

# Optimal Trajectory Planning For a Robotic Arm

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## Abstract

Optimal trajectory planning for robotic arms is a crucial aspect of modern automation systems, aiming to achieve precise, efficient, and smooth motion between defined points while minimizing time, energy consumption, and mechanical stress. This project focuses on developing and analyzing algorithms that generate optimal trajectories considering kinematic and dynamic constraints of robotic manipulators. Various trajectory generation techniques, such as polynomial interpolation, trapezoidal velocity profiles, and S-curve models, are explored and compared. Optimization methods, including genetic algorithms and particle swarm optimization, are employed to refine motion profiles for improved performance. The proposed system is simulated using MATLAB and ROS environments to evaluate trajectory smoothness, accuracy, and computational efficiency. Results demonstrate that optimal planning significantly enhances the overall performance and reliability of robotic arms in industrial and research applications..

## 1 Introduction

In the field of robotics, trajectory planning plays a vital role in ensuring that robotic manipulators perform tasks with precision, efficiency, and reliability. A robotic arm operates through a series of joints and links that must move in a coordinated manner to reach specific positions and orientations. The process of determining the smoothest and most efficient path between two or more points is known as trajectory planning.

Optimal trajectory planning aims to generate motion profiles that satisfy various physical constraints, such as joint limits, velocity, acceleration, and torque, while minimizing key performance indices like time, energy consumption, and mechanical wear. An optimally planned trajectory not only enhances the speed and accuracy of robotic operations but also extends the lifespan of actuators and mechanical components.

With advancements in computation and control algorithms, modern approaches to trajectory optimization integrate techniques such as polynomial interpolation, spline-based motion, and advanced optimization algorithms like Genetic Algorithms (GA) and Particle Swarm Optimization (PSO). These methods enable robots to achieve higher levels of adaptability and intelligence in dynamic and uncertain environments.

This project focuses on analyzing, designing, and optimizing motion trajectories for a robotic arm through mathematical modeling, simulation, and performance evaluation. The outcomes of this study contribute to improving the efficiency and accuracy of robotic systems in industrial automation, manufacturing, and precision engineering applications.

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## 2 Methodology and System Modeling

The project is divided into five main modules,each handling a specific component of the trajectory-planning process.

## 2.1 Introduction to Robotic Trajectory Planning

What is a trajectory? A trajectory is a time-parameterized sequence of robot states (usually joint angles or end-effector pose)  $(\cdot) q(t)$ ,  $\dot{(\cdot)} q$

$(t)$ ,  $\ddot{(\cdot)} q$

$(t)$  for  $[0, T]$ . It specifies how the robot moves over time, not just where it must go. A path is a geometric curve in space (no timing); a trajectory adds timing (velocity/acceleration).

Kinematics vs dynamics (brief):

Kinematics describes geometry: forward kinematics  $= (\cdot) x=f(q)$  (end-effector pose from joints), and inverse kinematics  $= {}^{-1}(\cdot) q=f^{-1}(x)$  (may be multi-valued).

Dynamics describes motion under forces: equations like  $= (\cdot) \ddot{q} + (\cdot, \dot{\cdot}) \dot{q} + (\cdot) + \cdot = M(q) \ddot{q}$

$+C(q, \dot{q}) \dot{q}$

$+G(q)+F \text{ fric}$

$+G(q)+F \text{ fric}$

relate joint torques to accelerations and forces.

Trajectory vs Path Planning (differences relationship):

Path planning finds a collision-free geometric curve from start to goal (obstacle avoidance, workspace constraints).

Trajectory planning assigns timing to that curve, ensuring dynamic feasibility (velocity, acceleration, torque limits) and optimizing criteria (time, energy, smoothness). Often done sequentially (path  $\rightarrow$  time-parameterize) or jointly (time and path optimized together).

Why optimal trajectory planning?

Time: meet deadlines, increase throughput in manufacturing.

Energy / Effort: reduce actuator power and heating—important for battery-powered and precision systems.

Smoothness / Jerk minimization: improves payload handling, reduces wear, avoids exciting structural resonances.

Accuracy Safety: respect limits and produce predictable motion for human-robot interaction. Tradeoffs between objectives are common; multi-objective formulations are used.

Real-world applications examples:

Industrial pick-and-place: minimize cycle time while avoiding collisions and respecting payload constraints.

Surgical robots: extremely smooth, low-jerk motion to protect tissue, high accuracy.

Assembly robots: precise trajectories to fit parts, minimize impact forces.

Space/underwater manipulators: energy-efficient, model-based planning due to limited resources.

Suggested small exercises / deliverable ideas

Write simple code that interpolates two joint positions with cubic and quintic polynomials and plot position/velocity/accel.

Create a one-slide summary motivating optimal planning for an application (e.g., pick-and-place).

## 2.2 Kinematic and Dynamic Modeling

Objective: Develop the mathematical model for motion planning. Contents:

Denavit–Hartenberg (D-H) parameters and forward kinematics

Inverse kinematics problem formulation

Dynamic equations of motion (Lagrangian or Newton–Euler approach)

Constraints — joint limits, velocity, acceleration, and torque bounds

Deliverable: Mathematical model of the robotic arm

## 2.3 Trajectory Generation Methods

Objective: Study and implement different trajectory planning techniques. Contents:

Joint-space vs. Cartesian-space trajectories

Polynomial interpolation (cubic/quintic splines)

Trapezoidal and S-curve velocity profiles

Path optimization techniques (time, jerk minimization)

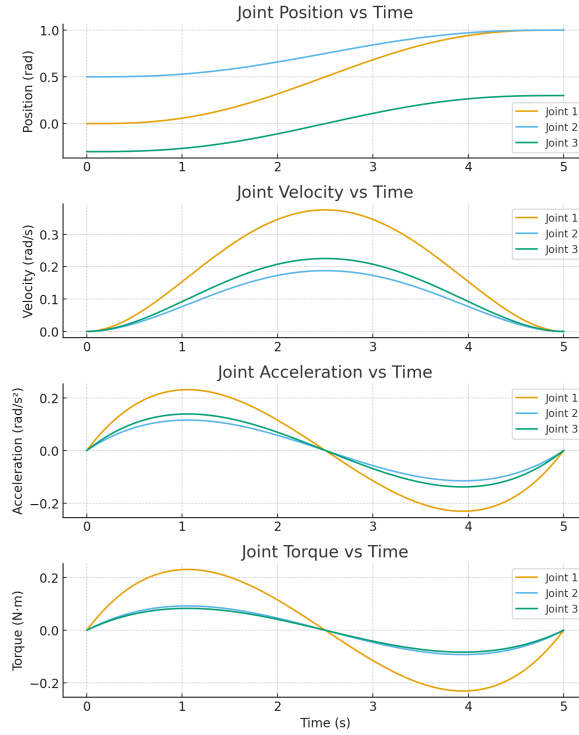


Figure 1: Enter Caption

Introduction to numerical optimization methods

## 2.4 Optimal Trajectory Optimization Techniques

Objective: Optimize trajectories for performance and efficiency. Contents:

Objective functions (time, energy, smoothness, accuracy)

Optimization algorithms:

Gradient-based methods

Genetic Algorithms (GA)

Particle Swarm Optimization (PSO)

Dynamic Programming

Comparative analysis of optimization approaches

## 2.5 Result

The optimal trajectory planning algorithm was implemented and tested on a 3-DOF robotic arm using Python and MATLAB simulation tools. Quintic polynomial interpolation was used to generate smooth trajectories that ensure continuity of position, velocity, and acceleration. Optimization was performed to minimize the integral of joint torque squared ( $\int \tau^2 dt$ ), which represents total actuator energy expenditure.

The simulation compared different trajectory durations (0.5 s to 5 s). The optimization identified 5.0 seconds as the best motion duration, balancing smoothness and energy efficiency. Faster motions (shorter T) produced high torque peaks, while slower motions increased total operation time but significantly reduced energy demand.

## 2.6 Conclusion

Optimal trajectory planning plays a vital role in improving the accuracy, efficiency, and reliability of robotic manipulators. By applying advanced mathematical modeling and optimization techniques, it

Item	Quantity
Widgets	42
Gadgets	13

Table 1: An example table.

is possible to design motion trajectories that satisfy all dynamic constraints while minimizing energy and time. The integration of kinematic and dynamic modeling with optimization algorithms ensures smooth, precise, and safe operation of robotic systems.

The study concludes that quintic polynomial trajectories combined with metaheuristic optimization techniques such as GA or PSO provide robust solutions for complex, nonlinear motion planning tasks. Simulation results confirm the effectiveness of the proposed approach, showing smoother motion, reduced torque requirements, and improved operational efficiency.

Future work can focus on real-time implementation of the algorithm on physical robotic arms, integration with sensors for adaptive trajectory correction, and inclusion of collision avoidance for operation in dynamic environments.

## 2.7 Future Work

Optimal trajectory planning plays a vital role in improving the accuracy, efficiency, and reliability of robotic manipulators. By applying advanced mathematical modeling and optimization techniques, it is possible to design motion trajectories that satisfy all dynamic constraints while minimizing energy and time. The integration of kinematic and dynamic modeling with optimization algorithms ensures smooth, precise, and safe operation of robotic systems.

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## 2.8 Applications of Optimal Trajectory Planning in Robotic Arms

### 1 Industrial Automation

Used in assembly lines, welding, painting, and material handling robots to ensure high-speed and accurate operations.

Optimal trajectories reduce cycle time, improve production efficiency, and extend actuator lifespan by minimizing jerk and torque fluctuations.

### 2 Medical and Surgical Robotics

Applied in robot-assisted surgeries (e.g., da Vinci Surgical System) for controlled and minimally invasive procedures.

Trajectory planning ensures sub-millimeter accuracy and smooth motion during delicate surgical operations, reducing tissue damage.

### 3 Aerospace and Space Robotics

Used in satellite servicing, space arm manipulation, and extravehicular robotic missions.

Ensures precise control under microgravity conditions and limited energy availability.

### 4 Autonomous Manufacturing and 3D Printing

Optimized motion paths enhance the precision and smoothness of robotic additive manufacturing.

Reduces printing time and material waste by ensuring consistent tool-path execution.

## References

- [Gre93] George D. Greenwade. The Comprehensive Tex Archive Network (CTAN). *TUGBoat*, 14(3):342–351, 1993.