

Date of Issue: 15.02.2016
Deadline: 29.02.2016, (at 17:00 and must be submitted to Assistant Prof. Dr. Yaprak Yalçın)

KON 326E
COMPUTER CONTROLLED SYSTEMS
PROJECT – 1

1. In continuous systems *Laplace transform* plays a unique role. That transform allows system and circuit designers to analyze systems and predict performance, and to think in different terms to help understand linear continuous systems. *z-transform* plays the role in sampled systems that *Laplace transform* plays in continuous systems.

Prepare a report for *z-transform* that includes:

- Definition
 - Properties (with proofs)
 - The role of z-transform to solve difference equations (with examples).
2. Determine the inverse *z-transform* of the following discrete time system with using the *Inverse Transform Integral (Contour Integral with using Residue Theorem)*.

$$X(z) = \frac{20}{(z-1)(z-2)}$$

3. Assuming that:

$$u(k) = 1 \quad k = 0, 1, 2, \dots$$

solve the difference equation:

$$x(k+2) - x(k+1) + 0.25x(k) = u(k+2)$$

with the initial conditions $x(0) = 1$ and $x(1) = 2$.

- a) Analytically
b) Numerically (Hint: You can use MATLAB for calculations.)

4. Continuous time transfer function of a system is given as follows:

$$X(s) = \frac{3s+9}{(s+1)(s+2)}$$

determine the discrete time transfer function of the system.

5. Analytically obtain the *z-transform* of the following equation.

$$X(s) = \frac{1 - e^{-Ts}}{s} \frac{2}{(s+a)^2}$$

Yaprak YALÇIN