

360.252 - Computational Science on Many-Core Architectures

WS 2020 - Exercise 6

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1 Dot Product with warp shuffles - shared memory

I tested my code setting N=5 which gave me the result shown in figure 1. I decided to implement everything with integers since the atomicMin() and atomicMax() would need some additional code snippets to work for double which, of course, I could have copied from the cuda documentation. But I wanted to avoid more overhead since I wanted to only focus on the principals here.

Compile output

[Compilation successful]

Run output

```
Input
-2 | -1 | 0 | 1 | 2 |
Sum of all entries: 0
Sum of maximum values: 6
Sum of squares: 10
Max-norm: 2
minimum value: -2
maximum value: 2
number of zeros: 1
```

Figure 1: Output of shared memory version

Listing 1: Calculations done with shared memory

```
#include <iostream>
2
    __global__ void sharedMemoryKernel(const
3
                                                   int*x,
                                                            int * y, const int N) {
        \_shared\_ int sharedMemory [7][256];
4
5
         int sum = 0;
         int maxSum = 0;
6
7
         int   sqrSum = 0;
8
         int \max Mod = 0;
9
         int min = x[0];
10
         int max = 0;
11
         int zeros = 0;
12
13
        for (int tid = blockDim.x * blockIdx.x + threadIdx.x;
        tid < N; tid += gridDim.x * blockDim.x) {
14
            int val = x[tid];
15
16
17
            sum += val;
18
            \max Sum += std :: abs(val);
19
            sqrSum += val*val;
20
            \max Mod = std :: abs(val) > \max Mod ? val : \max Mod;
21
            \min = \text{val} < \min ? \text{val} : \min;
            \max = val > \max ? val : \max;
22
23
            zeros += val == 0 ? 1 : 0;
24
25
26
        int tid = threadIdx.x;
27
        if (tid < N) {
            sharedMemory[0][threadIdx.x] = sum;
28
```

```
29
             sharedMemory[1][threadIdx.x] = maxSum;
             sharedMemory[2][threadIdx.x] = sqrSum;
30
             sharedMemory[3][threadIdx.x] = maxMod;
31
             sharedMemory[4][threadIdx.x] = min;
32
33
             sharedMemory[5][threadIdx.x] = max;
34
             sharedMemory[6][threadIdx.x] = zeros;
35
             _syncthreads();
36
37
             // blockDim.x needs to be a power of 2 in order for this to work
             for (int i = blockDim.x/2; i != 0; i /= 2) {
38
39
                  _syncthreads();
                  if (tid < i) 
40
                      \operatorname{sharedMemory}[0][\operatorname{tid}] += \operatorname{sharedMemory}[0][\operatorname{tid} + i];
41
                      sharedMemory[1][tid] += sharedMemory[1][tid + i];
42
                      sharedMemory [2][tid] += sharedMemory [2][tid + i];
43
44
                      sharedMemory[3][tid] = sharedMemory[3][tid] > sharedMemory[3][tid + i]
                      ? sharedMemory[3][tid] : sharedMemory[3][tid + i];
45
                      sharedMemory [4][tid] = sharedMemory [4][tid] < sharedMemory [4][tid + i]
46
                      ? sharedMemory [4] [tid] : sharedMemory [4] [tid + i];
47
                      \operatorname{sharedMemory}[5][\operatorname{tid}] = \operatorname{sharedMemory}[5][\operatorname{tid}] > \operatorname{sharedMemory}[5][\operatorname{tid}+\operatorname{i}]
48
49
                      ? sharedMemory [5] [tid] : sharedMemory [5] [tid + i];
                      sharedMemory [6] [tid] += sharedMemory [6] [tid + i];
50
51
                  }
             }
52
        }
53
54
        if (tid = 0) {
55
56
             atomicAdd(y, sharedMemory[0][0]);
             atomicAdd(y+1, sharedMemory[1][0]);
57
             atomicAdd(y+2, sharedMemory[2][0]);
58
59
             atomicMax(y+3, sharedMemory[3][0]);
60
             atomicMin (y+4, sharedMemory [4][0]);
61
             atomicMax(y+5, sharedMemory[5][0]);
             atomicAdd(y+6, sharedMemory[6][0]);
62
        }
63
64
   }
65
    template <typename T>
66
     void printContainer (T container,
67
         for (int i = 0; i < N; i++) {
68
              std::cout << container[i] << " | ";
69
70
   }
71
72
73
74
   int main() {
75
76
        int N = 5;
77
         int *x = (int *) malloc(sizeof(int) * N);
78
         int *y = (int *) malloc(sizeof(int) * 7);
79
80
81
        for (int i = 0; i < N; i++) {
             x[i] = i - N/2;
82
83
84
85
         int *cuda_x;
```

```
int *cuda_y;
 86
 87
           cudaMalloc(&cuda_x, sizeof( int) * N);
           cudaMalloc(&cuda_y, sizeof( int) * 7);
 88
 89
           cudaMemcpy(cuda_x, x, sizeof( int) * N, cudaMemcpyHostToDevice);
 90
 91
 92
           sharedMemoryKernel << <256, 256>>>(cuda_x, cuda_y, N);
 93
           cudaMemcpy(y, cuda_y, sizeof( int) * 7, cudaMemcpyDeviceToHost);
 94
 95
 96
           std::cout << "Input" << std::endl;
 97
           printContainer(x, N);
           std::cout << std::endl;
 98
 99
           std::cout << "Sum of all entries: " << y[0] << std::endl;\\
100
           std::cout << "Sum of maximum values: " << y[1] << std::endl;
101
           std::cout << "Sum of squares: " << y[2] << std::endl;
102
103
           std::cout << "Max-norm: " << y[3] << std::endl;
           \begin{array}{l} {\rm std}:: {\rm cout} << \text{"minimum value}: \text{"} << y[4] << {\rm std}:: {\rm endl}; \\ {\rm std}:: {\rm cout} << \text{"maximum value}: \text{"} << y[5] << {\rm std}:: {\rm endl}; \\ {\rm std}:: {\rm cout} << \text{"number of zeros}: \text{"} << y[6] << {\rm std}:: {\rm endl}; \\ \end{array}
104
105
106
107
108
           free(x);
109
           free (y);
110
           cudaFree(cuda_x);
           cudaFree(cuda_y);
111
112
113
           return EXIT_SUCCESS;
114
```

2 Dot Product with warp shuffles - warp shuffles

I tested my code by comparing to the version in point 1.

Listing 2: Calculations done with warp shuffles

```
#include <iostream>
   __global__ void shuffleKernel(const int * x, int * y, const int N) {
3
4
5
       int sum
                           = 0;
6
       int maxSum
                           = 0;
7
       int sqrSum
                           = 0;
8
       int maxMod
                           = 0;
                           = x[0];
9
       int min
10
       int max
                           = 0:
                           = 0:
11
       int zeros
12
13
       for (int tid = blockDim.x * blockIdx.x + threadIdx.x;
14
       tid < N; tid += gridDim.x * blockDim.x) 
15
           int val = x[tid];
16
17
           sum
                       += val;
                       += std::abs(val);
18
           maxSum
19
                       += val*val;
           sqrSum
                       = std :: abs(val) > maxMod ? val : maxMod;
20
           \max Mod
21
           min
                       = val < min ? val : min;
                       = val > max ? val :max;
22
           max
23
                       += val == 0 ? 1 : 0;
           zeros
24
       }
25
26
       int tid = threadIdx.x;
27
       for (int i = warpSize / 2; i != 0; i /= 2) {
                       += -shfl_down_sync(0 xffffffff, sum, i);
28
           sum
29
           \max Sum
                       += __shfl_down_sync(0xfffffffff, maxSum, i);
30
           sqrSum
                       += __shfl_down_sync(0xfffffffffffff, sqrSum, i);
           31
                       = temporary > maxMod ? temporary : maxMod;
32
           \max Mod
33
                       = -shfl_down_sync(0xffffffff, min, i);
           temporary
34
                       = temporary < min ? temporary : min;
           min
35
                       = -shfl_down_sync(0xffffffff, max, i);
           temporary
36
           max
                       = temporary > max ? temporary : max;
37
                       zeros
38
39
       _syncthreads();
40
       if (tid % warpSize = 0) {
41
           atomicAdd(y,
                          sum);
42
           atomicAdd(y+1, maxSum);
           atomicAdd(y+2, sqrSum);
43
44
           atomicMax(y+3, maxMod);
45
           atomicMin(y+4, min);
           atomicMax(y+5, max);
46
           atomicAdd(y+6, zeros);
47
48
       }
49
50
   template <typename T>
```

```
void printContainer(T container, int N) {
52
53
         for (int i = 0; i < N; i++) {
             std::cout << container[i] << " | ";
54
55
56
   }
57
58
59
   int main() {
60
        int N = 100000;
61
62
63
        int *x = (int *) malloc(size of (int) * N);
64
        int *y = (int *) malloc(size of (int) * 7);
65
66
        for (int i = 0; i < N; i++) {
67
            x[i] = i - N/2;
68
69
70
        int *cuda_x;
        int *cuda_y;
71
        cudaMalloc(&cuda_x, sizeof(int) * N);
72
73
        cudaMalloc(&cuda_y, sizeof(int) * 7);
74
75
        cudaMemcpy(cuda_x, x, sizeof(int) * N, cudaMemcpyHostToDevice);
76
        shuffleKernel \ll N/256, 128 >>> (cuda_x, cuda_y, N);
77
78
        cudaMemcpy(y, cuda_y, sizeof(int) * 7, cudaMemcpyDeviceToHost);
79
80
81
        //std::cout << "Input" << std::endl;
82
        //printContainer(x, N);
83
        // std :: cout << std :: endl;
84
        std::cout \ll "Sum of all entries:" \ll y[0] \ll std::endl;
85
        86
87
        \operatorname{std}::\operatorname{cout}<<\operatorname{"Max-norm}: " <<\operatorname{y}[3]<<\operatorname{std}::\operatorname{endl};
88
89
        std::cout << "minimum value: " << y[4] << std::endl;
        std::cout << "maximum value: " << y[5] << std::endl;
90
91
        std::cout << "number of zeros: " << y[6] << std::endl;
92
        free(x);
93
        free(y);
94
95
        cudaFree(cuda_x);
96
        cudaFree(cuda_y);
97
98
        return EXIT_SUCCESS;
99
```

3 Dot Product with warp shuffles - performance comparison

In order to compare the performances, I launched every kernel with [N/256, 128]. I additionally implemented the dot product in shared and shuffled version. The results can be found in figure 5. It can be seen that the shuffled versions perform a little better than the shared memory versions unless for one data point at the last N. I cannot really explain this behaviour. I doublechecked my tests and didn't find any errors in there.

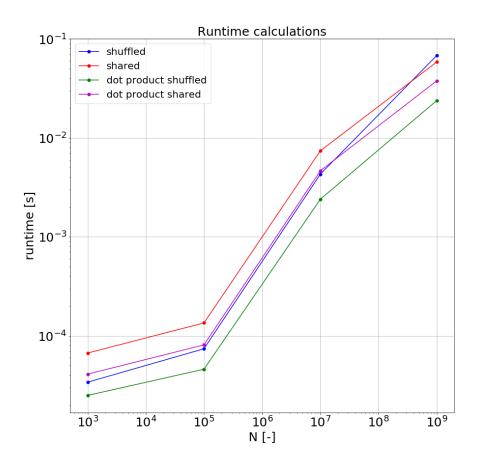


Figure 2: Runtimes for different versions

Listing 3: Dot product using shared memory

```
__global__ void dot_product(int* x, int* y, int* dot, int N) {
1
2
3
       int index = threadIdx.x + blockDim.x * blockIdx.x;
       int stride = blockDim.x * gridDim.x;
4
5
6
        _shared_ int cache[128];
7
8
       int temp = 0;
9
       while (index < N) {
10
            temp += x[index] * y[index];
            index += stride;
11
12
13
       cache[threadIdx.x] = temp;
14
15
        _syncthreads();
16
```

```
17
18
        for (int i = blockDim.x/2; i > 0; i/= 2) {
19
            __syncthreads();
            if (threadIdx.x < i)
20
                cache[threadIdx.x] += cache[threadIdx.x + i];
21
22
        }
23
        if (threadIdx.x == 0)
24
25
            atomicAdd(dot, cache[0]);
26
27
   }
```

Listing 4: Dot product using warp shuffles

```
__global__ void dot_product_shuffle(int* x, int* y, int* dot, int N) {
1
2
3
       int index = threadIdx.x + blockDim.x * blockIdx.x;
4
       int stride = blockDim.x * gridDim.x;
5
6
       int temp = 0;
        while (index < N) {
7
8
            temp += x[index] * y[index];
9
            index += stride;
10
       }
11
        for (int i = warpSize / 2; i != 0; i /= 2) {
12
13
                         += -shfl_down_sync(0xffffffff, temp, i);
14
15
16
       --syncthreads();
17
       int tid = threadIdx.x;
18
19
        if (tid % warpSize == 0) {
20
21
            atomicAdd(dot, temp);
22
23
24
```

4 Sparse Matrix Times Dense Matrix - The kernel

I tested my implementation of the sparse matrix times dense matrix with the matrix from the lecture, see figure 3, and by comparing it to a sparse matrix times a vector. Details and results please take from figure 4 and the code listing. I implemented it in column major style.

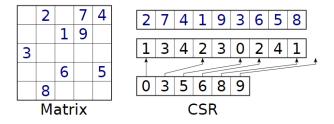


Figure 3: testmatrix from the lecture

Run output

```
x:
1 | 2 | 3 | 4 | 5 |
Result:
52 | 39 | 3 | 43 | 16 |
X:
1 | 2 | 3 | 4 | 5 | 1 | 2 | 3 | 4 | 5 | 1 | 2 | 3 | 4 | 1 |
Result:
52 | 39 | 3 | 43 | 16 | 52 | 39 | 3 | 43 | 16 | 36 | 39 | 3 | 23 | 16 |
```

Figure 4: results of matrix vector and matrix matrix product

Listing 5: matrix*vector and matrix*matrix

```
#include <iostream>
1
2
3
   // y = A * x
4
   --global-- void sparseVector(int N, int *csr_rowoffsets,
5
                                              int *csr_colindices , double *csr_values ,
6
                                              double *x, double *y)
7
8
     for (int i = blockIdx.x * blockDim.x + threadIdx.x;
9
     i < N; i += blockDim.x * gridDim.x)  {
10
        double sum = 0;
11
        for (int k = csr_rowoffsets[i]; k < csr_rowoffsets[i + 1]; k++) {
12
13
         sum += csr_values[k] * x[csr_colindices[k]];
14
15
       y[i] = sum;
16
17
   }
18
19
20
21
   // Y = A * X
   __global__ void sparseDense(int N, int K, int *csr_rowoffsets,
```

```
23
      int *csr_colindices, double *csr_values,
24
      double *x, double *y)
25
      for (int i = blockIdx.x * blockDim.x + threadIdx.x;
26
27
      i < N; i \leftarrow blockDim.x * gridDim.x) {
28
29
        for (int k = 0; k < K; k++) {
30
          double sum = 0;
31
          for \ (int \ jj = csr\_rowoffsets [i]; \ jj < csr\_rowoffsets [i+1]; \ jj++) \ \{
32
33
            sum += csr_values[jj] * x[csr_colindices[jj] + N*k];
34
35
          y[i + N*k] = sum;
36
37
38
39
      }
   }
40
41
42
43
   template <typename T>
    void printContainer(T container, int N) {
44
         for (int i = 0; i < N; i++) {
45
             std::cout << container[i] << " | ";
46
47
48
        std::cout << std::endl;
   }
49
50
51
52
   int main() {
53
54
      int N = 5;
      int K = 3;
55
56
      double *values = ( double *) malloc(sizeof( double) * 9);
57
      int *colindices = (int*) malloc(sizeof(int) * 9);
58
59
      int *offsets = (int*) malloc(sizeof(int) * 6);
60
      double *x = ( double *) malloc(sizeof( double) * N);
61
62
      double *X = (double*) malloc(sizeof(double) * N*K);
63
      double *y = ( double *) malloc(sizeof( double) * N);
64
      double *Y = (double*) malloc(sizeof(double) * N*K);
65
66
67
      values [0] = 2;
      values [1] = 7;
68
69
      values [2] = 4;
70
      values [3] = 1;
71
      values [4] = 9;
      values [5] = 3;
72
      values [6] = 6;
73
      values [7] = 5;
74
75
      values [8] = 8;
76
      colindices[0] = 1;
77
      colindices[1] = 3;
78
      colindices[2] = 4;
79
```

```
80
      colindices[3] = 2;
81
      colindices[4] = 3:
82
      colindices[5] = 0;
      colindices[6] = 2;
83
84
      colindices[7] = 4;
85
      colindices[8] = 1;
86
87
      offsets[0] = 0;
88
      offsets[1] = 3;
      offsets[2] = 5;
89
      offsets[3] = 6;
90
      offsets [4]
                  = 8;
91
      offsets[5] = 9;
92
93
94
      x[0] = 1;
95
      x[1] = 2;
96
      x[2]
           = 3;
97
      x[3]
           = 4;
      x[4] = 5;
98
99
100
      X[0] = 1;
      X[1]
           = 2;
101
      X[2]
102
           = 3;
      X[3]
103
           = 4;
104
      X[4]
           = 5;
105
      X[5]
           = 1;
106
      X[6]
           = 2;
      X[7]
107
           = 3;
108
      X[8]
           = 4;
109
      X[9] = 5;
      X[10] = 1;
110
111
      X[11] = 2;
      X[12] = 3;
112
      X[13] = 4;
113
      X[14] = 1;
114
115
116
      double *cuda_values;
117
      int *cuda_colindices;
118
      int *cuda_offsets;
119
      double *cuda_x:
120
      double *cuda_X:
121
      double *cuda_y;
122
      double *cuda_Y;
123
      cudaMalloc(&cuda_values, sizeof( double) * 9);
124
125
      cudaMalloc(&cuda_colindices, sizeof( int) * 9);
126
      cudaMalloc(&cuda_offsets, sizeof(int) * 6);
127
      cudaMalloc(&cuda_x, sizeof( double) * N);
128
      cudaMalloc(&cuda_X, sizeof( double) * N*K);
      cudaMalloc(&cuda_y, sizeof( double) * N);
129
      cudaMalloc(&cuda_Y, sizeof( double) * N*K);
130
131
132
      cudaMemcpy(cuda_values, values, sizeof( double) * 9, cudaMemcpyHostToDevice);
      cudaMemcpy(cuda_colindices, colindices, sizeof( int) * 9, cudaMemcpyHostToDevice);
133
134
      cudaMemcpy(cuda_offsets, offsets, sizeof( int) * 6, cudaMemcpyHostToDevice);
135
      cudaMemcpy(cuda_x, x, sizeof( double) * N, cudaMemcpyHostToDevice);
      cudaMemcpy(cuda_X, X, sizeof( double) * N*K, cudaMemcpyHostToDevice);
136
```

```
137
138
        sparseVector << <256, 256>>>(N, cuda_offsets,
139
        cuda_colindices , cuda_values , cuda_x , cuda_y );
        cudaMemcpy(y, cuda_y, sizeof(double) * N, cudaMemcpyDeviceToHost);
140
141
142
        sparseDense <<<256, 256>>>(N, K, cuda_offsets,
143
        \verb"cuda-colindices", \verb"cuda-values", \verb"cuda-X", \verb"cuda-Y");
        cudaMemcpy(Y, cuda_Y, sizeof(double) * N*K, cudaMemcpyDeviceToHost);
144
145
146
        std::cout << "x : " << std::endl;
147
        \begin{array}{l} \operatorname{printContainer}\left(x\,,\;N\right);\\ \operatorname{std}::\operatorname{cout}\;<<\;\overset{\scriptscriptstyle *}{\operatorname{Result}}\;:\;\;^{\scriptscriptstyle *}\;<<\;\operatorname{std}::\operatorname{endl}; \end{array}
148
149
        printContainer(y, N);
150
151
152
        std::cout << std::endl;
        std::cout << "X : " << std::endl;
153
        printContainer(X, N*K);
154
        std::cout << "Result : " << std::endl;
155
        printContainer(Y, N*K);
156
157
158
        free(x);
159
        free(X);
        free(y);
160
        free (Y);
161
        free (values);
162
163
        free (colindices);
        free (offsets);
164
165
        cudaFree(cuda_values);
166
        cudaFree(cuda_colindices);
167
168
        cudaFree(cuda_offsets);
169
        cudaFree(cuda_x);
        cudaFree(cuda_X);
170
        cudaFree(cuda_y);
171
        cudaFree(cuda_Y);
172
173
174
        return EXIT_SUCCESS;
175
```

5 Sparse Matrix Times Dense Matrix - benchmark

I added a row major implementation to my code, both kernels can be seen in the listing. For the benchmark I constructed dummy matrices without specific values, except for a few. Maybe this is a reason why my row and column major implementations perform almost identical. But on the other hand, both my implementations are very similar, even for the strided access in line 13 and 35 of the first code listing. I also timed the Memcopy(), since the matrix vector has to do that K times which makes my timings more realistic. As expected, the matrix * vector K times is always slower than the matrix * matrix multiplication.

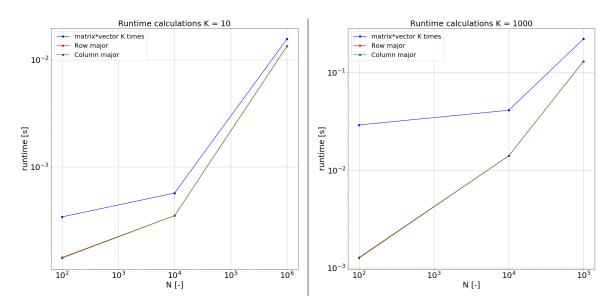


Figure 5: Runtimes of calculations for different N and K

Listing 6: Row- and Column major matrix multiplication

```
Y = A * X
    __global__ void sparseDenseRowMajor(int N, int K, int *csr_rowoffsets,
2
3
      int *csr_colindices, double *csr_values,
4
      double *x, double *y)
5
   {
6
      for (int i = blockIdx.x * blockDim.x + threadIdx.x;
7
      i < N; i += blockDim.x * gridDim.x)  {
8
        for (int k = 0; k < K; k++) {
9
10
          double sum = 0;
11
           for \ (int \ jj = csr\_rowoffsets [i]; \ jj < csr\_rowoffsets [i+1]; \ jj++) \ \{ \\
12
            sum += csr_values[jj] * x[csr_colindices[jj]*K + k];
13
14
          }
15
          y[i + N*k] = sum;
16
17
18
19
20
21
22
   // Y = A * X
```

```
__global__ void sparseDenseColumnMajor(int N, int K, int *csr_rowoffsets,
     int *csr_colindices, double *csr_values,
25
26
      double *x, double *y)
27
28
      for (int i = blockIdx.x * blockDim.x + threadIdx.x;
29
      i < N; i += blockDim.x * gridDim.x)  {
30
31
        for (int k = 0; k < K; k++) {
32
          double sum = 0;
33
34
          for (int jj = csr_rowoffsets[i]; jj < csr_rowoffsets[i + 1]; jj++) {
            sum += csr_values[jj] * x[csr_colindices[jj] + N*k];
35
36
37
38
         y[i + N*k] = sum;
39
40
41
     }
   }
42
```

Listing 7: Code for the timing benchmark

```
1 #include <iostream>
2 #include "timer.hpp"
3 #include <algorithm>
4 #include <iostream>
5 #include <stdio.h>
6 #include <vector>
8
   // y = A * x
9
   __global__ void sparseVector(int N, int *csr_rowoffsets,
10
                                              int *csr_colindices, double *csr_values,
                                              double *x, double *y)
11
12
     for (int i = blockIdx.x * blockDim.x + threadIdx.x;
13
14
     i < N; i \leftarrow blockDim.x * gridDim.x) {
15
       double sum = 0;
16
        for (int k = csr_rowoffsets[i]; k < csr_rowoffsets[i+1]; k++) {
17
         sum += csr_values[k] * x[csr_colindices[k]];
18
19
20
21
       y[i] = sum;
22
23
   }
24
25
26
   // Y = A * X
27
   __global__ void sparseDenseRowMajor(int N, int K, int *csr_rowoffsets,
     int *csr_colindices, double *csr_values,
28
29
     double *x, double *y)
30
31
     for (int i = blockIdx.x * blockDim.x + threadIdx.x;
32
     i < N; i \leftarrow blockDim.x * gridDim.x) {
33
34
        for (int k = 0; k < K; k++) {
35
          double sum = 0;
```

```
36
37
          for (int jj = csr\_rowoffsets[i]; jj < csr\_rowoffsets[i + 1]; jj++) {
38
            sum += csr_values[jj] * x[csr_colindices[jj]*K + k];
39
40
41
          y[i + N*k] = sum;
42
43
44
     }
   }
45
46
47
   // Y = A * X
48
   __global__ void sparseDenseColumnMajor(int N, int K, int *csr_rowoffsets,
49
50
     int *csr_colindices , double *csr_values ,
51
      double *x, double *y)
52
      for (int i = blockIdx.x * blockDim.x + threadIdx.x;
53
      i < N; i += blockDim.x * gridDim.x) {
54
55
56
        for (int k = 0; k < K; k++) {
57
          double sum = 0;
58
          for \ (int \ jj = csr\_rowoffsets[i]; \ jj < csr\_rowoffsets[i+1]; \ jj++) \ \{
59
            sum += csr_values[jj] * x[csr_colindices[jj] + N*k];
60
61
62
63
          y[i + N*k] = sum;
64
65
66
     }
67
   }
68
69
70
   template <typename T>
71
    void printContainer (T container, int N) {
72
         for (int i = 0; i < N; i++) {
73
             std::cout << container[i] << " | ";
74
75
        std::cout << std::endl;
76
   }
77
78
79
   int main() {
80
81
     Timer tim1, tim2, tim3;
82
      int N = 100000;
83
      int K = 1000;
84
      double *values = ( double *) malloc(sizeof( double) * N*10);
85
      int *colindices = (int*)malloc(sizeof(int) * N*10);
86
      int * offsets = (int*) malloc(size of(int) * (N+1));
87
88
      double *x = ( double *) malloc(sizeof( double) * N);
89
90
      double *X = (double*) malloc(size of (double) * N*K);
91
      double *y = ( double *) malloc(sizeof( double) * N);
92
```

```
93
       double *Y = (double*) malloc(sizeof(double) * N*K);
94
95
       values [0] = 2;
96
       values [1] = 7;
       values [2] = 4;
97
98
       values [3]
                  = 1;
99
       values [4]
                  = 9;
100
       values [5] = 3;
101
       values [6] = 6;
102
       values [7] = 5;
       values [8] = 8;
103
104
       colindices[0] = 1;
105
106
       colindices[1] = 3;
107
       colindices[2] = 4;
108
       colindices[3] = 2;
109
       colindices[4] = 3;
110
       colindices[5] = 0;
       colindices[6] = 2;
111
       colindices[7] = 4;
112
113
       colindices[8] = 1;
114
115
       offsets[0] = 0;
116
       offsets[1] = 3;
117
       offsets[2] = 5;
       offsets [3]
118
                   = 6;
119
       offsets [4]
                   = 8;
120
       offsets [5] = 9;
121
122
       x[0] = 1;
       x [1]
123
            = 2;
       x [2]
124
            = 3;
125
       x[3]
            = 4;
126
       x [4]
            = 5;
127
128
       X[0] = 1;
            = 1;
129
       X[1]
130
       X[2]
            = 1;
       X[3]
            = 2;
131
       X[4]
            = 2;
132
            = 2;
133
       X[5]
       X[6]
134
            = 3;
       X[7]
135
            = 3;
       X[8]
136
            = 3;
       X\lceil 9\rceil = 4;
137
138
       X[10] = 4;
139
       X[11] = 4;
140
       X[12] = 5;
141
       X[13] = 5;
       X[14] = 5;
142
143
144
       double
                   *cuda_values;
145
       int
                   *cuda_colindices;
146
                   *cuda_offsets;
       int
       double
147
                   *cuda_x;
148
       double
                   *cuda_X;
149
       double
                   *cuda_y;
```

```
150
      double
                 *cuda_Y;
151
152
      cudaMalloc(&cuda_values, sizeof( double) * N*10);
      cudaMalloc(&cuda_colindices, sizeof( int) * N*10);
153
      cudaMalloc(\&cuda\_offsets\;,\;\;sizeof(\;\;int\;)\;\;*\;\;(N+1));
154
155
      cudaMalloc(&cuda_x , sizeof( double) * N);
156
      cudaMalloc(&cuda_X, sizeof( double) * N*K);
      cudaMalloc(&cuda_y, sizeof( double) * N);
157
      cudaMalloc(&cuda_Y, sizeof( double) * N*K);
158
159
160
      cudaMemcpy(cuda_values, values, sizeof( double) * N*10, cudaMemcpyHostToDevice);
      {\it cudaMemcpy(cuda\_colindices\ ,\ colindices\ ,\ sizeof(\ int)\ *\ N*10\ ,\ cudaMemcpyHostToDevice);}
161
      {\it cudaMemcpy(cuda\_offsets\ ,\ offsets\ ,\ sizeof(\ int)\ *\ (N+1),\ cudaMemcpyHostToDevice);}
162
      cudaMemcpy(cuda_x, x, sizeof( double) * N, cudaMemcpyHostToDevice);
163
164
      cudaMemcpy(cuda_X, X, sizeof( double) * N*K, cudaMemcpyHostToDevice);
165
166
      std::vector<double> timings1;
167
        for (int reps=0; reps < 10; ++reps) {
168
             tim1.reset();
             for (int j = 0; j < K; j++) {
169
170
               sparseVector << <256, 256>>>(N, cuda_offsets, cuda_colindices, cuda_values,
               cuda_x, cuda_y);
171
               cudaMemcpy(y, cuda_y, sizeof(double) * N, cudaMemcpyDeviceToHost);
172
173
174
             timings1.push_back(tim1.get());
175
176
      std::sort(timings1.begin(), timings1.end());
      double time_elapsed1 = timings1[10/2];
177
      std::cout << "Time elapsed vector: " << time_elapsed1 << std::endl << std::endl;
178
179
180
181
182
183
184
185
      std::vector<double> timings2;
186
        for (int reps=0; reps < 10; ++reps) {
187
             tim2.reset();
             sparseDenseRowMajor << <256, 256>>>(N, K, cuda_offsets, cuda_colindices,
188
             cuda_values , cuda_X , cuda_Y );
189
             cudaMemcpy(Y, cuda_Y, sizeof(double) * N*K, cudaMemcpyDeviceToHost);
190
191
             timings2.push_back(tim2.get());
192
193
      std::sort(timings2.begin(), timings2.end());
      double time_elapsed2 = timings2[10/2];
194
      std::cout << "Time elapsed row: " << time_elapsed2 << std::endl << std::endl;
195
196
197
198
199
200
201
      std::vector<double> timings3;
202
      for (int reps=0; reps < 10; ++reps) {
203
           tim3.reset();
           sparseDenseRowMajor << <256, 256>>>(N, K, cuda_offsets, cuda_colindices,
204
           cuda_values , cuda_X , cuda_Y );
205
           cudaMemcpy(Y, cuda_Y, sizeof(double) * N*K, cudaMemcpyDeviceToHost);
206
```

```
207
            timings3.push_back(tim3.get());
       }
208
209
       std::sort(timings3.begin(), timings3.end());
       double time_elapsed3 = timings3[10/2];
std::cout << "Time elapsed column: " << time_elapsed3 << std::endl << std::endl;</pre>
210
211
212
213
214
215
216
       free(x);
217
       free(X);
218
       free (y);
       free(Y);
219
220
       free (values);
       free(colindices);
221
222
       free (offsets);
223
224
       cudaFree(cuda_values);
       cudaFree(cuda_colindices);
225
226
       cudaFree(cuda_offsets);
       cudaFree(cuda_x);
227
228
       cudaFree(cuda_X);
229
       cudaFree(cuda_y);
       cudaFree(cuda_Y);
230
231
232
233
       return EXIT_SUCCESS;
234
```