 0, so they can't be perpendicular.