```
In [1]: import numpy as np
    import matplotlib.pyplot as plt
    import pickle

    pkl_file = open('classifier_data.pkl', 'rb')
    x_train, y_train = pickle.load(pkl_file)

    n_train = np.size(y_train)

    plt.scatter(x_train[:,0],x_train[:,1], c=y_train[:,0])
    plt.title('training data')
    plt.show()
```

```
In [2]: def regularized_log_loss_function(X, y, w, lam):
                function takes a matrix X with each column a feature vector, a vector y of labels,
                takes a w, and returns a scalar representing the value of function in 2b
                m,n = np.shape(X)
                res = 0
for i in range(n):
                    res += np.log(1+np.exp(-y[i]*X[:,[i]].T@w))
                res += lam*w.T@w
                return res[0][0]
           def gradient(X,y,w,lam,addDimension):
                function takes a matrix X with each column a feature vector, a vector y of labels, takes a w, a lamda parameter which happens to be one in this whole program and a boolean value which judges if we need to append the dimensions of the matrix.
                There are two cases, one requires appending and one does not. This variable
                \label{facilitates} \mbox{ facilitates that result.}
                if(addDimension==True):
                     grad = np.zeros((len(X[0])+1,1))
                else:
                     grad = np.zeros((len(X[0]),1))
                \# grad = np.zeros((len(X[0]),1))
                for i in range(len(y)):
                    yi = y[i][0]
xi = X[i]
                     if(addDimension==True):
                          xiT = np.append(xi, np.array([[1]]))
                     else:
                          xiT = xi
                 \begin{array}{lll} & curr = -1*yi*(1-(1/(1+np.exp(-1*yi*(xiT@w)))))*xiT.reshape((len(xiT),1)) \\ & grad = grad + curr \\ & return \ (grad + 2*lam*w) \end{array} 
           def graddescent(X,y,tau,w_init,it,addDimension=True):
                compute 10 iterations of gradient descent starting at w1
                \frac{w_{k+1}=w_k-\tan^2x^*(x^*w_k-y)}{w_{k+1}=w_k-\tan^2x^*(x^*w_k-y)} There is a boolean value which judges if we need to append the dimensions of the matrix. There
                are two cases, one requires appending and one does not. This variable facilitates that result.
                W = np.zeros((w_init.shape[0],it))
                W[:,[0]] = w init
                for k in range(it-1):
                     #X.T @ (X @ W[:,[k]] - y)
W[:,[k+1]] = W[:,[k]] - tau * gradient(X,y,W[:,[k]],1,addDimension)
```

```
In [3]: w_init = np.array([[1],[1],[1]])
tau = 0.006
w = graddescent(x_train, y_train, tau, w_init, 95, True)
w = w[:,len(w[0])-1].reshape(len(w),1)
print("w=\n", w)

W=

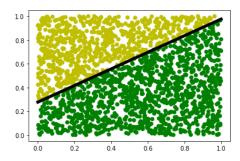
[[-6.44281082]
[ 9.21295439]
[-2.55074792]]
```

2 d)

```
In [4]: x_train = np.hstack((x_train, np.ones((len(x_train),1))))
yhat = np.sign(x_train@w)
plt.scatter(x_train[:,0],x_train[:,1],color=['g' if i==-1 else 'y' for i in yhat[:,0]])
error_vector = [0 if i[0]==i[1] else 1 for i in np.hstack((yhat, y_train))]
errors = sum(error_vector)
print("Rate of error: ", errors/len(error_vector))
slope = -w[0,0]/w[1,0]
y_int = -w[2,0]/w[1,0]
plt.plot([0,1], [y_int, y_int + slope], linewidth = 5, color='black')
```

Rate of error: 0.035

Out[4]: [<matplotlib.lines.Line2D at 0x266fc621550>]



2 e)

The error rate is greater (0.0455 > 0.035) than the one trained by logistic loss. The performance however is similiar.

2 f)

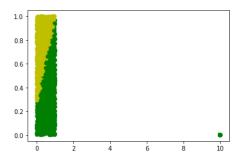
0.2

```
In [6]: #add new data
pkl_file = open('classifier_data.pkl', 'rb')
x_train, y_train = pickle.load(pkl_file)
x_train = np.hstack((x_train, np.ones((len(x_train),1))))
x_train_mod = x_train
y_train_mod = y_train
for i in range(1000):
    x_train_mod = np.vstack((x_train_mod, np.array([[10,0,1]])))
    y_train_mod = np.vstack((y_train_mod, np.array([[-1]])))

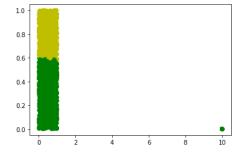
#logistic loss classifier
w_init = np.array([[1],[1],[1]])
tau = 0.006
#x_train_mod = np.vstack((x_train_mod, np.ones((1,len(x_train_mod)))))
w = graddescent(x_train_mod, y_train_mod, tau, w_init, 95,False)
w = w[:,len(w[0])-1].reshape(len(w),1)

yhat = np.sign(x_train_mod@w)
plt.scatter(x_train_mod[:,0],x_train_mod[:,1],color=['g' if i==-1 else 'y' for i in yhat[:,0]])
errors = sum(error_vector)
print("Rate of error" ", errors/len(error_vector))
```

Rate of error: 0.02466666666666667



The logistic classifier handles points which are very simple to classify, very well, and even sees the error rate go down.



The square error classifier does not handle the easy-to-classify points very well, and thus sees a huge error rate. It places a large importance on the distance from the boundary. The newly added points in the mod data points, thus have a huge effect on the decision boundary. Thus the error rate is high as we can see.