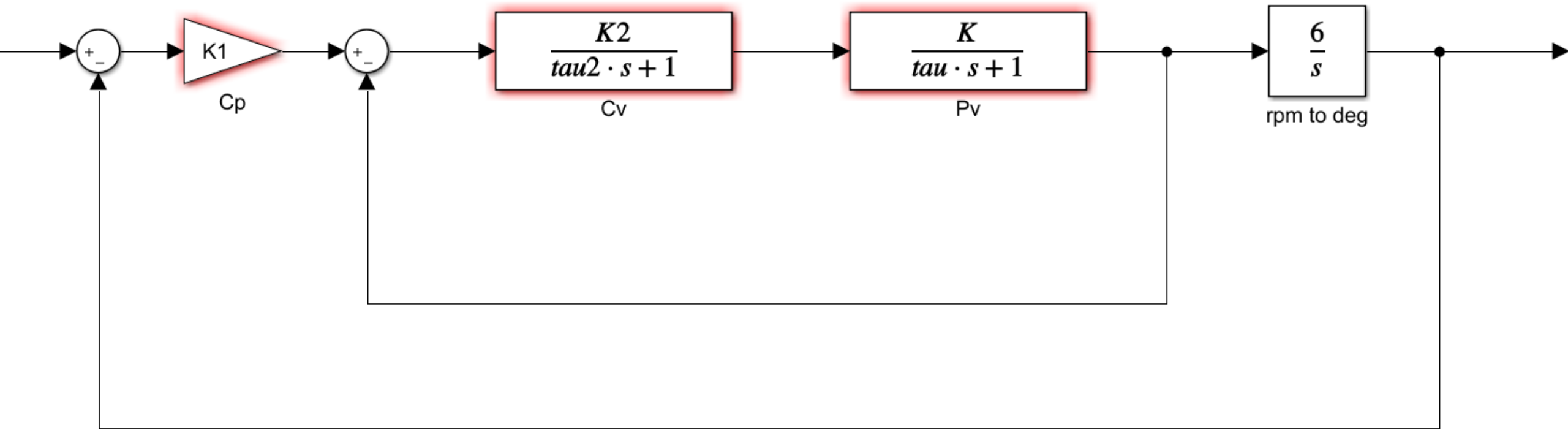


# EEE-342

## Lab-1 Preliminary Work Guide

# Initial Parametrization

- We are dealing with the system below



- Additionally, since we are only interested in transfer function of closed position loop, the position loop controller can be represented as  $C_p(s) = \frac{6K_1}{s}$

# Mathematical Analysis of Closed Position Loop

Definition	Parametrization
<i>Velocity loop controller (<math>C_v(s)</math>)</i>	$C_v(s) = \frac{K_2}{\tau_2 s + 1}$
<i>Velocity loop plant (<math>P_v(s)</math>)</i>	$P_v(s) = \frac{K}{\tau s + 1}$
<i>Position loop plant (<math>P_p(s) = T_v(s)</math>)</i>	$P_p(s) = \frac{P_v(s)C_v(s)}{1 + P_v(s)C_v(s)}$
<i>Position loop controller (<math>C_p(s)</math>)</i>	$C_p(s) = \frac{6K_1}{s}$
<i>Closed position loop (<math>T_p(s)</math>)</i>	$T_p(s) = \frac{P_p(s)C_p(s)}{1 + P_p(s)C_p(s)}$

# Mathematical Analysis of Closed Position Loop

- Instead of using numerical values, use parametric transfer functions to avoid complexity (Using 6 on  $C_p(s)$  does not affect complexity).
- At the end of calculation of  $T_p(s)$ , you will obtain the following form

$$\begin{aligned} T_p(s) &= \frac{d}{as^3 + bs^2 + cs + d} = \left( \frac{\omega_0^2}{s^2 + 2\zeta\omega_0s + \omega_0^2} \right) \times \left( \frac{1}{\tau_x s + 1} \right) \\ &= \frac{\omega_0^2}{\tau_x s^3 + (2\zeta\omega_0\tau_x + 1)s^2 + (\tau_x\omega_0^2 + 2\zeta\omega_0)s + \omega_0^2} \end{aligned}$$

# Mathematical Analysis of Closed Position Loop

- 3 unknowns:  $\tau_x, K, \tau$
- By replacing the parameters  $a, b, c, d$  with proper functions of  $K, K_1, K_2, \tau, \tau_2$  that you found by calculating  $T_p(s)$  from slide-3, you will have 3 equations for 3 unknowns.
- Note that since we are approximating a third order system with some nonlinearities to a second order linear system, it is unrealistic to find a matching response.
- However, there is also a crude approximation  $M_p = 1 - \frac{\zeta}{0.6}$ , which leads to a better matching output. (you can test it to be sure that your solution is correct, however you need to use the exact formula for  $M_p$  and explain why they do not match in your report).

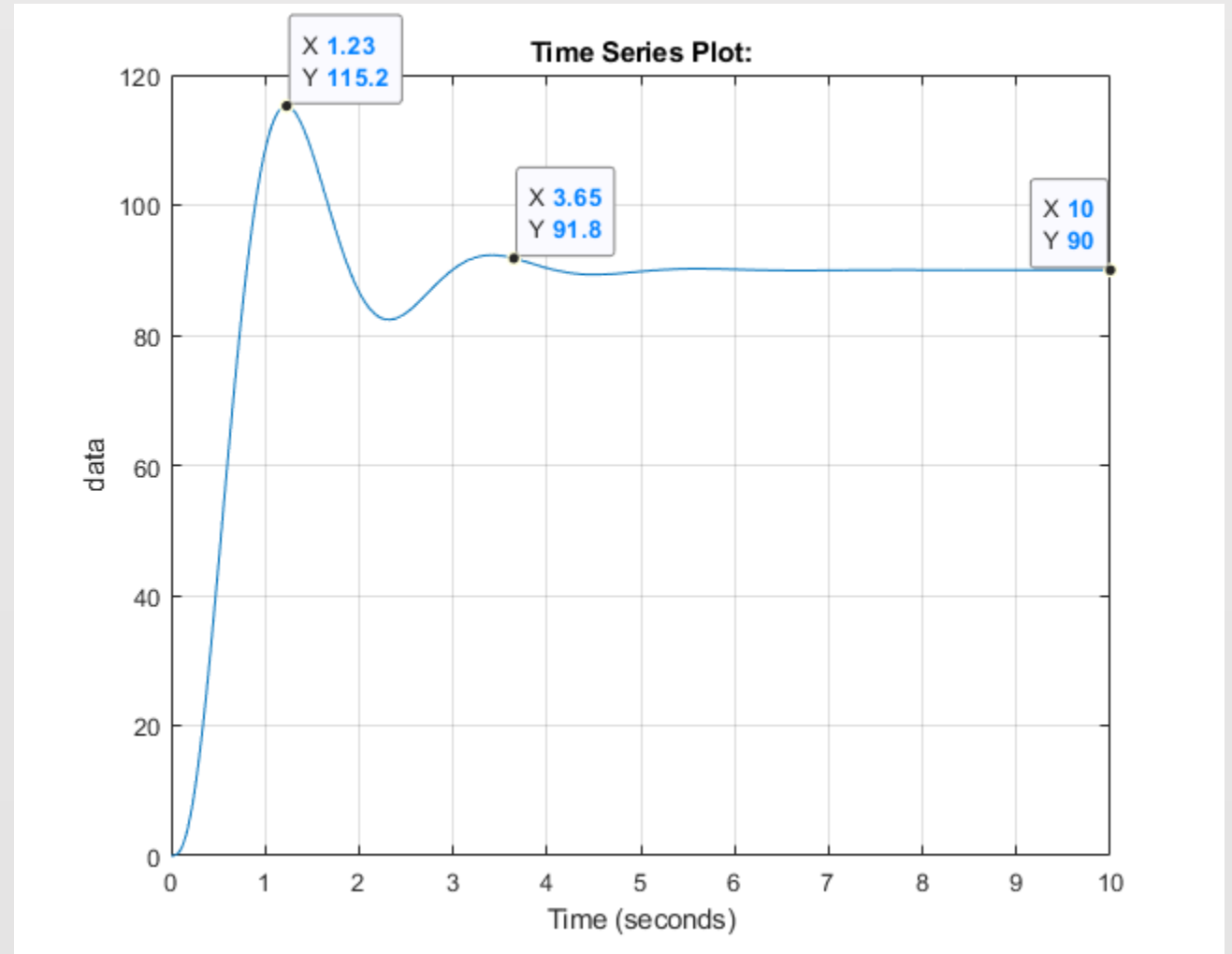
# Estimation of $\omega_0$ and $\zeta$

## Second Order System Response

- $M_p$ : Maximum overshoot
- $T_s$ : Settling time

→ Find the constants above by using data (the figure shows an example for another data).

→ Estimate  $\omega_0$  and  $\zeta$  by using appropriate formulas for second order system



# Estimation of $K$ and $\tau$

- Implement the parametric equations you found in Matlab. Initialize  $K_1, K_2, \tau_2, \omega_0$  and  $\zeta$  with proper values. Use the code to obtain  $K$  and  $\tau$ .
- Therefore, you do not need to do any numerical computation manually.
- Just put the parametric equations and the code you implemented in your reports. Also, show the values of  $K$  and  $\tau$  that are returned from Matlab.

If you have any questions, do not hesitate to send mail to  
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