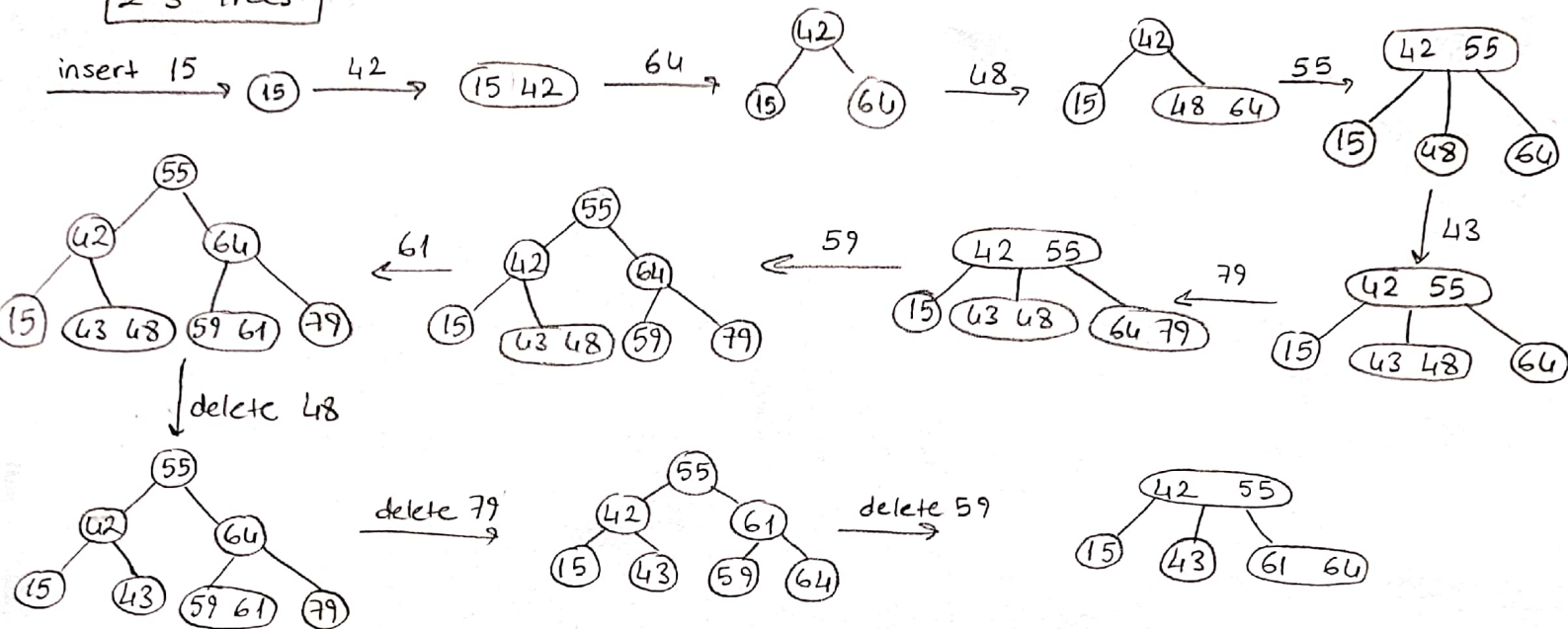
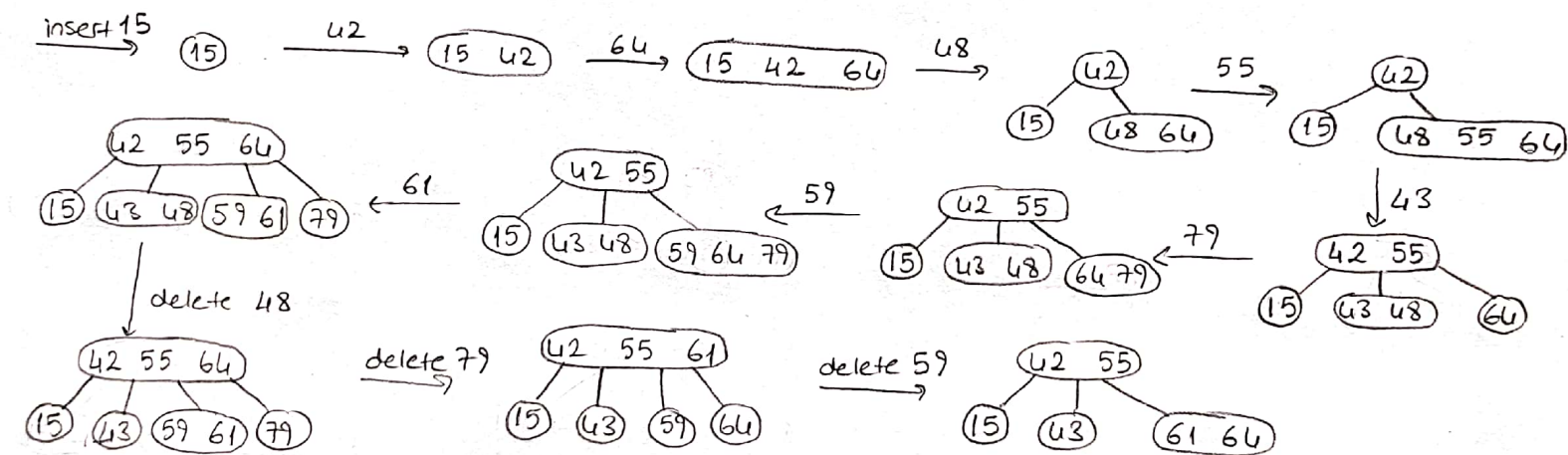


Question 1:

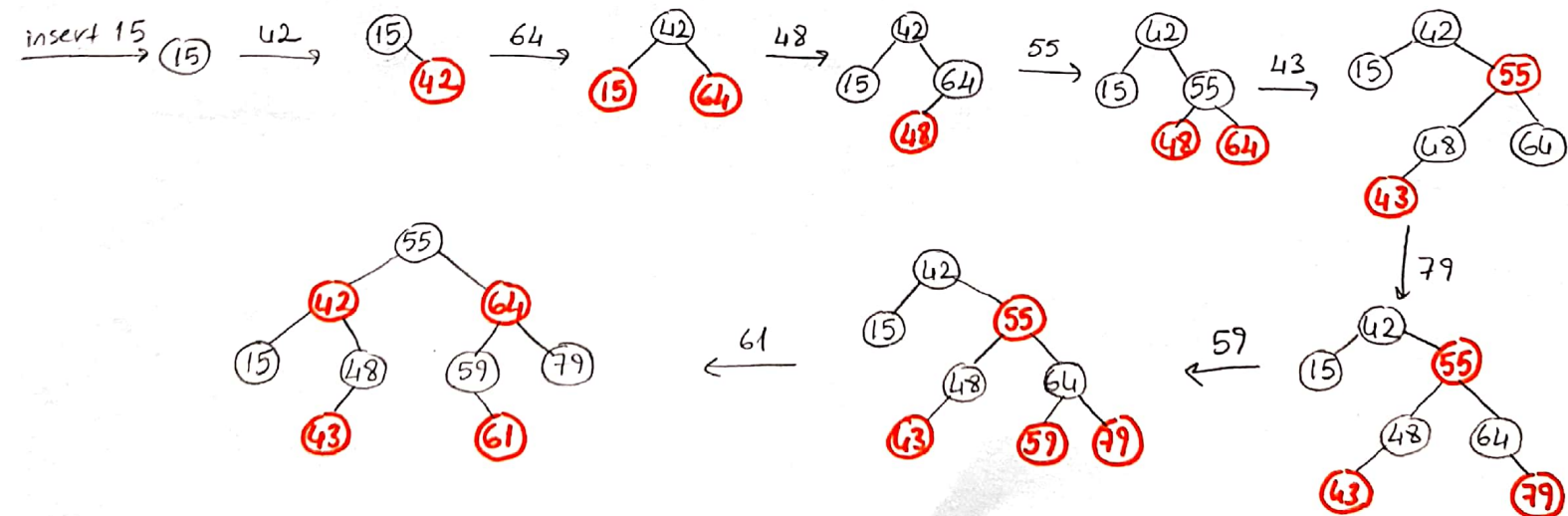
2-3 Trees



2-3-4 Trees



Red-black Trees



Question 2: Table size = 17

Open addressing with linear probing

$$\begin{aligned}
 22 \bmod 17 &= 5 \\
 23 \bmod 17 &= 6 \\
 26 \bmod 17 &= 7 \\
 39 \bmod 17 &= \cancel{5} \cancel{6} \cancel{7} 8 \\
 40 \bmod 17 &= \cancel{6} \cancel{7} \cancel{8} 9 \\
 26 \bmod 17 &= \cancel{9} 10 \\
 41 \bmod 17 &= \cancel{7} \cancel{8} \cancel{9} \cancel{10} 11 \\
 43 \bmod 17 &= \cancel{9} \cancel{10} \cancel{11} 12 \\
 26 \bmod 17 &= \cancel{9} \cancel{10} \cancel{11} \cancel{12} 13
 \end{aligned}$$

0	
1	
2	
3	
4	
5	22
6	23
7	24
8	39
9	40
10	26
11	41
12	43
13	26
14	
15	
16	

Open addressing with quadratic probing

$$\begin{aligned}
 22 \bmod 17 &= 5 \\
 23 \bmod 17 &= 6 \\
 26 \bmod 17 &= 7 \\
 39 \bmod 17 &= \cancel{5} \Rightarrow 5+1^2 = \cancel{6} \Rightarrow 5+2^2 = 9 \\
 40 \bmod 17 &= \cancel{6} \Rightarrow 6+1^2 = \cancel{7} \Rightarrow 6+2^2 = 10 \\
 26 \bmod 17 &= \cancel{9} \Rightarrow 9+1^2 = \cancel{10} \Rightarrow 9+2^2 = 13 \\
 41 \bmod 17 &= \cancel{7} \Rightarrow 7+1^2 = 8 \\
 43 \bmod 17 &= \cancel{9} \Rightarrow 9+1^2 = \cancel{10} \Rightarrow 9+2^2 = 13 \Rightarrow 9+3^2 = 18 \\
 &\quad \Rightarrow 18 \bmod 17 = 1 \\
 26 \bmod 17 &= \cancel{9} \Rightarrow 9+1^2 = \cancel{10} \Rightarrow 9+2^2 = \cancel{13} = 9+3^2 = \cancel{18} \\
 &\quad \Rightarrow 9+4^2 = 25 \\
 &\quad \Rightarrow 25 \bmod 17 = 8 \\
 &\quad \Rightarrow 9+5^2 = 34
 \end{aligned}$$

0	26
1	43
2	
3	
4	
5	22
6	23
7	24
8	41
9	39
10	40
11	
12	
13	26
14	
15	
16	

Separate Chaining

$$\begin{aligned}
 22 \bmod 17 &= 5 \\
 23 \bmod 17 &= 6 \\
 26 \bmod 17 &= 7 \\
 39 \bmod 17 &= 5 \\
 40 \bmod 17 &= 6 \\
 26 \bmod 17 &= 7 \\
 41 \bmod 17 &= 7 \\
 43 \bmod 17 &= 9 \\
 26 \bmod 17 &= 9
 \end{aligned}$$

