

Introducción a NLP

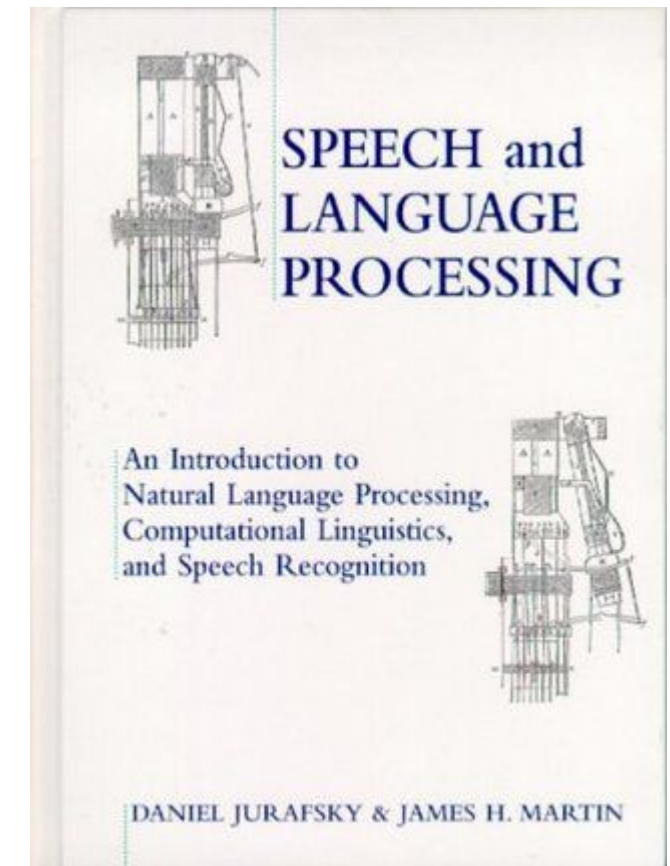
Diego Fernández Slezak

Ciencia de Datos - 2do. cuat. 2017

La biblia...

<https://web.stanford.edu/~jurafsky/slp3/>

- Introduction
- Regular Expressions, Text Normalization, and Edit Distance
- Finite State Transducers
- Language Modeling with N-Grams
- Spelling Correction and the Noisy Channel
- Naive Bayes Classification and Sentiment
- Logistic Regression
- Neural Nets and Neural Language Models
- Hidden Markov Models
- Neural Sequence Modeling: RNNs and LSTMs
- Part-of-Speech Tagging
- Formal Grammars of English
- Syntactic Parsing
- Statistical Parsing
- Dependency Parsing
- Vector Semantics
- Semantics with Dense Vectors
- Computing with Word Senses: WSD and WordNet
- Lexicons for Sentiment and Affect Extraction
- The Representation of Sentence Meaning

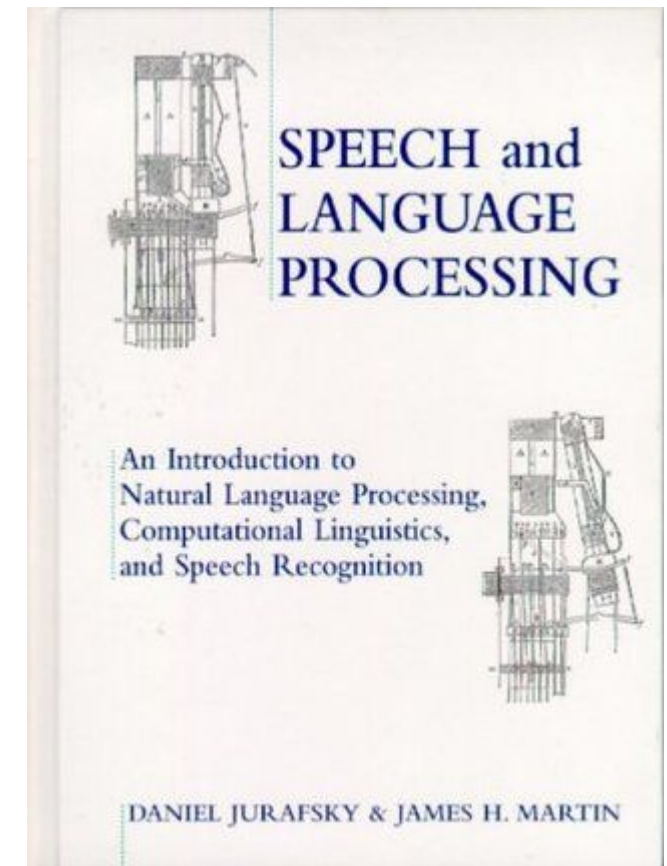


- Computational Semantics
- Information Extraction
- Semantic Role Labeling and Argument Structure
- Coreference Resolution and Entity Linking
- Discourse Coherence
- Seq2seq Models and Machine Translation
- Summarization
- Question Answering
- Dialog Systems and Chatbots
- Advanced Dialog Systems
- Speech Recognition
- Speech Synthesis

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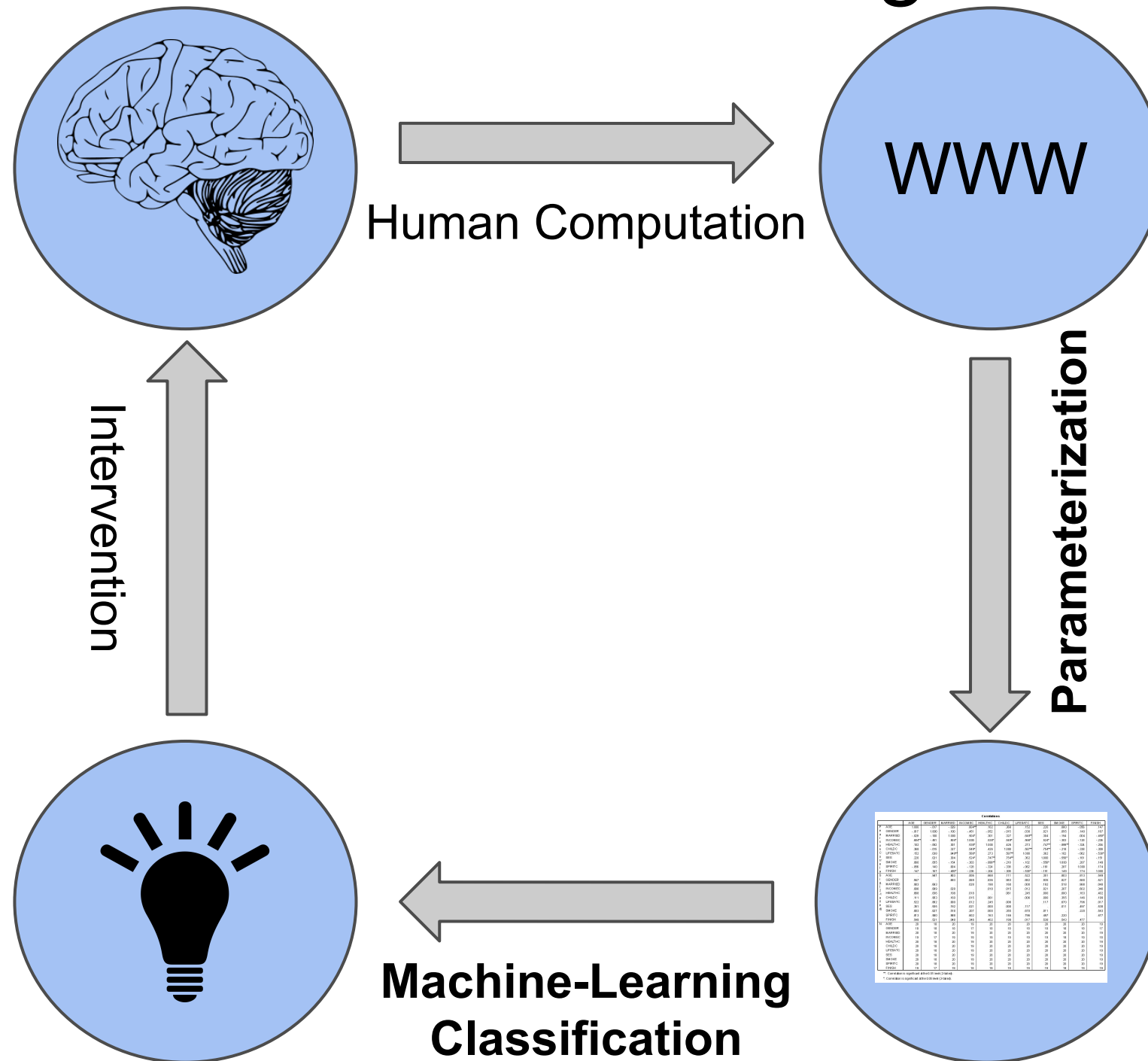


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Mi motivación: ¡aplicaciones!

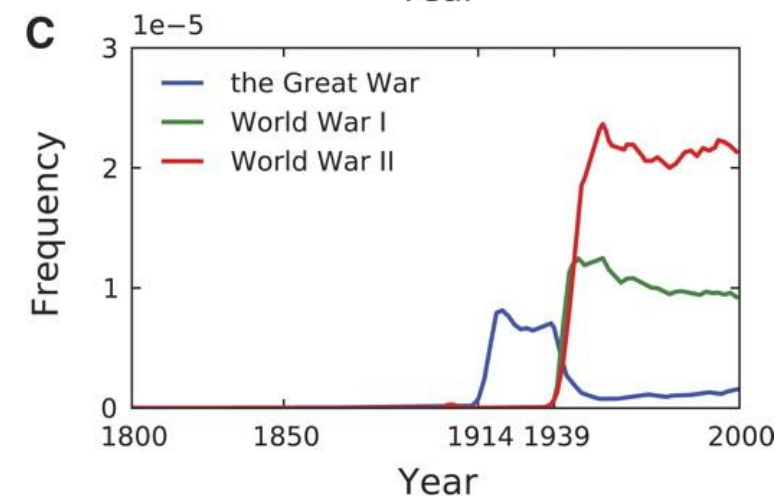
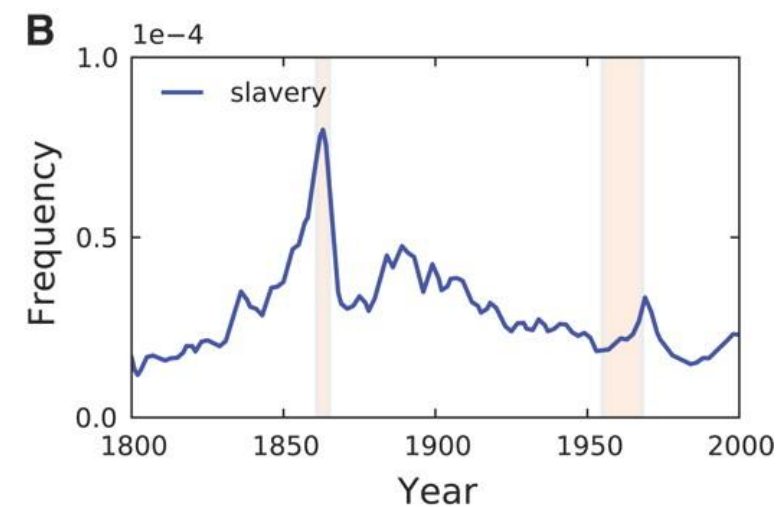
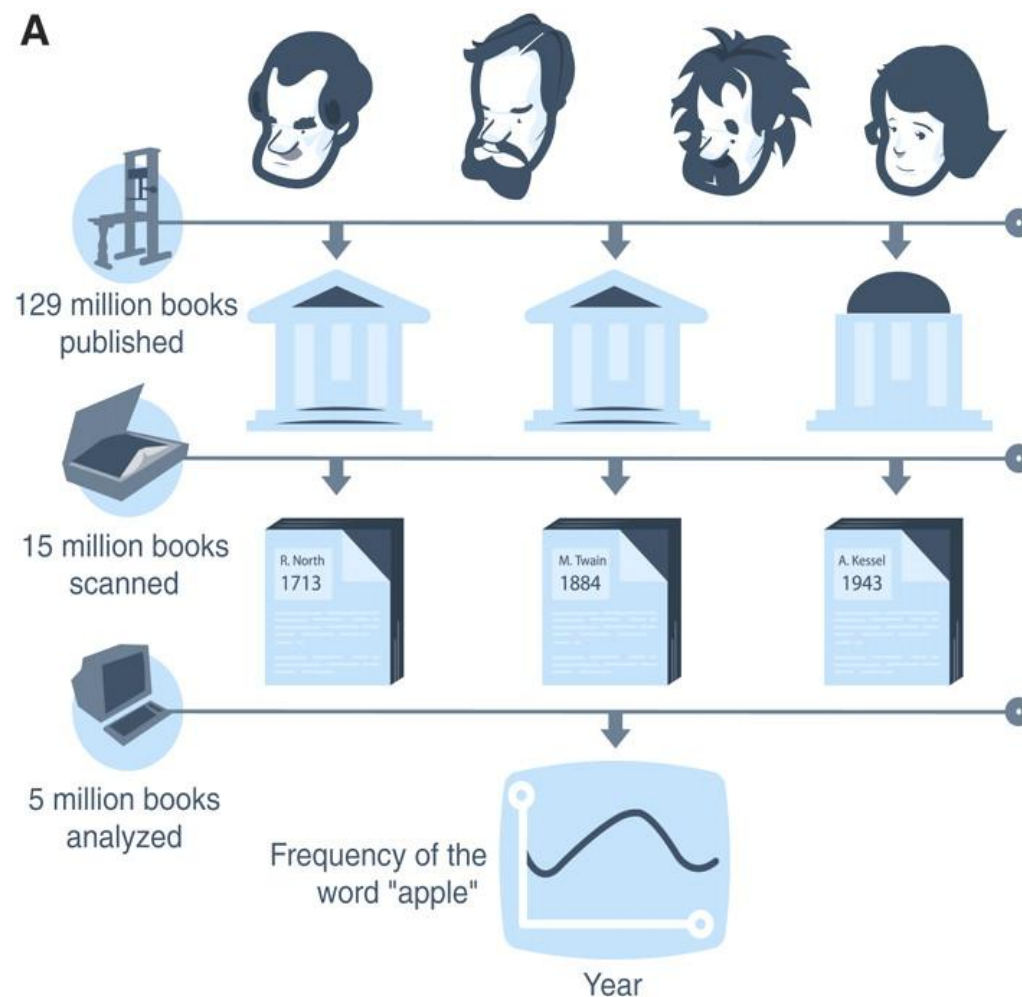
- ¿De qué están hablando las sociedades?
 - Text mining en millones de libros, blogs, páginas web, etc.
- Caracterización de estados mentales
 - Psiquiatría Computacional

Characterization of human behavior with the advent of Big Data



What people and societies are talking about...

- Michel, J.B. et. Al, *Quantitative analysis of culture using millions of digitized books*, **Science**, 2011.



Looking for abstract concepts

- Word Association
 - K. Church, P. Hanks, *Word association norms, mutual information and lexicography*, **J. of Computational Linguistics**, Volume 16 Issue 1, March 1990, pp 22-29, MIT Press.
- Latent Semantic Analysis
 - Deerwester, S. et. al, *Indexing by latent semantic analysis*, **J. of the American society for information science**, vol 416, pp 391-407, 1990.
 - Hofmann, T. *Probabilistic latent semantic indexing*, **Proc. of the 22nd annual international ACM SIGIR**, ACM, 1999.
- Latent Dirichlet Allocation
 - Blei, D., Ng, A. and Jordan, M., *Latent dirichlet allocation*, **Journal of machine Learning research**, 3: 993-1022, 2003.
- Deep Learning in NLP
 - Socher, R, Lin, C., Manning, C., Ng, A., *Parsing natural scenes and natural language with recursive neural networks*, **Proc of the 28th International Conference on Machine Learning (ICML-11)**. 2011.

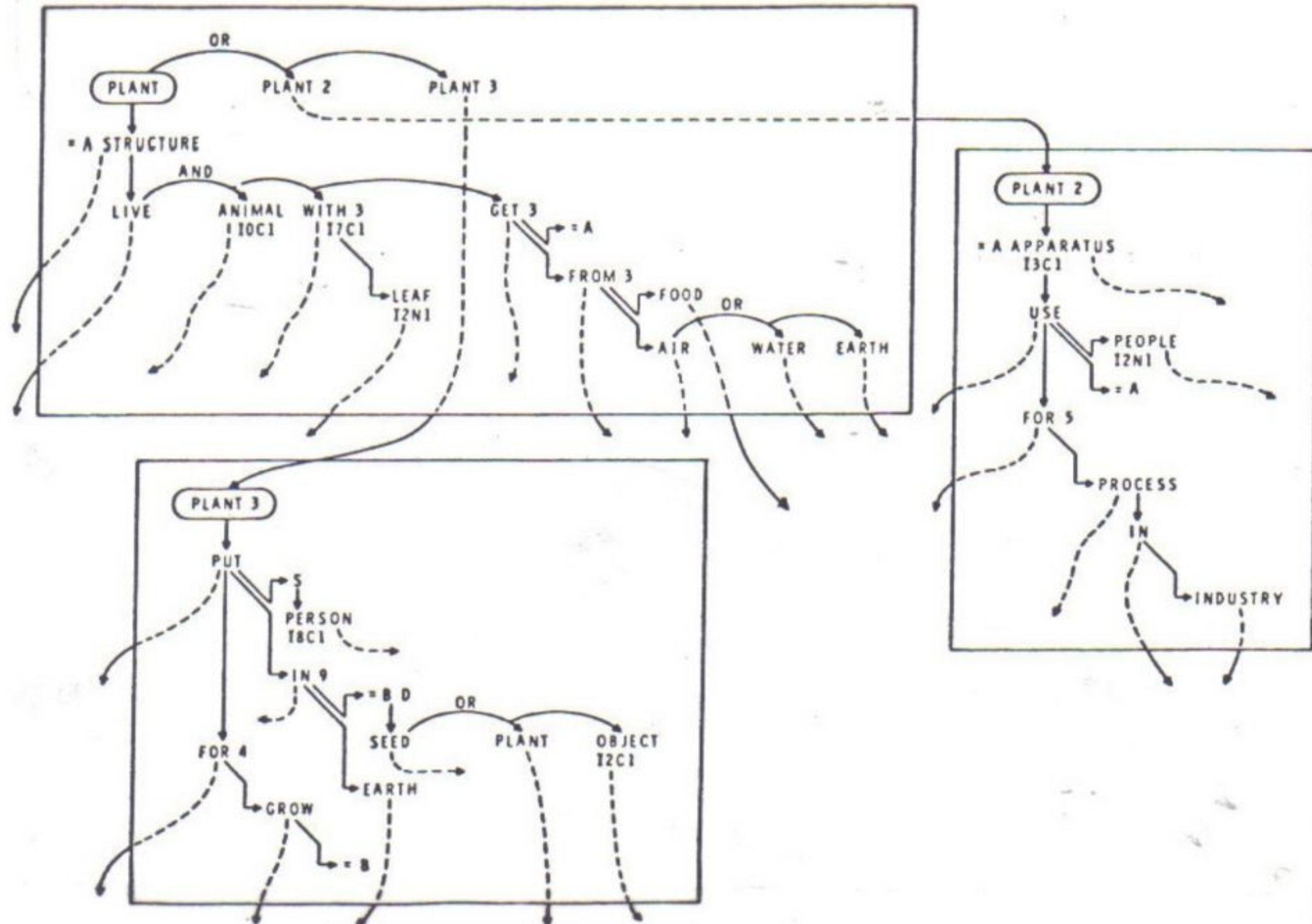
Word association

"Generally speaking, subjects respond quicker than normal to the word nurse if it follows a highly associated word such as doctor."

Empirical estimates of word association

Palermo, D. and Jenkins, J. 1964 "Word Association Norms." University of Minnesota Press, Minneapolis, MN.

Redes semánticas de Quillian



La evidencia I: Collins & Quillian

- Buscaban encontrar evidencia de la estructura jerárquica de la memoria semántica y del modelo de propagación de la activación (Spreading of activation).
- Tarea: con una tecla comunicar si la oración es verdadera o falsa.
- Oraciones de propiedades (del individuo o de la clase) o de pertenencia de clase.
- P0: Un roble tiene bellotas. P1: ... tiene hojas.
- S0: Un perro es un perro. S1: es un mamífero.
- Usaban oraciones falsas además.

Priming y estructura jerárquica.

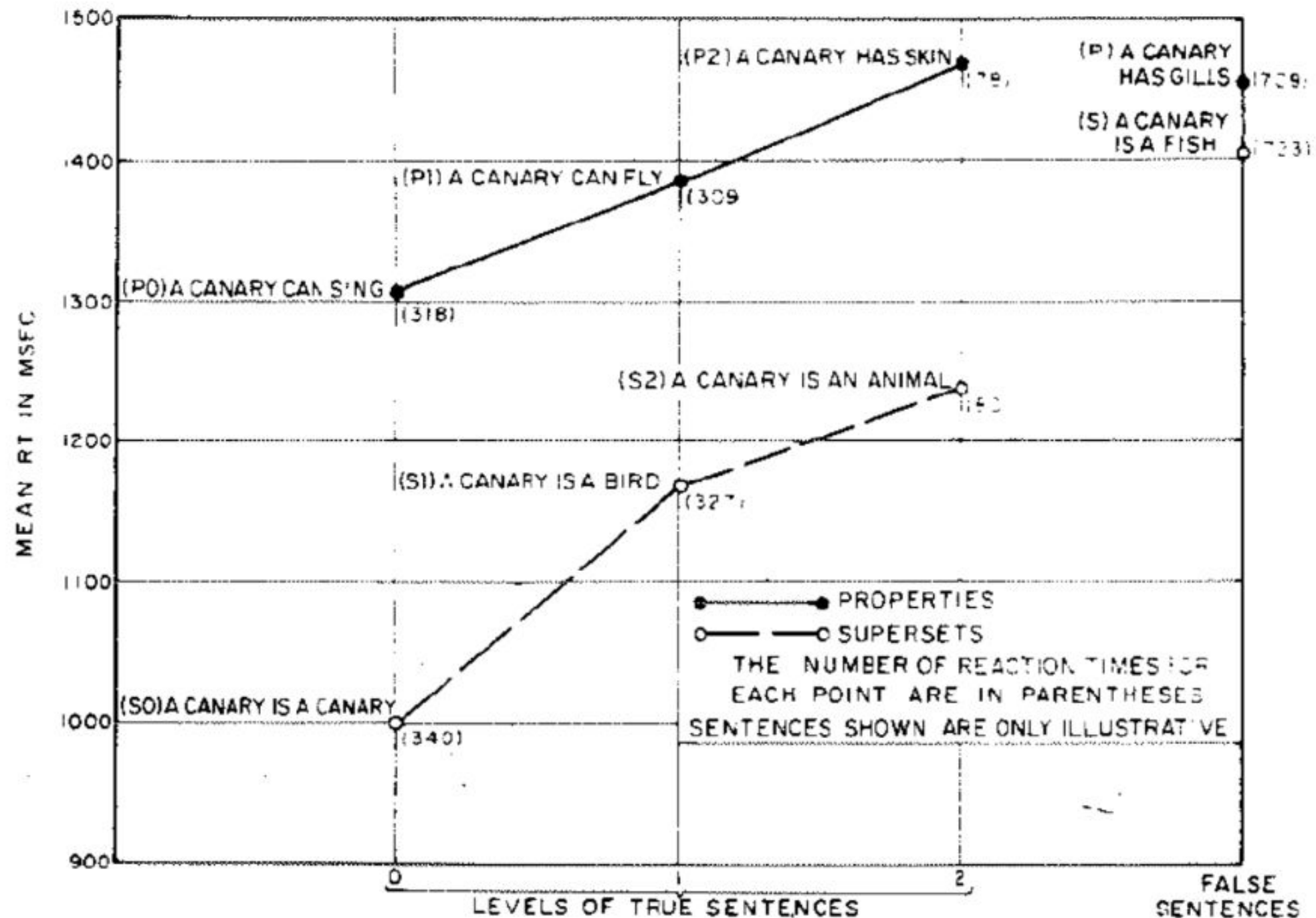


FIG. 2. Average reaction times for different types of sentences in three experiments.

Palabras y conceptos

- Visión, 1 palabra \leftrightarrow 1 concepto
 - Perro \leftrightarrow PERRO
 - Banco \leftrightarrow FINANCIERO? DE PLAZA? DE PECES?
 - \leftrightarrow Usar un clip para destapar la bombilla del mate
 - La \leftrightarrow Concepto u operador sobre concepto?
- Varias palabras \leftrightarrow un concepto y conceptos sin palabras.
- Palabras con diferentes sentidos (disco).
- Partes de conceptos (pestaña, etc).

Un ejemplo: wordnet

WordNet Search - 3.1

[WordNet home page](#) - [Glossary](#) - [Help](#)

Word to search for:

Display Options:

Key: "S:" = Show Synset (semantic) relations, "W:" = Show Word (lexical) relations

Display options for sense: (gloss) "an example sentence"

Noun

- [S: \(n\) bank](#) (sloping land (especially the slope beside a body of water)) *"they pulled the canoe up on the bank"; "he sat on the bank of the river and watched the currents"*
- [S: \(n\) depository financial institution, bank, banking concern, banking company](#) (a financial institution that accepts deposits and channels the money into lending activities) *"he cashed a check at the bank"; "that bank holds the mortgage on my home"*
- [S: \(n\) bank](#) (a long ride)
- [S: \(n\) bank](#) (an arrangement of switches) *bank of switches*
- [S: \(n\) bank](#) (a supply of resources for emergencies)
- [S: \(n\) bank](#) (the funds of a bank) *he tried to break the bank*
- [S: \(n\) bank, cant, cam](#) (a curved surface) *the inside in order to turn*
- [S: \(n\) savings bank, coin bank, money box, bank](#) (a place for keeping money) *the top) for keeping money*
- [S: \(n\) bank, bank building](#) (a building where money is kept) *"the bank is on the corner"*
- [S: \(n\) bank](#) (a flight maneuver) *(especially in turning)*

Verb

- [S: \(v\) bank](#) (tip laterally) *the ship banked to starboard*
- [S: \(v\) bank](#) (enclose with a bank) *the road banked the river*
- [S: \(v\) bank](#) (do business with) *bank in this town?*
- [S: \(v\) bank](#) (act as the bank) *the bank acted as the bank*
- [S: \(v\) bank](#) (be in the bank) *the bank was in the bank*
- [S: \(v\) deposit, bank](#) (put money in a bank) *month"*
- [S: \(v\) bank](#) (cover with a bank) *the bank covered the bank*
- [S: \(v\) count, bet, depend](#) (have confidence in) *"you can count on that!"; "You can bet on that!"; "Depend on your family in times of crisis"*

Noun

- [S: \(n\) bank](#)
 - [direct hyponym](#) / [full hyponym](#)
 - [direct hypernym](#) / [inherited hypernym](#) / [sister term](#)
 - [S: \(n\) slope, incline, side](#)
 - [derivationally related form](#)
- [S: \(n\) depository financial institution, bank, banking concern, banking company](#)
- [S: \(n\) bank](#)
- [S: \(n\) bank](#)
- [S: \(n\) bank](#)
- [S: \(n\) bank](#)
- [S: \(n\) bank, cant, camber](#)
- [S: \(n\) savings bank, coin bank, money box, bank](#)
- [S: \(n\) bank, bank building](#)
- [S: \(n\) bank](#)

An information theoretic measure

Association ratio, based on the information theoretic concept of **mutual information**.

$$I(x, y) \equiv \log_2 \frac{P(x, y)}{P(x)P(y)}$$

- If there is a **genuine association** between x and y , then $P(x, y)$ will be much larger than $P(x) \cdot P(y)$, and $I(x, y) \gg 0$.
- If there is **no interesting relationship** between x and y , then $P(x, y) = P(x) \cdot P(y)$, and thus, $I(x, y) \sim 0$.
- If x and y are in **complementary distribution**, then $P(x, y)$ will be much less than $P(x) P(y)$, forcing $I(x, y) \ll 0$.

Probability estimation

$P(x)$ and $P(y)$ are estimated by counting the number of observations of x and y in a corpus, $f(x)$ and $f(y)$, and normalizing by N , the size of the corpus.

$P(x,y)$, are estimated by counting the number of times that x is followed by y in a window of w words, $f_w(x,y)$, and normalizing by N .

(...the window size, w , will be set to five words as a compromise)

Since the association ratio becomes unstable when the counts are very small, we will not discuss word pairs with $f(x,y) < 6$.

Measure properties

- $l(x, y) = l(y, x)$. But, $f(x, y) \neq f(y, x)$
- Expected: $f(x, y) \leq f(x)$ and $f(x, y) \leq f(y)$
 - "Library workers were prohibited from saving books from this heap of ruins,"
 - $f(\text{prohibited}) = 1$ and $f(\text{prohibited, from}) = 2$
 - This problem can be fixed by dividing $f(x, y)$ by $(w-1)$

Corpus

- This paper: Associated Press
- Other corpus: TASA, Pagina12, La Nación, Google

Implementation

Python

- NLTK package for Natural Language Processing

<http://www.nltk.org/>

Example

```
>>> import nltk.data
>>> text = '''
... Punkt knows that the periods in Mr. Smith and Johann S. Bach
... do not mark sentence boundaries. And sometimes sentences
... can start with non-capitalized words. i is a good variable
... name.
... '''
>>> sent_detector =
nltk.data.load('tokenizers/punkt/english.pickle')
>>> sents = sent_detector.tokenize(text.strip()))
```

Implementation

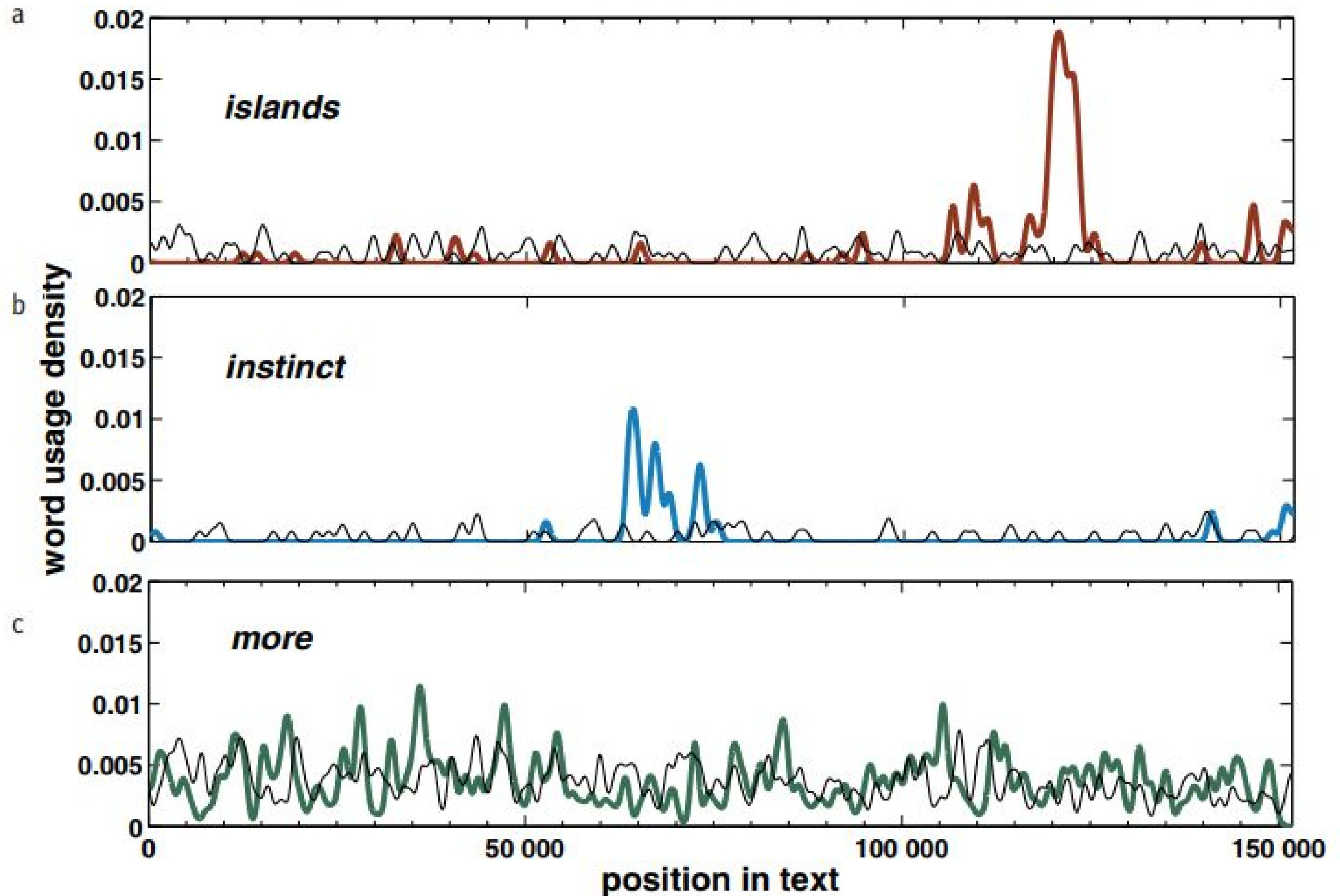
Word Association: Given the corpus X and w_i each different word in X

- Let k be the window size
- For each w_i calculate $f(w_i)$
- For each w_i and w_j calculate $f_k(w_i, w_j)$

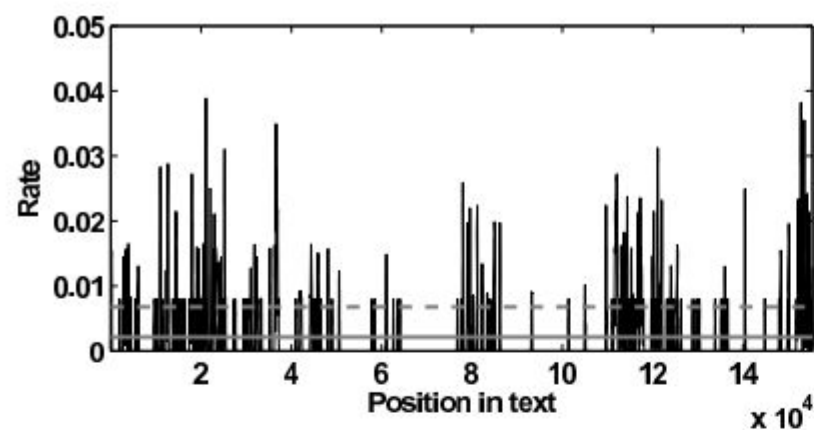
Pseudocode

- Let FM be the co-occurrence matrix
- For each position m ,
 - For each position p between $m+1$ and $m+k$
 - $FM(X_m, X_p)++$

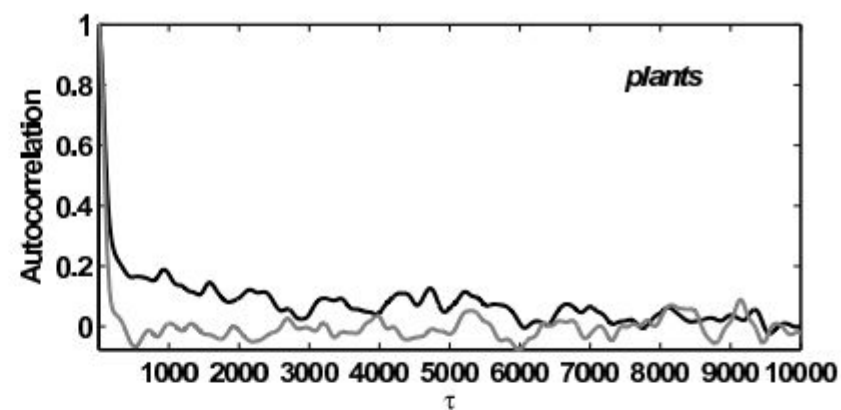
Información léxica



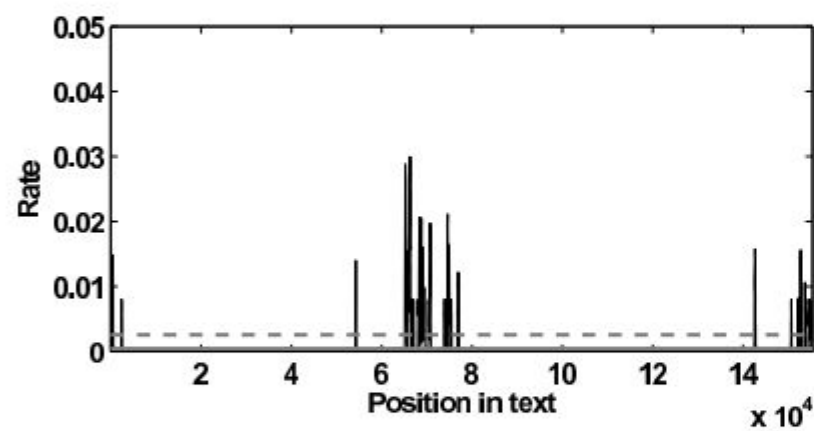
Escala de cada palabra



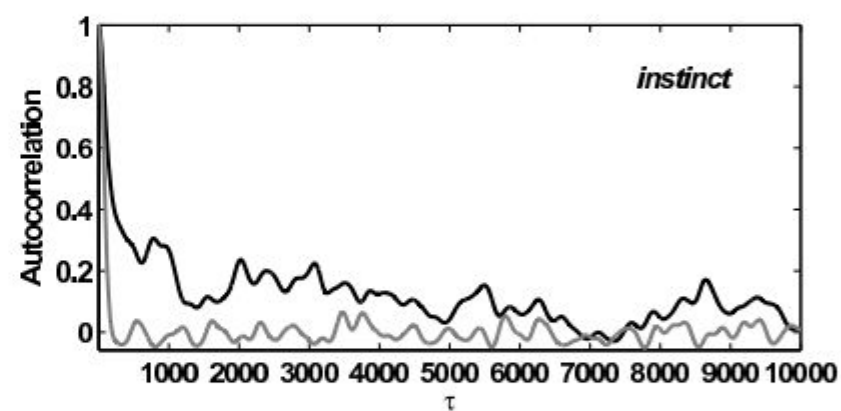
(a)



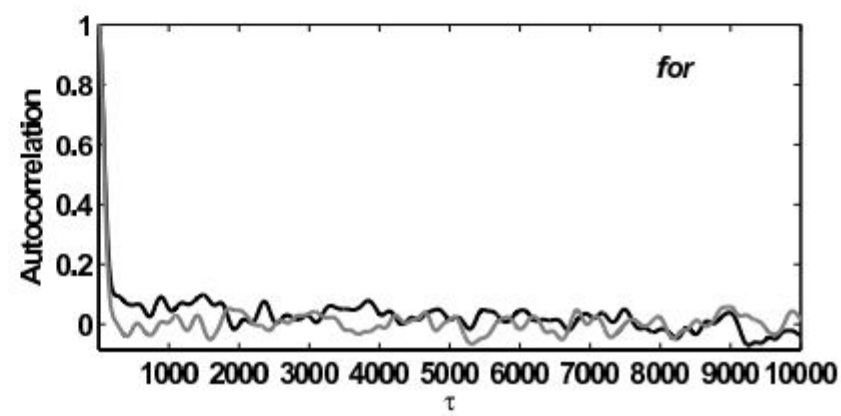
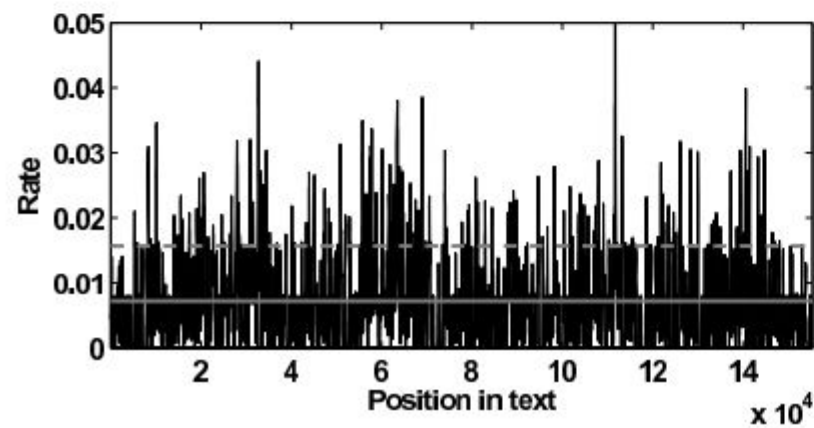
(d)



(b)



(e)



Pertenencia de palabras a secciones

$$\Delta I(s) = \sum_{w=1}^K p(w) [\langle \hat{H}(J|w) \rangle - H(J|w)],$$

Suma sobre todas las palabras del texto

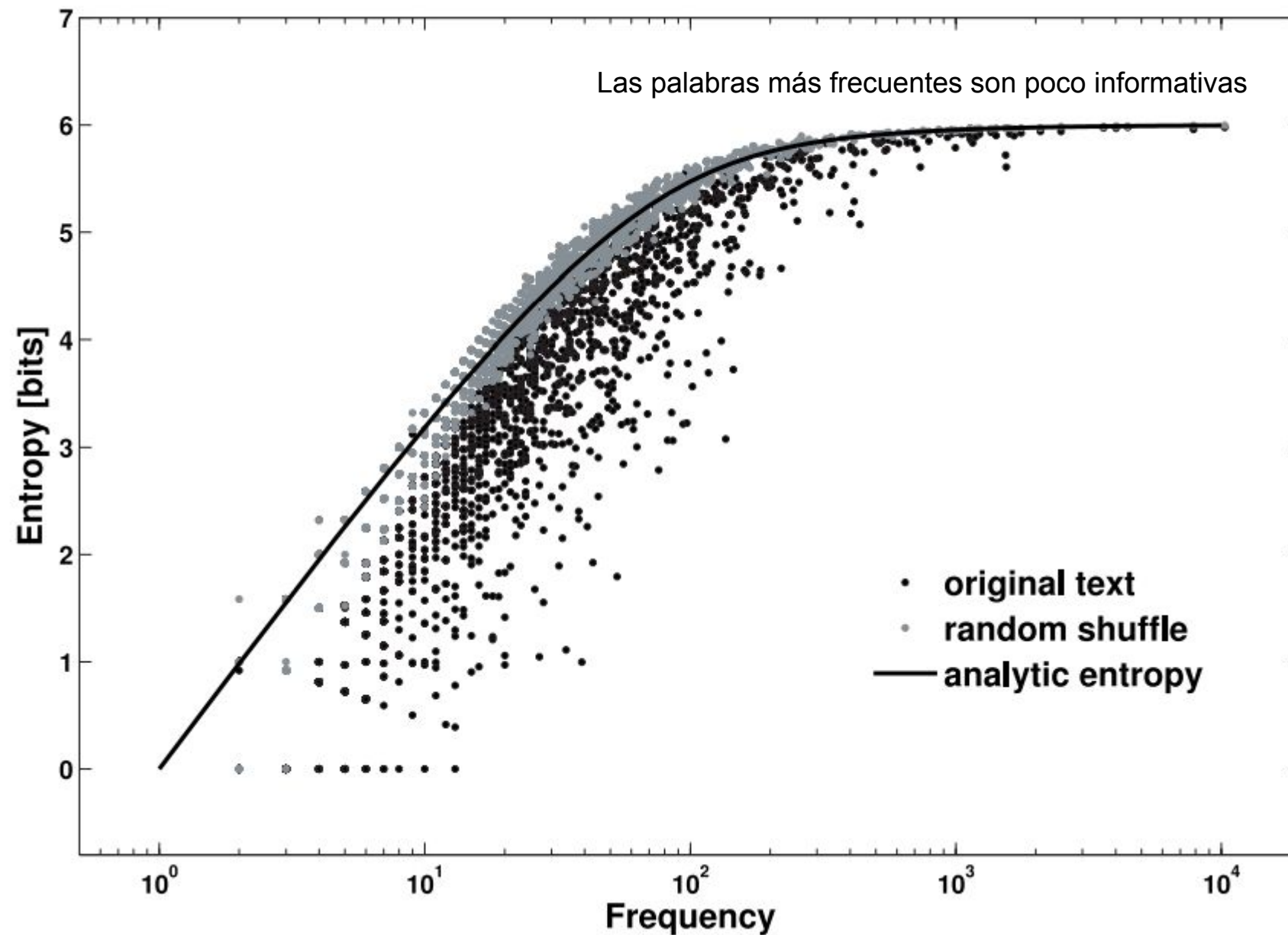
La frecuencia de la palabra w

La entropía permutada (el máximo que puede tomar)

$$H(J|w) = - \sum_{j=1}^P \frac{n_j}{n} \log_2 \frac{n_j}{n},$$

La entropía de la palabra w en las partes del texto. Es máxima si esta distribuida homogéneamente. Es mínima si esta concentrada en una sola parte. Es una información mutua porque nos dice cuanto informa la palabra respecto de la parte. Es una función paramétrica de la escala de la partición.

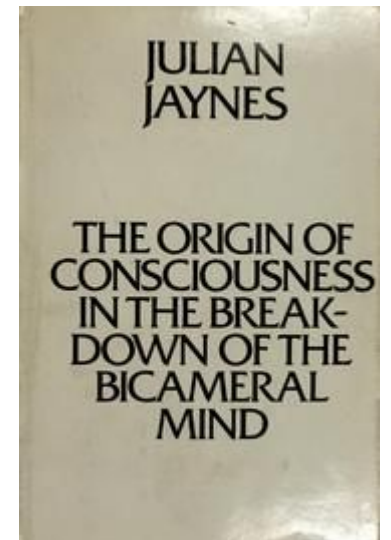
Entropía de las palabras



Looking for abstract concepts.

Introspection: A case study

J. Jaynes, *The origins of consciousness in the breakdown of the bicameral mind*, Mariner Books, 2000.

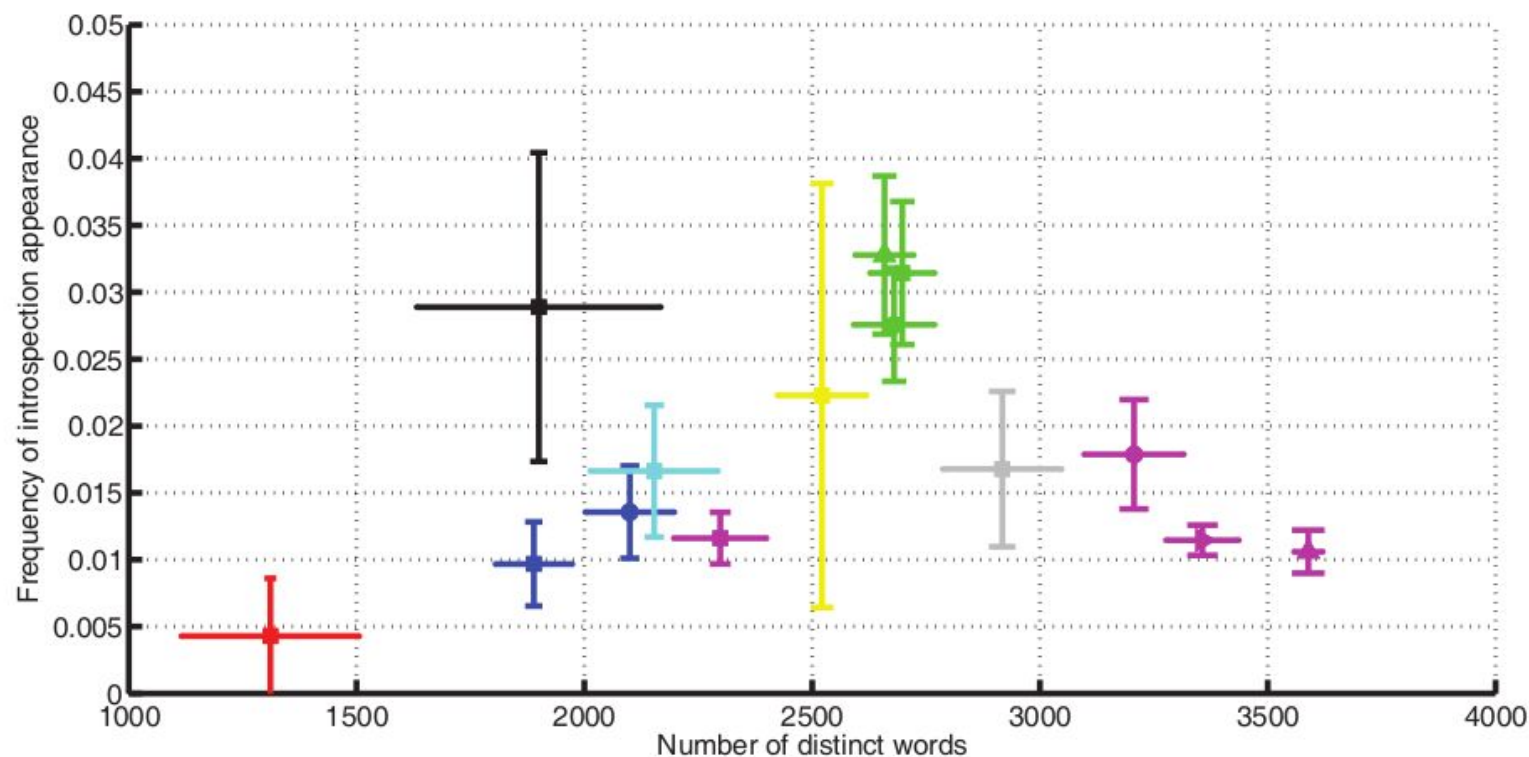


- **Psychological hypothesis:** human mind with cognitive functions divided in:
 - one part of the brain which appears to be "speaking", *acoustical hallucinations*
 - and a second part which listens and obeys
- Starting in about 10,000 BC and extending through about 1000 BC: agrarian empires and city-states, i.e. Egypt, the Levant, Mesopotamia, Greece, etc
- Introspection, Self-awareness, or Consciousness, was the cultural evolution
 - Development of language?
 - Cultural disruptions?

Using regular expressions

Words associated with introspection:

- think+ thought myself mind+ feel+ felt



- Iliad (approx. 1200 BCE to 900 BCE)
- Odyssey (approx. 1200 BCE to 900 BCE)
- The Bible (approx. 1400 BCE to 200 CE)
- Lucretius' On the Nature of Things (99 BCE - 55 BCE)
- St. Augustine's Confessions (397 - 398 CE)
- Cervantes' Quixote (1605 CE - 1615 CE)
- Shakespeare's The Merchant of Venice (1596 CE - 1598 CE)
- Shakespeare's Hamlet (approx. AD 1600)
- ▲ Shakespeare's Macbeth (AD 1603 - AD 1607)
- ▶ Shakespeare's Othello (AD 1603)
- Jean Austen's Mansfield Park (AD 1815)
- Jean Austen's Emma (AD 1815)
- ▲ Jean Austen's Persuasion (AD 1815)
- Proust's Time Regained (1927 CE)

Frequency of words related to introspection versus the amount of different words. Each author is identified by a unique color. Error bars show the standard deviation in both axis.

Selected text corpus representative of different ages in literature from the MIT classic text archive based on references in Jaynes' book.

Latent semantic analysis (LSA)

Similarity between concepts

based on documents and frequencies of terms

Technical Memo Example

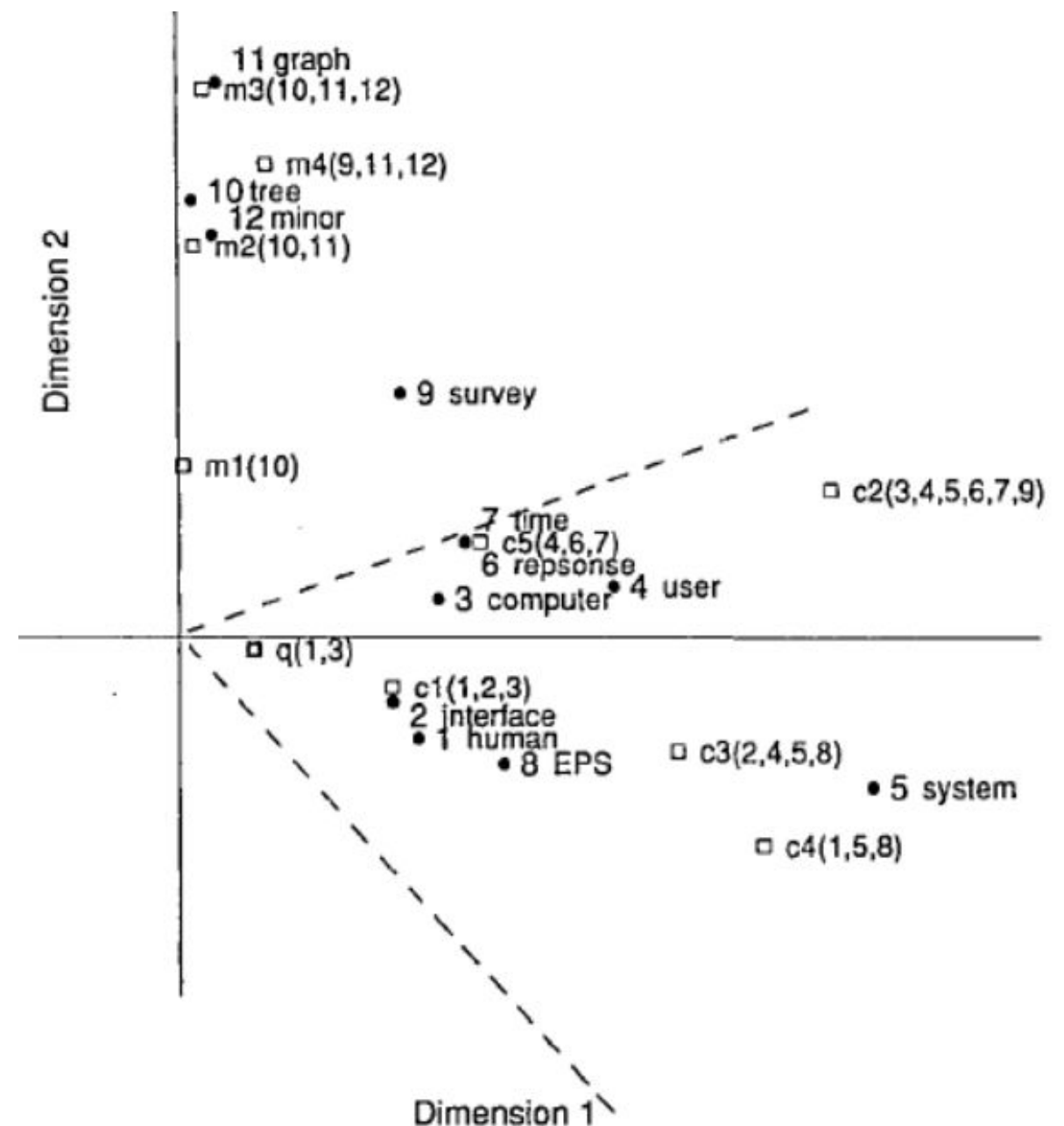
Titles

- c1: *Human machine interface for Lab ABC computer applications*
- c2: *A survey of user opinion of computer system response time*
- c3: *The EPS user interface management system*
- c4: *System and human system engineering testing of EPS*
- c5: *Relation of user-perceived response time to error measurement*
- m1: *The generation of random, binary, unordered trees*
- m2: *The intersection graph of paths in trees*
- m3: *Graph minors IV: Widths of trees and well-quasi-ordering*
- m4: *Graph minors: A survey*

Terms

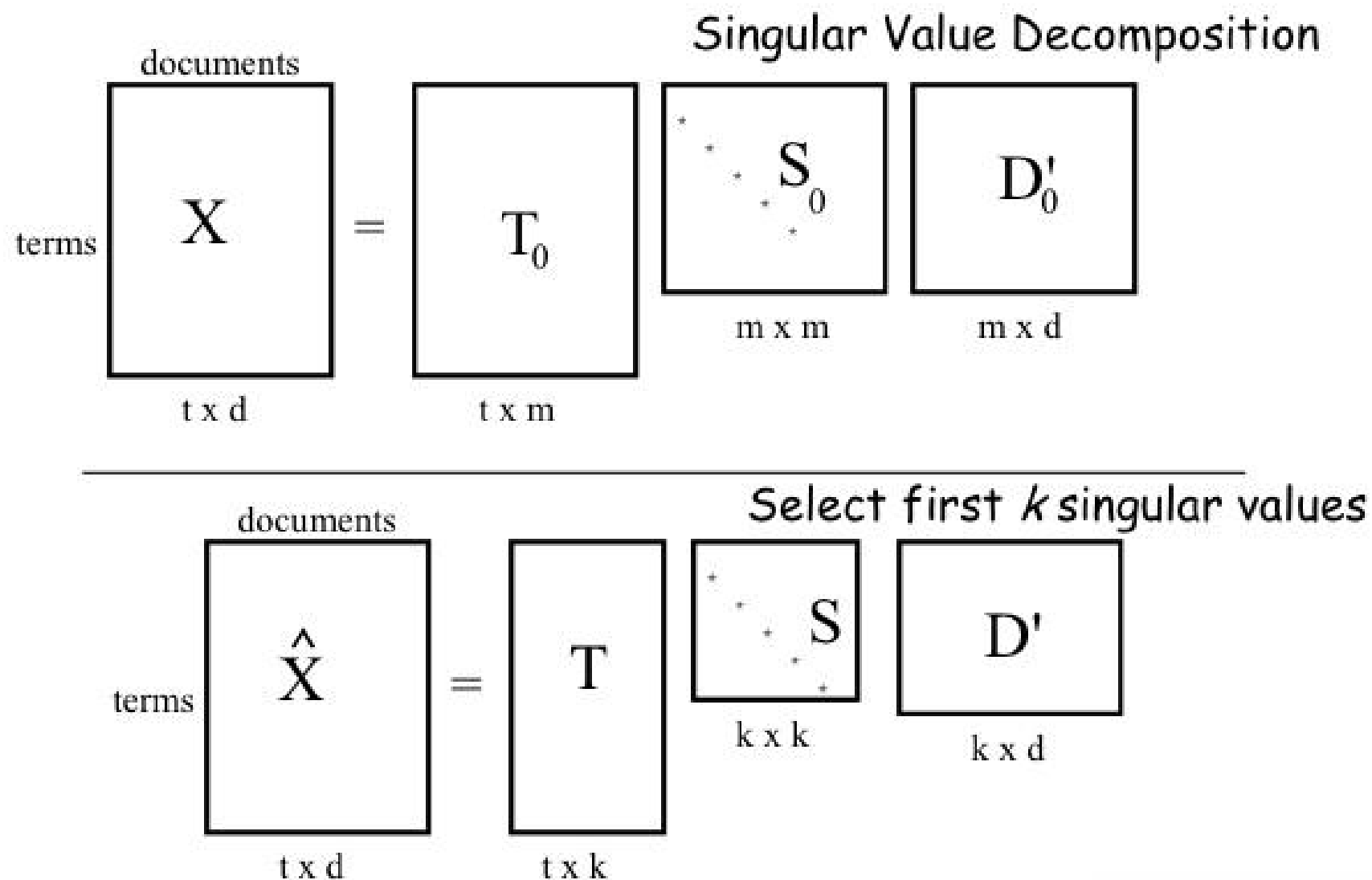
Documents

	c1	c2	c3	c4	c5	m1	m2	m3	m4
human	1	0	0	1	0	0	0	0	0
interface	1	0	1	0	0	0	0	0	0
computer	1	1	0	0	0	0	0	0	0
user	0	1	1	0	1	0	0	0	0
system	0	1	1	2	0	0	0	0	0
response	0	1	0	0	1	0	0	0	0
time	0	1	0	0	1	0	0	0	0
EPS	0	0	1	1	0	0	0	0	0
survey	0	1	0	0	0	0	0	0	1
trees	0	0	0	0	0	1	1	1	0
graph	0	0	0	0	0	0	1	1	1
minors	0	0	0	0	0	0	0	1	1



LSA in one slide

Given a text database, let X be the occurrence matrix of words in each text ($\#docs \times \#terms$).



LSA trained with TASA corpus

- TASA corpus: Touchstone Applied Science Associates, Inc.
 - texts, novels, newspaper articles, and other information used in elementary, secondary school and college.
 - TASA corpus used to develop The Educator's Word Frequency Guide.
- LSA @ Colorado: <http://lsa.colorado.edu/>
- We run LSA to TASA corpus with 300 components → we can measure distance between all words present in TASA.
 - Landauer, T.K., Dumais, S.T., *A solution to Plato's problem: The Latent Semantic Analysis theory of the acquisition, induction, and representation of knowledge*, **Psychological Review**, 104, 211-240, 1997.

Implementation

Python

- Gensim

- <http://radimrehurek.com/gensim/>

```
from gensim import corpora, models, similarities
dictionary = corpora.Dictionary.load('/tmp/deerwester.dict')
corpus = corpora.MmCorpus('/tmp/deerwester.mm')
lsi = models.LsiModel(corpus, id2word=dictionary, num_topics=2)
```

```
doc = "Human computer interaction"
vec_bow = dictionary.doc2bow(doc.lower().split())
vec_lsi = lsi[vec_bow] # convert the query to LSI space
print(vec_lsi)
[(0, -0.461821), (1, 0.070028)]
```

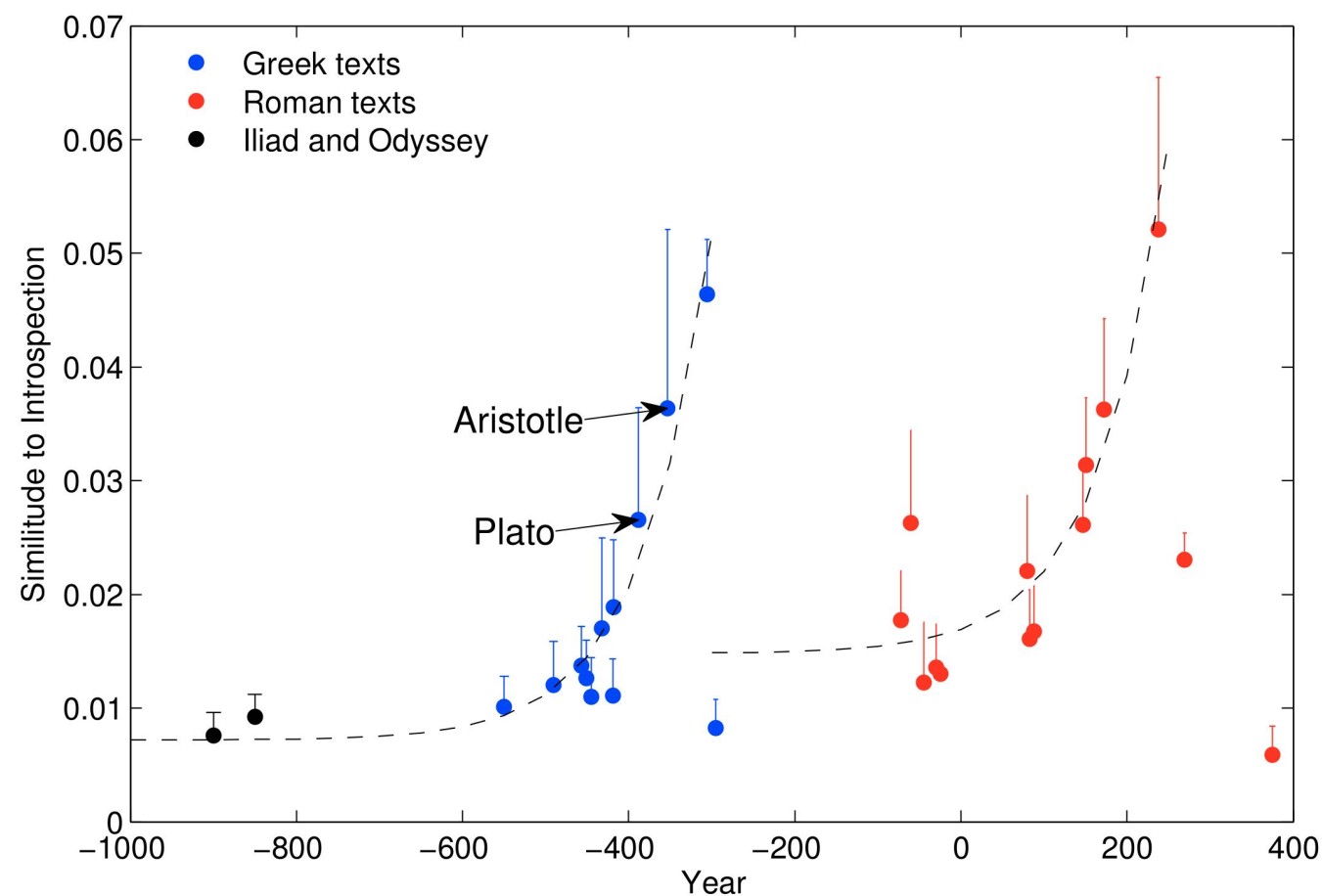
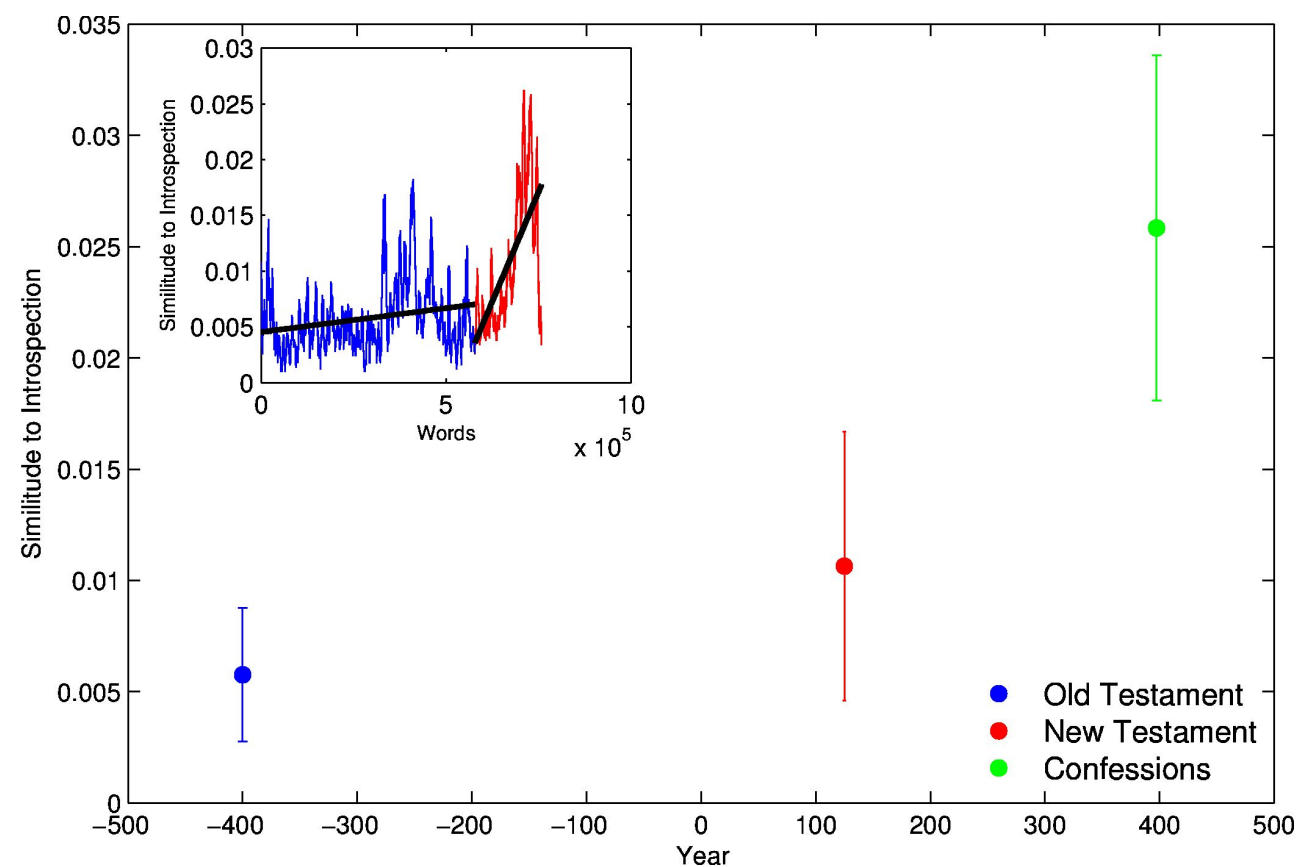
Using LSA...

Selected word: *introspection*

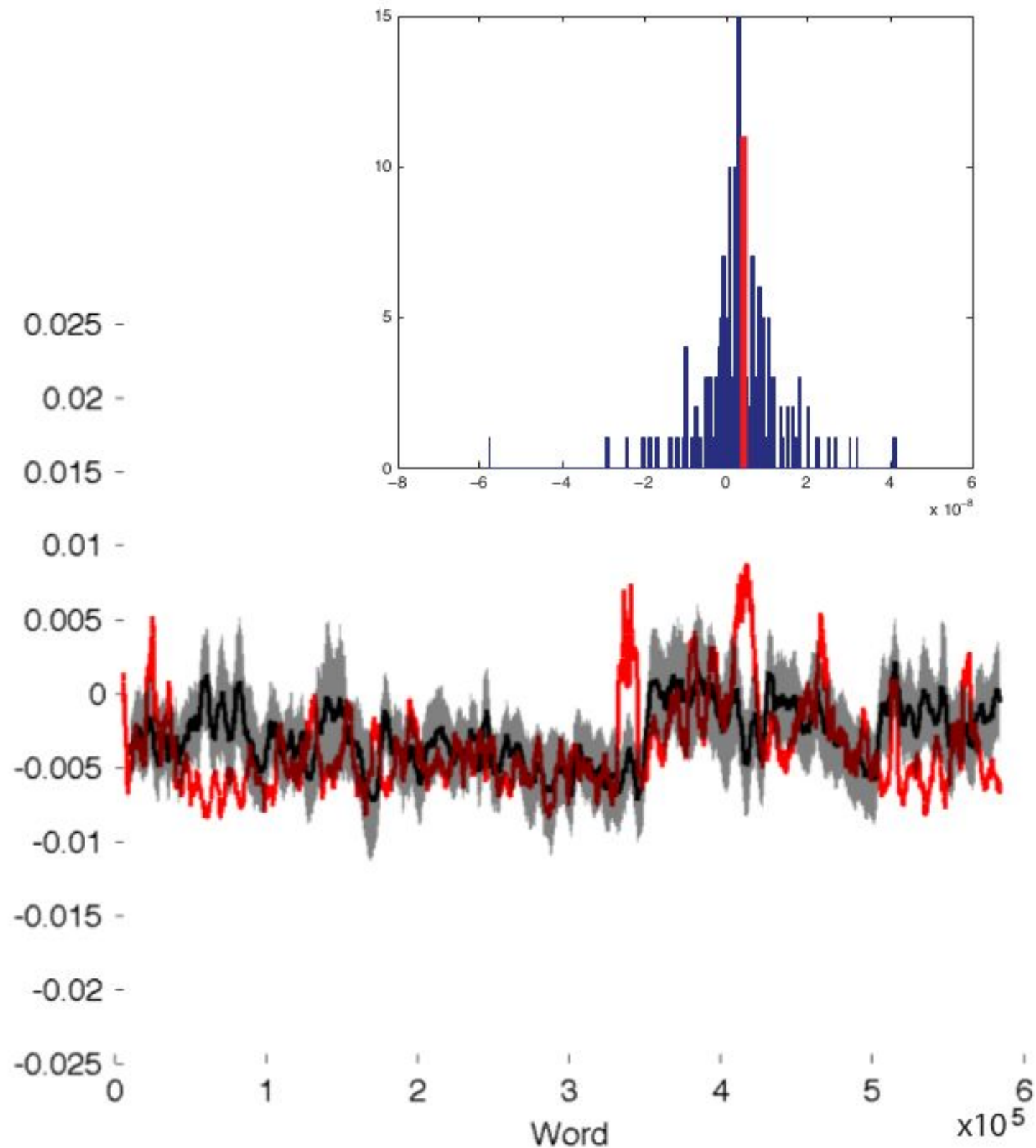
- For each document d :
 - For each word w in d :
 - Calculate LSA distance to introspection: $d_{\text{LSA}}(w, \text{'introspection'})$
- Calculate mean, std, median, etc, on d_{LSA}
- Compare with control words: 200 concepts deemed “fundamental” across 87 Indo-European
 - Pagel, M., Atkinson, Q. D., & Meade, A., *Frequency of word-use predicts rates of lexical evolution throughout Indo-European history*. **Nature**, 449 (7163), 717–720, 2007.

Confirmation of transition hypothesis

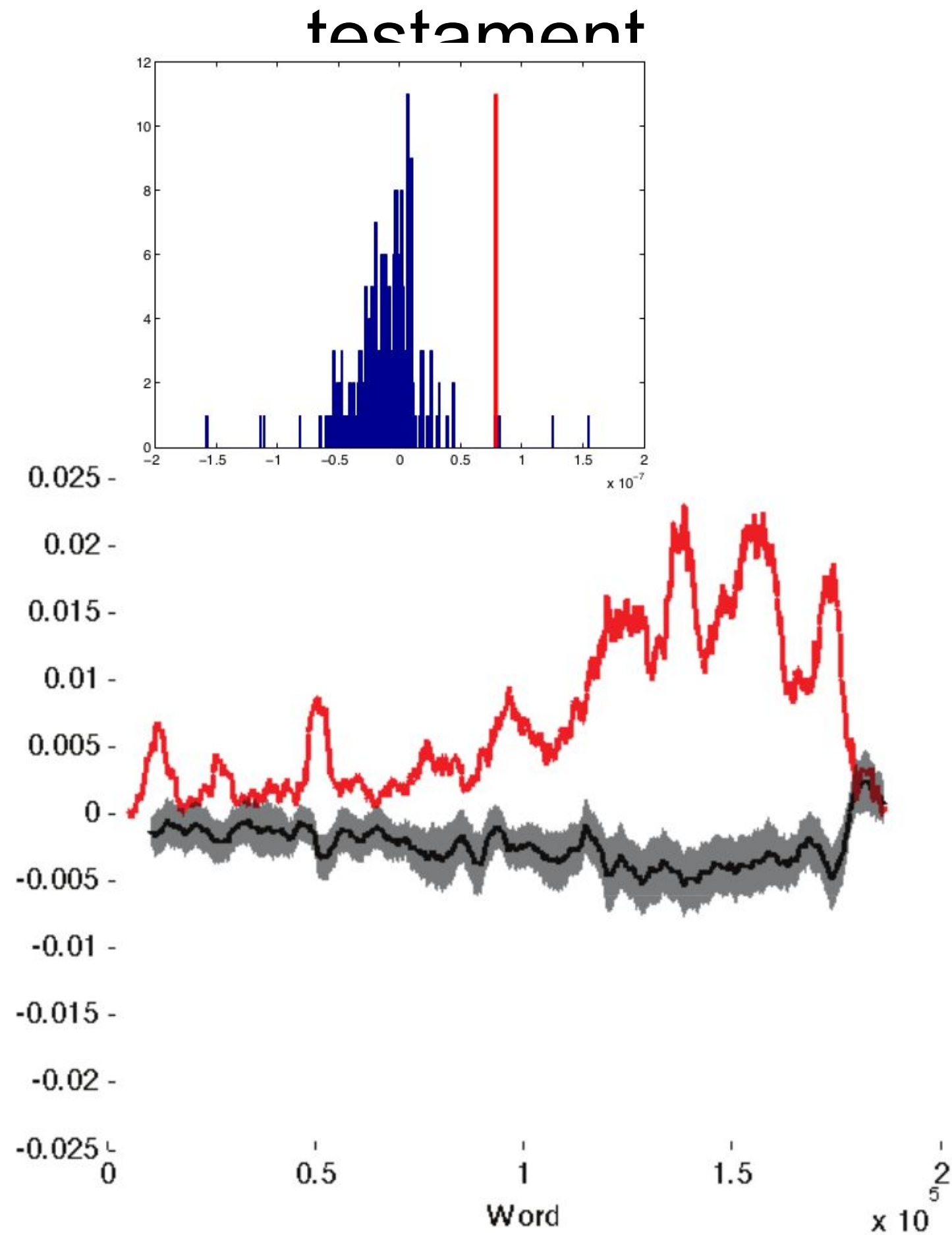
- Transition from the Bible to modern literature: Confessions, San Augustine (398 AC). First Autobiography, considered the first introspective text.



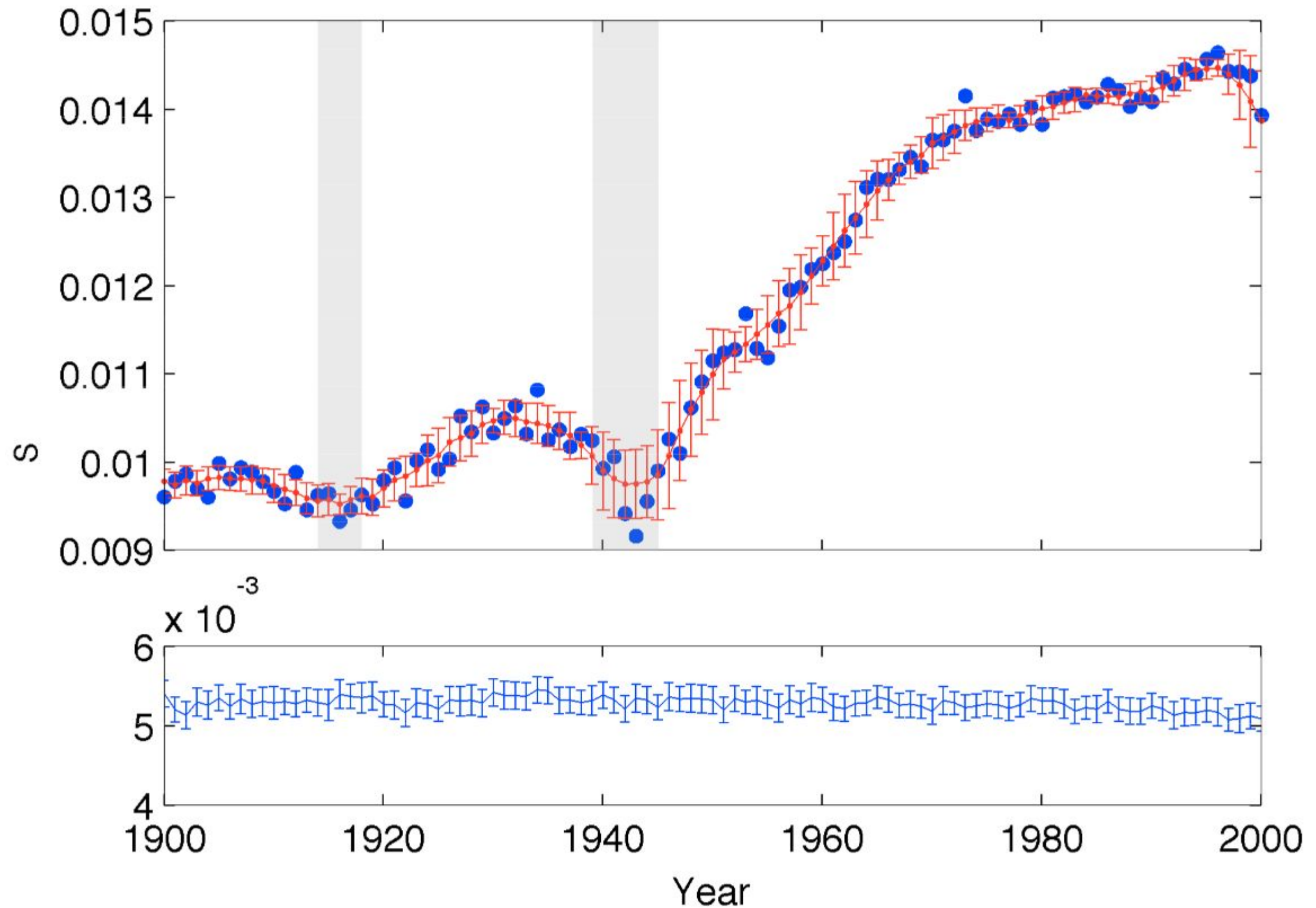
Introspection vs. control words @ Old testament



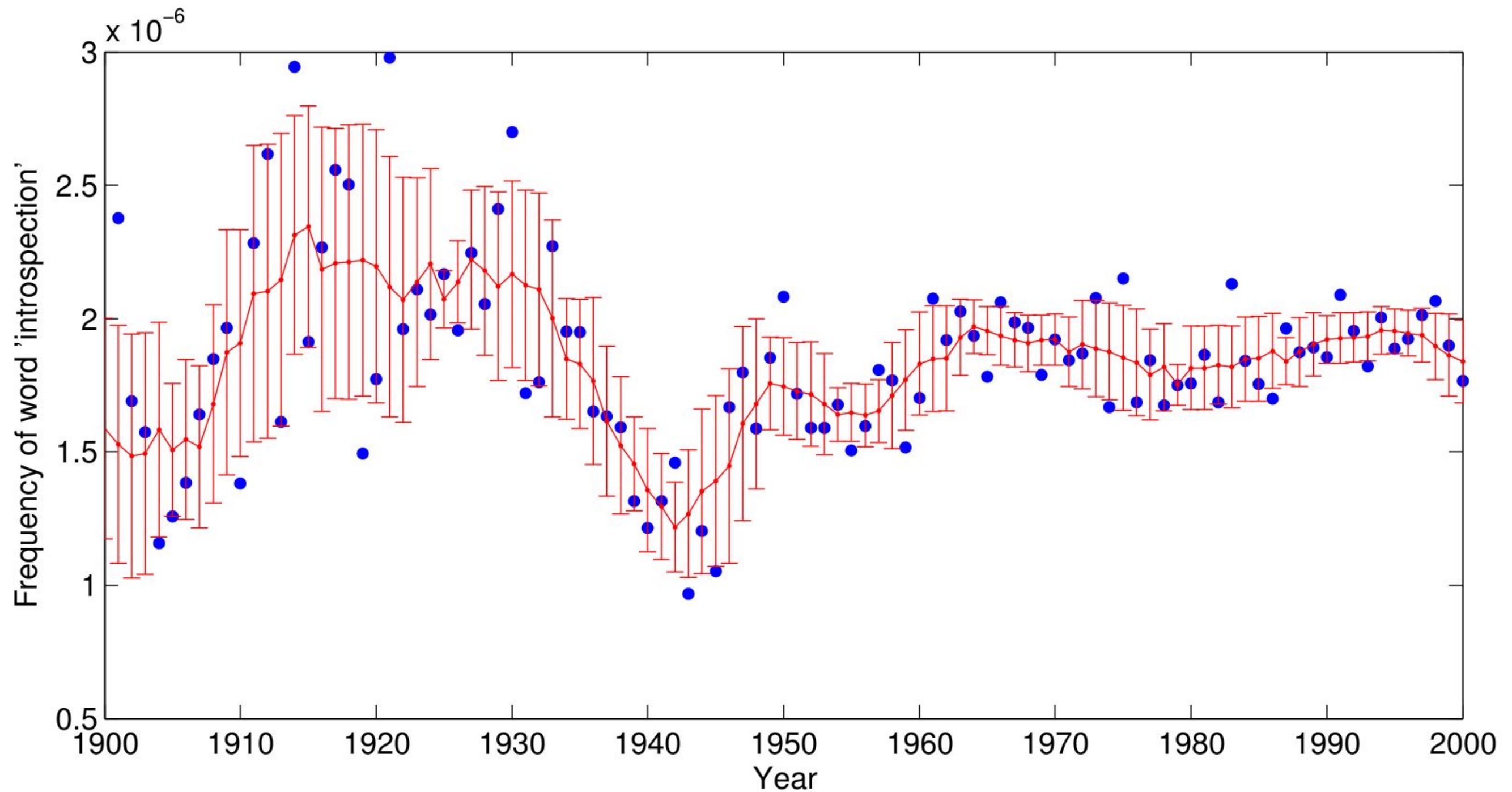
Introspection vs. control words @ New



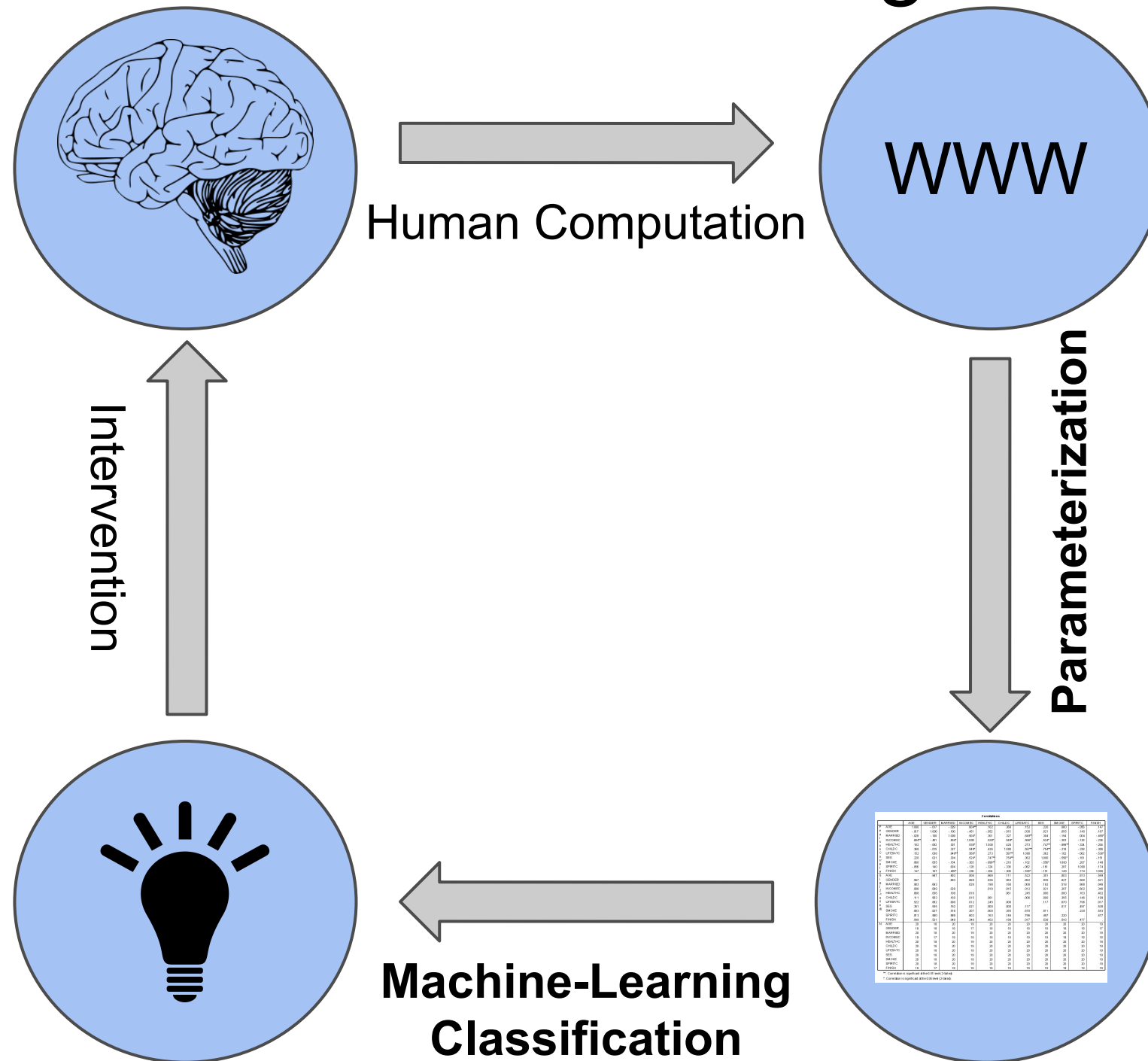
Evolution of Introspection in modern cultural records



Introspection @ Google Ngrams



Characterization of human behavior with the advent of Big Data



Can we analyse text from subjects to identify mental states?

Computational Psychiatry

- Characterize mental states by studying behavior through problem solving
 - Montague, P., et al. *Computational psychiatry*, **Trends in cognitive sciences** 16.1 (2012): 72-80.
- Text as a vehicle
- <http://computationalpsychiatry.org/>

Paradigm Pipeline



Interview



Manual
transcription



Hack



Machine Learning



Psychiatric Interview



input:

Interviewer
Subjects
Interview

output:

interview audio

problems:

interviewer bias



Interview



Manual
transcription



Hack



Machine
Learning

Manual Transcription



input:

interviews audio

output:

transcriptions texts + tags

problems:

audio quality

transcriber interpretation

punctuation, indeterminism



Interview



Manual
transcription



Hack



Machine
Learning



Hack:

input:

interview texts + tags

hypothesis, clues, etc

output:

features

problems:

computational performance,
availability, NLP



Interview



Manual
transcription



Hack



Machine
Learning

Machine Learning:

input:

features & classes

output:

classifier

performance

problems:

overfitting (data < features, feature selection)

validation strategies



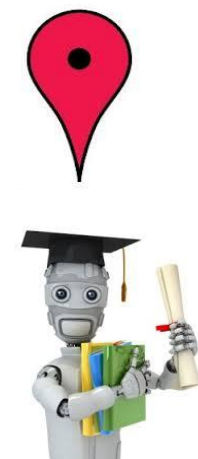
Entrevista
psiquiátrica



Transcripción
manual

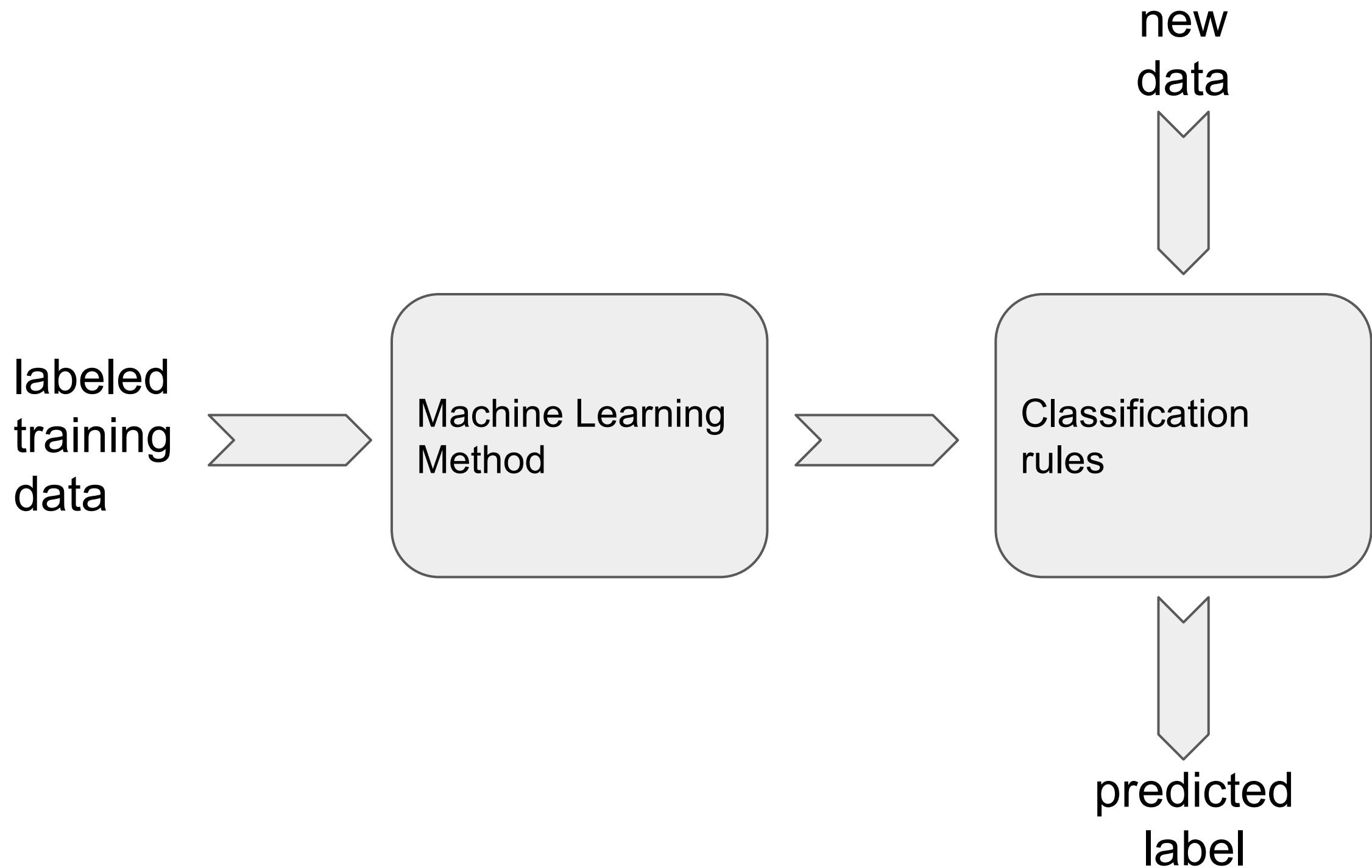


Hack



Machine
Learning

Classification

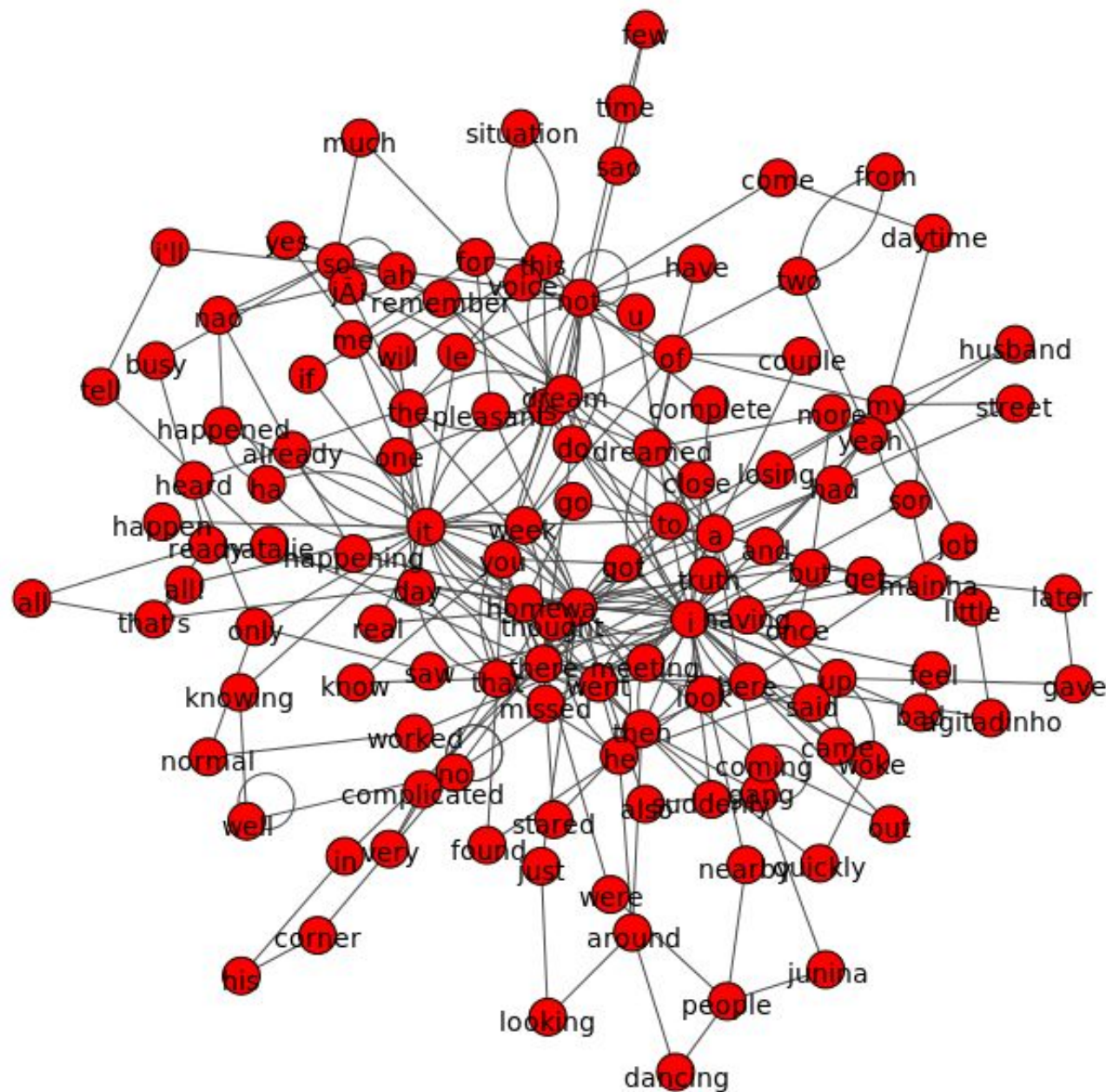


Applications

Characterizing mental states

- 63 millions of psychiatric interviews per year in USA
- Classification of speech as a marker of thought disorder in psychosis
- Classification of interviews of subjects under the effect of Ecstasy
- Classification of interviews of prodrome for schizophrenia

Psychographs



word \longrightarrow node

Classic metrics for graphs:

- # nodes, # edges
- parallel edges
- diameter
- shortest path mean

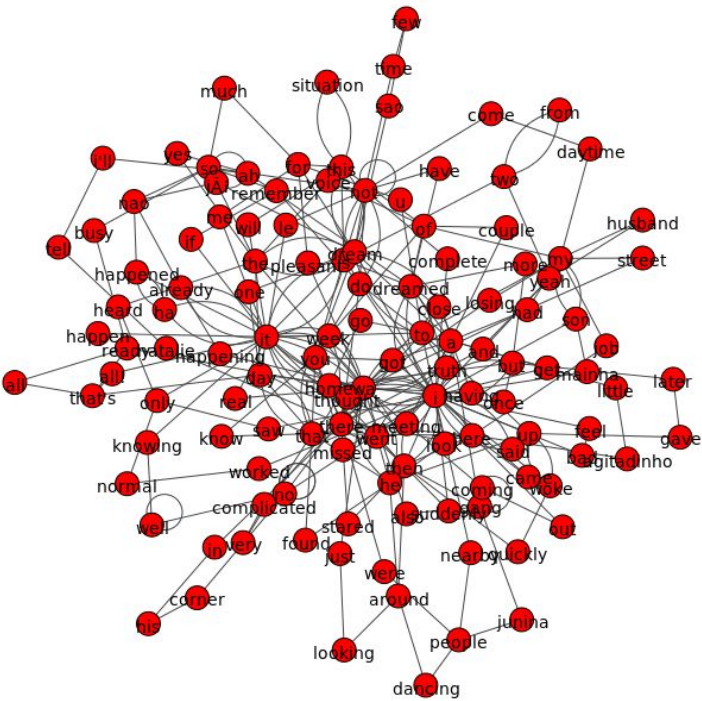
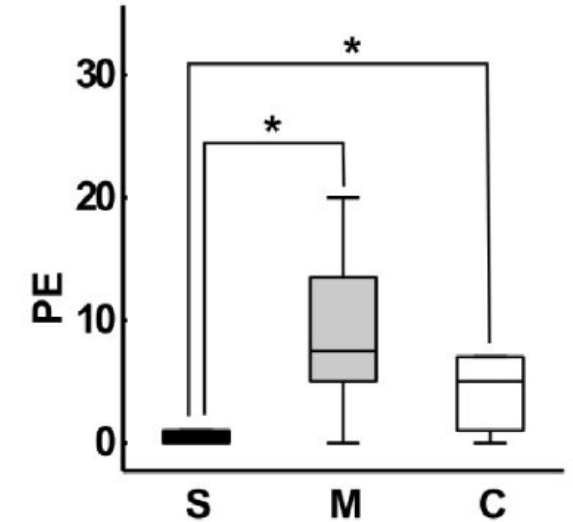
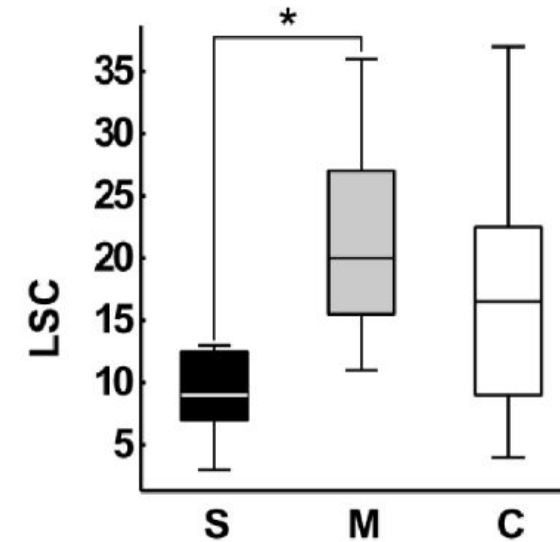
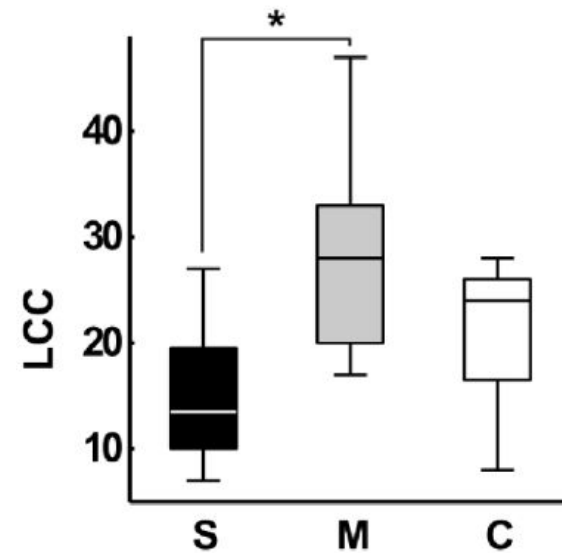
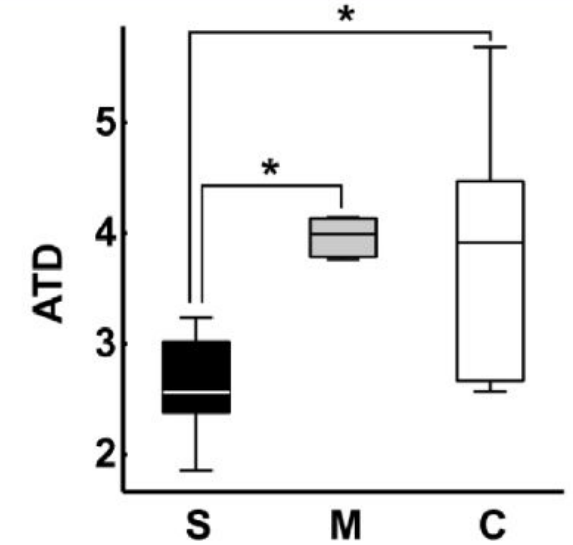
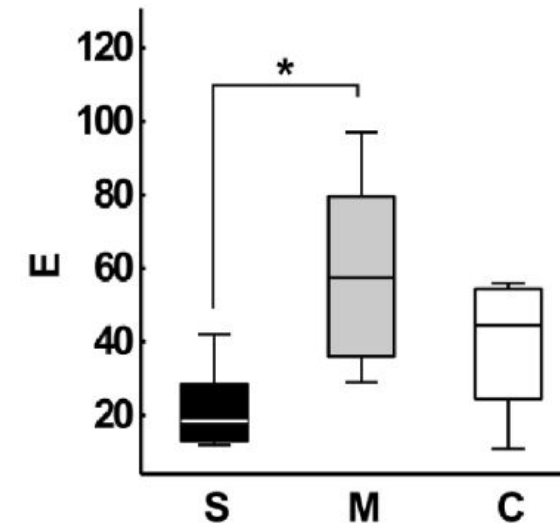
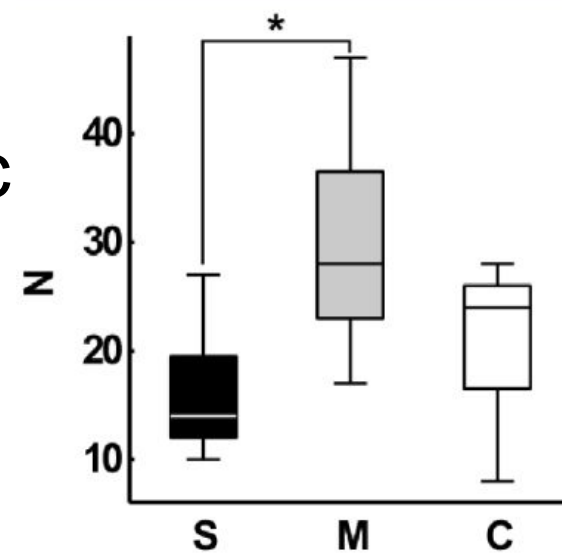
Manual process with ad hoc transformations

[1] : N.B. Mota, N.A.P. Vasconcelos, N. Lemos, A.C. Pieretti, O. Kinouchi, G.A. Cecchi, M. Copelli, and S. Ribeiro. Speech graphs provide a quantitative measure of thought disorder in psychosis. PloS one, 7(4):e34928, 2012.

Single metrics classification

Subjects

- 8 **S**chizophrenic
- 8 **M**aniac
- 8 **C**ontrol



[1] : N.B. Mota, N.A.P. Vasconcelos, N. Lemos, A.C. Pieretti, O. Kinouchi, G.A. Cecchi, M. Copelli, and S. Ribeiro. Speech graphs provide a quantitative measure of thought disorder in psychosis. PloS one, 7(4):e34928, 2012.

Graphs (automated)

- Automate process

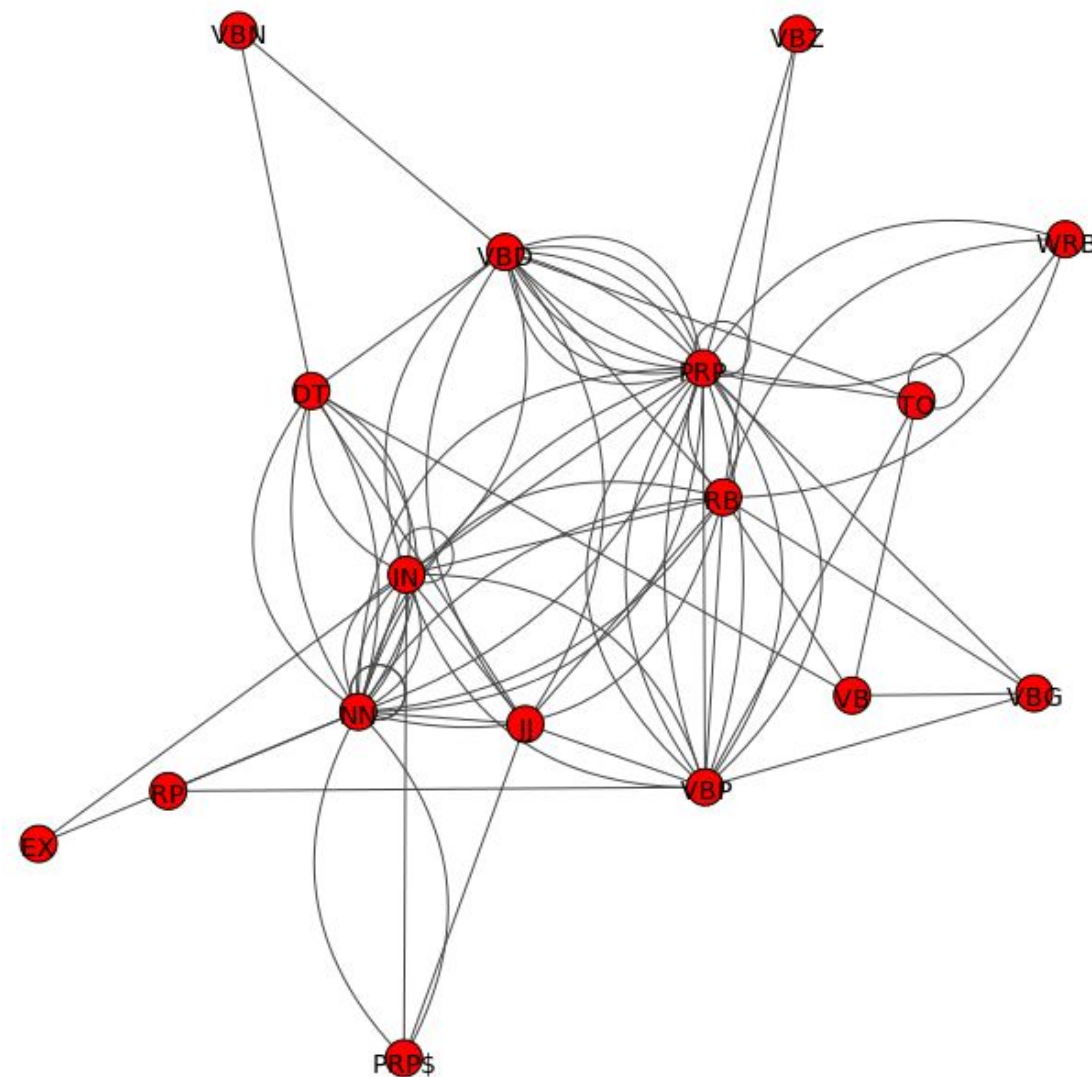
- **More** features!

word → node

word → Lemma → node

word → POS Tag → node

- Generate **classifier**



Full automatic classification

Classification with only two parameters
(Naive Bayes - 10 folds cross validation)

	S vs M vs C	S vs M	S vs C	M vs C
Previous work	0.6250	0.9380	0.8750	0.6880
Naive	0.6250 (naive_ATD y naive_L2)	0.9375 (naive_Nodes y naive_PE)	0.8750 (naive_ATD y naive_L1)	0.6875 (naive_L1 y naive_L2)
Lemmatized	0.7500 (lem_ATD y lem_L1)	1.0000 (lem_ATD y naive_PE)	0.8750 (naive_ATD y lem_L1)	0.8125 (lem_L1 y naive_PE)

S: Schizophrenia

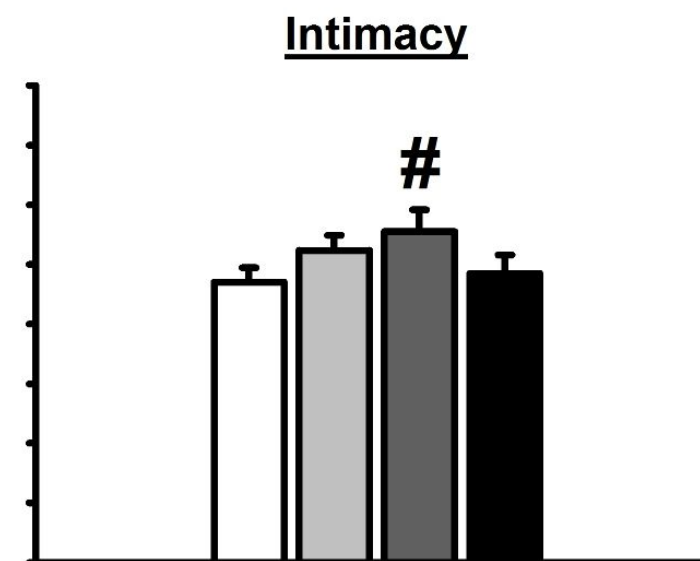
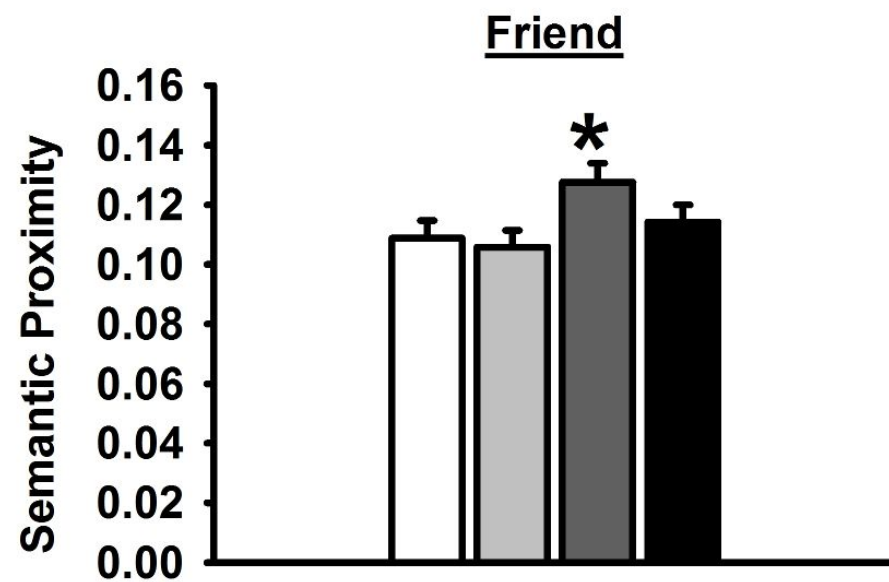
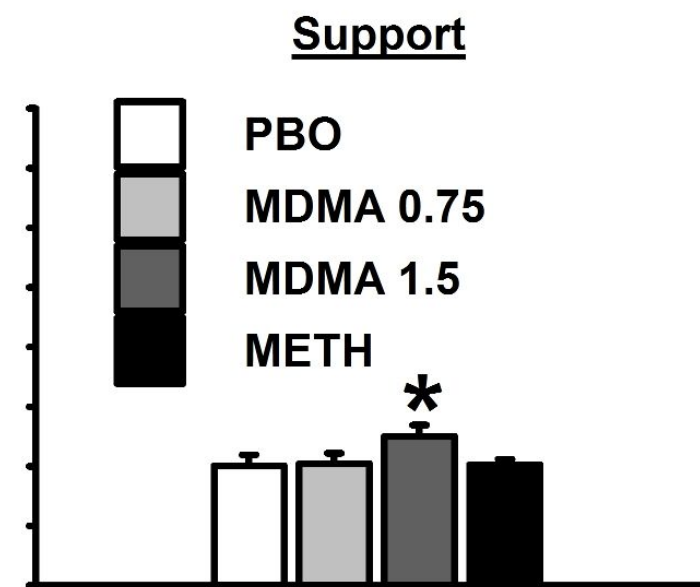
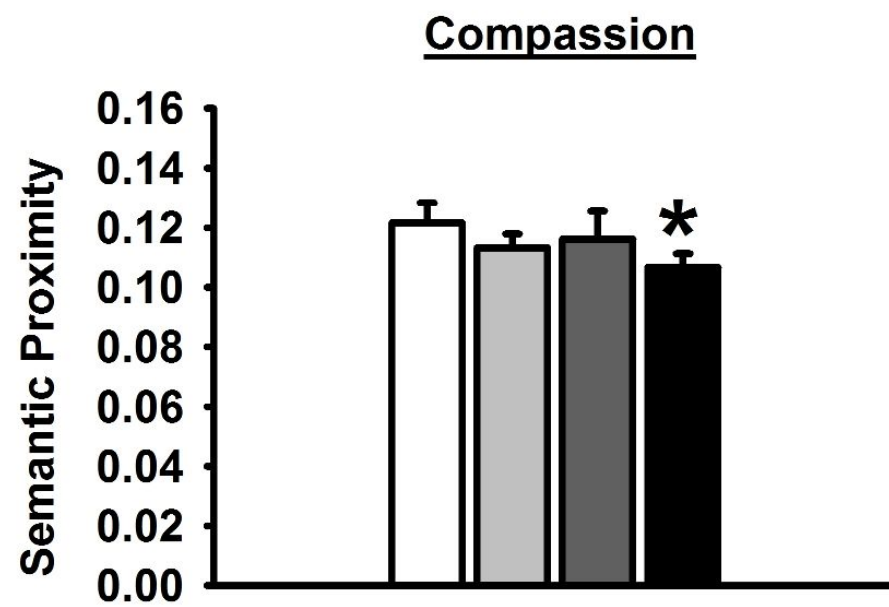
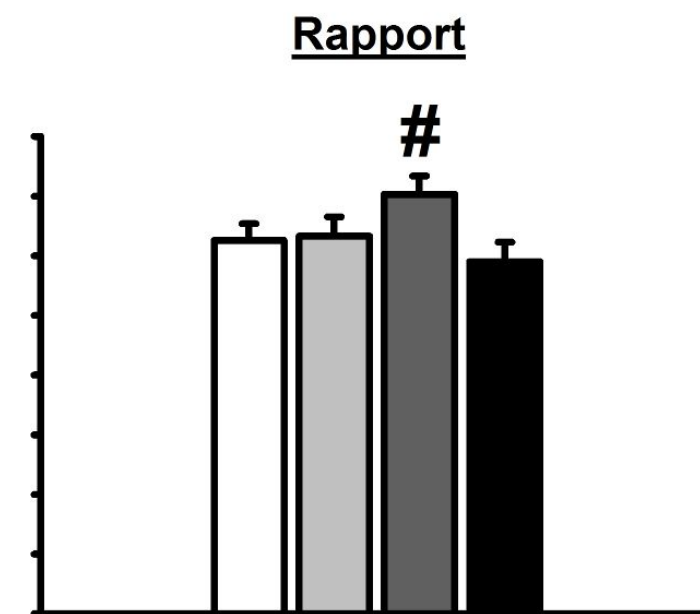
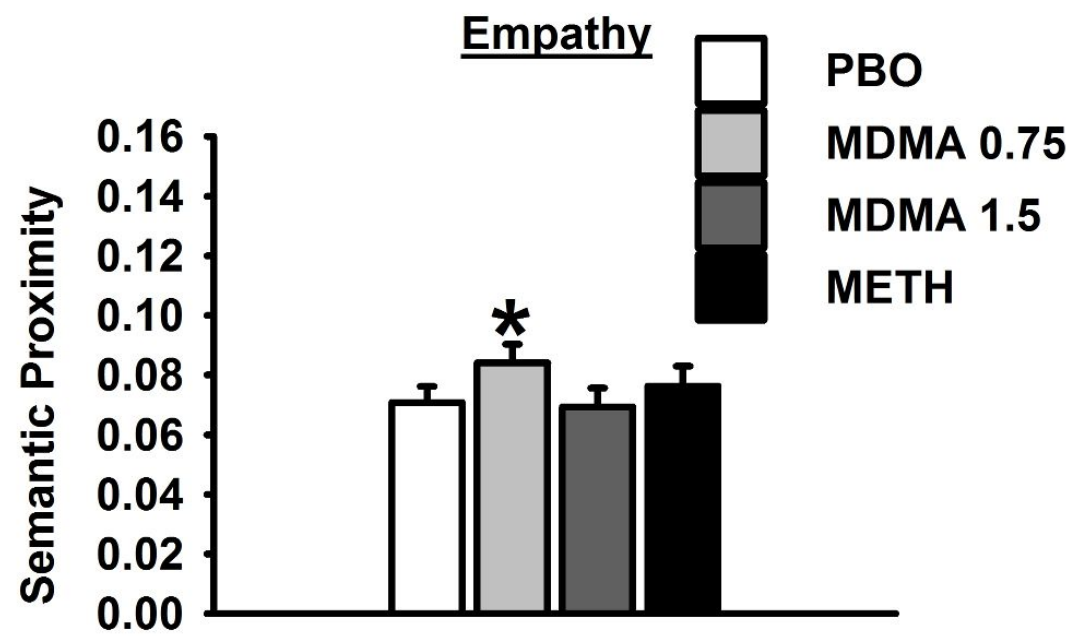
M: Mania

C: Control

New features... Application to Ecstasy

Experimental setup

- Regular Ecstasy Users (MDMA)
- Interviews in four conditions, blind to subject. (~2,000 words):
 - Placebo,
 - MDMA (high),
 - MDMA (low),
 - Methamphetamine.
- Measure semantic similarity to specific words: Empathy, Compassion, Forgiveness, etc
- Collapse interview to mean similarity to each concept word



A Window into the Intoxicated Mind

- Classifier: off-the-shelf SVM
- Leave-subject-out cross-validation

Condition I	Condition II	Accuracy		Baseline
MDMA1.5	PBO	88%	$\pm 6\%$	50%
MDMA1.5	METH	84%	$\pm 6\%$	50%
PBO	METH	69%	$\pm 10\%$	50%
MDMA1.5	MDMA0.75	57%	$\pm 11\%$	50%
METH	MDMA0.75	50%	$\pm 11\%$	50%
PBO	MDMA0.75	46%	$\pm 11\%$	50%
4-way		59%	$\pm 6\%$	25%

Classification of interviews of prodrome for schizophrenia

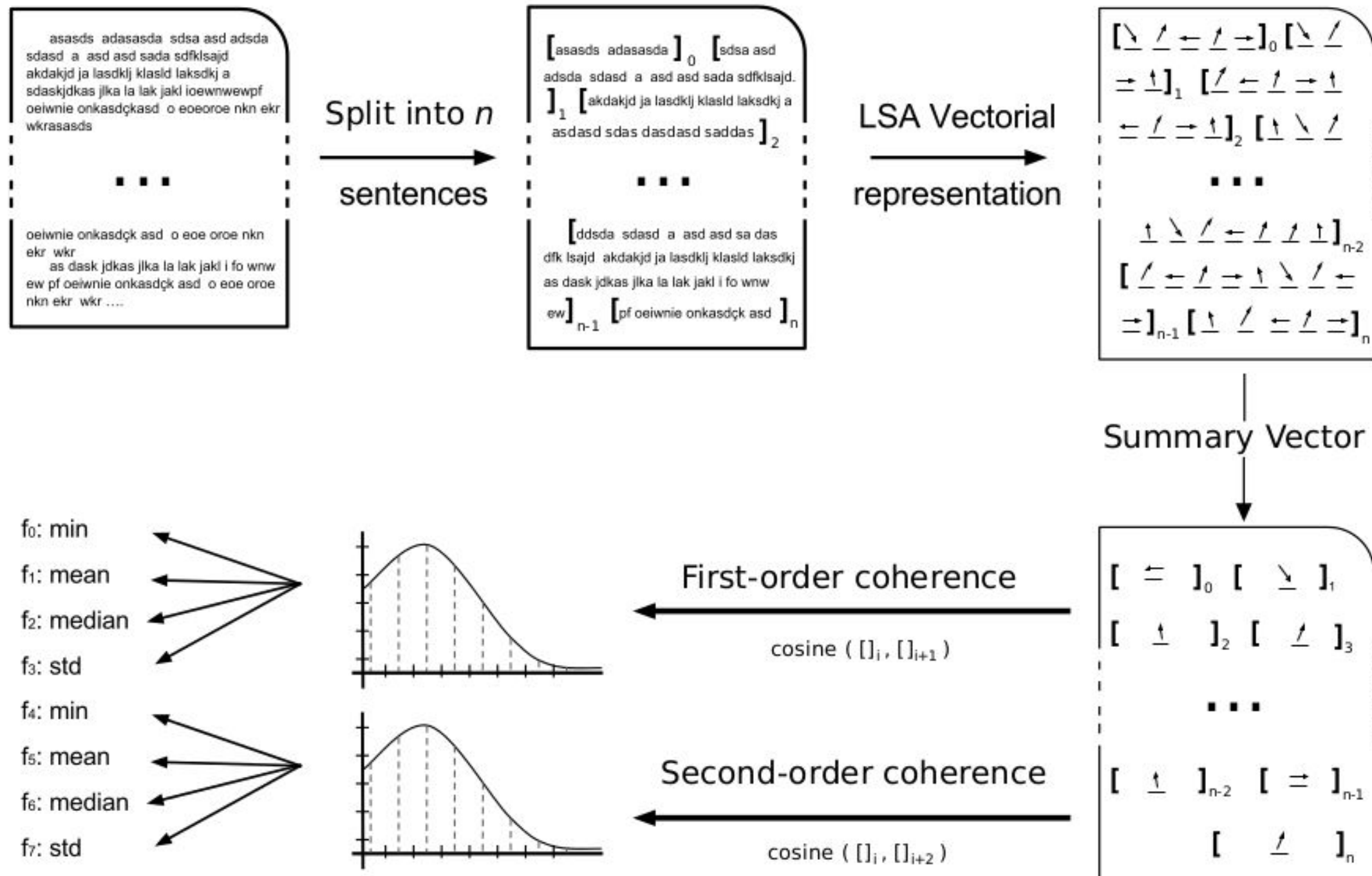
Schizophrenia

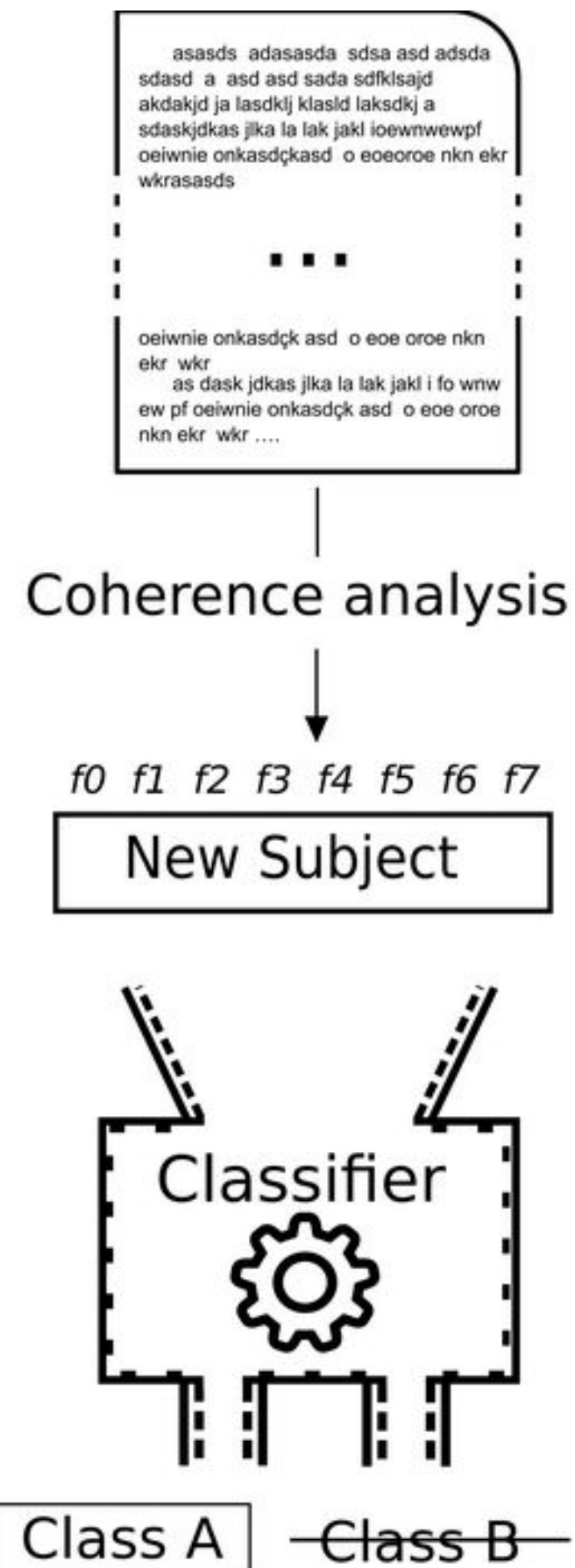
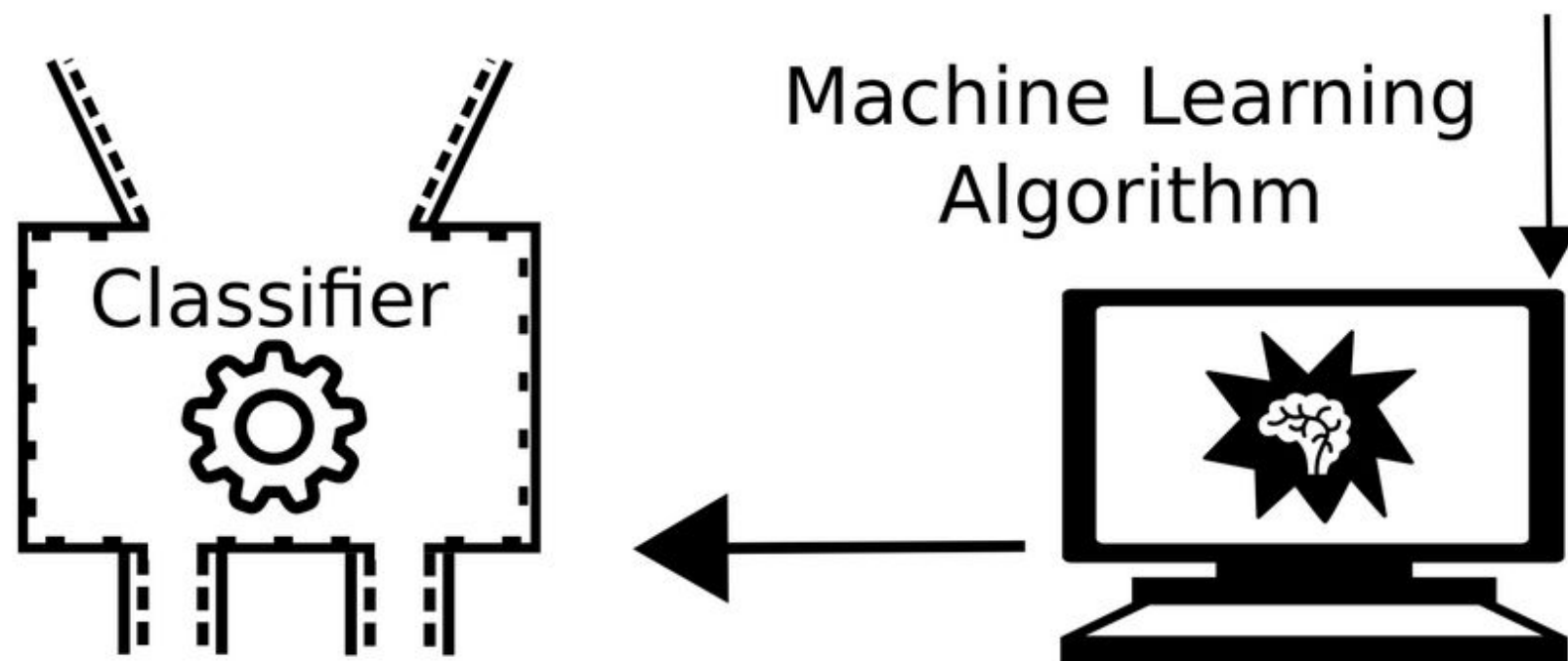
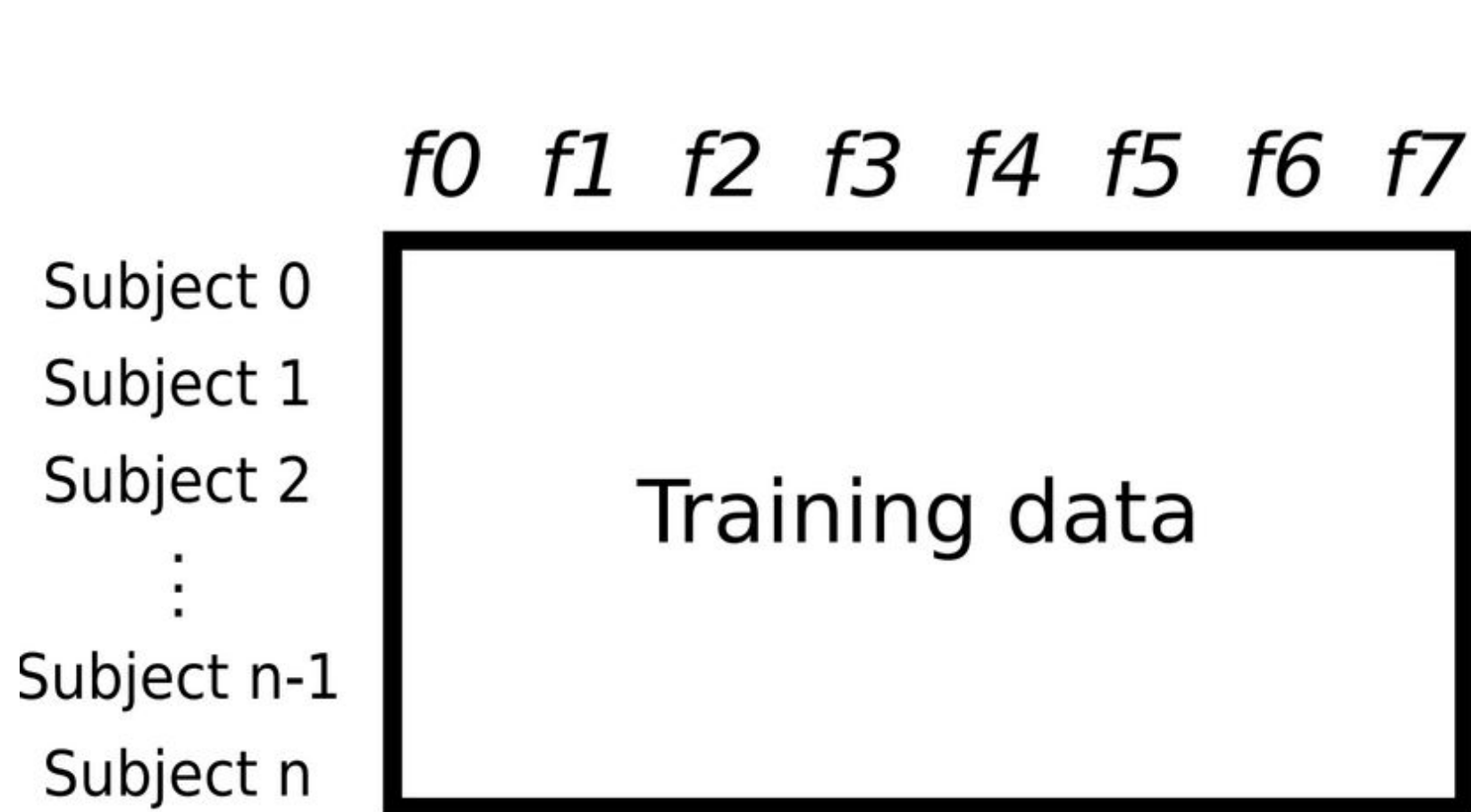
Wikipedia

- **Mental disorder** often characterized by **abnormal social behavior** and **failure to recognize what is real**.
- **Diagnosis** is based on observed behavior and the **person's reported experiences**.
- **Criteria**
 - DSM-5: To be diagnosed with schizophrenia, **two diagnostic criteria** have to be met over much of the time of a period of at least one month, with a significant impact on social or occupational functioning for at least six months. The person had to be suffering from **delusions, hallucinations or disorganized speech**.

Speech Coherence

- Coherence: semantic distance between sentences





Speech coherence: application to prodrome

Subjects (35) **decide to go** to Columbia Hospital because of anxiety, depression and other symptoms

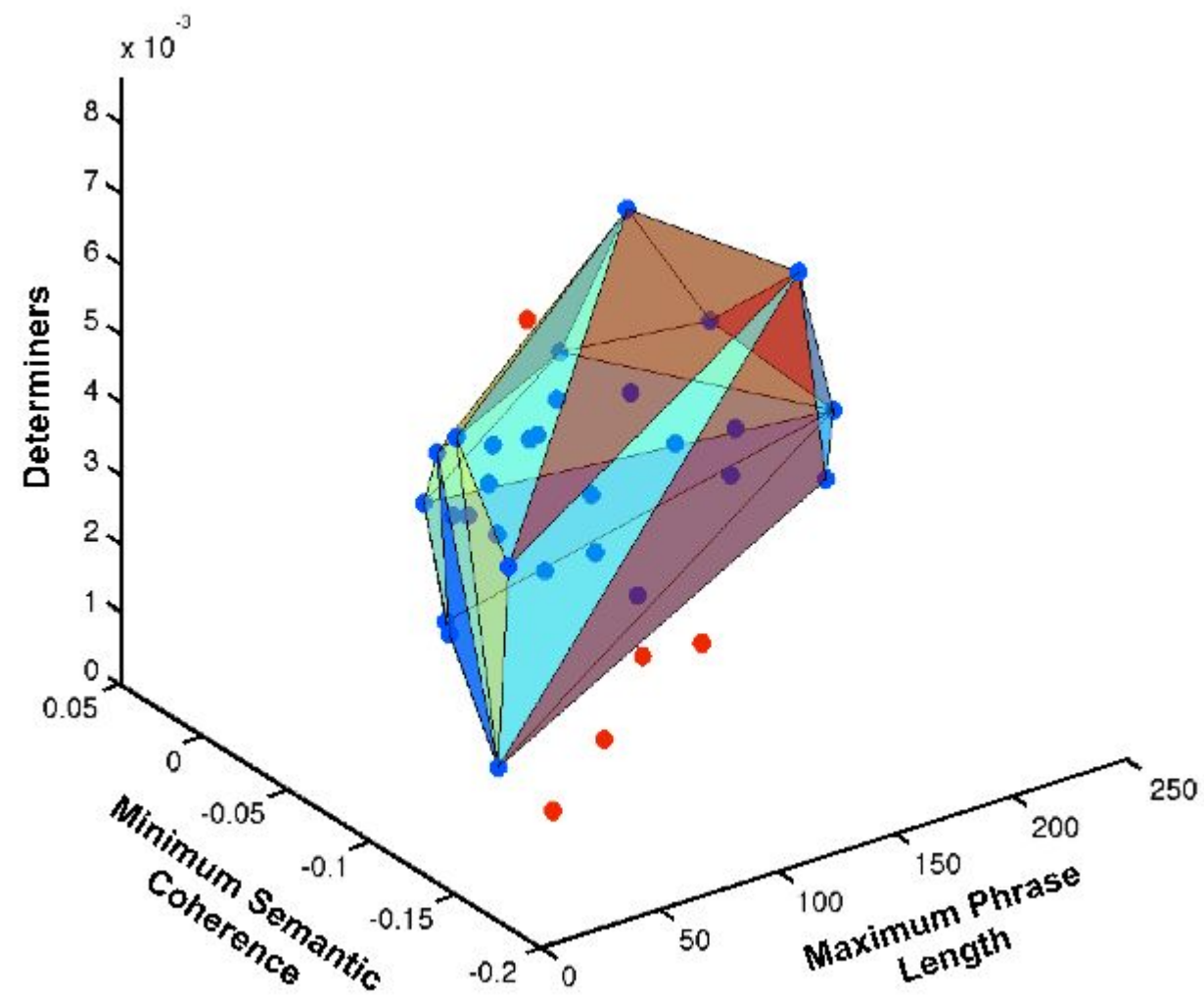
Guided interview **10'**: “Who are you? What are you feeling?”

No diagnostic before interview

One year later, **5 subjects** present psychotic episodes and declared **schizophrenic**

Classification Method

- Convex hull 3-features



Classification Performance

Method	PPV	NPV	Sens.	Spec	ROC
Convex Hull 3-features	100	100	100	100	1.0
'Black box' 22-features	67	96	80	93	0.8
SIPS/SOPS	33	89	40	86	0.47

PPV = Positive Predictive Value;

NPV = Negative Predictive Value;

Sens. = Sensitivity;

Spec. = Specificity;

ROC = Receiver Operating Characteristic Area Under the Curve;

SIPS/SOPS = Classification based on baseline scores on the Structured Interview for Prodromal Syndromes/Scale for Prodromal Symptoms;

Other semantic distances

Google Similarity Distance

- Cilibrasi, Rudi L., and Paul MB Vitanyi. "The google similarity distance", *IEEE Transactions on Knowledge and Data Engineering*, 19.3 (2007): 370-383.

$$\begin{aligned}\text{NGD}(x, y) &= \frac{G(x, y) - \min(G(x), G(y))}{\max(G(x), G(y))} && \text{(III.3)} \\ &= \frac{\max\{\log f(x), \log f(y)\} - \log f(x, y)}{\log N - \min\{\log f(x), \log f(y)\}},\end{aligned}$$

- Problems:
 - If you search for “Maradona”: About 8,080,000 results. **Very imprecise value**
 - IP blocking issues

Twitter similarity distance

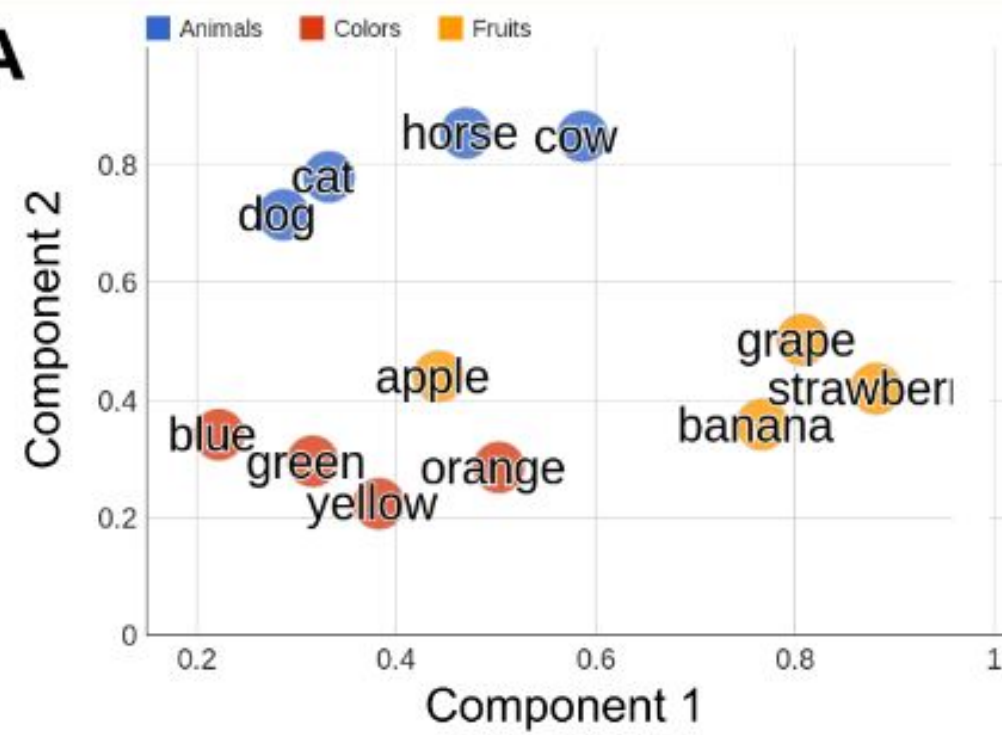
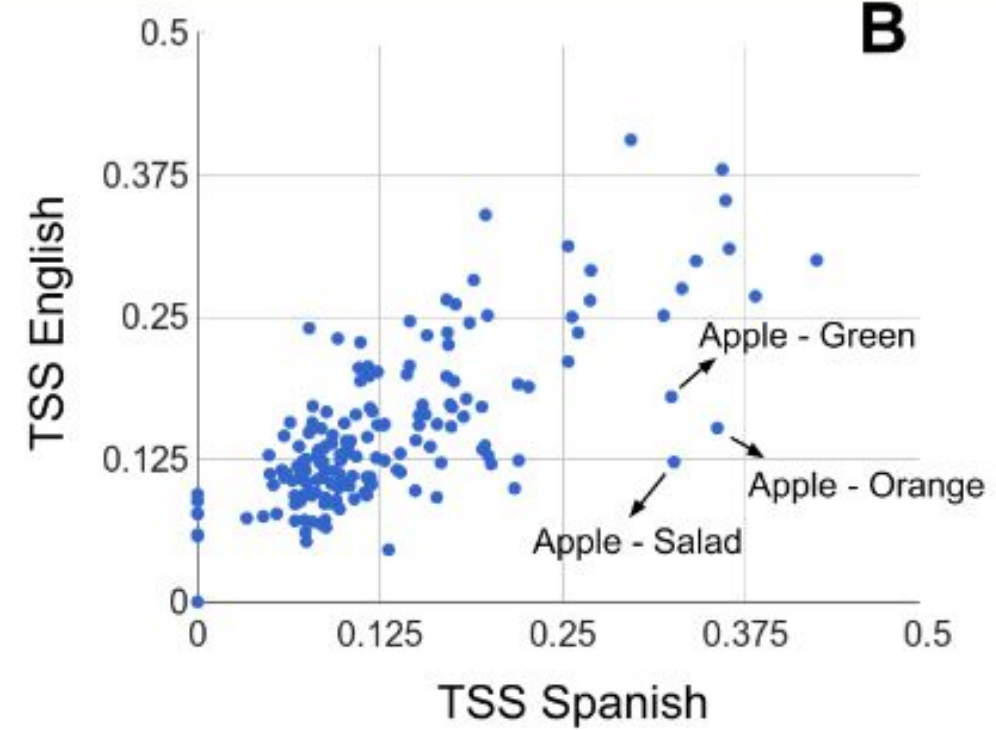
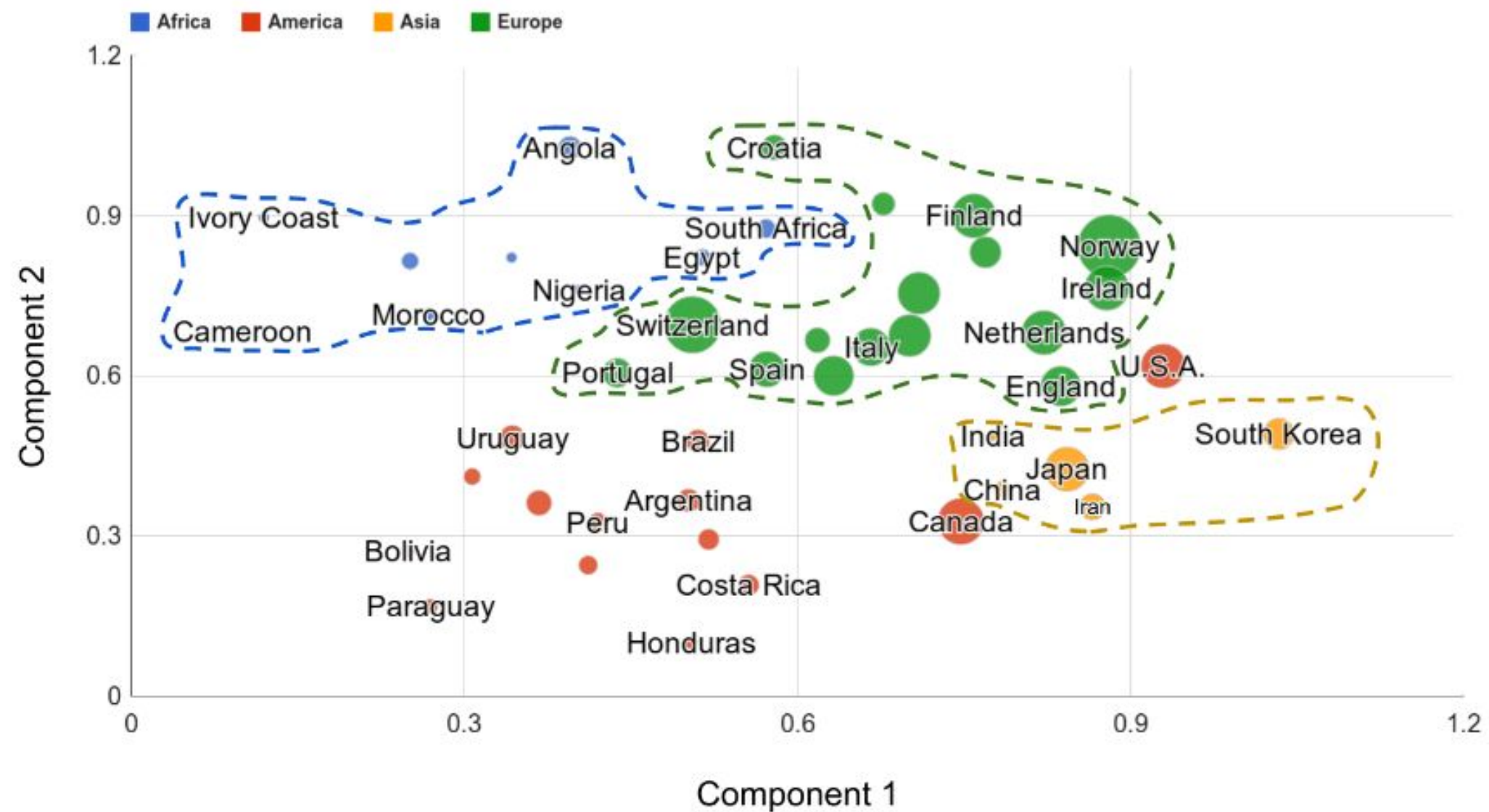
Twitter Similarity Distance

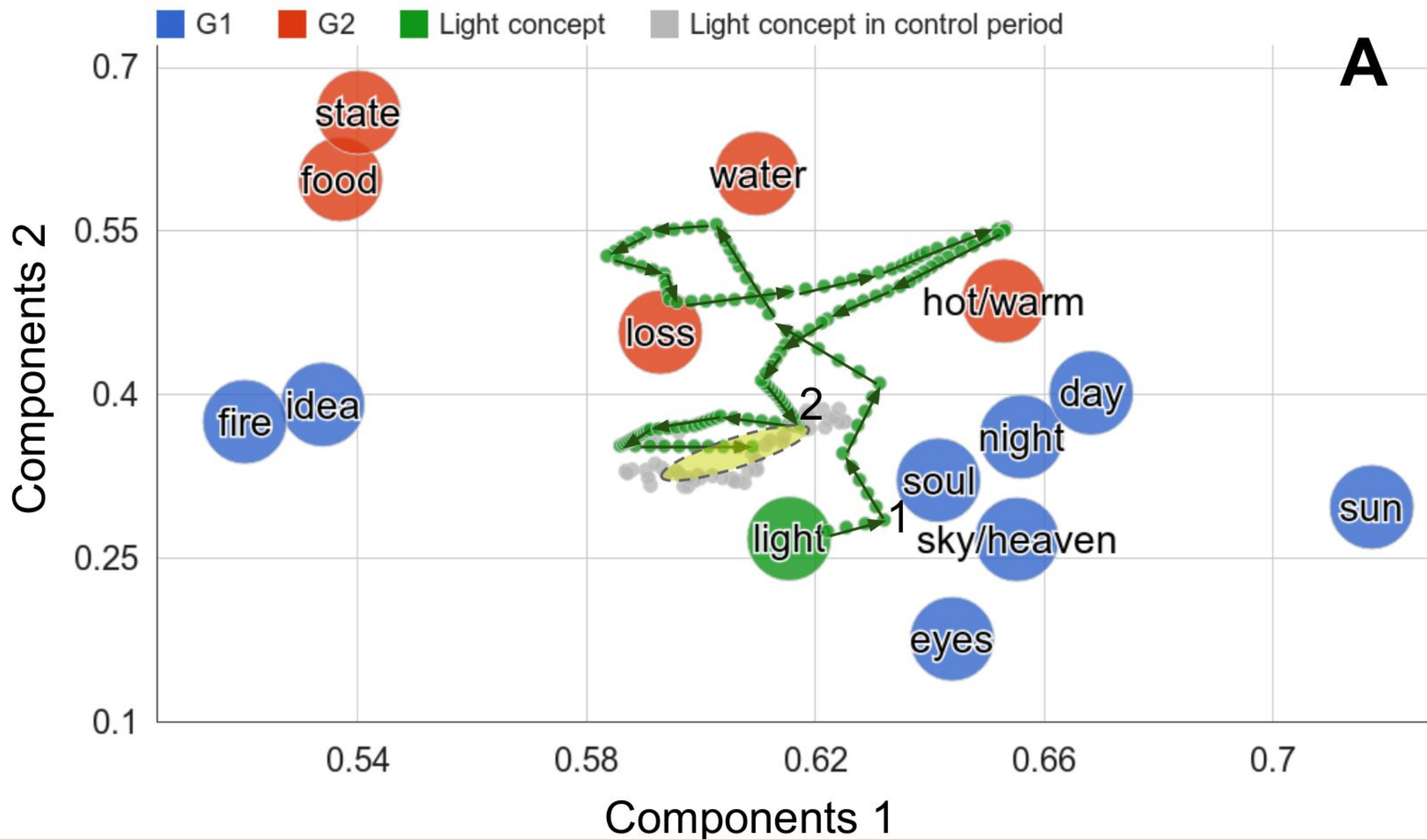
Considering the word w and the timestamp series T of tweets containing w :

$$\Phi(w) = \left(\frac{\sum_{i=1}^{N-1} (\tau_{i+1}(w) - \tau_i(w))}{N - 1} \right)^{-1}$$

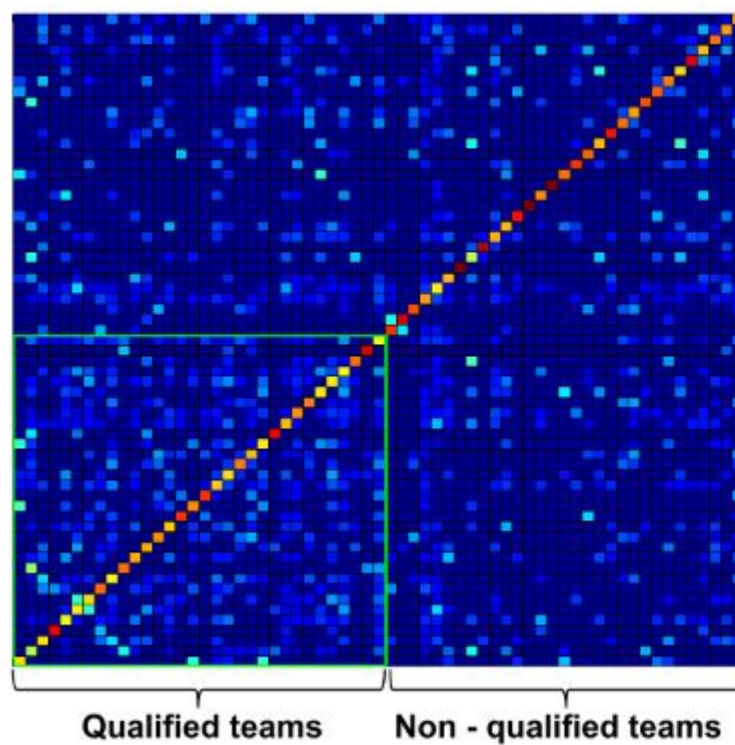
Then,

$$TSS(w_1, w_2) = \left(\frac{\Phi(w_1 \wedge w_2)}{\max(\Phi(w_1), \Phi(w_2))} \right)^{\alpha}$$

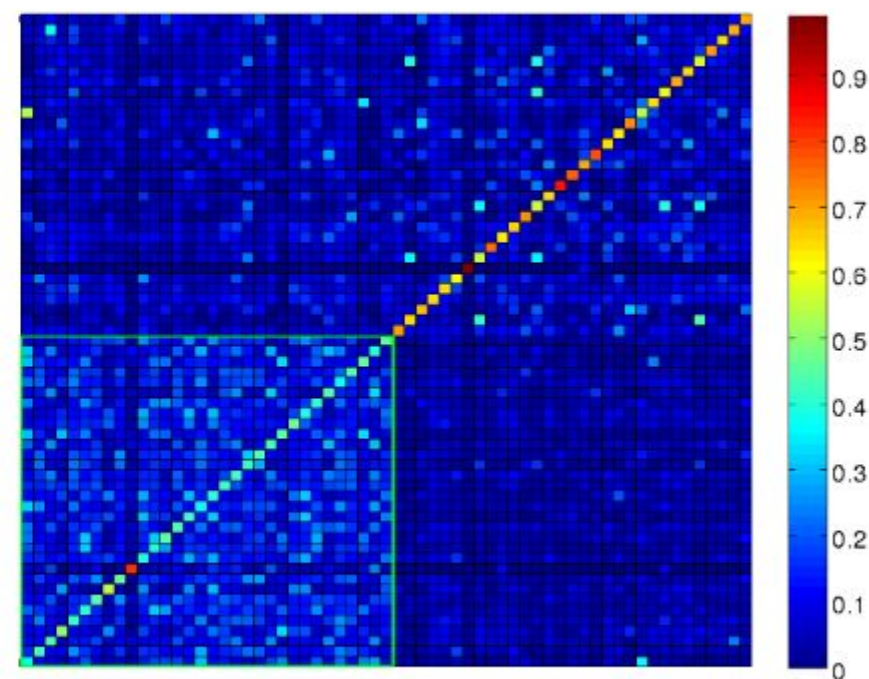
A**B****C**



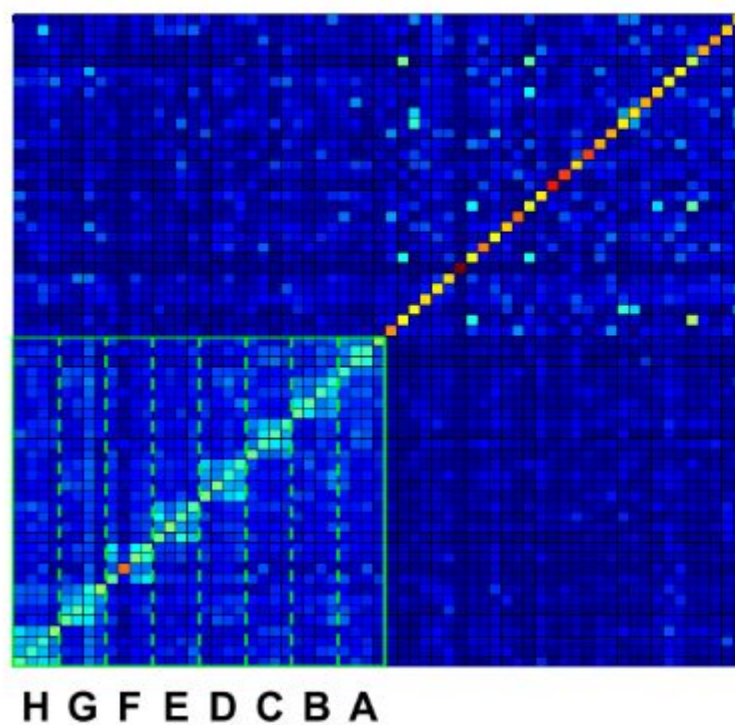
3 days before the draw (D-7)



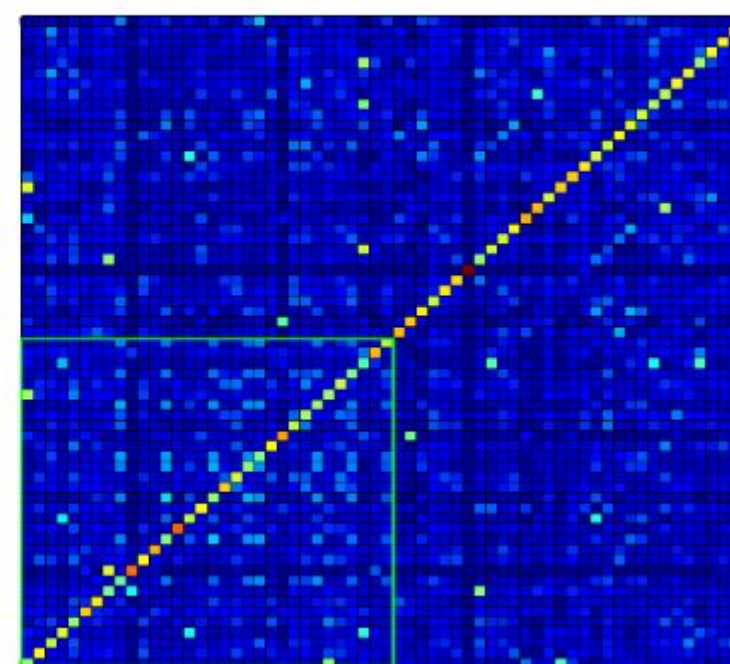
Just before the draw (D-1)



Just after the draw (D+1)



A week after the draw (D+7)



Groups classification

