Activity 23 Ayar Deep Hazra
ECE 532 1. a) $j = \chi_1^2 w_1 + \chi_2^2 w_2 + \sqrt{2} \chi_1 \chi_2 w_3$ $+ \sqrt{2} \chi_1 w_4 + \sqrt{2} \chi_2 w_5 + w_6$ $\hat{y} = \left[x_1^2 x_2^2 \sqrt{2}x_1 x_2 \sqrt{2}x_1 \sqrt{2}x_2 \right]$ where No, i & £ 1, 2, 3, 4, 5, 69 correspond to the weight. Thuy $\phi^{7}(x) = [x_1^2 x_2^2 f_2 x_1 x_2 f_2 x_1 f_2 x_2 1]$ b) \$\phi^T(\xi) \phi(\xi) = \xi^2 \xi^2 + \xi^2 + \xi^2 + 2xi, xi2 xj1 xj2 + 2xi, xj; + 2 x 1/2 x 1/2 +1 $X_{i}^{*} T_{x_{j}} + 1 = X_{i}^{*} + X_{j}^{*} + X_{i}^{*} X_{j}^{*} + 1$ $(x_i, x_j, +1) = (x_i, x_j, + x_i, x_j, + x_i, x_j, +1)^2$ $= x_{ij}^{2} x_{j1}^{2} + x_{i2}^{2} x_{j2}^{2} + 2 x_{i}, x_{j1}^{2} x_{i2}^{2} x_{j2}^{2} + 2 x_{i}, x_{j1}^{2} x_{i2}^{2} x_{j2}^{2} + 2 x_{i1}^{2} x_{j1}^{2} + 2 x_{i2}^{2} x_{j2}^{2} + 1$ Thus (x, otx j+1) = \$\phi(x, o) \phi(x, o) c) for (xiTx; +1), we have to calculate $\phi^{T}(x) = \int_{1}^{2} x_{1}^{2} x_{2}^{2} \int_{2}^{2} x_{1} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{1} \int_{2}^{2} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{1} \int_{2}^{2} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{1} \int_{2}^{2} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{2} \int_{2}^{2} x_{1} \int_{2}^{2} x_{$ 3 Multiplications for P(x) & pexceach. The inner peroduct $\Phi^T(x)$ $\Phi(x)$ has 5 multiplications of its own (not counting 1). Thus botal Multiplications = 3+3+5 = 11

2, a) Oriver, w = (4 + 11) 4 y Cideor expression ptp + 24" How faction of from the left, we get \$ (\$\$ \$\p' + \$\p' \) $= \phi^{T}(\phi\phi^{T} + \lambda I)$ If we faster of from the right, we get, $= (\phi^T \phi + \lambda I) \phi^T$ fince me started from the same expression, me get, $\phi^{T}(\phi\phi^{T}+\lambda I) = (\phi^{T}\phi+\lambda I)\phi^{T}$ sultiplying (pp+ xt) on the night and (ptp+ xt) or the left to go (ptp+11) (pt+11) (pp+11) (pp+11) = (中でサナンナ)(中でサンガエ)ゆで(カヤナンエ)

d) If $\phi(x)$ is defined as in Problem 1, then $(k1_{i,j} = (x_i^{-T}x_j^{-} + 1)^2$ (14" / 1 = Pr V V V 1 (1000)

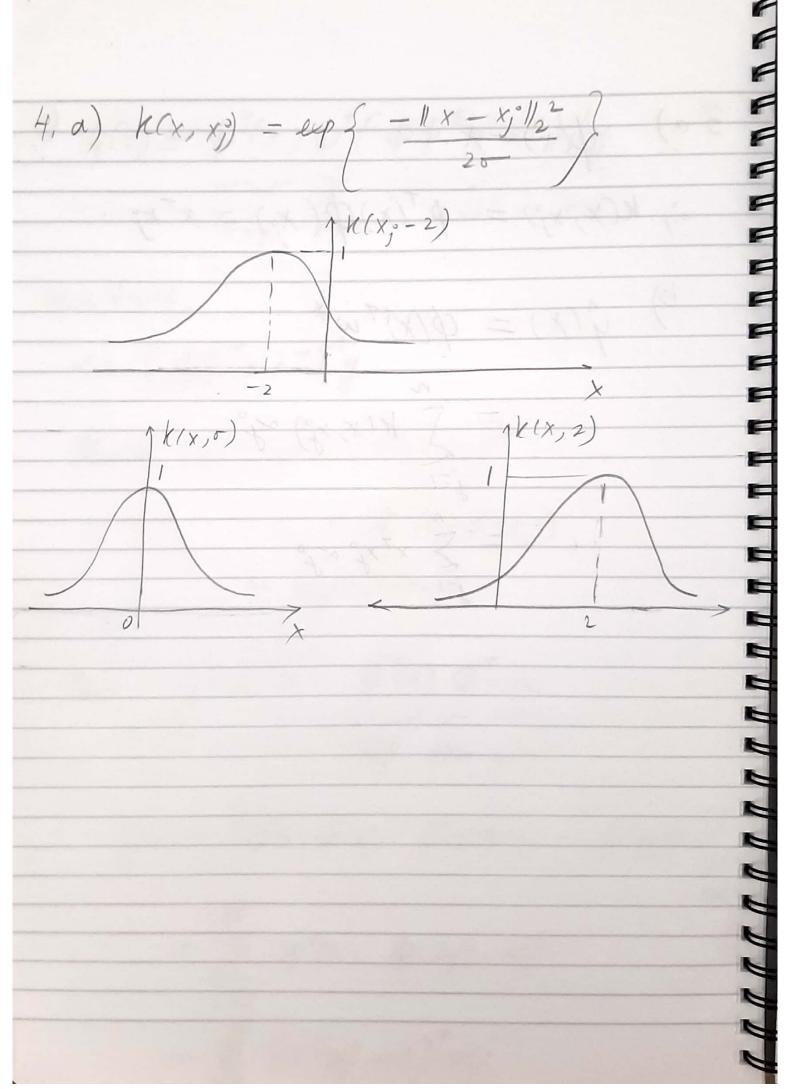
9 $\hat{y}(x) = \phi^T(x) \phi^T(\phi \phi^T + \lambda I)^{-1} y$ XP PXN DXN the have, Now, K(x,xj) = (xTxj+1)2 $= \phi^{T}(x)\phi(x^{2})$ by definition. Thus $\hat{y}(x) = \phi^T(x) \phi^T \propto$ $\int_{\mathbb{R}^n} p(x) dx dx dx dx dx dx dx$ $g(x) = \left[\phi^{T}(x) \phi(x_{1}) \quad \phi^{T}(x) \phi(x_{2}) \dots \quad \phi^{T}(x_{n}) \phi(x_{n})\right].$ $= \sum_{i=1}^{N} \phi^{T}(x), \phi(x_{j}), \omega_{j}^{*}$ $= \sum_{i=1}^{N} (X^{T}X_{i}^{o} + 1)^{2} \propto_{j}^{o}$

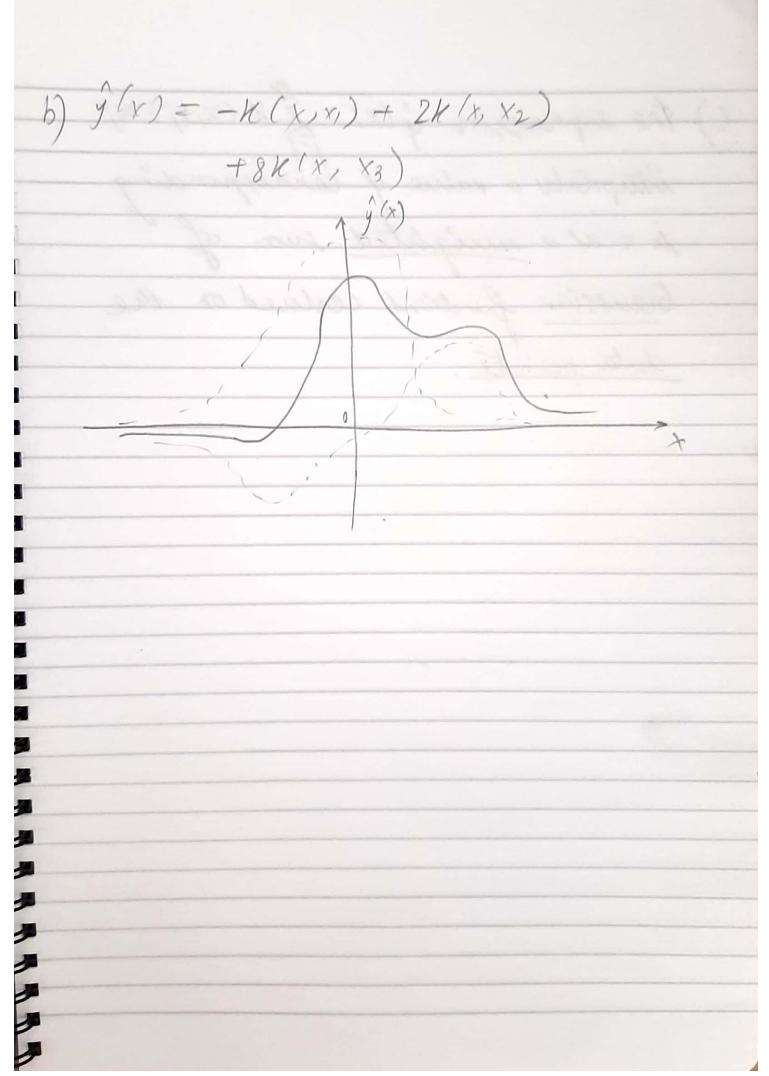
3 a)
$$\phi(x) = x$$

$$\vdots, k(x, x_j^2) = \phi^T(x)\phi(x_j) = x^Tx_j^2$$
b)
$$y(x) = \phi(x)^T \omega^*$$

$$= \sum_{j=1}^n k(x, x_j^2) \omega_j^2$$

$$\vdots = \sum_{j=1}^n x^Tx_j^2 \omega_j^2$$





The expression if (x) = EK (X, x,°) x,° interpolates a value y correspor weighted sur