STA303 Summer 2018 Midterm

July 25th, 2018

irst Name: SoluTions.
ast Name:
tudent Number:
his exam booklet contains 15 pages, and 40 multiple choice questions. Write all answers on the attached
cantron sheet, in pencil. Nothing written in the exam booklet will be marked. You must hand in your exam
ooklet. Aids permitted: non-programmable calculator.

- 1. Which of the following statements regarding Analysis of Variance (ANOVA) is correct?
- ANOVA analyzes differences in variances between several normally distributed populations
- (b) ANOVA analyzes differences in means between several normally distributed populations ANOVA analyzes differences in variances between several arbitrarily distributed populations
- d. ANOVA analyzes differences in means between several arbitrarily distributed populations
- Which of the following statements regarding Analysis of Variance (ANOVA) is correct?
- a. ANOVA is a linear model $y = X\beta + \epsilon$, where the columns of X can be anything
- ANOVA is a non-parametric regression model $y=X\beta+\epsilon$, where the columns of X can be
- ANOVA is a linear model $y = X\beta + \epsilon$, where the columns of X are all continuous
- ANOVA is a linear model $y = X\beta + \epsilon$, where the columns of X are all indicator variables
- Which of the following statements regarding Analysis of Variance (ANOVA) is correct?
- a.) ANOVA assumes that the population variances of all the groups are equal ANOVA assumes that the population means of all the groups are equal
- ANOVA assumes that the sample variances of all the groups are equal
- d. ANOVA assumes that the sample means of all the groups are equal
- Which of the following is NOT a model assumption when performing an ANOVA, assuming all the groups have an equal number of observations?
- The population variances of all the groups are equal
- The observations are mutually independent within and across groups
- The observations are normally distributed
- The total sum of squares equals the sum of the within-group sum of squares (error, SSE) and the between-group sum of squares (model SSM), SST = SSM + SSE
- ĊŢ Recall the cell means coding method of writing a linear model with one discrete predictor variable: $\beta = (\alpha_1, ... \alpha_K)$, what is the cross-product matrix $X^T X^T I_m$ is the m-dimensional identity matrix. $y_{ij} = \alpha_i + \epsilon_{ij}$, $i = 1 \dots m, j = 1 \dots n$. Writing this as a linear model in matrix form $\mathbf{y} = X\beta + \epsilon$ with

(a.)
$$X^TX = nI_m$$

b. $X^TX = (1/n)I_m$
 $X^TX = (1/n)I_m$

- c. $X^TX = I_m$
- d. It is not possible to say
- Recall effects coding, in contrast to cell-means coding: $y_{ij} = \mu + \alpha_i + \epsilon_{ij}$, with $\alpha_1 = 0$. The two study to compare a new treatment to a control group, with the aim of making a statement about the are interpreted in the context of the problem. Which coding would be preferable if we are designing a codings give the same estimated means; they differ in the manner in which their regression coefficients difference in means between the treatment and control group?
- Effects coding
- Cell means coding
- Not possible to say

- Which coding is used by the linear model underlying the standard ANOVA table?
- a. Effects coding
- b. Cell means coding
- (c.) Not possible to say

rubber-like stuff that sewer pipes are made of (look under your kitchen sink when you get home). For each of the plastic PVC, 3 operators used 8 different devices called resin railcars to produce PVC, that hard of the 24 combinations, two samples were produced. Here is a glimpse of the data: Recall the pvc data discussed in lecture: Data from an experiment to study factors affecting the production

```
##
                                                                                                                                       ## Variables:
                                                                                                                                                 ## Observations: 48
                                                                                                       ## $ resin
                             Particle Size
                                                                                                                            $ psize
                                    30.0
                                                   32.5
                                                                 35.0
                                                                                 37.5
                     27.5
                                                                                                                operator <fct> 1, 1, 1, 1, 1, 1,
                                                                                        PVC Pairwise Boxplots
                                                                                                                                        ω
                                                                                                     <fct> 1, 1,
                                                                                                                            <dbl> 36.2, 36.3,
                                                                                                    2, 2, 3,
Operator
                                                                                                                            35.3,
                                                                                                       ω
                                                                                                                            35.0,
                                                                                                       ດ
                                                                                                                            30.8,
           ω
                                                                                                       Ω.
                                                                                                       6,
6,
                                                                                                                            30.6,
                                                                                                                            29.8,
                                                                                                                            29.6,
                                                                                                               2, 2, \ldots
                                                                                                                          32.0,...
```

For the pvc data above, which of the following ggplot commands generates the pairwise boxplots shown in the figure entitled "PVC Pairwise Boxplots"? (note: code shown does not include the code that sets the title, axis labels, or theme of the plot).

b. pvc %>% ggplot(aes(x = resin,y = psize)) + geom_boxplot() $\bigcup_{pvc} \%\%$ ggplot(aes(x = operator,y = psize)) + geom_boxplot()

c. pvc %>% ggplot(aes(y = psize)) + geom_boxplot(x = operator)

d. pvc %>% ggplot(aes(y = psize,group = operator)) + geom_boxplot()

- Consider the pvc data and the "PVC Pairwise Boxplots" plot. We wish to run an ANOVA to assess the assumption of equality of variances across groups, and why? differences in particle size for levels of operator. Does the plot contain enough information to assess
- a. Yes- the only way to assess this assumption is by looking at this type of plot
- b. No- it is impossible to assess this assumption without the aid of a statistical test
- (c) Yes- it is reasonable to assess this assumption by looking at this type of plot No- this type of plot does not contain information about the variances of the groups
- 10. Consider the pvc data and the "PVC Pairwise Boxplots" plot. We wish to run an ANOVA to assess assumption of normality of the data, and why? differences in particle size for levels of operator. Based on this plot, are you comfortable with the
- a. Yes- we can tell that the distribution of each group is symmetric, and therefore normal, by looking
- Yes- the groups all look similar, which indicates normality
- No- the range of the y-axis is not -2 to 2, so the data is not normally distributed
- exist better diagnostic methods for assessing normality that are readily available, so we should No- while we can sort of tell the distribution of the data looks normal based on this plot, there

We fit an ANOVA to these data, obtaining the below ANOVA table:

Residuals	operator	
(4)	(1)	Df
333.8	20.7	Sum of Squares
(5)	(2)	Mean Square
	(3)	ਸ਼
	(3) .258	p

11. What is the total sum of squares, $SST = \sum_{i=1}^{3} \sum_{j=1}^{16} (y_{ij} - \bar{y}_{..})^2$

S33.7 + 20.7 = 354.5

(a.) 354.5

d. 313.1

12. What value should go in the cell labelled by (1)?

d. 48

13. What value should go in the cell labelled by (2)?

20.7

(a.)10.35

c. 0.062

d. 0.058

- 14. What value should go in the cell labelled by (3)?
- a. 1.4
- b. -1.4
- c. 16.13
- d. 0.742
- 15. What value should go in the cell labelled by (4)?

3(16-1)=45

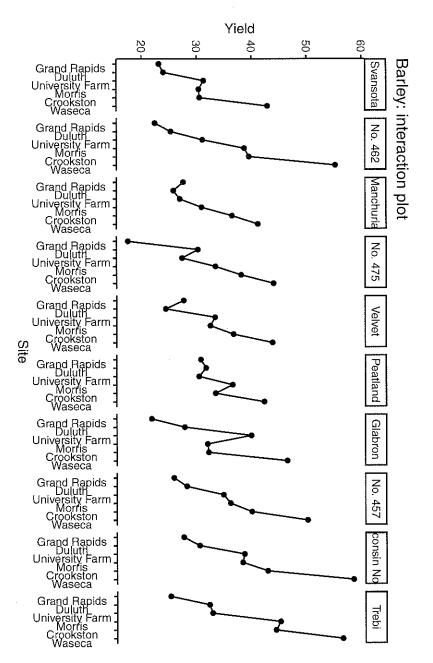
- © 45

d. 48

- 16. What value should go in the cell labelled by (5)?
- (a) 7.418
- 333.8/45 = 7.41B
- c. 16.13

b. 6.954

- d. 47.00
- 17. Denote the population group means μ_1, μ_2, μ_3 and the population group standard deviations $\sigma_1, \sigma_2, \sigma_3$. What null hypothesis is the F statistic testing?
- (a) $H_0: \mu_1 = \mu_2 = \mu_3$
- b. $H_0: \mu_1 = \mu_2 = \mu_3 = 0$
- c. $H_0: \sigma_1 = \sigma_2 = \sigma_3$
- d. $H_0: \mu_1 = \mu_2 = \mu_3$ and $\sigma_1 = \sigma_2 = \sigma_3$
- 18. Using the usual 0.05 significance level, what do you conclude?
- These data provide evidence to suggest that the population means of the groups are equal.
- These data provide evidence to suggest that the population means of the groups are not equal.
- (d) These data fail to provide evidence to suggest that the population means of the groups are not These data fail to provide evidence to suggest that the population means of the groups are equal. equal.
- relationship between mean yield and site is the same for each variety. to assess whether the yield differs across sites, whether the yield differs across varieties, and whether the Consider the following experiment: yield of barley per acre was measured for 10 varieties at 6 sites. We wish
- ## Observations: 120
- ## Variables: 4
- ## \$ yield <dbl> 27.00000, 48.86667, 27.43334, 39.93333, 32.96667, 28.9...
- variety <fct> Manchuria, Manchuria, Manchuria, Manchuria, Manchuria,...
- year <fct> 1931, 1931, 1931, 1931, 1931, 1931, 1931, 1931, ...
- site <fct> University Farm, Waseca, Morris, Crookston, Grand Rapi...



19. Consider the plot entitled "Barley: interaction plot". cannot be reasonably assessed by this plot? Which of the following aspects of these data

- a.)Normality of the data
- b. The marginal mean of yield across values of site
- The marginal mean of yield across values of variety
- d. How the relationship between mean of yield and site changes across levels of variety
- 20. Which is a reasonable claim to make about the mean of yield for Grand Rapids?
- The mean yield for Grand Rapids is lower than all the other sites, for every variety of barley barley The mean yield for Grand Rapids is lower than all the other sites, averaged across varieties of
- 6 The mean yield for Grand Rapids is higher than all the other sites, for every variety of barley
- The mean yield for Grand barley Rapids is higher than all the other sites, averaged across of

- 21.Which of the following four statements is the most reasonable claim to make about the mean yield across sites, based on this plot?
- The mean yield appears to differ across sites; a formal significance test of the existence of the difference is due to random chance interaction of yield and site would be an appropriate procedure to help decide whether this
- would be an appropriate procedure to help decide whether this difference is due to random chance of barley; a formal significance test of the existence of the interaction between variety and site The relationship between the mean of yield and site appears to be different for different varieties
- Ö The mean yield does not appear to differ across sites; a formal significance test is not necessary or desirable in this context
- This plot does not give information about the manner in which mean yield differs across sites

satisfied. Consider the below linear model. For what follows, you can assume any necessary model assumptions are

```
##
                                                                                                                                                           ##
                                                                                                                                                                                              ##
                                                                                                                                                                                                                      ##
                                                                                                                                                                                                                                              ##
varietyTrebi
           varietyWisconsin No.
                       varietyNo. 457
                                               varietyPeatland
                                                          varietyVelvet
                                                                      varietyNo. 475
                                                                                  varietyManchuria
                                                                                              varietyNo. 462
                                                                                                          siteWaseca
                                                                                                                     siteCrookston
                                                                                                                                  siteMorris
                                                                                                                                              siteUniversity Farm
                                                                                                                                                           siteDuluth
                                  varietyGlabron
                                                                                                                                                                                                                   -12.7439
                                                                                                                                                                                                                                              Residuals:
                                                                                                                                                                                                                                                                                  Call:
                                                                                                                                                                                              Coefficients:
                                                                                                                                                                                                                                                                     lm(formula =
                                                                                                                                                                      (Intercept)
                                                                                                                                                                                                                                  Min
                                                                                                                                                                                                                      -5.3051
                                                                                                                                                                                                                                                                     yield ~
                                                                                                                                                                                                                                  4
                                                                                                                                                                                                                      -0.0758
                                                                                                                                                                                                                                  Median
            38
                                                                                                                                                                                                                                                                     site + variety, data =
                                                                                                                                                                                 Estimate
                                                                                                          23.177
                                                                                                                      12.488
                                                                                                                                                                      20.889
                                                                                                                                  10.468
9.022
           9.017
                       5.469
                                               3.803
                                                                       1.383
                                                                                  1.086
                                                                                              5.000
                                                                                                                                             7.735
                                                                                                                                                          3.065
                                   2.964
                                                           2.683
                                                                                                                                                                                                                      5.1164
                                                                                                                                                                                   Std.
                                                                                                                                                                                                                                 30
                                                                                                                                                                                                                      16.7011
2.824
           2.824
                       2.824
                                   2.824
                                               2.824
                                                          2.824
                                                                      2.824
                                                                                  2.824
                                                                                              2.824
                                                                                                         2.187
                                                                                                                      2.187
                                                                                                                                  2.187
                                                                                                                                              2.187
                                                                                                                                                          2.187
                                                                                                                                                                      2.445
                                                                                                                                                                                 Error
                                                                                                                                                                                                                                 Max
                                                                                                                                                                                                                                                                     barley)
                                                                                                                                                                                   ۲t
                                                                                                          10.596
           3.193
                                   1.050
                                               1.347
                                                                                   0.385
                                                                                              1.771
                                                                                                                      5.709
                                                                                                                                 4.786
                                                                                                                                                          1.401
                                                                                                                                                                      8.542
                                                                                                                                                                                  value
3.195 0.001846
                                                          0.950 0.344164
                                                                      0.490 0.625238
                                                                                                                                              3.536
                                  0.296307
                                               0.180980
                                                                                  0.701291
                                                                                              0.079518
                                                                                                                                             0.000605
           0.001858
                      0.055443
                                                                                                                      1.06e-07
                                                                                                                                 5.59e-06
                                                                                                                                                          0.164082
                                                                                                                                                                                 Pr(>|t|)
                                                                                                                                                                      1.12e-13
                                                                                                          < 2e-16
*
*
                                                                                                                       *
*
                                                                                                                                   ***
                                                                                                                                               ***
```

```
## F-statistic: 11.48 on 14 and 105 DF, p-value: 1.542e-15
                                      ## Multiple R-squared: 0.6048, Adjusted R-squared:
                                                                                        ## Residual standard error: 6.917 on 105 degrees of freedom
                                                                                                                                                                                ## Signif. codes:
                                                                                                                                                                                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '
                                                    0.5521
```

- 22. What null hypothesis is the F statistic testing?
- a. The population mean yield is the same across sites
- b. The population mean yield is the same across varieties
- C. The population mean yield is the same across sites and varieties
- Using the usual arbitrary 0.05 significance level, do these data support the hypothesis that the popu-There is no significant interaction between site and variety
- a. Yes, some of the site p-values are less than the significance level

lation mean yield differs across sites?

- b. No, not all of the site p-values are less than the significance level
- Yes, the intercept p-value is less than the significance level
- d.)The p-values presented in this output do not provide sufficient information to answer this question

We think there might be an interaction between site and variety. We want to fit another model incorincrease in model complexity. porating this interaction term, and see whether the improvement in fit to the data is enough to justify the

24. What 1m call will generate the desired model?

```
a. lm(yield ~ site + variety, data = barley)
(b) lm(yield ~ site * variety, data = barley)
c. lm(yield ~ site : variety, data = barley)
d. lm(yield ~ site ! variety, data = barley)
```

- What would be the most reasonable inferential procedure for assessing whether a statistically significant interaction exists between these variables?
- Just look at the interaction plot; clearly there is none (this is why we make these plots in the make a conclusion. first place). We don't need to do a significance test with an arbitrary level every time we want to
- over regular \mathbb{R}^2 , because adding terms to a model will always increase \mathbb{R}^2 to the data, and look at which one has a higher adjusted R^2 . Adjusted R^2 is important to use Fit the model with only main effects, and the model with both main effects and the interaction
- Ċ Fit the model with only the main-effects, then fit the model with only the interaction, and compare their fit to the data. The model with main effects and interaction is saturated and will fit the data perfectly, so should not be considered.
- Fit the model with only main effects, and the model with both main effects and the interaction to the data, and compare them using an F test.

adhesion) and BNucl (bare nuclei) as follows: and y=1 corresponding to benign. We fit a binary regression model with two predictors: Adhes (marginal tumours. Recall the discussion from lecture of the Wisconsin Breast Cancer data: 681 cases of potentially cancerous The response variable is whether the tumor is benign, with y = 0 corresponding to malignant

```
## Coefficients:
                                                                                                                                                                                                                                                                                                                 #
AIC:
                Residual
                                                                                                                                       BNuc1
                                                                                                                                                        Adhes
                                                                                                                                                                                                                                                                             Deviance Residuals:
                                                                                                   Signif. codes:
                                                               (Dispersion parameter for binomial family taken to
                                                                                                                                                                                                                                                                                                                                  Call:
                                                                                                                                                                       (Intercept)
                                                                                                                                                                                                                                            -2.6635
                                                                                                                                                                                                                                                                                                               glm(formula = Class)
                                Null deviance:
                deviance:
                                                                                                                                                                                                                                            -0.0365
                                                                                                                                                       -0.69749
                                                                                                                                                                                        Estimate Std.
                                                                                                                                      -0.74367
                                                                                                                                                                         4.95908
                                                                                                 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '
                243.65
                                881.39
                                                                                                                                                                                                                                            0.2418
                                                                                                                                                                                                                                                            Median
                                                                                                                                                                                                                                                                                                           ~ Adhes + BNucl, family = binomial, data =
                                                                                                                                     0.07760
                                                                                                                                                      0.09616
                                                                                                                                                                       0.35760
                                                                                                                                                                                       Error
               on 678
                                on 680
                                                                                                                                                                                                                                            0.2418
                                                                                                                                                                                      z value Pr(>|z|)
                                                                                                                                                                                                                                                           30
                                                                                                                                   -9.584
                                                                                                                                                     -7.253 4.07e-13
                                                                                                                                                                       13.868
           degrees of freedom
                              degrees of freedom
                                                                                                                                                                                                                                            3.4547
                                                                                                                                                                                                                                                            Max
                                                                                                                                    < 2e-16
                                                                                                                                                                     < 2e-16
                                                                                                                                                      *
*
                                                                                                                                                                       **
```

Number of Fisher Scoring iterations: 7

- For a binary response, the binomial residual deviance reduces to $D=-2\sum_{i=1}^n(\hat{p}_i\log\hat{p}_i+(1-p_i))$ and why or why not? $\hat{p}_i)\log{(1-\hat{p}_i)})$. Would you recommend comparing binary regression models using residual deviance,
- a. Yes, binary regression is just a special case of binomial regression, and residual deviance is an appropriate statistic to consider when comparing the fits of binomial models
- Yes, when the data is binary the approximate distribution of the residual deviance is χ_1^2 , which has a mean of 1, and hence it will reject the null hypothesis of equal fit more often (higher power)
- No, when the data is binary the approximate distribution of the residual deviance is χ_1^2 , which has a mean of 1, and hence it will reject the null hypothesis of equal fit less often (lower power)
- 27. Recall the form of the binary regression model: $g(p_i) = \eta_i = \mathbf{x}_i^T \beta$, with $g(p) = \log\left(\frac{p}{1-p}\right)$ According to No, the point of looking at residual deviance is to compare the model fitted values to the observed responses, but the above expression depends only on the model fitted values
- BNucl = 1?the above model, what is the value of the linear predictor η_i for an observation with Adhes = 1 and
- a. 3.51 b. -3.67 7= 4.96 - . 697 - . 744 - 3.519
- d. -1.44 c. 4.959
- 28. What is the predicted probability of the tumor being malignant for an observation with a linear predictor $\hat{\eta} = 1$?

0.731 **(**00.269

P= 1+e-19 = 0.731 proto of BENIGN

- d. Not enough information; we also need to know ${\bf x}$ and $\hat{\beta}$
- 29. Suppose observation y_1 has BNucl = 1, and observation y_2 has BNucl = 2, and that they both have having a benign tumour? the same value of Adhes. What is the ratio of the odds of y_1 having a benign tumor to the odds of y_2 W, = exp(Bo+ & Adhus + 1xBz)

W= = exp(|35+ |31 Adhea + 2x|3=)

a. 0.744

(c.)2.103 $W_1/W_2 = \exp(-\beta_2) = \exp(0.744) = 0.1$ Impossible to say without knowing their common value of Adhes.

We think there might be an interaction between these two variables, so we fit a model:

Call:

glm(formula = Class ~ Adhes * BNucl, family = binomial, data = wbca)

```
## Number of Fisher Scoring iterations: 7
                                     ## AIC: 241.08
                                                       ## Residual deviance: 233.08
                                                                                                                                                  ## Signif. codes:
                                                                                                                                                                                                                                                                                                                                                               ## Deviance Residuals:
                                                                                                                                                                                                           BNucl
                                                                                                                                                                                        Adhes:BNucl
                                                                                                                                                                                                                                                                                    Coefficients:
                                                                                                                                                                                                                              Adhes
                                                                                                                                                                                                                                               (Intercept)
                                                                                                             (Dispersion parameter for binomial family taken to be 1)
                                                                                                                                                                                                                                                                                                                          -2.7837
                                                                          Null deviance: 881.39
                                                                                                                                                                                                                                                                                                                          -0.1525
                                                                                                                                                                                                          -1.02960
                                                                                                                                                                                                                             -1.02800
                                                                                                                                                                                                                                                                Estimate Std.
                                                                                                                                                                                        0.10345
                                                                                                                                                                                                                                                5.80758
                                                                                                                                                    0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1
                                                                                                                                                                                                                                                                                                                          0.2049
                                                                                                                                                                                                                                                                                                                                            Median
                                                                                                                                                                                                                                               0.48774
                                                                                                                                                                                        0.02631
                                                                                                                                                                                                          0.12277
                                                                                                                                                                                                                             0.15401
                                                                                                                                                                                                                                                                Error
                                                        on 677
                                                                        on 680
                                                                                                                                                                                                                                                                                                                          0.2049
                                                                                                                                                                                                                                                                z value Pr(>|z|)
                                                                                                                                                                                                                                               11.907
                                                                                                                                                                                                                             -6.675 2.48e-11
                                                                                                                                                                                                          -8.387
                                                                                                                                                                                        3.933 8.40e-05
                                                      degrees
                                                                       degrees of freedom
                                                                                                                                                                                                                                                                                                                          2.9977
                                                                                                                                                                                                                                                                                                                                            Max
                                                                                                                                                                                                           < 2e-16
                                                                                                                                                                                                                                               < 2e-16
                                                       of freedom
                                                                                                                                                                                                                              *
*
                                                                                                                                                                                                                                                *
*
                                                                                                                                                                                                           *
*
```

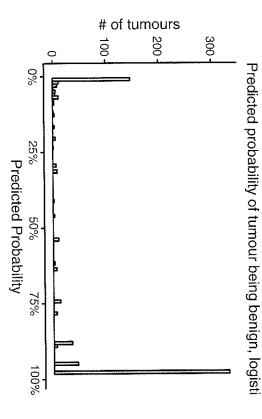
- 30. Under this model, what is the effect of a unit increase in Adhes, holding BNucl constant?
- a. Decrease the log-odds of the tumor being benign by -1.028
- be an increase or decrease without knowing the value of BNucl) Change the log-odds of the tumor being benign by $-1.028 + 0.103 \times$ BNucl (we can't say if it will
- Decrease the probability of the tumor being benign by a factor of -1.028
- d. Multiply the probability of the tumor being benign by $-1.028 + 0.103 \times$ BNucl (we can't say if it will be an increase or decrease without knowing the value of BNucl)
- 31. Both main effects are negative, but their interaction is positive. What of the following explanations for this sounds the most reasonable?
- The relationship between Adhes and BNucl is increasing: larger Adhes implies larger BNucl
- b. The model coefficients are unstable (have high variance)
- The intercept is huge, so the difference in sign between the interaction term and the main effects won't affect the model predictions much, and hence their estimates could be anything
- d.)The relationship between Adhes and the log-odds of the tumour being benign is different for different values of BNucl.

- 32. How would you interpret the relationship between the predictor variables and the log-odds of a tumour being benign?
- A larger BNucl decreases the amount by which increasing Adhes decreases the log-odds of the
- A larger Adhes decreases the amount by which increasing BNucl decreases the log-odds of the tumor being benign
- (c) Both A and B are correct
- d. Neither A nor B are correct

of our model. To operationalize our model for this purpose, we need to pick a cutoff 0 < h < 1 such that we classify a tumour as benign if $\hat{p} > h$ and malignant otherwise, where \hat{p} is the prediction from our model. We wish to assess the ability of our model to classify tumours as benign or malignant- the predictive accuracy dataset, entitled "Histogram of Predicted Probabilities". How to choose this cutoff? We make a histogram of the predicted probabilities for each individual in the

- 33. How would you use this chart to pick a cutoff? Select the most reasonable response.
- Choose h=0.5 because this bisects the range of possible predicted probabilities
- Choose h = 0.9 because it appears that most of the predicted probabilities are close to 1
- benign? type of error- e.g. is it worse to predict a benign tumour as malignant, or a malignant tumour as We cannot tell from this plot alone; we need more information about the cost associated with each
- d. We cannot tell from this plot alone; we also need to look at a plot of the residuals vs fitted values

Histogram of Predicted Probabilities



columns, actual is rows, i.e. there are 26 observations with actual = 0 and predicted = 1): Suppose we choose a cutoff of h = 0.5, leading to the following table of predicted vs actual (predicted is

d. Cannot tell from this table alone

35. What is the true positive rate for this cutoff?

What is the true positive rate for this cuton?
$$\frac{43!}{b} = 07.3\%$$

a. 94.3%

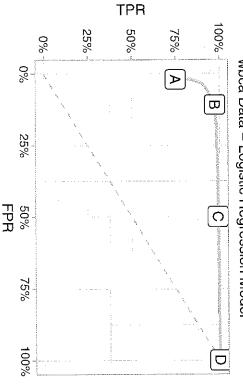
b) 97.3%

TPR = $\frac{77}{17+FN} = \frac{43!}{43!+12} = 07.3\%$
c. 63.3%

d. Cannot tell from this table alone

ROC Curve

wbca Data - Logistic Regression Model



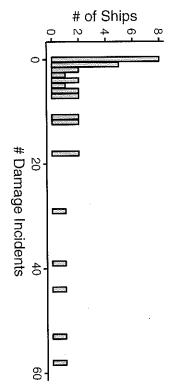
36. Consider the ROC curve shown in the plot "WBCA Model - ROC Curve". There are four letters on the curve. Which one corresponds to the above contingency table?

tion, period of operation, and type of ship. We wish to build a model of incidents The ships data gives the number of damage incidents by number of months of service, year of construc-

Observations:

\$ incidents <int> 0, 0; 3, 4, 6, 18, 11, 39, 29, 58, 53, 12, 44, 18, 1... ## \$ service ## \$ period ## Variables: 5 <int> 60, 75, 60, 75, 60, 75, 75, 60, 75, 60, 75, 60, 75, ... <int> 127, 63, 1095, 1095, 1512, 3353, 2244, 44882, 17176,... <int> 60, 60, 65, 65, 70, 70, 75, 60, 60, 65, 65, 70, 70, ... <fct> A, A, A, A, A, A, B, B, B, B, B, B, C, C, C, C...

Ships Data: number of damage incidents



- 37. Which of the following is assumed about the mean and variance of the response Y when fitting a Poisson regression?
- a. $Var(Y) = \sigma^2$, a constant
- Var(Y) > E(Y)
- $\bigcirc Var(Y) = E(Y)$
- d. There is no assumption; we know the mean-variance relationship because we know the data is Poisson distributed
- 38. How do you check this assumption?
- Plot the residuals vs the fitted values
- Plot the squared residuals vs the fitted values
- Plot the standardized residuals vs the fitted values
- d. Use a normal QQ-plot

- 39. I fit a model incidents ~ service + year + period. Then I fit another model: incidents log(service) + year + period. Why do you think I tried a log transformation of service? service is a count, so a log transformation is appropriate
- including log(service) models this perceived linear relationship. model models the log of the mean number of incidents as a linear function of the predictors, incidents would increase approximately linearly with service. Since the poisson regression service represents the aggregate lifetime in months of the ship. We would think that damage
- c service represents the aggregate lifetime in months of the ship. We would think that damage log(service) models this perceived multiplicative relationship. sion model models the mean number of incidents as a linear function of the predictors, including incidents would increase approximately multiplicatively with service. Since the poisson regres-
- d. service is strictly positive, which violates the normality assumption of the model
- 40. Suppose we think there might be overdispersion in these data. We estimate the dispersion parameter and refit the model. What will change?
- Regression coefficients remain the same; their standard errors will change
- Regression coefficients remain the same; their standard errors remain the same
- Regression coefficients will change; their standard errors will change
- d. Regression coefficients will change; their standard errors remain the same