

### Lab 3 - Margin Analysis of a System

The purpose of this lab is to understand how gain, phase and delay margins can be estimated by using mathematical model, and how these calculations can be verified.

#### **Part-1: Margin Estimation**

In the previous lab, we designed 3 PI controllers with various zero locations. You firstly need to choose the one that provides least settling time for the step response.

1. For this controller ( $G_c(s)$ ) and the final model of the plant ( $G_p(s)$ ) (the one after arithmetic-geometric mean operations), draw the Bode plot.
2. Calculate gain margin and phase margin by using this plot. Also, calculate the delay margin by using phase margin and crossover frequency.

**Check-1** Show your calculations and Bode plot to one of TAs.

**Report** Plot the Bode diagram and show your calculations and estimated margins.

#### **Part-2: Margin Verification**

1. Download `lab3_step_GM.slx` and `lab3_read.slx` from moodle. Configure these files as you did in first lab (you can use manual of first lab). Do not forget to adjust target hardware, baud rate, sampling period etc.
2. Set  $r(t) = 40u(t)$  rpm and your controller ( $G_c(s)$ ), and increase gain ( $K$ ) until the system is unstable (you need to find the gain margin experimentally, therefore you can start with the GM you estimated in part-1, and decrease if it is already unstable or increase if it is not. At the end, you need to find the exact value of  $K_f$  that makes the system unstable, so that the system is stable for  $K < K_f$ ).

**Check-2** Show your calculated GM, observed GM and response of the system for two cases:  $K_1$  is slightly less than  $K_f$ , so that the system is stable, and  $K_2$  is slightly larger than  $K_f$  such that the system is unstable.

3. Download `lab3_step_DM.slx` from moodle. Configure this file as you did in first lab (you can use manual of first lab). Do not forget to adjust target hardware, baud rate, sampling period etc.
4. Set  $r(t) = 40u(t)$  rpm and your controller ( $G_c(s)$ ). The block with the title 'Delay' causes time delay in system. Increase the time delay until the system is unstable to find the delay margin ( $h_f$ ). You can use the same procedure as explained in step-2.

**Check-3** Show your calculated DM, observed DM and response of the system for two cases:  $h_1$  is slightly less than  $h_f$ , so that the system is stable, and  $h_2$  is slightly larger than  $h_f$  such that the system is unstable.

**Report** Compare estimated and calculated margins. Draw the plots you used to get checks. If they are different, explain the reasons.

In your report, you are expected to explain the work done in order. It needs to include all plots you drew, all mathematical equations you did (handwritten results will not be accepted), and all the results you obtained in the lab. You also need to comment on each result you obtained between lab checks. All Matlab code should be included in your reports. Do not forget to use report template and write introduction and conclusion parts.