

1. Calculate the following summation with user input  $n$ , and plot  $S$  versus  $k$  graph.

$$S = \sum_{k=0}^n \frac{1}{k^2 + 1}$$

2. A function that classifies a flow according to the values of its Reynolds (Re) and Mach (Ma) numbers, such that if  $\text{Re} < 2000$ , the flow is laminar; if  $2000 < \text{Re} < 5000$ , the flow is transitional; if  $\text{Re} > 5000$ , the flow is turbulent; if  $\text{Ma} < 1$ , the flow is sub-sonic, if  $\text{Ma} = 1$ , the flow is sonic; and, if  $\text{Ma} > 1$ , the flow is super-sonic. Write an m-file classifying the flow according to its Reynolds and Mach numbers.

3. In one of your calculus classes you probably learned that  $\sin(x)$  can be expanded in a power series,  $\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$ . Compare  $\sin x$  to the first two and first three terms of this expansion for  $x = 0.01, 0.1$  and  $1$ .

4. In what follows, the value  $p_n$  should approach  $\pi$ . Let  $p_2 = 2\sqrt{2}$ , and

$$p_{n+1} = 2^n \sqrt{2 \left( 1 - \sqrt{1 - (p_n / 2^n)^2} \right)}$$

compute  $p_n$  for  $n = 3, 4, \dots, 20$  by the above formula. Plot the absolute error versus  $n$  graph.