

MACROECONOMICS

PSE Summer School, 2024

On the Optimal Design of Fiscal Policy

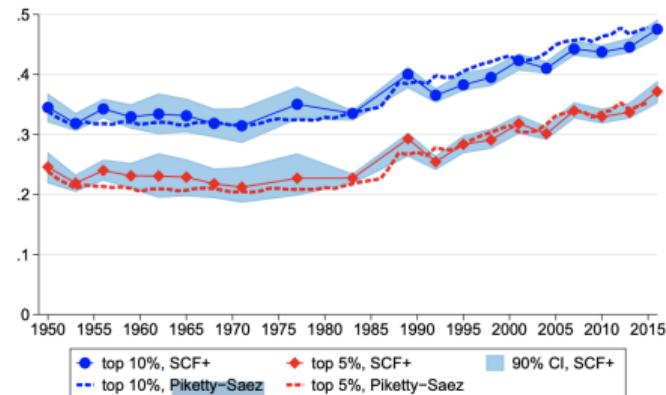
Axelle Ferriere

Summer School PSE

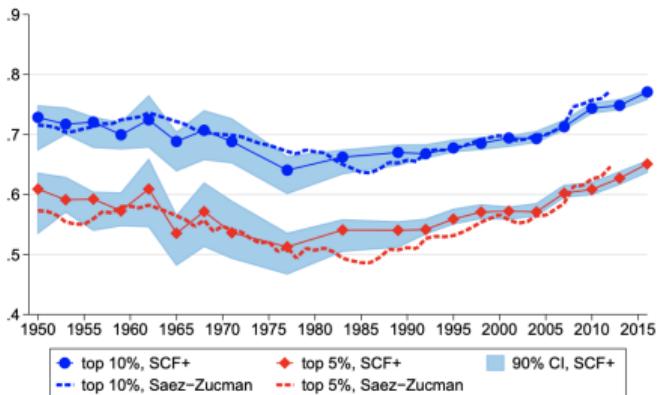
June 25, 2024

Income and wealth inequality have increased since 1950

Figure 5: Top 5% and top 10% income and wealth shares



(a) Income

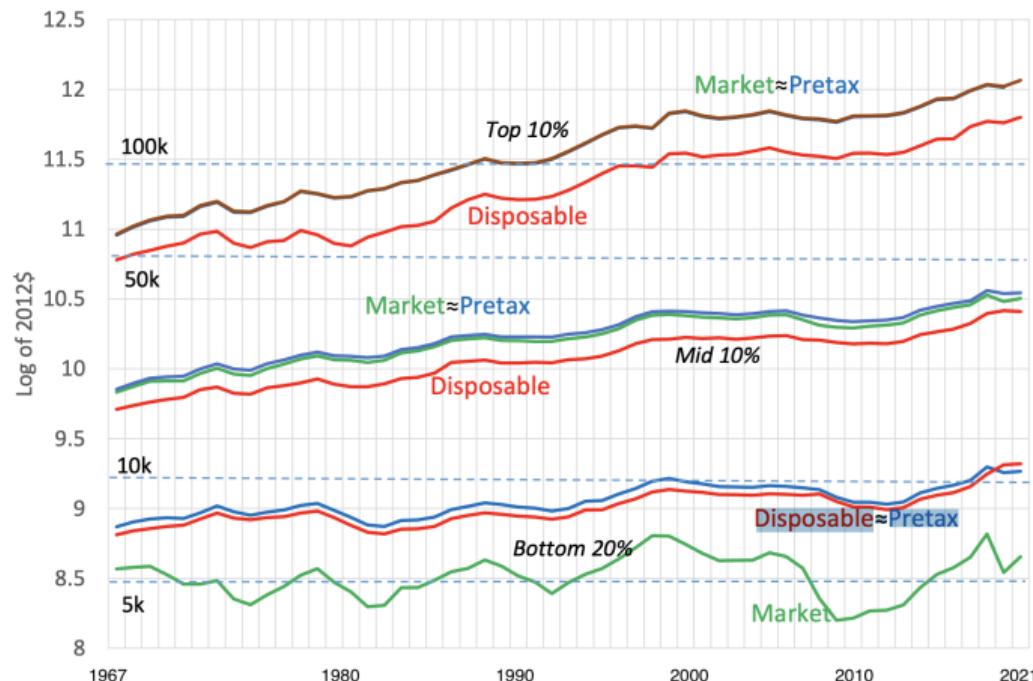


(b) Wealth

- Top-income and -wealth shares have increased (SCF+, United States)

Kuhn, Schularick and Stein (2020)

Income and wealth inequality have increased since 1950



- Household income has been flat for 5 decades at the bottom (CPS, United States)
Heathcote, Violante, Perri and Zhang (2023)

Rethinking fiscal policy

- High levels of **inequality**

Piketty Saez (2003), Heathcote Perri Violante (2010), Kuhn, Schularick and Stein (2020), Saez and Zucman (2020, 2022), Heathcote, Violante, Perri and Zhang (2022), ...

Rethinking fiscal policy

- High levels of **inequality**
Piketty Saez (2003), Heathcote Perri Violante (2010), Kuhn, Schularick and Stein (2020), Saez and Zucman (2020, 2022), Heathcote, Violante, Perri and Zhang (2022), ...
- New questions in the policy debate, **on the role of the welfare state**
 - Should we tax **wealth**?
 - Should we implement a **Universal Basic Income**? Should we increase **income tax progressivity**?

Rethinking fiscal policy

- High levels of **inequality**

Piketty Saez (2003), Heathcote Perri Violante (2010), Kuhn, Schularick and Stein (2020), Saez and Zucman (2020, 2022), Heathcote, Violante, Perri and Zhang (2022), ...

- New questions in the policy debate, **on the role of the welfare state**

- Should we tax **wealth**?
- Should we implement a **Universal Basic Income**? Should we increase **income tax progressivity**?

- This class: rethinking fiscal policy

- Optimal taxes at the household level
- Old classical theoretical literature, new **quantitative macro** literature

Lecture 1

Capital and Wealth Taxes

On capital taxes

Should we tax capital?

- A classic question in macro...
 - ... which came back in recent policy debate

On capital taxes

Should we tax capital?

- A classic question in macro...
 - ... which came back in recent policy debate
- Methodology
 - Ramsey plans
 - Quantitative heterogeneous-agent models
- Deterministic, long-run, steady-state

Should we tax capital?

1. Optimal fiscal policy in **representative-agent** models
 - Define **Ramsey plans** to compute optimal taxes

Should we tax capital?

1. Optimal fiscal policy in **representative-agent** models

- Define **Ramsey plans** to compute optimal taxes
- Capital taxes should be **zero**

Should we tax capital?

1. Optimal fiscal policy in **representative-agent** models

- Define **Ramsey plans** to compute optimal taxes
- Capital taxes should be **zero**

2. Optimal fiscal policy in a **standard Aiyagari** models

- Insurance, redistribution, and life-cycle dynamics

Should we tax capital?

1. Optimal fiscal policy in **representative-agent** models

- Define **Ramsey plans** to compute optimal taxes
- Capital taxes should be **zero**

2. Optimal fiscal policy in a **standard Aiyagari** models

- Insurance, redistribution, and life-cycle dynamics
- Capital taxes should be **34%**

Should we tax capital?

1. Optimal fiscal policy in **representative-agent** models

- Define **Ramsey plans** to compute optimal taxes
- Capital taxes should be **zero**

2. Optimal fiscal policy in a **standard Aiyagari** models

- Insurance, redistribution, and life-cycle dynamics
- Capital taxes should be **34%**

3. Optimal fiscal policy with heterogeneous capital returns

- New facts on capital returns

Should we tax capital?

1. Optimal fiscal policy in **representative-agent** models

- Define **Ramsey plans** to compute optimal taxes
- Capital taxes should be **zero**

2. Optimal fiscal policy in a **standard Aiyagari** models

- Insurance, redistribution, and life-cycle dynamics
- Capital taxes should be **34%**

3. Optimal fiscal policy with heterogeneous capital returns

- New facts on capital returns
- Capital taxes should be **negative**, wealth taxes should be positive

Literature Main references (many more at the end)

- On optimal fiscal policy in RA models and the latest controversies
 - Chamley (1986), Judd (1985), Straub and Werning (2020)
 - Chari, Christiano, and Kehoe (1994), Farhi (2010), ...

Literature

Main references (many more at the end)

- On optimal fiscal policy in RA models and the latest controversies
 - Chamley (1986), Judd (1985), Straub and Werning (2020)
 - Chari, Christiano, and Kehoe (1994), Farhi (2010), ...
- On capital taxes with insurance, redistribution, and life-cycle motives
 - Conesa, Kitao, and Krueger (2009)
 - Aiyagari (1995), Domeij and Heathcote (2002), Garriga (2017), ...

Literature

Main references (many more at the end)

- On optimal fiscal policy in RA models and the latest controversies
 - Chamley (1986), Judd (1985), Straub and Werning (2020)
 - Chari, Christiano, and Kehoe (1994), Farhi (2010), ...
- On capital taxes with insurance, redistribution, and life-cycle motives
 - Conesa, Kitao, and Krueger (2009)
 - Aiyagari (1995), Domeij and Heathcote (2002), Garriga (2017), ...
- On the new facts on capital returns
 - Fagereng, Guiso, Malacrino, and Pistaferri (2020)
 - Bach, Calvet, and Sodini (2020), Smith et al. (2019), Becker and Hvide (2022), ...

Literature

Main references (many more at the end)

- On optimal fiscal policy in RA models and the latest controversies
 - Chamley (1986), Judd (1985), Straub and Werning (2020)
 - Chari, Christiano, and Kehoe (1994), Farhi (2010), ...
- On capital taxes with insurance, redistribution, and life-cycle motives
 - Conesa, Kitao, and Krueger (2009)
 - Aiyagari (1995), Domeij and Heathcote (2002), Garriga (2017), ...
- On the new facts on capital returns
 - Fagereng, Guiso, Malacrino, and Pistaferri (2020)
 - Bach, Calvet, and Sodini (2020), Smith et al. (2019), Becker and Hvide (2022), ...
- On models with entrepreneurs and heterogeneous capital returns
 - Guvenen et al. (2023)
 - Kitao (2008), Bhandari and McGrattan (2020), Boar and Knowles (2020), Gaillard and Wangner (2022), ...

1. Optimal Taxes in a Deterministic Growth Model

General motivation

- Optimal taxes in a **competitive equilibrium**

General motivation

- Optimal taxes in a **competitive equilibrium**
 - Households' behaviors and prices

General motivation

- Optimal taxes in a **competitive equilibrium**
 - Households' behaviors and prices
- Taxes: **functional** forms

General motivation

- Optimal taxes in a **competitive equilibrium**

- Households' behaviors and prices

- Taxes: **functional** forms

- **Commitment** in time-zero

General motivation

- Optimal taxes in a **competitive equilibrium**
 - Households' behaviors and prices
- Taxes: **functional** forms
- **Commitment** in time-zero
- Outline: environment; equilibrium; Ramsey plan

Environment Preferences and resources

- Preferences of the representative household:

$$\sum_{t=0}^{\infty} \beta^t u(c_t, l_t), \quad (1)$$

where c_t : consumption, l_t : leisure.

Environment Preferences and resources

- Preferences of the representative household:

$$\sum_{t=0}^{\infty} \beta^t u(c_t, l_t), \quad (1)$$

where c_t : consumption, l_t : leisure.

- The two resource constraints are given by

$$l_t + n_t = 1$$

where n_t : labor, and

Environment Preferences and resources

- Preferences of the representative household:

$$\sum_{t=0}^{\infty} \beta^t u(c_t, l_t), \quad (1)$$

where c_t : consumption, l_t : leisure.

- The two resource constraints are given by

$$l_t + n_t = 1$$

where n_t : labor, and

$$g_t + c_t + k_{t+1} = A_t F(k_t, n_t) + (1 - \delta)k_t, \quad (2)$$

where g_t : government expenditure, A_t : TFP, k_t : capital with k_0 is given.

Environment First-Best

- Planner problem

Environment First-Best

- Planner problem
- Two efficiency conditions

$$u_{c,t} A_t F_{n,t} = u_{l,t} \quad (3)$$

$$u_{c,t} = \beta u_{c,t+1} [A_{t+1} F_{k,t+1} + 1 - \delta] \quad (4)$$

Competitive Equilibrium with Taxes

Three agents

- Representative household
- Representative firm
- Government

Competitive Equilibrium with Taxes

Government

- Government

- Spending g_t
- Public debt b_t , labor tax τ_t^n , capital tax τ_t^k , lump-sum taxes T_t
- b_0 given

Competitive Equilibrium with Taxes

Government

■ Government

- Spending g_t
- Public debt b_t , labor tax τ_t^n , capital tax τ_t^k , lump-sum taxes T_t
- b_0 given

■ Budget constraint:

$$g_t + b_t = \tau_t^k r_t k_t + \tau_t^n w_t n_t + b_{t+1}/R_t + T_t \quad (5)$$

where r_t : renting price of capital, w_t : price of labor, R_t : gross rate of return on one-period bonds from t to $t + 1$.

Competitive Equilibrium with Taxes

Households

- Household

- Save in b_t and k_t
- b_0 and k_0 given

Competitive Equilibrium with Taxes

Households

- Household

- Save in b_t and k_t
- b_0 and k_0 given

- Maximizes utility given budget constraint:

$$c_t + k_{t+1} + b_{t+1}/R_t = (1 - \tau_t^n)w_t n_t + (1 - \tau_t^k)r_t k_t - T_t + (1 - \delta)k_t + b_t \quad (6)$$

Competitive Equilibrium with Taxes

Households

- Household's maximization problem

Competitive Equilibrium with Taxes

Households

- Household's maximization problem

$$u_{l,t} = u_{c,t} w_t (1 - \tau_t^n) \quad (7)$$

$$u_{c,t} = \beta u_{c,t+1} [(1 - \tau_{t+1}^k) r_{t+1} + 1 - \delta] \quad (8)$$

$$R_t = (1 - \tau_{t+1}^k) r_{t+1} + 1 - \delta \quad (9)$$

Competitive Equilibrium with Taxes Firms

The representative firm is standard and maximizes its profit every period:

$$r_t = A_t F_{k,t} \quad (10)$$

$$w_t = A_t F_{n,t} \quad (11)$$

Competitive Equilibrium with Taxes Definition

Let $x \equiv \{x_t\}_{t=0}^{\infty}$.

Definition

A **feasible allocation** is a sequence (k, c, n, g) such that the resource constraint (2) holds $\forall t \geq 0$.

Competitive Equilibrium with Taxes

Definition

Let $x \equiv \{x_t\}_{t=0}^{\infty}$.

Definition

A **feasible allocation** is a sequence (k, c, n, g) such that the resource constraint (2) holds $\forall t \geq 0$.

Definition

A **price system** is a non-negative bounded sequence (w, r, R) .

Definition

A **government policy system** is a sequence $(g, \tau_k, \tau_n, T, b)$.

Competitive Equilibrium with Taxes

Definition

Definition

A **competitive equilibrium** is a **feasible** allocation, a price system, and a government policy, such that:

- a. Given the price system and the government policy, the allocation solves the firm's problem and the household's problem

- b. Given the allocation and the price system, the government policy satisfies the sequence of government budget constraints (5).

Competitive Equilibrium with Taxes

Definition

Definition

A **competitive equilibrium** is a **feasible** allocation, a price system, and a government policy, such that:

- a. Given the price system and the government policy, the allocation solves the firm's problem and the household's problem
 - b. Given the allocation and the price system, the government policy satisfies the sequence of government budget constraints (5).
-
- An infinity of CE! Why?

Competitive Equilibrium with Taxes

Distortions

Claim

The first-best allocation requires capital and labor taxes to be zero.

Competitive Equilibrium with Taxes

Distortions

Claim

The first-best allocation requires capital and labor taxes to be zero.

- Labor and capital taxes are said to be **distortionary**.
- What about τ_0^k ? What about lump-sum taxes?

Competitive Equilibrium with Taxes

Distortions

Claim

The first-best allocation requires capital and labor taxes to be zero.

- Labor and capital taxes are said to be **distortionary**.
- What about τ_0^k ? What about lump-sum taxes?

Claim

The first-best can be implemented by lump-sum taxes and balanced budget.

Competitive Equilibrium with Taxes

Distortions

Claim

The first-best allocation requires capital and labor taxes to be zero.

- Labor and capital taxes are said to be **distortionary**.
- What about τ_0^k ? What about lump-sum taxes?

Claim

The first-best can be implemented by lump-sum taxes and balanced budget.

Claim

Ricardian equivalence: the first-best allocation can be implemented by any path $\{b_t\}$ for debt, and $T_t = g_t + b_t - b_{t+1}/R_t$.

Ramsey Plan Definition

Government

- Choose **sequences** of tax rates at time-0
- Anticipate households' responses to tax plans
- Benevolent

Ramsey Plan Definition

Government

- Choose **sequences** of tax rates at time-0
- Anticipate households' responses to tax plans
- Benevolent

Definition

A Ramsey problem is to choose a competitive equilibrium which maximizes (ex ante) consumer welfare.

Ramsey Plan Definition

Government

- Choose **sequences** of tax rates at time-0
- Anticipate households' responses to tax plans
- Benevolent

Definition

A Ramsey problem is to choose a competitive equilibrium which maximizes (ex ante) consumer welfare.

- Rule-out lump-sum taxes and assume τ_0^k is given. Why?

Ramsey Plan Definition

- A Ramsey plan is a complicated problem
 - Choose allocations, price system, and government policy
 - To maximize utility (1)
 - S.T. all equations holds: resource (2), gov BC (5), HH BC (6) & FOC (7), (8), (9), Firm FOC (10), (11)

Ramsey Plan Definition

- A Ramsey plan is a complicated problem
 - Choose allocations, price system, and government policy
 - To maximize utility (1)
 - S.T. all equations holds: resource (2), gov BC (5), HH BC (6) & FOC (7), (8), (9), Firm FOC (10), (11)

⇒ Goal: to **simplify** the Ramsey plan

Ramsey Plan Simplify the problem

- First, we can ignore the household budget constraint

Ramsey Plan Simplify the problem

- First, we can ignore the household budget constraint
 - Euler theorem: $F(k, n) = F_k k + F_n n$

Ramsey Plan Simplify the problem

- First, we can ignore the household budget constraint

- Euler theorem: $F(k, n) = F_k k + F_n n$

- Resource constraint (2) + govt budget constraint

$$g_t + c_t + k_{t+1} = A_t F(k_t, n_t) + (1 - \delta) k_t \quad (2)$$

$$g_t + b_t = \tau_t^k r_t k_t + \tau_t^n w_t n_t + b_{t+1}/R_t \quad (5)$$

Ramsey Plan Simplify the problem

- Dual approach: use **after-tax prices**

- $\tilde{r}_t \equiv (1 - \tau_{kt})F_{k,t}$ and $\tilde{w}_t \equiv (1 - \tau_{nt})F_{n,t}$

- Solve for \tilde{r}_t and \tilde{w}_t instead of r_t and w_t

Ramsey Plan Simplify the problem

■ Dual approach: use **after-tax prices**

- $\tilde{r}_t \equiv (1 - \tau_{kt})F_{k,t}$ and $\tilde{w}_t \equiv (1 - \tau_{nt})F_{n,t}$
- Solve for \tilde{r}_t and \tilde{w}_t instead of r_t and w_t
- Get rid of two controls: τ_t^k and τ_t^n , and two FOC (firm)

Ramsey Plan Simplify the problem

- Dual approach: use **after-tax prices**

- $\tilde{r}_t \equiv (1 - \tau_{kt})F_{k,t}$ and $\tilde{w}_t \equiv (1 - \tau_{nt})F_{n,t}$
- Solve for \tilde{r}_t and \tilde{w}_t instead of r_t and w_t
- Get rid of two controls: τ_t^k and τ_t^n , and two FOC (firm)

- Rewrite government's budget constraint

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ u(c_t, 1 - n_t) + \right.$$

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ \begin{array}{l} u(c_t, 1 - n_t) + \\ + \Phi_t [A_t F(k_t, n_t) - \tilde{r}_t k_t - \tilde{w}_t n_t - g_t + b_{t+1}/R_t - b_t] + \end{array} \right\}$$

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ \begin{array}{l} u(c_t, 1 - n_t) + \\ + \Phi_t [A_t F(k_t, n_t) - \tilde{r}_t k_t - \tilde{w}_t n_t - g_t + b_{t+1}/R_t - b_t] + \\ + \lambda_t [A_t F(k_t, n_t) + (1 - \delta) k_t - k_{t+1} - c_t - g_t] \end{array} \right\}$$

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ \begin{array}{l} u(c_t, 1 - n_t) + \\ + \Phi_t [A_t F(k_t, n_t) - \tilde{r}_t k_t - \tilde{w}_t n_t - g_t + b_{t+1}/R_t - b_t] + \\ + \lambda_t [A_t F(k_t, n_t) + (1 - \delta) k_t - k_{t+1} - c_t - g_t] + \\ + \mu_{1t} [u_l(c_t, 1 - n_t) - u_c(c_t, 1 - n_t) \tilde{w}_t] + \\ + \mu_{2t} [u_c(c_t, 1 - n_t) - \beta u_c(c_{t+1}, 1 - n_{t+1}) (\tilde{r}_{t+1} + 1 - \delta)] \\ + \mu_{3t} [R_t - \tilde{r}_{t+1} + 1 - \delta] \end{array} \right.$$

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ \begin{array}{l} u(c_t, 1 - n_t) + \\ + \Phi_t [A_t F(k_t, n_t) - \tilde{r}_t k_t - \tilde{w}_t n_t - g_t + b_{t+1}/R_t - b_t] + \\ + \lambda_t [A_t F(k_t, n_t) + (1 - \delta) k_t - k_{t+1} - c_t - g_t] + \\ + \mu_{1t} [u_l(c_t, 1 - n_t) - u_c(c_t, 1 - n_t) \tilde{w}_t] + \\ + \mu_{2t} [u_c(c_t, 1 - n_t) - \beta u_c(c_{t+1}, 1 - n_{t+1}) (\tilde{r}_{t+1} + 1 - \delta)] \\ + \mu_{3t} [R_t - \tilde{r}_{t+1} + 1 - \delta] \end{array} \right\}$$

- No more taxes!
- What do I chose?
 - Allocations $\{c_t, k_{t+1}, n_t\}$ and after-tax prices $\{\tilde{w}_t, \tilde{r}_t, R_t\}$

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ \begin{array}{l} u(c_t, 1 - n_t) + \\ + \Phi_t [A_t F(k_t, n_t) - \tilde{r}_t k_t - \tilde{w}_t n_t - g_t + b_{t+1}/R_t - b_t] + \\ + \lambda_t [A_t F(k_t, n_t) + (1 - \delta) k_t - k_{t+1} - c_t - g_t] + \\ + \mu_{1t} [u_l(c_t, 1 - n_t) - u_c(c_t, 1 - n_t) \tilde{w}_t] + \\ + \mu_{2t} [u_c(c_t, 1 - n_t) - \beta u_c(c_{t+1}, 1 - n_{t+1}) (\tilde{r}_{t+1} + 1 - \delta)] \\ + \mu_{3t} [R_t - \tilde{r}_{t+1} + 1 - \delta] \end{array} \right\}$$

- No more taxes!
- What do I chose?
 - Allocations $\{c_t, k_{t+1}, n_t\}$ and after-tax prices $\{\tilde{w}_t, \tilde{r}_t, R_t\}$
- Then I can compute taxes:

$$\begin{aligned}\tilde{r}_t &= (1 - \tau_t^k) r_t = (1 - \tau_t^k) F_k(n_t, k_t) \\ \tilde{w}_t &= (1 - \tau_t^n) w_t = (1 - \tau_t^n) F_n(n_t, k_t)\end{aligned}$$

Ramsey Plan Lagrangian

$$L = \sum_{t=0}^{\infty} \beta^t \left\{ \begin{array}{l} u(c_t, 1 - n_t) + \\ + \Phi_t [A_t F(k_t, n_t) - \tilde{r}_t k_t - \tilde{w}_t n_t - g_t + b_{t+1}/R_t - b_t] + \\ + \lambda_t [A_t F(k_t, n_t) + (1 - \delta)k_t - k_{t+1} - c_t - g_t] + \\ + \mu_{1t} [u_l(c_t, 1 - n_t) - u_c(c_t, 1 - n_t) \tilde{w}_t] + \\ + \mu_{2t} [u_c(c_t, 1 - n_t) - \beta u_c(c_{t+1}, 1 - n_{t+1}) (\tilde{r}_{t+1} + 1 - \delta)] \\ + \mu_{3t} [R_t - \tilde{r}_{t+1} + 1 - \delta] \end{array} \right\}$$

Ramsey Plan Capital taxes in the long-run

- FOC w.r.t. k_{t+1}

$$\lambda_t = \beta [\Phi_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) - \tilde{r}_{t+1}) + \lambda_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) + 1 - \delta)]$$

Ramsey Plan Capital taxes in the long-run

- FOC w.r.t. k_{t+1}

$$\lambda_t = \beta [\Phi_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) - \tilde{r}_{t+1}) + \lambda_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) + 1 - \delta)]$$

- Long-run non-stochastic steady-state: $g_t = g$, $A_t = A$, assuming the steady-state converges

$$\lambda = \beta [\Phi (r - \tilde{r}) + \lambda(r + 1 - \delta)]$$

Ramsey Plan Capital taxes in the long-run

- FOC w.r.t. k_{t+1}

$$\lambda_t = \beta [\Phi_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) - \tilde{r}_{t+1}) + \lambda_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) + 1 - \delta)]$$

- Long-run non-stochastic steady-state: $g_t = g$, $A_t = A$, assuming the steady-state converges

$$\lambda = \beta [\Phi (r - \tilde{r}) + \lambda(r + 1 - \delta)]$$

- Households' Euler equation (8) in steady-state

$$1 = \beta ((1 - \delta) + \tilde{r})$$

Ramsey Plan Capital taxes in the long-run

- FOC w.r.t. k_{t+1}

$$\lambda_t = \beta [\Phi_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) - \tilde{r}_{t+1}) + \lambda_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) + 1 - \delta)]$$

- Long-run non-stochastic steady-state: $g_t = g$, $A_t = A$, assuming the steady-state converges

$$\lambda = \beta [\Phi (r - \tilde{r}) + \lambda(r + 1 - \delta)]$$

- Households' Euler equation (8) in steady-state

$$1 = \beta ((1 - \delta) + \tilde{r})$$

- Combining these equations

$$(\lambda + \Phi)(r - \tilde{r}) = 0$$

Ramsey Plan Capital taxes in the long-run

- FOC w.r.t. k_{t+1}

$$\lambda_t = \beta [\Phi_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) - \tilde{r}_{t+1}) + \lambda_{t+1} (A_{t+1} F_k(k_{t+1}, n_{t+1}) + 1 - \delta)]$$

- Long-run non-stochastic steady-state: $g_t = g$, $A_t = A$, assuming the steady-state converges

$$\lambda = \beta [\Phi (r - \tilde{r}) + \lambda(r + 1 - \delta)]$$

- Households' Euler equation (8) in steady-state

$$1 = \beta ((1 - \delta) + \tilde{r})$$

- Combining these equations

$$(\lambda + \Phi)(r - \tilde{r}) = 0$$

- Under some conditions, $\lambda + \Phi > 0 \Rightarrow r = \tilde{r} \Rightarrow \tau_k = 0$

Ramsey Plan Capital taxes should be zero...

- Capital should not be taxed in the long run!

Ramsey Plan Capital taxes should be zero...

- Capital should not be taxed in the long run!
 - How to finance g in the long-run? With labor taxes! (or assets?)

Ramsey Plan

Capital taxes should be zero...

- Capital should not be taxed in the long run!
 - How to finance g in the long-run? With labor taxes! (or assets?)
 - An **efficiency** argument

Ramsey Plan

Capital taxes should be zero... or one!

- Capital should not be taxed in the long run!
 - How to finance g in the long-run? With labor taxes! (or assets?)
 - An **efficiency** argument
- But in the short run... $\tau_0^k = \bar{\tau}!$
 - Terrible time-consistency problem

Ramsey Plan Should capital taxes really be zero??

- Straub and Werning (2020)

Ramsey Plan Should capital taxes really be zero??

- Straub and Werning (2020)
- Key argument: $\tau_k < \bar{\tau}$ in the long-run and an **interior steady-state** exists

Ramsey Plan Should capital taxes really be zero??

- Straub and Werning (2020)
- Key argument: $\tau_k < \bar{\tau}$ in the long-run and an **interior steady-state** exists
- Writing the constraint explicitly...
 - One more constraint in the Lagrangian:

$$\tilde{r}_t = (1 - \tau_t^k) F_k(k_t, n_t) \geq (1 - \bar{\tau}) F_k(k_t, n_t)$$

- One more multiplier...

Ramsey Plan Should capital taxes really be zero??

- Straub and Werning (2020)
- Key argument: $\tau_k < \bar{\tau}$ in the long-run and an **interior steady-state** exists
- Writing the constraint explicitly...
 - One more constraint in the Lagrangian:

$$\tilde{r}_t = (1 - \tau_t^k) F_k(k_t, n_t) \geq (1 - \bar{\tau}) F_k(k_t, n_t)$$

- One more multiplier...
- Is there an interior steady-state? Where all multipliers converge?
 - Depends on the intertemporal elasticity of substitution!

Ramsey Plan Should capital taxes really be zero??

- Straub and Werning (2020)
- Key argument: $\tau_k < \bar{\tau}$ in the long-run and an **interior steady-state** exists
- Writing the constraint explicitly...
 - One more constraint in the Lagrangian:

$$\tilde{r}_t = (1 - \tau_t^k) F_k(k_t, n_t) \geq (1 - \bar{\tau}) F_k(k_t, n_t)$$

- One more multiplier...
- Is there an interior steady-state? Where all multipliers converge?
 - Depends on the intertemporal elasticity of substitution!

⇒ Not **as general** as we thought it was...

Optimal Fiscal Policy in RBC Model

Taking stock

- Capital taxes should be zero...
- ...in the long-run, and under some conditions

2. Optimal Fiscal Policy in Standard Aiyagari Models

Fiscal policy in standard Aiyagari models

Capital taxes

- Optimal taxes with heterogeneity
 - Redistribution/insurance concerns

Fiscal policy in standard Aiyagari models

Capital taxes

- Optimal taxes with heterogeneity
 - Redistribution/insurance concerns
- Heterogeneous-agent model a la Aiyagari (1995)
 - Idiosyncratic income risk
 - Incomplete markets and borrowing constraints

Fiscal policy in standard Aiyagari models

Capital taxes

- Optimal taxes with heterogeneity
 - Redistribution/insurance concerns
- Heterogeneous-agent model a la Aiyagari (1995)
 - Idiosyncratic income risk
 - Incomplete markets and borrowing constraints
- Quantitative exercise
 - Calibration
 - Optimization on some parameters of the tax function

Fiscal policy in standard Aiyagari models

Capital taxes

- Optimal taxes with heterogeneity
 - Redistribution/insurance concerns
- Heterogeneous-agent model a la Aiyagari (1995)
 - Idiosyncratic income risk
 - Incomplete markets and borrowing constraints
- Quantitative exercise
 - Calibration
 - Optimization on some parameters of the tax function
- Environment; equilibrium; optimal policy

- J generations of households
 - Work until age J_r , then retired
 - Probability of survival ψ_j with $\psi_J = 0$

- J generations of households
 - Work until age J_r , then retired
 - Probability of survival ψ_j with $\psi_J = 0$
 - Unintended bequests redistributed lump-sum Tr
 - Born with zero wealth (but bequests)

- J generations of households

- Work until age J_r , then retired
- Probability of survival ψ_j with $\psi_J = 0$
- Unintended bequests redistributed lump-sum Tr
- Born with zero wealth (but bequests)

- Value consumption and labor:

$$\mathbb{E} \sum_{j=1}^J \beta^{j-1} u(c_j, n_j)$$

- Idiosyncratic productivity of agent with type i and age j : $\varepsilon_j \alpha_i \eta$
- Heterogeneity in several dimensions
 - Age j : ε_j captures the age-profile productivity, with $\varepsilon_j = 0 \forall j > J_r$
 - Type i : α_i distributed with probability p_i
 - Idiosyncratic shocks: η follows an AR(1) with probability Π

- Idiosyncratic productivity of agent with type i and age j : $\varepsilon_j \alpha_i \eta$
- Heterogeneity in several dimensions
 - Age j : ε_j captures the age-profile productivity, with $\varepsilon_j = 0 \forall j > J_r$
 - Type i : α_i distributed with probability p_i
 - Idiosyncratic shocks: η follows an AR(1) with probability Π
- Households can trade risk-free bonds a up to \underline{a}

- Idiosyncratic productivity of agent with type i and age j : $\varepsilon_j \alpha_i \eta$
- Heterogeneity in several dimensions
 - Age j : ε_j captures the age-profile productivity, with $\varepsilon_j = 0 \forall j > J_r$
 - Type i : α_i distributed with probability p_i
 - Idiosyncratic shocks: η follows an AR(1) with probability Π
- Households can trade risk-free bonds a up to \underline{a}
- Household state: (a, η, i, j)

- Technology

$$G_t + C_t + K_{t+1} - (1 - \delta)K_t = K_t^\alpha N_t^{1-\alpha} \quad (12)$$

- Aggregate stationary steady-state

- Aggregates are constant... but not idiosyncratic variables!

■ Social Security

- Lump-sum SS_t distributed to all **retired** households
- A tax on labor income τ_{ss} up to a cap \bar{y}

■ Social Security

- Lump-sum SS_t distributed to all **retired** households
- A tax on labor income τ_{ss} up to a cap \bar{y}

■ Exogenous spending G_t financed by

- A **linear** tax τ_k on **capital** income $r_t(A_t + Tr_t)$
- A linear tax τ_c on consumption c
- A **progressive** tax $T(\cdot)$ on taxable **labor** income $y_L - \tau_{ss}\min\{y_L, \bar{y}\}$ where $y_L = w\varepsilon_j\alpha_i\eta$

Competitive Equilibrium

Definition

A stationary recursive competitive equilibrium (RCE) is:

- a policy $\{G, \tau_c, \tau_k, T, \tau_{ss}, \bar{y}, SS\}$
- a policy for the firm $\{N, K\}$
- value and policy functions for the household $\{\nu(a, \eta, i, j), c(a, \eta, i, j), a'(a, \eta, i, j), n(a, \eta, i, j)\}$ and bequests (Tr)
- prices $\{w, r\}$ and a distribution $\Phi(a, \eta, i, j)$

s.t.:

Competitive Equilibrium

Definition

A **stationary recursive competitive equilibrium** (RCE) is:

- a policy $\{G, \tau_c, \tau_k, T, \tau_{ss}, \bar{y}, SS\}$
- a policy for the firm $\{N, K\}$
- value and policy functions for the household $\{\nu(a, \eta, i, j), c(a, \eta, i, j), a'(a, \eta, i, j), n(a, \eta, i, j)\}$ and bequests (Tr)
- prices $\{w, r\}$ and a distribution $\Phi(a, \eta, i, j)$

s.t.:

- Given prices and policies, the **household** behaves optimally:

$$\nu(a, \eta, i, j) = \max_{c, a', n} u(c, n) + \beta \psi_j \int_{\eta' | \eta} \nu(a', \eta', i, j+1) \pi(\eta' | \eta) \text{ s.t.}$$

$$(1 + \tau_c)c + a' = y_L - \tau_{ss} \min\{y_L, \bar{y}\} - T(y_L^T) + [1 + r(1 - \tau_k)](a + Tr) \text{ if } j < J_r, \text{ where } y_L = w\varepsilon_j \alpha_i \eta n$$

$$(1 + \tau_c)c + a' = ss + [1 + r(1 - \tau_k)](a + Tr) \text{ if } j \geq J_r$$

$$a' \geq \underline{a}$$

Competitive Equilibrium

Definition

2. Firms behave optimally:

$$r = \alpha \left(\frac{N}{K} \right)^{1-\alpha} - \delta, \text{ and } w = (1-\alpha) \left(\frac{K}{N} \right)^\alpha$$

Competitive Equilibrium

Definition

2. Firms behave optimally:

$$r = \alpha \left(\frac{N}{K} \right)^{1-\alpha} - \delta, \text{ and } w = (1-\alpha) \left(\frac{K}{N} \right)^\alpha$$

3. Social Security system is balanced:

$$\tau_{ss} \int \min\{w\alpha_i \varepsilon_j \eta n(a, \eta, i, j), \bar{y}\} \Phi(a, \eta, i, j) = SS \int \Phi(a, \eta, i, j \geq J_r)$$

Competitive Equilibrium

Definition

2. Firms behave optimally:

$$r = \alpha \left(\frac{N}{K} \right)^{1-\alpha} - \delta, \text{ and } w = (1-\alpha) \left(\frac{K}{N} \right)^\alpha$$

3. Social Security system is balanced:

$$\tau_{ss} \int \min\{w\alpha_i \varepsilon_j \eta n(a, \eta, i, j), \bar{y}\} \Phi(a, \eta, i, j) = SS \int \Phi(a, \eta, i, j \geq J_r)$$

4. Transfers solve:

$$Tr \int \Phi'(a, \eta, i, j) = \int (1 - \psi_j) a'(a, \eta, i, j) \Phi(a, \eta, i, j)$$

Competitive Equilibrium

Definition

2. Firms behave optimally:

$$r = \alpha \left(\frac{N}{K} \right)^{1-\alpha} - \delta, \text{ and } w = (1-\alpha) \left(\frac{K}{N} \right)^\alpha$$

3. Social Security system is balanced:

$$\tau_{ss} \int \min\{w\alpha_i \varepsilon_j \eta n(a, \eta, i, j), \bar{y}\} \Phi(a, \eta, i, j) = SS \int \Phi(a, \eta, i, j \geq J_r)$$

4. Transfers solve:

$$Tr \int \Phi'(a, \eta, i, j) = \int (1 - \psi_j) a'(a, \eta, i, j) \Phi(a, \eta, i, j)$$

5. The government's budget constraint holds:

$$\begin{aligned} G &= \int \tau_k r(a + Tr) \Phi(a, \eta, i, j) + \int T(y_L^T(\eta, i, j)) \Phi(a, \eta, i, j) \cdots \\ &\quad + \int \tau_c c(a, \eta, i, j) \Phi(a, \eta, i, j) \end{aligned}$$

Competitive Equilibrium

Definition

6. Markets clear:

$$K = \int a\Phi(a, \eta, i, j)$$
$$N = \int \varepsilon_j \alpha_i \eta n(a, \eta, i, j) \Phi(a, \eta, i, j)$$

Competitive Equilibrium

Definition

6. Markets clear:

$$K = \int a\Phi(a, \eta, i, j)$$
$$N = \int \varepsilon_j \alpha_i \eta n(a, \eta, i, j) \Phi(a, \eta, i, j)$$

7. The **measure** is stationary: $\forall \mathcal{J}$ s.t. 1 non in \mathcal{J} ,

$$\Phi(A \times E \times \mathcal{I} \times \mathcal{J}) = \int Q((a, \eta, i, j); A \times E \times \mathcal{I} \times \mathcal{J}) \Phi(a, \varepsilon, i, j)$$

where

$$Q(a, \eta, i, j; A \times E \times \mathcal{I} \times \mathcal{J}) = \dots$$
$$\psi_j \int \mathbf{1}_{(a' (a, \eta, i, j) \in A) \times (i \in \mathcal{I}) \times (j+1) \in \mathcal{J}} \sum_{\eta'} P(\eta' \in E | \eta) \Phi(a, \eta, i, j)$$

Calibration

■ Demographics

- Agents born at age 20, retire at age 65, die w.p.1 at age 100
- Survival probabilities: actuarial data

Calibration

■ Demographics

- Agents born at age 20, retire at age 65, die w.p.1 at age 100
- Survival probabilities: actuarial data

■ Preferences: : $u(c, n) = (c^\gamma(1 - n)^{1-\gamma})^{(1-\sigma)} / (1 - \sigma)$

- $\sigma = 4$, (β, γ) s.t. $K/Y = 2.7$ and $\int n = 1/3$

Calibration

■ Demographics

- Agents born at age 20, retire at age 65, die w.p.1 at age 100
- Survival probabilities: actuarial data

■ Preferences: : $u(c, n) = (c^\gamma(1 - n)^{1-\gamma})^{(1-\sigma)} / (1 - \sigma)$

- $\sigma = 4$, (β, γ) s.t. $K/Y = 2.7$ and $\int n = 1/3$

■ Technology: $\alpha = 0.36$, δ s.t. $\frac{I}{Y} = 25\%$

Calibration

■ Demographics

- Agents born at age 20, retire at age 65, die w.p.1 at age 100
- Survival probabilities: actuarial data

■ Preferences: : $u(c, n) = (c^\gamma(1 - n)^{1-\gamma})^{(1-\sigma)} / (1 - \sigma)$

- $\sigma = 4$, (β, γ) s.t. $K/Y = 2.7$ and $\int n = 1/3$

■ Technology: $\alpha = 0.36$, δ s.t. $\frac{I}{Y} = 25\%$

■ Heterogeneity

- Age-profile productivities $\{\epsilon_j\}$ follow Hansen (93)
- Two types $\{\alpha_i\}$
- Productivity $\{\eta\}$ follows Storesletten, Telmer, Yaron (04)

Calibration

■ Social Security

- $\tau_{ss} = 12.4\%$, \bar{y} : 2.5 of the average income
- SS to balance the budget constraint

Calibration

■ Social Security

- $\tau_{ss} = 12.4\%$, \bar{y} : 2.5 of the average income
- SS to balance the budget constraint

■ Government

- G s.t. $G/Y = 0.17$
- $\tau_c = 5\%$
- Total income (including capital) taxed a la Gouveia and Strauss (94)

$$T(y) = \kappa_0 \left(y - (y^{-\kappa_1} + \kappa_2)^{-\frac{1}{\kappa_1}} \right)$$

where κ_0 captures the average tax rate (26%), κ_1 level of progressivity (0.76), κ_2 solves the budget constraint

Calibration A comment on tax functions

- Often, capital income is taxed linearly at $\approx 30\%$

Calibration A comment on tax functions

- Often, capital income is taxed linearly at $\approx 30\%$
 - Short-run capital gains are taxed differently in the U.S.
 - Real estate is taxed linearly
 - Corporate profits are taxed linearly
 - Measurement issues...

Results Optimal plan

- Main experiment: optimize on $\tau_k, \kappa_0, \kappa_1$
 - Find κ_2 s.t. the government's budget constraint holds

Results Optimal plan

- Main experiment: optimize on $\tau_k, \kappa_0, \kappa_1$
 - Find κ_2 s.t. the government's budget constraint holds
- Optimal parameters
 - Progressive labor tax: $\kappa_0 = 0.23$, $\kappa_1 \approx 7$ i.e. flat tax rate of 23% with a deduction of about 15% of mean income

Results Optimal plan

- Main experiment: optimize on $\tau_k, \kappa_0, \kappa_1$
 - Find κ_2 s.t. the government's budget constraint holds
- Optimal parameters
 - Progressive labor tax: $\kappa_0 = 0.23$, $\kappa_1 \approx 7$ i.e. flat tax rate of 23% with a deduction of about 15% of mean income
 - Positive capital tax: $\tau_k = 36\%$

Results Why are capital taxes positive?

- Life cycle motives

Results Why are capital taxes positive?

■ Life cycle motives

- OLG: households may work too much at early age
 - + To accumulate wealth and finance retirement

Results Why are capital taxes positive?

■ Life cycle motives

- OLG: households may work too much at early age
 - + To accumulate wealth and finance retirement
- Optimal labor tax is **age-dependent**
 - + Typically, high for the young, low for the old

Results Why are capital taxes positive?

■ Life cycle motives

- OLG: households may work too much at early age
 - + To accumulate wealth and finance retirement
- Optimal labor tax is **age-dependent**
 - + Typically, high for the young, low for the old
- Restrictions: no age-dependent taxes
 - + Progressive labor taxes and positive capital taxes

Results Why are capital taxes positive?

■ Life cycle motives

- OLG: households may work too much at early age
 - + To accumulate wealth and finance retirement
- Optimal labor tax is **age-dependent**
 - + Typically, high for the young, low for the old
- Restrictions: no age-dependent taxes
 - + Progressive labor taxes and positive capital taxes

■ Insurance motives

Results Why are capital taxes positive?

■ Life cycle motives

- OLG: households may work too much at early age
 - + To accumulate wealth and finance retirement
- Optimal labor tax is **age-dependent**
 - + Typically, high for the young, low for the old
- Restrictions: no age-dependent taxes
 - + Progressive labor taxes and positive capital taxes

■ Insurance motives

- Incomplete markets generates overaccumulation of capital

Results Why are capital taxes positive?

■ Life cycle motives

- OLG: households may work too much at early age
 - + To accumulate wealth and finance retirement
- Optimal labor tax is **age-dependent**
 - + Typically, high for the young, low for the old
- Restrictions: no age-dependent taxes
 - + Progressive labor taxes and positive capital taxes

■ Insurance motives

- Incomplete markets generates overaccumulation of capital

■ Redistribution motives

- Tax capital to lower labor taxes

Results Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components
 - Drop η -shocks and α -types, retain ϵ -profiles and social security
 - **Recalibrate** the model

Results

Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components
 - Drop η -shocks and α -types, retain ϵ -profiles and social security
 - **Recalibrate** the model
 - Optimize on τ_k and κ_0 (assuming flat labor tax)

Results

Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components
 - Drop η -shocks and α -types, retain ϵ -profiles and social security
 - **Recalibrate** the model
 - Optimize on τ_k and κ_0 (assuming flat labor tax) $\Rightarrow \tau_k = 34\%$

Results Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components
 - Drop η -shocks and α -types, retain ϵ -profiles and social security
 - **Recalibrate** the model
 - Optimize on τ_k and κ_0 (assuming flat labor tax) $\Rightarrow \tau_k = 34\%$
- Add **redistribution** purposes
 - Add α -types and **recalibrate**
 - Optimize on τ_k , κ_0 **and** κ_1

Results Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components
 - Drop η -shocks and α -types, retain ϵ -profiles and social security
 - **Recalibrate** the model
 - Optimize on τ_k and κ_0 (assuming flat labor tax) $\Rightarrow \tau_k = 34\%$
- Add **redistribution** purposes
 - Add α -types and **recalibrate**
 - Optimize on τ_k , κ_0 **and** κ_1 $\Rightarrow \tau_k = 32\%$

Results Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components

- Drop η -shocks and α -types, retain ϵ -profiles and social security
- **Recalibrate** the model
- Optimize on τ_k and κ_0 (assuming flat labor tax) $\Rightarrow \tau_k = 34\%$

- Add **redistribution** purposes

- Add α -types and **recalibrate**
- Optimize on τ_k , κ_0 **and** κ_1 $\Rightarrow \tau_k = 32\%$

- Add **insurance** purposes

- Add η -shock and a and **recalibrate**

Results Why are capital taxes positive?

Quantitative decomposition

- Evaluate **life-cycle** components

- Drop η -shocks and α -types, retain ϵ -profiles and social security
- **Recalibrate** the model
- Optimize on τ_k and κ_0 (assuming flat labor tax) $\Rightarrow \tau_k = 34\%$

- Add **redistribution** purposes

- Add α -types and **recalibrate**
- Optimize on τ_k , κ_0 **and** κ_1 $\Rightarrow \tau_k = 32\%$

- Add **insurance** purposes

- Add η -shock and a and **recalibrate** $\Rightarrow \tau_k = 36\%$

Results Why are capital taxes positive?

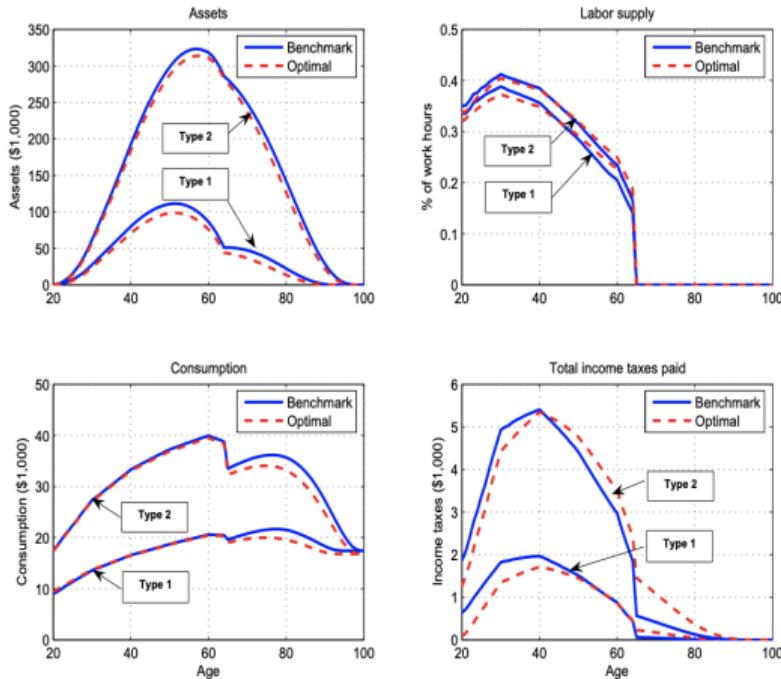


Figure 1: Life Cycle Profiles of Assets, Labor Supply, Consumption and Taxes

Results Why are capital taxes positive?

- It's all about life-cycle motives!

Results Why are capital taxes positive?

- It's all about life-cycle motives!
- Extensive robustness checks
 - Less elastic labor supply decreases τ_k

Results

Why are capital taxes positive?

- It's all about **life-cycle** motives!

- Extensive robustness checks
 - Less elastic labor supply decreases τ_k
 - Robustness w.r.t.: *IES*, D/GDP , social welfare function, U , ...
 - No transitions **(!!!)**

3. Heterogeneous Capital Returns

Taxing capital? An ongoing debate

- Wealth inequality is very large in the data
 - Top-10% owns 65% of wealth, top-1% owns 34% (SCF 2004)

Taxing capital? An ongoing debate

- Wealth inequality is very large in the data
 - Top-10% owns 65% of wealth, top-1% owns 34% (SCF 2004)
 - (Depends on the exact definition of wealth, depends on the years, depends on how you impute wealth to the top-1%...)
 - Saez Zucman: the top 0.1% holds 20% of the economy's net worth

Taxing capital? An ongoing debate

- Wealth inequality is very large in the data
 - Top-10% owns 65% of wealth, **top-1% owns 34%** (SCF 2004)
 - (Depends on the exact definition of wealth, depends on the years, depends on how you impute wealth to the top-1%...)
 - Saez Zucman: the top 0.1% holds 20% of the economy's net worth
 - Wealth distribution is **much more skewed than income distribution**

Taxing capital? An ongoing debate

■ Wealth inequality is very large in the data

- Top-10% owns 65% of wealth, **top-1% owns 34%** (SCF 2004)
- (Depends on the exact definition of wealth, depends on the years, depends on how you impute wealth to the top-1%...)
- Saez Zucman: the top 0.1% holds 20% of the economy's net worth
- Wealth distribution is **much more skewed than income distribution**

■ Policy: Taxing capital to redistribute?

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model **fails** to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes
 - De Nardi and Fella (2017)
 - + Earnings,

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes
 - De Nardi and Fella (2017)
 - + Earnings, bequests,

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes
 - De Nardi and Fella (2017)
 - + Earnings, bequests, discount rates,

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes
 - De Nardi and Fella (2017)
 - + Earnings, bequests, discount rates, health shocks...

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes
 - De Nardi and Fella (2017)
 - + Earnings, bequests, discount rates, health shocks...
 - + Entrepreneurship,

Understanding capital? Mechanisms of accumulation

- Basic Aiyagari model fails to generate realistic wealth distributions
 - Standard log-AR(1) process (Floden and Lindé 2001) & preferences

	Q1	Q2	Q3	Q4	Q5	Top 10%	Top 1%
Data (04)	-0%	1%	4%	12%	83%	65%	34%
Model	0%	4%	12%	25%	58%	37%	6%

- An example from my own research
- Why do some households save so much?
 - Exact mechanisms matter for taxation purposes
 - De Nardi and Fella (2017)
 - + Earnings, bequests, discount rates, health shocks...
 - + Entrepreneurship, and more generally, heterogeneous capital returns

Heterogeneous returns Theory

- Heterogeneous capital returns: most promising theoretical avenue
 - Can generate **fat tails** in wealth distribution
 - Benhabib, Bisin, and Zhu (2011), Benhabib, Bisin, and Luo (2019)
 - Gabaix, Lasry, Lions, and Moll (2016)

Heterogeneous returns Theory

- Heterogeneous capital returns: most promising theoretical avenue
 - Can generate **fat tails** in wealth distribution
 - Benhabib, Bisin, and Zhu (2011), Benhabib, Bisin, and Luo (2019)
 - Gabaix, Lasry, Lions, and Moll (2016)
- Needed ingredients
 - **Persistent** idiosyncratic returns (even across generations)
 - + “*Type dependence*”

Heterogeneous returns Theory

- Heterogeneous capital returns: most promising theoretical avenue
 - Can generate **fat tails** in wealth distribution
 - Benhabib, Bisin, and Zhu (2011), Benhabib, Bisin, and Luo (2019)
 - Gabaix, Lasry, Lions, and Moll (2016)
- Needed ingredients
 - **Persistent** idiosyncratic returns (even across generations)
 - + “*Type dependence*”
 - **Correlation** of wealth and returns
 - + “*Scale dependence*”

Heterogeneous returns Theory

- Heterogeneous capital returns: most promising theoretical avenue
 - Can generate **fat tails** in wealth distribution
 - Benhabib, Bisin, and Zhu (2011), Benhabib, Bisin, and Luo (2019)
 - Gabaix, Lasry, Lions, and Moll (2016)
- Needed ingredients
 - **Persistent** idiosyncratic returns (even across generations)
 - + “*Type dependence*”
 - **Correlation** of wealth and returns
 - + “*Scale dependence*”
- Plausible in the data?

Heterogeneous capital returns Data

Fagereng, Guiso, Malacrino, and Pistaferri (2020)

- Norwegian administrative data
 - Individual tax records 2004-2015
 - + Labor and capital **income**
 - + **Asset holdings and liabilities**

Heterogeneous capital returns Data

Fagereng, Guiso, Malacrino, and Pistaferri (2020)

- Norwegian administrative data

- Individual tax records 2004-2015
 - + Labor and capital **income**
 - + **Asset holdings and liabilities**
- Private business balance sheet
- Housing transactions registry
- Data on deposits and loans

- Compute individual returns to wealth

Heterogeneous capital returns Data

- Very heterogeneous returns on wealth

- Large **heterogeneity**: standard deviation 22.1%
- Large **scale dependence**: from net worth-10th to 90th, returns +18pp
- Strong **persistence** across generations

Heterogeneous capital returns

Data

- Very heterogeneous returns on wealth

- Large **heterogeneity**: standard deviation 22.1%
- Large **scale dependence**: from net worth-10th to 90th, returns +18pp
- Strong **persistence** across generations

- Where does heterogeneity come from?

- Portfolio: exposure to risk (Swedish data...)
- Type: heterogeneity within narrow classes of assets

Heterogeneous capital returns

Data

- Very heterogeneous returns on wealth

- Large **heterogeneity**: standard deviation 22.1%
- Large **scale dependence**: from net worth-10th to 90th, returns +18pp
- Strong **persistence** across generations

- Where does heterogeneity come from?

- Portfolio: exposure to risk (Swedish data...)
- Type: heterogeneity within narrow classes of assets

⇒ Implications for taxation?

Implications for taxation

- Under **homogenous returns**, **taxing capital = taxing wealth**

$$(1 + r(1 - \tau_k))a_i = (1 - \tau_a)(1 + r)a_i$$

- τ_k is a tax on capital income
- τ_a is a tax on the stock of capital (wealth)

Implications for taxation

- Under **homogenous returns**, **taxing capital = taxing wealth**

$$(1 + r(1 - \tau_k))a_i = (1 - \tau_a)(1 + r)a_i$$

- τ_k is a tax on capital income
- τ_a is a tax on the stock of capital (wealth)
 - + Equivalent as long as $\tau_a = \tau_k r / (1 + r)$

Implications for taxation

- Under **homogenous returns**, **taxing capital = taxing wealth**

$$(1 + r(1 - \tau_k))a_i = (1 - \tau_a)(1 + r)a_i$$

- τ_k is a tax on capital income
- τ_a is a tax on the stock of capital (wealth)
 - + Equivalent as long as $\tau_a = \tau_k r / (1 + r)$

- What if returns are **heterogeneous**?

$$(1 + r_i(1 - \tau_k))a_i \text{ vs. } (1 - \tau_a)(1 + r_i)a_i$$

- Guvenen et al. (2023)

“Use it or lose it!” A simple idea

- Assume two agents, a and b
 - Same wealth $k = \$1000$; but **different returns**: $r^a = 0 < r^b = 0.2$

“Use it or lose it!” A simple idea

- Assume two agents, a and b
 - Same wealth $k = \$1000$; but **different returns**: $r^a = 0 < r^b = 0.2$
- Policy 1: $\tau^k = 10\%$ on capital income
 - Agent a pays no taxes
 - Agent b pays $10\% \times 20\% \times 1000 = \20

“Use it or lose it!” A simple idea

- Assume two agents, a and b
 - Same wealth $k = \$1000$; but **different returns**: $r^a = 0 < r^b = 0.2$
- Policy 1: $\tau^k = 10\%$ on capital income
 - Agent a pays no taxes
 - Agent b pays $10\% \times 20\% \times 1000 = \20
- (**Revenue-neutral**) policy 2: $\tau^a = 0.91\%$ tax rate on wealth
 - Agent a pays $0.91\% \times 1000 = \$9.10$
 - Agent b pays $0.91\% \times (1000 + 200) = \10.90
- A **wealth** tax shifts the tax burden **away** from the **more productive** hh

“Use it or lose it!” A simple idea

- Assume two agents, a and b
 - Same wealth $k = \$1000$; but **different returns**: $r^a = 0 < r^b = 0.2$
- Policy 1: $\tau^k = 10\%$ on capital income
 - Agent a pays no taxes
 - Agent b pays $10\% \times 20\% \times 1000 = \20
- (**Revenue-neutral**) policy 2: $\tau^a = 0.91\%$ tax rate on wealth
 - Agent a pays $0.91\% \times 1000 = \$9.10$
 - Agent b pays $0.91\% \times (1000 + 200) = \10.90
- A **wealth** tax shifts the tax burden **away** from the **more productive** hh
 - Good for efficiency

“Use it or lose it!” A simple idea

- Assume two agents, a and b
 - Same wealth $k = \$1000$; but **different returns**: $r^a = 0 < r^b = 0.2$
- Policy 1: $\tau^k = 10\%$ on capital income
 - Agent a pays no taxes
 - Agent b pays $10\% \times 20\% \times 1000 = \20
- (**Revenue-neutral**) policy 2: $\tau^a = 0.91\%$ tax rate on wealth
 - Agent a pays $0.91\% \times 1000 = \$9.10$
 - Agent b pays $0.91\% \times (1000 + 200) = \10.90
- A **wealth** tax shifts the tax burden **away** from the **more productive** hh
 - Good for efficiency, bad for redistribution?

“Use it or lose it!”

Three channels

In a dynamic general-equilibrium model

1. “Use-it-or-lose-it” channel
 - Capital reallocates toward more productive entrepreneurs

“Use it or lose it!”

Three channels

In a dynamic general-equilibrium model

1. “Use-it-or-lose-it” channel
 - Capital reallocates toward more productive entrepreneurs
2. “Behavior response” channel
 - More productive entrepreneurs will save more

“Use it or lose it!”

Three channels

In a dynamic general-equilibrium model

1. “Use-it-or-lose-it” channel
 - Capital reallocates toward more productive entrepreneurs
2. “Behavior response” channel
 - More productive entrepreneurs will save more
3. “Price” channel
 - Wages and interest rates will adjust

Environment Demographics

- Overlapping generations (OLG) model
 - Age h , live up to H years
 - Wealth inheritance (no bequests motives)

Environment Demographics

- Overlapping generations (OLG) model
 - Age h , live up to H years
 - Wealth inheritance (no bequests motives)
- Households make three decisions
 - Endogenous **labor** until retirement R

Environment Demographics

- Overlapping generations (OLG) model
 - Age h , live up to H years
 - Wealth inheritance (no bequests motives)
- Households make three decisions
 - Endogenous **labor** until retirement R
 - **Consumption**-savings decision

Environment Demographics

- Overlapping generations (OLG) model

- Age h , live up to H years
 - Wealth inheritance (no bequests motives)

- Households make three decisions

- Endogenous **labor** until retirement R
 - **Consumption**-savings decision
 - **Portfolio** choice
 - + Choose how much to invest in own technology ("entrepreneurship")

Environment Households

- Labor productivity w_{ih} s.t. $\log w_{ih} = \kappa_i + g(h) + e_{ih}$

Environment Households

■ Labor **productivity** w_{ih} s.t. $\log w_{ih} = \kappa_i + g(h) + e_{ih}$

- Type: κ_i imperfectly inherited from parents
- Age-profile $g(h)$
- Idiosyncratic shock: e_{ih} follows an AR(1)

Environment Households

■ Labor **productivity** w_{ih} s.t. $\log w_{ih} = \kappa_i + g(h) + e_{ih}$

- Type: κ_i imperfectly inherited from parents
- Age-profile $g(h)$
- Idiosyncratic shock: e_{ih} follows an AR(1)

■ Social security: $y^R(\kappa, e) = \phi(\kappa, e)\bar{E}$ when $h > R$

Environment Households

■ Labor **productivity** w_{ih} s.t. $\log w_{ih} = \kappa_i + g(h) + e_{ih}$

- Type: κ_i imperfectly inherited from parents
- Age-profile $g(h)$
- Idiosyncratic shock: e_{ih} follows an AR(1)

■ Social security: $y^R(\kappa, e) = \phi(\kappa, e)\bar{E}$ when $h > R$

■ Entrepreneurial **ability** z_{ih}

- Type: \bar{z}_i imperfectly inherited from parents

Environment Households

■ Labor **productivity** w_{ih} s.t. $\log w_{ih} = \kappa_i + g(h) + e_{ih}$

- Type: κ_i imperfectly inherited from parents
- Age-profile $g(h)$
- Idiosyncratic shock: e_{ih} follows an AR(1)

■ Social security: $y^R(\kappa, e) = \phi(\kappa, e)\bar{E}$ when $h > R$

■ Entrepreneurial **ability** z_{ih}

- Type: \bar{z}_i imperfectly inherited from parents
- **Stochastic process** $\mathbb{I}_{ih} \in \{\mathcal{H}, \mathcal{L}, 0\}$

$$z_{ih} = \begin{cases} (\bar{z}_i)^\lambda & \text{if } \mathbb{I}_{ih} = \mathcal{H} \\ \bar{z}_i & \text{if } \mathbb{I}_{ih} = \mathcal{L} \\ 0 & \text{if } \mathbb{I}_{ih} = 0 \end{cases} \quad \text{with } \lambda > 1 : \text{"fast-lane" entrepreneurs}$$

Environment Households

■ Labor **productivity** w_{ih} s.t. $\log w_{ih} = \kappa_i + g(h) + e_{ih}$

- Type: κ_i imperfectly inherited from parents
- Age-profile $g(h)$
- Idiosyncratic shock: e_{ih} follows an AR(1)

■ Social security: $y^R(\kappa, e) = \phi(\kappa, e)\bar{E}$ when $h > R$

■ Entrepreneurial **ability** z_{ih}

- Type: \bar{z}_i imperfectly inherited from parents
- **Stochastic process** $\mathbb{I}_{ih} \in \{\mathcal{H}, \mathcal{L}, 0\}$

$$z_{ih} = \begin{cases} (\bar{z}_i)^\lambda & \text{if } \mathbb{I}_{ih} = \mathcal{H} \\ \bar{z}_i & \text{if } \mathbb{I}_{ih} = \mathcal{L} \\ 0 & \text{if } \mathbb{I}_{ih} = 0 \end{cases} \quad \text{with } \lambda > 1 : \text{"fast-lane" entrepreneurs}$$

- Stochastic transition **downwards**

Environment Production

■ Final good: $Y = Q^\alpha L^{1-\alpha}$

- Aggregate labor L , with $\alpha = 0.4$
- Intermediates: $Q = (\int x_{ih}^\mu)^{\frac{1}{\mu}}$, with $\mu = 0.9$
- Competitive sector

■ Intermediate goods: $x_{ih} = z_{ih} k_{ih}$

- Price $p_{ih} = \alpha x_{ih}^{\mu-1} Q^{\alpha-\mu} L^{1-\alpha}$

Environment Household problem and equilibrium

1. Choose capital to max profits

$$\pi(a, z) = \max_{k \leq v(z)a} p(zk)zk - (r + \delta)k$$

- Financial friction which generates misallocation
- Invests more if z is higher and if a is higher

Environment Household problem and equilibrium

1. Choose **capital** to max profits

$$\pi(a, z) = \max_{k \leq \nu(z)a} p(zk)zk - (r + \delta)k$$

- **Financial friction** which generates misallocation
- Invests more if z is higher and if a is higher

2. Choose how much to **work** (when $h \leq R$), **consume**, and **save** in assets

$$V_h(a, \bar{z}, \mathcal{I}, e, \kappa) = \max_{c, n, a'} u(c, n) + \beta s_{h+1} \mathbb{E} [V_{h+1}(a', \bar{z}, \mathcal{I}', e', \kappa)]$$

Environment Household problem and equilibrium

1. Choose capital to max profits

$$\pi(a, z) = \max_{k \leq \nu(z)a} p(zk)zk - (r + \delta)k$$

- Financial friction which generates misallocation
- Invests more if z is higher and if a is higher

2. Choose how much to work (when $h \leq R$), consume, and save in assets

$$V_h(a, \bar{z}, \mathcal{I}, e, \kappa) = \max_{c, n, a'} u(c, n) + \beta s_{h+1} \mathbb{E}[V_{h+1}(a', \bar{z}, \mathcal{I}', e', \kappa)]$$

such that

$$(1 + \tau_c)c + a' = (1 - \tau_\ell)\bar{w}w(\kappa, e)n + a + (1 - \tau_k)(\pi(a, z(\bar{z}, \mathcal{I})) + ra)$$

Environment Household problem and equilibrium

1. Choose capital to max profits

$$\pi(a, z) = \max_{k \leq \nu(z)a} p(zk)zk - (r + \delta)k$$

- Financial friction which generates misallocation
- Invests more if z is higher and if a is higher

2. Choose how much to work (when $h \leq R$), consume, and save in assets

$$V_h(a, \bar{z}, \mathcal{I}, e, \kappa) = \max_{c, n, a'} u(c, n) + \beta s_{h+1} \mathbb{E}[V_{h+1}(a', \bar{z}, \mathcal{I}', e', \kappa)]$$

such that

$$(1 + \tau_c)c + a' = (1 - \tau_\ell)\bar{w}w(\kappa, e)n + a + (1 - \tau_k)(\pi(a, z(\bar{z}, \mathcal{I})) + ra) \\ \dots + (1 - \tau_a)(a + (\pi(a, z(\bar{z}, \mathcal{I})) + ra))$$

Environment Household problem and equilibrium

1. Choose capital to max profits

$$\pi(a, z) = \max_{k \leq \nu(z)a} p(zk)zk - (r + \delta)k$$

- Financial friction which generates misallocation
- Invests more if z is higher and if a is higher

2. Choose how much to work (when $h \leq R$), consume, and save in assets

$$V_h(a, \bar{z}, \mathcal{I}, e, \kappa) = \max_{c, n, a'} u(c, n) + \beta s_{h+1} \mathbb{E}[V_{h+1}(a', \bar{z}, \mathcal{I}', e', \kappa)]$$

such that

$$\begin{aligned} (1 + \tau_c)c + a' &= (1 - \tau_\ell)\bar{w}w(\kappa, e)n + a + (1 - \tau_k)(\pi(a, z(\bar{z}, \mathcal{I})) + ra) \\ &\quad \cdots + (1 - \tau_a)(a + (\pi(a, z(\bar{z}, \mathcal{I})) + ra)) \\ a' &\geq a \end{aligned}$$

Environment Household problem and equilibrium

1. Choose capital to max profits

$$\pi(a, z) = \max_{k \leq \nu(z)a} p(zk)zk - (r + \delta)k$$

- Financial friction which generates misallocation
- Invests more if z is higher and if a is higher

2. Choose how much to work (when $h \leq R$), consume, and save in assets

$$V_h(a, \bar{z}, \mathcal{I}, e, \kappa) = \max_{c, n, a'} u(c, n) + \beta s_{h+1} \mathbb{E}[V_{h+1}(a', \bar{z}, \mathcal{I}', e', \kappa)]$$

such that

$$\begin{aligned} (1 + \tau_c)c + a' &= (1 - \tau_\ell)\bar{w}w(\kappa, e)n + a + (1 - \tau_k)(\pi(a, z(\bar{z}, \mathcal{I})) + ra) \\ &\quad \cdots + (1 - \tau_a)(a + (\pi(a, z(\bar{z}, \mathcal{I})) + ra)) \\ a' &\geq a \end{aligned}$$

- Equilibrium: $\int a = \int k$

Calibration

- Dynamics of entrepreneurship to match fast wealth growth of super wealthy (Forbes 400)
- Standard earnings risk
- Taxes: $\tau_k = 25\%$, $\tau_\ell = 22.4\%$, $\tau_c = 7.5\%$

Calibration

- Dynamics of entrepreneurship to match fast wealth growth of super wealthy (Forbes 400)
 - Standard earnings risk
 - Taxes: $\tau_k = 25\%$, $\tau_\ell = 22.4\%$, $\tau_c = 7.5\%$
- ⇒ Generates high **wealth inequality!**

	top-50	top-10	top-1	top-0.5	top-0.1
Data	0.99	0.75	0.36	0.27	0.14
Model	0.97	0.66	0.36	0.31	0.23

- Data: SCF+Forbes 2010

Main experiment A wealth tax

Tax reform

- Set $\tau_k = 0$, balance budget with a **wealth tax**
 - Wealth tax $\tau_a = 1.13\%$

Main experiment A wealth tax

Tax reform

- Set $\tau_k = 0$, balance budget with a **wealth tax**
 - Wealth tax $\tau_a = 1.13\%$
- New economy features
 - Larger K : +20% → agents save more

Main experiment A wealth tax

Tax reform

- Set $\tau_k = 0$, balance budget with a **wealth tax**
 - Wealth tax $\tau_a = 1.13\%$
- New economy features
 - Larger K : +20% → agents save more
 - Larger Q : +25% → less misallocation

Main experiment A wealth tax

Tax reform

- Set $\tau_k = 0$, balance budget with a **wealth tax**
 - Wealth tax $\tau_a = 1.13\%$
- New economy features
 - Larger K : +20% → agents save more
 - Larger Q : +25% → less misallocation
 - Larger Y and C : +10%

Main experiment A wealth tax

Tax reform

- Set $\tau_k = 0$, balance budget with a **wealth tax**
 - Wealth tax $\tau_a = 1.13\%$
- New economy features
 - Larger K : +20% → agents save more
 - Larger Q : +25% → less misallocation
 - Larger Y and C : +10%
 - Higher **wages**, smaller net interest rates on the risk-free rate
 - Large **welfare gains**: +7.4%!

Main experiment A wealth tax

- Why does capital increase? Three channels

Main experiment A wealth tax

- Why does capital increase? Three channels
 - “Use-it-or-lose-it” [fixing prices & decision rules to benchmark] $K \uparrow$

Main experiment A wealth tax

- Why does capital increase? Three channels

- “Use-it-or-lose-it” [fixing prices & decision rules to benchmark] $K \uparrow$
- GE effects [with prices of new equilibrium] $K \downarrow$

Main experiment A wealth tax

- Why does capital increase? Three channels

- “Use-it-or-lose-it” [fixing prices & decision rules to benchmark] $K \uparrow$
- GE effects [with prices of new equilibrium] $K \downarrow$
- Behavioral responses [with new decision rules] $K \uparrow$

Main experiment A wealth tax

- Who wins from the reform?

Main experiment A wealth tax

- Who wins from the reform? Welfare gains by age and entrepreneurial ability

TABLE IX – Welfare Gain/Loss by Age Group and Entrepreneurial Ability

Age groups:	<i>Entrepreneurial Ability Groups (\bar{z}_i Percentiles)</i>					
	0–40	40–80	80–90	90–99	99–99.9	99.9+
	<i>RN Reform</i>					
20	7.0	7.3	7.9	8.9	10.6	11.7
21–34	6.5	6.3	6.3	6.6	7.0	6.8
35–49	5.1	4.4	3.9	3.3	1.7	0.1
50–64	2.3	1.8	1.4	0.8	-0.6	-1.8
65+	-0.2	-0.3	-0.4	-0.6	-1.2	-1.8

- The high-wealth/low- z (= the old) **lose**
- The young **benefit**...
 - + From $\tau_k = 0$ (high z)
 - + From higher w (low a)

Optimal taxation

Optimize steady-state fiscal system

- Optimal capital tax

- $\tau_k = -34\% (!), \tau_\ell = 36\%$

Optimal taxation

Optimize steady-state fiscal system

- Optimal **capital** tax

- $\tau_k = -34\% (!)$, $\tau_\ell = 36\%$

- Optimal **wealth** tax:

- $\tau_a = 3\%$, $\tau_\ell = 14\%$, much larger welfare gains

Optimal taxation

Optimize steady-state fiscal system

- Optimal **capital** tax

- $\tau_k = -34\% (!)$, $\tau_\ell = 36\%$

- Optimal **wealth** tax:

- $\tau_a = 3\%$, $\tau_\ell = 14\%$, much larger welfare gains

- Transitions

Taxing capital? Heterogeneous returns

- With heterogeneous capital returns, positive wealth tax
 - Mostly for efficiency reasons!

Taxing capital? Heterogeneous returns

- With heterogeneous capital returns, positive wealth tax
 - Mostly for **efficiency** reasons!
- What about redistribution?

Taxing capital? Heterogeneous returns

- With heterogeneous capital returns, positive wealth tax
 - Mostly for **efficiency** reasons!
- What about redistribution?
- A very active research field overall
 - Boar and Knowles (2020), Bhandari and McGrattan (2020), MacNamara, Pidkuyko, and Rossi (2021), **etc.**

Taxing capital? Heterogeneous returns

- With heterogeneous capital returns, positive wealth tax
 - Mostly for **efficiency** reasons!
- What about redistribution?
- A very active research field overall
 - Boar and Knowles (2020), Bhandari and McGrattan (2020), MacNamara, Pidkuyko, and Rossi (2021), **etc.**
 - Gaillard and Wangner (2023), Ferey, Lockwood, Taubinsky (2023), Guvenen et al. (2023b), **etc.!**

Taxing capital? Gaillard and Wangner (2023)

- On taxation and heterogeneous returns

- Productivity or rents?
 - Scale or type dependency?

⇒ Capital income or wealth taxation?

Taxing capital? Gaillard and Wangner (2023)

- On taxation and heterogeneous returns
 - Productivity or rents?
 - Scale or type dependency?
- ⇒ Capital income or wealth taxation?
- A follow up: Gaillard, Hellwig, Wangner, and Werquin (2024)
 - Non-homothetic utility

Lecture 2

Labor Taxes and Transfers

Should we tax labor? Yes! But how?

Should we tax labor? Yes! But how?

1. Optimal fiscal policy in **representative-agent** models

- Linear labor taxes to finance **spending** $G \dots$

Should we tax labor? Yes! But how?

1. Optimal fiscal policy in **representative-agent** models

- Linear labor taxes to finance **spending** G . . .
 . . . but not to absorb shocks: “smooth distortions!”
- Lucas Jr. and Stokey (1983), Aiyagari, Marcet, Sargent, and Seppälä (2002)

Should we tax labor? Yes! But how?

1. Optimal fiscal policy in **representative-agent** models

- Linear labor taxes to finance **spending** G ...
... but not to absorb shocks: "**smooth distortions!**"
 - Lucas Jr. and Stokey (1983), Aiyagari, Marcet, Sargent, and Seppälä (2002)

2. Optimal fiscal policy in **Aiyagari** models with **redistribution** motives

- Linear labor taxes to finance transfers T !
 - Floden and Lindé (2001)

Should we tax labor? Yes! But how?

1. Optimal fiscal policy in **representative-agent** models

- Linear labor taxes to finance **spending** G ...
- ... but not to absorb shocks: "**smooth distortions!**"
- Lucas Jr. and Stokey (1983), Aiyagari, Marcet, Sargent, and Seppälä (2002)

2. Optimal fiscal policy in **Aiyagari** models with **redistribution** motives

- Linear labor taxes to finance transfers T !
- Floden and Lindé (2001)
- Going further: **Progressive** taxes?

Optimal progressivity

Why should we care?

Optimal progressivity

Why should we care?

- Multiple trade-offs associated with progressivity

Optimal progressivity Why should we care?

- Multiple trade-offs associated with progressivity
 - Welfare gains
 - + Insurance, redistribution, etc.

Optimal progressivity

Why should we care?

- Multiple trade-offs associated with progressivity
 - Welfare gains
 - + Insurance, redistribution, etc.
 - Welfare costs
 - + Labor supply, investment in skills, etc.

Optimal progressivity

Why should we care?

- Multiple trade-offs associated with progressivity
 - Welfare gains
 - + Insurance, redistribution, etc.
 - Welfare costs
 - + Labor supply, investment in skills, etc.
 - General equilibrium effects

Optimal progressivity

Why should we care?

- Multiple trade-offs associated with progressivity

- Welfare gains
 - + Insurance, redistribution, etc.
- Welfare costs
 - + Labor supply, investment in skills, etc.
- General equilibrium effects

- Hard to analyze?

- A highly multi-dimensional object
- Computational?

The U.S. tax-and-transfer system

- Personal income taxes
 - Progressive taxes (brackets) on labor and capital income taxes

The U.S. tax-and-transfer system

- Personal income taxes
 - Progressive taxes (brackets) on labor and capital income taxes
 - + Deductions
 - + Long-run capital gains are partly exempted

The U.S. tax-and-transfer system

- Personal income taxes
 - Progressive taxes (brackets) on labor and capital income taxes
 - + Deductions
 - + Long-run capital gains are partly exempted
- Fiscal rebates
 - Tax credits: EITC, CTC, ...

The U.S. tax-and-transfer system

- Personal income taxes
 - Progressive taxes (brackets) on labor and capital income taxes
 - + Deductions
 - + Long-run capital gains are partly exempted
- Fiscal rebates
 - Tax credits: EITC, CTC, . . . partially refundable

The U.S. tax-and-transfer system

- Personal income taxes

- Progressive taxes (brackets) on labor and capital income taxes
 - + Deductions
 - + Long-run capital gains are partly exempted

- Fiscal rebates

- Tax credits: EITC, CTC, ... partially refundable
- Transfers: SNAP, TANF, ...

The U.S. tax-and-transfer system

- Personal income taxes

- Progressive taxes (brackets) on labor and capital income taxes
 - + Deductions
 - + Long-run capital gains are partly exempted

- Fiscal rebates

- Tax credits: EITC, CTC, . . . partially refundable
- Transfers: SNAP, TANF, . . . means-tested

The U.S. tax-and-transfer system

- Personal income taxes

- Progressive taxes (brackets) on labor and capital income taxes
 - + Deductions
 - + Long-run capital gains are partly exempted

- Fiscal rebates

- Tax credits: EITC, CTC, . . . partially refundable
- Transfers: SNAP, TANF, . . . means-tested

- Non-monetary transfers: spending on education, etc.

Optimal progressivity

Two approaches

Optimal progressivity Two approaches

■ Public finance: Mirrlees

- Fully flexible tax-and-transfer function
- Difficult to bring into rich quantitative models?

Optimal progressivity

Two approaches

■ Public finance: Mirrlees

- Fully flexible tax-and-transfer function
- Difficult to bring into rich quantitative models?

■ Macroeconomics: Ramsey

- Quantitatively realistic model
- But simple tax functions?

Optimal progressivity

Two approaches

■ Public finance: Mirrlees

- Fully flexible tax-and-transfer function
- Difficult to bring into rich quantitative models?

■ Macroeconomics: Ramsey

- Quantitatively realistic model
- But simple tax functions?

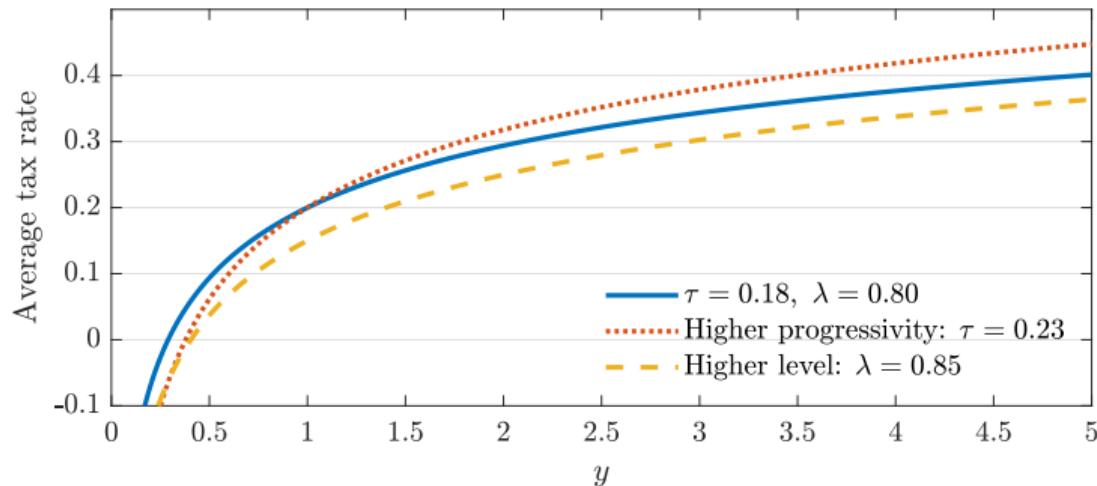
■ “New” approach: a rich Ramsey approach

- Heathcote, Storesletten, and Violante (2014), Heathcote, Storesletten, and Violante (2017)
- Heathcote and Tsuijiyama (2021a, 2021b)
- Ferriere, Grübener, Navarro, and Vardishvili (2023a)

1. Optimal Progressivity With Loglinear Income Taxes

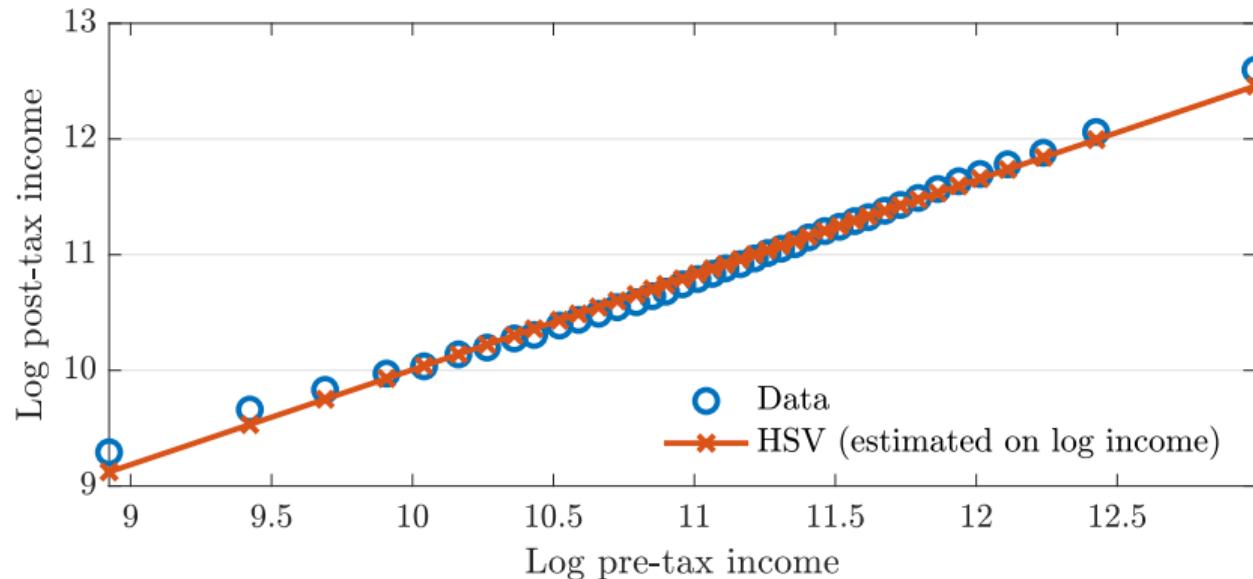
Loglinear tax function

- A loglinear tax scheme: $\mathcal{T}(y) = y - \lambda y^{1-\tau}$
- Tax progressivity is captured by τ
 - If $\tau = 0$: flat average (and marginal) tax rate $\mathcal{T}(y) = (1 - \lambda)y$
 - If $\tau > 0$: progressive tax
 - If $\tau = 1$: full redistribution $y - \mathcal{T}(y) = \lambda \quad \forall y$



- CPS 2013, working-age population
 - Total pre-tax income
 - **Minus** personal federal and state income taxes; payroll taxes
 - **Minus** payroll taxes (including employer share)
 - **Plus** tax credits
 - **Plus** SNAP and Housing Assistance (CBO imputation); Welfare
IPUMS CPS
Imputation of transfers following CBO Habib (2018)

Log-linear tax function



- Linear estimate on log income: $\log(y^{at}) = \log(\lambda) + (1 - \tau) \log(y)$
- Estimated progressivity $\tau = 0.18$

Log-linear tax function

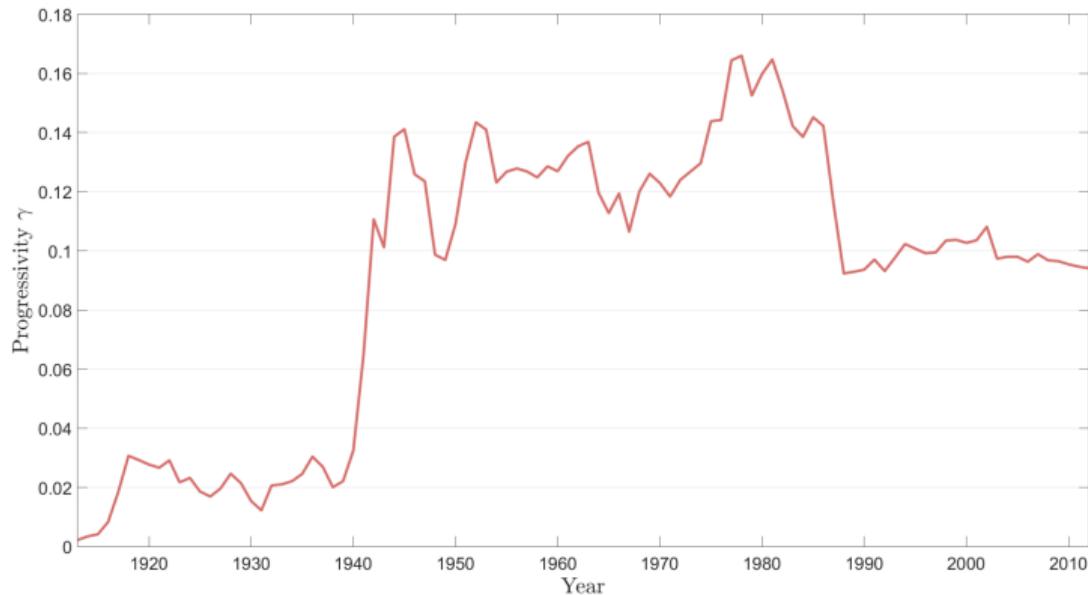


Figure 12: U.S. Federal Income Tax Progressivity

- A crude estimate over time Ferriere and Navarro (2023)

A tractable environment HSV (2017), FGNV (2023)

- No capital, representative **firm** with linear production function

A tractable environment HSV (2017), FGNV (2023)

- No capital, representative **firm** with linear production function
- **Utilitarian government**
 - Budget: $G = \int y_{it} di - \lambda \int y_{it}^{1-\tau} di$

A tractable environment

HSV (2017), FGNV (2023)

- No capital, representative **firm** with linear production function

- **Utilitarian government**

- Budget: $G = \int y_{it} di - \lambda \int y_{it}^{1-\tau} di$

- A continuum of **workers**

- Heterogenous **wages**: log-normal distribution with variance v_ω

- Separable **utility** function: $\log c_{it} - B \frac{n_{it}^{1+\varphi}}{1+\varphi}$

- **Hand-to-mouth** workers: $c_{it} = \lambda(z_{it} n_{it})^{1-\tau}$

Welfare Heterogeneous agents

- Policy function for **labor** is $n_{it} = [(1 - \tau)/B]^{\frac{1}{1+\varphi}} \equiv n_0(\tau)$

Welfare Heterogeneous agents

- Policy function for **labor** is $n_{it} = [(1 - \tau)/B]^{\frac{1}{1+\varphi}} \equiv n_0(\tau)$
- Compute Y , λ and c_{it} and obtain **welfare** in closed-form

$$\mathcal{W}(\tau) = \underbrace{\log(n_0(\tau) - G)}_{\text{Size}} - \underbrace{\frac{1-\tau}{1+\varphi}}_{\text{Labor disutility}} - \underbrace{(1-\tau)^2 \frac{v_\omega}{2}}_{\text{Redistribution}}$$

Efficiency

Welfare Heterogeneous agents

- Policy function for **labor** is $n_{it} = [(1 - \tau)/B]^{\frac{1}{1+\varphi}} \equiv n_0(\tau)$
- Compute Y , λ and c_{it} and obtain **welfare** in closed-form

$$\mathcal{W}(\tau) = \underbrace{\log(n_0(\tau) - G)}_{\text{Size}} - \underbrace{\frac{1-\tau}{1+\varphi}}_{\text{Labor disutility}} - \underbrace{(1-\tau)^2 \frac{v_\omega}{2}}_{\text{Redistribution}}$$

Efficiency

- Two **efficiency** terms
 - Size term \downarrow with τ ; Labor disutility term \uparrow with τ

Welfare Heterogeneous agents

- Policy function for **labor** is $n_{it} = [(1 - \tau)/B]^{\frac{1}{1+\varphi}} \equiv n_0(\tau)$
- Compute Y , λ and c_{it} and obtain **welfare** in closed-form

$$\mathcal{W}(\tau) = \underbrace{\log(n_0(\tau) - G)}_{\text{Size}} - \underbrace{\frac{1-\tau}{1+\varphi}}_{\text{Labor disutility}} - \underbrace{(1-\tau)^2 \frac{v_\omega}{2}}_{\text{Redistribution}}$$

Efficiency

- Two **efficiency** terms
 - Size term \downarrow with τ ; Labor disutility term \uparrow with τ
- **Redistribution** term \uparrow with τ

Welfare Heterogeneous agents

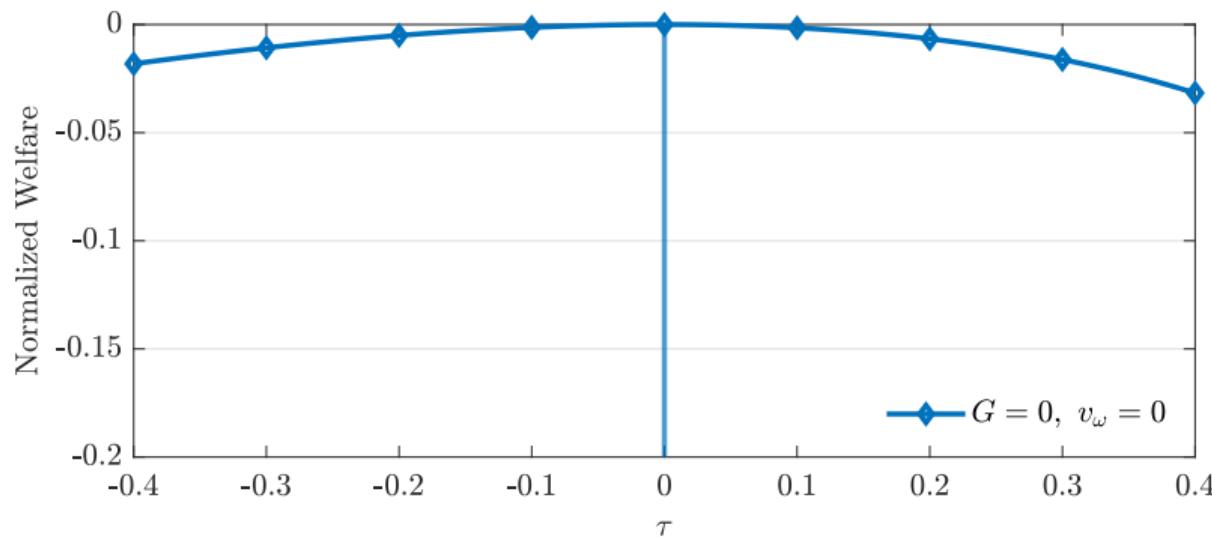
- Policy function for **labor** is $n_{it} = [(1 - \tau)/B]^{\frac{1}{1+\varphi}} \equiv n_0(\tau)$
- Compute Y , λ and c_{it} and obtain **welfare** in closed-form

$$\mathcal{W}(\tau) = \underbrace{\log(n_0(\tau) - G)}_{\text{Size}} - \underbrace{\frac{1-\tau}{1+\varphi}}_{\text{Labor disutility}} \underbrace{-(1-\tau)^2 \frac{v_\omega}{2}}_{\text{Redistribution}}$$

Efficiency

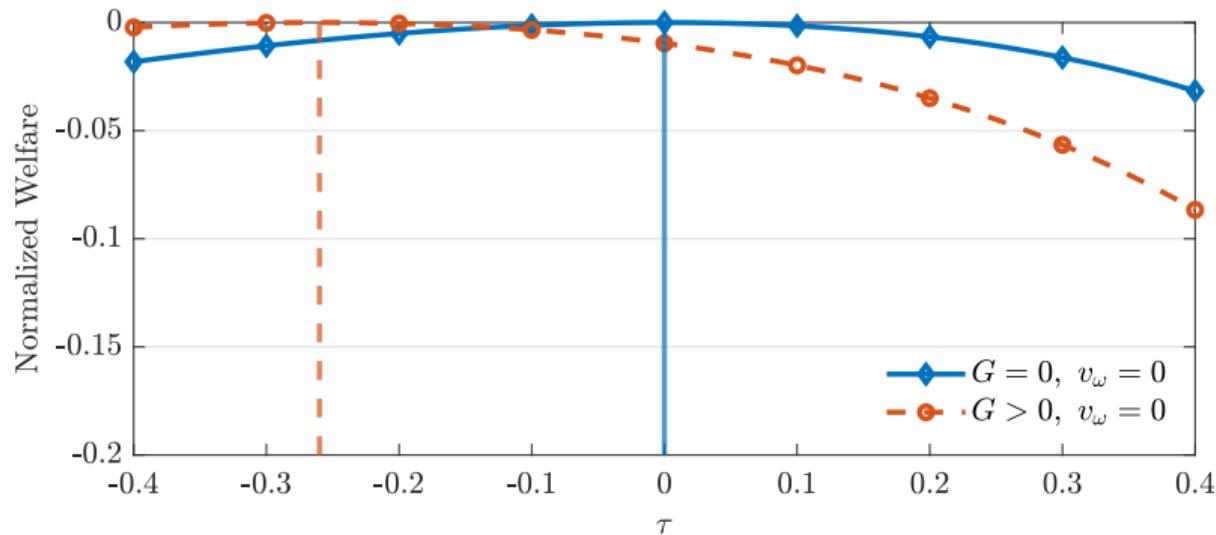
- Two **efficiency** terms
 - Size term \downarrow with τ ; Labor disutility term \uparrow with τ
- **Redistribution** term \uparrow with τ
- Calibration: $\tau = 0.18$, $\varphi = 2.5$, $G/Y = 0.223$, v_ω to match $\mathbb{V}[\log c] = 0.18$

Welfare Optimal τ



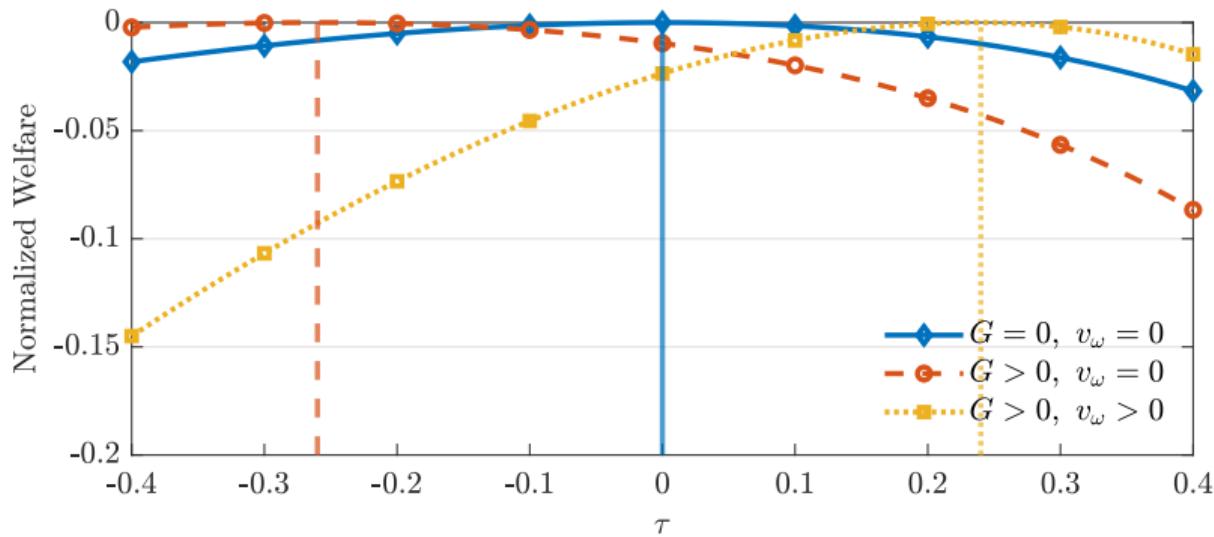
- Optimal income-tax progressivity:
 - No spending, no heterogeneity: $\tau = 0$

Welfare Optimal τ



- Optimal income-tax progressivity:
 - No spending, no heterogeneity: $\tau = 0$
 - Spending, no heterogeneity: $\tau < 0$

Welfare Optimal τ



- Optimal income-tax progressivity:
 - No spending, no heterogeneity: $\tau = 0$
 - Spending, no heterogeneity: $\tau < 0$
 - Spending, with heterogeneity: $\tau > 0$

Adding savings HSV (2014)

- A richer model with hand-to-mouth households *in equilibrium*
 - Richer structure of stochastic process

$$\log w_t = \alpha_t + \varepsilon_t$$

where

$$\alpha_t = \alpha_{t-1} + w_t, \quad \varepsilon_t = \theta_t$$

with w_t and θ_t normally i.i.d. (+ stochastic death)

Adding savings HSV (2014)

- A richer model with hand-to-mouth households *in equilibrium*

- Richer structure of stochastic process

$$\log w_t = \alpha_t + \varepsilon_t$$

where

$$\alpha_t = \alpha_{t-1} + w_t, \quad \varepsilon_t = \theta_t$$

with w_t and θ_t normally i.i.d. (+ stochastic death)

- When $v_\theta = 0$, **no-trade theorem**
 - + Permanent uninsurable shock & homothetic framework
 - ⇒ No savings in equilibrium

Adding savings HSV (2014)

- A richer model with hand-to-mouth households *in equilibrium*

- Richer structure of stochastic process

$$\log w_t = \alpha_t + \varepsilon_t$$

where

$$\alpha_t = \alpha_{t-1} + w_t, \quad \varepsilon_t = \theta_t$$

with w_t and θ_t normally i.i.d. (+ stochastic death)

- When $v_\theta = 0$, **no-trade theorem**
 - + Permanent uninsurable shock & homothetic framework
 - ⇒ No savings in equilibrium
 - Fully insurable ε_t -shock: alters labor supply but still closed-form

Adding savings HSV (2014)

- A richer model with hand-to-mouth households *in equilibrium*

- Richer structure of stochastic process

$$\log w_t = \alpha_t + \varepsilon_t$$

where

$$\alpha_t = \alpha_{t-1} + w_t, \quad \varepsilon_t = \theta_t$$

with w_t and θ_t normally i.i.d. (+ stochastic death)

- When $v_\theta = 0$, **no-trade theorem**
 - + Permanent uninsurable shock & homothetic framework
 - ⇒ No savings in equilibrium
 - Fully insurable ε_t -shock: alters labor supply but still closed-form

⇒ “**Partial-insurance**” framework

- $v_\omega + v_\theta$ to capture variance of log income
 - v_ω to capture variance of log consumption

Optimal income-tax progressivity HSV (2017)

- A richer model with many more features

1. Endogenous spending
2. Distribution over preference parameters

$$u_i(c_{it}, h_{it}, G) = \log c_{it} - B_i \frac{n_{it}^{1+\varphi}}{1+\varphi} + \chi \log G$$

where $\log B_i \sim \mathcal{N}\left(\frac{v_B}{2}, v_B\right)$

Optimal income-tax progressivity HSV (2017)

- A richer model with many more features

1. Endogenous **spending**

2. Distribution over **preference** parameters

$$u_i(c_{it}, h_{it}, G) = \log c_{it} - B_i \frac{n_{it}^{1+\varphi}}{1+\varphi} + \chi \log G$$

where $\log B_i \sim \mathcal{N}\left(\frac{v_B}{2}, v_B\right)$

3. Investment in **education**

$$U_i = -v_i(s_i) + \mathbb{E}_0 \sum_{t=0}^{\infty} (\beta \delta)^t u_i(c_{it}, n_{it}, G)$$

where $v_i(s_i) = \frac{1}{\kappa_i^{1/\psi}} \frac{s_i^{1+1/\psi}}{1+1/\psi}$, where $\kappa_i \sim \exp(1)$

Optimal income-tax progressivity HSV (2017)

- A richer model with many more features

1. Endogenous **spending**

2. Distribution over **preference** parameters

$$u_i(c_{it}, h_{it}, G) = \log c_{it} - B_i \frac{n_{it}^{1+\varphi}}{1+\varphi} + \chi \log G$$

where $\log B_i \sim \mathcal{N}\left(\frac{v_B}{2}, v_B\right)$

3. Investment in **education**

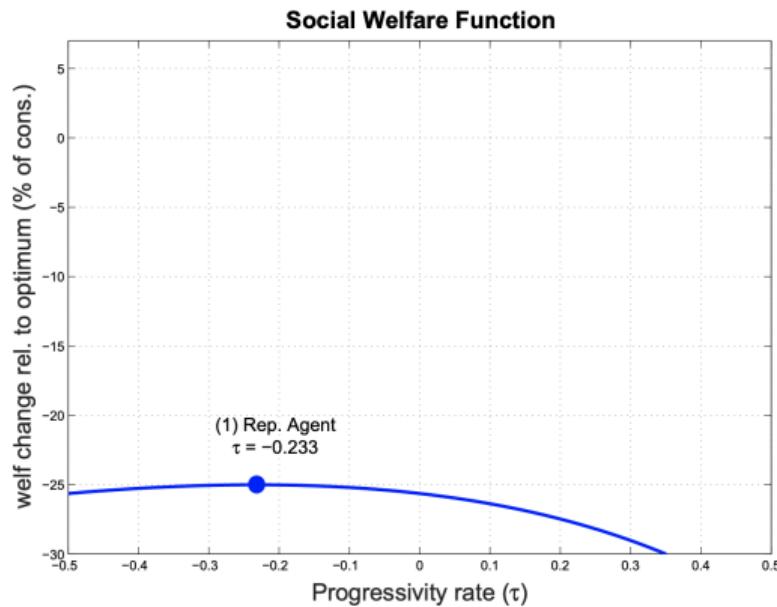
$$U_i = -v_i(s_i) + \mathbb{E}_0 \sum_{t=0}^{\infty} (\beta \delta)^t u_i(c_{it}, n_{it}, G)$$

where $v_i(s_i) = \frac{1}{\kappa_i^{1/\psi}} \frac{s_i^{1+1/\psi}}{1+1/\psi}$, where $\kappa_i \sim \exp(1)$

4. [Insurable shocks] ε

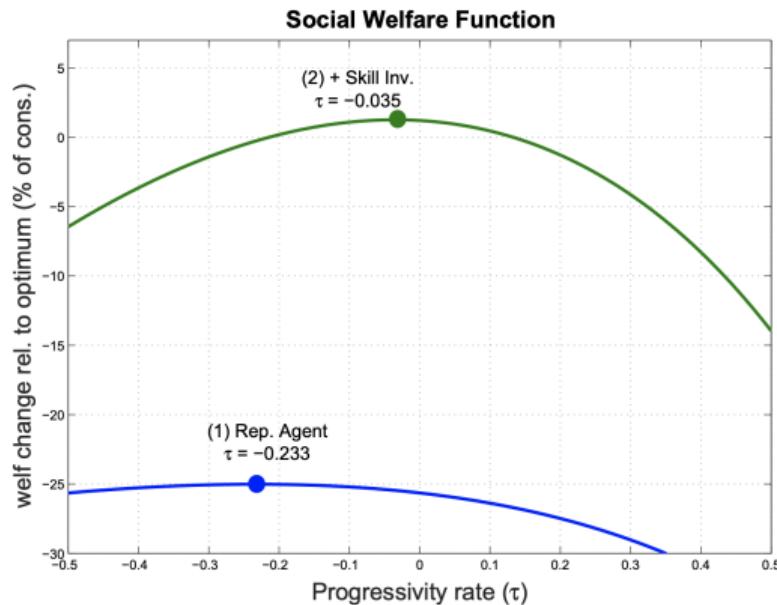
Welfare HSV (2017)

- Representative-agent, $\chi > 0$



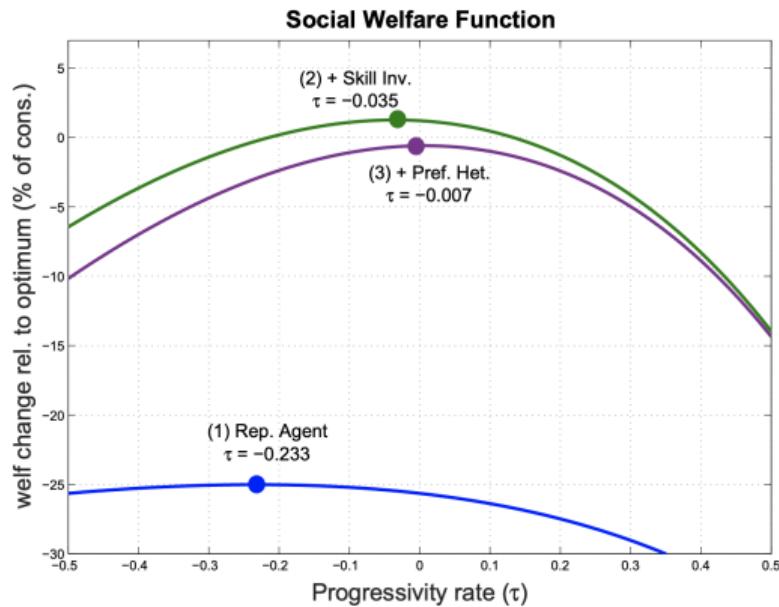
Welfare HSV (2017)

- With heterogeneity in skills



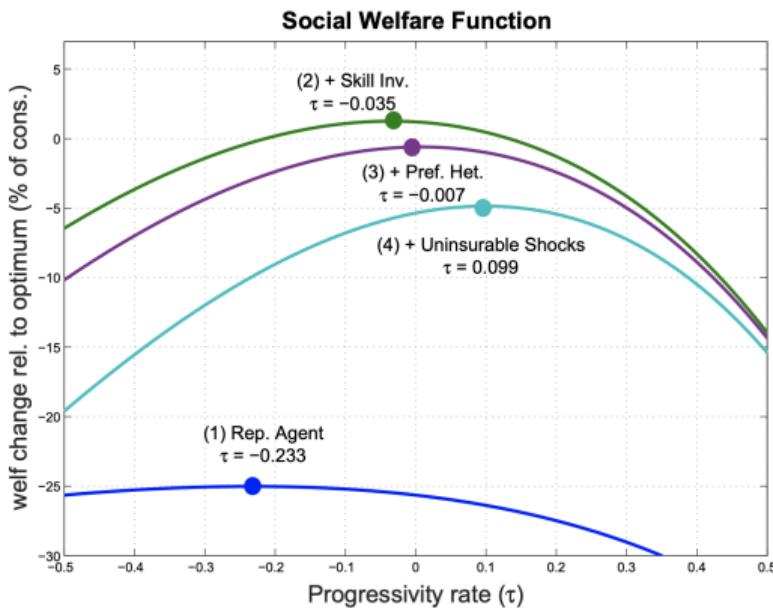
Welfare HSV (2017)

- With heterogeneity in labor disutility



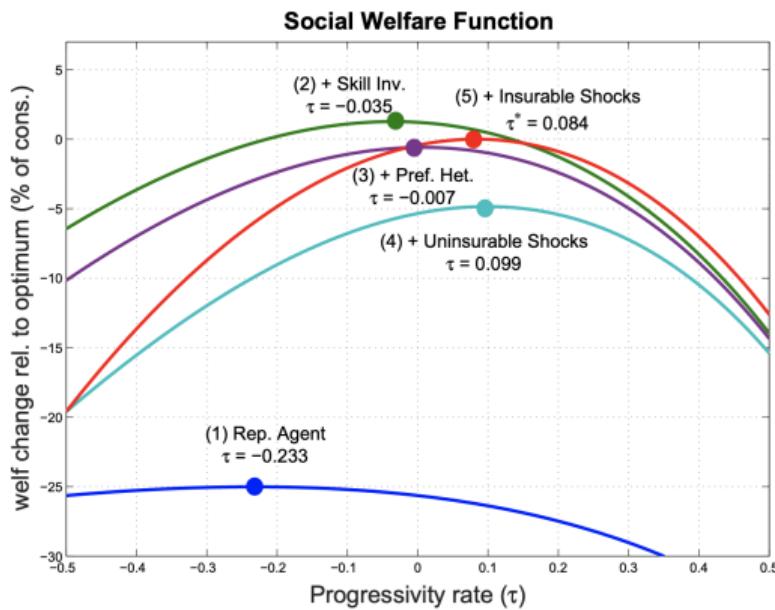
Welfare HSV (2017)

■ With uninsurable shocks



Welfare HSV (2017)

■ With insurable shocks



Taking stock HSV (2017)

- Taxes should be progressive
 - Optimal **progressivity** should be **lower** than in the U.S. . . .

Taking stock HSV (2017)

- Taxes should be progressive
 - Optimal **progressivity** should be **lower** than in the U.S. . . .
- A great **framework** to think about optimal progressivity!
- Going further: adding an intercept?
 - **Mirrlees** typical findings: a quick overview
 - Revisiting the **data**

Adding Transfers

■ Tax and transfer functions

- Progressive income taxes: $\mathcal{T}(y) = y - \lambda y^{1-\tau}$
- A lump-sum transfer T

Adding Transfers

■ Tax and transfer functions

- Progressive income taxes: $\mathcal{T}(y) = y - \lambda y^{1-\tau}$
- A lump-sum transfer T

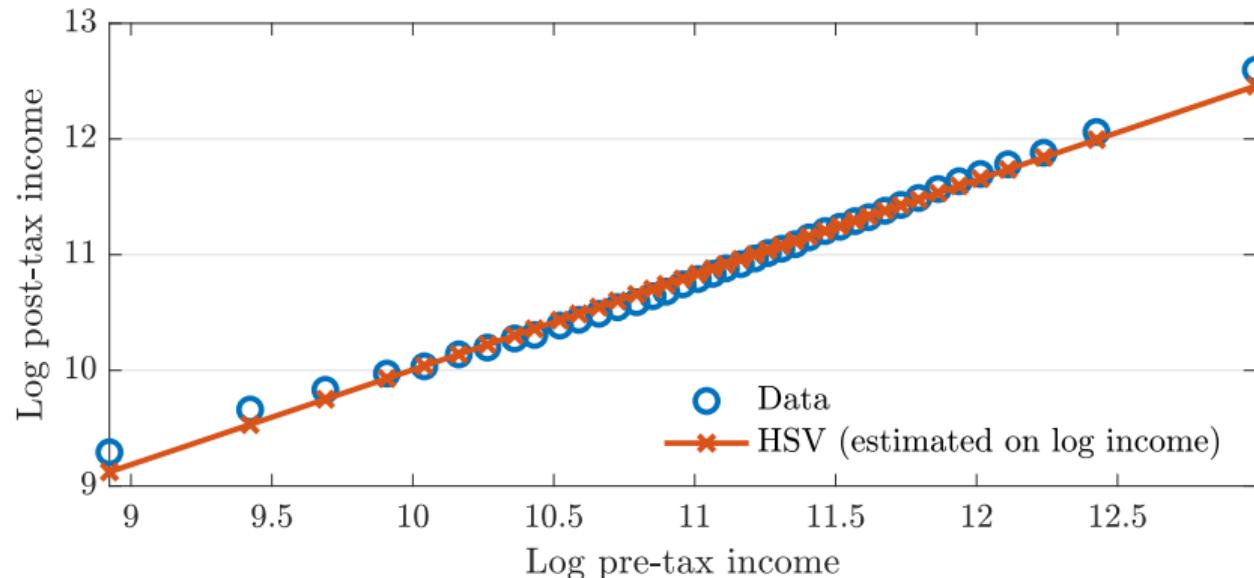
■ Utilitarian government

- Budget: $G + T = \int y_{it} di - \lambda \int y_{it}^{1-\tau} di$

■ A continuum of workers

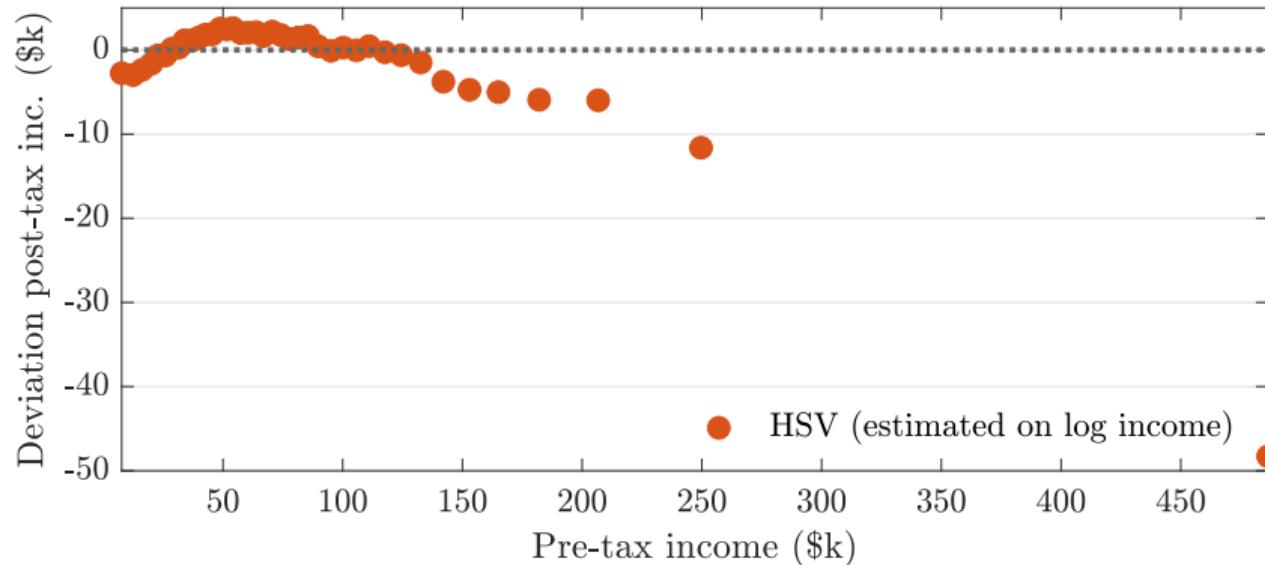
- Hand-to-mouth workers: $c_{it} = \lambda(z_{it} n_{it})^{1-\tau} + T$

Loglinear tax function No transfer (HSV)



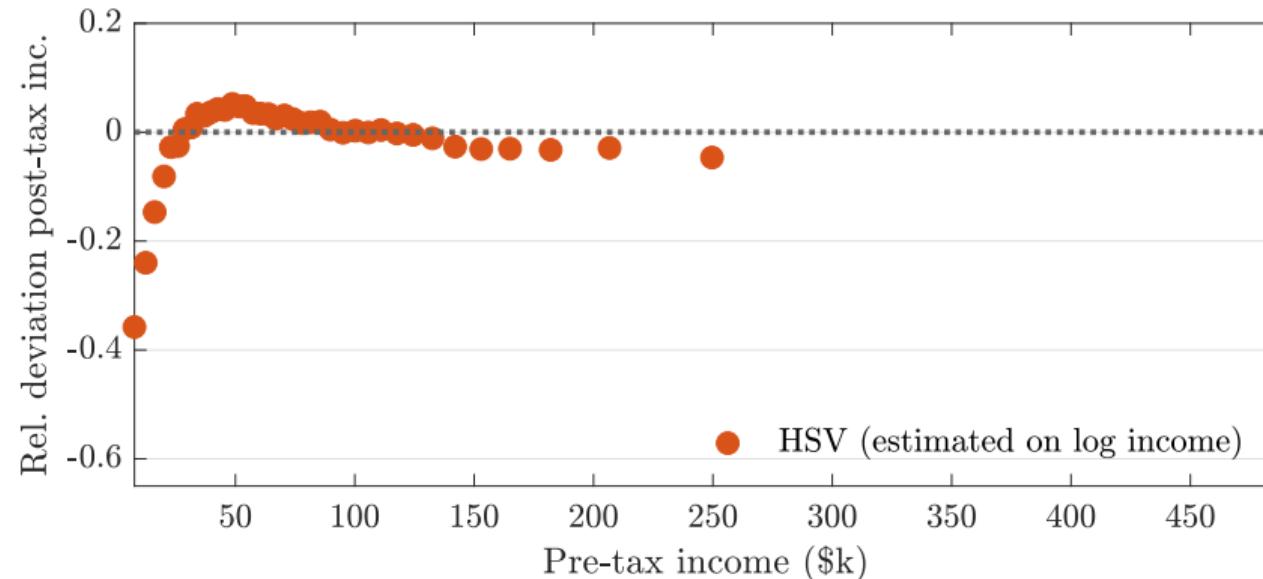
- Linear estimate on log income: $\log(y^{at}) = \log(\lambda) + (1 - \tau) \log(y)$
- Estimated progressivity $\tau = 0.18$

Loglinear tax function No transfer (HSV)



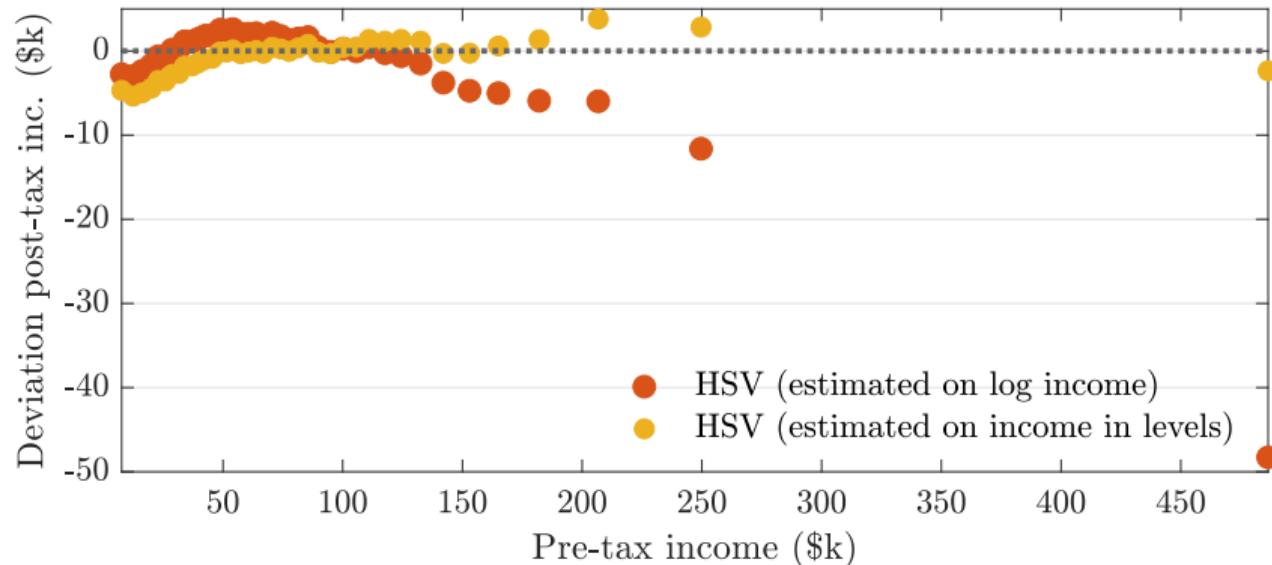
- Linear estimate on log income: $\log(y^{at}) = \log(\lambda) + (1 - \tau) \log(y)$
- Estimated progressivity $\tau = 0.18$

Loglinear tax function No transfer (HSV)



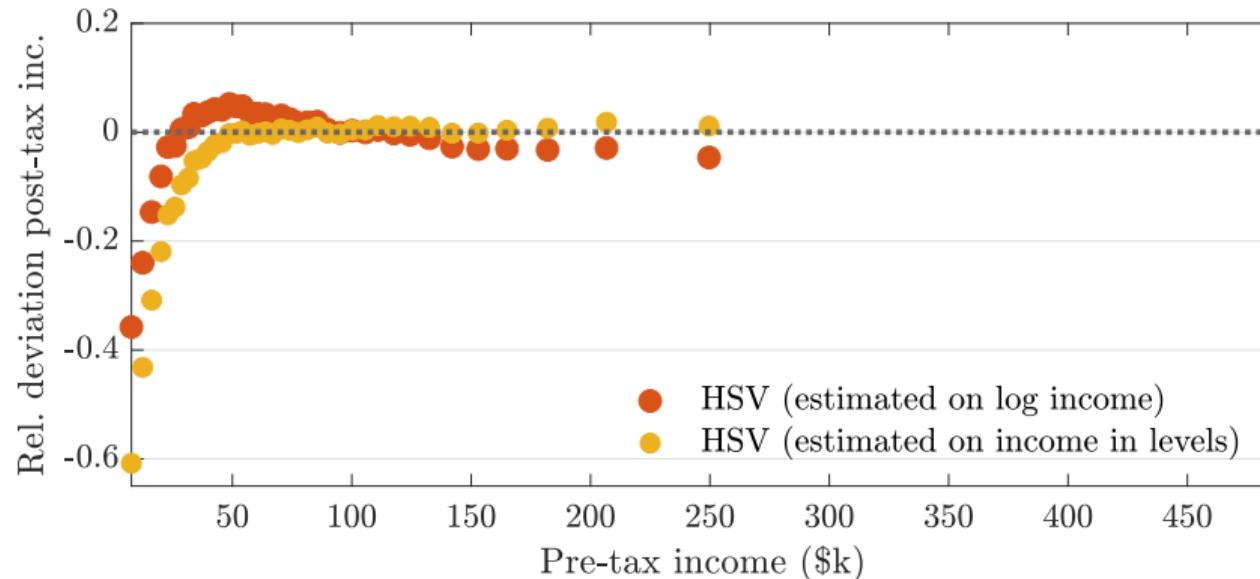
- Linear estimate on log income: $\log(y^{at}) = \log(\lambda) + (1 - \tau) \log(y)$
- Estimated progressivity $\tau = 0.18$

Loglinear tax function No transfer



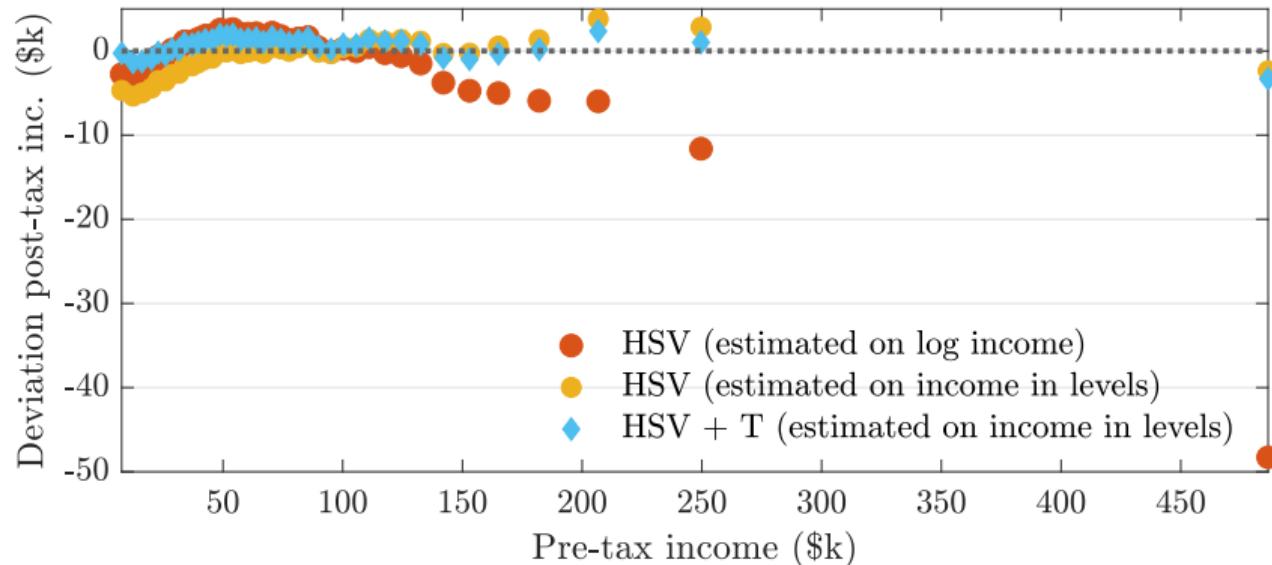
- Non-linear estimate on income in **levels**: $y^{at} = \lambda y^{1-\tau}$
- Estimated progressivity: $\tau = 0.09$

Loglinear tax function No transfer



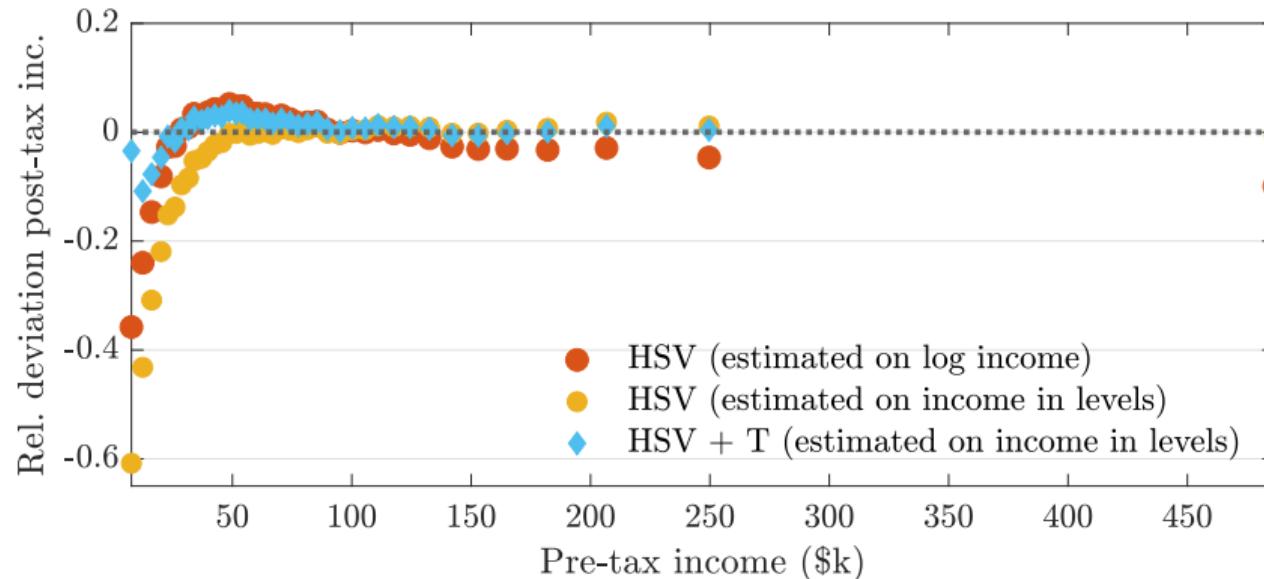
- Non-linear estimate on income in **levels**: $y^{at} = \lambda y^{1-\tau}$
- Estimated progressivity: $\tau = 0.09$

Empirical fit Loglinear tax function with a transfer



- Non-linear estimate on income in levels: $y^{at} = \lambda y^{1-\tau} + T$
- Estimated progressivity $\tau = 0.06$, transfer $T \approx \$5,400$

Empirical fit Loglinear tax function with a transfer



- Non-linear estimate on income in levels: $y^{at} = \lambda y^{1-\tau} + T$
- Estimated progressivity $\tau = 0.06$, transfer $T \approx \$5,400$

Transfers Heterogeneous agents

- **Implicit function theorem:** approximation of the FOC around $T = 0$:

$$\hat{n}_{it} \approx n_0(\tau) - \frac{T}{1 + \varphi} \frac{n_0(\tau)}{n_0(\tau) - G} \exp(-\tau(1 - \tau)v_\omega) z_{it}^{-(1-\tau)}$$

Transfers Heterogeneous agents

- **Implicit function theorem:** approximation of the FOC around $T = 0$:

$$\hat{n}_{it} \approx n_0(\tau) - \frac{T}{1 + \varphi} \frac{n_0(\tau)}{n_0(\tau) - G} \exp(-\tau(1 - \tau)v_\omega) z_{it}^{-(1-\tau)}$$

- Approximated formula with heterogeneity $v_\omega > 0$

$$W(\tau, T) = W(\tau, 0) + T \left[\Omega_e(\tau, v_\omega) + \Omega_r(\tau, v_\omega) \right],$$

where the two terms capture

- **Efficiency** concerns
- **Redistribution** concerns ($\Omega_r(\tau, v_\omega) = 0$ when $v_\omega = 0$)

Transfers Welfare: Efficiency

- Efficiency with a representative agent ($v_\omega = 0$):

$$\Omega_e(\tau, 0) \equiv U_c(C_0(\tau)) \underbrace{\frac{\partial Y^{ra}(\tau, T)}{\partial T} \Big|_{T=0}}_{\text{Size } < 0} + U_n(n_0(\tau)) \underbrace{\frac{\partial n^{ra}(\tau, T)}{\partial T} \Big|_{T=0}}_{\text{Labor disutility } > 0}$$

- Claim: Ω_e decreases with τ
 - + Offset the effects of progressivity on labor supply incentives
 - With heterogeneity, efficiency Ω_e numerically decreases with τ
- ⇒ Efficiency gains of T are decreasing in τ

Transfers

Welfare: Redistribution

- Redistribution $\Omega_r(\tau, v_\omega)$

$$\Omega_r(\tau, v_\omega) \equiv \mathbb{E}[U_c(c_0(\tau))] - U_c(C_0(\tau)) = (1 - \tau)^2 \frac{1}{n_0(\tau) - G} v_\omega$$

- Positive as long as $v_\omega > 0$ and decreases with τ

\Rightarrow Redistribution gains of T are decreasing in τ

\Rightarrow Overall negative optimal relationship between T and τ

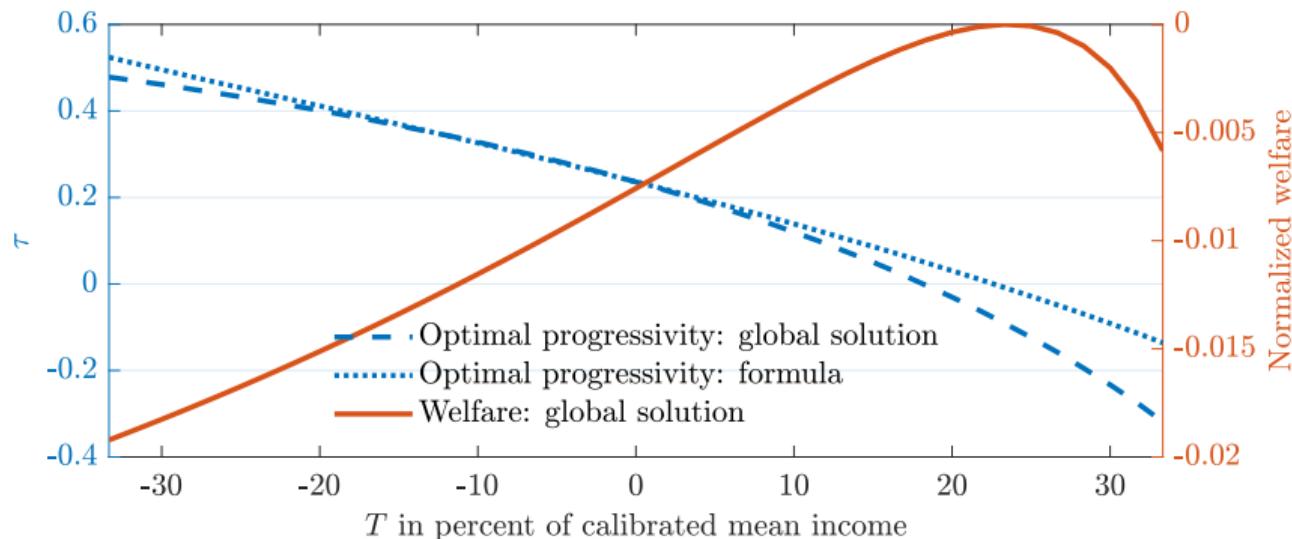
- Use formula to evaluate local welfare gains of transfers:

$$W(\tau, T) = W(\tau, 0) + T \left[\Omega^e(\tau, v_\omega) + \Omega^r(\tau, v_\omega) \right]$$

- At calibrated v_ω and τ : $-0.54 + 0.78 > 0$

Transfers Heterogeneous agents

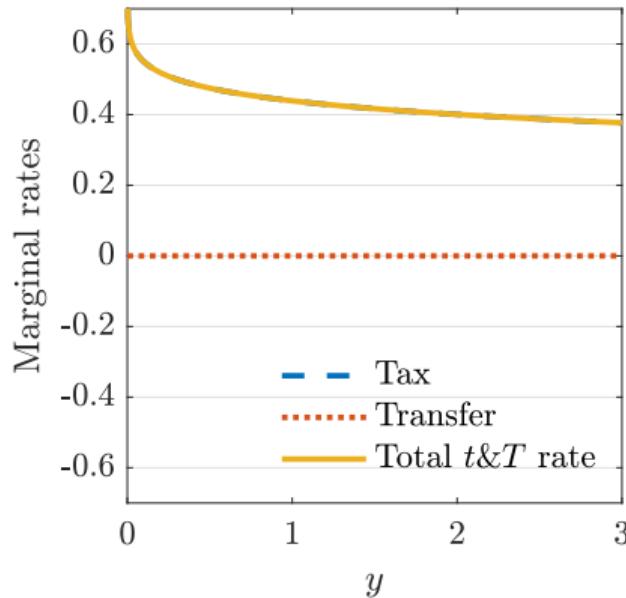
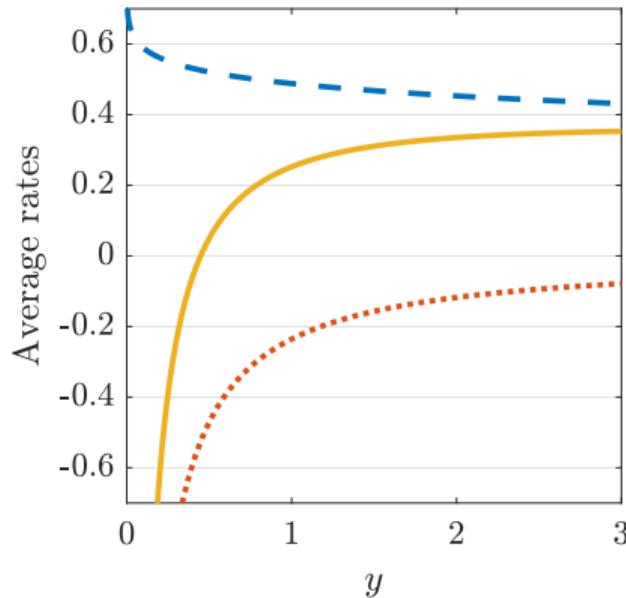
- A **negative** relationship between τ and T



- Formula: a good **approximation**
- Optimal transfers are **large**, with **regressive** income taxes

Optimal plan with transfers Global static solution

- Generous transfers: $T/Y = 23\%$, regressive income taxes: $\tau = -0.09$

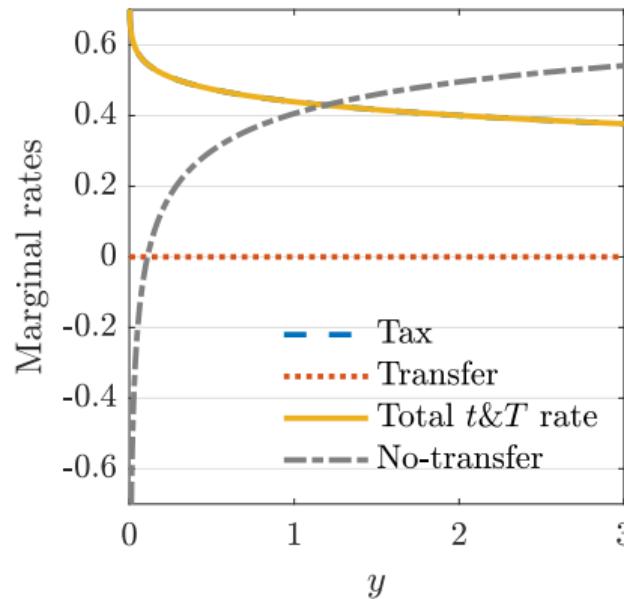
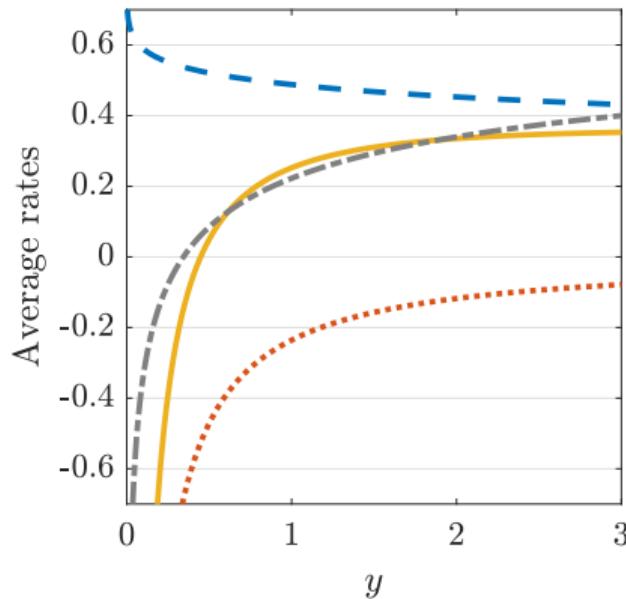


- Average taxes are increasing, marginal taxes are decreasing

- Transfers to disentangle average from marginal $t\&T$ rates

Optimal plan with transfers Global static solution

- Generous transfers: $T/Y = 23\%$, regressive income taxes: $\tau = -0.09$



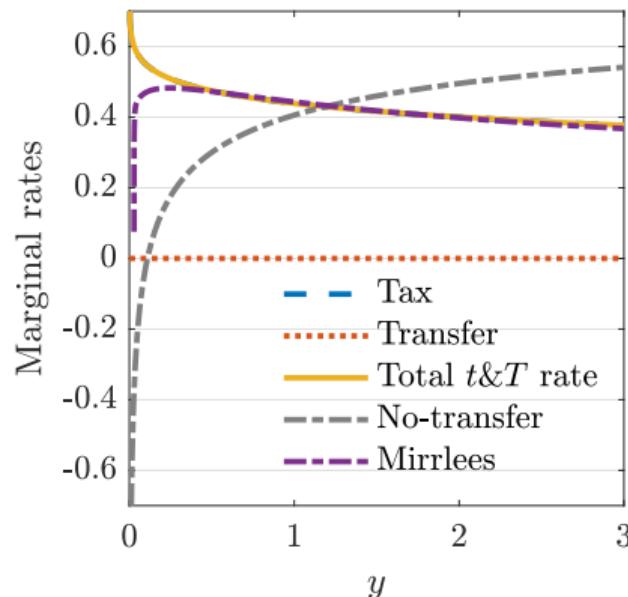
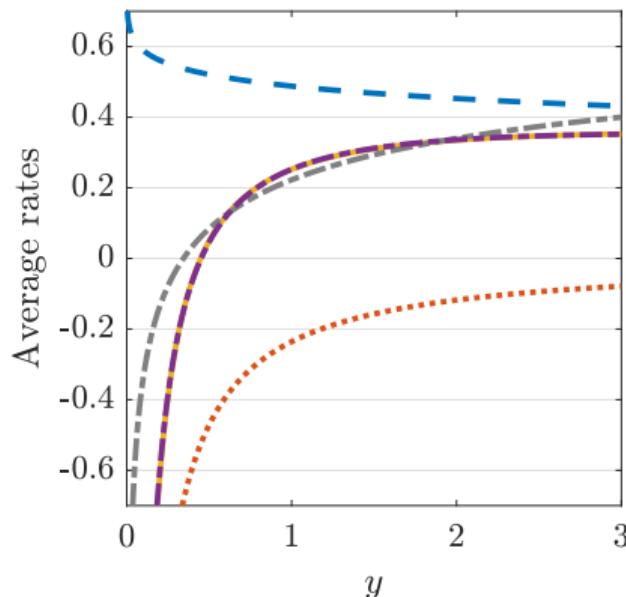
- Average taxes are increasing, marginal taxes are decreasing

- Transfers to disentangle average from marginal $t&T$ rates

Optimal plan with transfers

Comparison to second-best

- Welfare in CE terms: HSV: +0.14%, HSV+T: +0.90%



- Close to welfare gains of the Mirrlees/second-best allocation: +0.93%

Taking stock

- Loglinear taxes plus a transfer
 - Is still simple and tractable
 - Fits the data better
- Welfare gains from allowing for transfers
 - Break the link between average and marginal $t\&T$ rates
 - Systematically close to the second-best!

2. Revisiting the Welfare State

A Quantitative Approach

The Welfare State in the US

A complex safety net

- Complex design
 - Means-tested (on labor and capital income), phasing-in, phasing-out in time, etc.
 - Partly refundable, partly not...
 - Federal and state level
 - Very heterogeneous take-up rates (and difficult to align in the data)
- It's big: 2.5% of GDP
- It depends a lot on the number of children, on the structure of the household, etc.

The Welfare State in the US

Is it optimal?

- Effects of **both**:

- Transfers themselves, and associated taxes to finance them...

The Welfare State in the US

Is it optimal?

- Effects of **both**:

- Transfers themselves, and associated taxes to finance them...

- On multiple margins

- Labor supply: intensive margin, extensive margin, search
 - Human capital accumulation: college decision, over the working life
 - Savings, self-insurance, physical capital accumulation

The Welfare State in the US

Is it optimal?

- Effects of **both**:

- Transfers themselves, and associated taxes to finance them...

- On multiple margins

- Labor supply: intensive margin, extensive margin, search
 - Human capital accumulation: college decision, over the working life
 - Savings, self-insurance, physical capital accumulation
 - Housing decisions?
 - Entrepreneurship?

The Welfare State in the US

Is it optimal?

- Effects of **both**:

- Transfers themselves, and associated taxes to finance them...

- On multiple margins

- Labor supply: intensive margin, extensive margin, search
 - Human capital accumulation: college decision, over the working life
 - Savings, self-insurance, physical capital accumulation
 - Housing decisions?
 - Entrepreneurship?
 - Investment in early childhood?

The Welfare State in the US

Is it optimal?

- Effects of **both**:

- Transfers themselves, and associated taxes to finance them...

- On multiple margins

- Labor supply: intensive margin, extensive margin, search
 - Human capital accumulation: college decision, over the working life
 - Savings, self-insurance, physical capital accumulation
 - Housing decisions?
 - Entrepreneurship?
 - Investment in early childhood?
 - The gender gap?

The Welfare State in the US

Is it optimal?

- Effects of **both**:

- Transfers themselves, and associated taxes to finance them...

- On multiple margins

- Labor supply: intensive margin, extensive margin, search
 - Human capital accumulation: college decision, over the working life
 - Savings, self-insurance, physical capital accumulation
 - Housing decisions?
 - Entrepreneurship?
 - Investment in early childhood?
 - The gender gap?
 - Household status? Number of children?
 - ...

Reforms: Typical proposals

- Universal Basic Income

- Guaranteed unconditional (lump-sum) transfer
- At the individual or hh level? Children?

Reforms: Typical proposals

- Universal Basic Income

- Guaranteed unconditional (lump-sum) transfer
- At the individual or hh level? Children?

- Negative Income Tax

- Friedman's proposal

Reforms: Typical proposals

■ Universal Basic Income

- Guaranteed unconditional (lump-sum) transfer
- At the individual or hh level? Children?

■ Negative Income Tax

- Friedman's proposal
- Nothing else but a lump-sum tax with a flat rate

Reforms: Typical proposals

- Universal Basic Income

- Guaranteed unconditional (lump-sum) transfer
- At the individual or hh level? Children?

- Negative Income Tax

- Friedman's proposal
- Nothing else but a lump-sum tax with a flat rate

- Can we disentangle the optimal transfers from the optimal tax?

Roadmap

- Separating taxes and transfers in the data: new functional forms
- Optimizing on transfers
 - Ferriere et al. (2023)
 - Guner et al. (2023)
 - Jaimovich, Saporta-Eksten, Setty and Yedid-Levi (2022)
 - Daruich and Fernandez (2023)
 - Holter, Krueger and Stepanchuk (2024)
 - ...

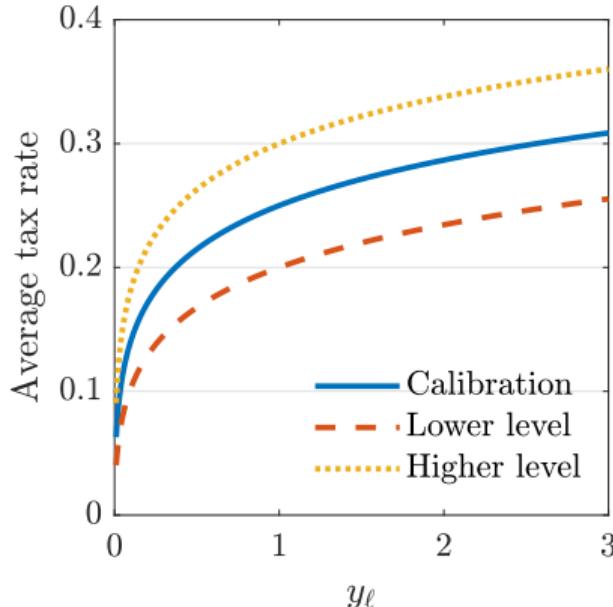
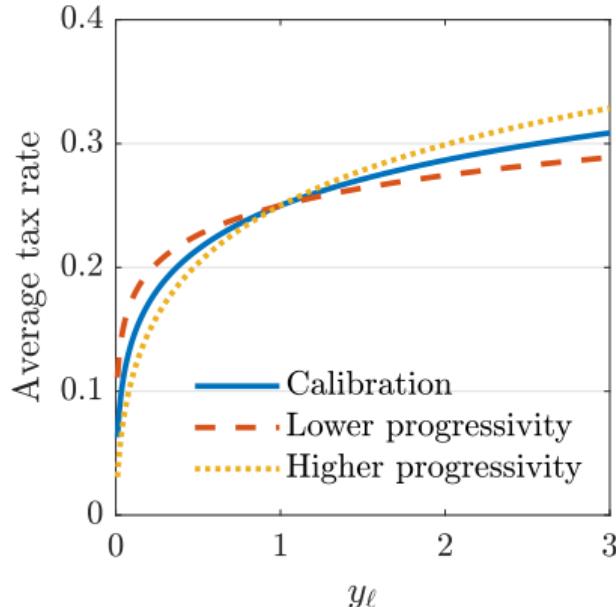
Taxes and transfers in the data

- Ferriere et al (2023)
- New functional forms for taxes and transfers
- Fit to the data
- Optimized fiscal instruments

Fiscal system

Income taxes

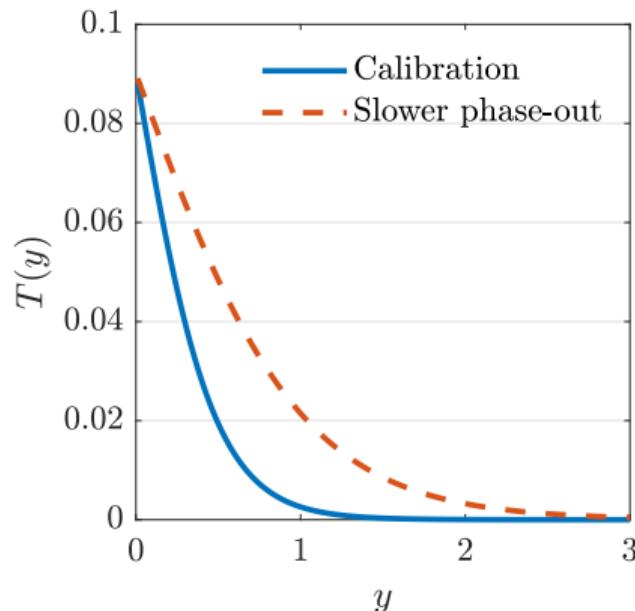
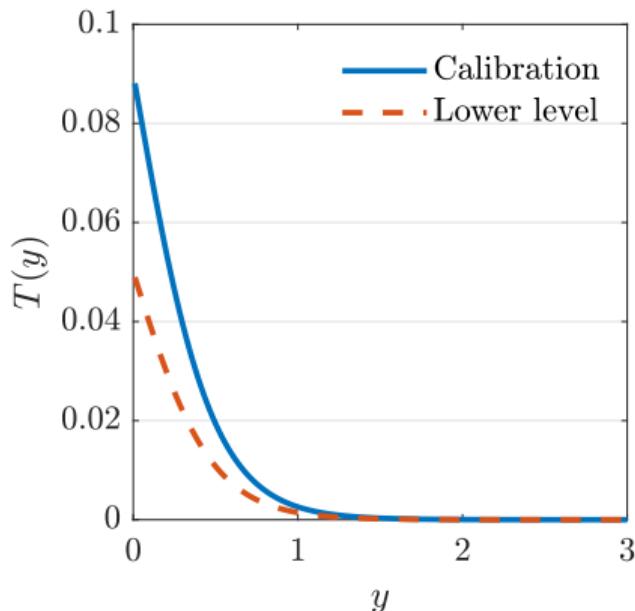
- Flat capital tax τ_k
- Progressive labor tax: $\exp\left(\log(\lambda)\left(\frac{y_\ell}{\bar{y}}\right)^{-2\theta}\right)y_\ell$, with level λ and progressivity θ



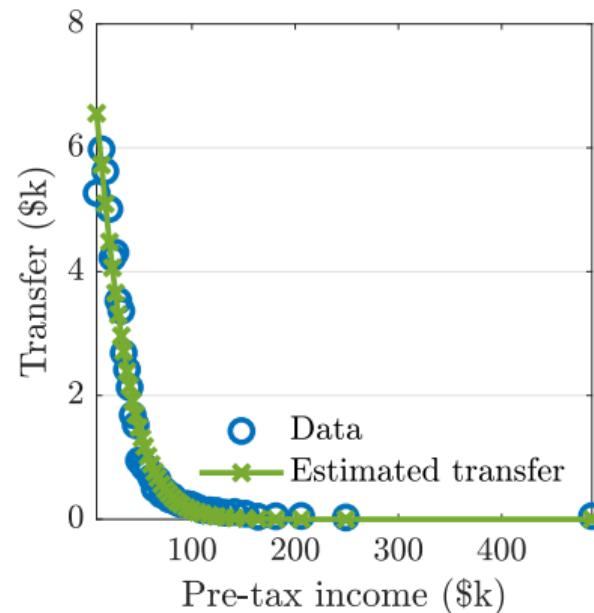
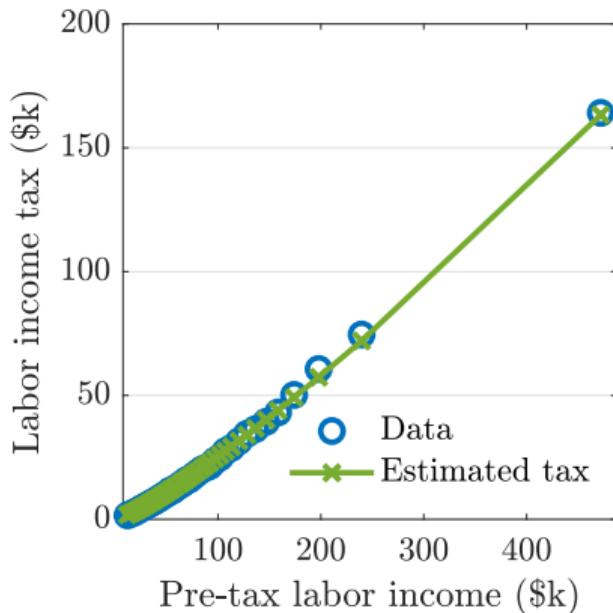
Fiscal system Transfers

■ New targeted-transfers function: $m\bar{y} \frac{2 \exp\left\{-\xi\left(\frac{y}{\bar{y}}\right)\right\}}{1+\exp\left\{-\xi\left(\frac{y}{\bar{y}}\right)\right\}}$

- m is the **level** at $y = 0$, ξ is the **speed** of phasing-out



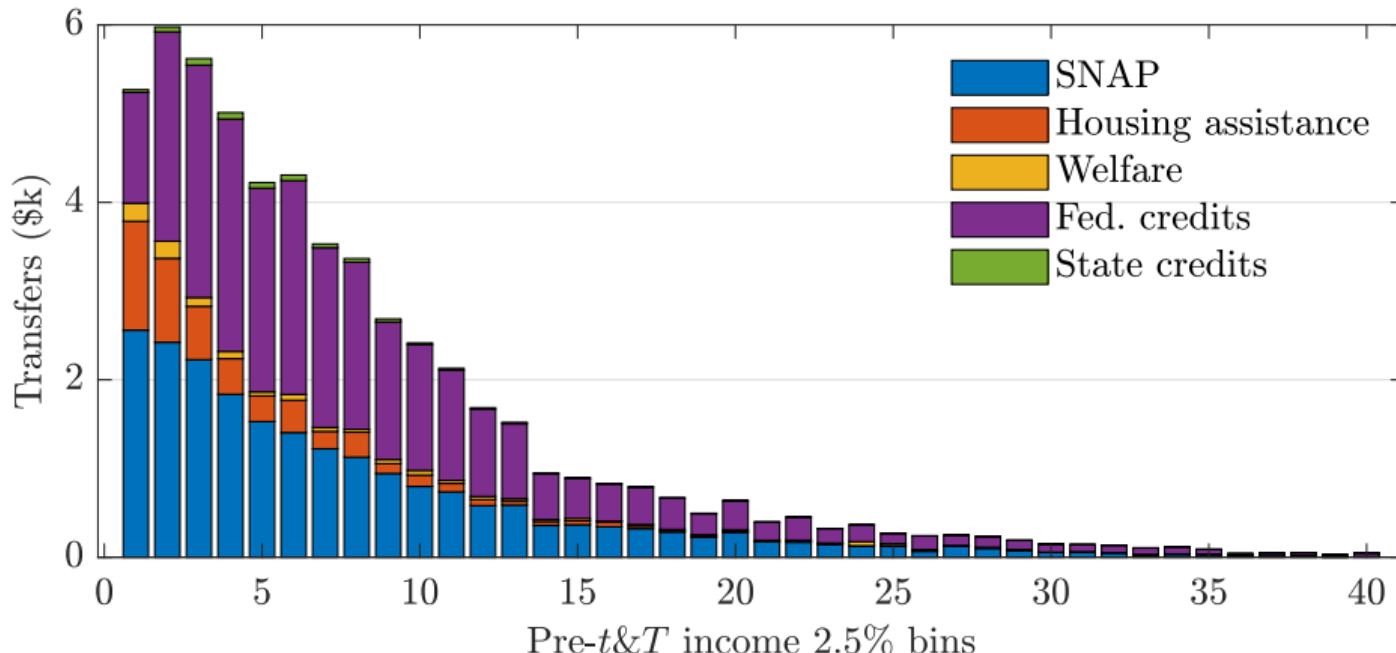
Calibration Fiscal system: Micro estimates



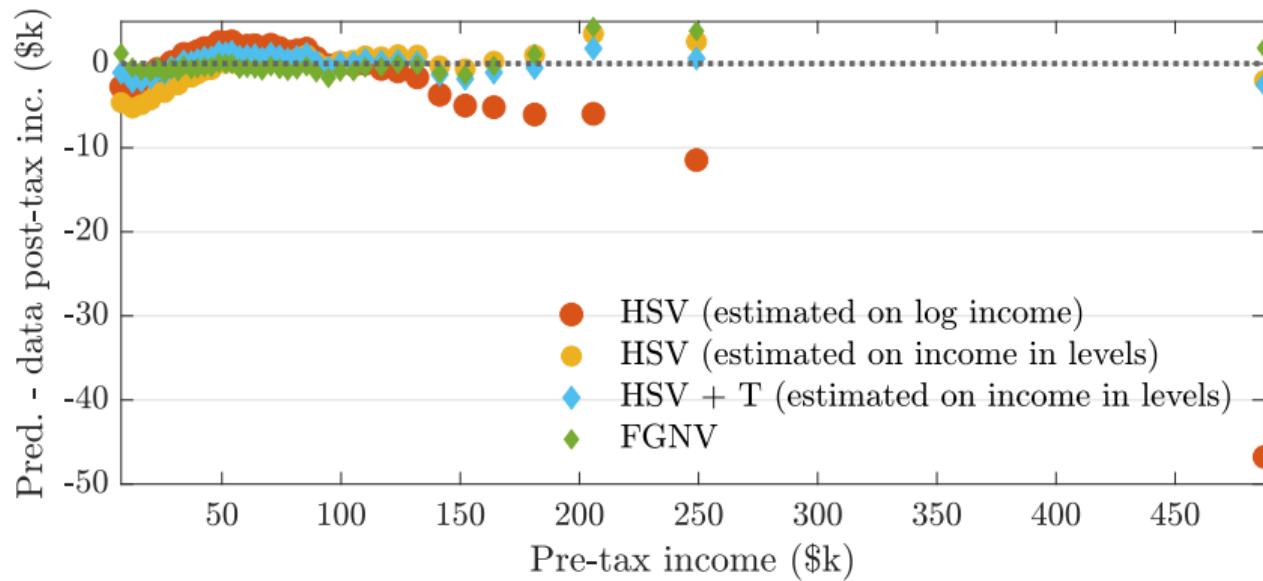
- Estimated on taxes and transfers: $\theta = 0.08$, $m = 0.09$, $\xi = 4.22$

Transfers

Components across the distribution

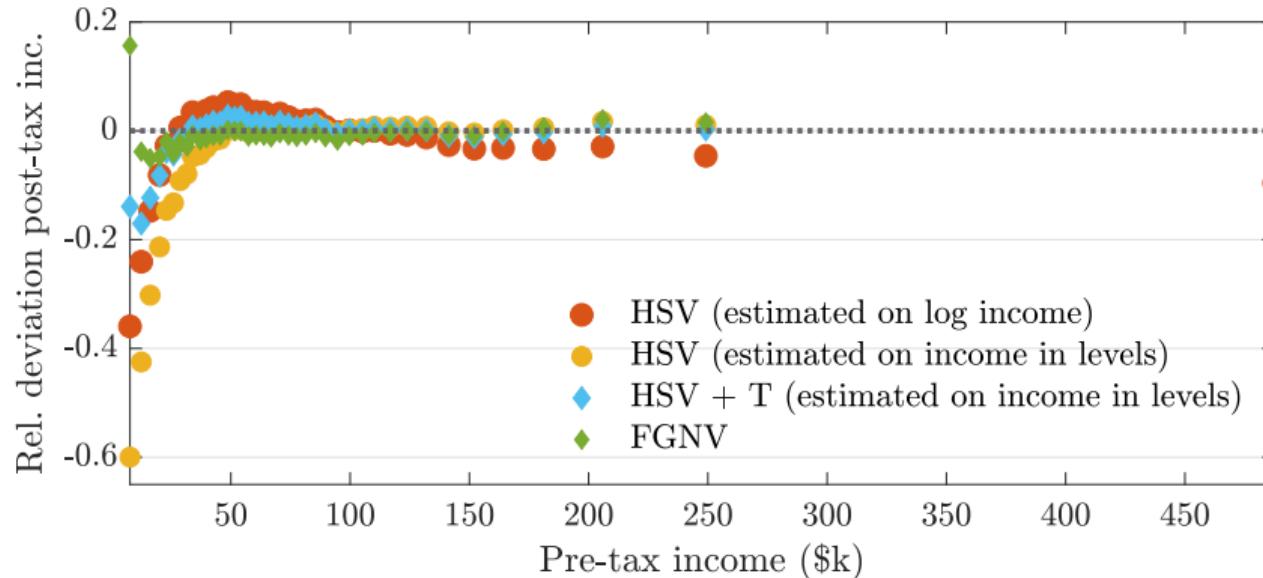


Fiscal system After-tax-and-transfer income fit



■ Predicted after-tax-and-transfer income

Fiscal system After-tax-and-transfer income fit



- Predicted after-tax-and-transfer income
 - Relative to pre-tax income

Calibration

- Income process to match household income risk
 - Annual earnings growth distribution from PSID (1978-1992)
Guvenen, Karahan, Ozkan, and Song (2021)
 - + Std deviation: 0.33, Skewness: -0.33, Kurtosis: 12, P9010: 0.60
 - And top-10 labor income share: 41% (Aoki and Nirei, 2017)

Calibration

- Income process to match household income risk
 - Annual earnings growth distribution from PSID (1978-1992)
Guvenen, Karahan, Ozkan, and Song (2021)
 - + Std deviation: 0.33, Skewness: -0.33, Kurtosis: 12, P9010: 0.60
 - And top-10 labor income share: 41% (Aoki and Nirei, 2017)

- Fiscal parameters
 - Flat taxes: $\tau_k = 30\%$ and $\tau_c = 6\%$ to match corresponding tax revenues
 - Debt: $D/Y = 100\%$, residual $G/Y \approx 21\%$

Calibration

- Income process to match household income risk
 - Annual earnings growth distribution from PSID (1978-1992)
Guvenen, Karahan, Ozkan, and Song (2021)
 - + Std deviation: 0.33, Skewness: -0.33, Kurtosis: 12, P9010: 0.60
 - And top-10 labor income share: 41% (Aoki and Nirei, 2017)
- Fiscal parameters
 - Flat taxes: $\tau_k = 30\%$ and $\tau_c = 6\%$ to match corresponding tax revenues
 - Debt: $D/Y = 100\%$, residual $G/Y \approx 21\%$
- Production: labor share $\alpha = 0.64$, depreciation $\delta = 0.06$
- Preferences: $\sigma = 2$, $\varphi^{-1} = 0.4$; β to match $r = 2\%$
- Borrowing constraint: a a quarter of mean income

Calibration Income and tax distribution, wealth effects and elasticities

- Income distribution, including at the bottom
- Distribution of taxes and transfers

Calibration Income and tax distribution, wealth effects and elasticities

- Income distribution, including at the bottom

- Distribution of taxes and transfers

- Compare model implied **wealth effects** to evidence

Golosov, Gruber, Mogstad, and Novgorodsky (2023)

- Five-year average change in labor income for every \$100 won:

Data: 2.3, model: **2.4**

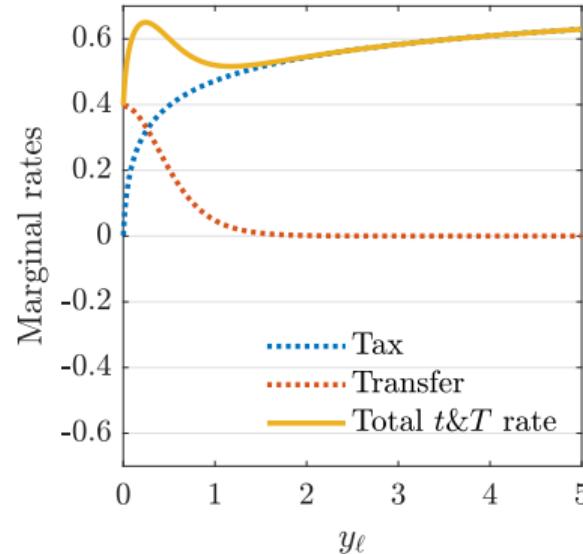
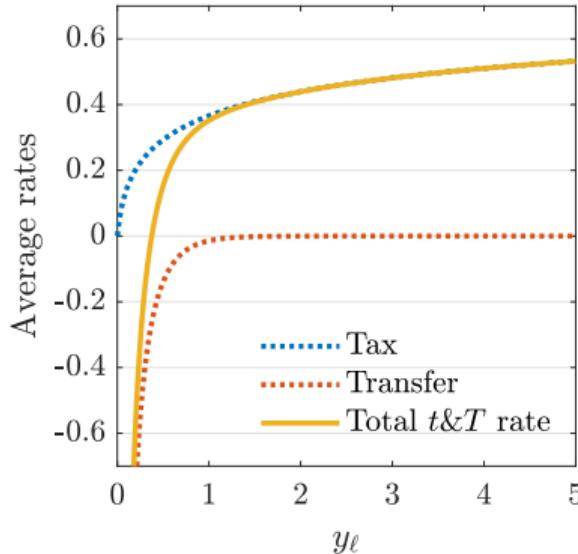
- Labor **elasticity** of the top-1%

- A 1% increase in marginal rates: 0.12-0.33 depending on persistence

Optimal tax-and-transfer plan

■ The **optimal plan** features

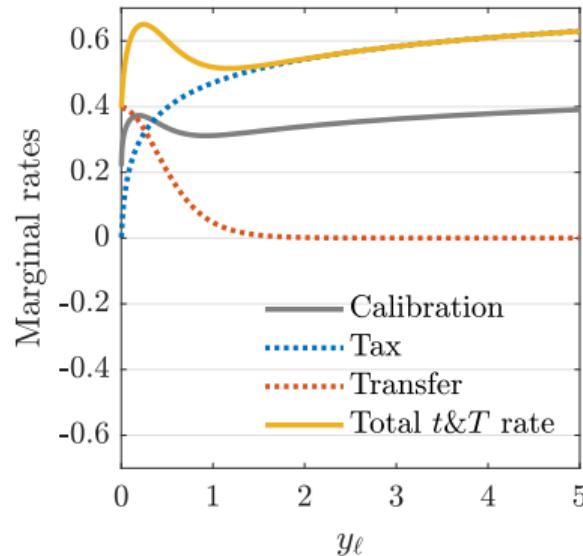
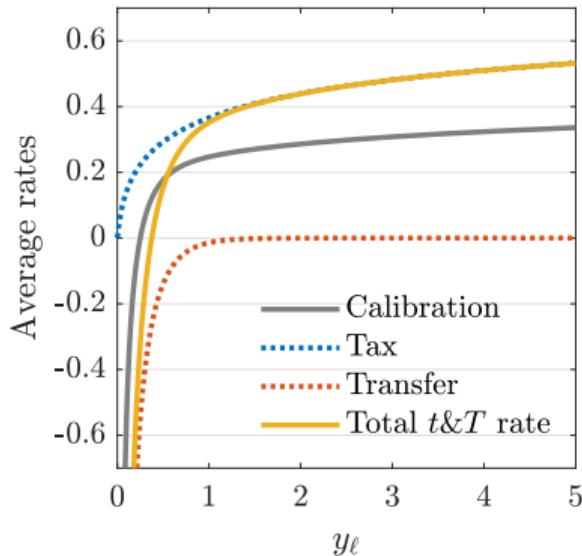
- Large transfers $m = 0.23$, i.e. \$20k, with phase-out $\xi = 3.41$
- Moderate tax progressivity $\theta = 0.14$



Optimal tax-and-transfer plan

■ The **optimal plan** features

- Large transfers $m = 0.23$, i.e. \$20k, with phase-out $\xi = 3.41$
- Moderate tax progressivity $\theta = 0.14$



Optimal plan Average and marginal rates

Data	Q1	Q2	Q3	Q4	Q5
Tax rate	16%	19%	22%	24%	29%
Transfer rate	23%	4%	1%	0%	0%

Optimal (long-run)	Q1	Q2	Q3	Q4	Q5
Tax rate	19%	23%	26%	26%	36%
Transfer rate	85%	24%	8%	2%	0%

Optimal plan Average and marginal rates

Data	Q1	Q2	Q3	Q4	Q5
Tax rate	16%	19%	22%	24%	30%
Transfer rate	23%	4%	0%	0%	0%
Average $t\&T$ rate	-7%	16%	21%	24%	29%
Optimal (long-run)	Q1	Q2	Q3	Q4	Q5
Tax rate	19%	23%	26%	26%	36%
Transfer rate	85%	24%	8%	2%	%
Average $t\&T$ rate	-66%	-1%	19%	24%	36%

- Average $t\&T$ rates are strongly increasing...

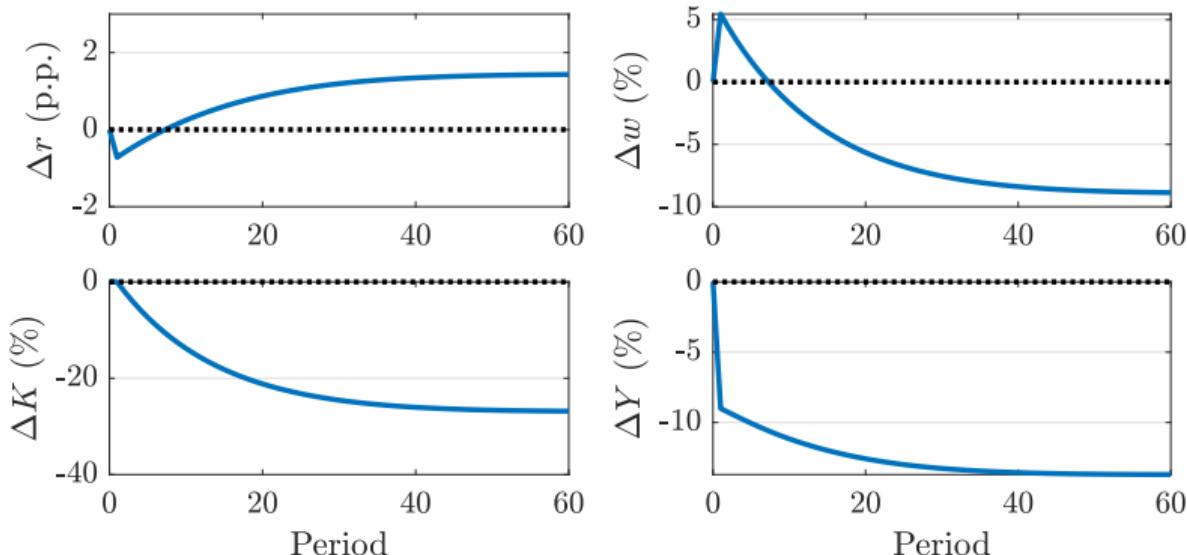
Optimal plan Average and marginal rates

Data	Q1	Q2	Q3	Q4	Q5
Tax rate	16%	19%	22%	24%	29%
Transfer rate	23%	4%	1%	0%	0%
Average $t\&T$ rate	-7%	16%	21%	24%	29%
Optimal (long-run)	Q1	Q2	Q3	Q4	Q5
Tax rate	19%	23%	26%	26%	36%
Transfer rate	85%	24%	8%	2%	0%
Average $t\&T$ rate	-66%	-1%	19%	24%	36%
Marginal $t\&T$ rate	63%	61%	55%	48%	50%

- Average $t\&T$ rates are strongly increasing...but not marginal $t\&T$ rates

Optimal tax-and-transfer plan

Transitions and welfare



- The economy (output, capital, wages) shrinks

Optimal tax-and-transfer plan

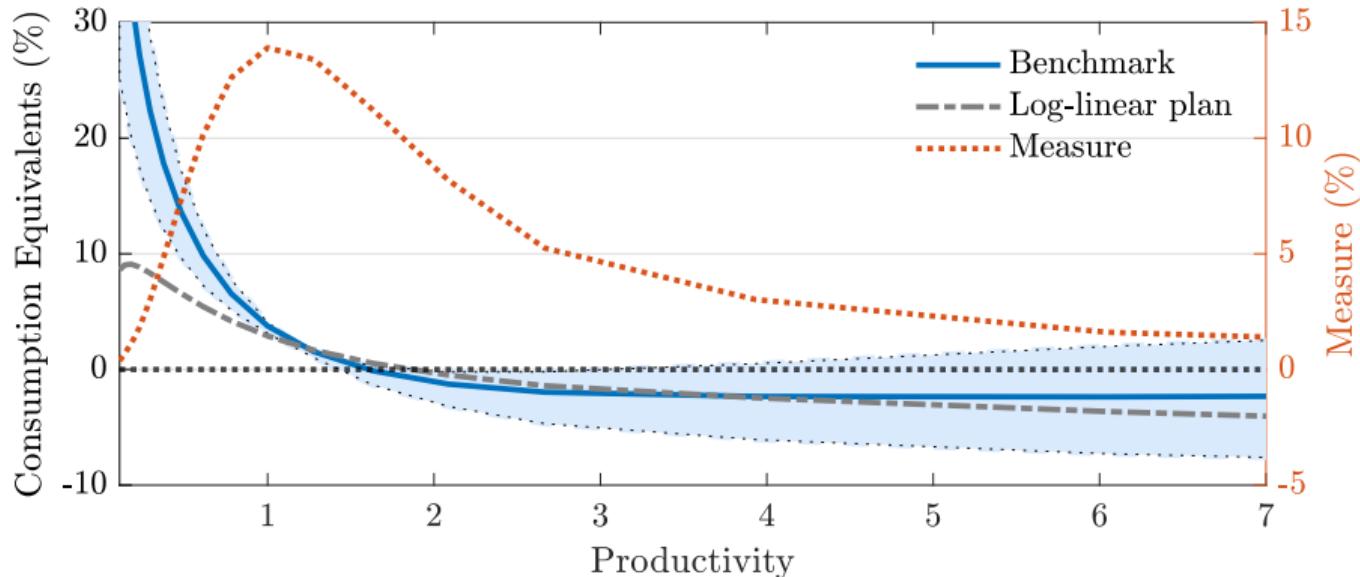
Transitions and welfare

Mean hours	Hours worked quintile				
Calibration	0.20	0.28	0.32	0.35	0.38
Optimal	0.18	0.25	0.28	0.31	0.34
Log hours deviation	Wage quintile				
Calibration	-0.03	0.00	-0.04	0.05	0.01
Optimal	-0.18	-0.07	-0.01	0.12	0.13

- The economy (output, capital, wages) shrinks, but better allocation of hours worked

Optimal tax-and-transfer plan

Transitions and welfare



- The economy (output, capital, wages) shrinks, but better allocation of hours worked
- Large welfare gains (6%); 76% of households benefit

Non-monotonic marginal rates UBI and log-linear plans

- Optimal plan with **lump-sum** transfers ($\xi = 0$)
 - Large transfer: \$19k financed with **flatter** taxes $\theta = 0.04$

Non-monotonic marginal rates UBI and log-linear plans

- Optimal plan with **lump-sum** transfers ($\xi = 0$)
 - Large transfer: \$19k financed with **flatter** taxes $\theta = 0.04$
 - **Welfare gains** are **5.36%** vs. 6.00% with phase-out

Non-monotonic marginal rates UBI and log-linear plans

- Optimal plan with **lump-sum** transfers ($\xi = 0$)
 - Large transfer: \$19k financed with **flatter** taxes $\theta = 0.04$
 - **Welfare gains** are **5.36%** vs. 6.00% with phase-out
- Optimal **affine**: transfer of \$20k, tax 60%, **CE 5.26%**

Optimal UBI

Average and marginal rates

With phase-out	Q1	Q2	Q3	Q4	Q5
Tax rate	19%	23%	26%	26%	36%
Transfer rate	85%	24%	8%	2%	0%
Average $t\&T$ rate	-66%	-1%	19%	24%	36%
Marginal $t\&T$ rate	63%	61%	55%	48%	50%
Lump-sum	Q1	Q2	Q3	Q4	Q5
Tax rate	48%	46%	47%	41%	48%
Transfer rate	97%	49%	33%	22%	9%
Average $t\&T$ rate	-48%	-3%	15%	19%	40%
Marginal $t\&T$ rate	56%	58%	59%	59%	61%

- Different tax rates and transfer rates, **not so different overall rates**

Taking stock

- With a Utilitarian planner, transfers should be more generous, but taxes should not be much more progressive
- Monotonic marginal rates deliver large welfare gains
 - **UBI** delivers large gains

A focus on the household structure

- Guner, Kaygusuz and Ventura (2023)
 - A very rich modeling of the current US system
 - Simple exploration of the optimal welfare state

A focus on the household structure

- Guner, Kaygusuz and Ventura (2023)
 - A very rich modeling of the current US system
 - Simple exploration of the optimal welfare state
- Depart from the typical household structure
 - Heterogeneity in **gender** x **hh structure** x **education**
 - + Income risk
 - + Number of kids and cost of labor force participation
 - + Tax-and-transfer system

A focus on the household structure

Guner et al. (2023)

- Detailed modeling of the existing tax-and-transfer system

- Progressive taxes by hh structure: τ^M , τ^F
- Tax credits as in the data
- Childcare subsidies as a function of hh structure and children age
- Other transfers

A focus on the household structure

Guner et al. (2023)

- Detailed modeling of the existing tax-and-transfer system

- Progressive taxes by hh structure: τ^M , τ^F
- Tax credits as in the data
- Childcare subsidies as a function of hh structure and children age
- Other transfers

- Control: consumption, savings, extensive and intensive labor decision

A focus on the household structure

Guner et al. (2023)

- Detailed modeling of the existing tax-and-transfer system
 - Progressive taxes by hh structure: τ^M , τ^F
 - Tax credits as in the data
 - Childcare subsidies as a function of hh structure and children age
 - Other transfers
- Control: consumption, savings, extensive and intensive labor decision
- Capture accurately income risk by hh structure, gender, education
 - Increasing of the wage-gender gap over the life-cycle
 - Smaller increase in variance of log earnings for female
 - U-shape female labor force participation

A focus on the household structure

Guner et al. (2023)

Very simple exploration of the welfare state **in PE** and **steady-state**

A focus on the household structure

Guner et al. (2023)

Very simple exploration of the welfare state **in PE** and **steady-state**

- Replacing the welfare state with... **nothing**
 - Aggregate welfare losses, especially for single females
 - Majority support

A focus on the household structure

Guner et al. (2023)

Very simple exploration of the welfare state **in PE** and **steady-state**

- Replacing the welfare state with... **nothing**
 - Aggregate welfare losses, especially for single females
 - Majority support

- Implementing a **UBI**: optimal \$12,500
 - Keeping the progressivity fixed, adjusting λ
 - Aggregate **welfare losses**, especially from unskilled single females
 - Welfare gains from married households, and **majority support**

A focus on the household structure

Guner et al. (2023)

■ Implementing a Negative Income Tax

- Income tax progressivity at $\tau = 0$, adjust λ
- Optimal transfer is \$18,500 per individual

A focus on the household structure

Guner et al. (2023)

■ Implementing a Negative Income Tax

- Income tax progressivity at $\tau = 0$, adjust λ
- Optimal transfer is \$18,500 per individual
- Welfare gains, and majority support, output roughly constant
- Still, unskilled single females loose

A focus on the household structure

Guner et al. (2023)

■ Implementing a Negative Income Tax

- Income tax progressivity at $\tau = 0$, adjust λ
- Optimal transfer is \$18,500 per individual
- Welfare gains, and majority support, output roughly constant
- Still, unskilled single females loose

■ Important to think of transfers with taxes!

Quantitative Macro Public Finance

- Very active field to bridge the gap between Mirrlees and Ramsey
 - Quantify redistribution needs and efficiency concerns
 - Flexible modeling yet serious calibration
 - Policy!

3. Revisiting the Welfare State

Fighting the Recession

Motivation

- Design of counter-cyclical policies
 - Monetary policy: short-term nominal interest rate
 - Fiscal policy: spending, unemployment benefits, lump-sum checks

Motivation

- Design of counter-cyclical policies
 - Monetary policy: short-term nominal interest rate
 - Fiscal policy: spending, unemployment benefits, lump-sum checks
- Explore the distribution of labor income taxes as a counter-cyclical policy

Motivation

- Design of counter-cyclical policies

- Monetary policy: short-term nominal interest rate
 - Fiscal policy: spending, unemployment benefits, lump-sum checks

- Explore the distribution of labor income taxes as a counter-cyclical policy

- Not commonly used in practice
 - Empirically, tax cuts have large macro effects

Mertens and Ravn (2013), Zidar (2019)

Motivation

- Design of counter-cyclical policies
 - Monetary policy: short-term nominal interest rate
 - Fiscal policy: spending, unemployment benefits, lump-sum checks
- Explore the distribution of labor income taxes as a counter-cyclical policy
 - Not commonly used in practice
 - Empirically, tax cuts have large macro effects
Mertens and Ravn (2013), Zidar (2019)
- “Fiscal Management of Aggregate Demand” Ferriere Navarro (2024)
 - Quantitative HANK model
 - Effectiveness of various fiscal stabilization packages after a negative demand shock

Framework

- Standard HANK model with three additional components

Framework

- Standard HANK model with three additional components
 - **Heterogeneous** stochastic discount factors → heterogeneous mpc

Framework

- Standard HANK model with three additional components
 - Heterogeneous stochastic discount factors → heterogeneous mpc
 - An extensive labor supply margin → heterogeneous labor elasticities

Framework

- Standard HANK model with three additional components
 - Heterogeneous stochastic discount factors → heterogeneous mpc
 - An extensive labor supply margin → heterogeneous labor elasticities
 - Unemployment risk of heterogeneous incidence & varying with the cycle

Framework

- Standard HANK model with three additional components
 - Heterogeneous stochastic discount factors → heterogeneous mpc
 - An extensive labor supply margin → heterogeneous labor elasticities
 - Unemployment risk of heterogeneous incidence & varying with the cycle
- ⇒ Relevant framework to quantify fiscal stabilization packages

Framework

- Standard HANK model with three additional components
 - Heterogeneous stochastic discount factors → heterogeneous mpc
 - An extensive labor supply margin → heterogeneous labor elasticities
 - Unemployment risk of heterogeneous incidence & varying with the cycle
- ⇒ Relevant framework to quantify fiscal stabilization packages
- Demand-driven recession
 - Negative shock to marginal utility: unexpected, deterministic, transitory

Fiscal Stabilization Packages

- Three fiscal stabilization packages

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (TT) Package: a transfer targeted to **low-income** households

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (**TT**) Package: a transfer targeted to **low-income** households
 - Unemployment Insurance (**UI**) Package: a transfer to **unemployed** households

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (**TT**) Package: a transfer targeted to **low-income** households
 - Unemployment Insurance (**UI**) Package: a transfer to **unemployed** households
 - Tax Credit (**TC**) Package: a tax credit to **low-income working** households

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (**TT**) Package: a transfer targeted to **low-income** households
 - Unemployment Insurance (**UI**) Package: a transfer to **unemployed** households
 - Tax Credit (**TC**) Package: a tax credit to **low-income working** households
- ⇒ The **TC Package** is **the most effective** to stabilize the economy
 - Output **multiplier above 0.8**, compared to ≈ 0.5 for UI & 0.3 for TT

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (**TT**) Package: a transfer targeted to **low-income** households
 - Unemployment Insurance (**UI**) Package: a transfer to **unemployed** households
 - Tax Credit (**TC**) Package: a tax credit to **low-income working** households
- ⇒ The **TC Package** is **the most effective** to stabilize the economy
 - Output **multiplier above 0.8**, compared to ≈ 0.5 for UI & 0.3 for TT
 - Operates through both labor supply and consumption

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (**TT**) Package: a transfer targeted to **low-income** households
 - Unemployment Insurance (**UI**) Package: a transfer to **unemployed** households
 - Tax Credit (**TC**) Package: a tax credit to **low-income working** households
- ⇒ The **TC Package** is **the most effective** to stabilize the economy
 - Output **multiplier above 0.8**, compared to ≈ 0.5 for UI & 0.3 for TT
 - Operates through both labor supply and consumption
 - Despite the larger unemployment risk

Fiscal Stabilization Packages

- Three fiscal stabilization packages
 - Targeted-Transfer (TT) Package: a transfer targeted to **low-income** households
 - Unemployment Insurance (UI) Package: a transfer to **unemployed** households
 - Tax Credit (TC) Package: a tax credit to **low-income working** households
- ⇒ The **TC Package** is **the most effective** to stabilize the economy
 - Output **multiplier above 0.8**, compared to ≈ 0.5 for UI & 0.3 for TT
 - Operates through both labor supply and consumption
 - Despite the larger unemployment risk
- **Robustness:** Alternative calibrations, other standard fiscal packages
- Discussion: **Implementability** and limits

A HANK model with some twists

■ Households

- Bond economy with borrowing constraint
- Stochastic discount factors
- Indivisible labor choice
- Idiosyncratic labor productivity shocks + **unemployment** shocks

■ NK block with sticky prices

- Linear technology in labor
- Monetary authority implements a standard Taylor rule

■ Government

- Finances spending, transfers, UI benefits and debt with labor and capital taxes

Households

Working households

- Individual **state**: asset a , discount factor β , productivity x , and employment $\eta \in \{e, u\}$

Households

Working households

- Individual **state**: asset a , discount factor β , productivity x , and employment $\eta \in \{e, u\}$
- Value function when not into unemployment $\eta = e$

$$V_t(a, x, e, \beta) = \max_{c, h, a'} \{ \log c - Bh + \beta \mathbb{E}_t [V_{t+1}(a', x', \eta', \beta') | x, \beta, e] \} \quad \text{s.t.}$$
$$c + a' = a + y^\ell + y^k - \mathcal{T}_t(y^\ell, y^k) + T_t + d_t^h(x),$$
$$y^\ell = w_t x h, \quad y^k = r_t a, \quad h \in \{0, \bar{h}\}, \quad a' \geq 0.$$

Households

Working households

- Individual **state**: asset a , discount factor β , productivity x , and employment $\eta \in \{e, u\}$
- Value function when not into unemployment $\eta = e$

$$V_t(a, x, e, \beta) = \max_{c, h, a'} \{ \log c - Bh + \beta \mathbb{E}_t [V_{t+1}(a', x', \eta', \beta') | x, \beta, e] \} \quad \text{s.t.}$$
$$c + a' = a + y^\ell + y^k - \mathcal{T}_t(y^\ell, y^k) + T_t + d_t^h(x),$$
$$y^\ell = w_t x h, \quad y^k = r_t a, \quad h \in \{0, \bar{h}\}, \quad a' \geq 0.$$

- Preference shock on discrete labor choice, distributed Gumbel with variance ρ_h
+ $\rho_h \geq 0$ calibrated to discipline labor elasticities
- AR(1) process for discount factor, productivity and employment status
- Flat capital tax τ^k , progressive loglinear labor tax (λ_t, τ^ℓ)
Heathcote, Storesletten, and Violante (2017)

Households

Unemployed households

- Value function when unemployed $\eta = u$

$$V_t(a, x, u, \beta) = \max_{c, a'} \left\{ \log c - B\bar{h} + \beta \mathbb{E}_t [V_{t+1}(a', x', \eta', \beta') | x, \beta, u] \right\} \quad \text{s.t.}$$
$$c + a' = a + y^\ell + y^k + \mathcal{B}_t(w_t x) - \mathcal{T}_t(y^\ell, y^k) + T_t + d_t^h(x),$$
$$y^\ell = \chi w_t x \bar{h}, \quad y^k = r_t a, \quad a' \geq 0.$$

Households

Unemployed households

- Value function when unemployed $\eta = u$

$$\begin{aligned} V_t(a, x, u, \beta) &= \max_{c, a'} \left\{ \log c - B\bar{h} + \beta \mathbb{E}_t [V_{t+1}(a', x', \eta', \beta') | x, \beta, u] \right\} \quad \text{s.t.} \\ c + a' &= a + y^\ell + y^k + \mathcal{B}_t(w_t x) - \mathcal{T}_t(y^\ell, y^k) + T_t + d_t^h(x), \\ y^\ell &= \chi w_t x \bar{h}, \quad y^k = r_t a, \quad a' \geq 0. \end{aligned}$$

- Unemployment benefits function of hourly wage $\mathcal{B}_t(w_t x) = \zeta \max (\mathcal{R} w_t x \bar{h}, \overline{ui})$
Kekre (2022)
 - + ζ to match fraction of recipients, \mathcal{R} the replacement rate, \overline{ui} the UI cap
- χ to capture household labor income received while in unemployment
Kekre (2022)
 - + Calibrated to match the consumption ratio of unemployed to employed
- AR(1) process for discount factors, productivity and employment status

Firms

- Standard two-layer structure with a final-good producer and intermediate good producers
 - Sticky prices a la Rotemberg

Firms and Government

- Standard two-layer structure with a final-good producer and intermediate good producers
 - Sticky prices a la Rotemberg
- Monetary authority follows a Taylor rule with parameter Φ_{Π} on inflation

Firms and Government

- Standard two-layer structure with a final-good producer and intermediate good producers
 - Sticky prices a la Rotemberg
- Monetary authority follows a Taylor rule with parameter Φ_{Π} on inflation
- Fiscal authority faces a standard borrowing constraint

$$G_t + (1 + r_t)D_t + T_t + \int \mathcal{B}_t(w_t x) d\mu_t = D_{t+1} + \int \mathcal{T}_t(y_t^\ell, y_k^t) d\mu_t$$

Firms and Government

- Standard two-layer structure with a final-good producer and intermediate good producers
 - Sticky prices a la Rotemberg
- Monetary authority follows a Taylor rule with parameter Φ_{Π} on inflation
- Fiscal authority faces a standard borrowing constraint

$$G_t + (1 + r_t)D_t + T_t + \int \mathcal{B}_t(w_t x) d\mu_t = D_{t+1} + \int \mathcal{T}_t(y_t^\ell, y_k^t) d\mu_t$$

- Fiscal rule with parameter Φ_D for public debt, λ_t clears the budget constraint
Uhlig (2010)
 - + $\Phi_D = 0$ for constant debt, $\Phi_D = 1$ for constant λ
 - + $\Phi_D > 0$ implies larger debt in case of lower tax base and higher expenditures

Steady State Households

- Quarterly model calibrated to liquid wealth
- Stochastic β with average duration of 50 years
 - Mean s.t. $r \equiv 3\%$ annually
 - Variance s.t. top-quintile liquid wealth $\approx 90\%$ (SCF)

Steady State Households

- Quarterly model calibrated to liquid wealth
- Stochastic β with average duration of 50 years
 - Mean s.t. $r \equiv 3\%$ annually
 - Variance s.t. top-quintile liquid wealth $\approx 90\%$ (SCF)
- Labor supply decisions
 - B to match employment $\approx 78\%$
Jang, Sunakawa, and Yum (2023)
 - ρ_h to match annual labor elasticity of ≈ 0.5 for the bottom quartile
Ferriere and Navarro (2024)
Triest (1990), Eissa and Liebman (1996), Kleven and Kreiner (2006), Meghir and Phillips (2010)

Steady State Households

- Quarterly model calibrated to liquid wealth
- Stochastic β with average duration of 50 years
 - Mean s.t. $r \equiv 3\%$ annually
 - Variance s.t. top-quintile liquid wealth $\approx 90\%$ (SCF)
- Labor supply decisions
 - B to match employment $\approx 78\%$
Jang, Sunakawa, and Yum (2023)
 - ρ_h to match annual labor elasticity of ≈ 0.5 for the bottom quartile
Ferriere and Navarro (2024)
Triest (1990), Eissa and Liebman (1996), Kleven and Kreiner (2006), Meghir and Phillips (2010)
- Productivity $(\rho_x, \sigma_x) = (0.989, 0.287)$
Chang and Kim (2007)

Steady State Unemployment

- Job finding rates and separation rates across hourly wage distribution

Steady State Unemployment

- Job finding rates and separation rates across hourly wage distribution
- Job finding rates are constant in the distribution distribution
Mueller (2017)
 - Monthly finding rate of 0.32 $\Rightarrow \pi_\eta(e|u) = 0.691$

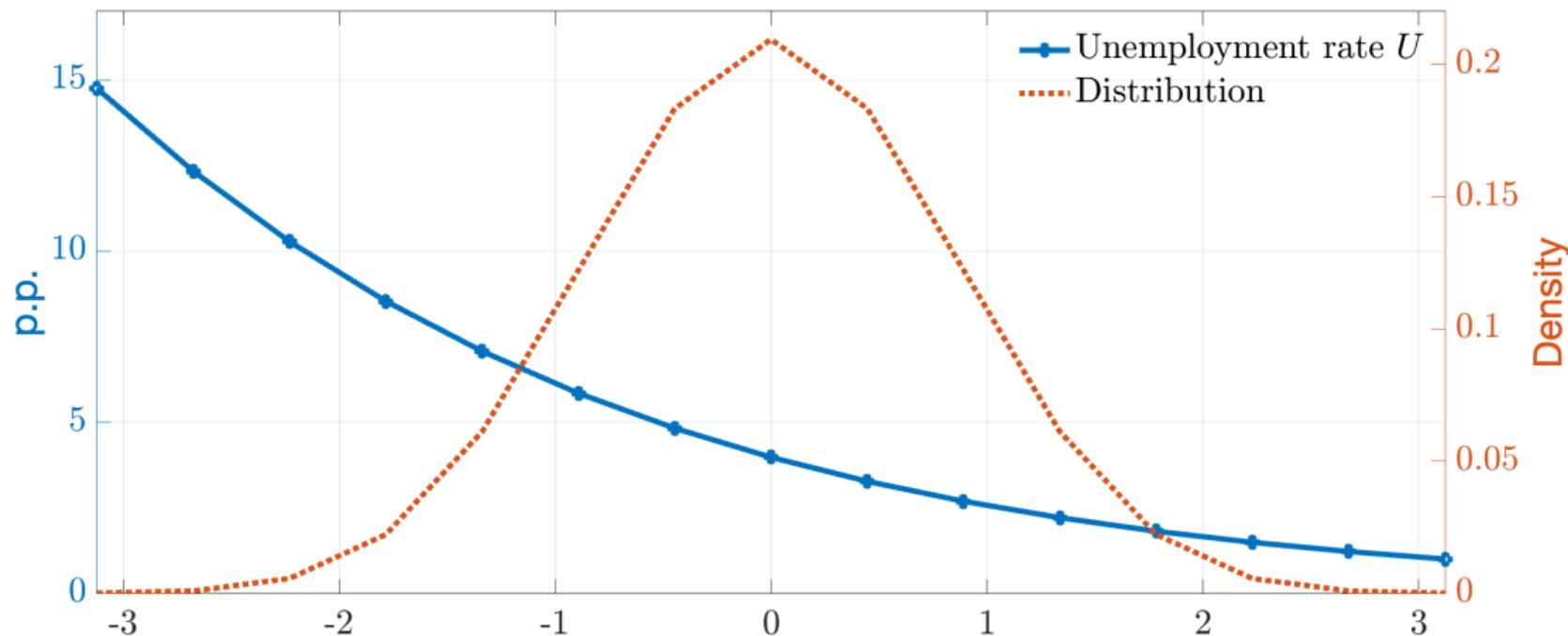
Steady State Unemployment

- Job finding rates and separation rates across hourly wage distribution
- Job finding rates are constant in the distribution distribution
Mueller (2017)
 - Monthly finding rate of 0.32 $\Rightarrow \pi_\eta(e|u) = 0.691$
- Separation rates falling in hourly wage/productivity x
Mueller (2017)
 - Monthly separation rates of $\approx 1.4\%$ and 0.7% below and above median, respectively
 - $\Rightarrow \pi_\eta(u|e, x) = \phi_0 x^{\phi_1}$, with $\phi_0 = 0.029$ and $\phi_1 = -0.446$

Steady State Unemployment

- Job finding rates and separation rates across hourly wage distribution
- Job finding rates are constant in the distribution distribution
Mueller (2017)
 - Monthly finding rate of 0.32 $\Rightarrow \pi_\eta(e|u) = 0.691$
- Separation rates falling in hourly wage/productivity x
Mueller (2017)
 - Monthly separation rates of $\approx 1.4\%$ and 0.7% below and above median, respectively
 - $\Rightarrow \pi_\eta(u|e, x) = \phi_0 x^{\phi_1}$, with $\phi_0 = 0.029$ and $\phi_1 = -0.446$
- Average unemployment rate at 4.3% with unequal incidence in the distribution
- Fraction of labor income when unemployed $\chi = 0.21$ to match $C_u/C_e \approx 75\%$
Gorn and Trigari (2024)

Steady State Unemployment in the Distribution



Steady State Firm and government

- Technology: $\varepsilon = 7$, $\Theta = 200$

Galí and Gertler (1999)

- Dividends redistributed linearly in x

Farhi and Werning (2019)

Steady State Firm and government

- Technology: $\varepsilon = 7$, $\Theta = 200$

Galí and Gertler (1999)

- Dividends redistributed linearly in x

Farhi and Werning (2019)

- Government

- Capital tax $\tau_k = 35\%$

Chen, Imrohoroglu, and Imrohoroglu (2007)

- Labor income tax progressivity $\tau_\ell = 0.1$

Heathcote, Storesletten, and Violante (2017), Ferriere, Grübener, Navarro, and Vardishvili (2023b)

- Spending $G/Y = 10\%$, transfers $T/Y = 8\%$, debt $D/Y = 100\%$

- Unemployment benefits: $\zeta = 0.4$, $\mathcal{R} = 0.5$, $\overline{ui} = 60\% \bar{y}$

Kekre (2022)

- Automatic responses: $\Phi_\Pi = 1.5$, $\Phi_D = 0.75$

Unemployment and the Business Cycle Okun's law

- Okun's law type of relation between output and unemployment
 - Okun coefficient $c_{OK} = 0.5$: $U_t = U - 0.5 \log(Y_t/Y) = U - 0.5\Delta Y_t$
Ball, Leigh, and Loungani (2017)

Unemployment and the Business Cycle

Okun's law

- Okun's law type of relation between output and unemployment
 - Okun coefficient $c_{OK} = 0.5$: $U_t = U - 0.5 \log(Y_t/Y) = U - 0.5\Delta Y_t$
Ball, Leigh, and Loungani (2017)
- Job finding rates increase homogeneously with U_t
Mueller (2017)
 - Elasticity of monthly job finding rates to unemployment rate of **-0.6**

Unemployment and the Business Cycle

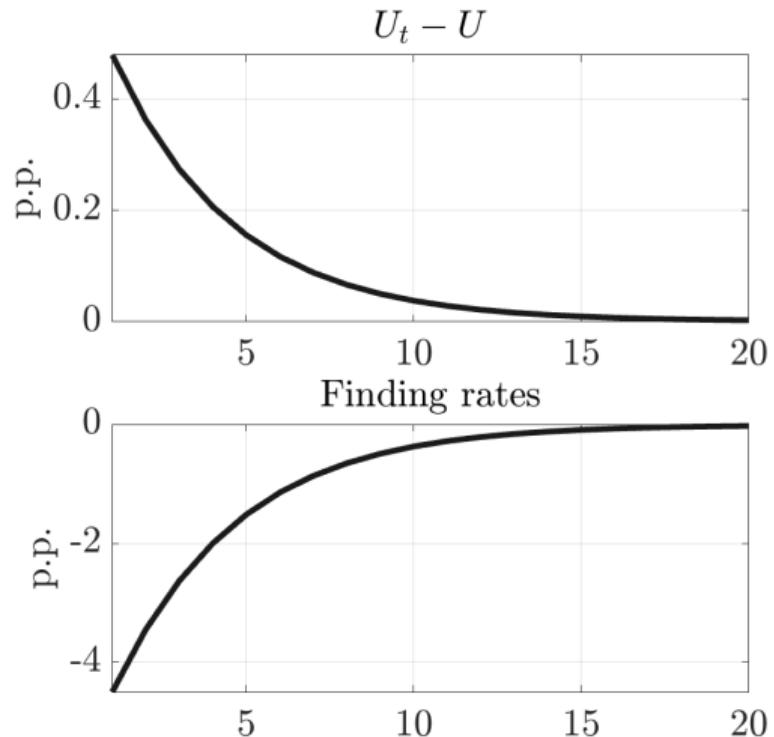
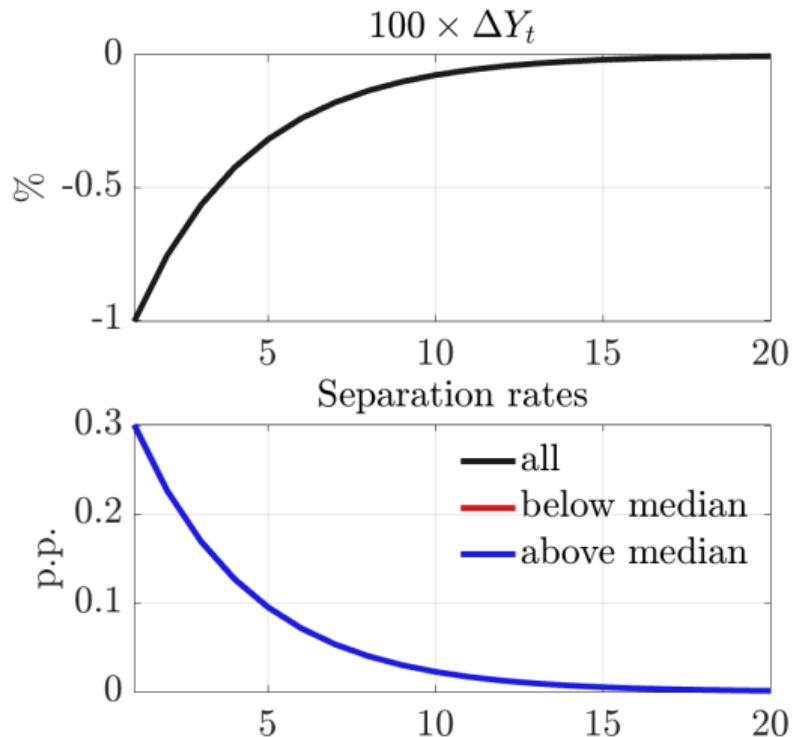
Okun's law

- Okun's law type of relation between output and unemployment
 - Okun coefficient $c_{OK} = 0.5$: $U_t = U - 0.5 \log(Y_t/Y) = U - 0.5\Delta Y_t$
Ball, Leigh, and Loungani (2017)
- Job finding rates increase homogeneously with U_t
Mueller (2017)
 - Elasticity of monthly job finding rates to unemployment rate of -0.6
- Job separation rates? A flexible formulation

$$\pi_{\eta,t}(u|x, e) = \pi_\eta(u|x, e) - \phi_{eu}^a \Delta Y_t x^{-\phi_{eu}^b}$$

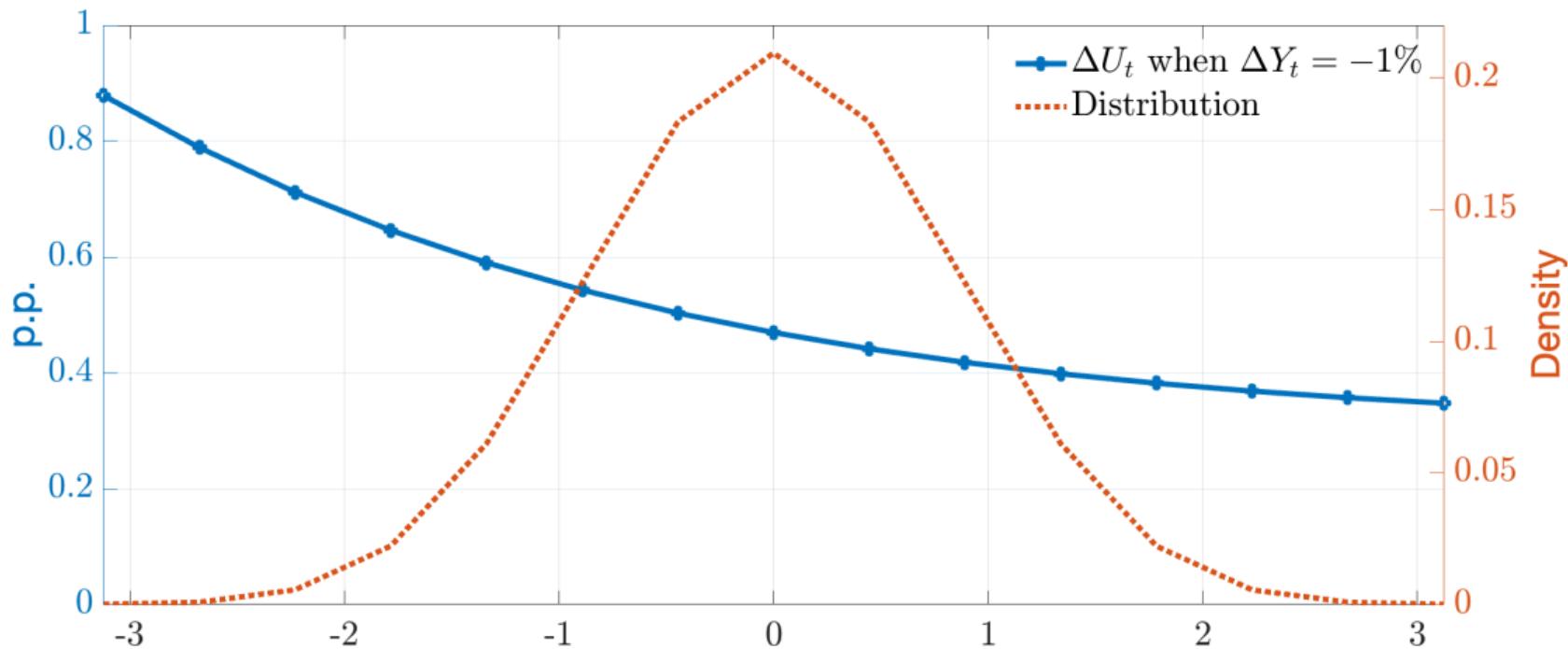
Unemployment and the Business Cycle

Okun's law



Unemployment and the Business Cycle

Okun's law



Investigating the Calibration mpc

- Marginal propensities to consume (**mpc**) out of a \$500 rebate quarterly

Parker, Souleles, Johnson, and McClelland (2013), Kaplan and Violante (2014), ...

- Average quarterly mpc of **0.13**, declining with wealth

Wealth quartile	1	2	3	4
mpc	0.19	0.15	0.07	0.03

Investigating the Calibration mpc

- Marginal propensities to consume (**mpc**) out of a \$500 rebate quarterly

Parker, Souleles, Johnson, and McClelland (2013), Kaplan and Violante (2014), ...

- Average quarterly mpc of **0.13**, declining with wealth

Wealth quartile	1	2	3	4
mpc	0.19	0.15	0.07	0.03

- Larger for unemployed at **0.32**
 - + Unemployment drop when falling into unemployment: **-10%**
Ganong Noel (2017)

Investigating the Calibration

Labor elasticities

- Labor elasticities decline with income

- Simulate steady-state model annually and run applied-micro regression

Rogerson and Wallenius (2009), Chang and Kim (2006)

- + Estimate b_1 in $\log h_{in} = b_0 + \textcolor{red}{b}_1 \log \tilde{w}_{in} - b_2 \log c_{in} + \varepsilon_{in}$

- + Aggregate labor elasticity is **0.28**, declining with income

Investigating the Calibration

Labor elasticities

■ Labor elasticities decline with income

- Simulate steady-state model annually and run applied-micro regression
Rogerson and Wallenius (2009), Chang and Kim (2006)
 - + Estimate b_1 in $\log h_{in} = b_0 + \textcolor{red}{b}_1 \log \tilde{w}_{in} - b_2 \log c_{in} + \varepsilon_{in}$
 - + Aggregate labor elasticity is **0.28**, declining with income
- Compute labor responses to a temporary tax shock
Erosa, Fuster, and Kambourov (2016)
 - + Annual hours response to a 1% change in after-tax rate for one year
 - + Aggregate labor elasticity is **0.31**, declining with income

Investigating the Calibration

Labor elasticities

■ Labor elasticities decline with income

- Simulate steady-state model annually and run applied-micro regression
Rogerson and Wallenius (2009), Chang and Kim (2006)
 - + Estimate b_1 in $\log h_{in} = b_0 + \textcolor{red}{b}_1 \log \tilde{w}_{in} - b_2 \log c_{in} + \varepsilon_{in}$
 - + Aggregate labor elasticity is **0.28**, declining with income
- Compute labor responses to a temporary tax shock
Erosa, Fuster, and Kambourov (2016)
 - + Annual hours response to a 1% change in after-tax rate for one year
 - + Aggregate labor elasticity is **0.31**, declining with income

Income quartile	1	2	3	4
Labor elasticities (regression)	0.54	0.32	0.13	0.11
Labor elasticities (tax shock)	0.43	0.33	0.25	0.22

Investigating the calibration Tax shocks

- Further investigate aggregate effects of tax shocks

Investigating the calibration Tax shocks

- Further investigate aggregate effects of tax shocks
- Compute tax multipliers as in Mertens and Ravn (2013)
 - Tax multiplier at about 0.6 in the model, vs. above 2 in the data
 - Peaks on impact in the model, at 3 quarters in the model

Investigating the calibration

Tax shocks

- Further investigate aggregate effects of tax shocks
- Compute tax multipliers as in Mertens and Ravn (2013)
 - Tax multiplier at about 0.6 in the model, vs. above 2 in the data
 - Peaks on impact in the model, at 3 quarters in the model
- Replicate a tax shock on bottom-90 vs. top-10 as in Zidar (2019)
 - Tax cut on bottom-90 increases employment by 1% in the model vs. above 3% in the data
 - Tax cut on the top-10 has no effects
 - Peaks on impact in the model, at 2 years in the model

Investigating the calibration

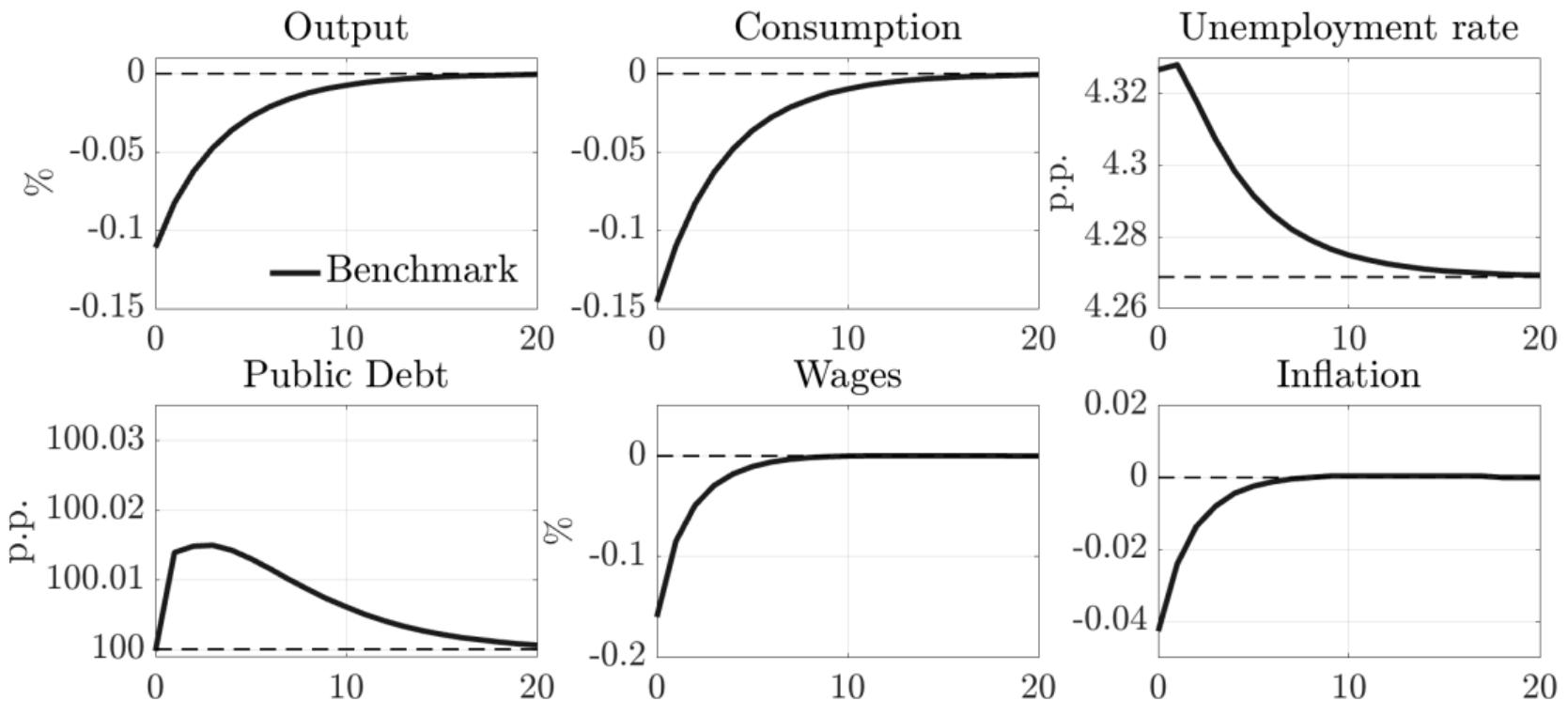
Tax shocks

- Further investigate aggregate effects of tax shocks
 - Compute tax multipliers as in Mertens and Ravn (2013)
 - Tax multiplier at about 0.6 in the model, vs. above 2 in the data
 - Peaks on impact in the model, at 3 quarters in the model
 - Replicate a tax shock on bottom-90 vs. top-10 as in Zidar (2019)
 - Tax cut on bottom-90 increases employment by 1% in the model vs. above 3% in the data
 - Tax cut on the top-10 has no effects
 - Peaks on impact in the model, at 2 years in the model
- ⇒ Conservative calibration regarding tax responses

Benchmark No Fiscal Stabilization

- Recession induced by a negative demand shock: $(1 - \omega_t)u(c_t, n_t)$
 - ω_0 such that $\Delta Y_t = -0.10\%$ on impact
 - Reverts to $\omega = 0$ with persistence $\rho_\omega = 0.75$ at the quarterly level
- Unexpected, transitory, perfect foresight: a ‘MIT’ shock

Benchmark No Fiscal Stabilization



Three Fiscal Stabilization Packages TT Package

- A Targeted Transfer (TT) Package
 - Design to mimic checks sent in 2008: For all **low-income** households, based on **last-year** income
 - An “automatic stabilizer” flavor: Phase out over time with persistence ρ_ω

Three Fiscal Stabilization Packages TT Package

■ A Targeted Transfer (TT) Package

- Design to mimic checks sent in 2008: For all **low-income** households, based on **last-year** income
- An “automatic stabilizer” flavor: Phase out over time with persistence ρ_ω
- Temporary transfer modeled as a **logistic** function

Ferriere, Grübener, Navarro, and Vardishvili (2023b)

$$\hat{T}_t(y) = m_t \frac{2 \exp(-\chi y / \bar{y})}{1 + \exp(-\chi y / \bar{y})}, \quad m_t \text{ the } \text{transfer} \text{ at } y = 0, \chi \text{ the } \text{phasing-out} \text{ speed}$$

Three Fiscal Stabilization Packages TT Package

■ A Targeted Transfer (TT) Package

- Design to mimic checks sent in 2008: For all **low-income** households, based on **last-year** income
- An “automatic stabilizer” flavor: Phase out over time with persistence ρ_ω
- Temporary transfer modeled as a **logistic** function

Ferriere, Grübener, Navarro, and Vardishvili (2023b)

$$\hat{T}_t(y) = m_t \frac{2 \exp(-\chi y / \bar{y})}{1 + \exp(-\chi y / \bar{y})}, \quad m_t \text{ the transfer at } y = 0, \chi \text{ the phasing-out speed}$$

+ “Based on **no-recession** income”: $\tilde{y}(x, \eta, \beta)$

Three Fiscal Stabilization Packages

TT Package

■ A Targeted Transfer (TT) Package

- Design to mimic checks sent in 2008: For all **low-income** households, based on **last-year** income
- An “automatic stabilizer” flavor: Phase out over time with persistence ρ_ω
- Temporary transfer modeled as a **logistic** function

Ferriere, Grübener, Navarro, and Vardishvili (2023b)

$$\hat{T}_t(y) = m_t \frac{2 \exp(-\chi y / \bar{y})}{1 + \exp(-\chi y / \bar{y})}, \quad m_t \text{ the transfer at } y = 0, \chi \text{ the phasing-out speed}$$

- + “Based on **no-recession** income”: $\tilde{y}(x, \eta, \beta)$
- Calibration such that $\sum_t \int \hat{T}_t(y) d\mu_t$ equals a one-time check of \$200 to all households
 - + Initial check at $y = 0$ is $m_0 = \$900$
 - + Quick phase-out at $\chi = 12$: 20% households receive more than \$50 at $t = 0$

Three Fiscal Stabilization Packages

UI Package

- A Unemployment Insurance (UI) Package
 - A check to **all** unemployed households, phase out with persistence ρ_ω

Three Fiscal Stabilization Packages

UI Package

■ A Unemployment Insurance (UI) Package

- A check to **all** unemployed households, phase out with persistence ρ_ω
- **Calibration** such that equals a one-time lump-sum check of \$200
 - + Initial check equal to \$1,1000

Three Fiscal Stabilization Packages

UI Package & TC Package

- A Unemployment Insurance (UI) Package

- A check to **all** unemployed households, phase out with persistence ρ_ω
 - **Calibration** such that equals a one-time lump-sum check of \$200
 - + Initial check equal to \$1,1000

- A Tax Credit (TC) Package

- A check to **working low-income** households

Three Fiscal Stabilization Packages

UI Package & TC Package

- A Unemployment Insurance (UI) Package

- A check to **all** unemployed households, phase out with persistence ρ_ω
 - **Calibration** such that equals a one-time lump-sum check of \$200
 - + Initial check equal to \$1,1000

- A Tax Credit (TC) Package

- A check to **working low-income** households
 - + **Phase out** with current labor income $w_t x \bar{h}$
 - + Eligible **only if** $\eta = e$ and $h = \bar{h}$

Three Fiscal Stabilization Packages

UI Package & TC Package

■ A Unemployment Insurance (UI) Package

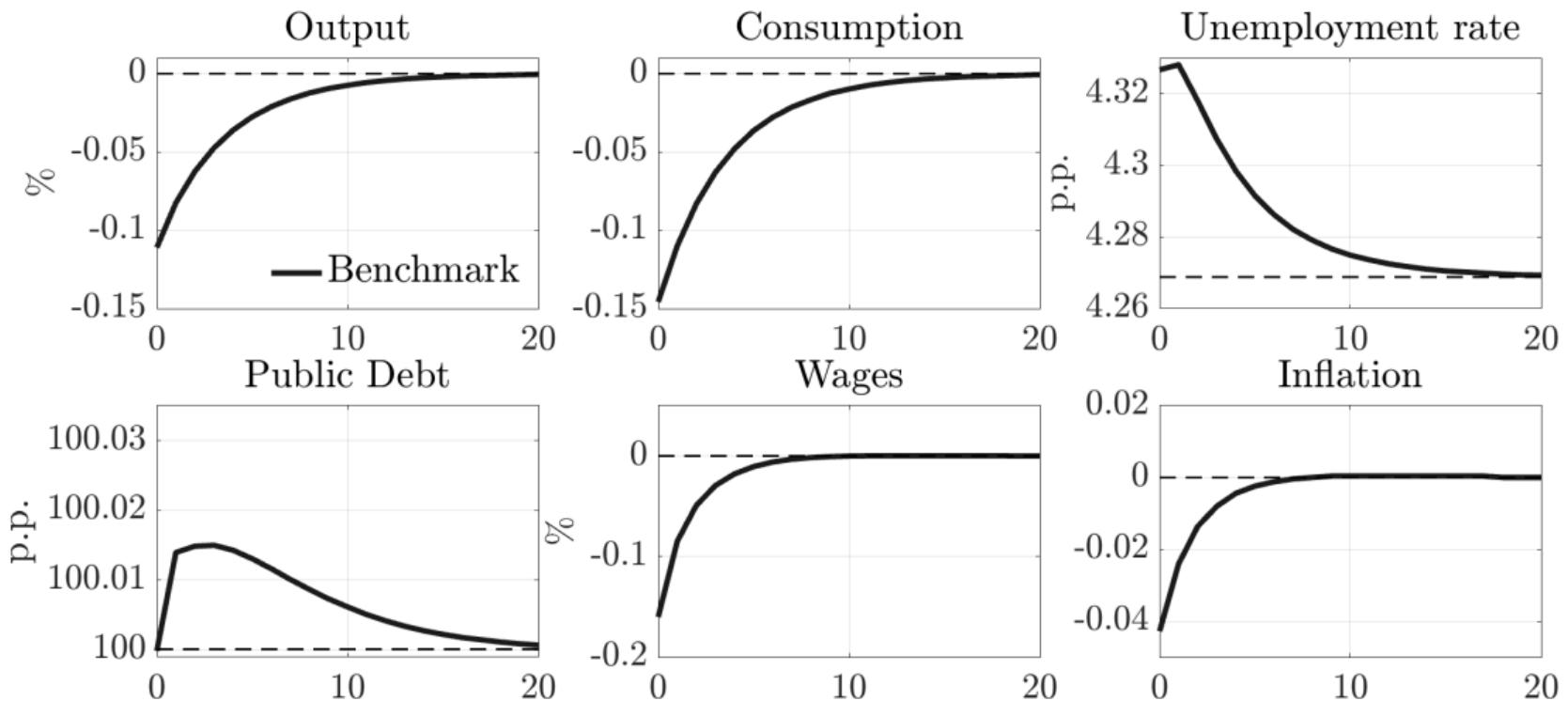
- A check to **all** unemployed households, phase out with persistence ρ_ω
- **Calibration** such that equals a one-time lump-sum check of \$200
 - + Initial check equal to \$1,1000

■ A Tax Credit (TC) Package

- A check to **working low-income** households
 - + **Phase out** with current labor income $w_t x \bar{h}$
 - + Eligible **only if** $\eta = e$ and $h = \bar{h}$
- **Calibration** such that equals a one-time lump-sum check of \$200
 - + Initial maximum check of \$800, slower phase-out at $\chi = 6$

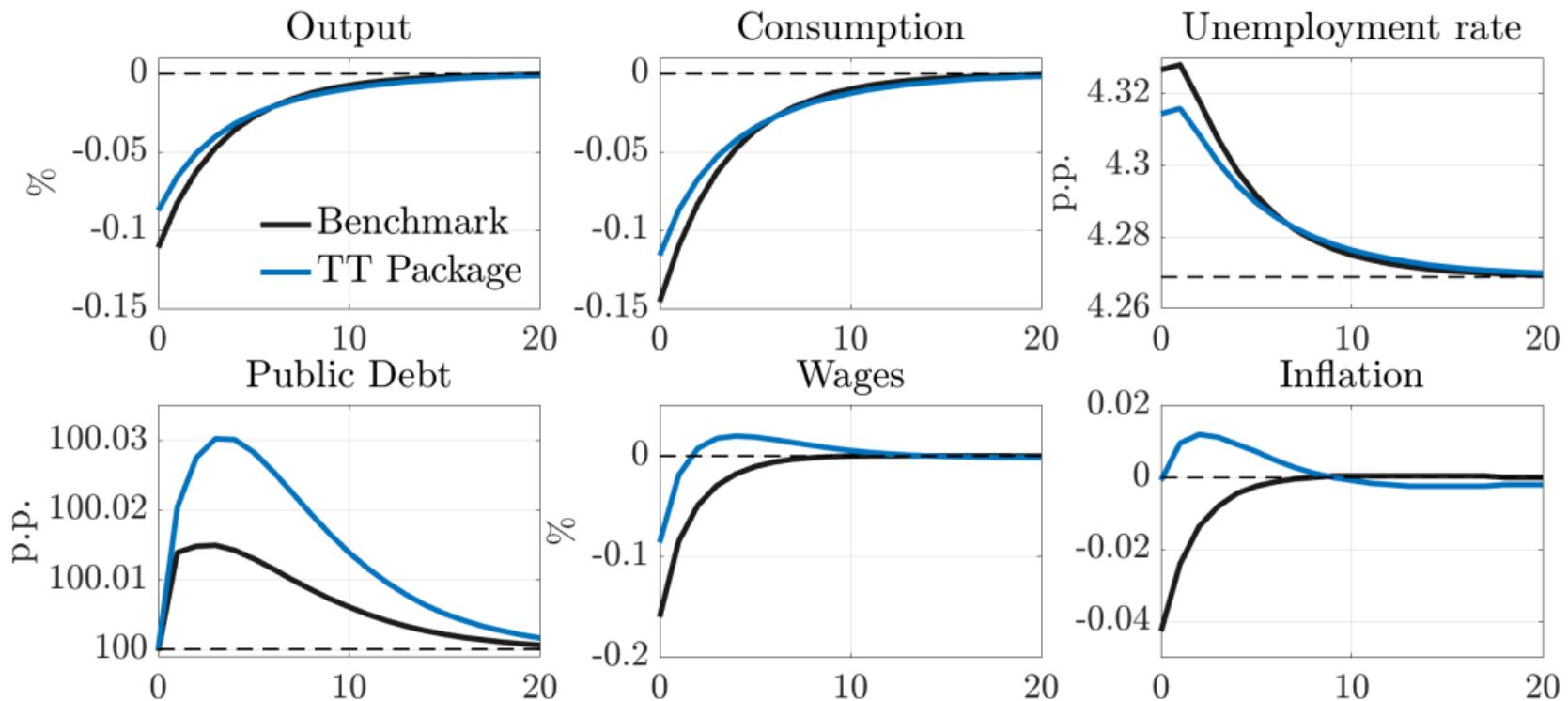
Three Fiscal Stabilization Packages

Impulse Response Functions



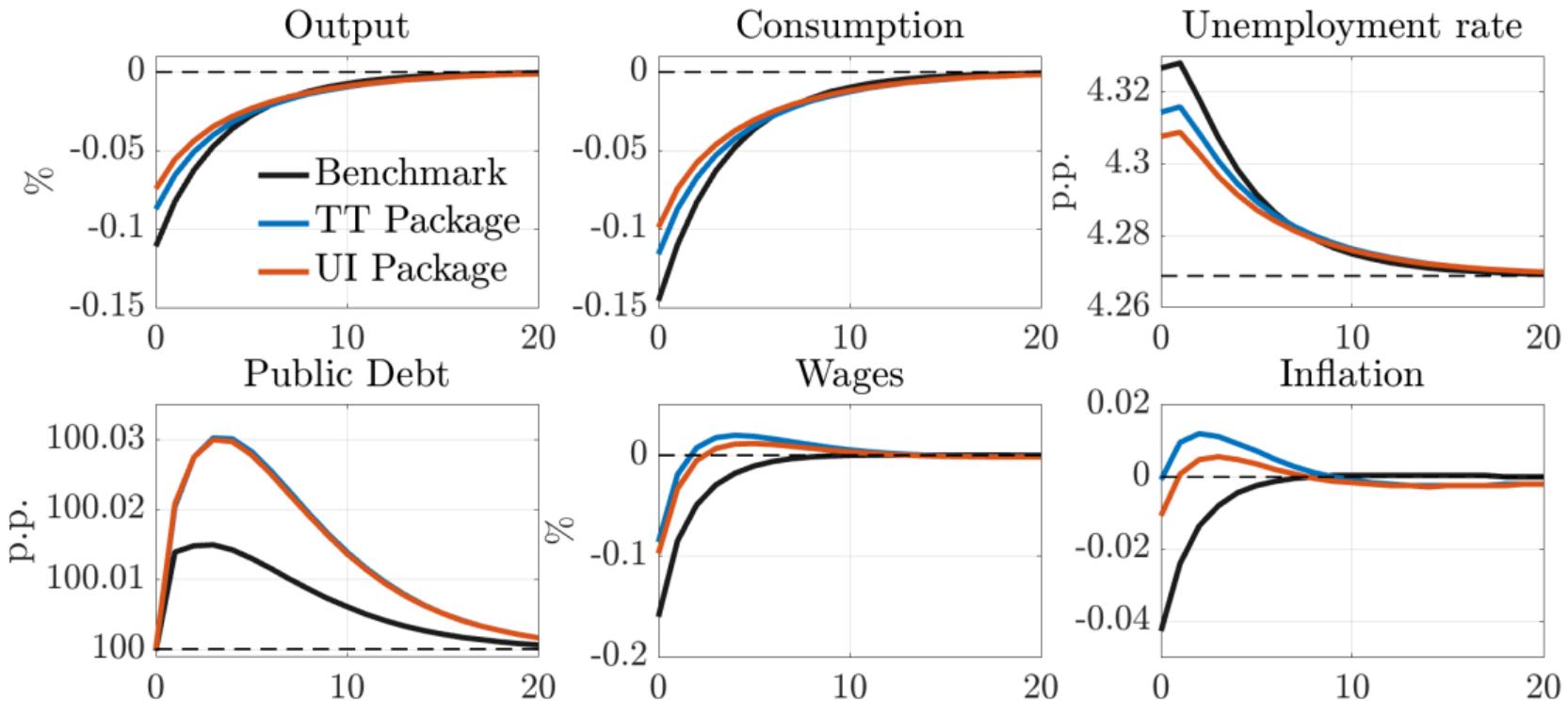
Three Fiscal Stabilization Packages

Impulse Response Functions

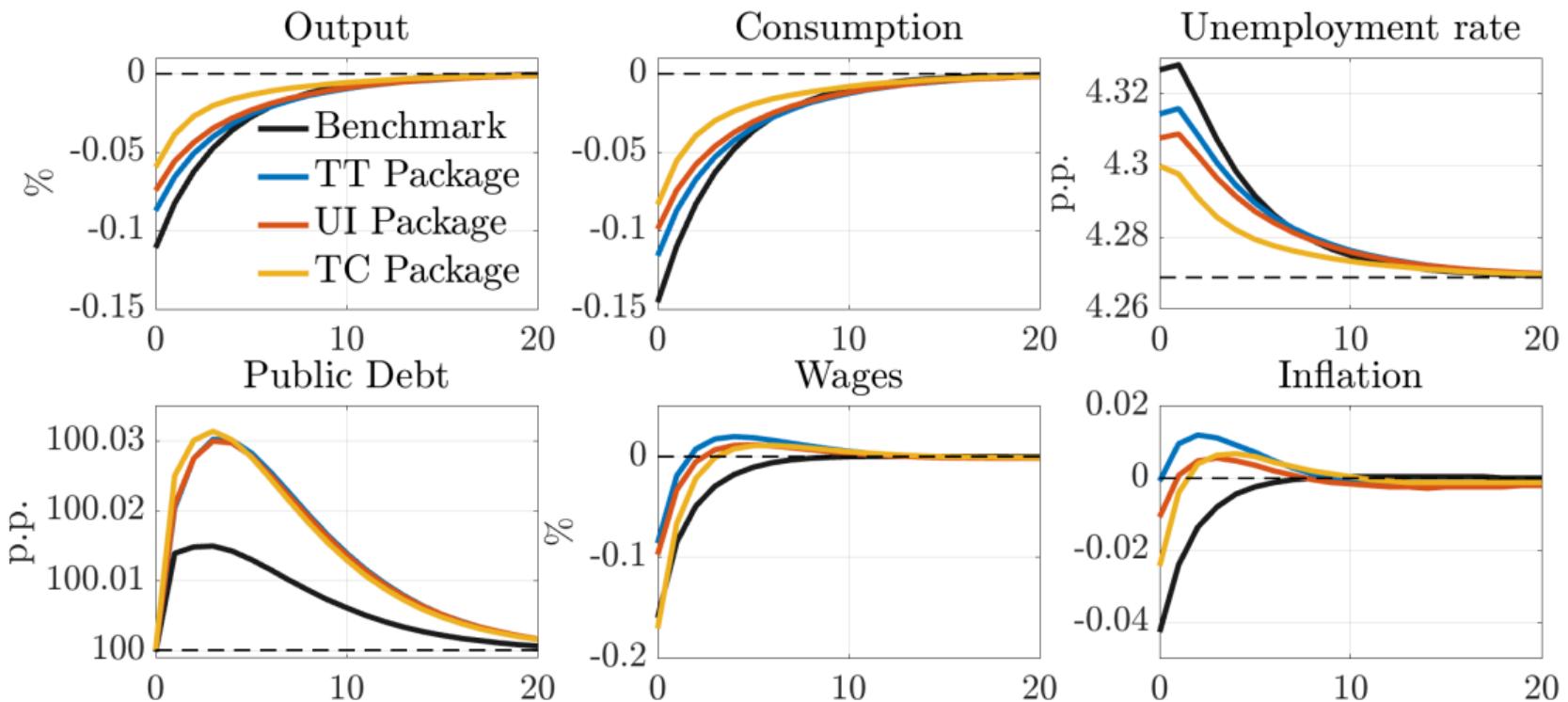


Three Fiscal Stabilization Packages

Impulse Response Functions

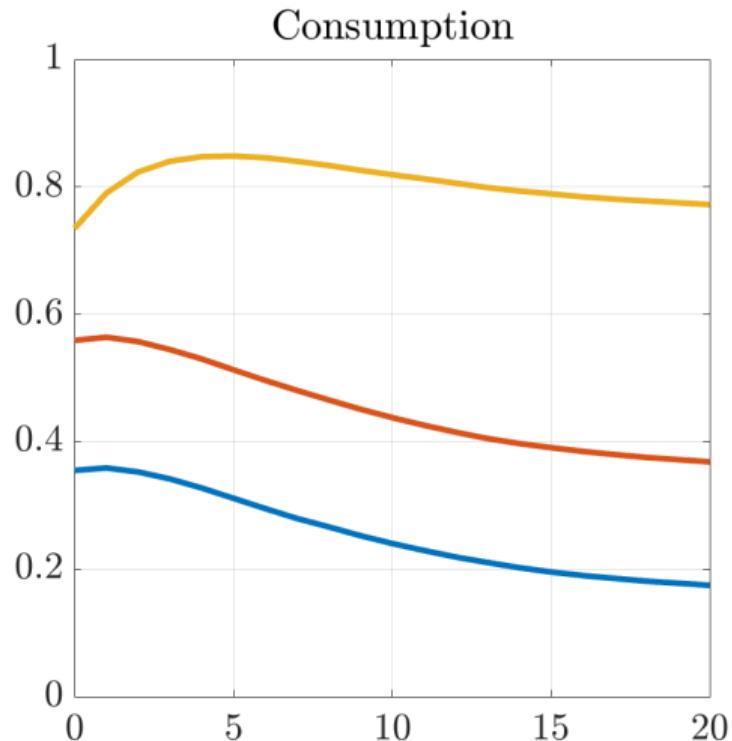
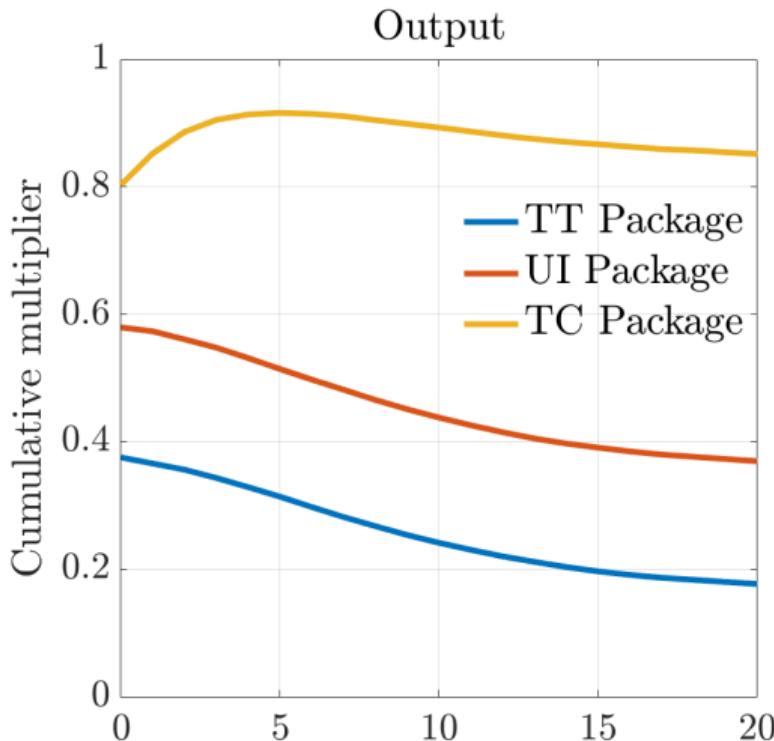


Three Fiscal Stabilization Packages Impulse Response Functions



Three Fiscal Stabilization Packages

Multipliers



Conclusion

- A temporary increase in labor income tax progressivity can stabilize the economy
 - Labor income tax cuts to low-income households
 - Operates also through consumption responses

Conclusion

- A temporary increase in labor income tax progressivity can stabilize the economy
 - Labor income tax cuts to low-income households
 - Operates also through consumption responses
- Temporary cuts in consumption taxes may also be a good idea?

Conclusion

- A temporary increase in labor income tax progressivity can stabilize the economy
 - Labor income tax cuts to low-income households
 - Operates also through consumption responses
- Temporary cuts in consumption taxes may also be a good idea?

Thank you!

Appendix

References

- Aiyagari, S. Rao (1995). "Optimal capital income taxation with incomplete markets, borrowing constraints, and constant discounting". Journal of Political Economy 103.6, pp. 1158–1175.
- Aiyagari, S. Rao, Albert Marcet, Thomas J. Sargent, and Juha Seppälä (2002). "Optimal taxation without state-contingent debt". Journal of Political Economy 110.6, pp. 1220–1254.
- Bach, Laurent, Laurent E. Calvet, and Paolo Sodini (2020). "Rich pickings? Risk, return, and skill in the portfolios of the wealthy". American Economic Review 110.9, pp. 2703–47.
- Ball, Laurence, Daniel Leigh, and Prakash Loungani (2017). "Okun's Law: Fit at 50?" Journal of Money, Credit and Banking 49.7, pp. 1413–1441.
- Bhandari, Anmol and Ellen R McGrattan (Dec. 2020). "Sweat Equity in U.S. Private Business". The Quarterly Journal of Economics 136.2, pp. 727–781.
- Boar, Corina and Matthew Knowles (2020). "Entrepreneurship, Agency Frictions and Redistributive Capital Taxation". Working Paper.
- Chamley, Christophe (1986). "Optimal taxation of capital income in general equilibrium with infinite lives". Econometrica, pp. 607–622.

References (cont.)

- Chang, Yongsung and Sun-Bin Kim (2006). "From individual to aggregate labor supply: A quantitative analysis based on a heterogeneous agent macroeconomy". International Economic Review 47.1, pp. 1–27.
- (2007). "Heterogeneity and Aggregation: Implications for Labor Market Fluctuations". American Economic Review 97, pp. 1939–1956.
- Chari, Varadarajan V., Lawrence J. Christiano, and Patrick J. Kehoe (1994). "Optimal fiscal policy in a business cycle model". Journal of Political Economy 102.4, pp. 617–652.
- Chen, Kaiji, Aye Imrohoroglu, and Selahattin Imrohoroglu (2007). "The Japanese Saving Rate Between 1960 and 2000: Productivity, Policy Changes, and Demographics". Economic Theory 32.1, pp. 87–104.
- Conesa, Juan Carlos, Sagiri Kitao, and Dirk Krueger (2009). "Taxing capital? Not a bad idea after all!" The American Economic Review 99.1, pp. 25–48.
- De Nardi, Mariacristina and Giulio Fella (2017). "Saving and Wealth Inequality". Review of Economic Dynamics 26, pp. 280–300.
- Eissa, Nada and Jeffrey B Liebman (1996). "Labor supply response to the earned income tax credit". The Quarterly Journal of Economics 111.2, pp. 605–637.

References (cont.)

- Erosa, Andrés, Luisa Fuster, and Gueorgui Kambourov (2016). "Towards a micro-founded theory of aggregate labour supply". The Review of Economic Studies 83.3, pp. 1001–1039.
- Fagereng, Andreas, Luigi Guiso, Davide Malacrino, and Luigi Pistaferri (2020). "Heterogeneity and Persistence in Returns to Wealth". Econometrica 88.1, pp. 115–170.
- Farhi, Emmanuel (2010). "Capital Taxation and Ownership when Markets are Incomplete". Journal of Political Economy 118.5, pp. 908–948.
- Ferriere, Axelle, Philipp Grübener, Gaston Navarro, and Oliko Vardishvili (2023a). "On the Optimal Design of Transfers and Income Tax Progressivity". Working Paper.
- (2023b). "On the Optimal Design of Transfers and Income Tax Progressivity". Journal of Political Economy Macroeconomics 1.2, pp. 276–333.
- Ferriere, Axelle and Gaston Navarro (2024). "The Heterogeneous Effects of Government Spending: It's All About Taxes". The Review of Economic Studies Forthcoming.
- Floden, Martin and Jesper Lindé (2001). "Idiosyncratic risk in the United States and Sweden: Is there a role for government insurance?" Review of Economic dynamics 4.2, pp. 406–437.

References (cont.)

- Galí, Jordi and Mark Gertler (1999). "Inflation Dynamics: A Structural Econometric Analysis". Journal of Monetary Economics 44.2, pp. 195–222.
- Garriga, Carlos (2017). "Optimal Fiscal Policy in Overlapping Generations Models". Public Finance Review 47.1, pp. 3–31.
- Gorn, Alexey and Antonella Trigari (2024). "Assessing the Stabilizing Effects of Unemployment Benefit Extensions". American Economic Journal: Macroeconomics 16.1.
- Guvenen, Fatih, Gueorgui Kambourov, Burhan Kuruscu, Sergio Ocampo-Diaz, and Daphne Chen (2023). "Use It or Lose It: Efficiency Gains from Wealth Taxation". QJE.
- Heathcote, Jonathan, Kjetil Storesletten, and Giovanni L. Violante (2014). "Consumption and labor supply with partial insurance: An analytical framework". The American Economic Review 104.7, pp. 2075–2126.
- (2017). "Optimal tax progressivity: An analytical framework". The Quarterly Journal of Economics 132.4, pp. 1693–1754.
- Jang, Youngsoo, Takeki Sunakawa, and Minchul Yum (2023). "Tax-and-Transfer Progressivity and Business Cycles". Quantitative Economics 14 (4), pp. 1367–1400.
- Judd, Kenneth L. (1985). "Redistributive taxation in a simple perfect foresight model". Journal of Public Economics 28.1, pp. 59–83.

References (cont.)

- Kaplan, Greg and Giovanni L Violante (2014). "A model of the consumption response to fiscal stimulus payments". Econometrica 82.4, pp. 1199–1239.
- Kekre, Rohan (Dec. 2022). "Unemployment Insurance in Macroeconomic Stabilization". The Review of Economic Studies 90.5, pp. 2439–2480.
- Kitao, Sagiri (2008). "Entrepreneurship, taxation and capital investment". Review of Economic Dynamics 11.1, pp. 44–69.
- Kleven, Henrik Jacobsen and Claus Thustrup Kreiner (2006). "The Marginal Cost of Public Funds: Hours of Work Versus Labor Force Participation". Journal of Public Economics 90.10, pp. 1955–1973.
- Lucas Jr., Robert E. and Nancy L. Stokey (1983). "Optimal fiscal and monetary policy in an economy without capital". Journal of Monetary Economics 12.1, pp. 55–93.
- MacNamara, Patrick, Myroslav Pidkuyko, and Rafaelle Rossi (2021). "Marginal Tax Changes with Risky Investment". Working Paper.
- Meghir, Costas and David Phillips (2010). "Labour supply and taxes". Dimensions of tax design: The Mirrlees review, pp. 202–74.

References (cont.)

- Mertens, Karel and Morten O. Ravn (2013). "The Dynamic Effects of Personal and Corporate Income Tax Changes in the United States". American Economic Review 103.4, pp. 1212–47.
- Mueller, Andreas I. (2017). "Separations, Sorting, and Cyclical Unemployment". American Economic Review 107.7, pp. 2081–2107.
- Parker, Jonathan A., Nicholas S. Souleles, David S. Johnson, and Robert McClelland (2013). "Consumer Spending and the Economic Stimulus Payments of 2008". American Economic Review 103.6, pp. 2530–53.
- Rogerson, Richard and Johanna Wallenius (2009). "Micro and macro elasticities in a life cycle model with taxes". Journal of Economic theory 144.6, pp. 2277–2292.
- Straub, Ludwig and Iván Werning (2020). "Positive Long-Run Capital Taxation: Chamley-Judd Revisited". American Economic Review 110.1, pp. 86–119.
- Triest, Robert K (1990). "The Effect of Income Taxation on Labor Supply in the United States". Journal of Human Resources, pp. 491–516.
- Uhlig, Harald (2010). "Some Fiscal Calculus". American Economic Review 2.100, pp. 30–34.

References (cont.)

Zidar, Owen (2019). "Tax Cuts for Whom? Heterogeneous Effects of Tax Changes on Growth and Employment".
Journal of Political Economy 127.3, pp. 1437–1472.