

HVAC System Efficiency Calculations

Performance Analysis & Compliance Verification - ASHRAE Standards

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1. Chiller Performance Calculations

Coefficient of Performance (COP)

$$COP = Q_{cooling} / W_{electrical}$$

Where:

- $Q_{cooling}$ = Cooling capacity (kW)
- $W_{electrical}$ = Electrical power input (kW)

Magnetic Bearing Centrifugal Chiller Analysis:

Load Condition	Cooling Output (kW)	Power Input (kW)	COP	Efficiency (%)
100% Load	1,760	284	6.20	620%
75% Load	1,320	169	7.81	781%
50% Load	880	99	8.89	889%
25% Load	440	62	7.10	710%

IPLV Calculation (Integrated Part Load Value):

$$IPLV = 0.01(6.20) + 0.42(7.81) + 0.45(8.89) + 0.12(7.10)$$

$$IPLV = 0.062 + 3.280 + 4.001 + 0.852 = 8.195$$

Full Load COP: 6.20 | IPLV: 8.20
ASHRAE 90.1 Minimum: COP \geq 5.5, IPLV \geq 7.0
Status: COMPLIANT ✓

2. Heat Pump Performance

Heating Seasonal Performance Factor (HSPF)

$\text{HSPF} = \text{Total Heating Output (Btu)} / \text{Total Electrical Input (Wh)}$

$\text{COP}_{\text{heating}} = \text{Heat Output (kW)} / \text{Power Input (kW)}$

Variable Refrigerant Flow (VRF) System:

Heating Mode Performance:

- Heating Capacity: 45 kW @ 7°C outdoor
- Power Input: 12.8 kW
- $\text{COP}_{\text{heating}} = 45 \div 12.8 = 3.52$
- Seasonal Average COP: 3.85

HSPF Calculation:

- Annual Heating Load: 125,000 kWh
- Annual Energy Input: 32,468 kWh
- $\text{HSPF} = (125,000 \times 3,412) \div (32,468 \times 1,000)$
- $\text{HSPF} = 426,500,000 \div 32,468,000 = 13.1 \text{ Btu/Wh}$

Calculated HSPF: 13.1 Btu/Wh

ENERGY STAR Requirement: $\geq 10.0 \text{ Btu/Wh}$

Status: EXCEEDS STANDARD ✓

3. Air Handling Unit Efficiency

Fan Efficiency & Specific Fan Power

$$\text{Fan Efficiency} = (\text{Airflow} \times \text{Pressure}) / (\text{Power} \times 1000)$$

$$\text{SFP} = \text{Fan Power (W)} / \text{Airflow (L/s)}$$

Variable Air Volume (VAV) System Analysis:

Parameter	Design Value	Measured Value	Efficiency
Airflow Rate	15,000 CFM	14,850 CFM	99.0%
Static Pressure	2.5 in. w.g.	2.3 in. w.g.	108.7%
Fan Power	25 kW	22.1 kW	113.1%
Motor Efficiency	94.5%	95.2%	100.7%

Fan Efficiency Calculation:

- Airflow: 14,850 CFM = 7,008 L/s
- Pressure: 2.3 in. w.g. = 573 Pa
- Fan Efficiency = $(7,008 \times 573) / (22,100 \times 1000)$
- Fan Efficiency = $4,015,584 / 22,100,000 = 0.182 = 18.2\%$

Specific Fan Power:

$$\text{SFP} = 22,100 \text{ W} \div 7,008 \text{ L/s} = 3.15 \text{ W/(L/s)}$$

ASHRAE 90.1 Limit: $\leq 4.0 \text{ W/(L/s)}$

Fan Efficiency: 18.2% | SFP: 3.15 W/(L/s)
Both parameters within acceptable limits ✓

4. Heat Recovery Systems

Heat Recovery Effectiveness

$$\text{Sensible Effectiveness} = (T_{\text{supply}} - T_{\text{outdoor}}) / (T_{\text{exhaust}} - T_{\text{outdoor}})$$

$$\text{Latent Effectiveness} = (W_{\text{supply}} - W_{\text{outdoor}}) / (W_{\text{exhaust}} - W_{\text{outdoor}})$$

Energy Recovery Ventilator (ERV) Performance:

Outdoor Air

-5°C

35% RH

Exhaust Air

22°C

45% RH

Supply Air

16°C

42% RH

Return Air

1°C

38% RH

Sensible Effectiveness:

$$\eta_{\text{sensible}} = (16 - (-5)) / (22 - (-5))$$

$$\eta_{\text{sensible}} = 21 / 27 = 0.778 = 77.8\%$$

Latent Effectiveness (using humidity ratios):

$$\bullet \quad W_{\text{outdoor}} = 1.2 \text{ g/kg}, \quad W_{\text{exhaust}} = 7.8 \text{ g/kg}, \quad W_{\text{supply}} = 6.9 \text{ g/kg}$$

$$\eta_{\text{latent}} = (6.9 - 1.2) / (7.8 - 1.2) = 5.7 / 6.6 = 0.864 = 86.4\%$$

Sensible Effectiveness: 77.8%

Latent Effectiveness: 86.4%

ASHRAE 90.1 Minimum: ≥ 50% sensible

Status: EXCEEDS REQUIREMENTS ✓

5. Duct System Performance

Duct Leakage & Pressure Loss

$$\text{Duct Leakage Rate} = Q_{\text{leak}} / Q_{\text{total}} \times 100\%$$

$$\text{Pressure Loss} = f \times (L/D) \times (\rho V^2/2)$$

Where: f = friction factor, L = length, D = diameter, ρ = air density, V = velocity

Duct System Leakage Test Results:

Test Section	Test Pressure (Pa)	Measured Leakage (CFM)	System Airflow (CFM)	Leakage Rate (%)
Supply Ductwork	250	420	12,000	3.5%
Return Ductwork	125	180	11,500	1.6%
Total System	-	600	12,000	5.0%

Pressure Loss Calculation - Main Supply Duct:

- Duct: 24" diameter, 150 ft length
- Airflow: 8,000 CFM, Velocity: 1,592 FPM
- Friction factor: 0.018
- Pressure Loss = $0.018 \times (150/2) \times (0.075 \times 1592^2/2)$
- Pressure Loss = $1.35 \times 9,520 = 0.32$ in. w.g.

Total Duct Leakage: 5.0%

ASHRAE 90.1 Limit: ≤ 6.0%

Pressure Loss: 0.32 in. w.g. (within design)

Status: COMPLIANT ✓

6. System Integration & Controls

Demand Control Ventilation (DCV)

$$\text{Required Ventilation} = \text{People} \times R_p + \text{Area} \times R_a$$

$$\text{CO}_2\text{-based Control: OA\%} = (C_{\text{space}} - C_{\text{outdoor}}) / (C_{\text{exhaust}} - C_{\text{outdoor}})$$

Office Space Ventilation Control:

ASHRAE 62.1 Requirements:

- Occupancy: 150 people
- Floor Area: 15,000 ft²
- People component: $150 \times 5 \text{ CFM/person} = 750 \text{ CFM}$
- Area component: $15,000 \times 0.06 \text{ CFM/ft}^2 = 900 \text{ CFM}$
- Total Required: $750 + 900 = 1,650 \text{ CFM}$

CO₂-Based DCV Calculation:

- Outdoor CO₂: 400 ppm
- Space CO₂ setpoint: 1,000 ppm
- Exhaust CO₂ (design): 1,200 ppm
- Required OA% = $(1,000 - 400) / (1,200 - 400) = 75\%$
- At 50% occupancy: OA% = $(800 - 400) / (1,200 - 400) = 50\%$

Minimum Ventilation: 1,650 CFM

DCV Energy Savings: ~35% during low occupancy

Annual Energy Reduction: 45,000 kWh