

MA678_homework__08

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Getting to know stan

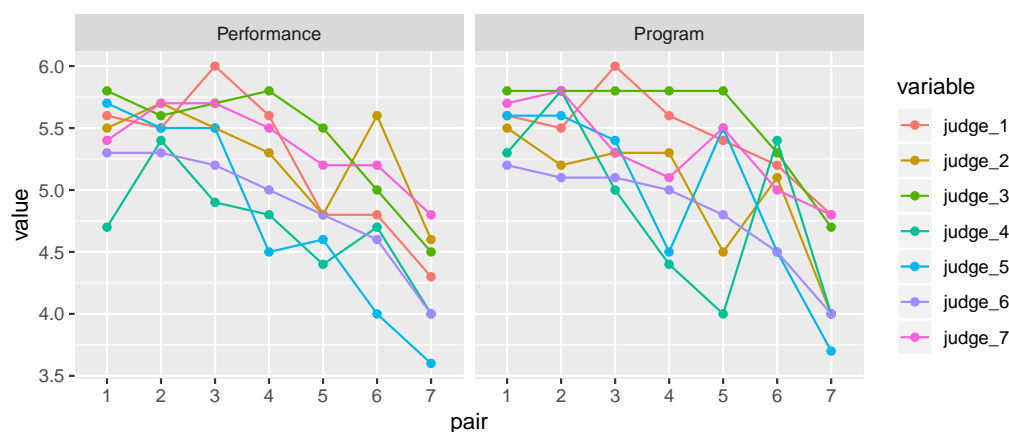
Read through the tutorial on Stan <https://github.com/stan-dev/rstan/wiki/RStan-Getting-Started>

- Explore Stan website and Stan reference manual and try to connect them with Gelman and Hill 16 - 17.

Data analysis

Using stan:

The folder olympics has seven judges' ratings of seven figure skaters (on two criteria: "technical merit" and "artistic impression") from the 1932 Winter Olympics. Take a look at <http://www.stat.columbia.edu/~gelman/arm/examples/olympics/olympics1932.txt>



##	Program	Performance	pair	Judge
## 1:	5.6	5.6	1	judge_1
## 2:	5.5	5.5	1	judge_2
## 3:	5.8	5.8	1	judge_3
## 4:	5.3	4.7	1	judge_4
## 5:	5.6	5.7	1	judge_5
## 6:	5.2	5.3	1	judge_6

use stan to fit a non-nested multilevel model (varying across skaters and judges) for the technical merit ratings.

$$y_i \sim N(\mu + \gamma_{j[i]} + \delta_{k[i]}, \sigma_y^2), \text{ for } i = 1, \dots, n \quad (1)$$

$$\gamma_j \sim N(0, \sigma_\gamma^2) j = 1, \dots, 7 \quad (2)$$

$$\delta_k \sim N(0, \sigma_\delta^2) k = 1, \dots, 7 \quad (3)$$

https://github.com/stan-dev/example-models/blob/master/ARM/Ch.17/17.3_flight_simulator.stan https://github.com/stan-dev/example-models/blob/master/ARM/Ch.17/17.3_non-nested_models.R

```

fit_program<-lmer(Program~1+(1|pair) + (1|Judge),olympics_long)

dataList.1 <- list(N=49, n_judges=7, n_pairs=7, judge=as.integer(olympics_long$Judge), pair=as.integer

skating_stan<-"
data {
  int<lower=0> N;
  int<lower=0> n_judges;
  int<lower=0> n_pairs;
  int<lower=0,upper=n_judges> judge[N];
  int<lower=0,upper=n_pairs> pair[N];
  vector[N] y;
}
parameters {
  real<lower=0> sigma;
  real<lower=0> sigma_gamma;
  real<lower=0> sigma_delta;
  vector[n_judges] gamma;
  vector[n_pairs] delta;
  real mu;
}
model {
  vector[N] y_hat;

  sigma ~ uniform(0, 100);
  sigma_gamma ~ uniform(0, 100);
  sigma_delta ~ uniform(0, 100);

  mu ~ normal(0, 100);

  gamma ~ normal(0, sigma_gamma);
  delta ~ normal(0, sigma_delta);

  for (i in 1:N)
    y_hat[i] = mu + gamma[judge[i]] + delta[pair[i]];
  y ~ normal(y_hat, sigma);
}
"

```

```

pilots <- read.table ("http://www.stat.columbia.edu/~gelman/arm/examples/pilots/pilots.dat",
header=TRUE)

```

```

flight_simulator.sfl <- stan( model_code=skating_stan , data=dataList.1, iter=2000, chains=4)

```

Multilevel logistic regression

The folder **speed.dating** contains data from an experiment on a few hundred students that randomly assigned each participant to 10 short dates with participants of the opposite sex (Fisman et al., 2006). For each date, each person recorded several subjective numerical ratings of the other person (attractiveness, compatibility, and some other characteristics) and also wrote down whether he or she would like to meet the other person again. Label $y_{ij} = 1$ if person i is interested in seeing person j again 0 otherwise. And r_{ij1}, \dots, r_{ij6} as person i 's numerical ratings of person j on the dimensions of attractiveness, compatibility, and so forth. Please look at <http://www.stat.columbia.edu/~gelman/arm/examples/speed.dating/Speed%20Dating%20Data%20Key.doc> for details.

```

dating<-fread("http://www.stat.columbia.edu/~gelman/arm/examples/speed.dating/Speed%20Dating%20Data.csv")
dating_pooled <- glm(match~attr_o +sinc_o +intel_o +fun_o +amb_o +shar_o,data=dating,family=binomial)
dating_pooled <- glmer(match~gender + attr_o +sinc_o +intel_o +fun_o +amb_o +shar_o+(1|iid)+(1|pid),data=dating,family=binomial)

## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge with max|grad| = 0.67667 (tol
## = 0.001, component 1)

```

1. Fit a classical logistic regression predicting $Pr(y_{ij} = 1)$ given person i 's 6 ratings of person j . Discuss the importance of attractiveness, compatibility, and so forth in this predictive model.

```

glm1 <- glm(match~attr_o +sinc_o +intel_o +fun_o +amb_o +shar_o,data=dating,family=binomial)
summary(glm1)

```

```

##
## Call:
## glm(formula = match ~ attr_o + sinc_o + intel_o + fun_o + amb_o +
##      shar_o, family = binomial, data = dating)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.5300  -0.6362  -0.4420  -0.2381   3.1808
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -5.62091    0.21859 -25.714 < 2e-16 ***
## attr_o       0.22047    0.02388   9.233 < 2e-16 ***
## sinc_o      -0.01996    0.03067  -0.651  0.5152
## intel_o      0.07176    0.03716   1.931  0.0535 .
## fun_o        0.25315    0.02922   8.665 < 2e-16 ***
## amb_o       -0.12099    0.02838  -4.264 2.01e-05 ***
## shar_o       0.21225    0.02209   9.608 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 6466.6  on 7030  degrees of freedom
## Residual deviance: 5611.0  on 7024  degrees of freedom
## (1347 observations deleted due to missingness)
## AIC: 5625
##
## Number of Fisher Scoring iterations: 5

```

$$\text{logodds}(\text{match} = 1) = -5.6 + 0.22\text{attr} - 0.02\text{sinc} + 0.07\text{intel} + 0.25\text{fun} - 0.12\text{amb} + 0.21\text{shar}$$

One unit increase in **attractiveness** will lead to 5.5% ($\frac{0.22}{4}$) increased willingness to have another date.

One unit increase in **sincerity** will lead to 0.5% ($\frac{-0.02}{4}$) decreased willingness to have another date.

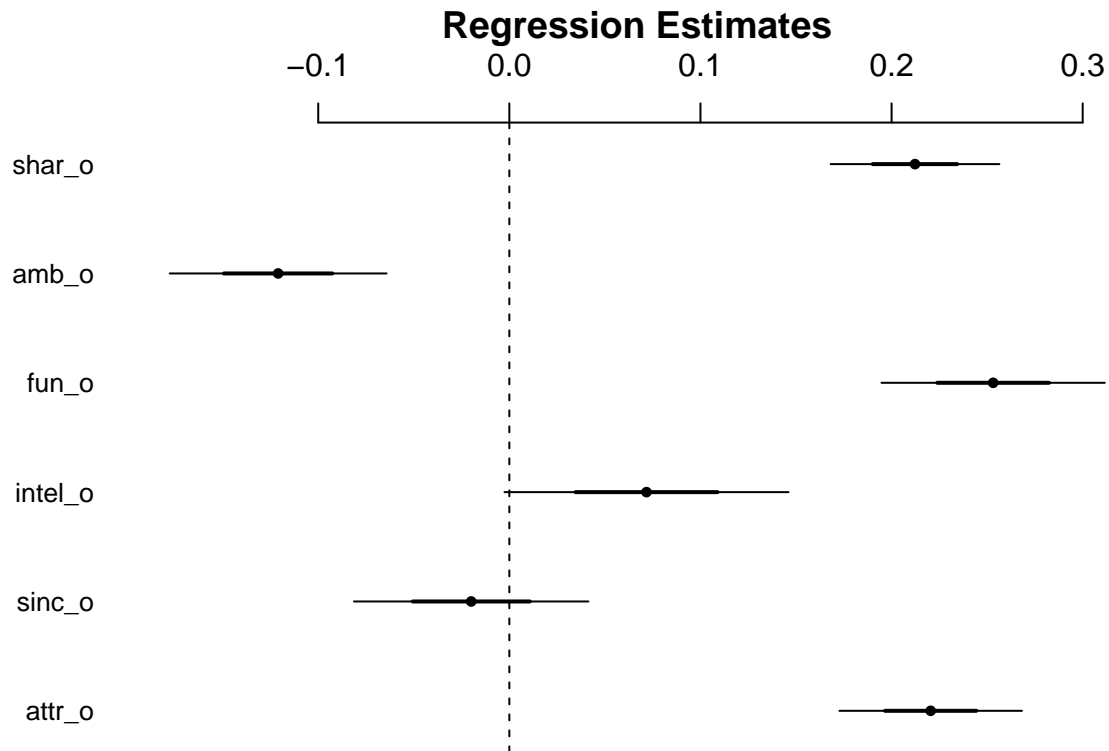
One unit increase in **intelligence** will lead to 1.75% ($\frac{-0.07}{4}$) increased willingness to have another date.

One unit increase in **humor** will lead to 6.25% ($\frac{-0.25}{4}$) increased willingness to have another date.

One unit increase in **ambition** will lead to 3% ($\frac{-0.12}{4}$) decreased willingness to have another date.

One unit increase in **shared interest** will lead to 5.25% ($\frac{0.21}{4}$) increased willingness to have another date.

```
coefplot(glm1)
```



From the coefficient plot we can see that only sincerity is not statistically significant influential to the odds of switching to another data.

2. Expand this model to allow varying intercepts for the persons making the evaluation; that is, some people are more likely than others to want to meet someone again. Discuss the fitted model.

```
glm2 <- glmer(match~gender+scale(attr_o) +scale(sinc_o) +scale(intel_o) +scale(fun_o) +scale(amb_o) +scale(shar_o) + (1|id), data=dating, family=binomial)
```

```
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge: degenerate Hessian with 5
## negative eigenvalues
```

```
summary(glm2)
```

```
## Warning in vcov.merMod(object, use.hessian = use.hessian): variance-covariance matrix computed from Hessian is
## not positive definite or contains NA values: falling back to var-cov estimated from RX
## Warning in vcov.merMod(object, correlation = correlation, sigma = sigma): variance-covariance matrix computed from Hessian is
## not positive definite or contains NA values: falling back to var-cov estimated from RX
## Generalized linear mixed model fit by maximum likelihood (Laplace
## Approximation) [glmerMod]
## Family: binomial ( logit )
## Formula:
## match ~ gender + scale(attr_o) + scale(sinc_o) + scale(intel_o) +
##       scale(fun_o) + scale(amb_o) + scale(shar_o) + (1 | id)
## Data: dating
```

```

##
##      AIC      BIC    logLik deviance df.resid
##    5543.2    5605.0   -2762.6    5525.2     7022
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -1.7458 -0.4453 -0.2877 -0.1454  10.3764
##
## Random effects:
##   Groups Name      Variance Std.Dev.
##   iid      (Intercept) 0.4294   0.6553
## Number of obs: 7031, groups: iid, 551
##
## Fixed effects:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -2.13226    0.07079  -30.122 < 2e-16 ***
## gender         0.15452    0.09322   1.658  0.0974 .
## scale(attr_o)  0.46047    0.05203   8.850 < 2e-16 ***
## scale(sinc_o) -0.02474    0.05728  -0.432  0.6658
## scale(intel_o) 0.10874    0.06203   1.753  0.0796 .
## scale(fun_o)   0.51341    0.06192   8.291 < 2e-16 ***
## scale(amb_o)  -0.23570    0.05468  -4.311 1.63e-05 ***
## scale(shar_o)  0.48474    0.05045   9.609 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) gender scl(t_) scl(sn_) scl(n_) scl(f_) scl(m_)
## gender       -0.672
## scale(ttr_)  -0.202  0.109
## scale(snc_)  -0.022  0.048 -0.123
## scale(ntl_)   0.026 -0.055 -0.039 -0.466
## scale(fun_)  -0.156  0.015 -0.246 -0.150 -0.132
## scale(amb_)   0.143 -0.092 -0.062 -0.014 -0.370 -0.187
## scale(shr_)  -0.135  0.009 -0.100 -0.054 -0.005 -0.268 -0.203
## convergence code: 0
## unable to evaluate scaled gradient
## Model failed to converge: degenerate Hessian with 5 negative eigenvalues
#head(coef(glm2))

```

Fixed effect:

$\text{Logodds}(\text{match} = 1) = -2.13 + 0.15\text{gender} + 0.46\text{scale}(\text{attr}) - 0.02\text{scale}(\text{sinc}) + 0.11\text{scale}(\text{intel}) + 0.51\text{scale}(\text{fun}) - 0.23\text{scale}(\text{amb}) + 0.48\text{scale}(\text{shar}) + \text{iid}_i$

A **male** dating partner, comparing with a female dating partner, will be $4\% \frac{0.16}{4}$ more likely to have another date.

One unit increase in **attractiveness** will lead to $11.5\% (\frac{0.46}{4})$ increased willingness to have another date.

One unit increase in **sincerity** will lead to $0.5\% (\frac{-0.02}{4})$ decreased willingness to have another date.

One unit increase in **intelligence** will lead to $2.75\% (\frac{0.11}{4})$ increased willingness to have another date.

One unit increase in **humor** will lead to $12.75\% (\frac{0.51}{4})$ increased willingness to have another date.

One unit increase in **ambition** will lead to 5.75% ($\frac{-0.23}{4}$) decreased willingness to have another date.

One unit increase in **shared interest** will lead to 12% ($\frac{0.48}{4}$) increased willingness to have another date.

Random effect:

Person 1:

$$\text{Logodds}(\text{match} = 1) = -1.64 + 0.15\text{gender} + 0.46\text{scale}(\text{attr}) - 0.02\text{scale}(\text{sinc}) + 0.11\text{scale}(\text{intel}) + 0.51\text{scale}(\text{fun}) - 0.23\text{scale}(\text{amb}) + 0.48\text{scale}(\text{shar}) + \text{iid}_i$$

Person 2:

$$\text{Logodds}(\text{match} = 1) = -2.31 + 0.15\text{gender} + 0.46\text{scale}(\text{attr}) - 0.02\text{scale}(\text{sinc}) + 0.11\text{scale}(\text{intel}) + 0.51\text{scale}(\text{fun}) - 0.23\text{scale}(\text{amb}) + 0.48\text{scale}(\text{shar}) + \text{iid}_i$$

Person 3:

$$\text{Logodds}(\text{match} = 1) = -2.59 + 0.15\text{gender} + 0.46\text{scale}(\text{attr}) - 0.02\text{scale}(\text{sinc}) + 0.11\text{scale}(\text{intel}) + 0.51\text{scale}(\text{fun}) - 0.23\text{scale}(\text{amb}) + 0.48\text{scale}(\text{shar}) + \text{iid}_i$$

Person 4:

$$\text{Logodds}(\text{match} = 1) = -2.24 + 0.15\text{gender} + 0.46\text{scale}(\text{attr}) - 0.02\text{scale}(\text{sinc}) + 0.11\text{scale}(\text{intel}) + 0.51\text{scale}(\text{fun}) - 0.23\text{scale}(\text{amb}) + 0.48\text{scale}(\text{shar}) + \text{iid}_i$$

3. Expand further to allow varying intercepts for the persons being rated. Discuss the fitted model.

```
glm3 <- glmer(match~gender+scale(attr_o) +scale(sinc_o) +scale(intel_o) +scale(fun_o) +scale(amb_o) +scale(shar_o) + (1|pid), data=dating, family=binomial)
```

```
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge with max|grad| = 0.263517
## (tol = 0.001, component 1)
```

```
summary(glm3)
```

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
## Approximation) [glmerMod]
## Family: binomial ( logit )
## Formula:
## match ~ gender + scale(attr_o) + scale(sinc_o) + scale(intel_o) +
## scale(fun_o) + scale(amb_o) + scale(shar_o) + (1 | iid) +
## (1 | pid)
## Data: dating
##
##      AIC      BIC   logLik deviance df.resid
## 5257.6   5326.1  -2618.8   5237.6     7021
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.7847 -0.3824 -0.2194 -0.0917  9.1546
##
## Random effects:
## Groups Name          Variance Std.Dev.
## iid    (Intercept) 0.595     0.7713
## pid    (Intercept) 1.262     1.1235
## Number of obs: 7031, groups: iid, 551; pid, 537
##
## Fixed effects:
##              Estimate Std. Error z value Pr(>|z|)
```

```
## (Intercept)    -2.53475    0.11733 -21.604 < 2e-16 ***
## gender         0.16773    0.14956   1.121  0.2621
## scale(attr_o)  0.63906    0.06376  10.023 < 2e-16 ***
## scale(sinc_o)  0.03499    0.06786   0.516  0.6061
## scale(intel_o) 0.17125    0.07360   2.327  0.0200 *
## scale(fun_o)   0.57661    0.07099   8.122 4.59e-16 ***
## scale(amb_o)  -0.16544    0.06466  -2.559  0.0105 *
## scale(shar_o)  0.58881    0.06158   9.561 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##          (Intr) gender scl(t_) scl(sn_) scl(n_) scl(f_) scl(m_)
## gender      -0.646
## scale(ttr_) -0.221  0.092
## scale(snc_) -0.049  0.036 -0.064
## scale(ntl_) -0.009 -0.044 -0.024 -0.438
## scale(fun_) -0.139  0.008 -0.220 -0.123 -0.098
## scale(amb_)  0.072 -0.070 -0.051  0.011 -0.334 -0.167
## scale(shr_) -0.138  0.004 -0.072 -0.057 -0.020 -0.234 -0.158
## convergence code: 0
## Model failed to converge with max|grad| = 0.263517 (tol = 0.001, component 1)
```

```
#coef(glm3)
```

4. You will now fit some models that allow the coefficients for attractiveness, compatibility, and the other attributes to vary by person. Fit a no-pooling model: for each person i , fit a logistic regression to the data y_{ij} for the 10 persons j whom he or she rated, using as predictors the 6 ratings r_{ij1}, \dots, r_{ij6} . (Hint: with 10 data points and 6 predictors, this model is difficult to fit. You will need to simplify it in some way to get reasonable fits.)

```
glm4 <- glm(match~attr_o + sinc_o + intel_o + fun_o + amb_o + shar_o + factor(iid)-1, data=dating)
#summary(glm4)
```

5. Fit a multilevel model, allowing the intercept and the coefficients for the 6 ratings to vary by the rater i .

```
glm5 <- glmer(match~(1+attr_o+sinc_o+intel_o+fun_o+amb_o+shar_o|iid) + attr_o + sinc_o + intel_o + fun_o
```

```
## Warning in optwrap(optimizer, devfun, start, rho$lower, control =
## control, : convergence code 1 from bobyqa: bobyqa -- maximum number of
## function evaluations exceeded
## Warning in (function (fn, par, lower = rep.int(-Inf, n), upper =
## rep.int(Inf, : failure to converge in 10000 evaluations
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge: degenerate Hessian with 1
## negative eigenvalues
```

```
#summary(glm5)
```

6. Compare the inferences from the multilevel model in (5) to the no-pooling model in (4) and the complete-pooling model from part (1) of the previous exercise.

```
anova(glm5, glm1, glm4)
```

```

## Data: dating
## Models:
## glm1: match ~ attr_o + sinc_o + intel_o + fun_o + amb_o + shar_o
## glm5: match ~ (1 + attr_o + sinc_o + intel_o + fun_o + amb_o + shar_o |
## glm5:      iid) + attr_o + sinc_o + intel_o + fun_o + amb_o + shar_o
## glm4: match ~ attr_o + sinc_o + intel_o + fun_o + amb_o + shar_o +
## glm4:      factor(iid) - 1
##      Df      AIC      BIC logLik deviance  Chisq Chi Df Pr(>Chisq)
## glm1   7 5625.0 5673.0 -2805.5  5611.0
## glm5  35 5576.8 5816.8 -2753.4  5506.8  104.23    28 1.034e-10 ***
## glm4 558 5607.8 9434.6 -2245.9  4491.8 1014.93   523 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

AIC for all three model are not very much different. Model 5 is slightly better.