

# **Microscopic Simulation of Solid State Sintering Regarding Irregularly Shaped Powder Particles**

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# Preface

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