#### Joint Taxation of Income and Wealth

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#### **Examples:**

- Abgeltungssteuer in Germany
- Cap on wealth tax liability as a proportion of income

There were 12 European countries who levied wealth taxes in 1990. 7 of them imposed some kind of cap on wealth tax liability.

Is this (in)efficient?

## This project

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- 2. A structural model to understand cross-effects. (Work in progress)
  - Pro Jointness: Wealth and income are positively correlated. This should
    - lower distortions
    - allow for more targeted redistribution
  - Contra Jointness: Jointness implies two distortions.
    - E.g. increasing wealth tax only for people with income > \$100k not only distorts wealth margin but also income margin

#### Reduced-form model

#### We consider

- A joint distribution of income and wealth, F(y, a)
  - Independent if  $F(y, a) = F_Y(y) \cdot F_A(a)$
- A bivariate tax payment function, T(y, a)
  - Marginal income tax rate:  $\frac{\partial T(y,a)}{\partial y} = T'_Y(y,a)$
  - Marginal wealth tax rate:  $\frac{\partial T(y,a)}{\partial a} = T'_A(y,a)$
  - Separable if  $\frac{\partial^2 T(y,a)}{\partial y \partial a} = 0 \implies T(y,a) = T_Y(y) + T_A(a)$

## Model analysis

- Tax perturbation approach
  - Change in tax liability  $\Delta T(y, a)$
- Rely on sufficient statistics
  - Elasticity of income,  $\varepsilon_{\gamma,1-T_{\nu}'}$
  - Elasticity of wealth,  $\varepsilon_{a,1-T_A'}$
  - Extension to cross-elasticities work in progress, main mechanisms very similar

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We look at the revenue and welfare effects of ...

- separable income and wealth tax reforms
- joint tax reforms

## Separable income tax reform

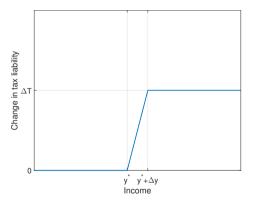


Figure: Simple income tax reform

## Separable income tax reform

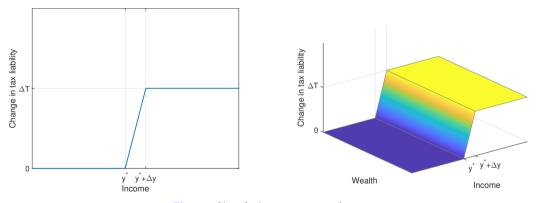


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## Marginal excess burden – separable tax reforms

- Marginal excess burden for increasing  $T'_{\nu}(y^*)$ 

$$MEB_{Y}(y^{*}) = \frac{T'_{Y}(y^{*})}{1 - T'_{Y}(y^{*})} \varepsilon_{y^{*}, 1 - T'_{Y}} \frac{f_{Y}(y^{*})y^{*}}{1 - F_{Y}(y^{*})}$$

- The term  $\frac{f_Y(y^*)y^*}{1-F_Y(y^*)}$  plays a key role. (Saez, 2001)
- Similar analysis for  $T_A'(a^*)$ . (Saez and Stantcheva, 2018)

## Joint reform

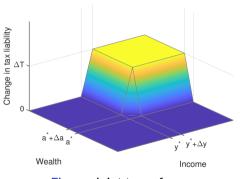


Figure: Joint tax reform

- Increases tax payment for people with  $y > y^*$  and  $a > a^*$ .

## Effects of a joint reform

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- 1. Increase in tax revenue
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- 3. Distortion on wealth accumulation

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 $\mbox{Marginal excess burden} = \frac{\mbox{Distortion on income} + \mbox{Distortion on wealth}}{\mbox{Increased tax revenue}}$ 

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## Marginal excess burden I

#### **Proposition 1**

If the initial tax schedule is separable, it can be shown that

$$\begin{aligned} \textit{MEB}_{joint}(\textit{y}^*,\textit{a}^*) &= \textit{w}_{\textit{Y}}(\textit{y}^*,\textit{a}^*) \cdot \textit{MEB}_{\textit{Y}}(\textit{y}^*) \cdot \frac{\varepsilon_{\textit{y},1-\textit{T}_{\textit{Y}}^{\prime}}|\textit{a}>\textit{a}^*}{\varepsilon_{\textit{y},1-\textit{T}_{\textit{Y}}^{\prime}}} \\ &+ \textit{w}_{\textit{A}}(\textit{y}^*,\textit{a}^*) \cdot \textit{MEB}_{\textit{A}}(\textit{a}^*) \cdot \frac{\varepsilon_{\textit{a},1-\textit{T}_{\textit{A}}^{\prime}}|\textit{y}>\textit{y}^*}{\overline{\varepsilon_{\textit{a},1-\textit{T}_{\textit{A}}^{\prime}}}} \end{aligned}$$

where  $w_Y(y, a)$  and  $w_A(y, a)$  are the weights that depend on the joint distribution of income and wealth. They are given by

$$w_{Y}(y^{*}, a^{*}) = \frac{Pr(a > a^{*}|y = y^{*})}{Pr(a > a^{*}|y > y^{*})} \qquad w_{A}(y^{*}, a^{*}) = \frac{Pr(y > y^{*}|a = a^{*})}{Pr(y > y^{*}|a > a^{*})}$$

## **Graphical intuition**

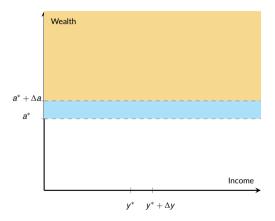


Figure: Graphical intuition of Proposition 1

$$w_A(y^*, a^*) = \frac{Pr(y > y^* | a = a^*)}{Pr(y > y^* | a > a^*)}$$

## **Graphical intuition**

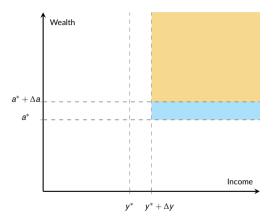


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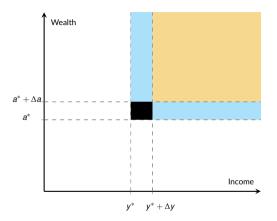


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## Marginal excess burden II

#### **Proposition 2**

If income and wealth are independently distributed, elasticites are cross-independent, and the initial tax schedule is separable, then the marginal excess burden of a joint reform is given by

$$\textit{MEB}_{\mbox{joint}}(\textit{y}^*, \textit{a}^*) = \textit{MEB}_{\mbox{\scriptsize Y}}(\textit{y}^*) + \textit{MEB}_{\mbox{\scriptsize A}}(\textit{a}^*)$$



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- The sum of the weights is above two for a negative correlation.
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- For the empirically plausible case of positive correlation
  - $\rightarrow$  sum of weights is between 1 and 2
- Let's look at some data!

#### Data

#### **Survey of Consumer Finances**

- Representative household survey
- Data from 2016
- 5000+ households

#### Variable definitions:

- Income
  - Wages, salaries and self-employment income
- Wealth
  - Assets (financial and non-financial) net of liabilities

#### Data

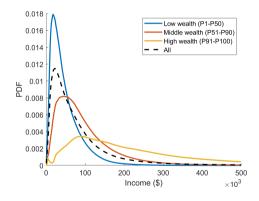
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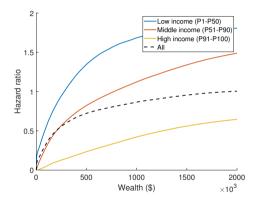
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## Non-parametric estimation of the joint distribution Data fit



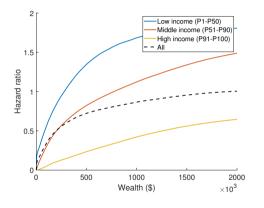
High correlation between income and wealth.

#### Conditional hazard rates



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Tagging!

## Assumptions on elasticities & current taxes

- Elasticities
  - $\varepsilon_{y,1-T_Y'}=0.3$
  - $\varepsilon_{a,1-T'_{A}} = 10$  (Jakobsen et al., 2020)
- Taxes: we assume separable tax
  - Income tax schedule is estimated using TAXSIM calculator. Then polynomial fit for marginal labor income tax rate. 

    Estimation
  - For wealth tax: assume that it is currently  $1\% \leftrightarrow 5\%$  capital return and 20% capital income tax rate.

## MEB of joint reforms

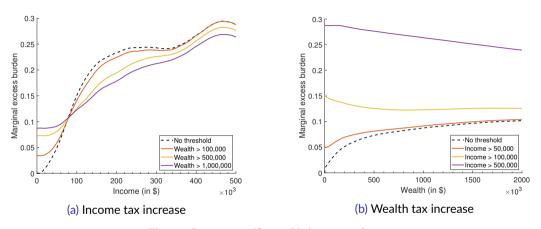


Figure: Revenue effect of joint tax reforms

## **Takeaways**

- Excess burden of increasing high income taxes is lower if conditional on high wealth
- Excess burden of wealth tax is higher if conditional on high income
- Main reason: Distortions on the wealth margin very low in the benchmark

▶ Alternative calibration

## Welfare analysis

- So far we only talked about distortions but **distributional gains** also change.

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Assume that the initial, separable tax schedules are optimal.

- 1. Estimate welfare weights for income and wealth. (Inverse-optimum approach)
- 2. Combine two separate welfare weights to obtain a joint welfare weight.

▶ Welfare weights

## Welfare effects of joint reforms

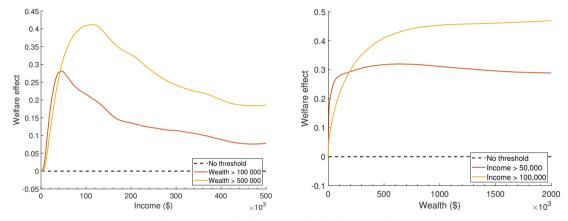


Figure: Marginal effects of a joint tax reform



#### Conclusion

- Joint reforms introduce another front of distortion.
- This needs to be traded off against the welfare gain of tagging.
- Future work:
  - More careful calibration
  - Distinguishing different concepts of wealth
  - Structural model approach

# Any questions?

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## **Proof of Proposition 1**

$$\begin{split} \textit{MEB}_{1} &= y^{*} \varepsilon_{y} \frac{\int\limits_{a^{*}}^{\infty} \frac{T_{1}(y^{*}, a)}{1 - T_{1}(y^{*}, a)} f(y^{*}, a) \, da}{\int\limits_{y^{*}}^{\infty} \int\limits_{a^{*}}^{\infty} f(y, a) \, da \, dy} + a^{*} \varepsilon_{a} \frac{\int\limits_{y^{*}}^{\infty} \frac{T_{2}(y, a^{*})}{1 - T_{2}(y, a^{*})} f(y, a^{*}) \, dy}{\int\limits_{y^{*}}^{\infty} \int\limits_{a^{*}}^{\infty} f(y, a) \, da \, dy} \\ \textit{MEB}_{1} &= y^{*} \varepsilon_{y} \frac{\tau_{y}}{1 - \tau_{y}} \frac{f_{Y}(y^{*}) \int\limits_{a^{*}}^{\infty} f_{A}(a) \, da}{\int\limits_{y^{*}}^{\infty} f_{Y}(y) \int\limits_{a^{*}}^{\infty} f_{A}(a) \, da \, dy} + a^{*} \varepsilon_{a} \frac{\tau_{a}}{1 - \tau_{a}} \frac{f_{A}(a^{*}) \int\limits_{y^{*}}^{\infty} f_{Y}(y) \, dy}{\int\limits_{a^{*}}^{\infty} f_{Y}(y) \int\limits_{a^{*}}^{\infty} f_{A}(a) \, da \, dy} \\ \textit{MEB}_{1} &= y^{*} \varepsilon_{y} \frac{\tau_{y}}{1 - \tau_{y}} \frac{f_{Y}(y^{*})(1 - F_{A}(a^{*}))}{(1 - F_{Y}(y^{*}))(1 - F_{A}(a^{*}))} + a^{*} \varepsilon_{a} \frac{\tau_{a}}{1 - \tau_{a}} \frac{f_{A}(a^{*})(1 - F_{Y}(y^{*}))}{(1 - F_{Y}(y^{*}))(1 - F_{A}(a^{*}))} \\ \textit{MEB}_{1} &= \textit{MEB}_{Y} + \textit{MEB}_{A} \end{split}$$



## **Estimation Fit**

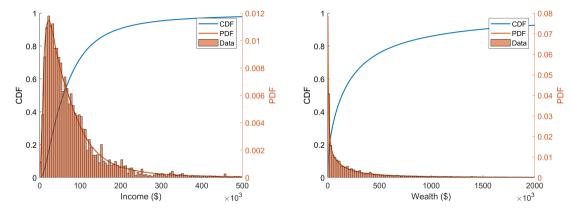


Figure: Estimation fit



## **Income Tax Rate Estimation**

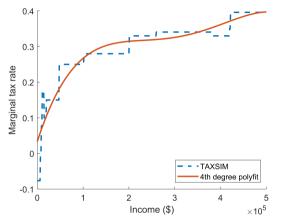


Figure: Polynomial fit for marginal income tax rate



## MEB of joint reforms

#### Alternative calibration

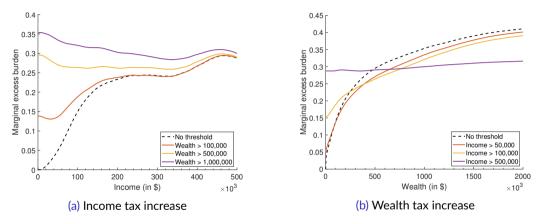


Figure: Revenue effect of joint tax reforms (Alternative calibration)



## Welfare Weights for Income and Wealth

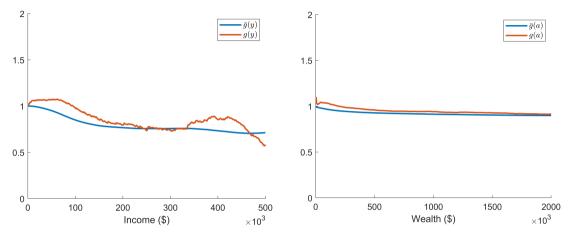


Figure: Welfare weights



## Welfare effects of joint reforms

#### **Alternative Calibration**

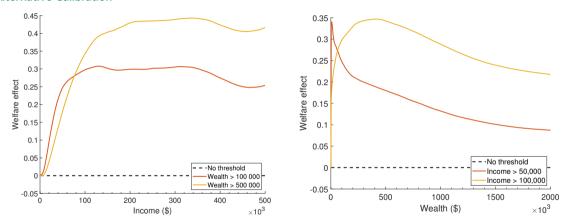


Figure: Marginal effects of a joint tax reform (Alternative)



#### Income Tax Reform

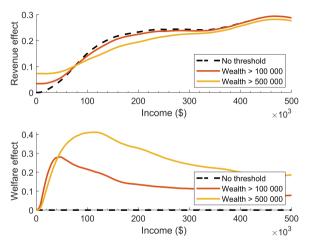


Figure: Income tax reform conditional on wealth



## Wealth Tax Reform

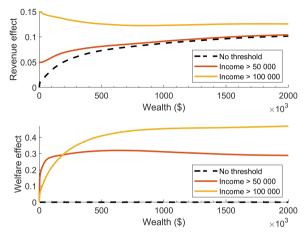


Figure: Wealth tax reform conditional on income

