

State Truth Table

| $s_1$ | $s_0$ | $a$ | $b$ | $n_1$ | $n_0$ | $x$ |
|-------|-------|-----|-----|-------|-------|-----|
| 0     | 0     | 0   | 0   | 0     | 0     | 0   |
| 0     | 0     | 0   | 1   | 0     | 0     | 0   |
| 0     | 0     | 1   | 0   | 0     | 1     | 0   |
| 0     | 0     | 1   | 1   | 0     | 0     | 0   |
| 0     | 1     | 0   | 0   | 0     | 0     | 0   |
| 0     | 1     | 0   | 1   | 0     | 0     | 0   |
| 0     | 1     | 1   | 0   | 1     | 1     | 0   |
| 0     | 1     | 1   | 1   | 1     | 0     | 0   |
| 1     | 0     | 0   | 0   | 1     | 0     | 1   |
| 1     | 0     | 0   | 1   | 1     | 1     | 1   |
| 1     | 0     | 1   | 0   | 0     | 0     | 1   |
| 1     | 0     | 1   | 1   | 1     | 0     | 1   |
| 1     | 1     | 0   | 0   | 0     | 0     | 1   |
| 1     | 1     | 0   | 1   | 1     | 1     | 1   |
| 1     | 1     | 1   | 0   | 0     | 0     | 1   |
| 1     | 1     | 1   | 1   | 1     | 1     | 1   |

Boolean Equations

$$n_0 = \bar{s}_1 \cdot \bar{s}_0 \cdot a \cdot \bar{b} + \bar{s}_1 \cdot s_0 \cdot a \cdot \bar{b} + s_1 \cdot \bar{s}_0 \cdot \bar{a} \cdot b + s_1 \cdot s_0 \cdot b \cdot (\underbrace{\bar{a} + a}_1)$$

$$= \bar{s}_1 \cdot \bar{b} (\bar{s}_0 \cdot a + s_0 \cdot a) + s_1 \cdot b (\bar{s}_0 \cdot \bar{a} + s_0)$$

$$n_0 = \bar{s}_1 \cdot b \cdot a + s_1 \cdot b (\bar{s}_0 \cdot \bar{a} + s_0)$$

$$n_1 = \bar{s}_1 \cdot s_0 \cdot a \cdot \bar{b} + \bar{s}_1 \cdot s_0 \cdot a \cdot b + s_1 \cdot \bar{s}_0 \cdot \bar{a} \cdot \bar{b} + s_1 \cdot \bar{s}_0 \cdot \bar{a} \cdot b +$$

$$s_1 \cdot \bar{s}_0 \cdot a \cdot b + s_1 \cdot s_0 \cdot \bar{a} \cdot b + s_1 \cdot s_0 \cdot a \cdot b$$

$$= \bar{s}_1 \cdot s_0 \cdot a (\underbrace{\bar{b} + b}_1) + s_1 \cdot \bar{s}_0 \cdot \bar{a} (b + \bar{b}) + s_1 \cdot \bar{s}_0 \cdot a \cdot b + s_1 \cdot s_0 \cdot b \cdot (\underbrace{\bar{a} + a}_1)$$

$$n_1 = \bar{s}_1 \cdot s_0 \cdot a + s_1 \cdot \bar{s}_0 \cdot \bar{a} + s_1 \cdot \bar{s}_0 \cdot a \cdot b + s_1 \cdot s_0 \cdot b$$

$$x = s_1 \cdot \bar{s}_0 + s_1 \cdot s_0$$

$$= s_1 (\bar{s}_0 + s_0)$$

$$x = s_1$$

$$n_1 = \bar{s}_1 \cdot s_0 \cdot a + s_1 \cdot \bar{s}_0 (\bar{a} + a \cdot b) + s_1 \cdot s_0 \cdot b$$