the half-sector corresponding to the sweep direction, let pluster. Hence, hopefully a better schedule could be obtained lalf-sector will be relatively far away from the new he intuition behind partitioning the unscheduled customers isector be the seed for a new cluster (see diagram below). ographical cohesiveness, one might consider different seed is then repeated until all customers have been scheduled. ie ray from the depot through that customer and the ie unscheduled customer with the smallest angle formed by lection criteria for the next cluster. A simple rule that istering-scheduling process is repeated. ounterclockwise used is to bisect the sector just considered, and, by scheduling them at a later stage. The process sector sweep, in two subsets is that, assuming a the customers in the right ij preserve

this new reference customer and the best solution obtained a11 over all possible rotations. customers. A different initial seed can be obtained by rotating The algorithm can then be restarted with

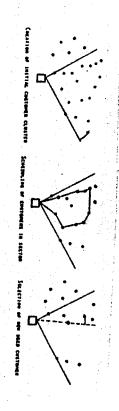


Diagram 3.6.

3.2.5 A giant-tour heuristic for (VRSPTW).

tour over phases of the algorithm consist of call this a sequence first, schedule second method. time constraints accounts. windows in this case study where manually accomodated for, and Russell(1978) for a case study in (VRSPTW). The time the fleet size and mix vehicle routing problem, and by Cook for routing electric meter readers, by Levi et al. (1980) for the context of school bus routing, by Stern and Dror(1979) by Newton and Thomas(1974), and by Bodin and Berman(1979) in (see Bodin and Golden(1981)). This approach has been taken route-first, cluster-second methodology in was possible due to the relatively small percentage of all the heuristic customers and the creation of time and In the context of (VRSPTW) we is ta the based construction vehicle routing 9 the

pacity feasible subtours by partitioning the original

equence to the previous tour). Results obtained by Golden omposite heuristic (tour construction, 2-opt, applied in õ iant tour" into contiguous segments. initial (TSP) tour over all the customers. We use a Various approaches have been used for the creation such procedures relatively fast

t al.(1980) found

of the problem of splitting a (TSP) tour into feasible subtours of contiguous customers, as a shortest path problem rehicle schedules from this original tour is in the modeling omputationally and giving excellent results. The gist of the procedure for creating feasible

distance between customers N(m) and N(p) in the new network, on a transformed network. denoted by D(m,p) is the total cost of having a vehicle Such distances are computed for pairs of customers who are service customers N(m+1),...,N(p), for m < p, in that order-Let the (TSP) tour be (0,N(1),...,N(n),0). Then the

time and capacity feasible, i.e. D(m,p) = central depot to the last customer on the tour in this acyclic network. The number of trucks used will equal the $\Big(+ \omega \ , \ \text{if} \ \sum_{i=m+1}^p a_i > b_k, \ \text{or} \ \exists \ i, \ m+1 \leq i \leq p, \ \text{st} \ t_i > d_i$ The problem is then to find the shortest path from the ${c_{0,N(m+1)} + \sum_{i=m+1}^{p-1} c_{N(i),N(i+1)} + c_{N(p),0}}$

number of arcs in the solution to this problem

procedures. that this label-correcting approach seems to perform better computational study by Klingman et al. (1977) has revealed shortest path algorithm is that of Pape(1974). than other the network(see Klingman et al.(1977)). Our choice of a algorithms. We use a sorted forward star representation for significantly reduce Efficient types of algorithms, including "label-setting" data storage and the computation time of network manipulation

3.2.6 Improvement heuristics.

giant-tour heuristic. and capacity feasibility checks could be implemented through reduction in overall schedule time and distance. the same number of vehicles as before, and it leads to a interchange would be performed only if it produces at most interchanges among and/or within vehicle schedules. An approaches to (VRSPTW). be used as initialization heuristics for k-optimal The heuristics described in the previous sections or, the transformed network described for the One could consider k-opt

We have implemented Ŋ 3-optimal approach for the

problems with sufficiently tight capacity or time window constraints a lot of interchanges will be examined and found (VRSPTW) and found it computationally prohibitive. infeasible, research. One idea could be to examine only interchanges in the vicinity of each customer, and/or the ones requiring service at about consideration. one has to somehow limit the number examined. This is the same time a question for further as the customer under the customers Since in

3.3 Summary

we have focused on approximate methods for its solution. features that formally. complexities. computational experience with these methods will be reported in the next chapter. this chapter, we of. Ιt heuristic approaches are described. Extensive allow was shown that our model has many attractive Given it the intrinsic difficulty of (VRSPTW), to accomodate important problem have introduced the (VRSPTW)

CHAPTER IV

COMPUTATIONAL STUDY

4.1 Introduction

horizon. windows, used to environments which differ in terms of the type of data being problems. This problem set includes routing and problems presented, given that no benchmark problem set is available study of the methods described previously. In order to evaluate the computational capabilities of the their tightness and positioning, and the scheduling literature for generate this chapter we conduct an extensive computational with time windows, we have developed such a set of the problems, the vehicle routing and scheduling percentage scheduling heuristics og S

parametric analysis of the best heuristics. behavior computational experience with the heuristics Of, the The the or first part of the chapter describes the generation various these effect heuristics. problem of time window related factors on sets. Finally, we present ¥e developed report our

.2 Development of the Problem Sets.

We have generated six sets of problems. The design of these test problems highlights several factors that can affect the behavior of routing and scheduling heuristics. These factors include: geographical data, the number of customers serviced by a vehicle, and time window characteristics such as percentage of time constrainted characteristics such as percentage of the time customers, and tightness and positioning of the time

corresponding problem sets by R1 and R2), clustered (denote semi-clustered (denote the corresponding problem sets by RC1 containing a mix of randomly generated and Problem sets R1, C1, RC1 have a short scheduling horizon. The length of route-time constraint acts as a capacity constraints, allow only a few customers to be serviced by the same vehicle. long scheduling horizon; capacities, permit many customers to be on the same vehicle RC2). corresponding far as the geographical and demand they are randomly generated (denote By a semi-clustered problem we mean a problem which, together with the vehicle capacity problem sets by C1 and C2), and In contrast, the sets R2, C2, RC2 have a this, coupled with data and clusters. large vehicle data are

Given a certain geographical and demand data, we have created the (VRSPTW) test problems by generating time windows of various widths for different percentages of customers. In terms of time windows' density, i.e. the percentage of customers with time windows, we have created problems with 25 %, 50 %, 75 %, and 100 % time windows.

normally distributed random number. number in the interval (t_{0,i_j} , $h-t_{i_j,0}-s_{i_j}$), where h is the length of the scheduling horizon. To create the time window's width for customer i_j , $j=1,\ldots,n_1$, as being a randomly fn, $0 < f \le 1$. The time windows have a randomly generated randomly selected. receive time windows; RC1, RC2. First, we select the percentage of customers was used for the development of the problem sets R1, random and width. We choose the center of the time window generation of time window constraints. This method Mou present a method we have designed for for i_j, we generate half the width as a Let these customers be i,..., in, n, = then, the actual customers generated R2,

A somewhat different method was used for the clustered problems, C1 and C2. Here, we first run a 3-opt routine on each cluster to create routes and then produce schedules by selecting an orientation for each cluster. The time window constraints are generated by choosing the center as the arrival time at each customer; the width and density are

prived as before. The rationale for using this method of problems is that it leads to the creation of structured roblems. Such problems serve a double purpose: Not only an one examine the relative performance of heuristics on lustered problems, but one can also test the robustness and ntelligence of the heuristics being examined since their ntelligence of the heuristics being examined since their pehavior can be compared in the absolute against a very good pehavior can be compared in the absolute against a very good

All the test problems are 100 customer problems. This problem size is not limiting for the methods presented, as much larger problems could be solved. Rather, we selected this size since it strikes a nice compromise between problem comprehensive computer resources made available for this customers are taken to equal the corresponding distances. Furthermore a homogeneous fleet is assumed. We now present a detailed description of each set of test problems.

Problem Set R1.

The customer coordinates and demand data for this problem set are those of problem 8 from the standard set of routing test problems given in Christofides et al.(1979). Without time window constraints, a fleet of 10 vehicles, each of capacity 200 units, is necessary to satisfy the

characteristics of these problems are given in table 4.1. realistic. This problem is depicted in diagram 4.1. window constraints. Moreover, as mentioned above, its size problems in the test set since it allows enough customers service time. is assumed. the length of route constraint make this problem truck to permit the nontrivial introduction of the time generated requirements. We have selected problem A maximum allowable route time of 230 units 12 test problems Each customer requires 10 units of n H this set. 8 among all the

iagram 4.1

				, w.	b	r.	€	4	₹ ₽
3	3	<u> </u>	24 D	TWM	TWSD	ETM	ETSD	LTM	LTSD
Problem	% TW	Mean	St.D.					123.52	45.56
1 2 3 4 5 6 7 8 9	100% 75% 50% 25% 100% 75% 25% 20% 100%	5. 5. 5. 15. 15. 15. 160.	0. 0. 0. 0. 0. 0. 0. 7.50	10. 10. 10. 30. 30. 30. 30. 58.89 86.50	0. 0. 0. 0. 0. 0. 0. 8.93 39.27	96.48 100.04 101.26 104.60 86.73 90.25 91.18 93.96 73.01 60.18	45.56 45.50 48.38 47.89 43.80 45.80 45.83 38.79 33.90	119.96 118.74 115.40 113.27 109.75 108.82 106.04 98.10 83.32	45.50 48.38 47.89 43.80 43.31 45.80 45.33 37.85 36.02
10 11	50% 25% 25%	30. 15. 30.	15. 3.75 7.50	93.10	54.73	61.35	40.49	75.55	42.19
12	25% 25% 100%	60. 90. 60.	15. 22.50 15.	117.64	17.45	47.20	22.67	65.16	22.93

Problem Set C1.

difficulty of a given (VRSPTW).

the intervals (d_1,h) , $j=1,\ldots,n_1$. They describe the positioning of the time windows within the scheduling horizon. Overall, the above measures indicate the relative

intervals $(0,e_1)$, $j=1,\ldots,n_1$, while the columns headed LTM and LTSD give the sample means and standard deviations of

the problem or the problem 's density. The values in the columns headed Mean and St.D. are the means and standard deviations of the normal distributions used to create the time windows' widths. Columns 5 and 6 show the actual mean and standard deviation of the time windows obtained. The average time window, when compared to the length of the scheduling horizon, provides a measure of the tightness of the time windows in the problem. The values in the columns

and 8 are the sample means and standard deviations of the

For this problem set, the geographical and demand data are those of problem 12 (Christofides et al.(1979)); (see diagram 4.2). Vehicle capacity is assumed to be 200 units. Each customer requires 90 units of service time. A restriction on the maximum allowable time per route of 1236 units is imposed. The best cluster by cluster solution we

Column 2 represents the percentage of time windows in

Table 4.2 Problem Set C1

Problem	% TW	Mean	St.D.	TWM	TWSD	ETM	ETSD	LTM	LTSD
1	100%	30.	7.50	60.76	10.53	426.80	282.20	748.44	282.05
2	75%	30.	7.50	61.27	9.89	401.11	265.88	773.63	265.04
3	50%	30.	7.50	59.90	9.76	430.74	256.65	745.36	256.06
4	25%	30.	7.50	60.64	9.37	410.32	243.80	765.04	244.13
5	100%	60	15.	121.61	20.98	399.16	277.29	715.23	276.89
6	25% 25% 25% 25%	30. 60. 90. 120.	15. 30. 45. 60.	156.15	91.86	383.74	272.73	696.11	280.06
7	100%	90.	0.	180.	0.	272 00	000 00		
8	100%	120.	30.	243.28	41.96	372.98 347.22	272.92	683.02	272.92
9	100%	180.	0.	360.	0.	298.33	261.43 245.98	645.50 577.67	261.36 245.98

distinguishes five clusters (see diagram 4.3). These

the outside clusters of problem 12 containing 43 customers,

consolidated with 7 additional customers.

customers limitation

Unloading time

Ę.

units.

o**f** are

240 time units per route

10 units per customer. The capacity of

fleet of 10 vehicles

selected from those of

problem 8.

ŗ.

assumed.

The other 50

two routing problems mentioned above. Geographically, one

This problem set was created by using data from the

each vehicle is 200 in table 4.3. necessary to satisfy demand. This problem set is described

Table 4.3 Problem Set RC1.

Problem	% TW	Mean	St.D.	TWM	TWSD	ETM	ETSD	LTM	LTSI
1	100%	15.	0.	30.	0.	91.82	42.23	118.18	42.23
2	75%	15.	0.	30.	0.	94.84	42.43	115.16	42.43
3	50%	15.	0.	30.	0.	95.76	46.01	114.24	46.01
4	25%	15.	0.	· 30.	0.	95.92	42.39	114.08	42.39
5	25% 25% 25% 25%	5. 15. 30. 60.	0. 3.75 7.50	54.33	41.81	82.59	44.04	103.08	42.16
6	100%	30.	0.	60.	0.	77.54	37.52	102.46	37.52
7	50% 50%	60. 30.	15. 7.50	88.21	32.82	64.12	31.45	87.67	34.03
8	100%	60.	30.	112.33	30.80	55.09	24.70	72.58	25.02

Problem Set R2.

To permit the servicing of many customers by a hicle, we have modified the data of problem set R1 by creasing the allowable route time to 1000 units and the apacity of each vehicle to 1000 units. Two vehicles are indows are not present. Summary characteristics of these roblems can be found in table 4.4.

Problem Set C2

Using the data from problem 12, we have relocated some of the customers to create a structured problem with three large clusters of customers (see diagram 4.4). A fleet of three vehicles, each of capacity 700 units, is assumed. The maximum allowable time per route is 3390, and the customer service times are 90 units. For this set of problems, the best schedule we found (believed to be optimal) requires a distance traveled is 591 units. Table 4.5 summarizes this problem class.

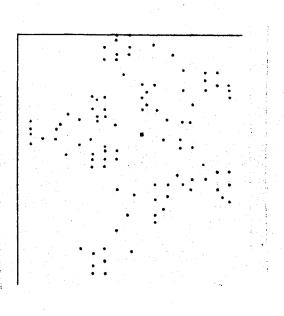


Diagram 4.4

Problem Set RC2

The geographical, demand, and service time data for this set of problems are the same as for RC1. We have modified the length of route-time constraint and the vehicle capacities to allow a vehicle to visit many customers on a route. The route-time limitation is 960 units and vehicles are assumed to have a capacity of 1000 units. Without time windows, a fleet of two vehicles is sufficient to satisfy demand. Problem characteristics are presented in table 4.6.

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Table 4.4 Problem Set R2

Problem	% TW	Mean	St.D.	TWM	TWSD	ETM	ETSD	LTM	LTSD
1 2 3 4 5 6 7	100% 75% 50% 25% 100% 75% 50% 25%	60. 60. 60. 120. 120. 120. 240.	30. 30. 30. 30. 0. 0.	115.96 115.23 117.34 111.80 240. 240. 240. 240. 349.50	35.78 35.56 34.35 31.13 0. 0. 0.	391.21 407.91 411.70 431.76 330.26 346.07 349.84 362.56 280.59	244.71 244.51 258.15 243.53 230.27 229.53 240.08 232.45 202.44	492.83 476.87 470.96 456.44 429.74 413.93 410.16 397.44 369.91	238.03 241.82 257.39 251.01 230.27 229.53 240.08 232.45 204.73
9 10	50% 50% 25% 25%	120. 60. 120.	60. 15. 30.	383.27	237.98	282.66	230.98	334.07	226.10
11	25% 25% 100%	240. 360. 240.	60. 90. 60.	471.94	71.67	225.24	175.51	302.82	168.40

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Table 4.5 Problem Set C2.

Problem	% TW	Mean	St.D.	TWM	TWSD	ETM	ETSD	LTM	LTSD
1	100%	80.	0.	160.	0.	1470.21	921.06	1759.79	921.06
2	75%	80.	0.	160.	0.	1493.44	933.91	1736.56	933.91
3	50%	80.	0.	160.	0.	1472.94	957.90	1757.06	957.90
ц	25%	80.	0.	160.	0.	1598.36	974.76	1631.64	974.76
5	100%	160.	0.	320.	0.	1393.28	911.54	1676.72	911.54
6	100%	240.	60.	486.64	83.99	1312.95	898.33	1590.41	901.23
7	25% 25% 25% 25%	120. 240. 360. 480.	30. 60. 90. 120.	612.32	302.72	1243.78	862.29	1533.90	939.21
8	100%	320.	0.	640.	0.	1242.69	879.90	1507.31	879.90

		.4	·					·	
Problem	% T4	/ Mean	St.D.	TWM	TWSD	ETM	ETSD	LTM	LTSD
 ,									

Problem	% TW	Mean	St.D.	TWM	TWSD	ETM	ETSD	LTM	LTSD
1	100%	60.	0.	120.	0.	371.18	229.80	468.82	229.80
2	75%	60.	0.	120.	0.	386.39	232.60	453.61	232.60
3	50 %	60.	0.	120.	0.	391.70	247.85	448.30	247.85
4	25%.	60.	0.	120.	0.	405.88	233.59	434.12	233.59
5	25% 25% 25% 25%	30. 60. 120. 240.	0. 15. 30. 0.	223.06	162.66	327.96	237.33	408.98	222.23
6	100%	120.	0.	240.	0.	313.03	214.05	406.97	214.05
7	50% 50%	240°. 120.	120. 60.	349.50	163.84	263.34	186.39	347.16	189.32
8	100%	240.	60.	471.93	71.67	208.61	156.10	279.46	149.83

4.3 Computational Results.

been performed on the problem classes described above. remark that, in obtaining the computational results, we have not used any k-optimal improvement procedures. In the DEC-10, which includes the time to read the data and the are the number of routes and the CPU time in seconds on the time, respectively. the total schedule time, total distance and total waiting tables that follow the numbers to the left of each box are actual computation of intercustomer distances in results are provided in the Appendix. that order, for the minimum number of trucks that will admit methods tested on the problem set R1 are shown in table $^4 ext{-}7 ext{-}$ feasible solution. terms of minimum schedule time and minimum distance , in programmed in Fortran, and computational tests were The heuristics described in the previous section have As discussed in chapter 3, we measure solution quality parameter values used to obtain the computational The numbers to the right of each box The relative performances and times. We must