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**Particle Swarm Optimization (PSO)**

**Abstract:**

This project will introduce the particle swarm optimization (PSO) algorithm as a stochastic algorithm used for solving optimization problems. So as to officially introduce the scientific detailing of PSO algorithm, the classical inertial version of PSO will be used, meanwhile PSO variants will be summarized. Before looking into implementation, this project will introduce important concepts and functions of PSO. Based on this knowledge, mathematical model of PSO algorithm will be formulated. Other than this, the theoretical analysis and experimental analysis will be discussed. Two study cases of optimizing functions, one of ‘Sphere’ and another is ‘Rastrigrn function’, are provided for implementation of PSO algorithm. This is to show how handful and versatile is to work with PSO.

**Introduction:**

Particle swarm optimization (PSO) is one of the rare tools which is amusingly easy to code and implement to produce bizarrely good results. This algorithm was proposed by Eberhart and Kennedy in 1995. It is a population based stochastic, something randomly determined, algorithm which is used to solve a numerical optimization problems like predicting score of a football team using a math equation. According to this algorithm, basically, goal is to minimize error terms (difference between actual answer and predicted answer). Such goal categorizes PSO as metaheuristic approach which means that a higher level procedure is used to find optimal solution for any optimization problem with imperfect data or limited computation capacity.

PSO, a unique computational method, is inspired from social behaviors of nature. By social behavior we mean, the collective behaviors of simple individuals interacting with their environment and each other like social foraging behaviors of birds’ flocking, schooling of fishes etc. Hence, it is also classified as swarm intelligence algorithm like other bacterial foraging algorithm, ant colony algorithm etc.

**Important concepts and functions of PSO:**

**Mathematical model od PSO:**

For every particle two vectors are considered, the velocity vector and the position vector. The position vector shows the position of a particle in certain landscape and the other, velocity vector shows the intensity and direction of movement of that particle. There are two equations mentioned below, which make up back bone of PSO. Note that the “k” in equations denotes the current iteration, therefore “k+1″ implies the next iteration.

Position of individual particles updated as follows:

With the velocity calculated as follows:

Where,

|  |  |
| --- | --- |
|  | Particle position |
|  | Particle velocity |
|  | Best individual particle position |
|  | Best swarm position |
|  | Constant inertial weight |
|  | Cognitive and social parameters |
|  | Random numbers between 0 and 1 |

And,

* is the inertial component
* is the cognitive component.
* is the cognitive component.

The first equation for position of particle tells that the next day’s position of individual particle is calculated by summing today’s position of particle and its velocity for the next day. Then, in order to calculate particle’s velocity for next day, the inertial component, the cognitive component and the social component are summed up in second equation. In this equation,  gives distance to the personal best and gives distance to the global best. The cognitive component helps particles in exploring the search space and the social component helps particles in exploiting the search space. Note that velocity in current day is used to calculate the velocity for next day and this is how it helps in deducing the position for next day.

**Impact of variants:**

Analysis of inertia weight selection:

The inertial parameter of PSO tunes the exploitation and exploration of particles and also shows the influence of previous velocity on the current velocity. If w = 0, the velocity of particle depends on its personal best and global best. On the other hand, if w ≠ 0, then the particle has the tendency of exploring new space. The larger the inertia weight, the greater the velocity and exploration rate will be. Similarly the smaller the inertial weight, smaller will be the velocity and particle will tend to perform local exploitation.

Analysis of selection of cognitive and social parameters:

These parameters are also known as accelerating constants and are responsible to represent stochastic acceleration of particle towards its personal best point and the global best point. From the equation above we can infer that if c1 = c2 = 0, then particle will fly with constant velocity till the border. This makes difficult for particle to approach optimum point because then the particle only have ability to search in definite local space.

Similarly if only c1 = 0, particle losses its cognitive ability and depends on its social component, decision made by whole swarm so far. This increases convergent rate of particles and exploitation is done at highest level. In contrast to this, the particle loses its social component when c2 = 0. This means that every particle search in its local space and do not exchange information with one another. In this case, the exploitation is done at its lowest level and exploration is done at its highest level.

With all of this, we can conclude that, higher value of the cognitive parameter results in excessive exploitation in local search space of individuals. On the other hand, relatively higher value of social parameter provides tendency to particle to rush prematurely towards the optimum point.

**References:**

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