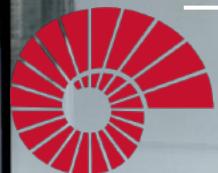


COMP527

COMPUTATIONAL IMAGING

Lecture #02 – Image Formation



KOÇ
UNIVERSITY

Aykut Erdem // Koç University // Spring 2023

Previously on COMP527

- Course info
- History of photography
- Limitations of traditional photography
- Recent accomplishments

image is from our recent work on text-guided image editing.



Today's Lecture

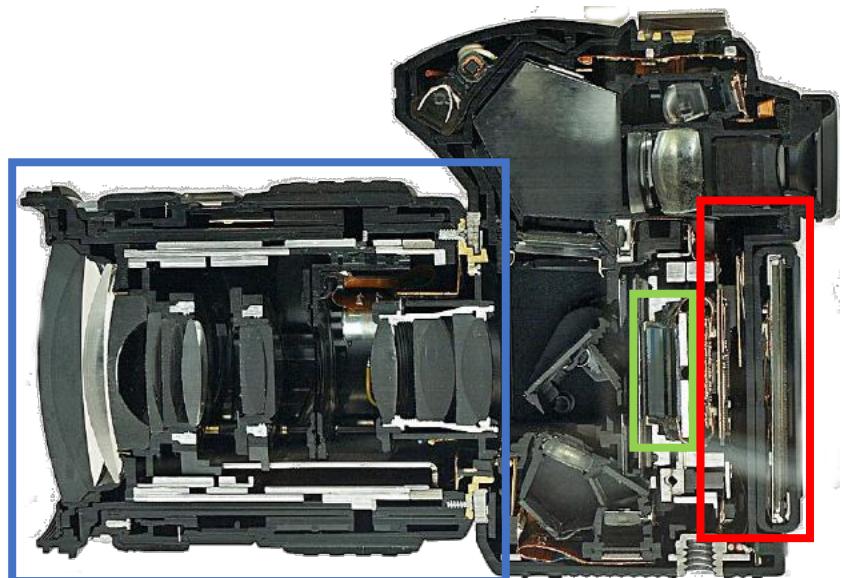
- Pinhole camera
- Basics of geometric optics and lenses
- Field of view
- Magnification and perspective
- Zooming
- Orthographic camera and telecentric lenses

Disclaimer: The material and slides for this lecture were borrowed from
—Ioannis Gkioulekas' 15-463/15-663/15-862 "Computational Photography" class
—Steve Marschner's CS6640 "Computational Photography" class
—David Lindell's CSC2529 "Computational Imaging" class
—Antonio Torralba's MIT 6.869 "Advances in Computer Vision" class

The modern photography pipeline



post-capture processing
(lectures 5-10)



optics and optical controls

sensor, analog front-end, and color filter array

in-camera image processing pipeline

Some motivational imaging experiments

Let's say we have a sensor...



digital sensor
(CCD or CMOS)

... and an object we like to photograph

real-world
object



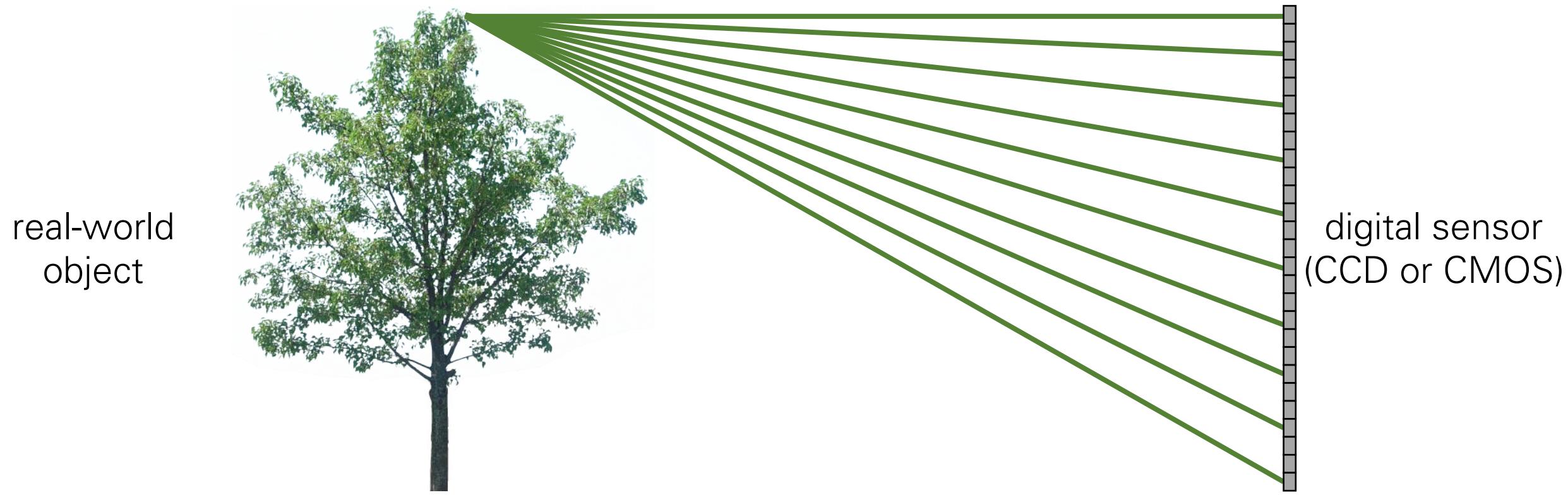
digital sensor
(CCD or CMOS)

What would an image taken like this look like?

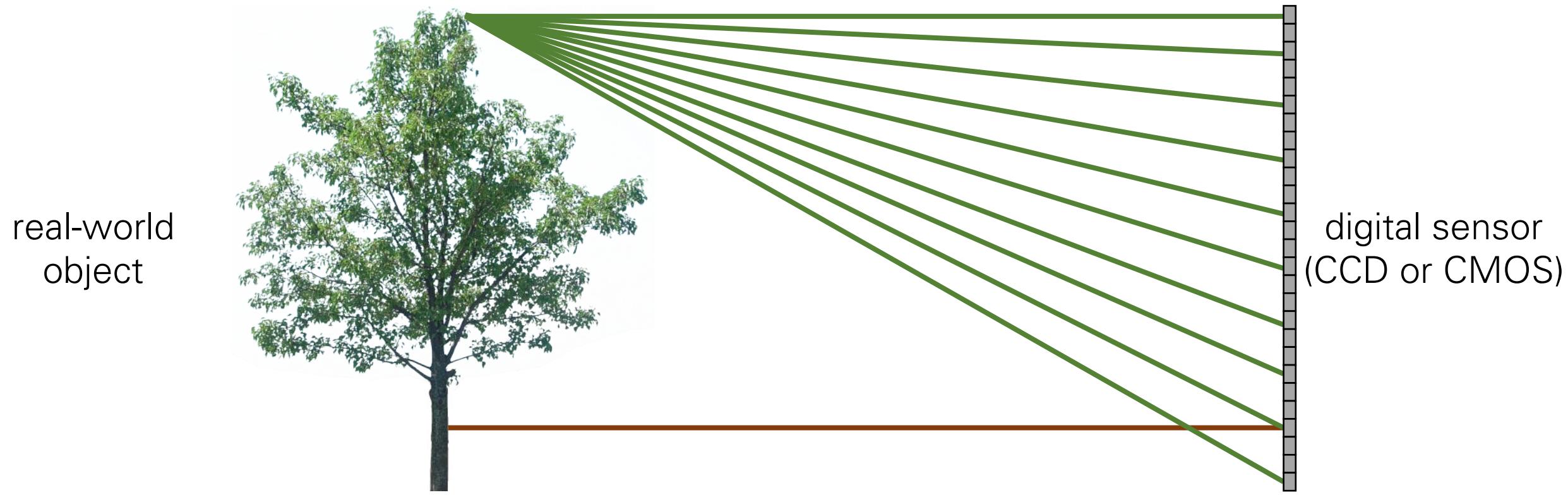
Bare-sensor imaging



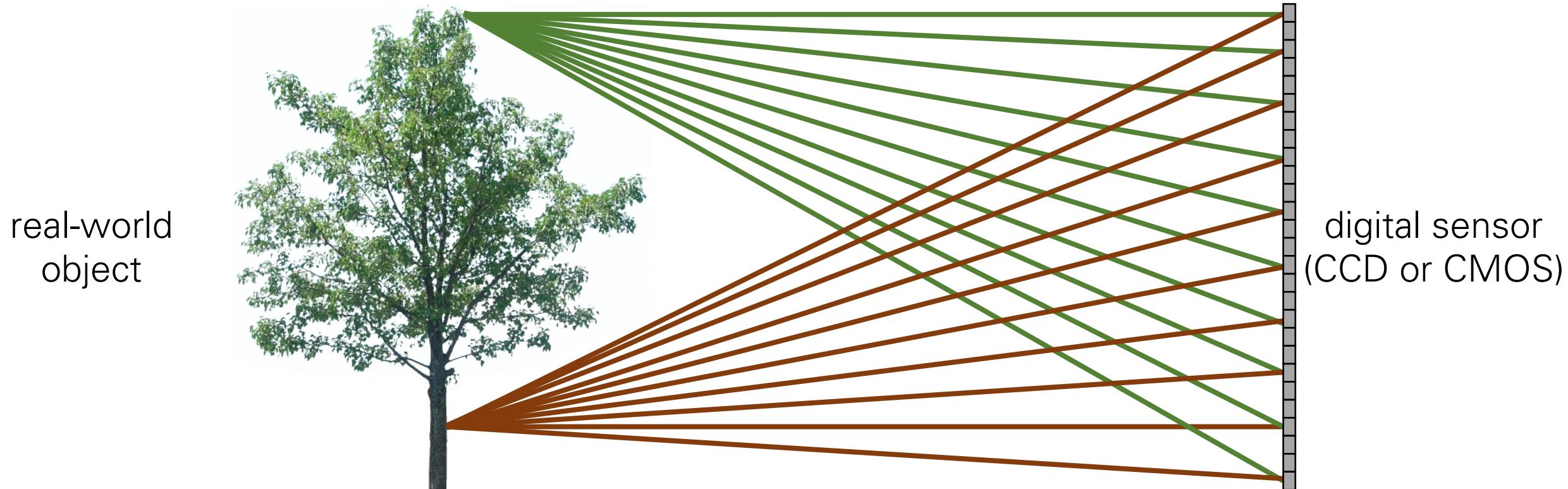
Bare-sensor imaging



Bare-sensor imaging



Bare-sensor imaging



All scene points contribute to all sensor pixels

What does the image
on the sensor look like?

Bare-sensor imaging



All scene points contribute to all sensor pixels

What can we do to make our image look better?

real-world
object



digital sensor
(CCD or CMOS)

Let's add something to this scene



barrier (diaphragm)



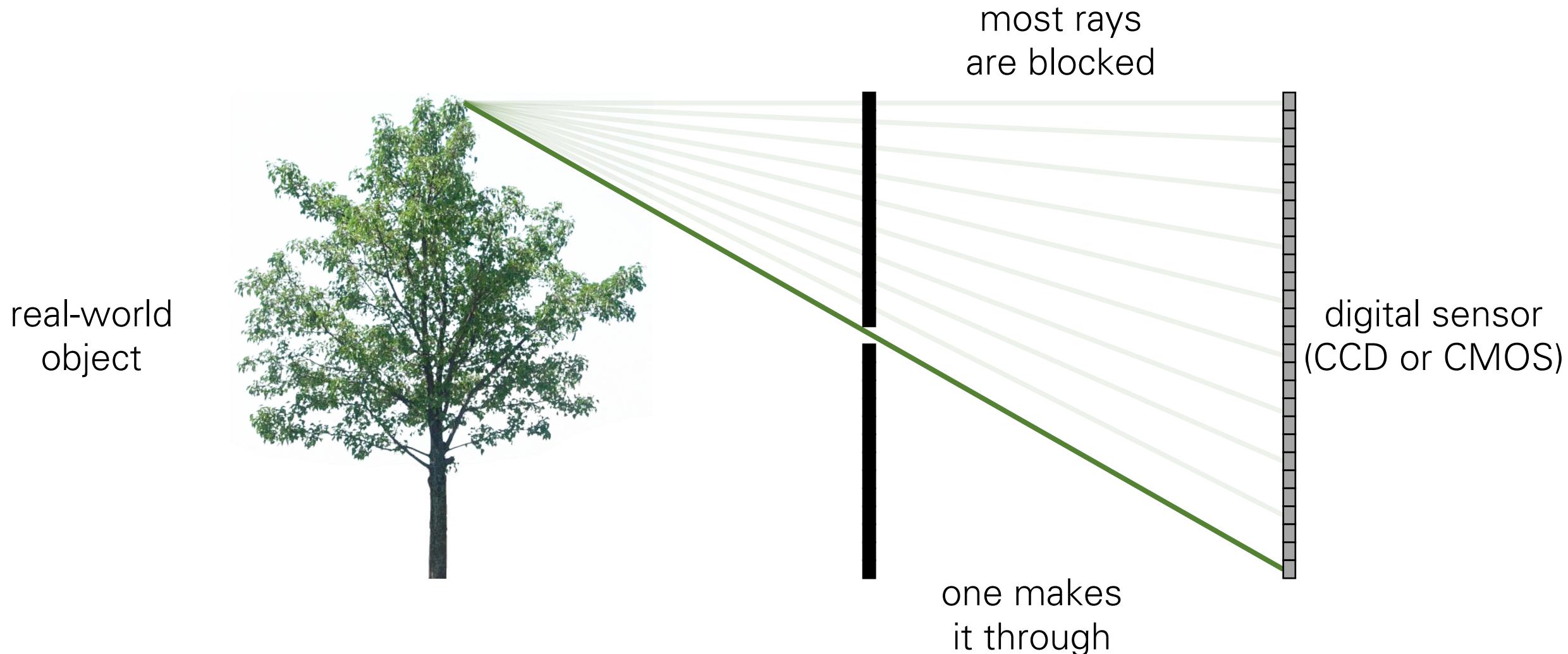
pinhole
(aperture)



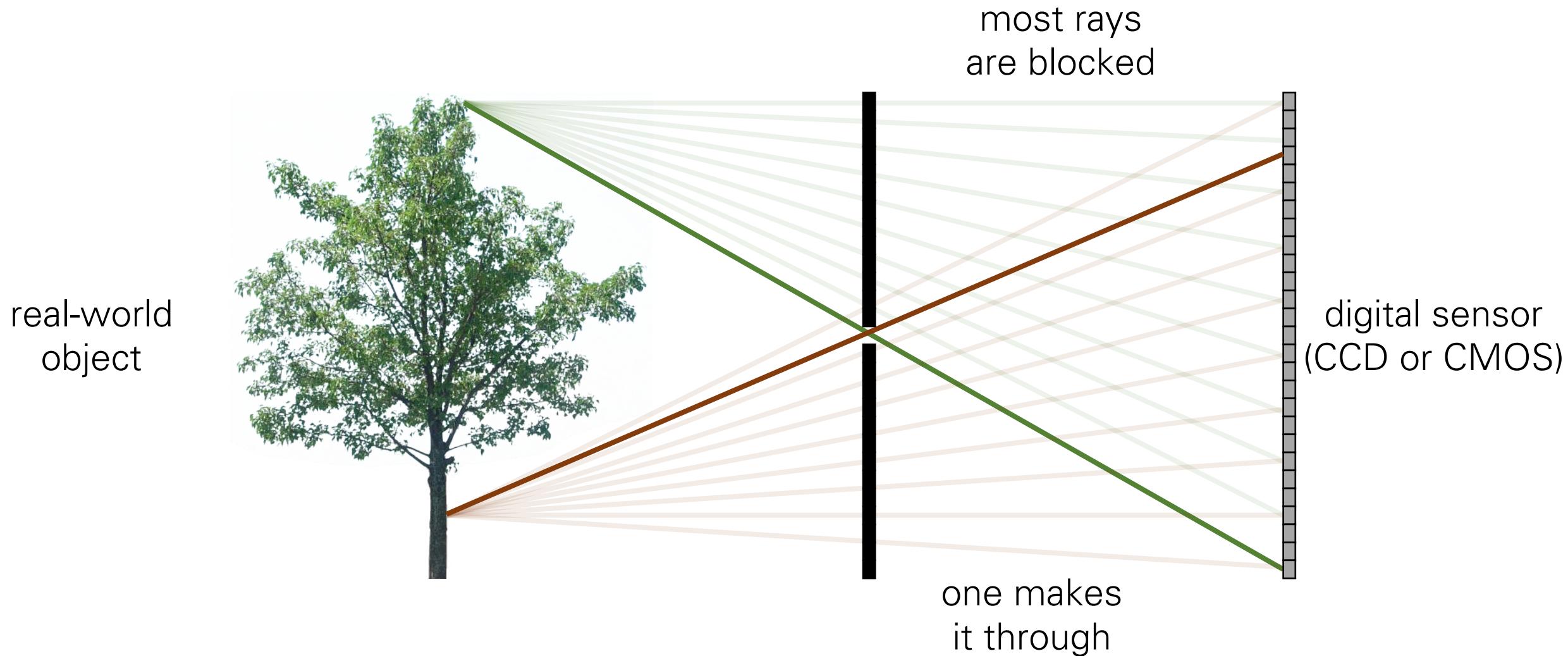
digital sensor
(CCD or CMOS)

What would an image taken like this look like?

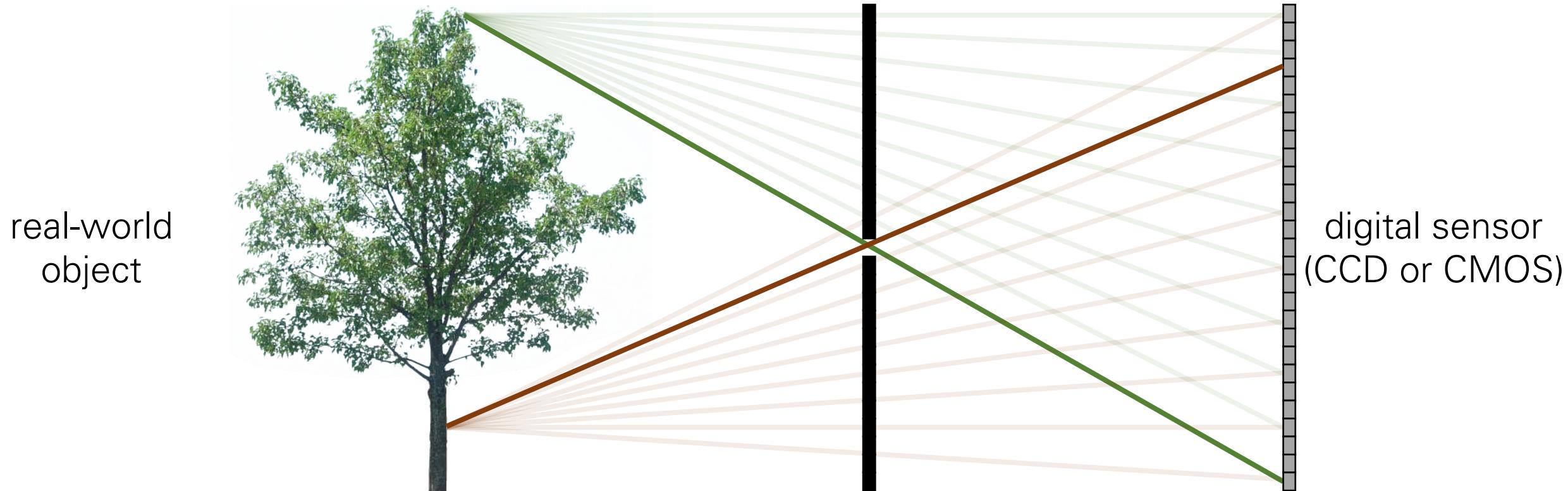
Pinhole imaging



Pinhole imaging



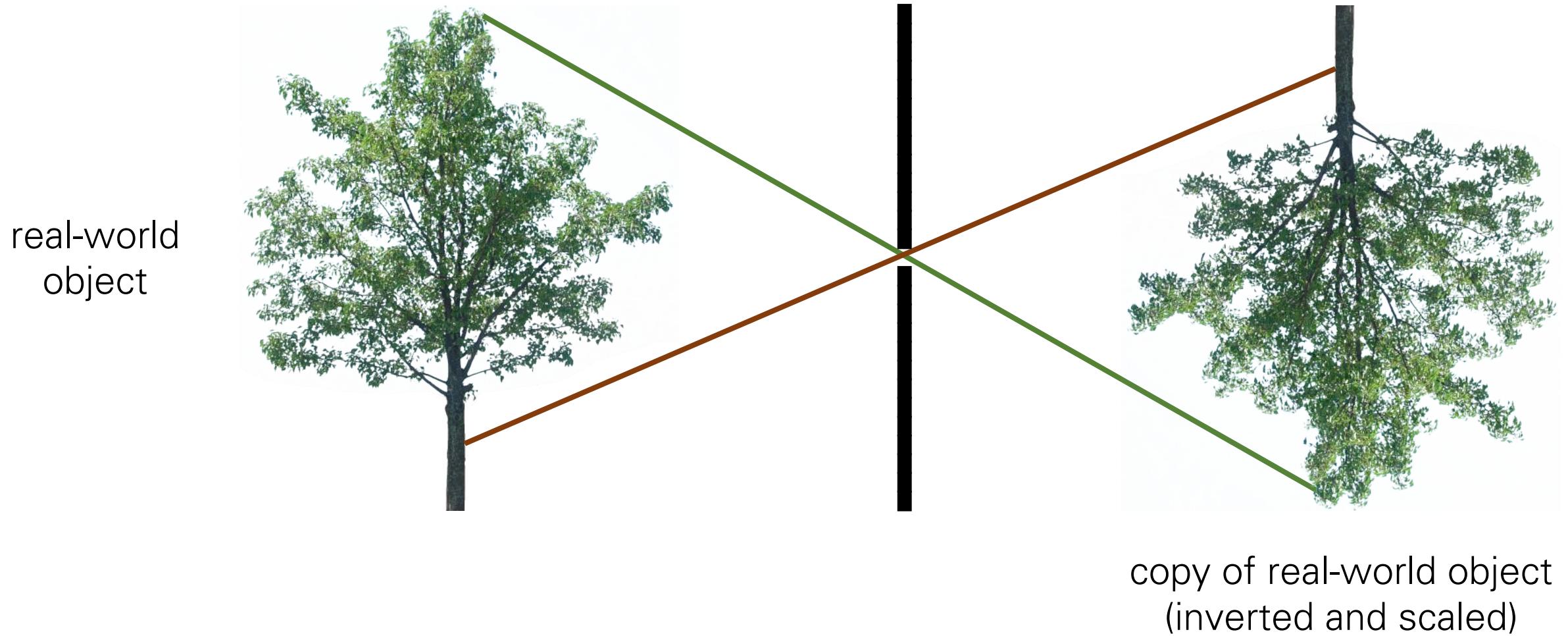
Pinhole imaging



Each scene point contributes to only one sensor pixel

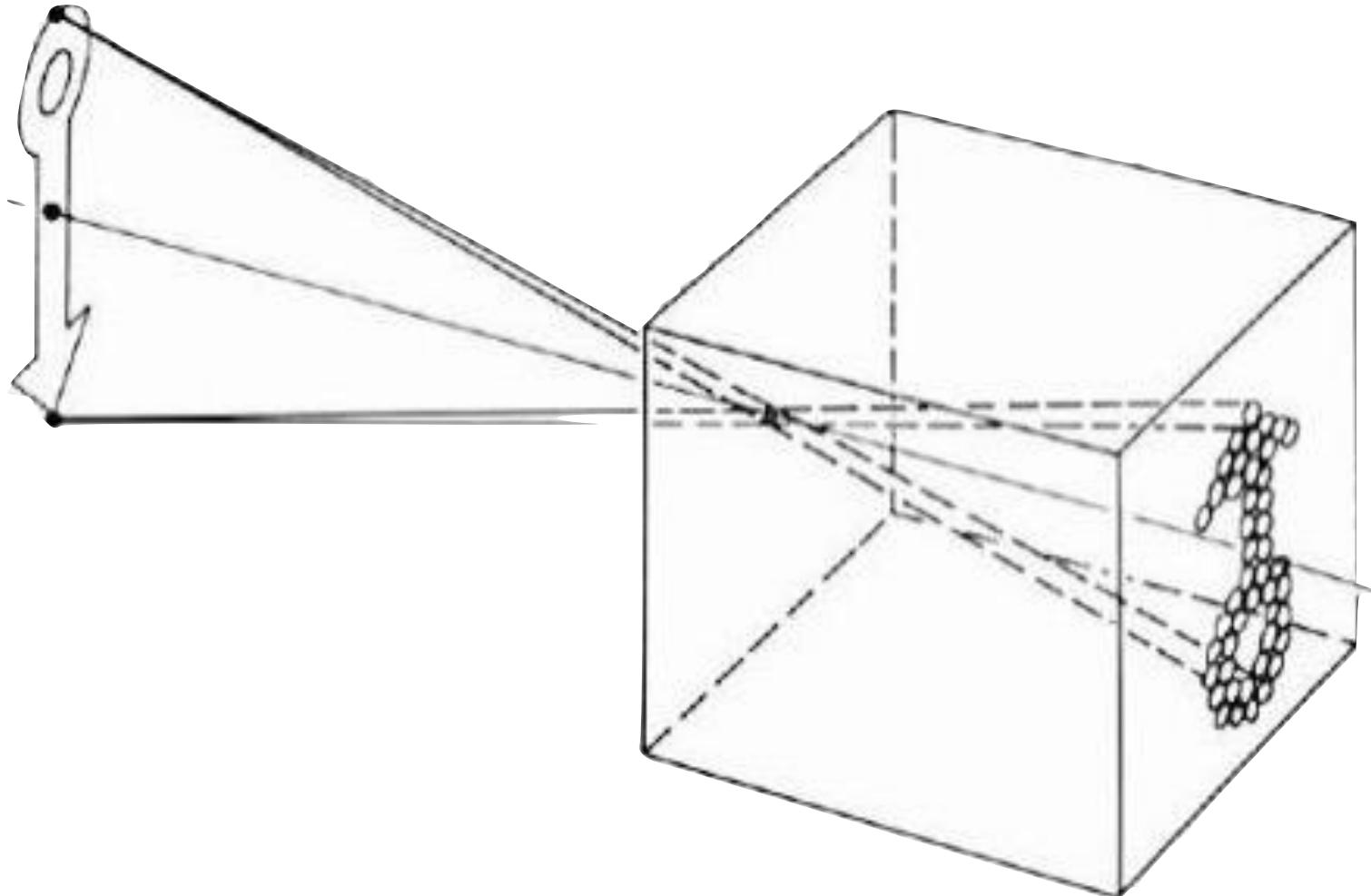
What does the image
on the sensor look like?

Pinhole imaging



Pinhole camera

Pinhole camera a.k.a. camera obscura



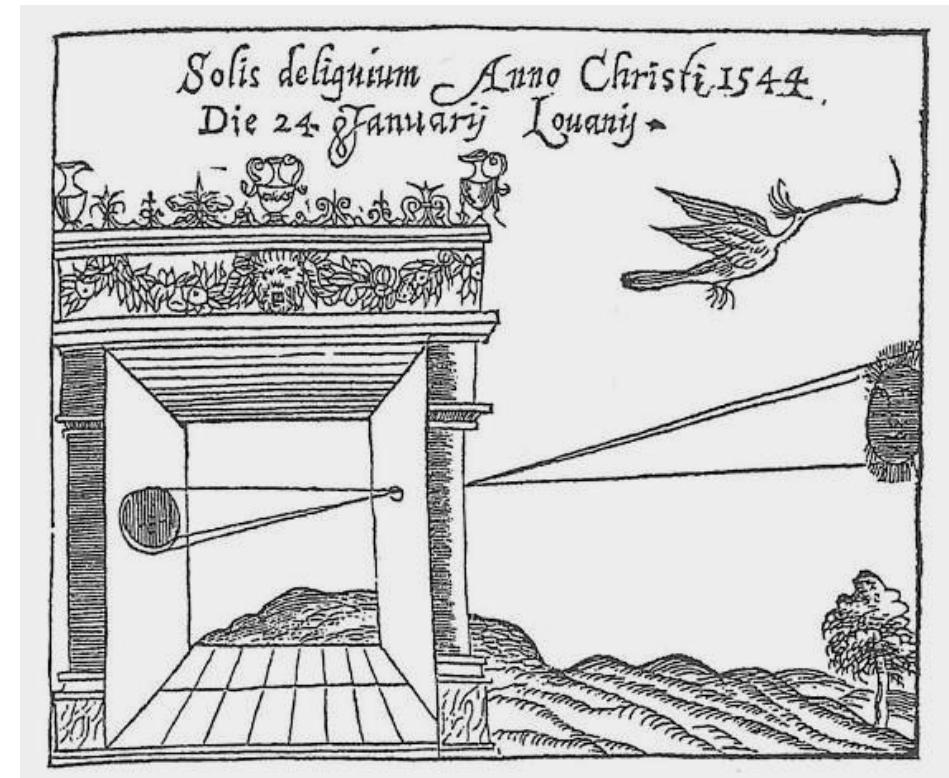
Pinhole camera a.k.a. camera obscura

First mention ...

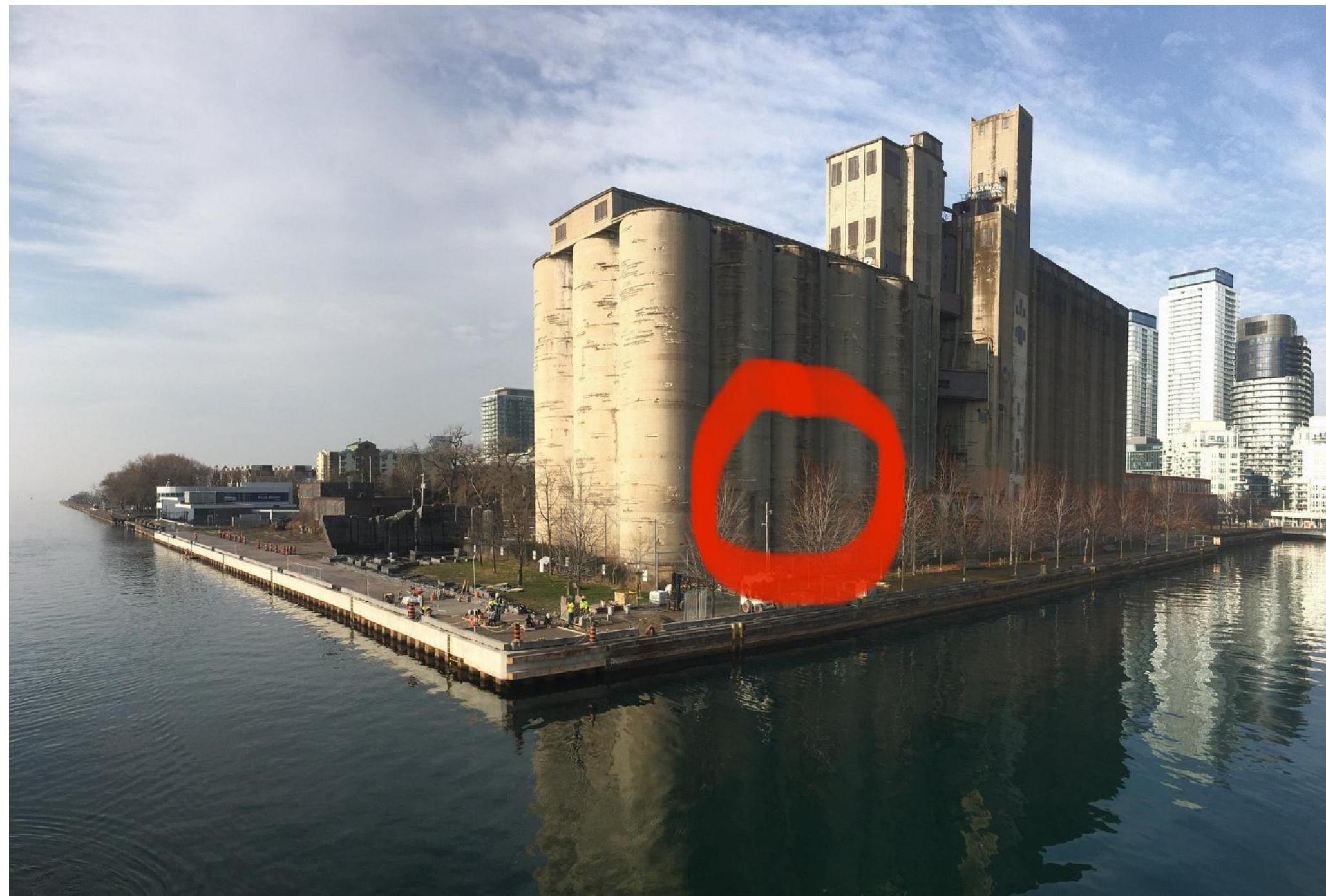


Chinese philosopher Mozi
(470 to 390 BC)

First camera ...



Greek philosopher Aristotle
(384 to 322 BC)

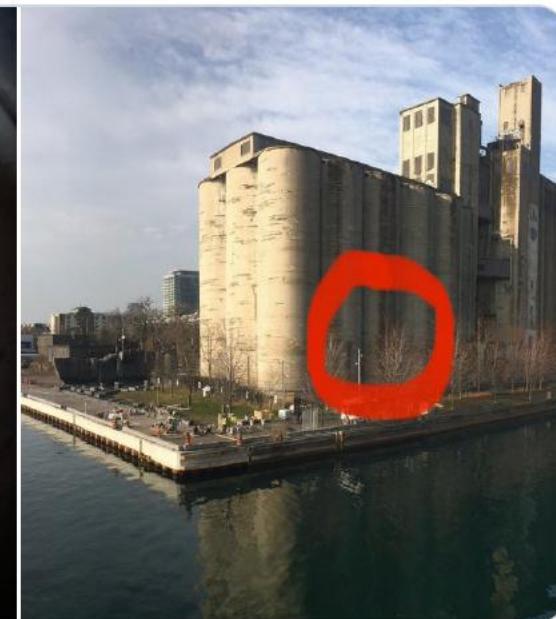




Bryan Bowen
@bryanmbowen

...

Fun discovery - a small crack in the eastern facade of the Canada Malting Co silos has created a perfect pinhole camera. The result: real time projection of Toronto's waterfront on the silo's interior curved surfaces. An unplugged projection show!



9:37 AM · Jan 27, 2022 · Twitter for iPhone

656 Retweets 70 Quote Tweets 2,836 Likes





Abelardo Morell



Abelardo Morell

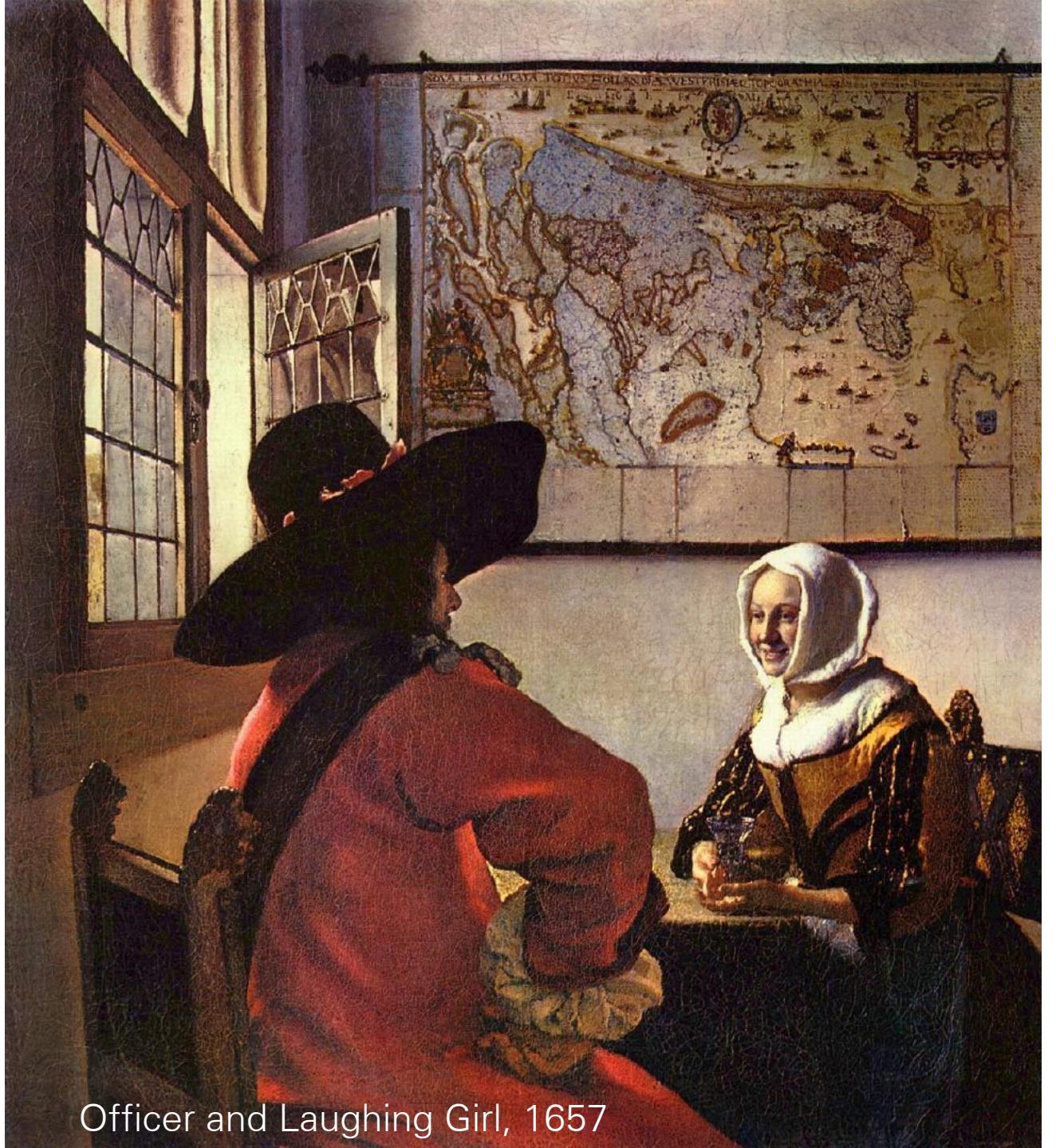


BBC FOUR

From BBC's The Genius Of Photography: "Fixing the Shadows"

Vermeer and The Camera Obscura

[http://www.essentialvermeer.com/camera_obscura/
co_one.html](http://www.essentialvermeer.com/camera_obscura/co_one.html)



Officer and Laughing Girl, 1657

Vermeer and The Camera Obscura

IMDb.com

IMDb

Menu All Search IMDb

Cast & crew · User reviews · Trivia · IMDbPro · All topics

IMDb RATING YOUR RATING
7.8/10 8.3K Rate

Tim's Vermeer

2013 · PG-13 · 1h 20m

Play trailer 2:05

Documentary History

Inventor Tim Jenison seeks to understand the painting techniques used by Dutch Master Johannes Vermeer.

Director Teller

Writers Penn Jillette · Teller

Stars Tim Jenison · Penn Jillette · Martin Mull

IMDb Pro See production, box office & company info

Nominated for 1 BAFTA Award 1 win & 6 nominations total

Add to Watchlist

52 User reviews 84 Critic reviews 76 Metascore

More to explore

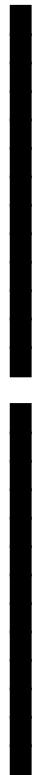
31

Pinhole camera terms

real-world
object



barrier (diaphragm)



pinhole
(aperture)



digital sensor
(CCD or CMOS)

Pinhole camera terms

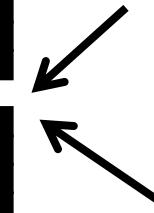
real-world object



barrier (diaphragm)



pinhole
(aperture)



camera center
(center of projection)

image plane

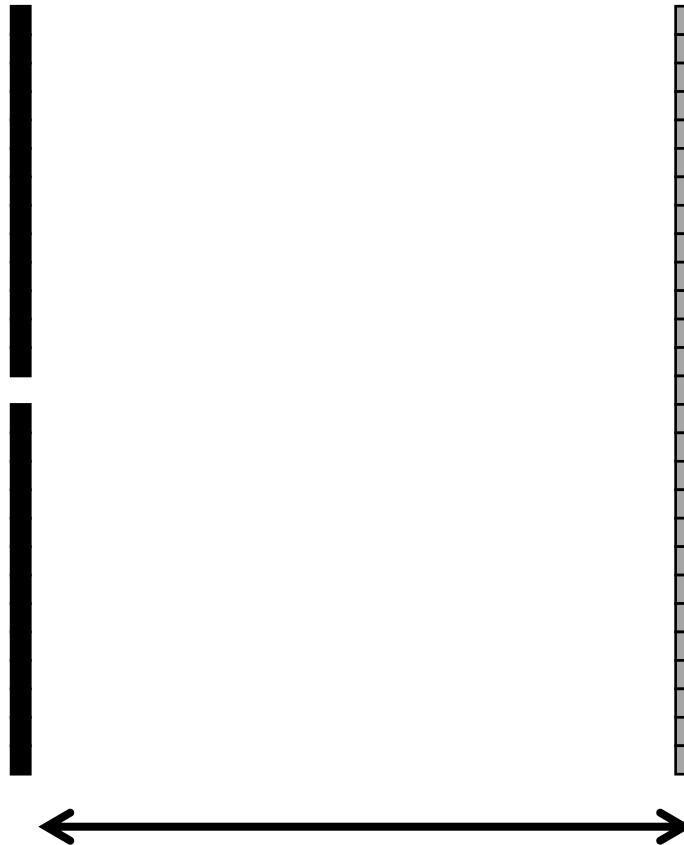


digital sensor
(CCD or CMOS)



Focal length

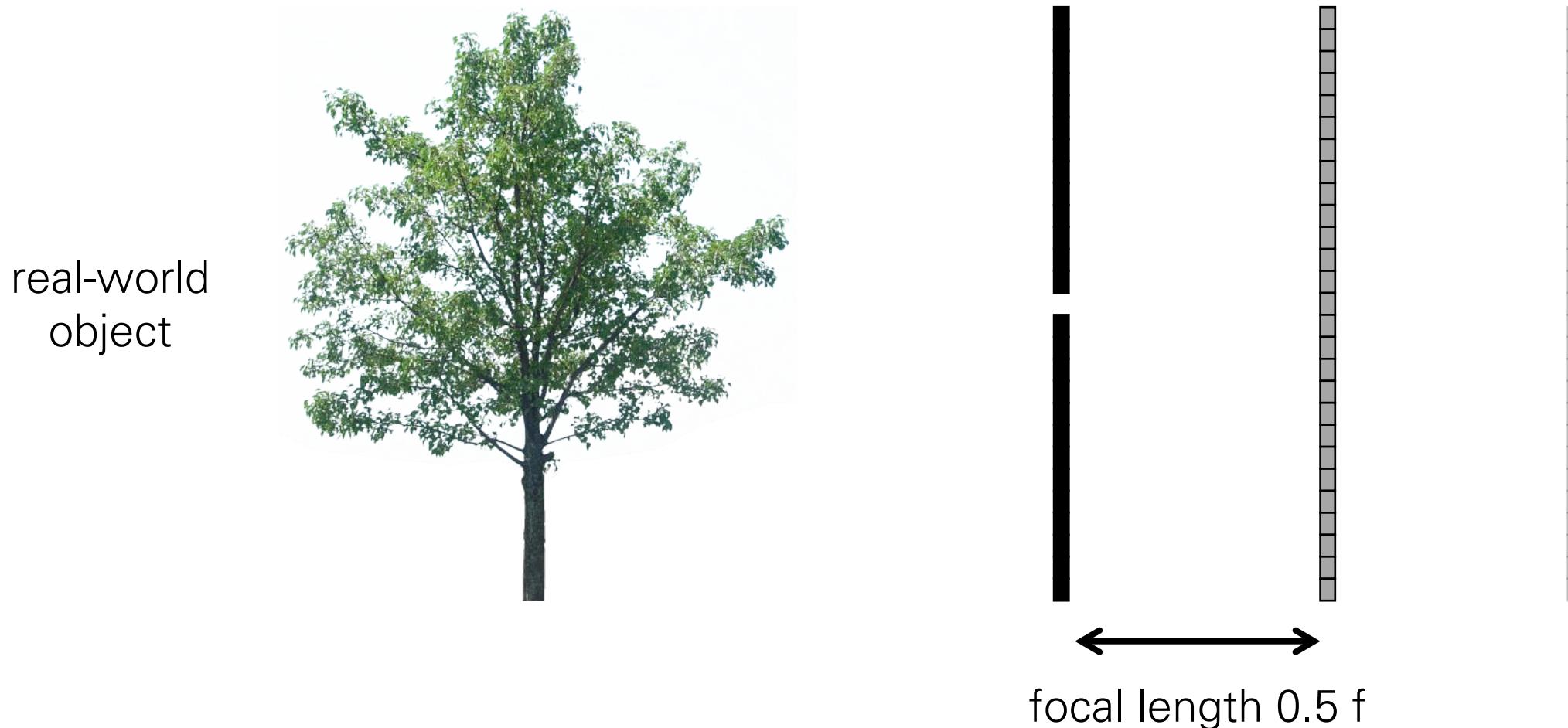
real-world
object



focal length f

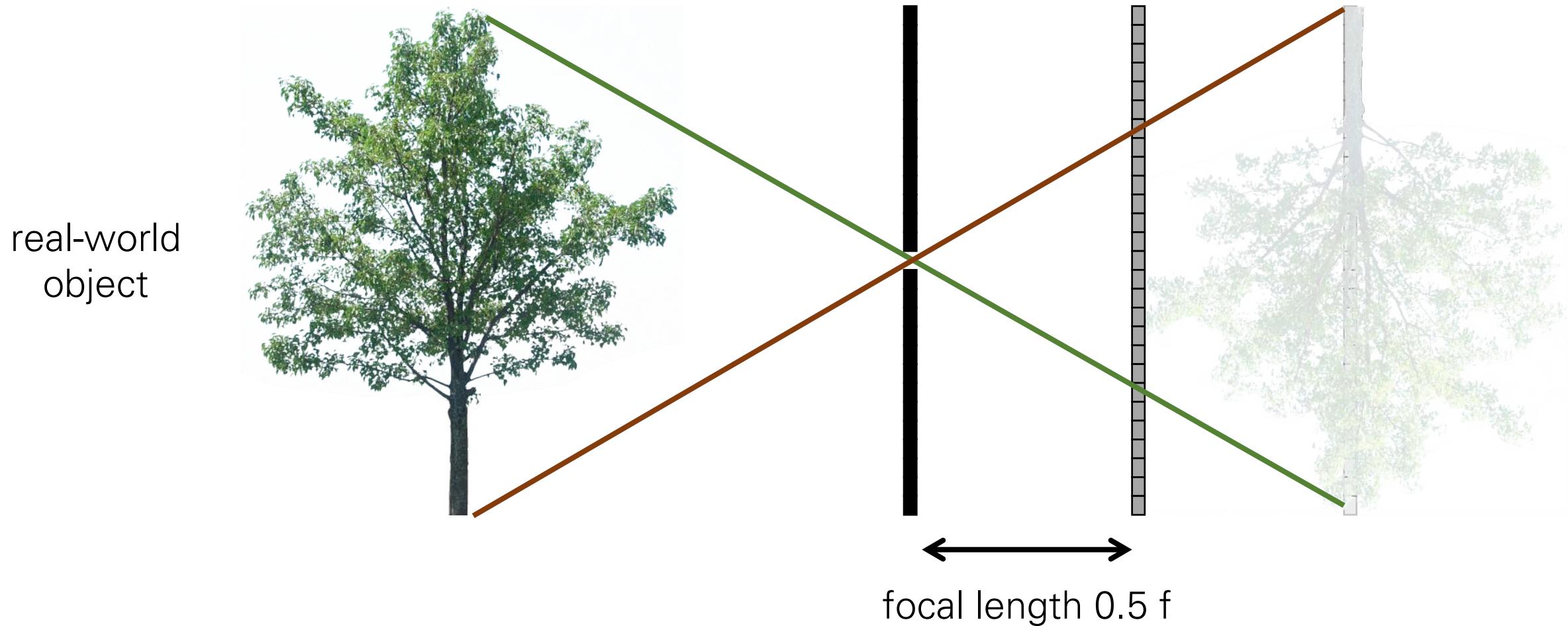
Focal length

What happens as we change the focal length?



Focal length

What happens as we change the focal length?

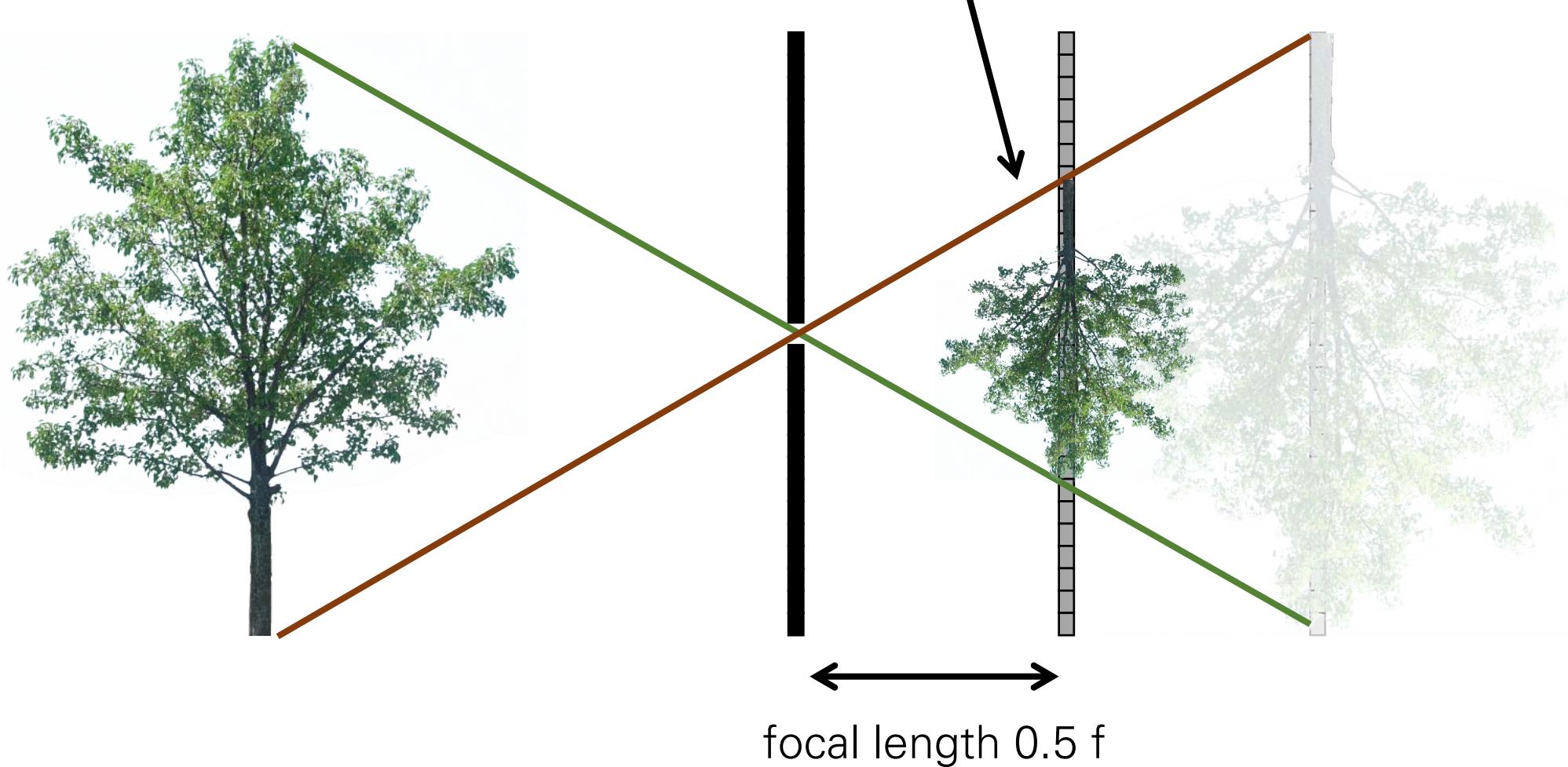


Focal length

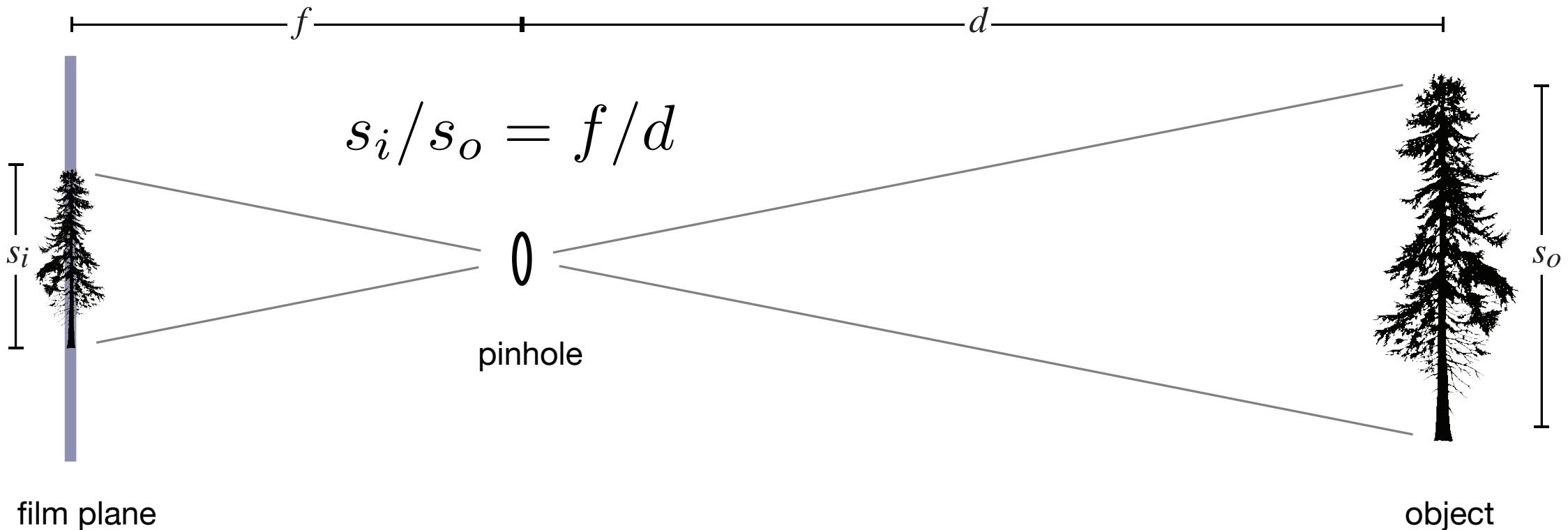
What happens as we change the focal length?

real-world
object

object projection is half the size



Focal length



- Double “focal length” leads to
 - image twice as large
 - one fourth as much illumination at image plane

Pinhole size

real-world object



pinhole diameter



Ideal pinhole has infinitesimally small size

- In practice that is impossible!

Pinhole size

What happens as we change the pinhole diameter?

real-world
object



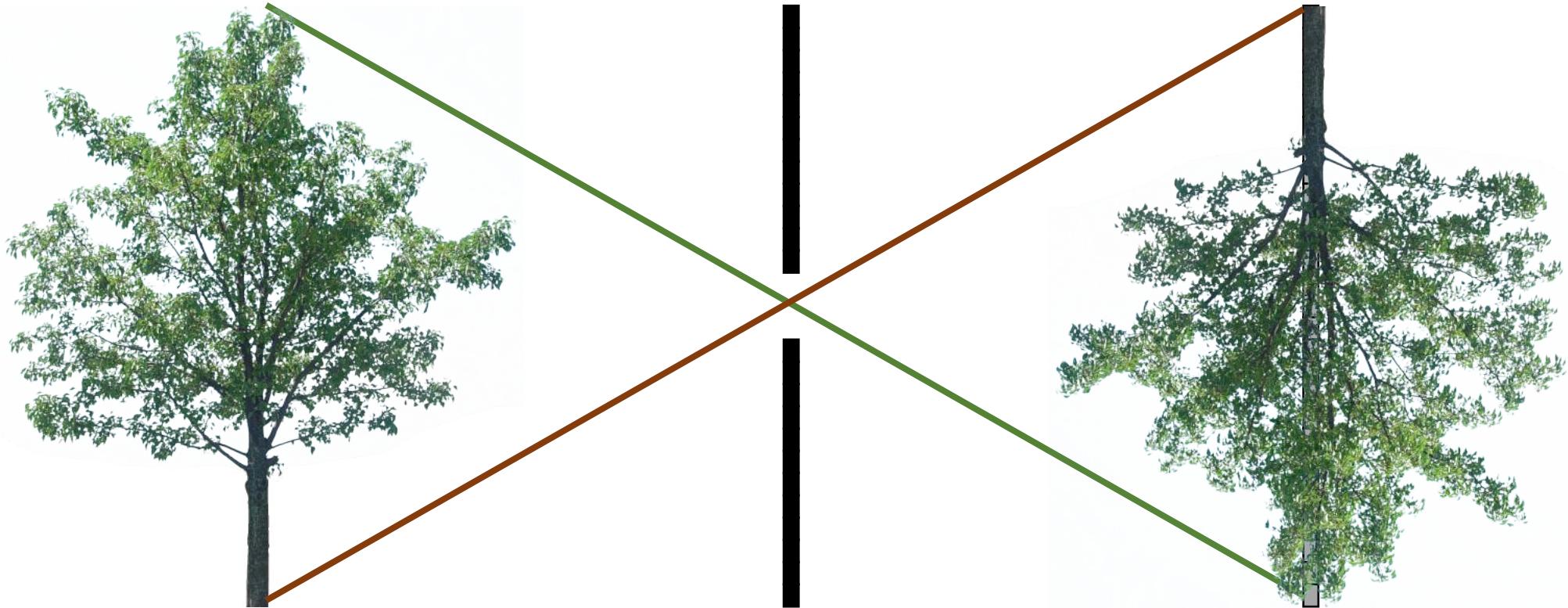
pinhole
diameter



Pinhole size

What happens as we change the pinhole diameter?

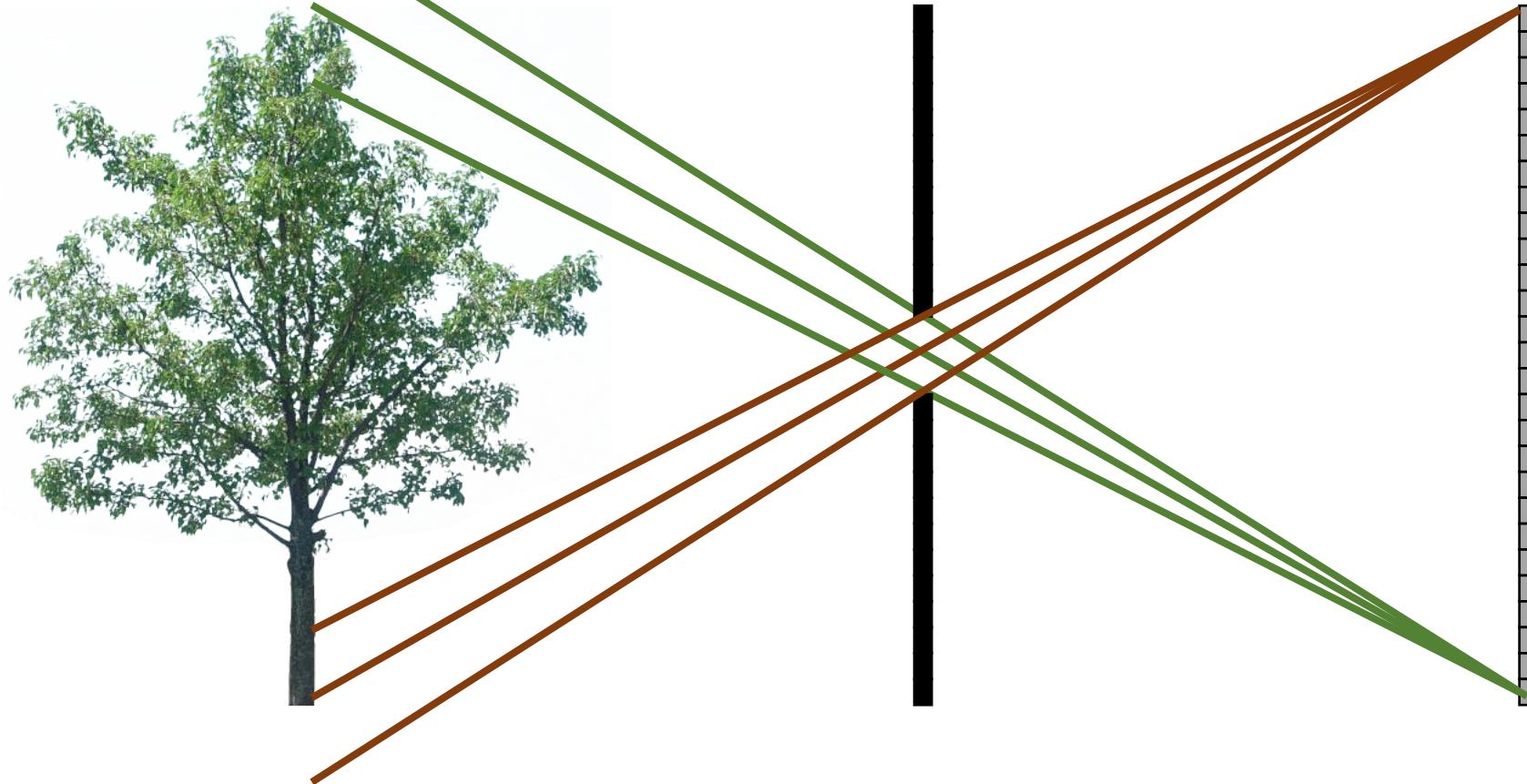
real-world
object



Pinhole size

What happens as we change the pinhole diameter?

real-world
object

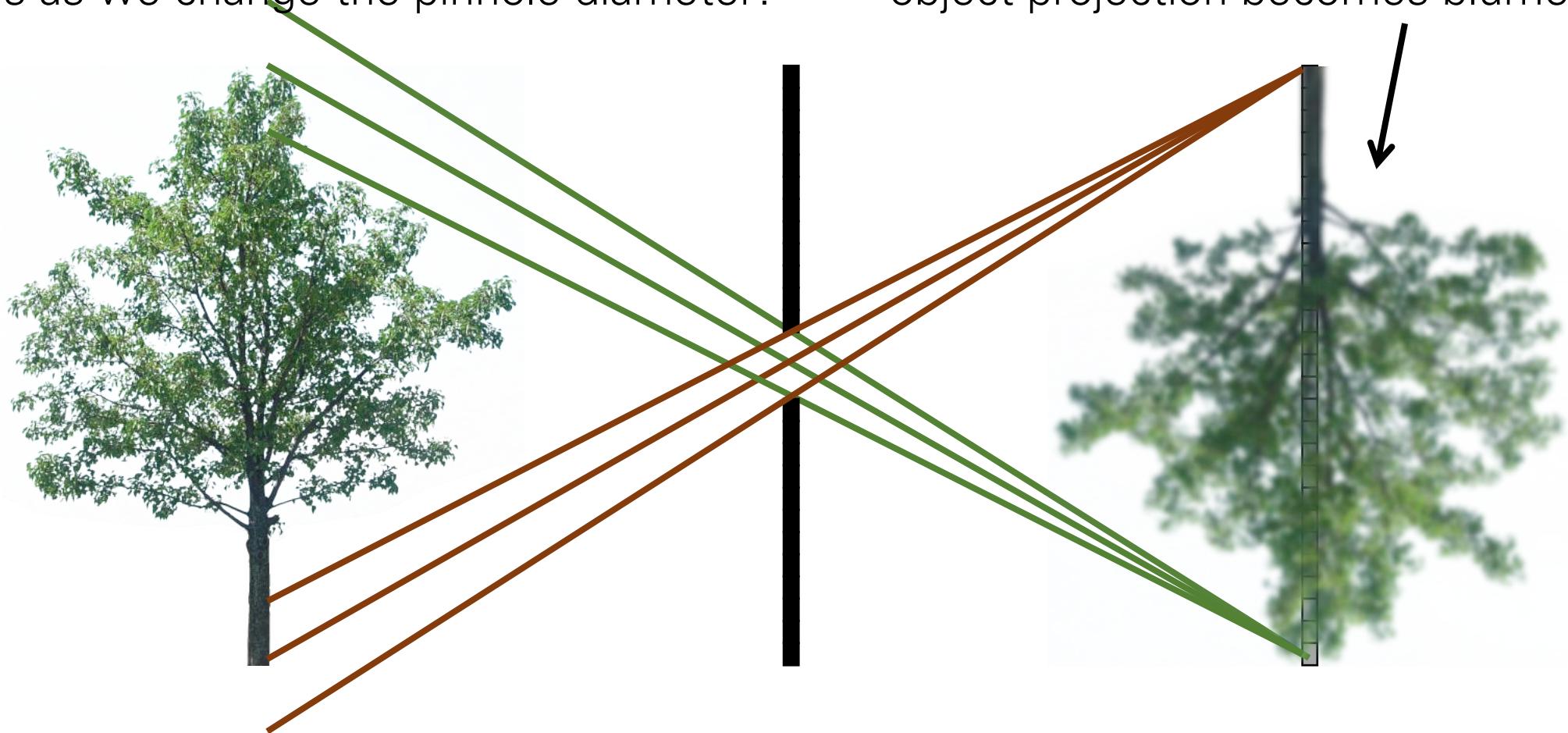


Pinhole size

What happens as we change the pinhole diameter?

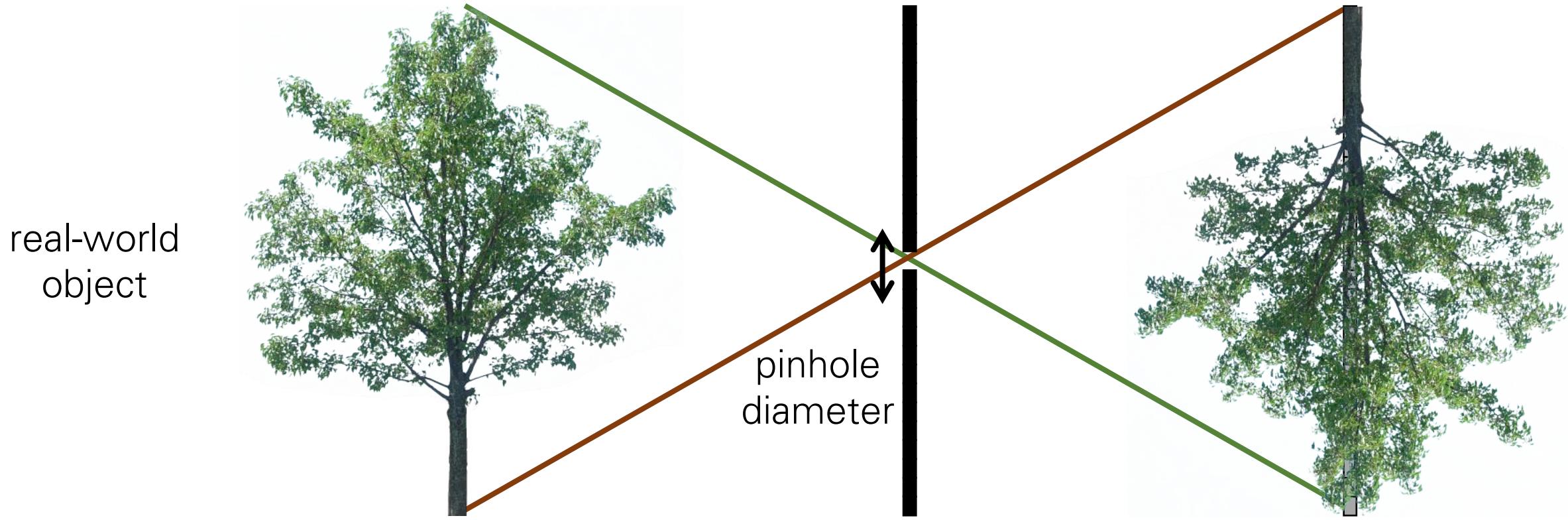
object projection becomes blurrier

real-world
object



Pinhole size

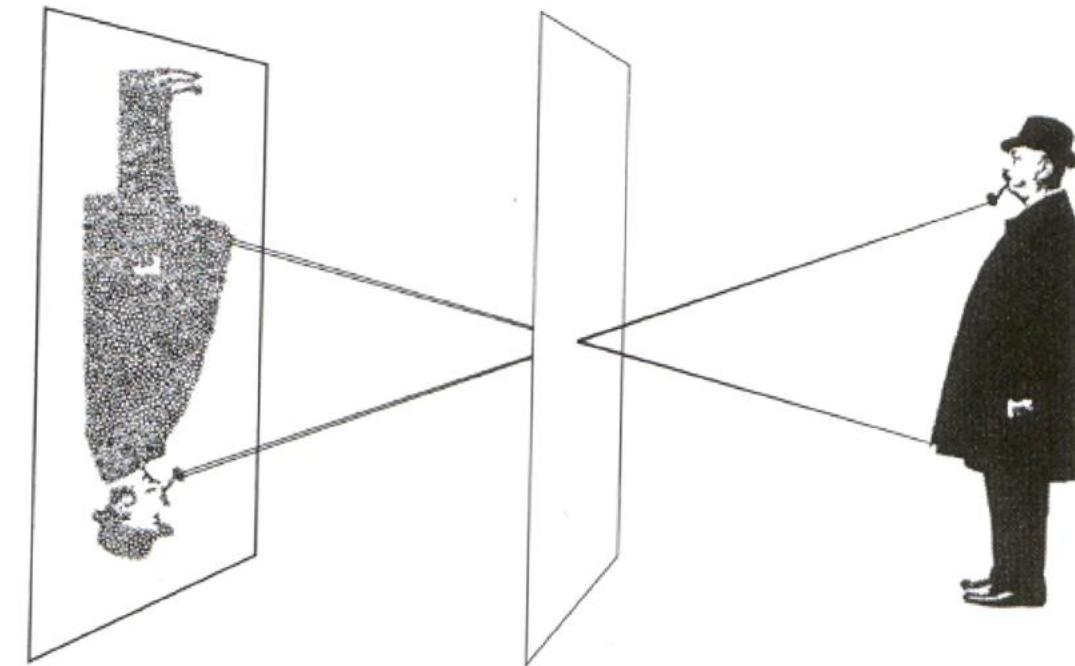
What happens as we change the pinhole diameter?



Will the image keep getting sharper the smaller we make the pinhole?

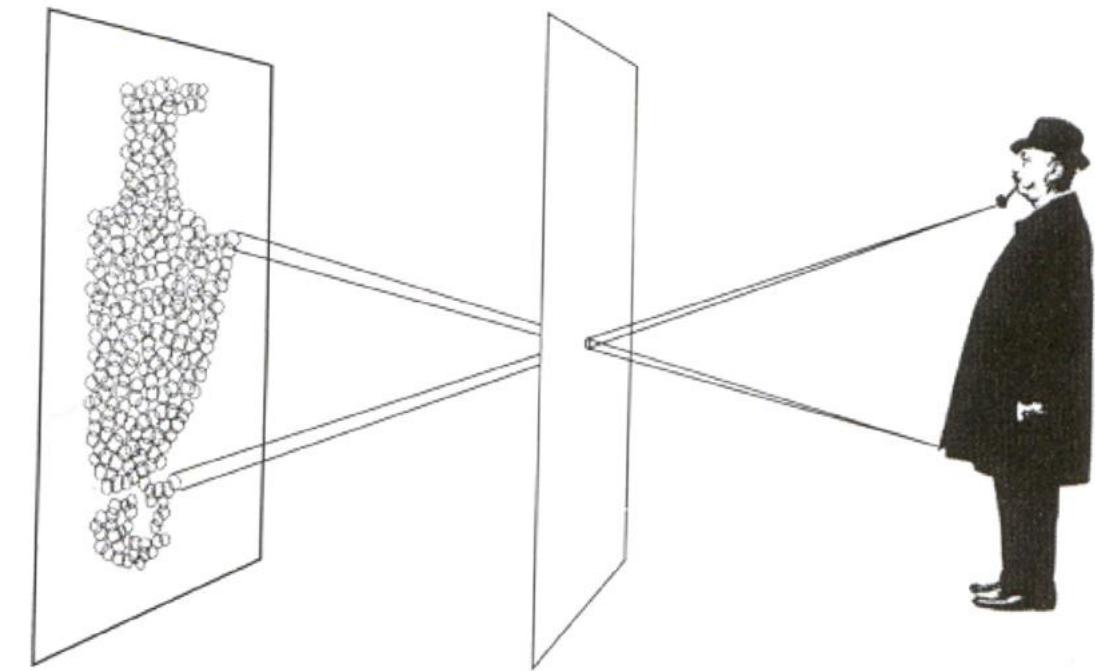
Effect of pinhole size

Photograph made with small pinhole

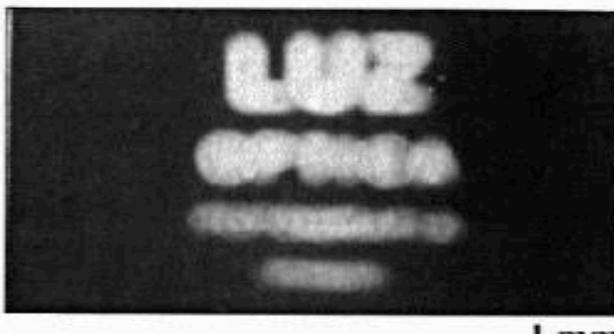
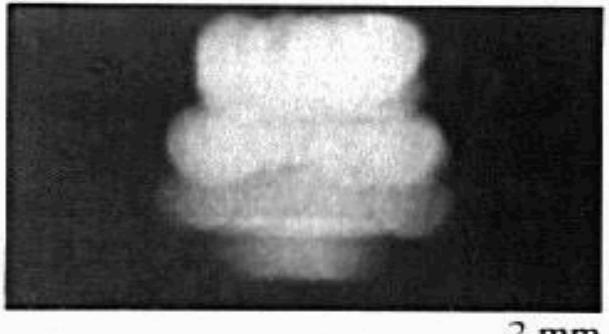


Effect of pinhole size

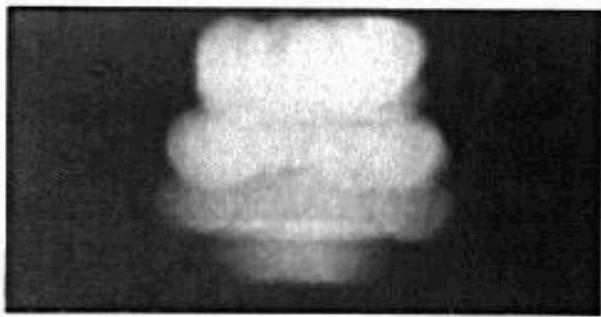
Photograph made with larger pinhole



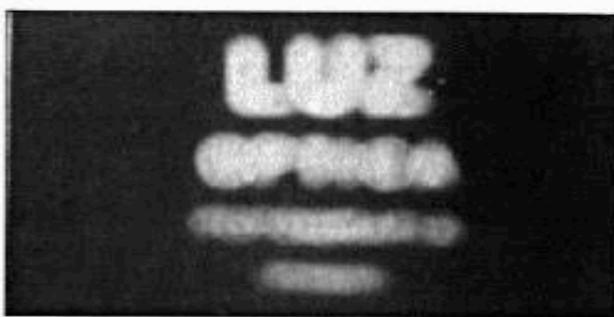
Smaller pinhole is sharper



Smaller pinhole is sharper ... to a point



2 mm



1 mm



0.6mm



0.35 mm



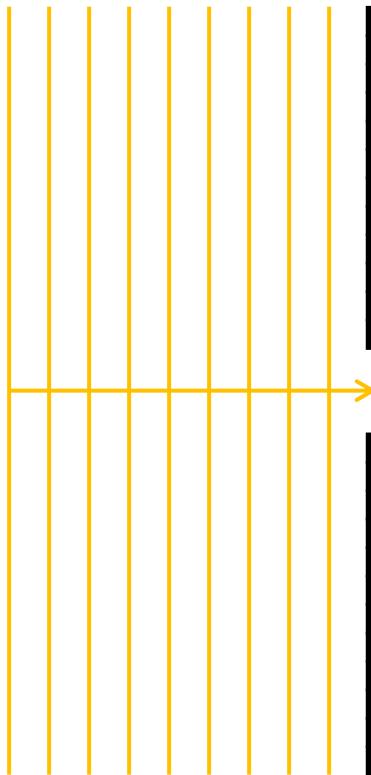
0.15 mm



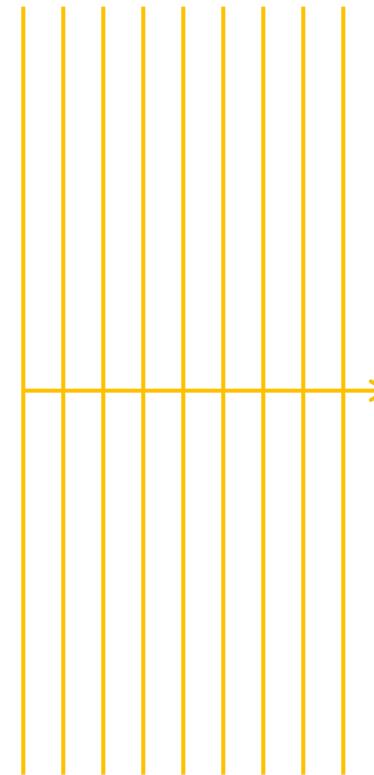
0.07 mm

Diffraction limit

A consequence of the wave nature of light



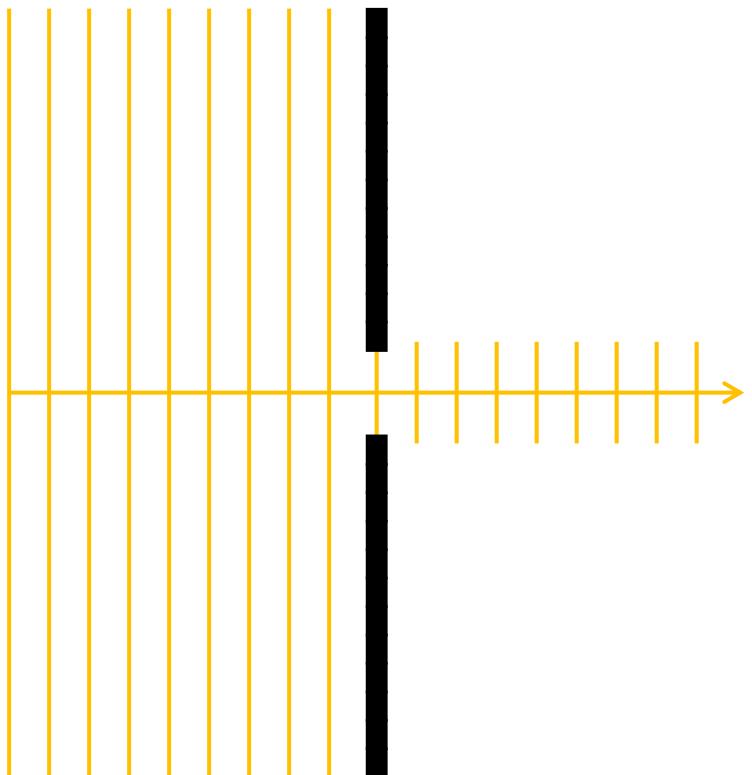
What do geometric optics
predict will happen?



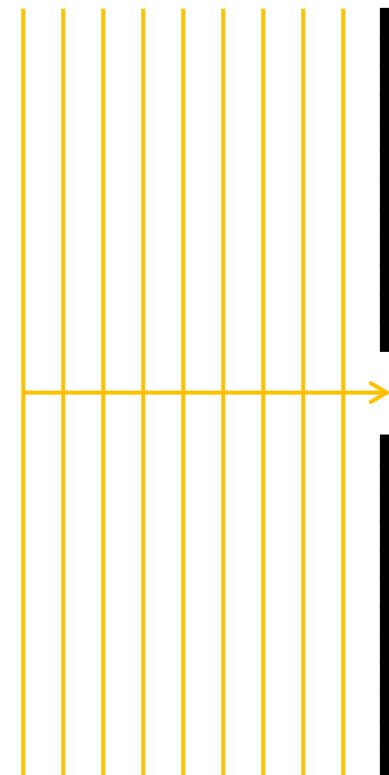
What do wave optics
predict will happen?

Diffraction limit

A consequence of the wave nature of light



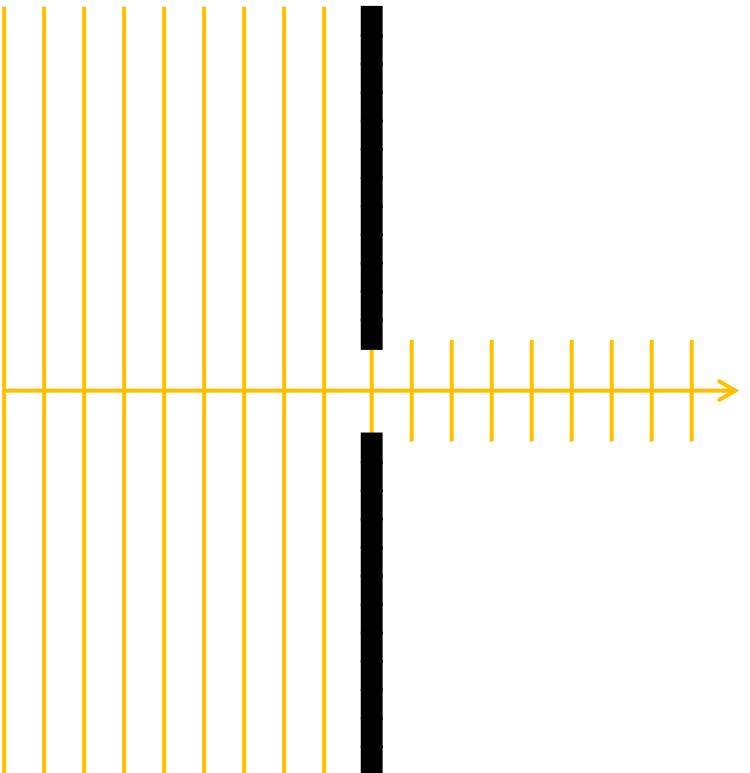
What do geometric optics
predict will happen?



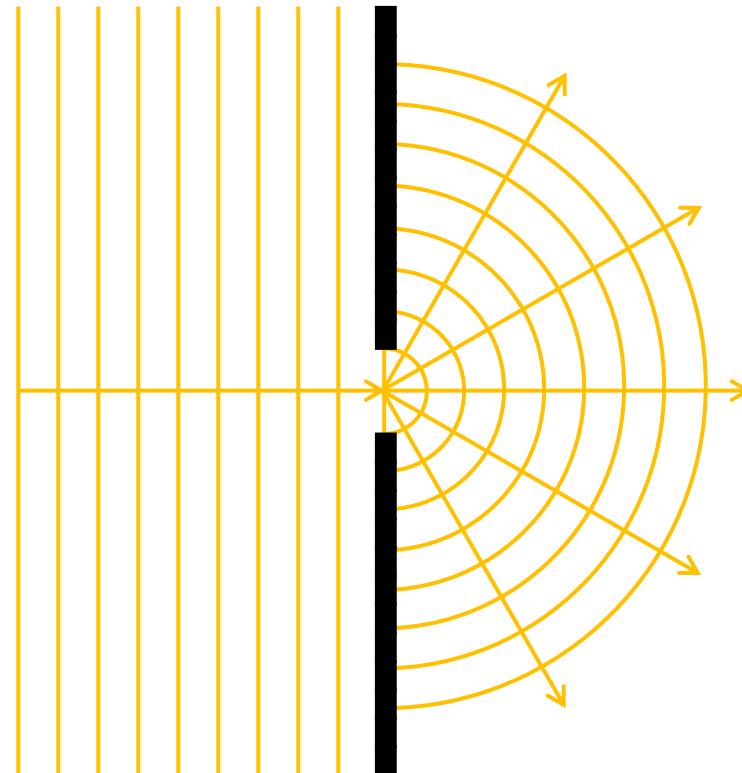
What do wave optics
predict will happen?

Diffraction limit

A consequence of the wave nature of light



What do geometric optics
predict will happen?

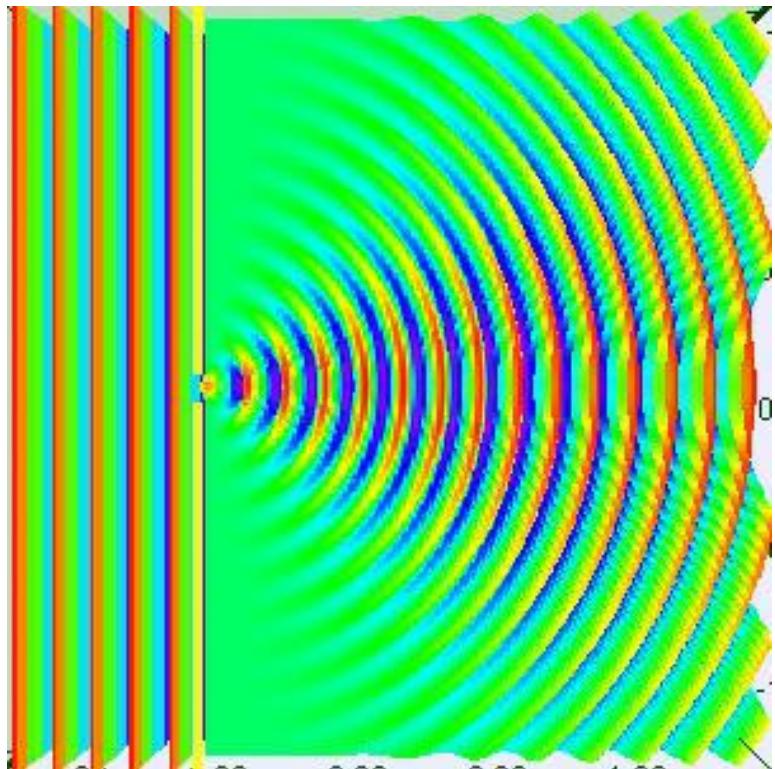


What do wave optics
predict will happen?

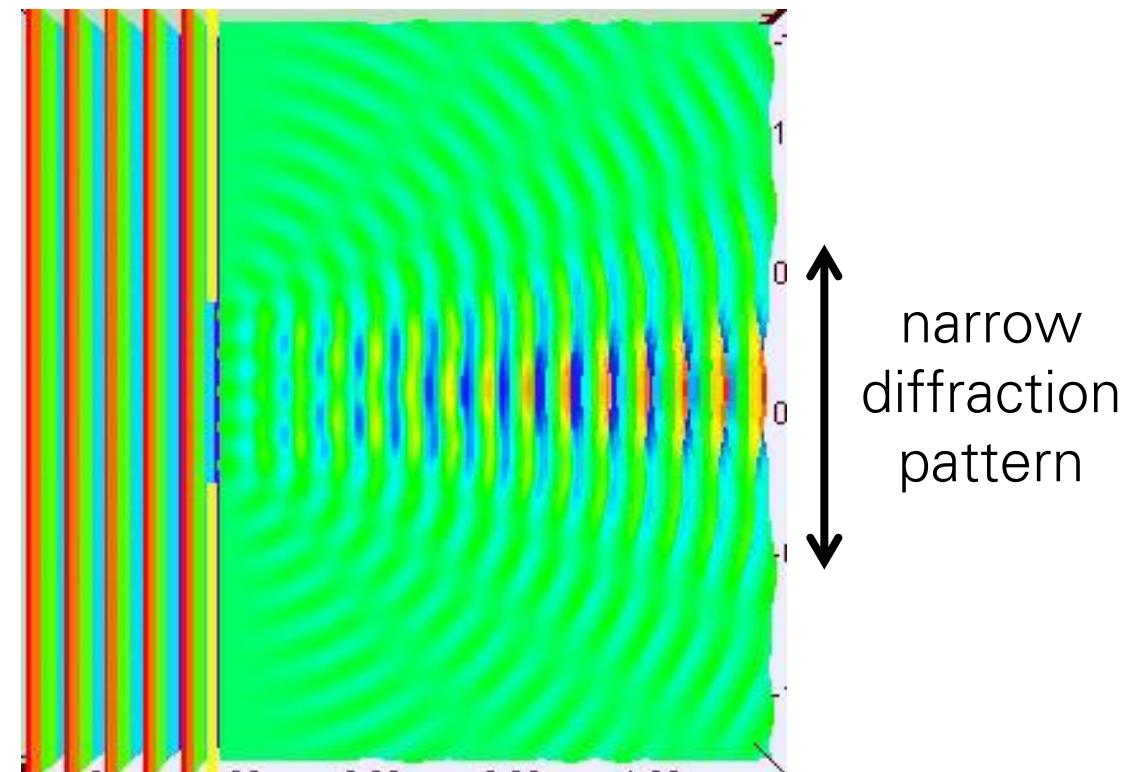
Diffraction limit

Diffraction pattern = Fourier transform of the pinhole.

- Smaller pinhole means bigger Fourier spectrum.
- Smaller pinhole means more diffraction.

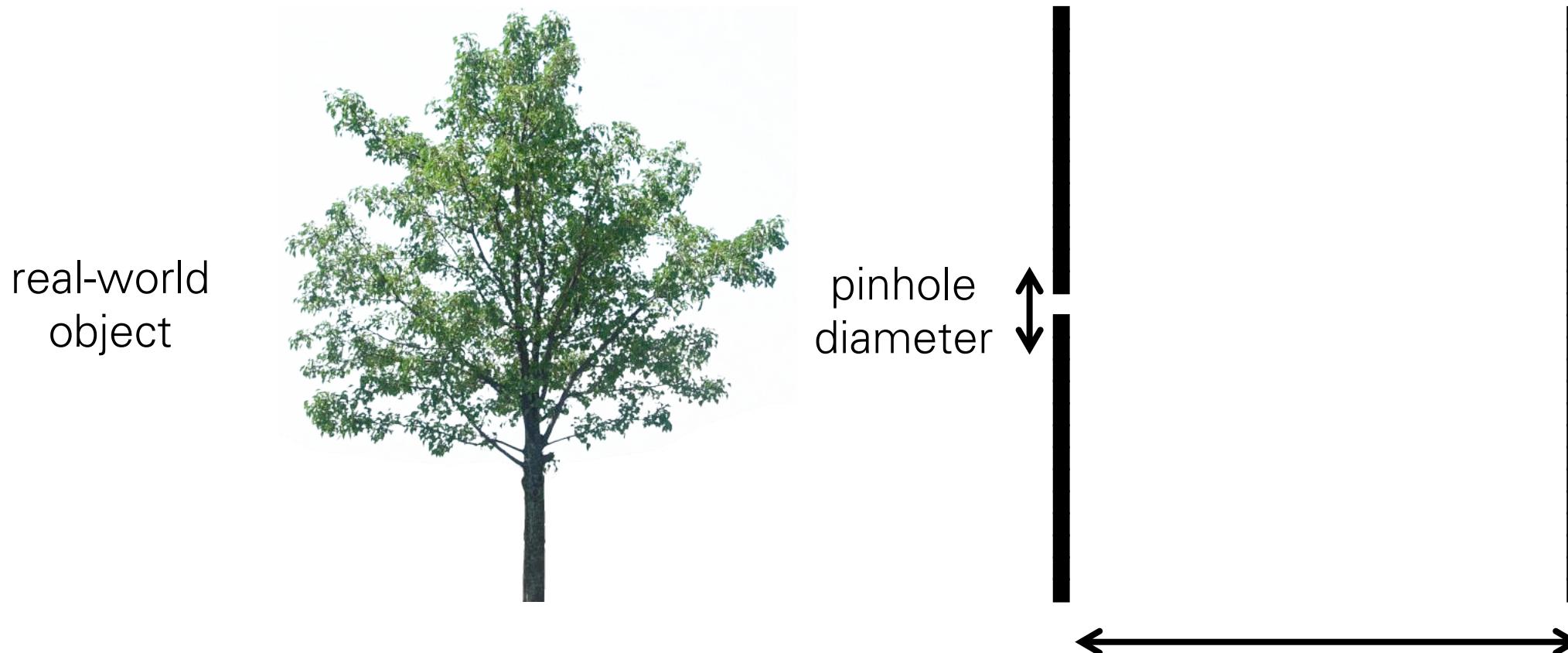


small pinhole



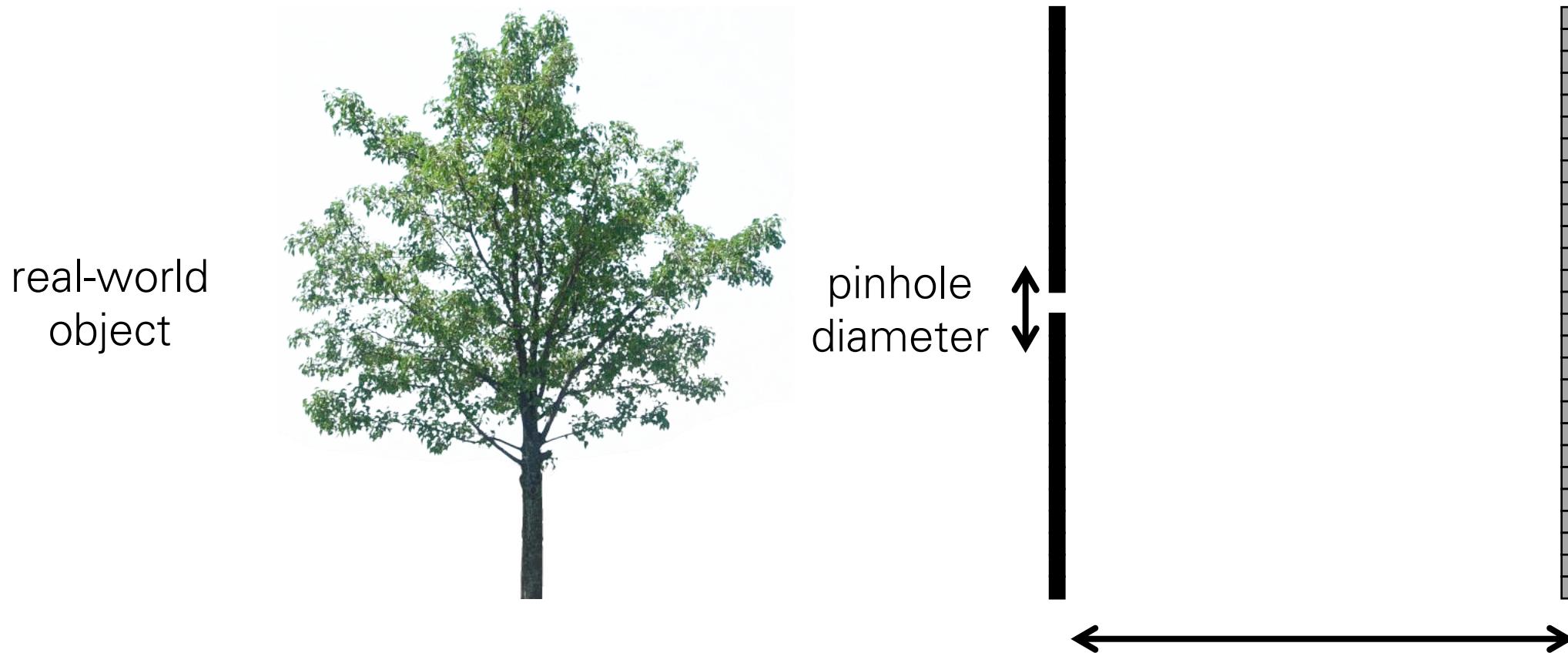
large pinhole

What about light efficiency?



- What is the effect of doubling the pinhole diameter?
- What is the effect of doubling the focal length?

What about light efficiency?

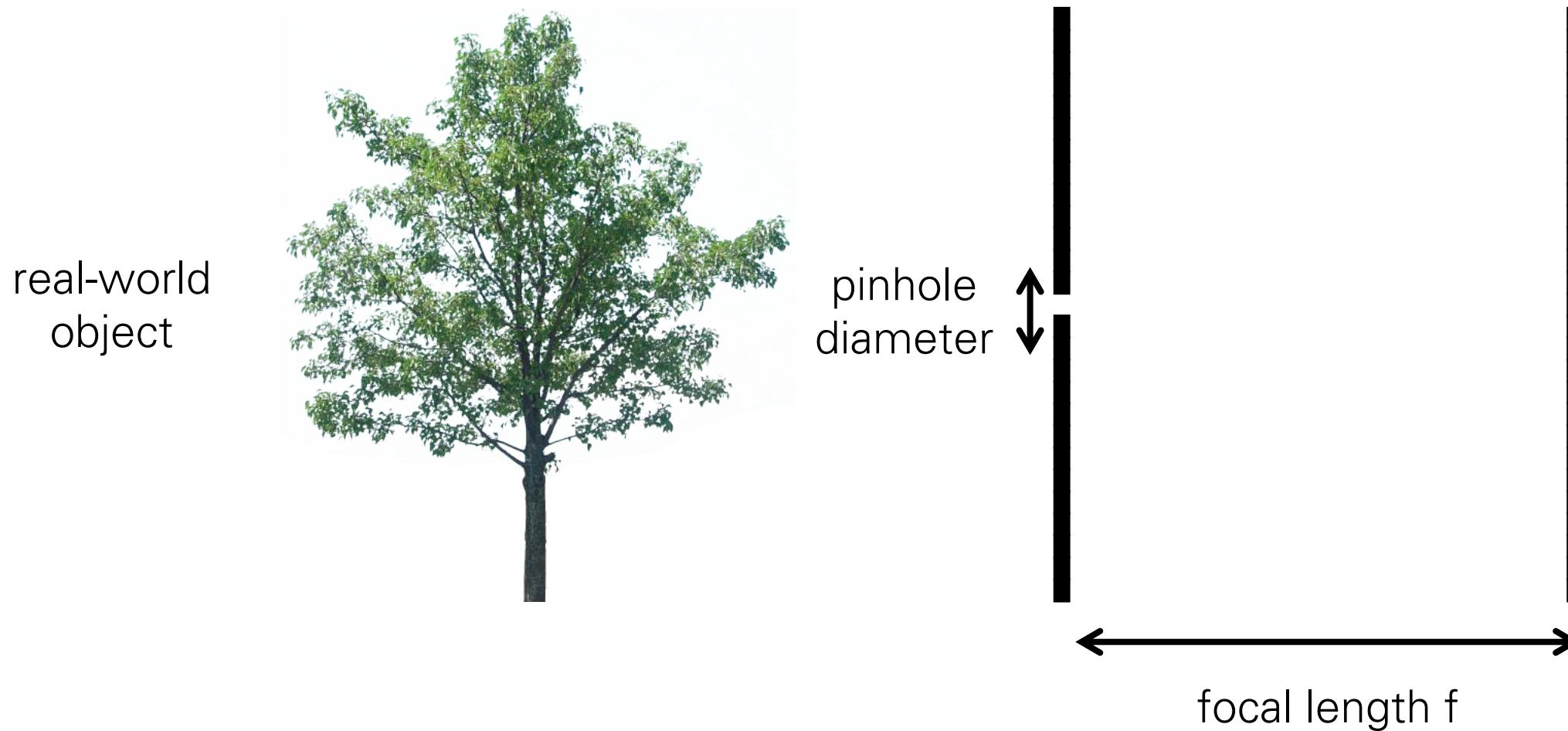


- $2 \times$ pinhole diameter $\rightarrow 4 \times$ light
- $2 \times$ focal length $\rightarrow \frac{1}{4} \times$ light

focal length f

Some terminology notes

A “stop” is a change in camera settings that changes amount of light by a factor of 2



The “f-number” is the ratio: focal length / pinhole diameter

Accidental pinholes

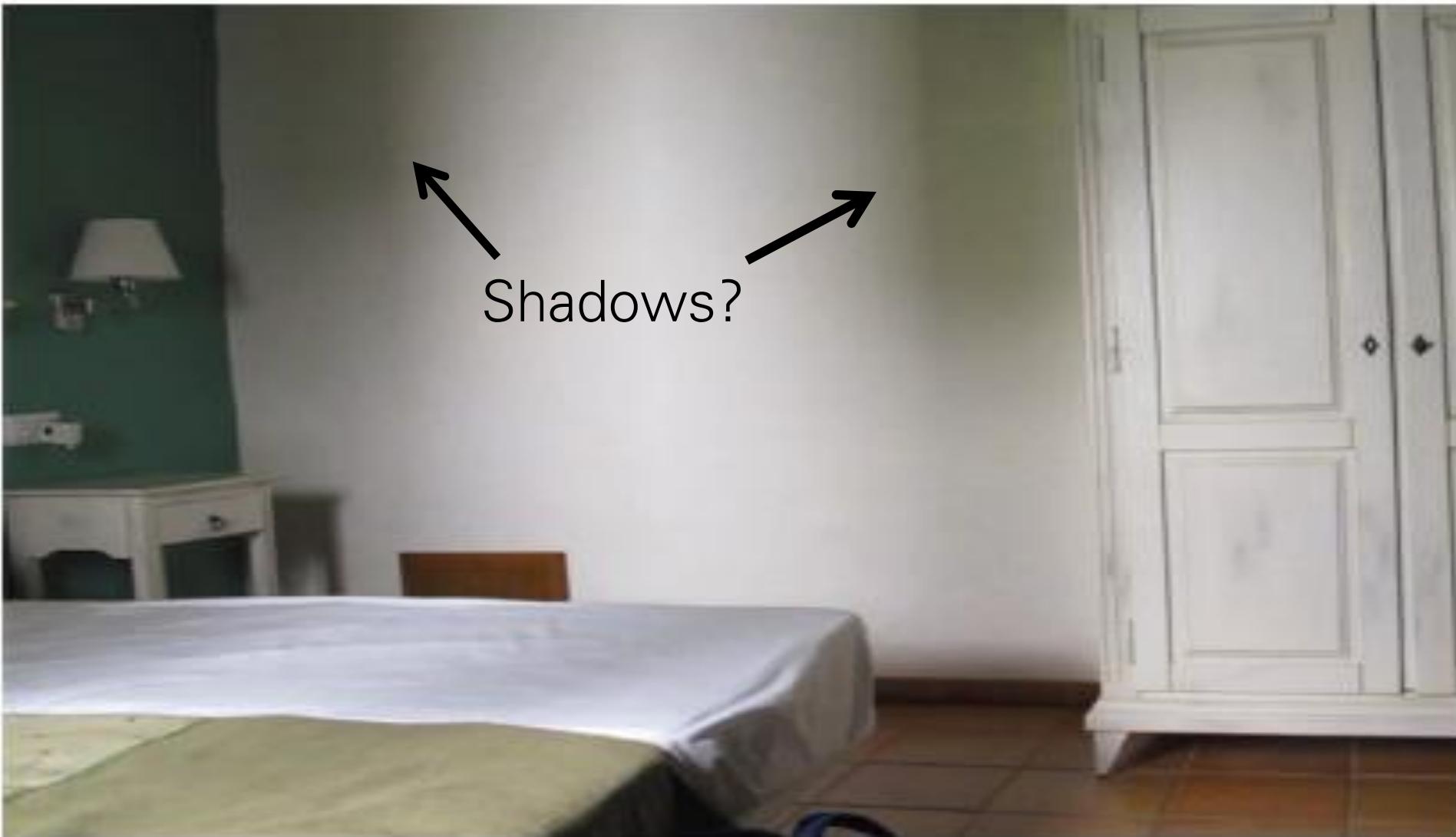
What does this image say about the world outside?



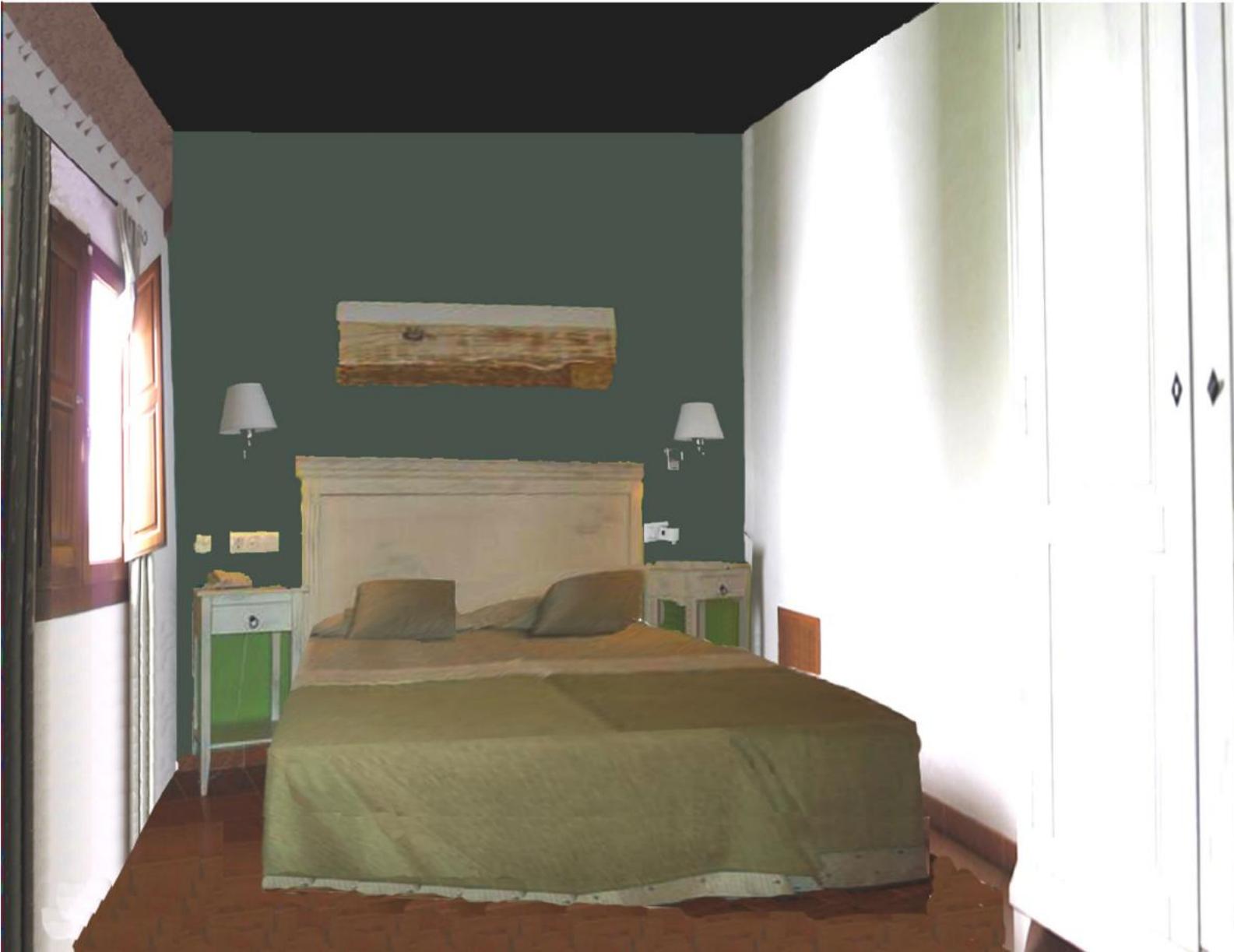
Accidental pinhole camera



Accidental pinhole camera



Accidental pinhole camera



Accidental pinhole camera



Accidental pinhole camera

Antonio Torralba, William T. Freeman
Computer Science and Artificial Intelligence Laboratory (CSAIL)
MIT
torralba@mit.edu, billf@mit.edu



Anti-pinhole or Pinspeck cameras

OPTICA ACTA, 1982, VOL. 29, NO. 1, 63-67

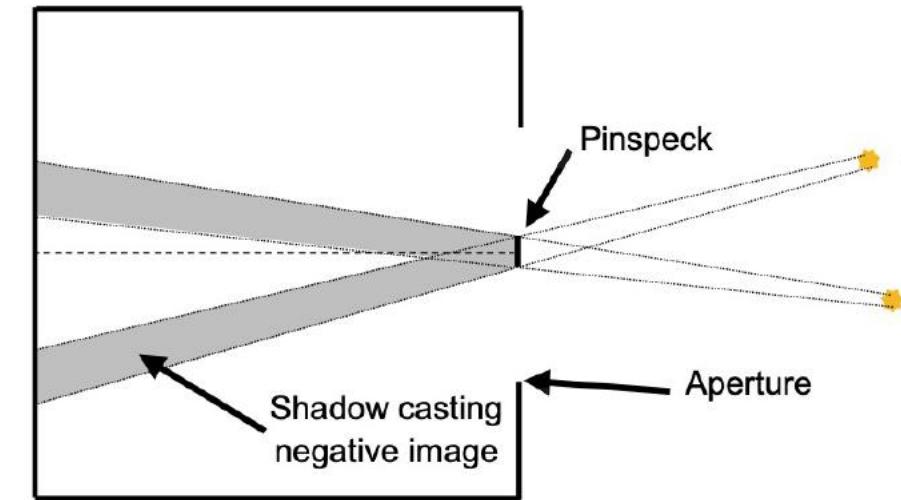
Anti-pinhole imaging

ADAM LLOYD COHEN

Parmly Research Institute, Loyola University of Chicago,
Chicago, Illinois 60626, U.S.A.

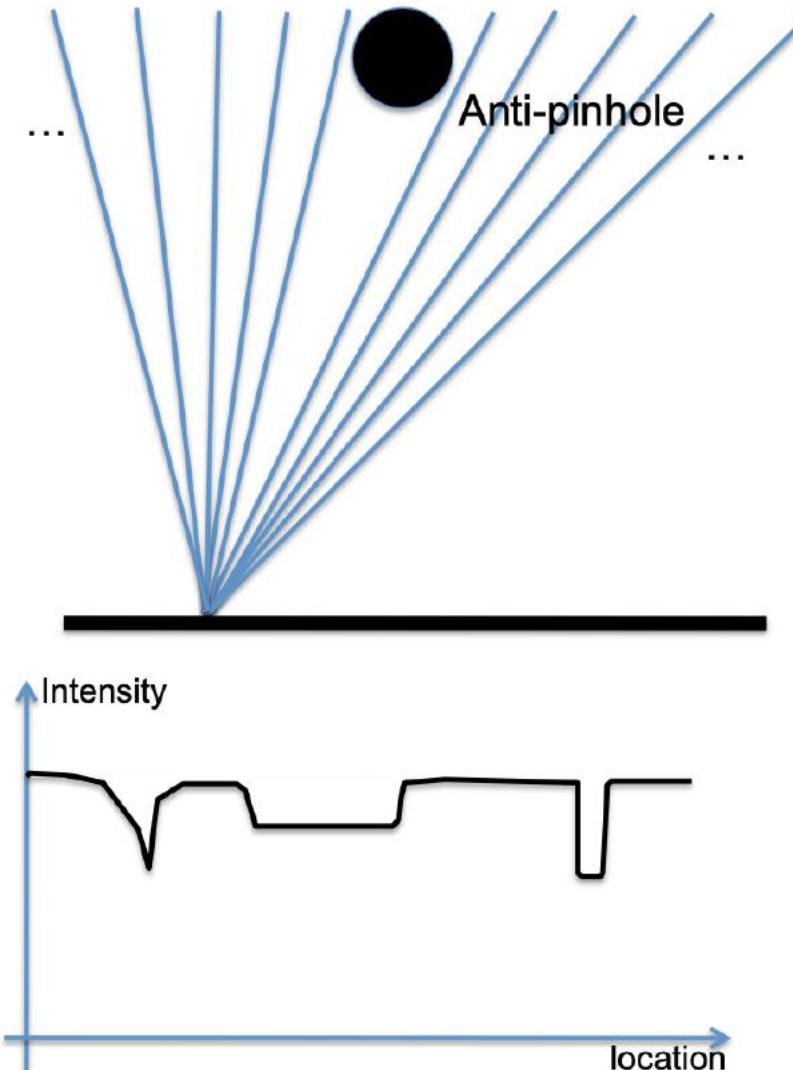
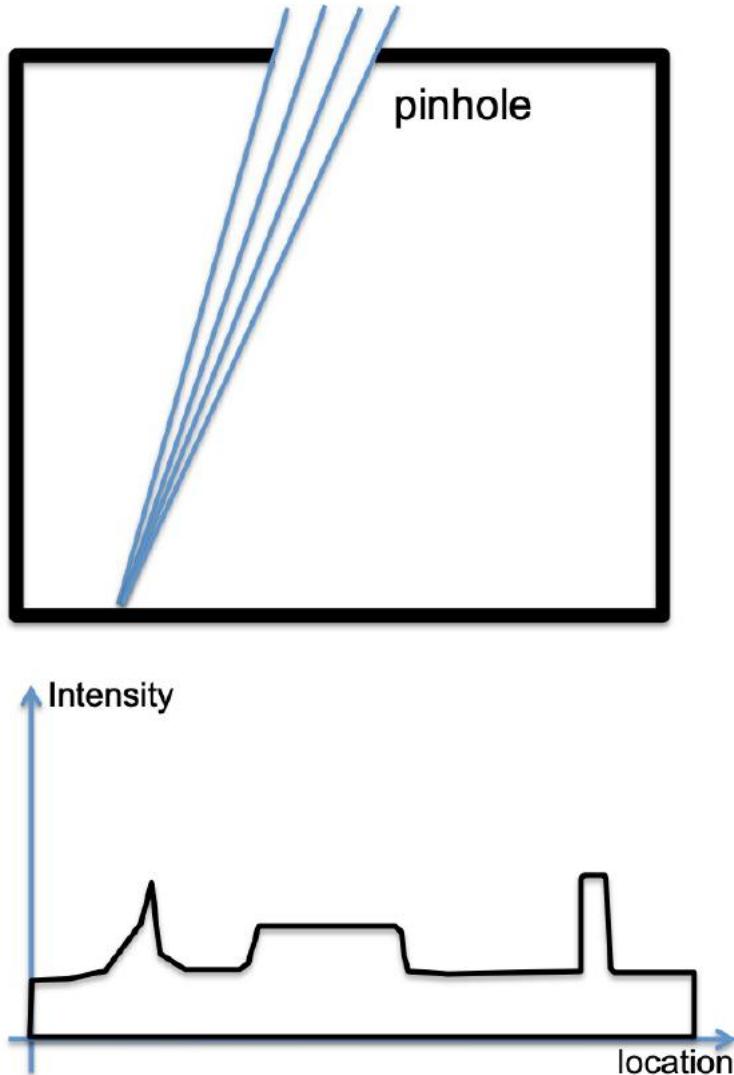
(Received 16 April 1981; revision received 8 July 1981)

Abstract. By complementing a pinhole to produce an isolated opaque spot, the light ordinarily blocked from the pinhole image is transmitted, and the light ordinarily transmitted is blocked. A negative geometrical image is formed, distinct from the familiar 'bright-spot' diffraction image. Anti-pinhole, or 'pinspeck' images are visible during a solar eclipse, when the shadows of objects appear crescent-shaped. Pinspecks demonstrate unlimited depth of field, freedom from distortion and large angular field. Images of different magnification may be formed simultaneously. Contrast is poor, but is improvable by averaging to remove noise and subtraction of a d.c. bias. Pinspecks may have application in X-ray space optics, and might be employed in the eyes of simple organisms.



A pinspeck camera is based on a wide aperture with a small speck in the middle. When objects are illuminating the camera, the speck is casting a shadow on the projection plane, effectively creating a negative image.

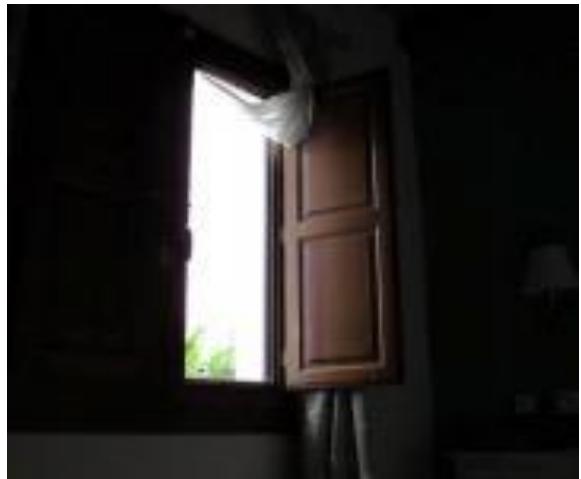
Pinhole and Anti-pinhole cameras



Adam L. Cohen, 1982

Accidental pinhole camera

projected pattern on the wall



window is an
aperture



upside down

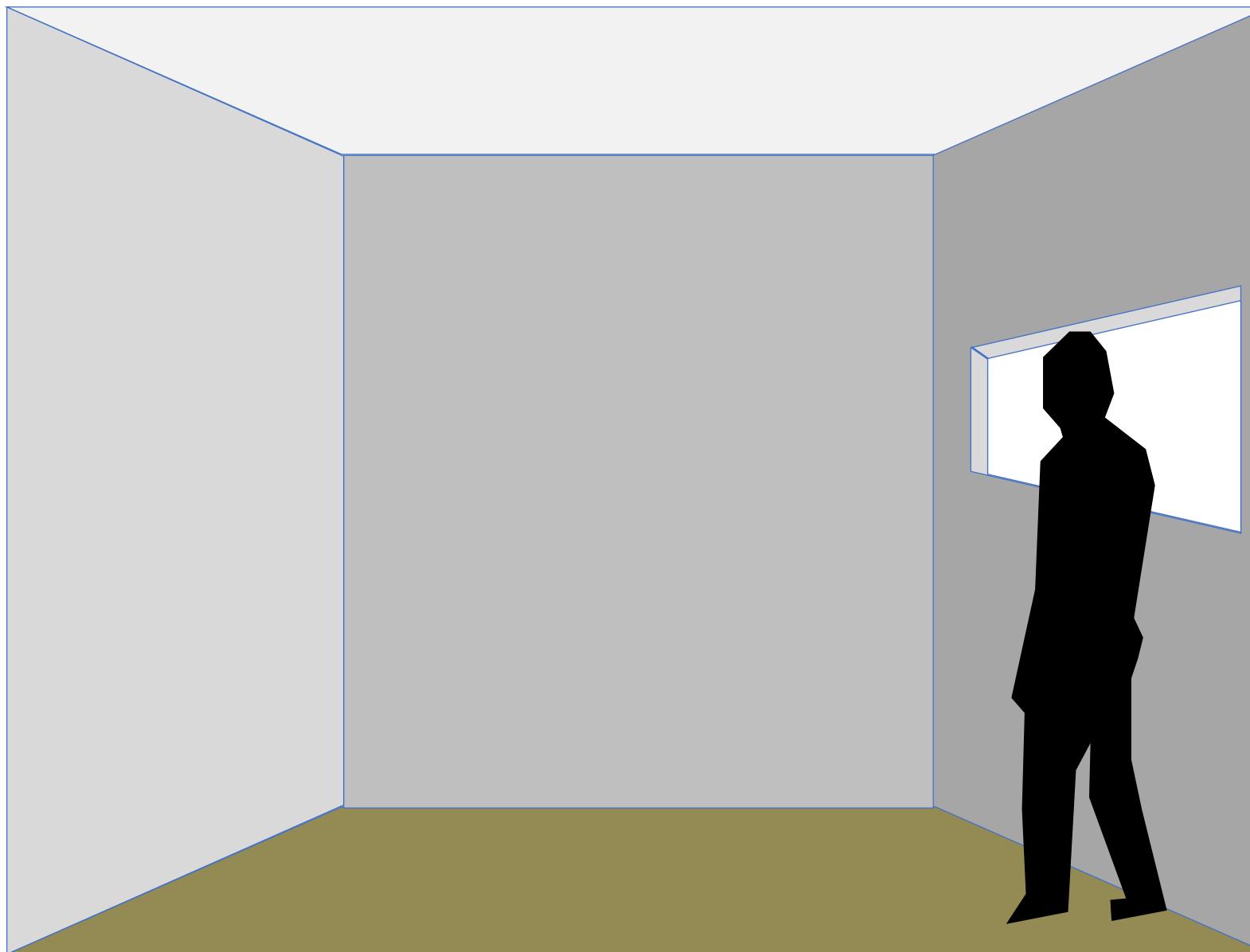
window with smaller gap



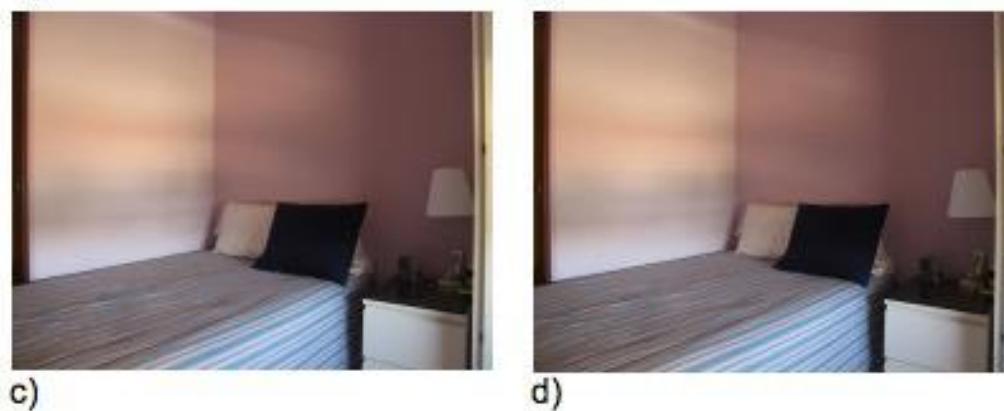
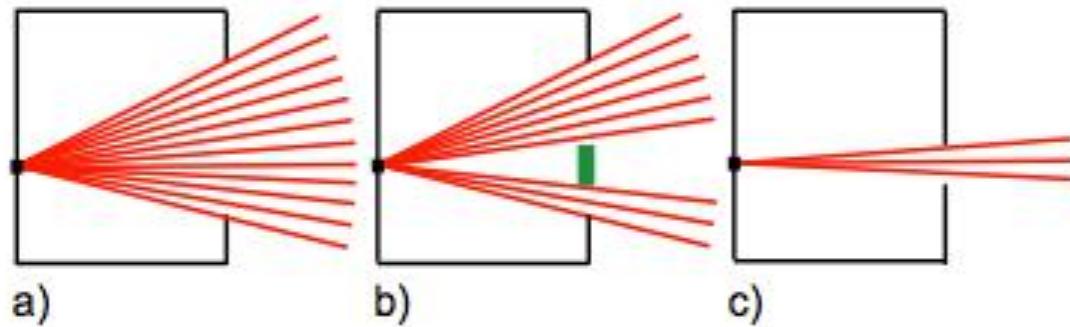
view outside window



Mixed accidental pinhole and anti-pinhole cameras



Accidental pinspeck camera



a) Difference image

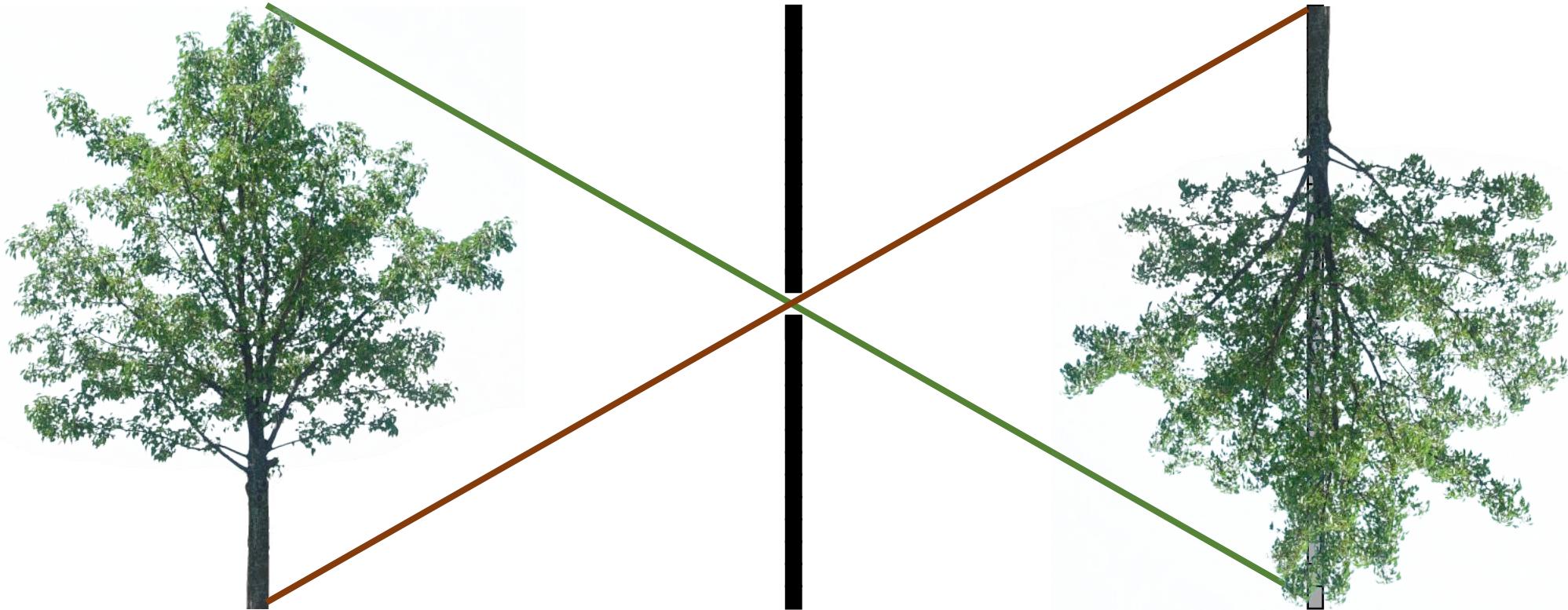


b) Difference upside down



c) True outdoor view

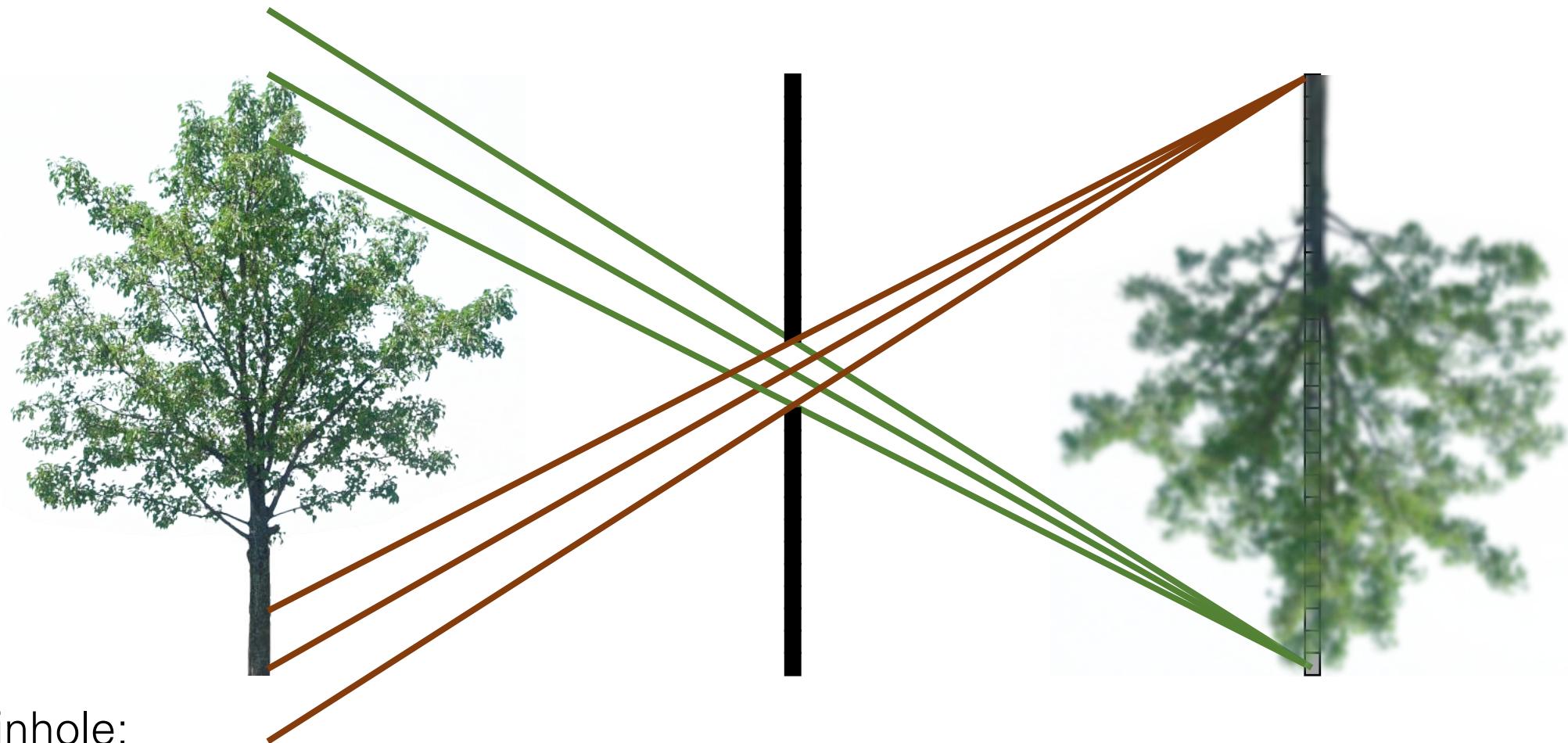
Pinhole camera trade-off



Small (ideal) pinhole:

1. Image is sharp.
2. Signal-to-noise ratio is low.

Pinhole camera trade-off

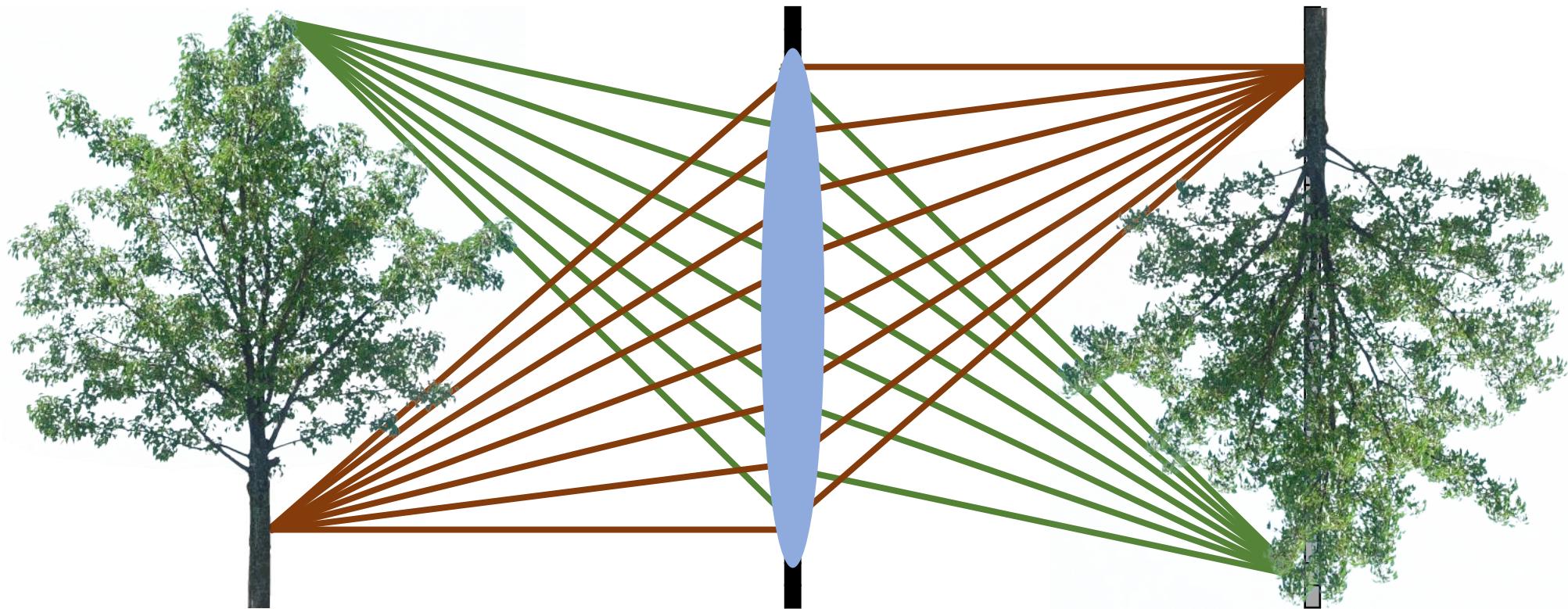


Large pinhole:

1. Image is blurry.
2. Signal-to-noise ratio is high.

Can we get best of both worlds?

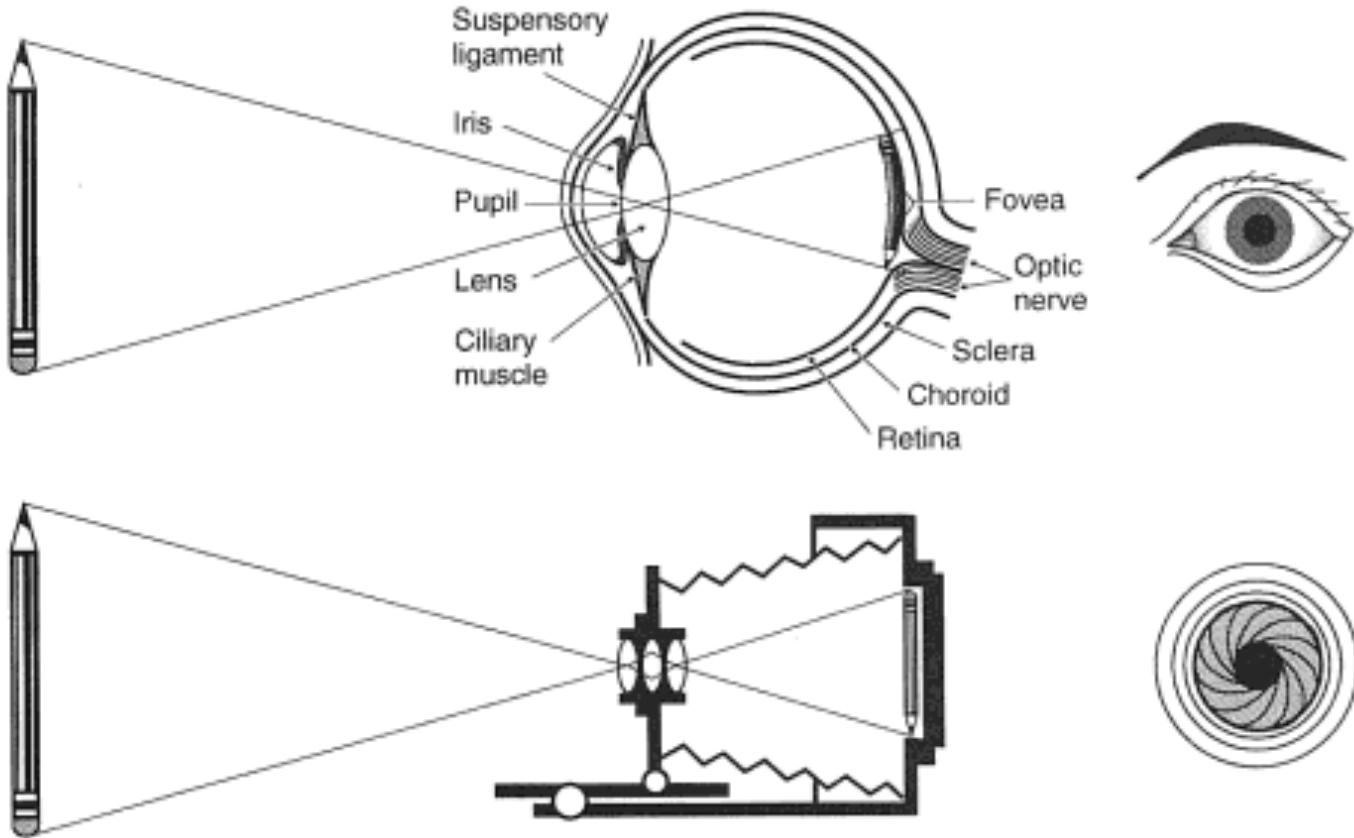
Almost, by using lenses



Lenses map “bundles” of rays from points on the scene to the sensor.

How does this mapping work exactly?

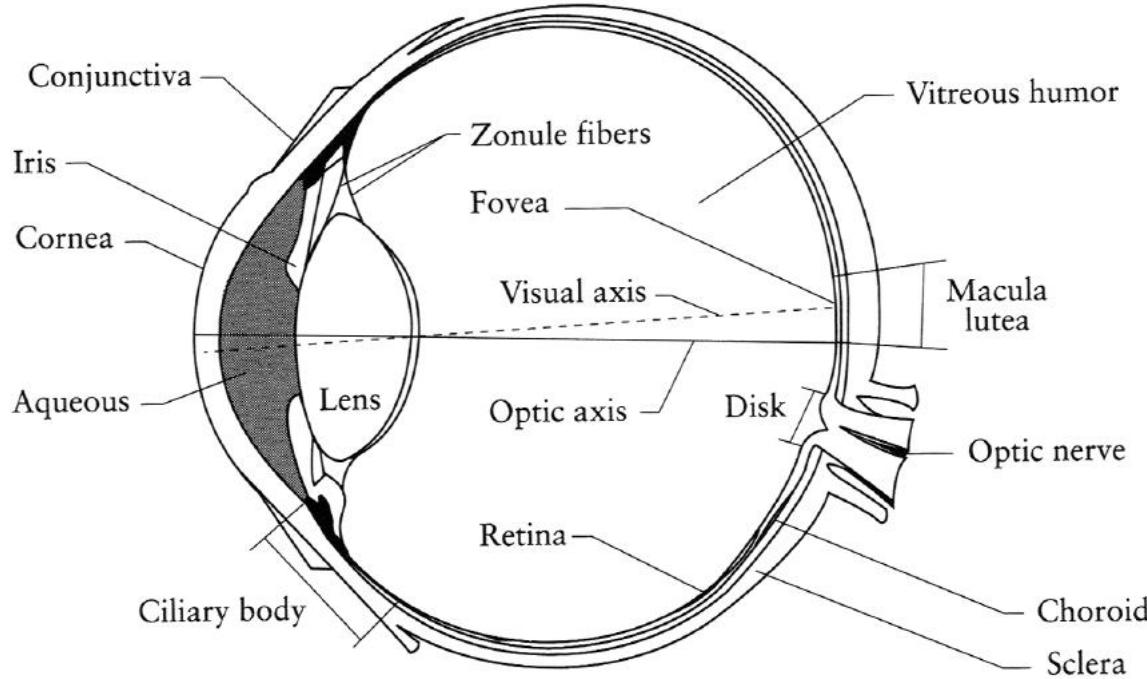
The Eye



Figures: Francis Crick, The Astonishing Hypothesis, 1995

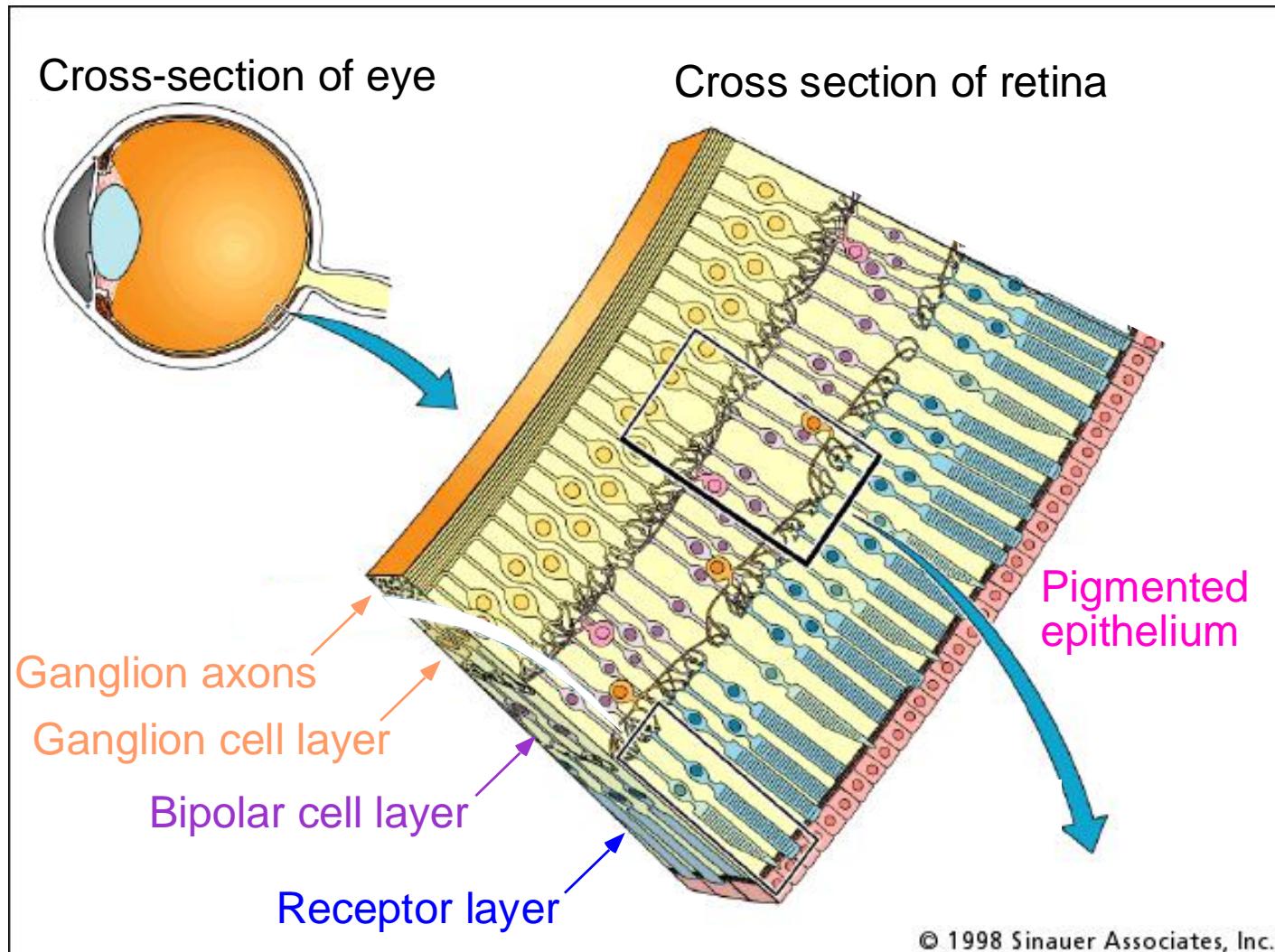
- The human eye is a camera

The Eye

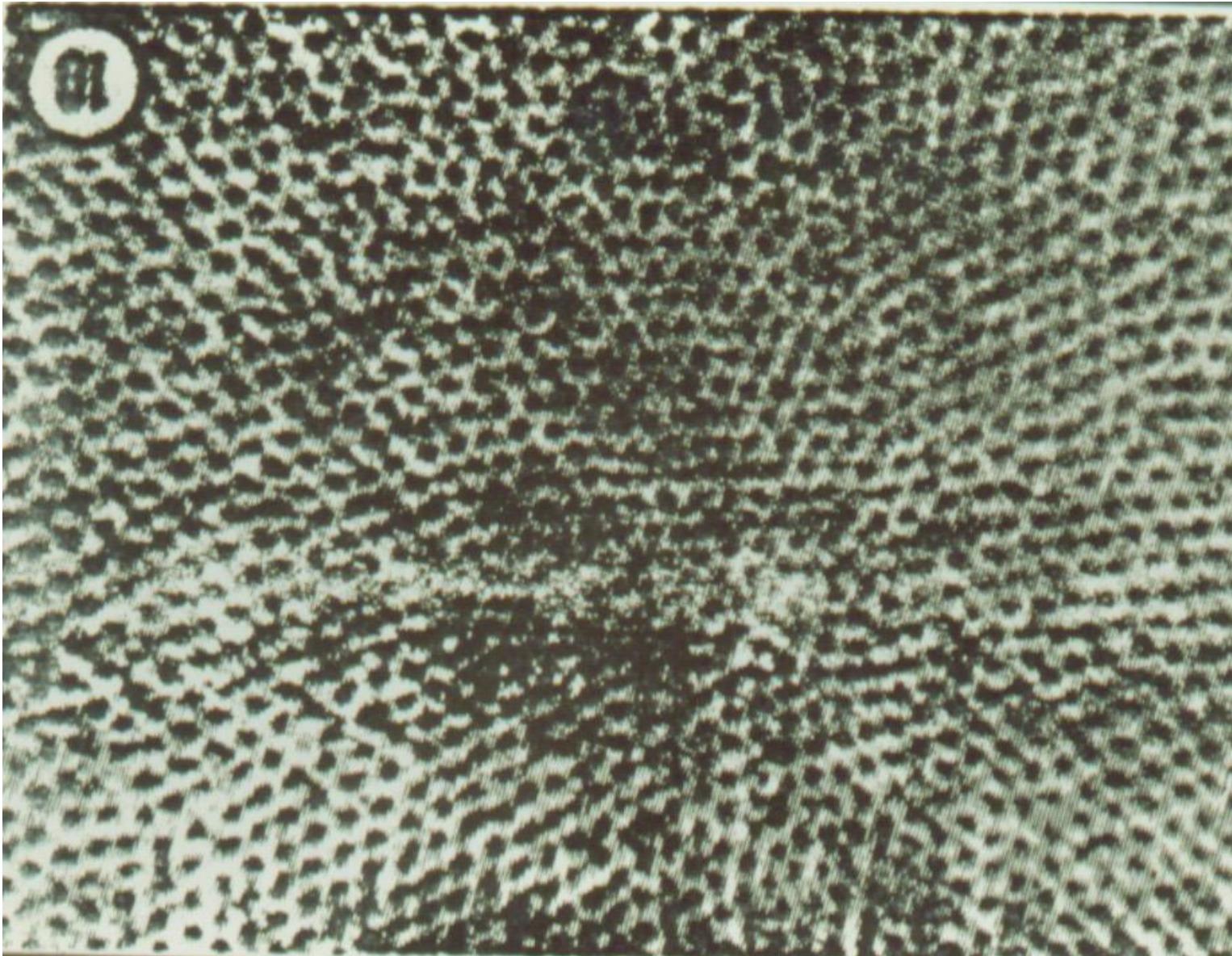


- The human eye is a camera!
 - Iris - colored annulus with radial muscles
 - Pupil - the hole (aperture) whose size is controlled by the iris
 - What's the "film"?
 - photoreceptor cells (rods and cones) in the retina

The Retina



Receptors Density - Fovea



64	66	76	85	99	100	101	101	106	112	117	118	105	77	57	50	51	43	52	55	62	
65	69	76	84	97	89	93	107	121	121	121	122	125	101	71	43	45	41	52	52	68	
66	72	78	83	91	86	91	102	108	104	106	113	136	118	86	43	49	47	60	55	64	
73	79	83	85	94	93	90	83	79	79	85	92	124	124	108	62	58	43	57	57	64	
78	84	86	86	69	71	68	68	86	108	115	109	117	135	139	93	73	37	49	58	70	
75	75	73	77	75	80	62	84	90	94	98	102	102	110	114	100	80	58	51	51	51	
77	72	73	83	84	91	80	77	71	70	73	80	80	87	99	103	93	67	53	50	51	
74	66	69	88	98	101	95	65	56	55	55	60	64	70	93	114	112	82	56	47	53	
64	59	66	86	108	103	98	54	52	57	54	54	67	77	103	124	125	96	64	46	53	
56	57	66	83	112	108	104	59	55	60	59	60	78	94	115	125	121	98	68	43	46	
56	58	66	80	114	121	117	85	71	67	69	76	87	101	116	117	112	94	68	43	46	
61	57	61	77	111	125	119	114	98	87	87	94	97	102	111	113	108	90	65	43	44	
63	52	54	73	103	117	107	126	119	108	103	104	106	103	108	115	112	91	65	48	42	
66	63	58	63	94	115	120	108	102	104	106	108	105	108	107	105	105	97	72	47	41	
68	65	58	61	86	108	115	106	102	103	103	104	98	99	97	97	103	101	81	57	43	
72	68	62	64	78	102	111	105	101	101	103	99	98	96	97	104	104	86	63	48		
74	71	64	64	69	93	104	99	94	93	96	101	99	101	102	103	108	106	90	69	53	

Animal Eyes

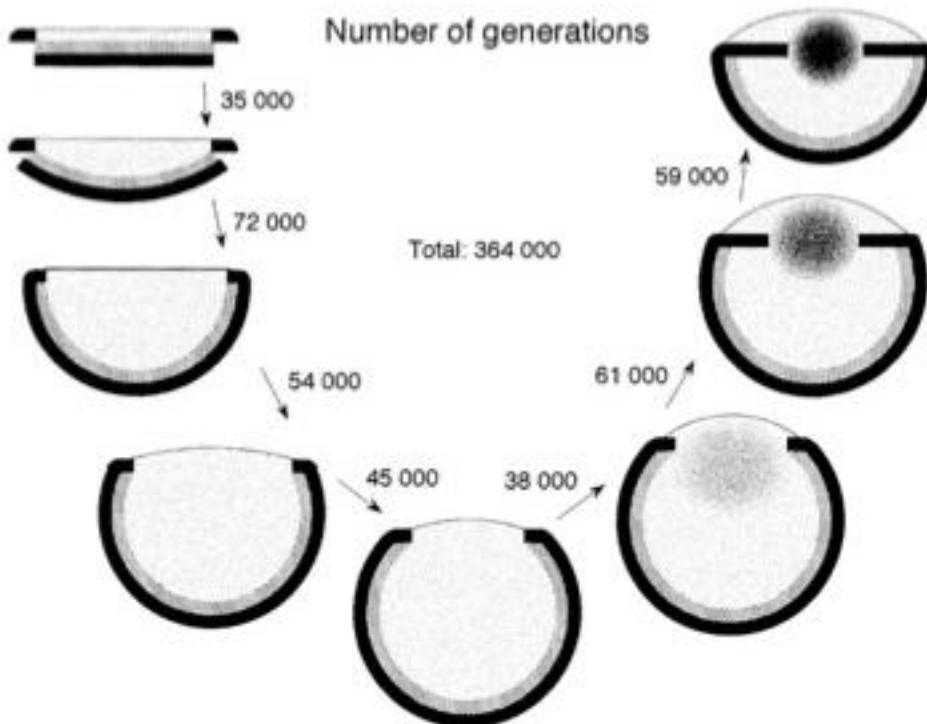
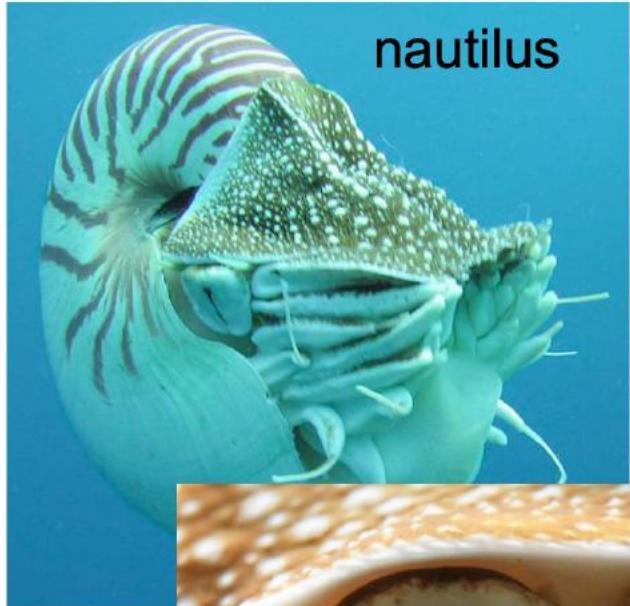
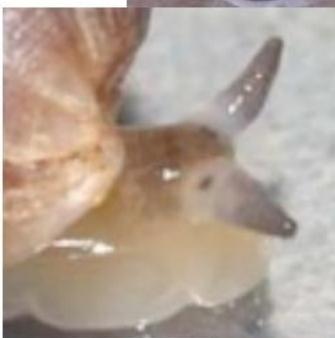


Fig. 1.6 A patch of light sensitive epithelium can be gradually turned into a perfectly focussed camera-type eye if there is a continuous selection for improved spatial vision. A theoretical model based on conservative assumptions about selection pressure and the amount of variation in natural populations suggest that the whole sequence can be accomplished amazingly fast, in less than 400 000 generations. The number of generations is also given between each of the consecutive intermediates that are drawn in the figure. The starting point is a flat piece of epithelium with an outer protective layer, an intermediate layer of receptor cells, and a bottom layer of pigment cells. The first half of the sequence is the formation of a pigment cup eye. When this principle cannot be improved any further, a lens gradually evolves. Modified from Nilsson and Pelger (1994).

Natural Eyes



lenses



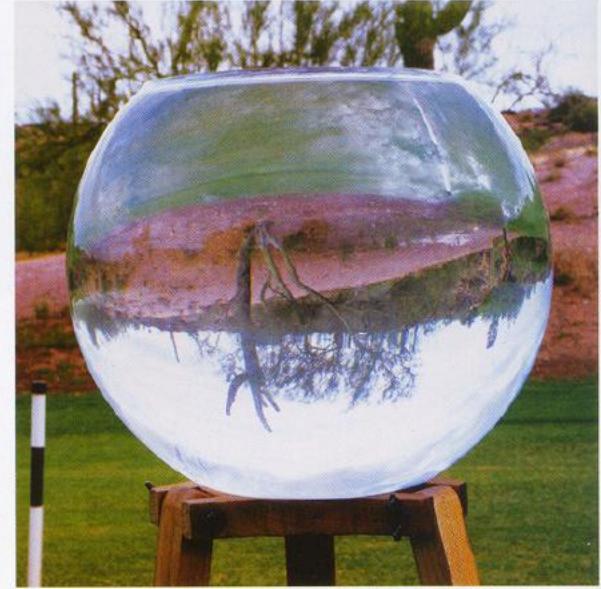
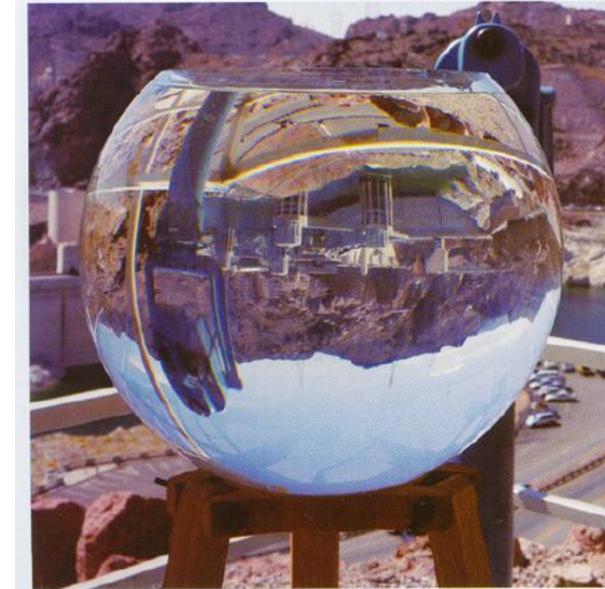
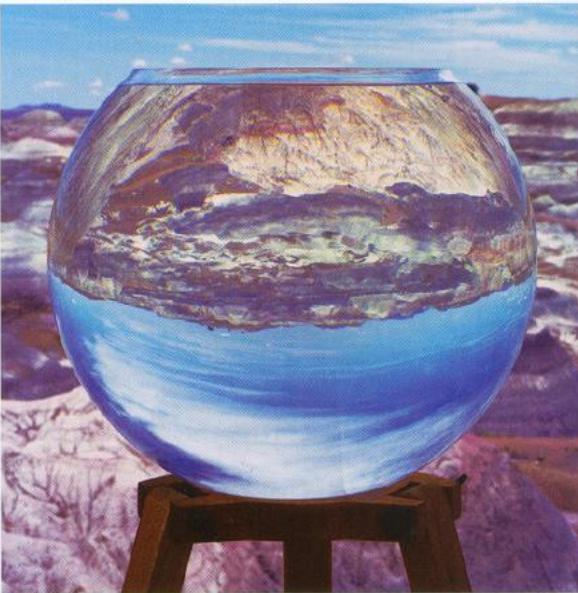
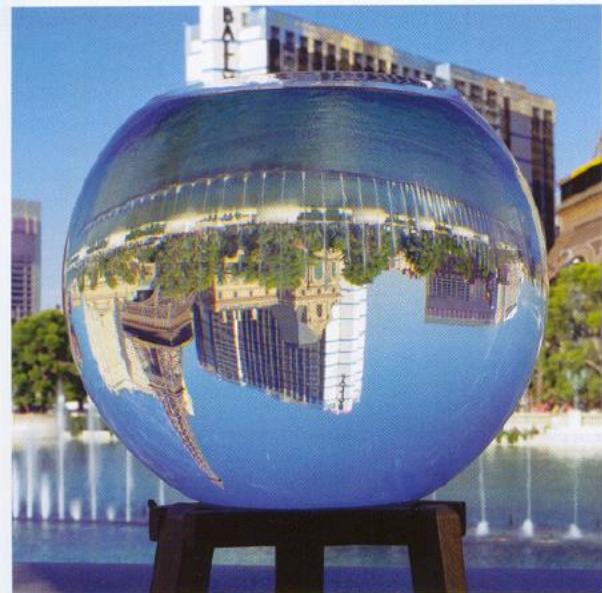
pinhole



pinspeck

Lens (very) basics

Replacing pinholes with lenses



Niepce "View from the Window at Le Gras", 1826

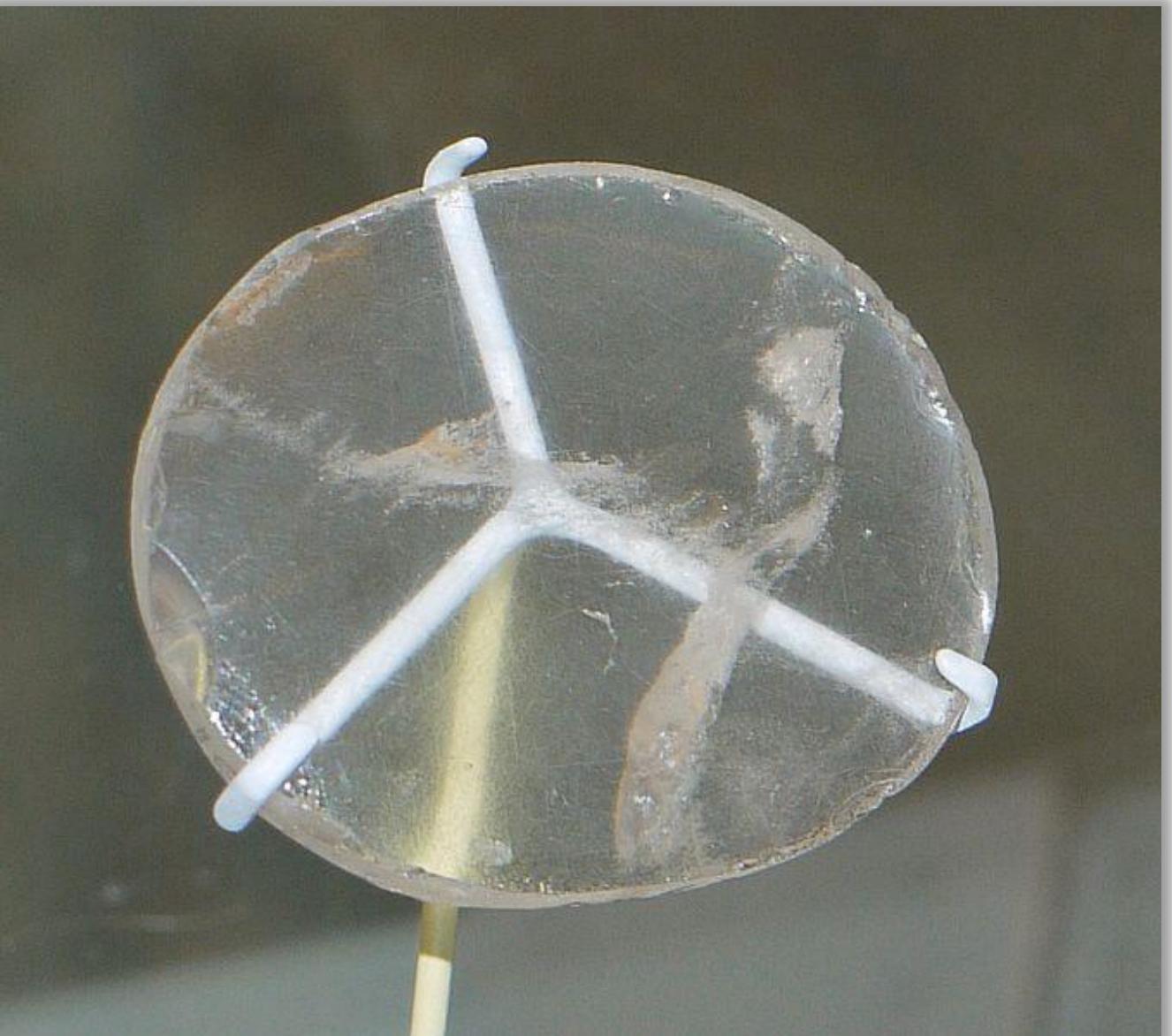


1826
8h exp



Lenses

- focus light
- magnify objects



Nimrud lens - 2700 years old

Lenses



Lenses

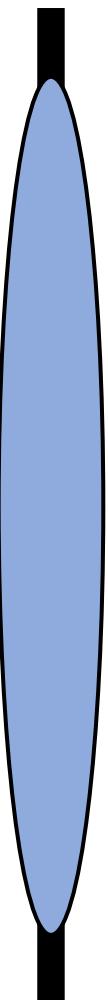


Lenses



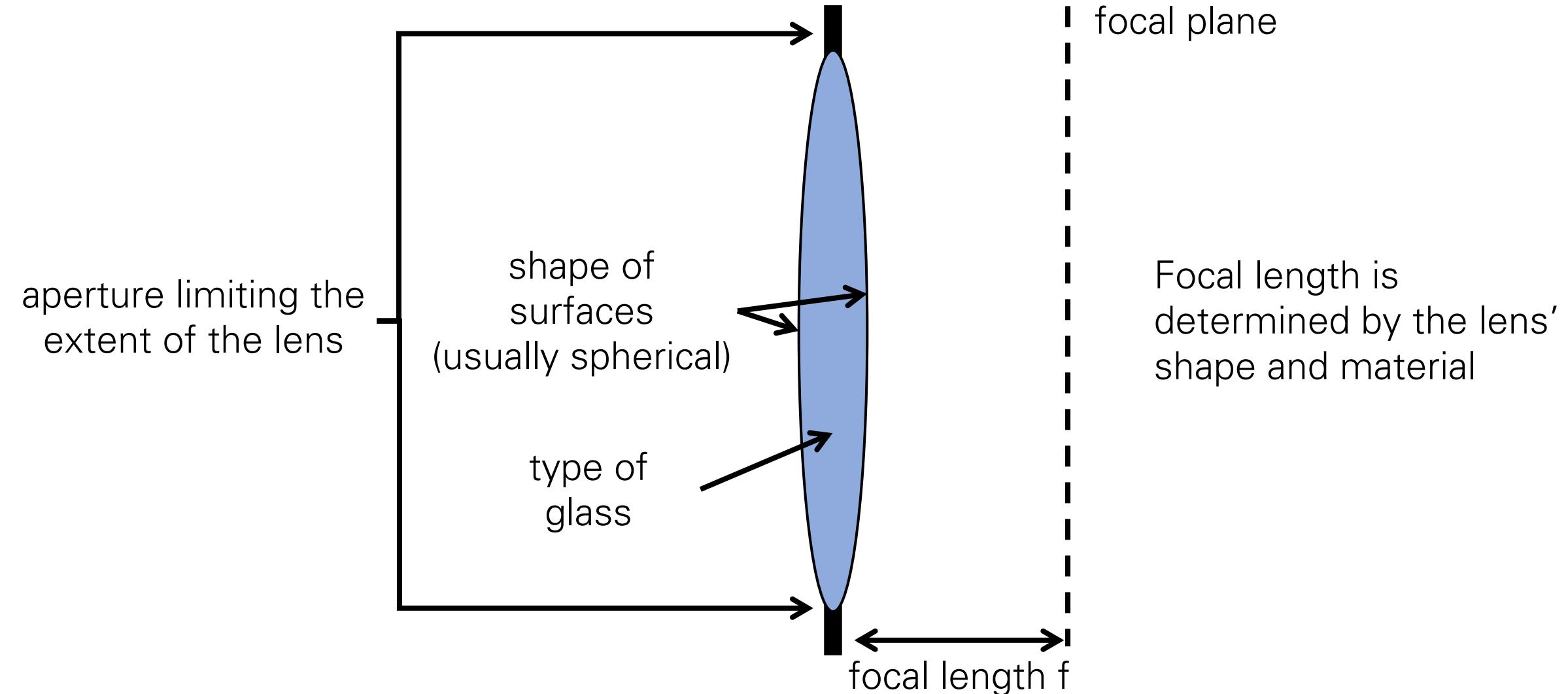
What is a lens?

A piece of glass manufactured to have a specific shape



What is a lens?

A piece of glass manufactured to have a specific shape



The lens on your camera

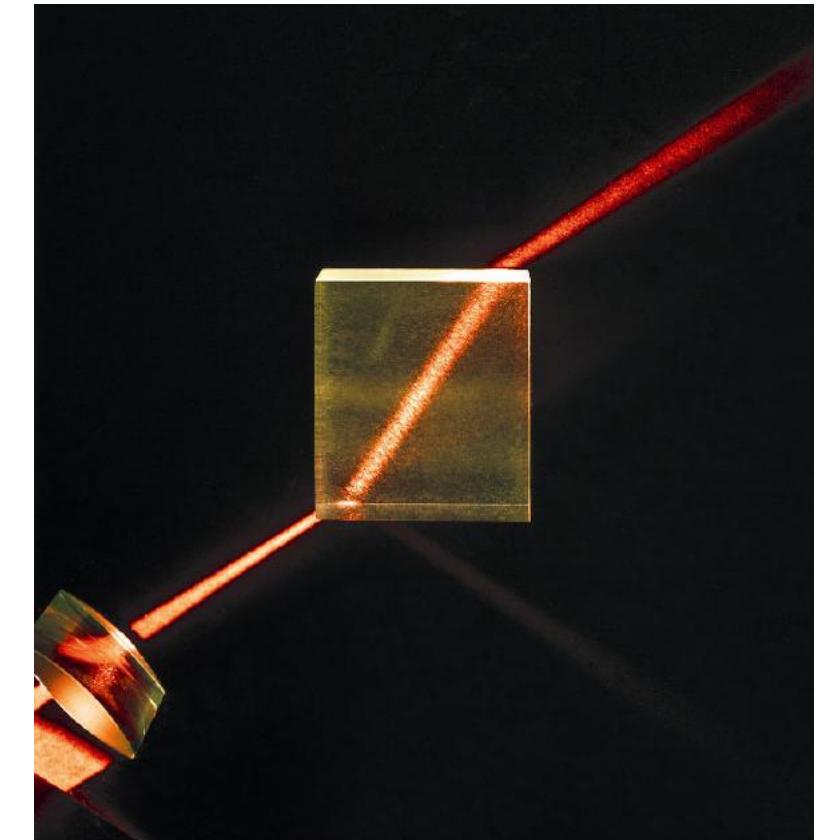
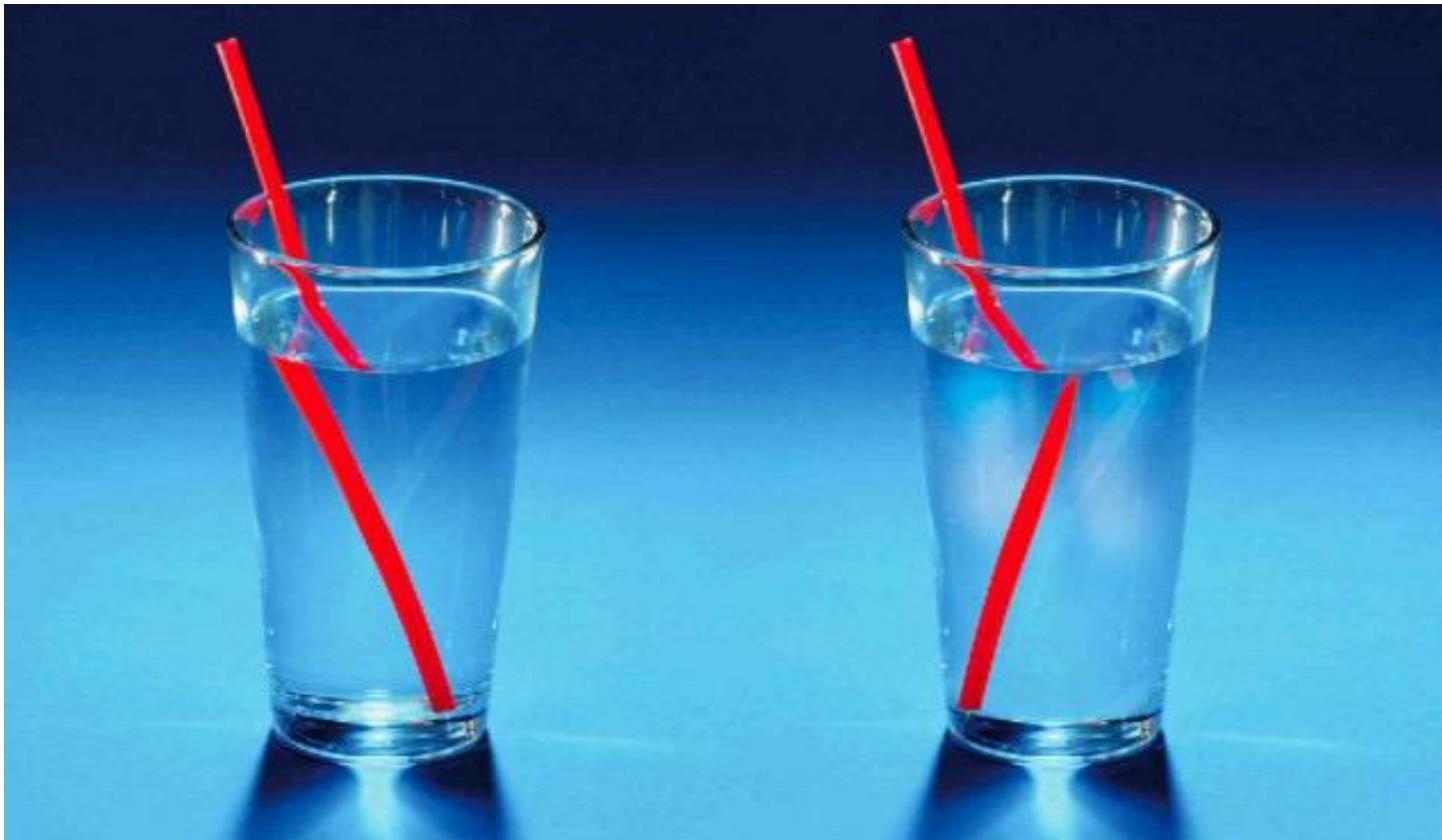


How does a lens work?



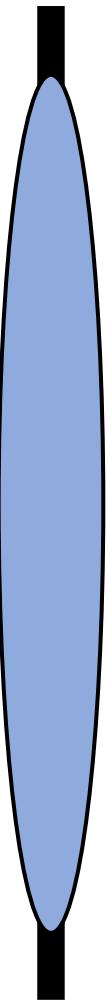
Refraction

Refraction is the bending of rays of light when they move from one material to another



How does a lens work?

Lenses are designed so that their refraction makes light rays bend in a very specific way.



The thin lens model

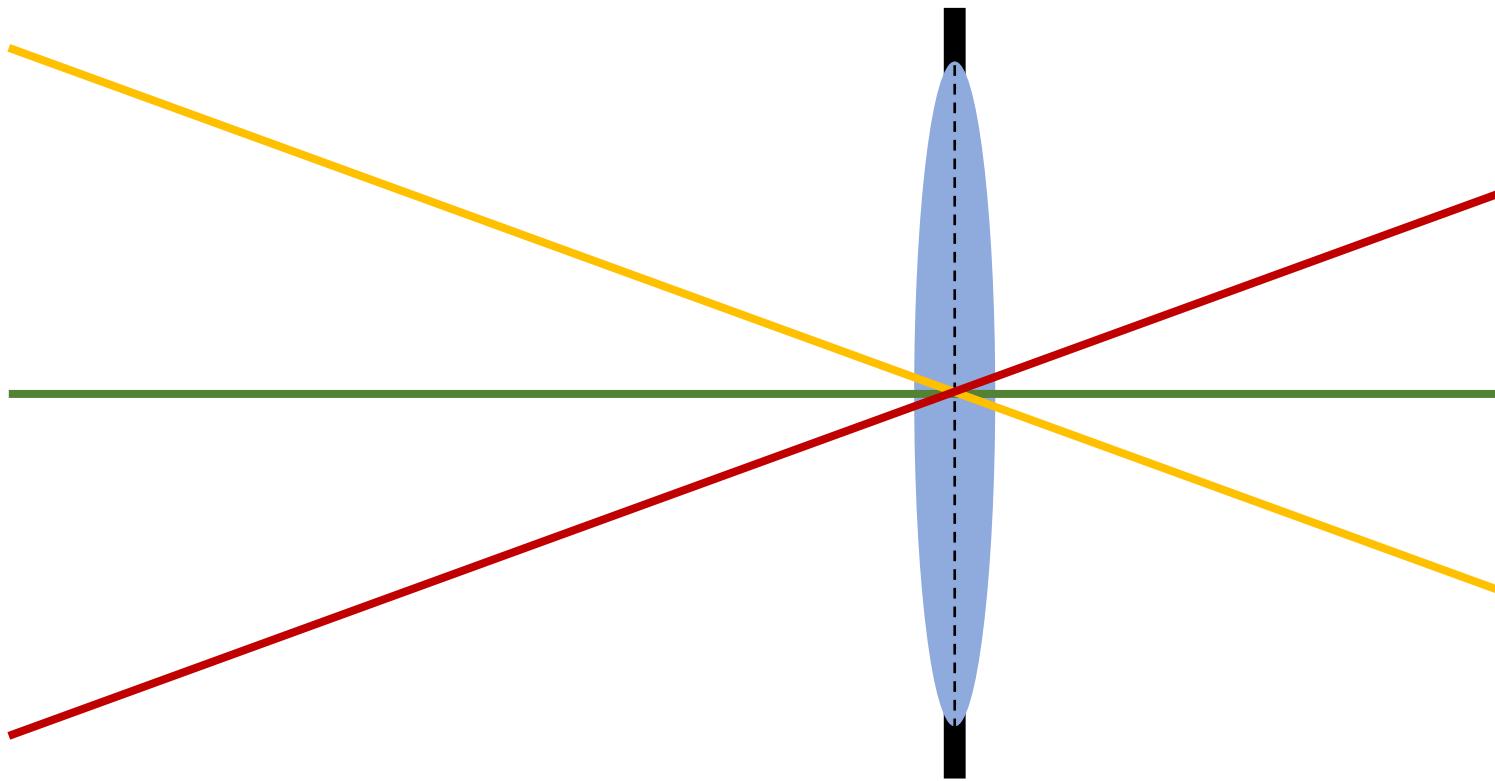
Thin lens model

Simplification of geometric optics for well-designed lenses.



Thin lens model

Simplification of geometric optics for well-designed lenses.

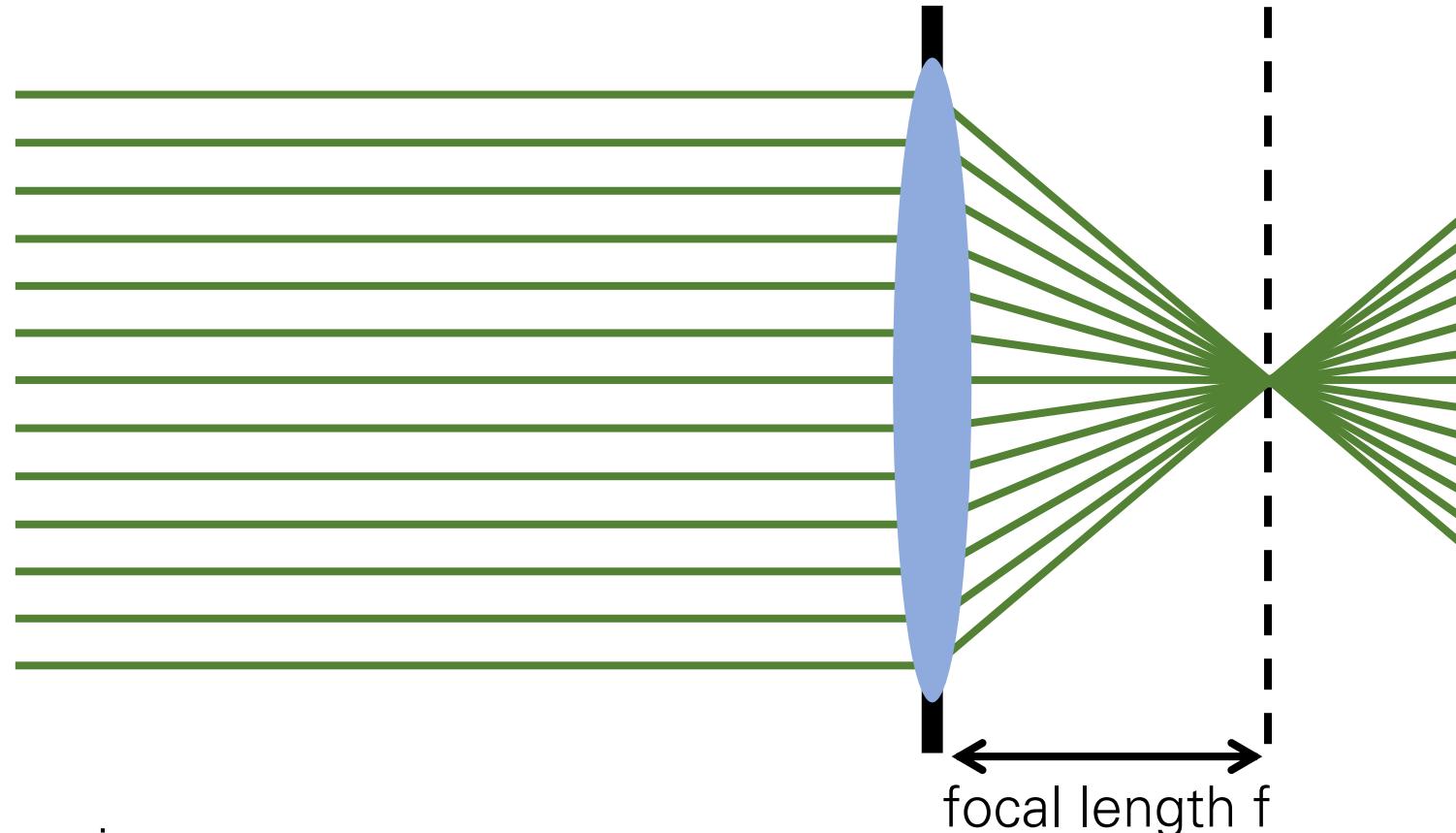


Two assumptions:

1. Rays passing through lens center are unaffected.

Thin lens model

Simplification of geometric optics for well-designed lenses.

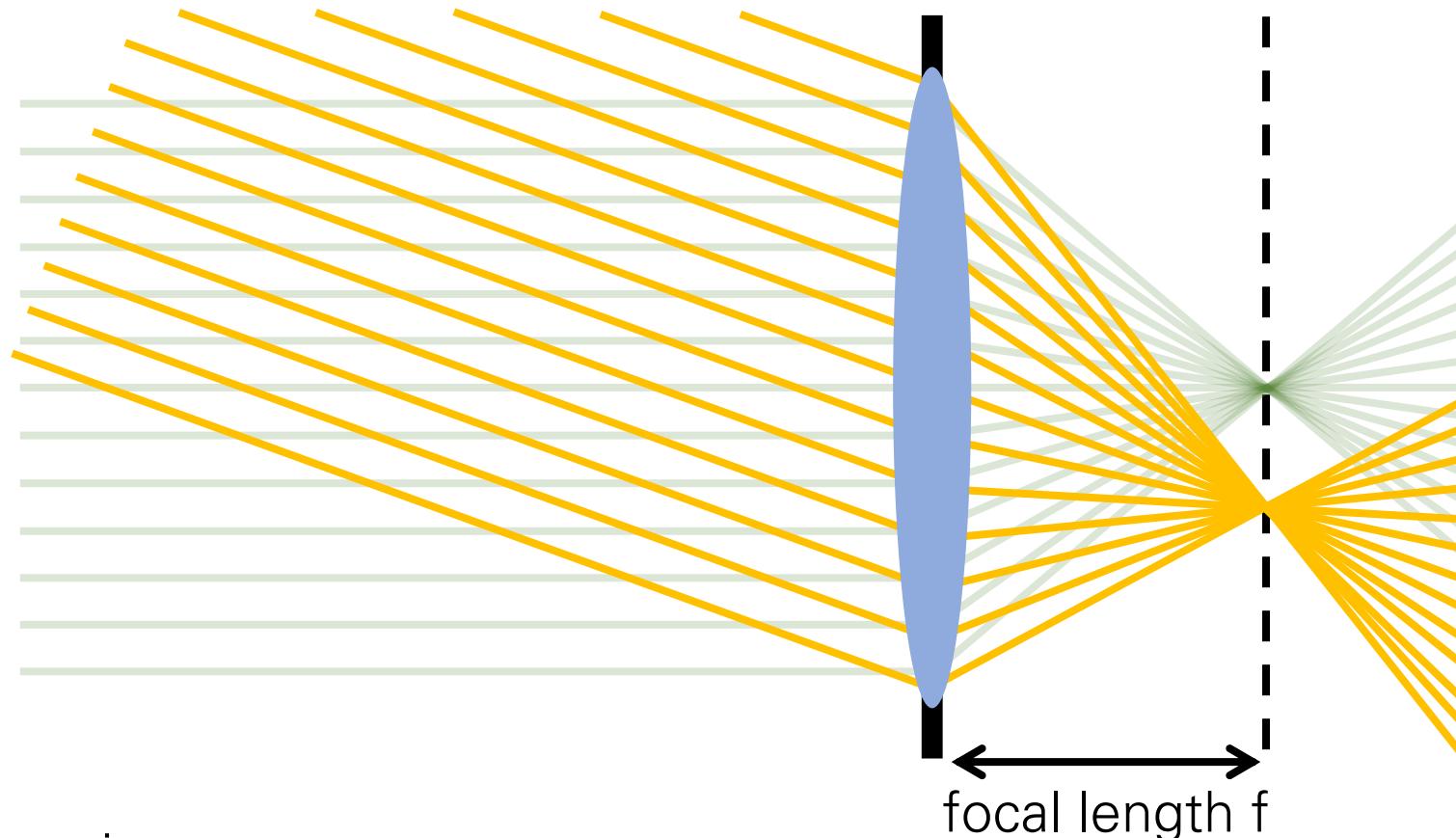


Two assumptions:

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2. Parallel rays converge to a single point located on focal plane.

Thin lens model

Simplification of geometric optics for well-designed lenses.

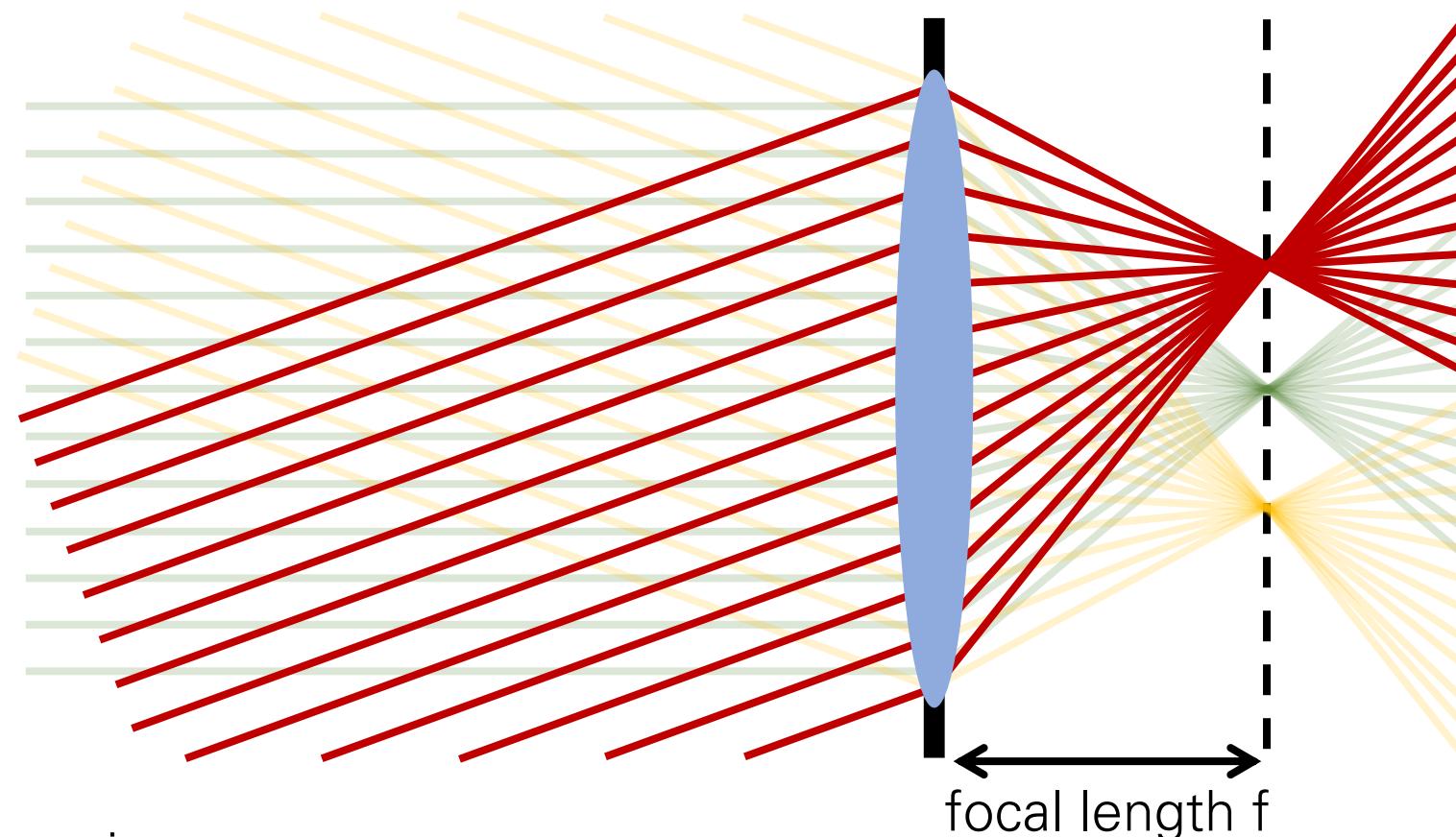


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Thin lens model

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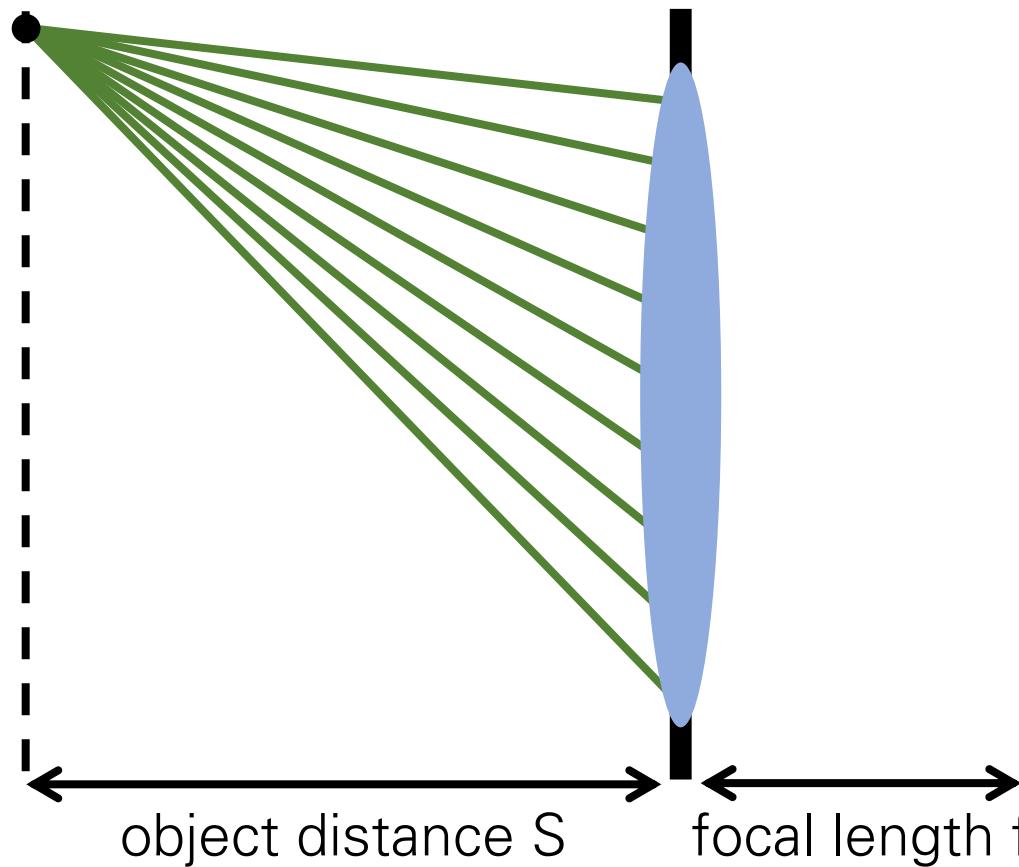


Two assumptions:

1. Rays passing through lens center are unaffected.
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Tracing rays through a thin lens

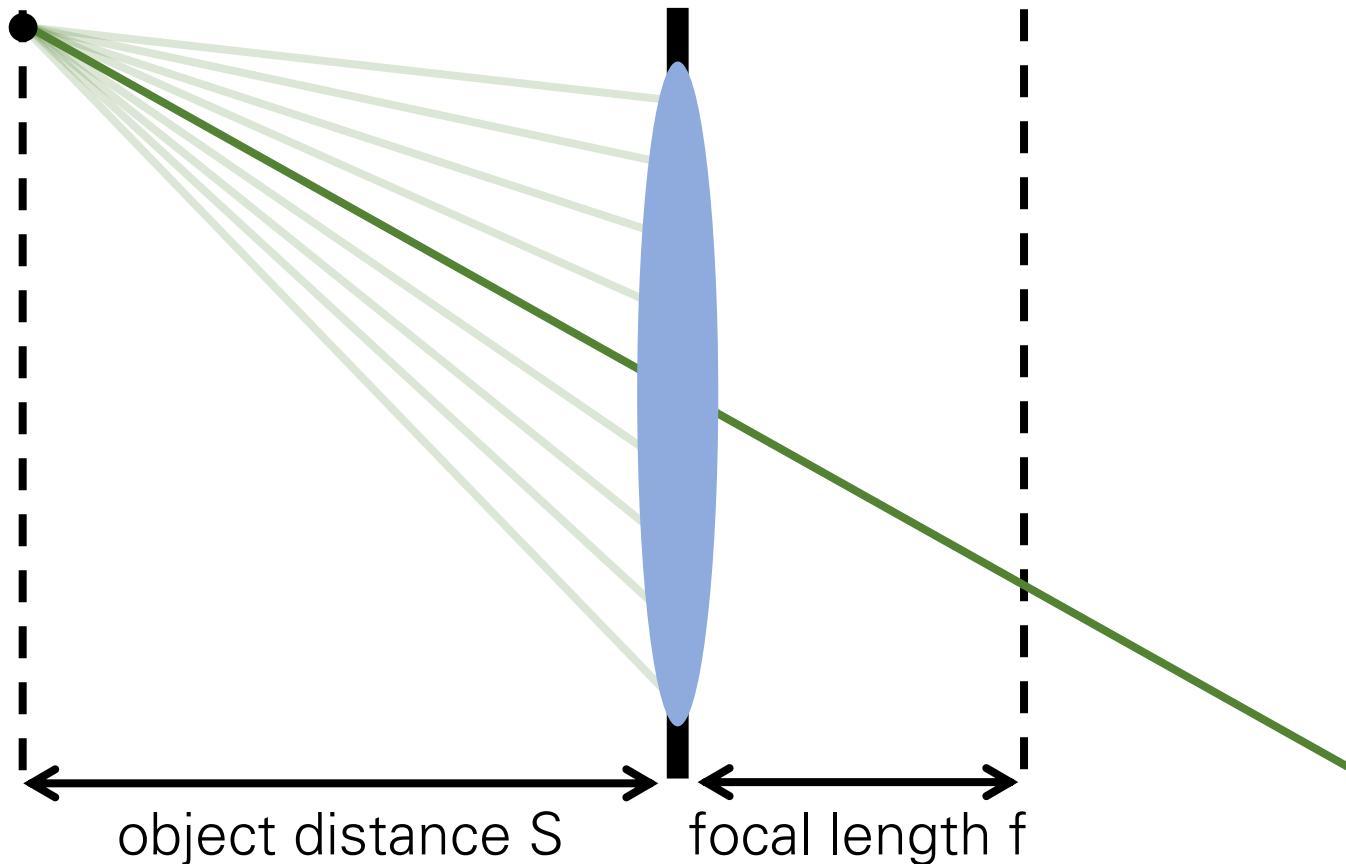
Consider an object emitting a bundle of rays. How do they propagate through the lens?



Tracing rays through a thin lens

Consider an object emitting a bundle of rays. How do they propagate through the lens?

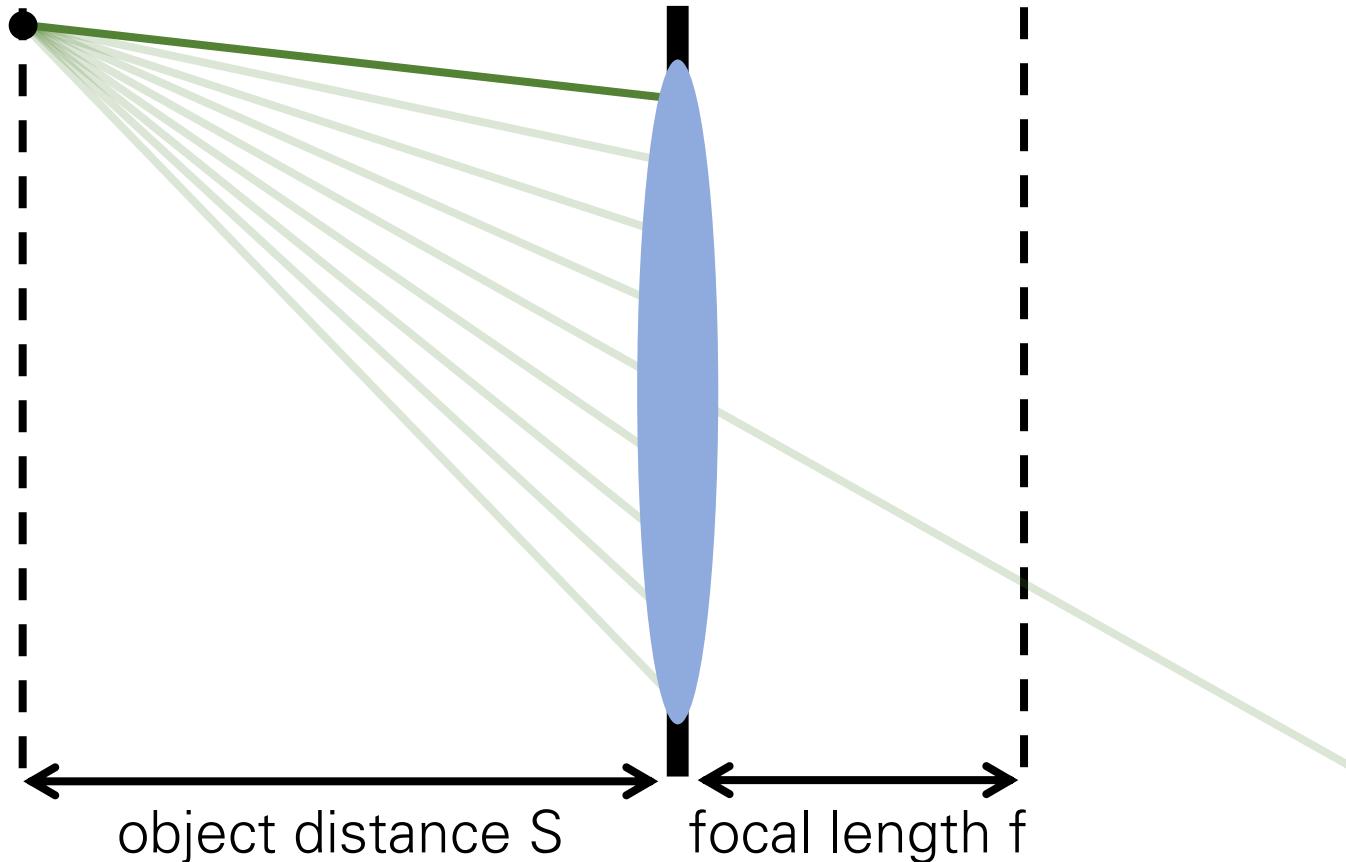
1. Trace rays through lens center.



Tracing rays through a thin lens

Consider an object emitting a bundle of rays. How do they propagate through the lens?

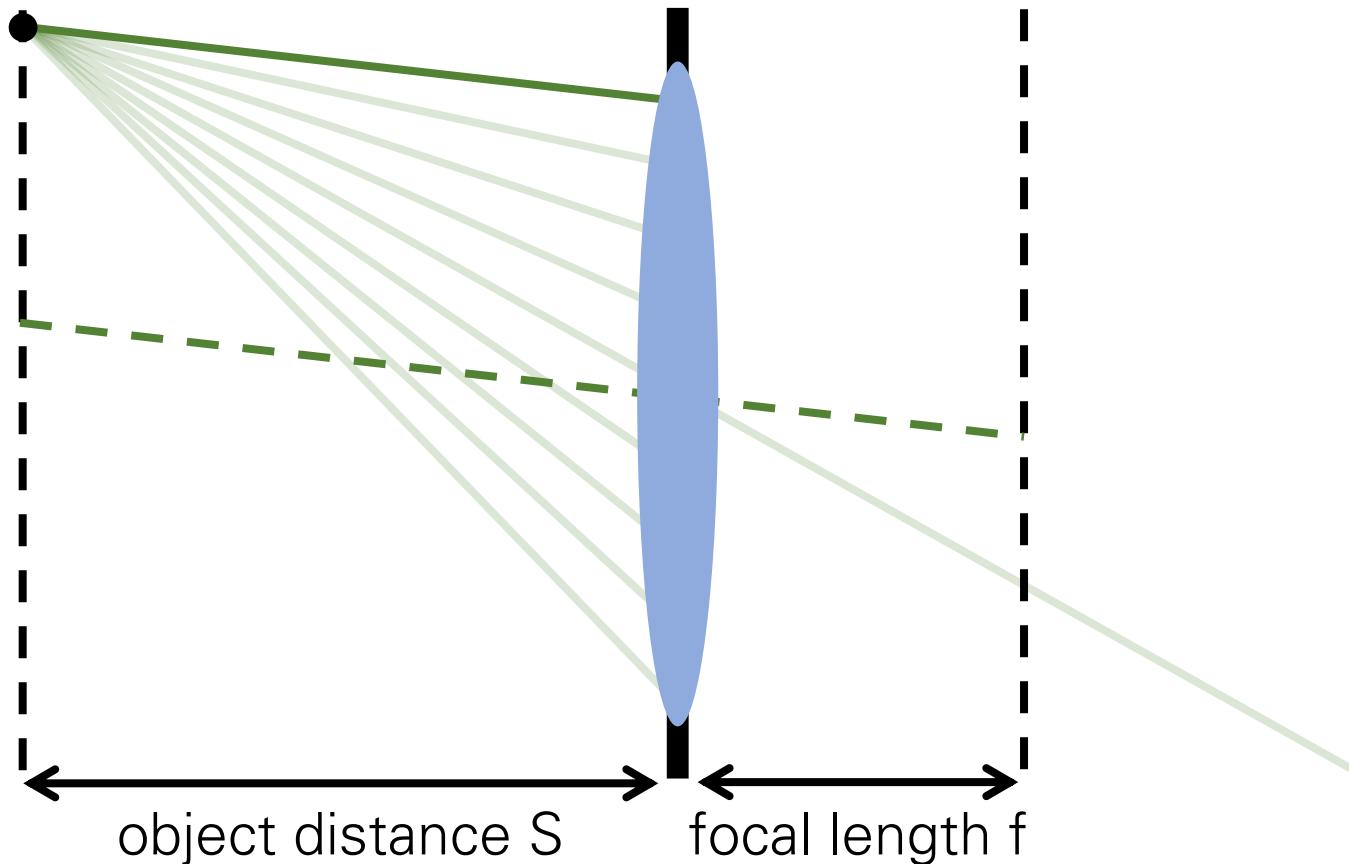
1. Trace rays through lens center.
2. For all other rays:



Tracing rays through a thin lens

Consider an object emitting a bundle of rays. How do they propagate through the lens?

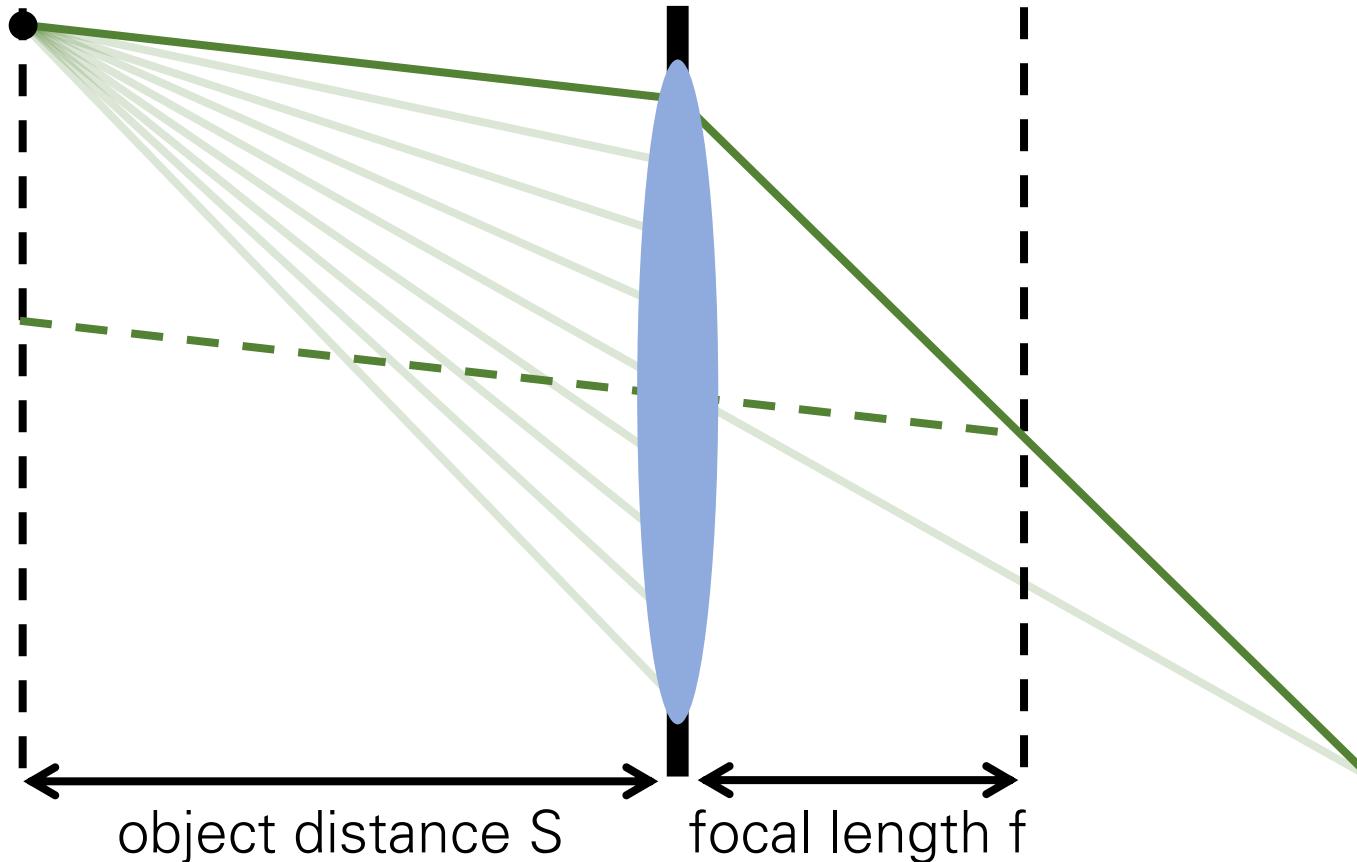
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2. For all other rays:
 - a. Trace their parallel through lens center.



Tracing rays through a thin lens

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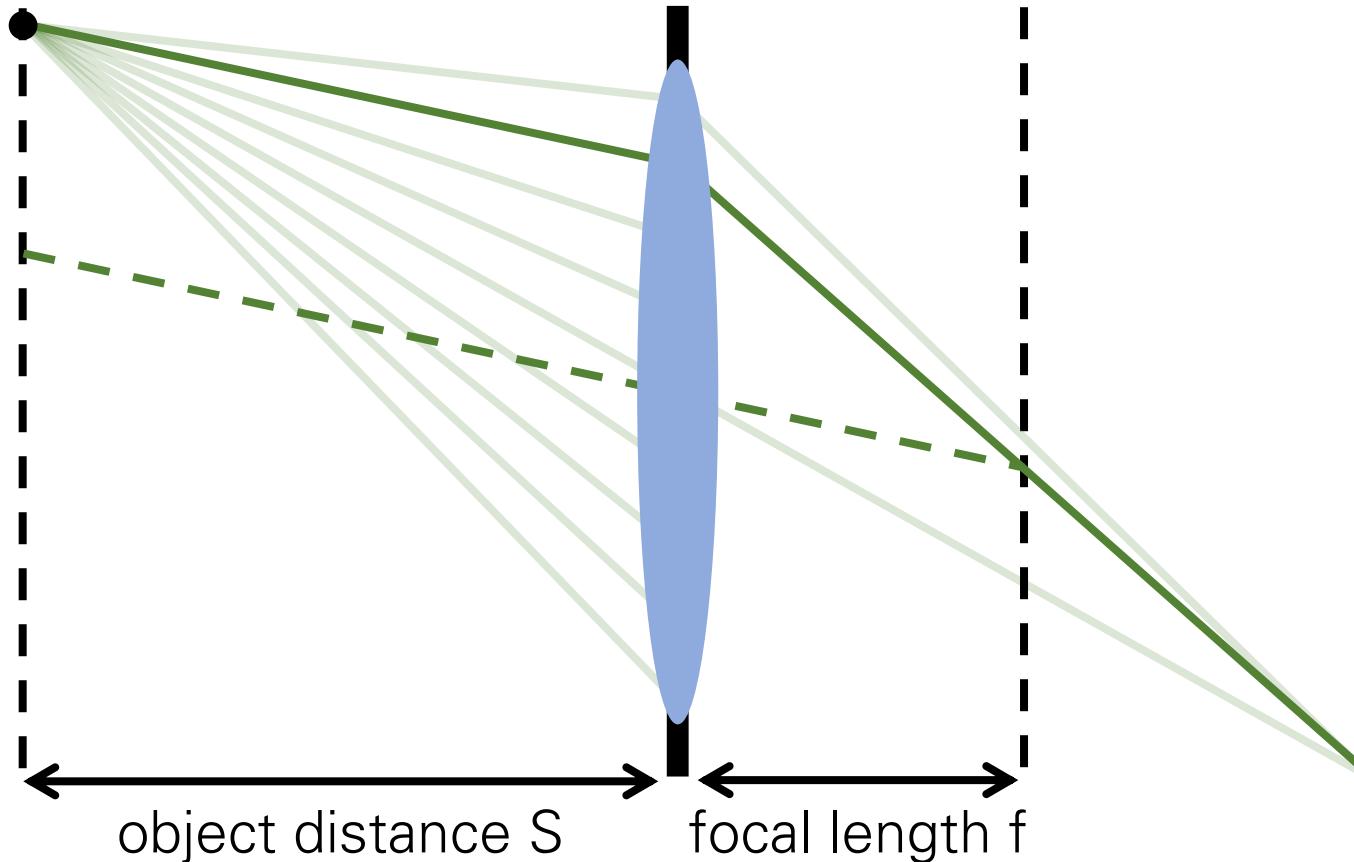
1. Trace rays through lens center.
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 - a. Trace their parallel through lens center.
 - b. Connect on focal plane.



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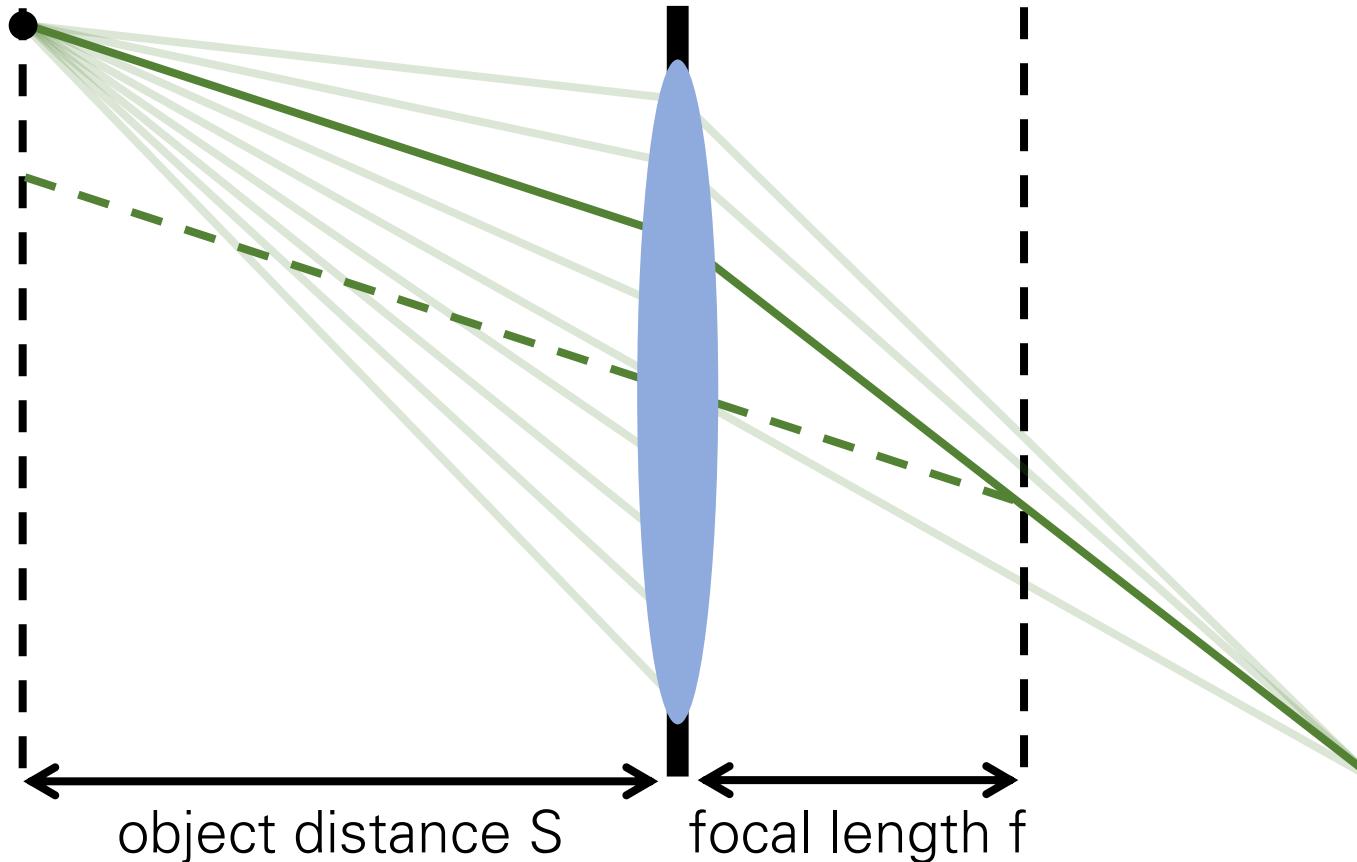
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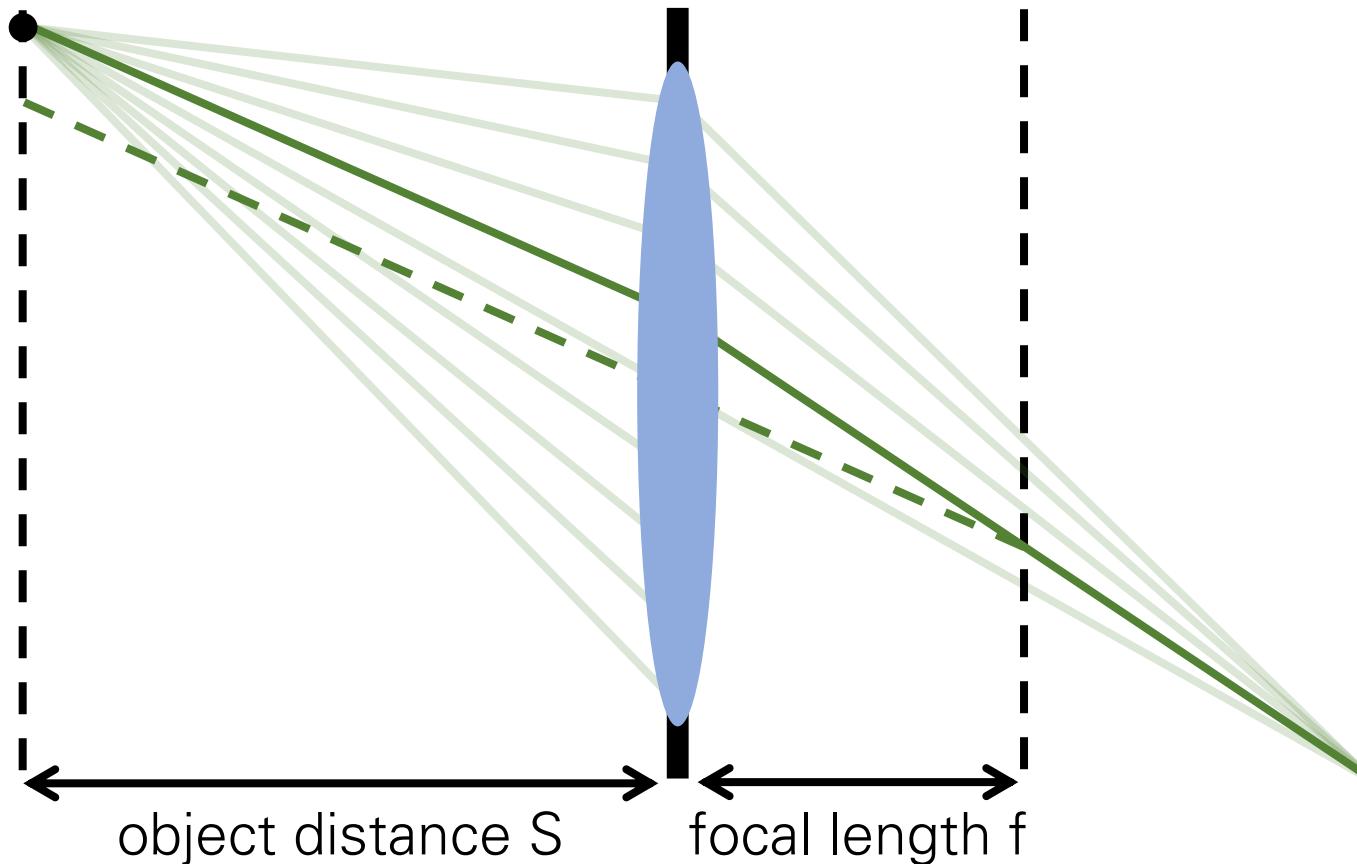
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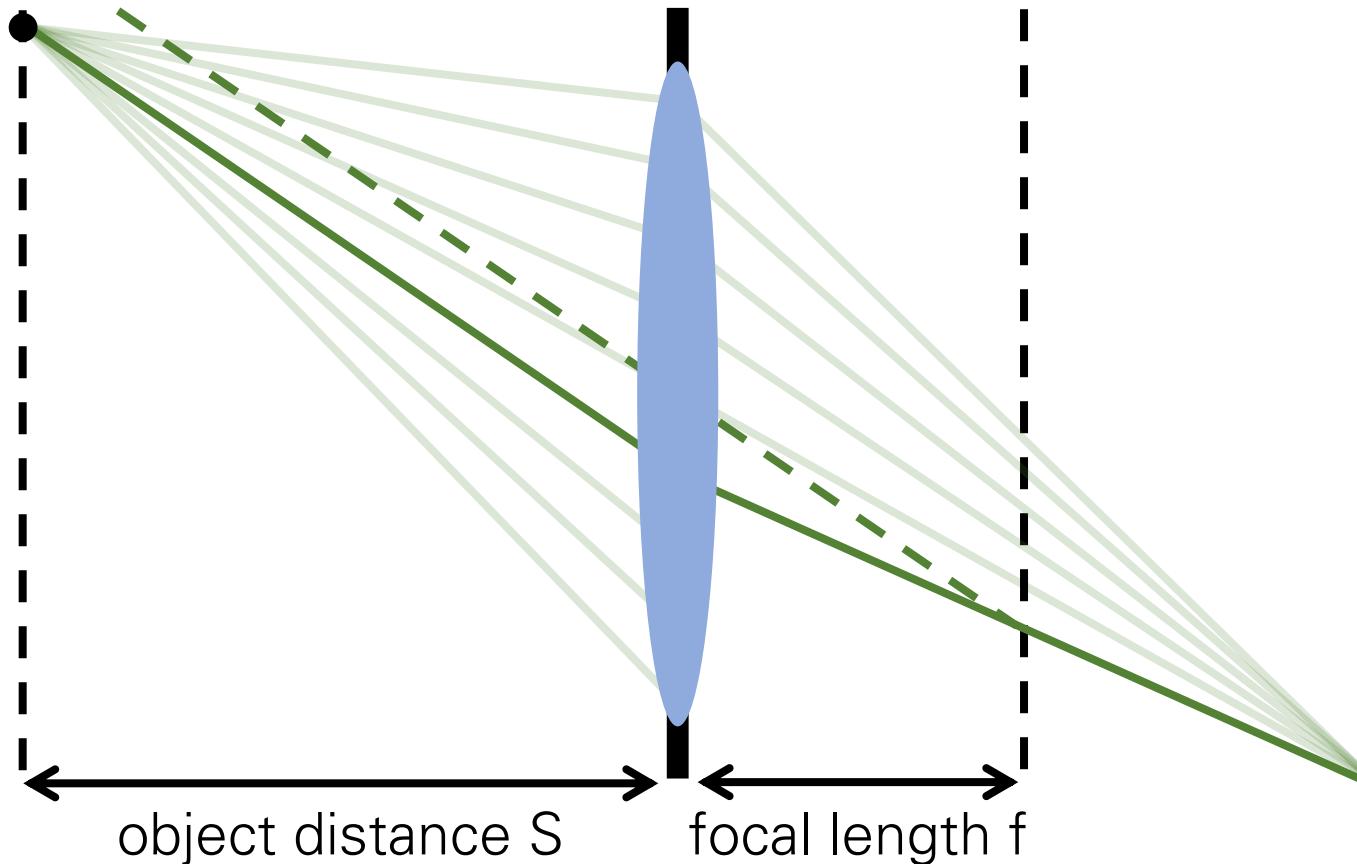
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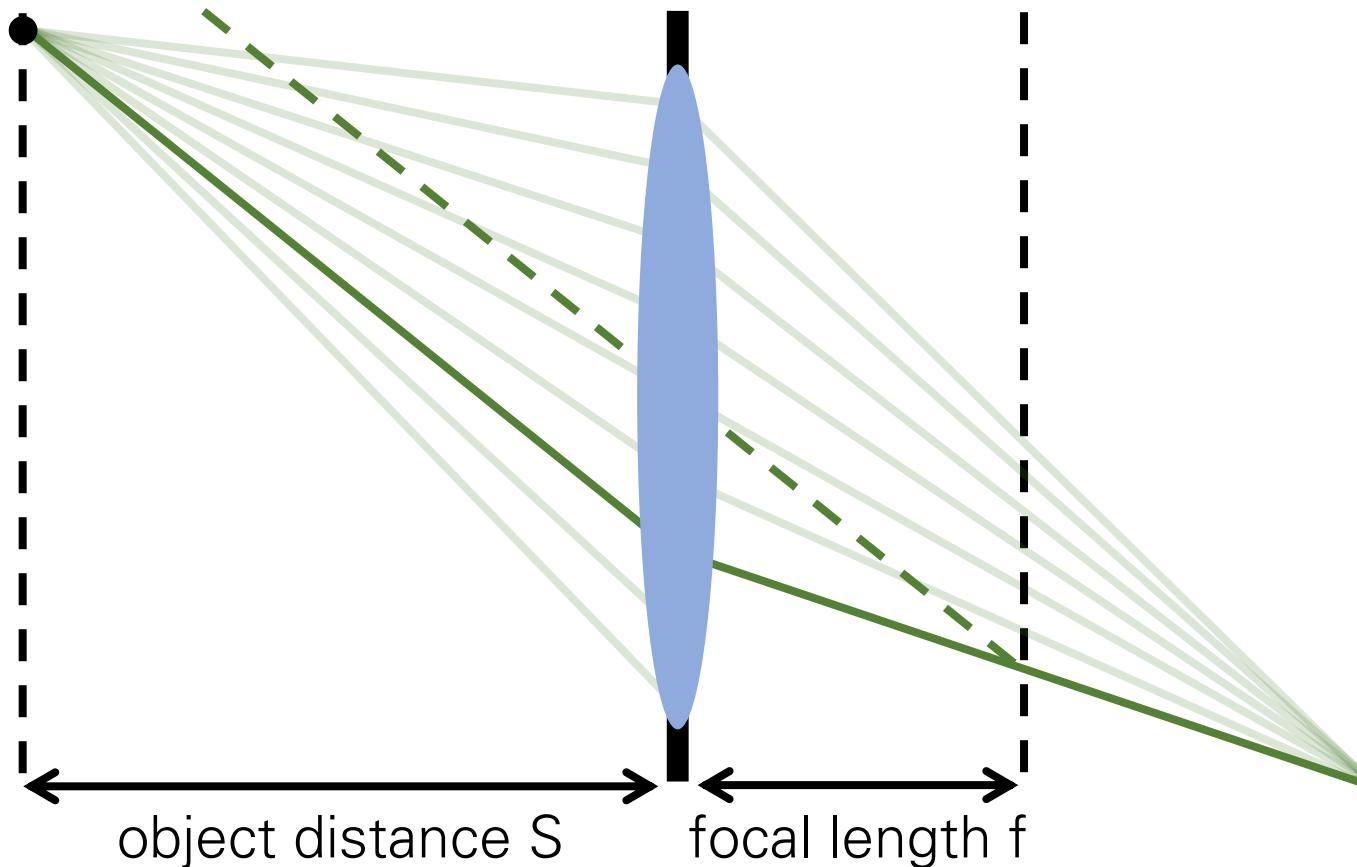
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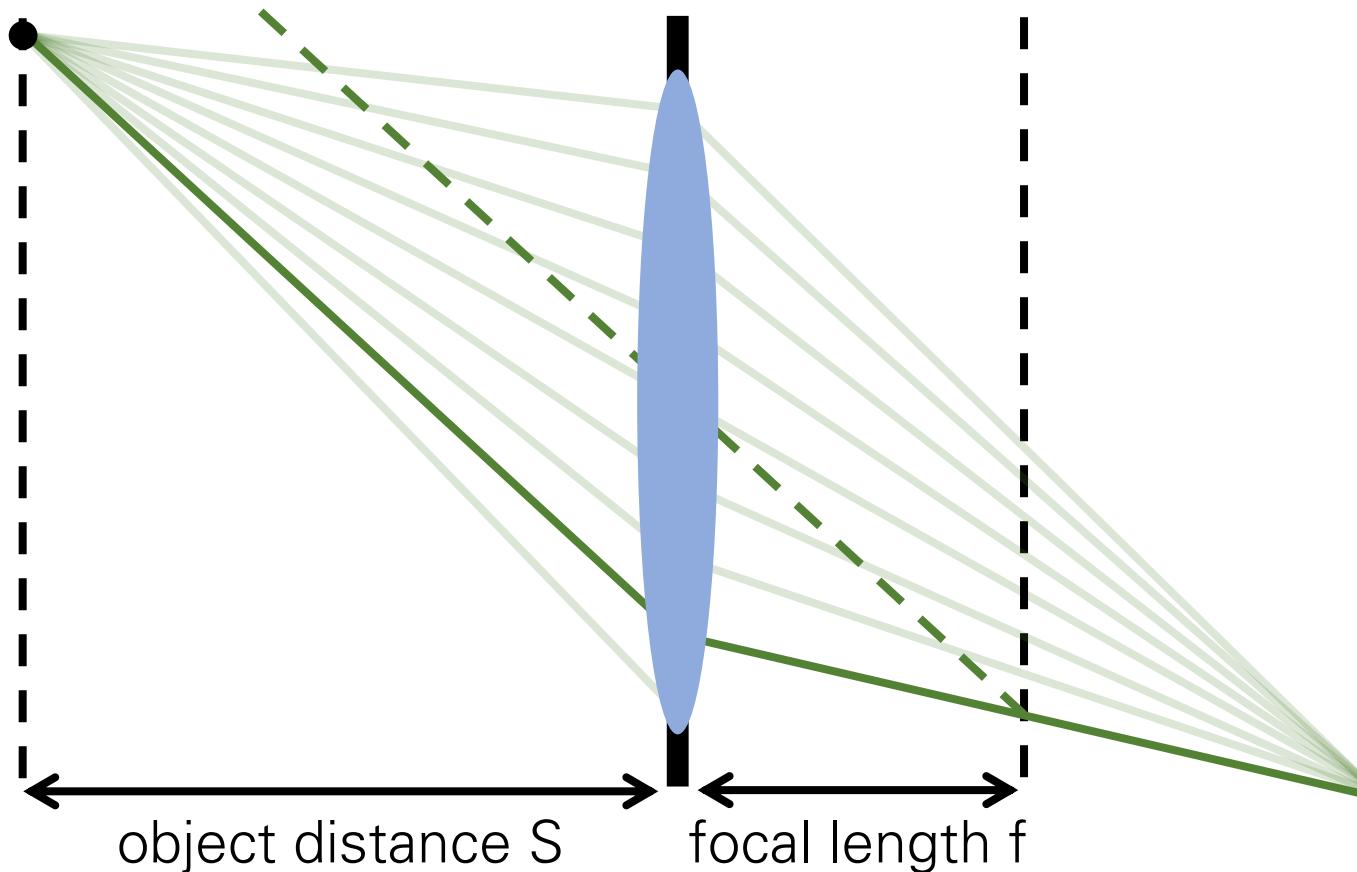
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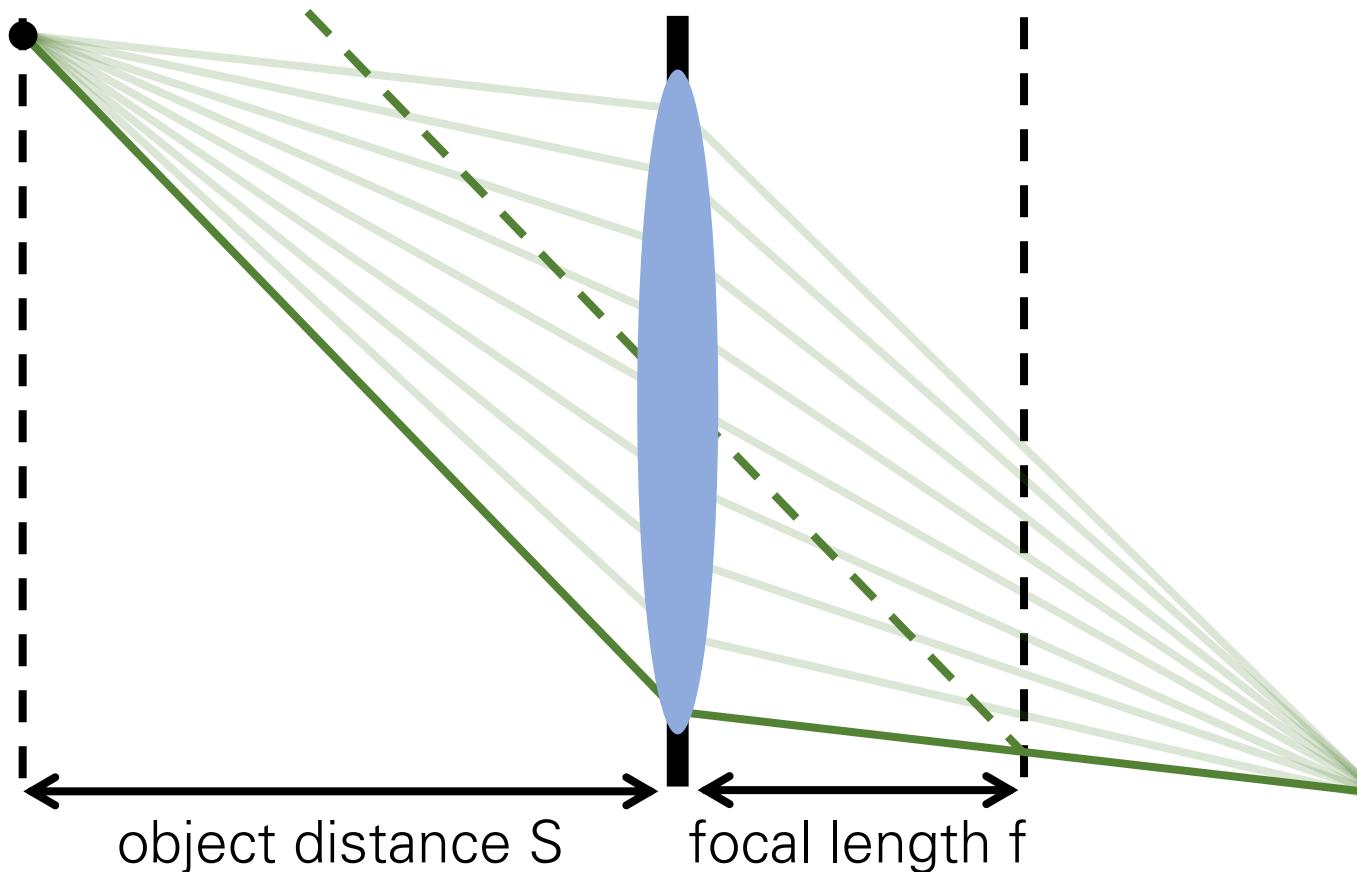
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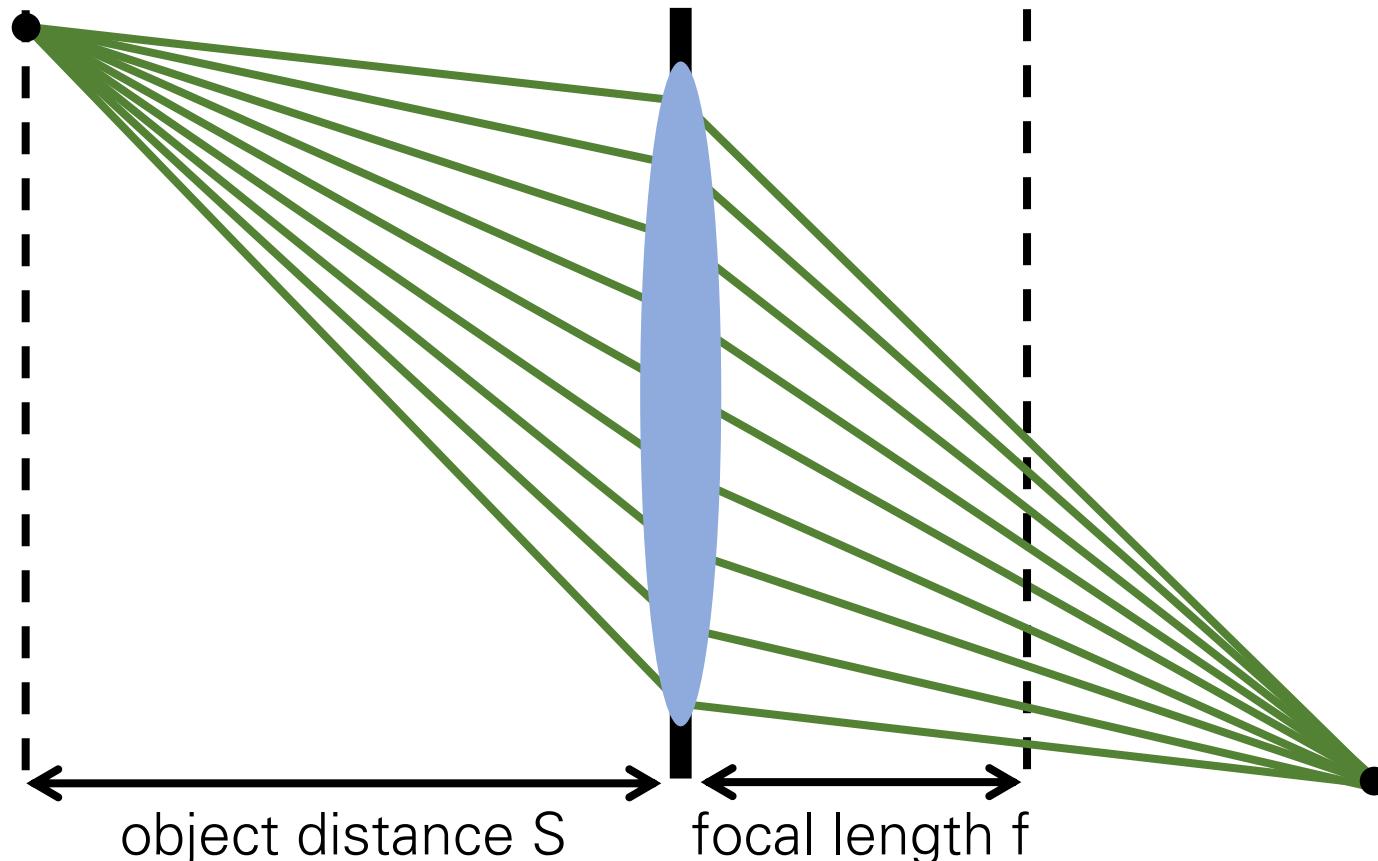
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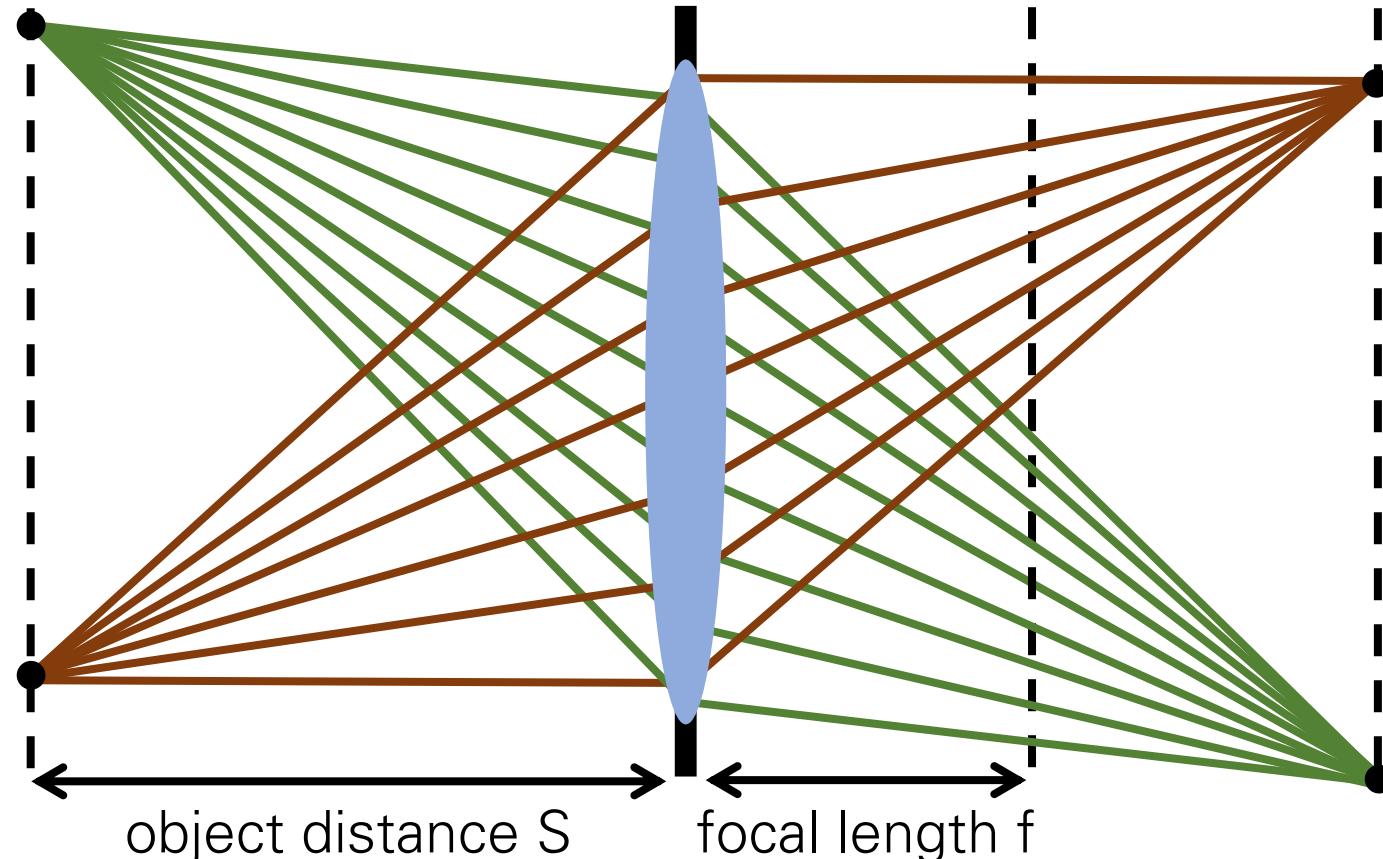
Focusing property:

1. Rays emitted from a point on one side converge to a point on the other side.

Tracing rays through a thin lens

Consider an object emitting a bundle of rays. How do they propagate through the lens?

1. Trace rays through lens center.
2. For all other rays:
 - a. Trace their parallel through lens center.
 - b. Connect on focal plane.

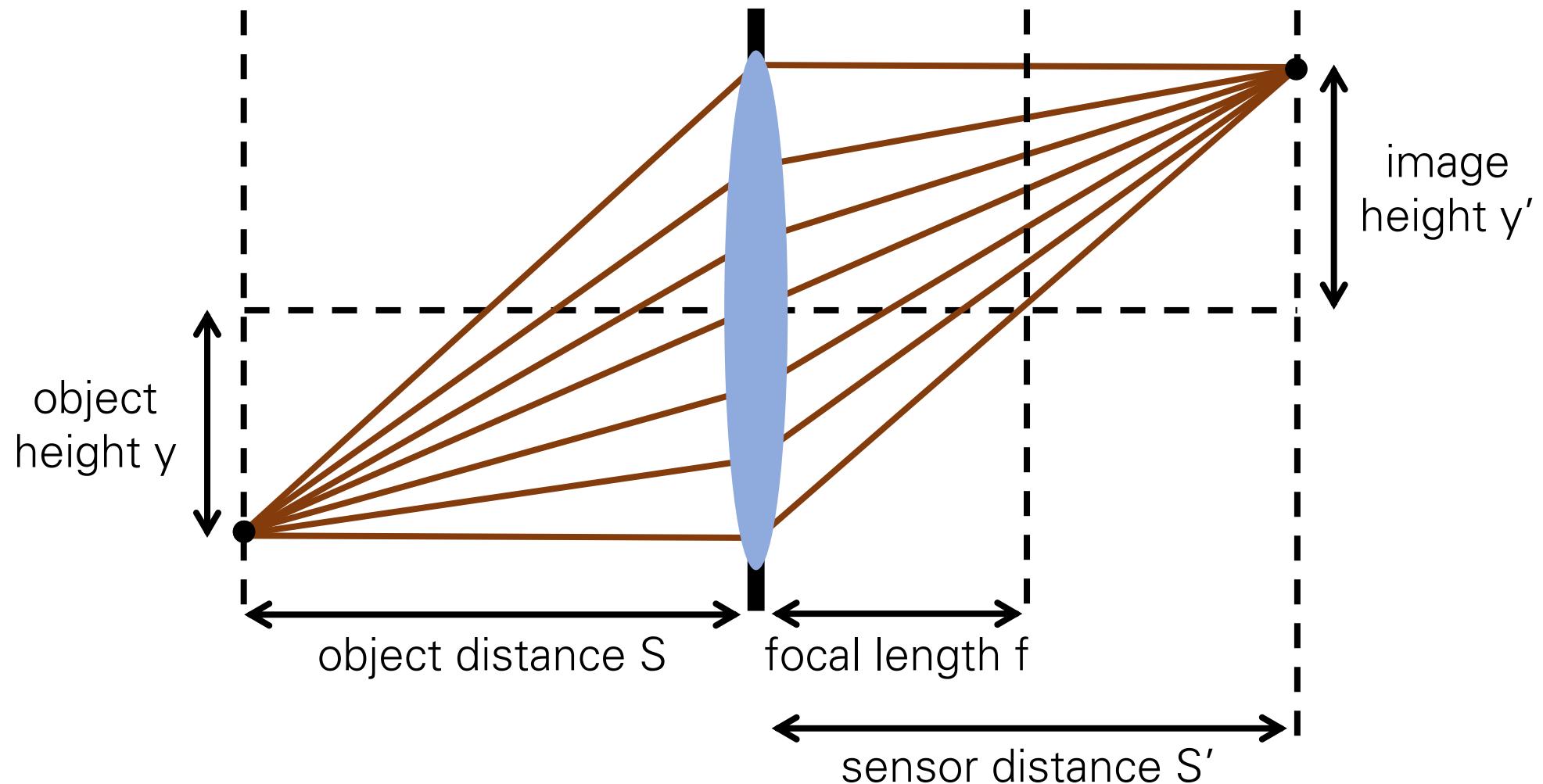


Focusing property:

1. Rays emitted from a point on one side converge to a point on the other side.
2. Bundles emitted from a plane parallel to the lens converge on a common plane.

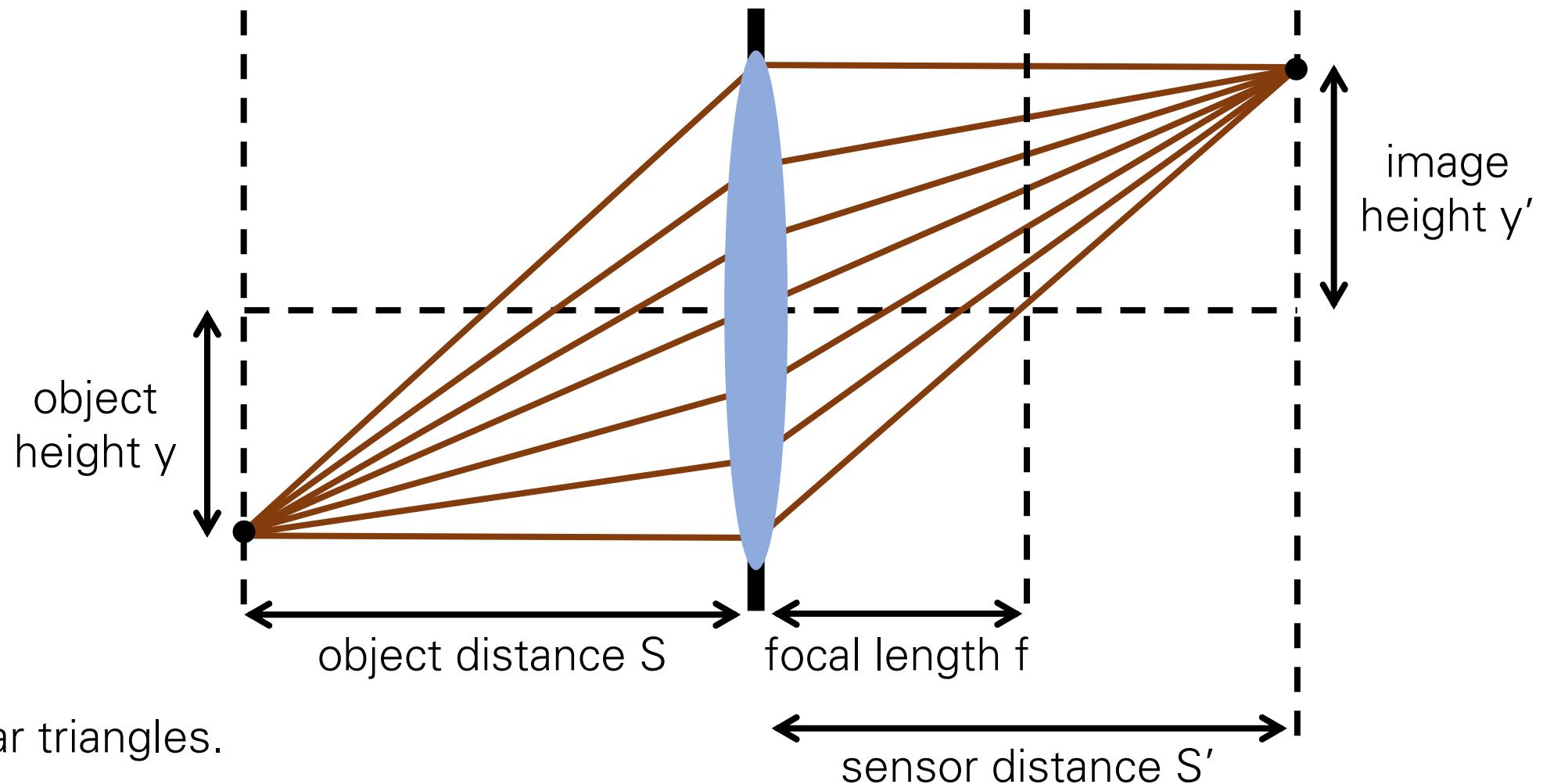
Gaussian lens formula

How can we relate scene-space (S , y) and image space (S' , y') quantities?



Gaussian lens formula

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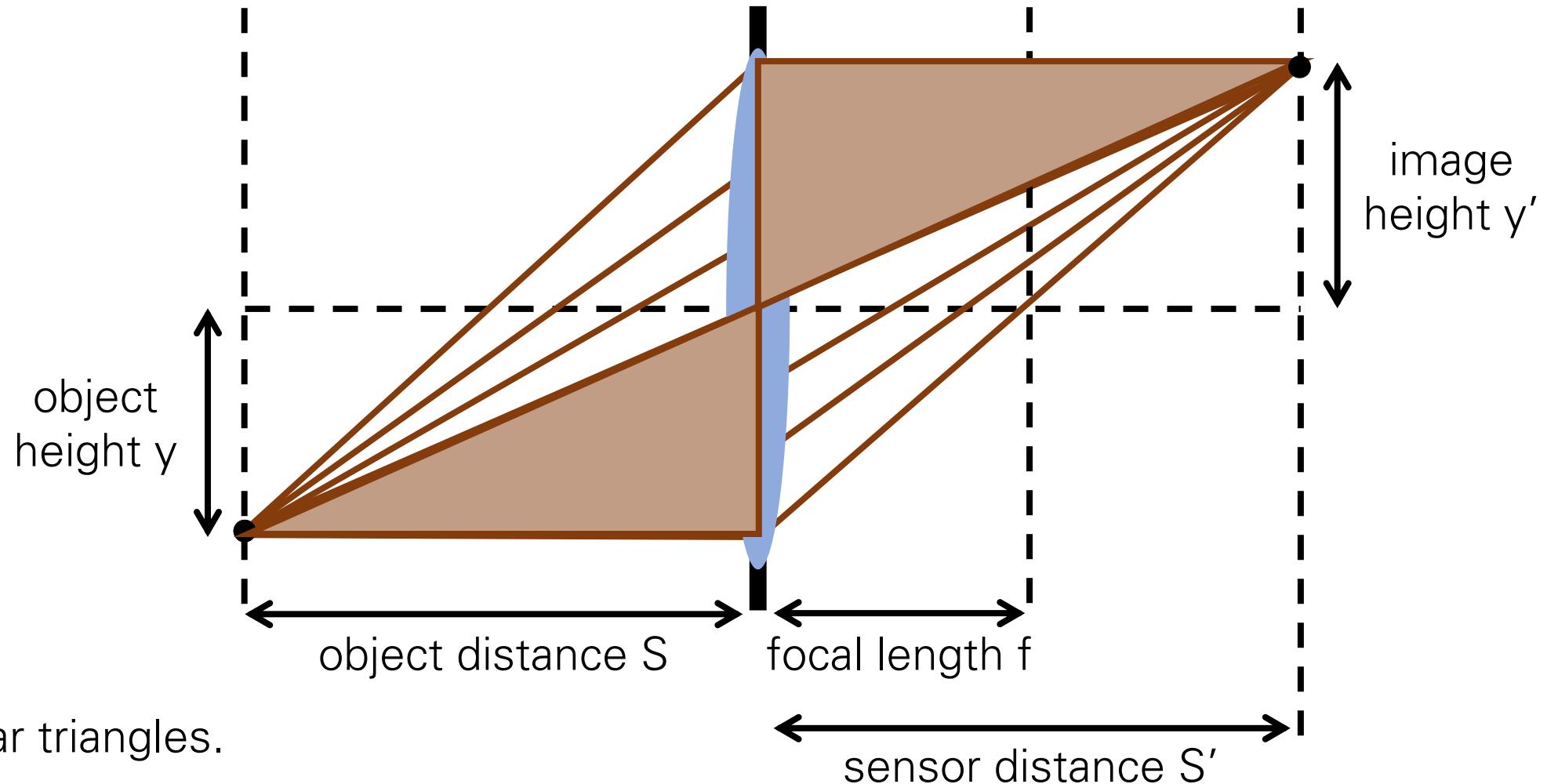


Use similar triangles.

Gaussian lens formula

How can we relate scene-space (S , y) and image space (S' , y') quantities?

$$\frac{y'}{y} = ?$$

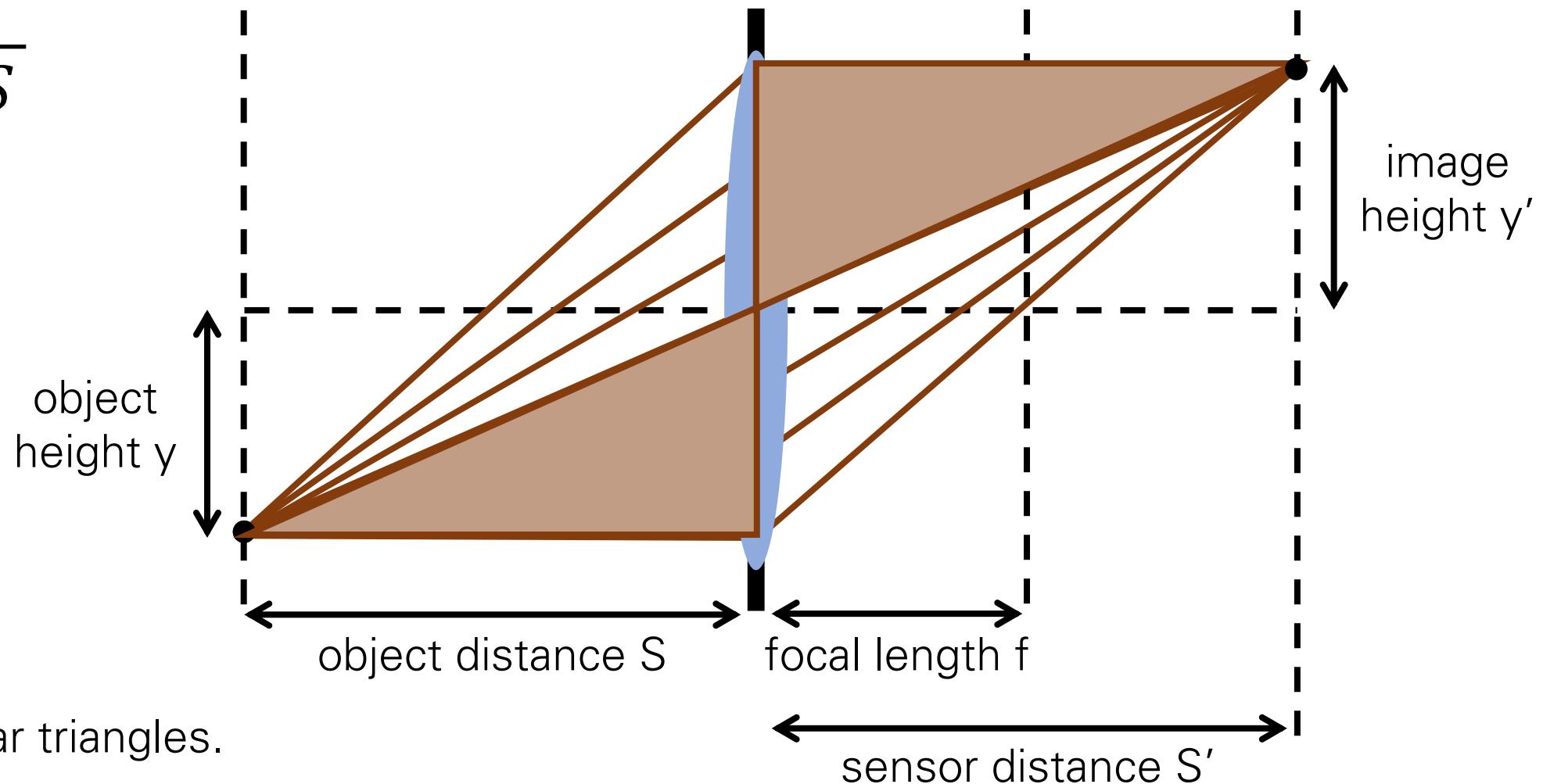


Use similar triangles.

Gaussian lens formula

How can we relate scene-space (S , y) and image space (S' , y') quantities?

$$\frac{y'}{y} = \frac{S'}{S}$$

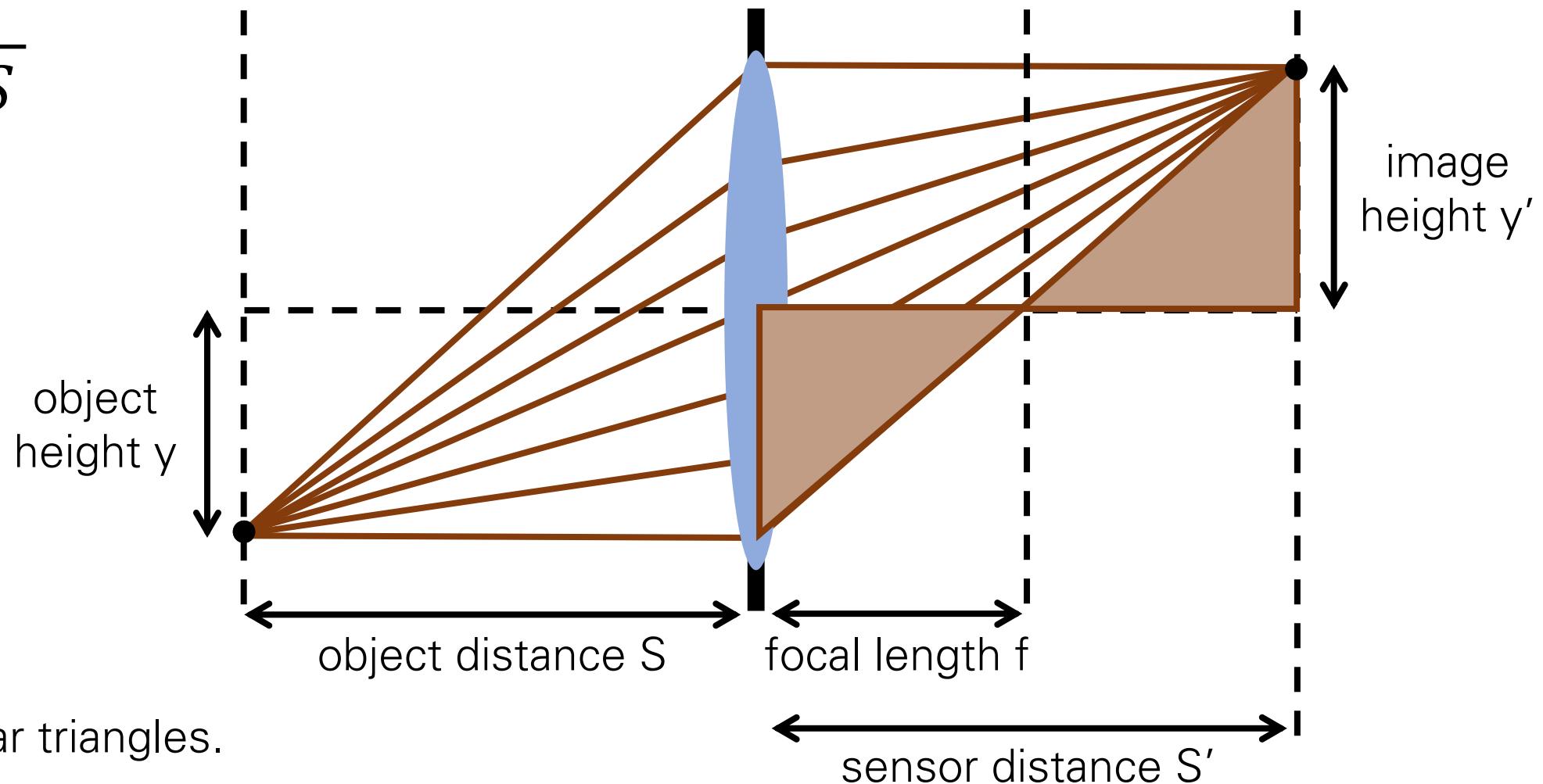


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Gaussian lens formula

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$$\frac{y'}{y} = \frac{S'}{S}$$
$$\frac{y'}{y} = ?$$



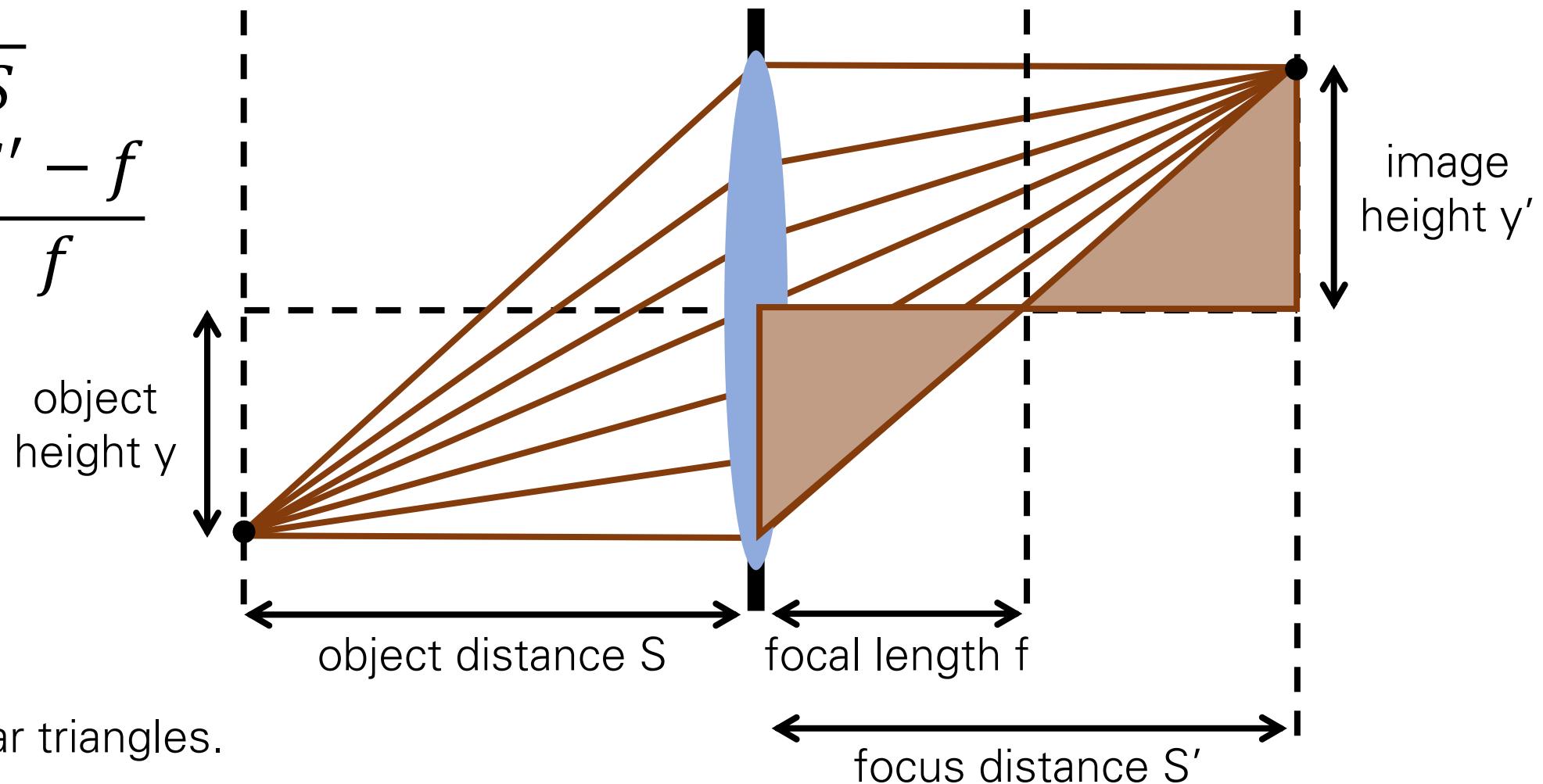
Use similar triangles.

Gaussian lens formula

How can we relate scene-space (S , y) and image space (S' , y') quantities?

$$\frac{y'}{y} = \frac{S'}{S}$$

$$\frac{y'}{y} = \frac{S' - f}{f}$$

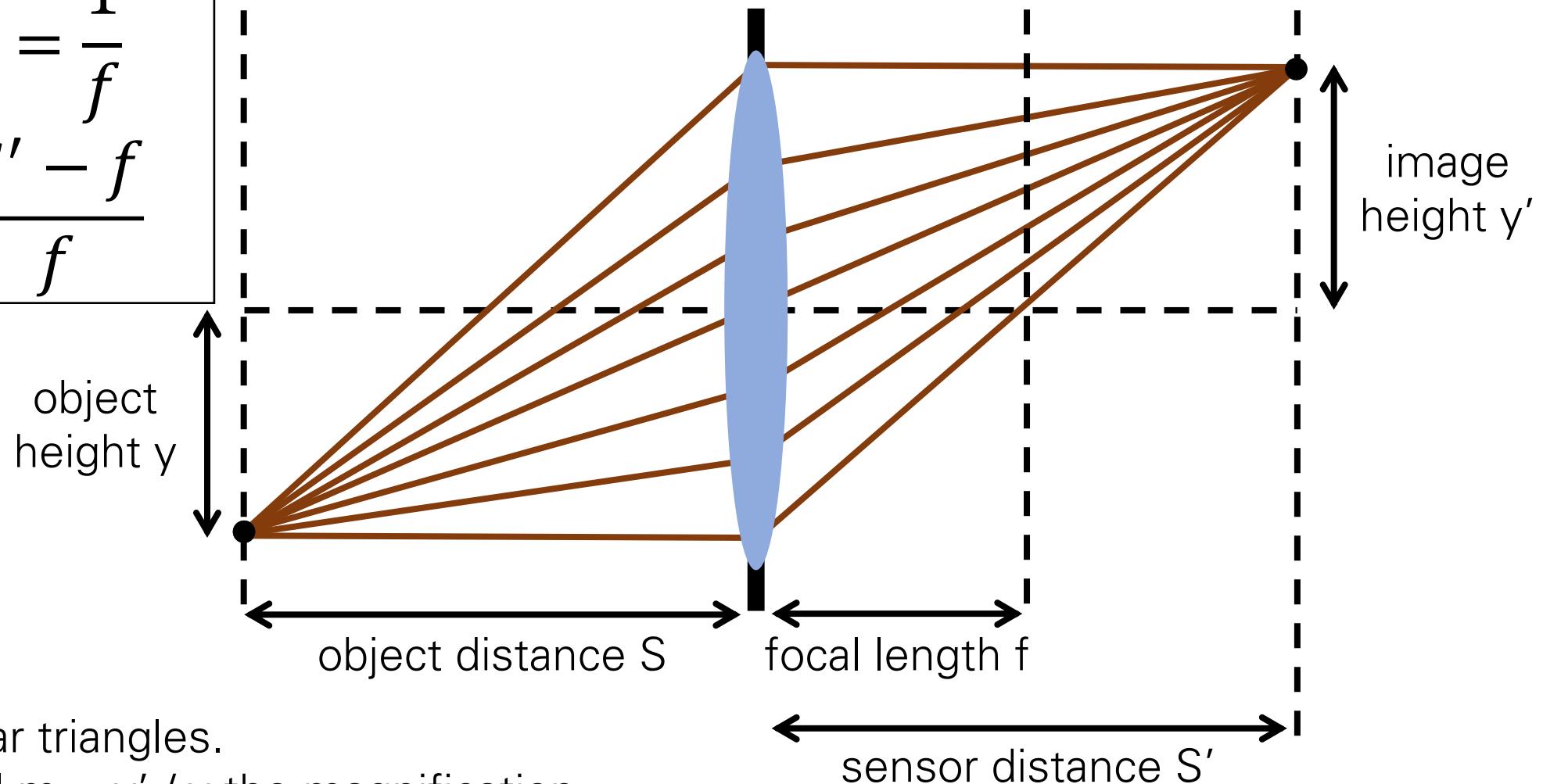


Use similar triangles.

Gaussian lens formula

How can we relate scene-space (S , y) and image space (S' , y') quantities?

$$\frac{1}{S'} + \frac{1}{S} = \frac{1}{f}$$
$$m = \frac{S' - f}{f}$$



Use similar triangles.

- We call $m = y' / y$ the magnification.

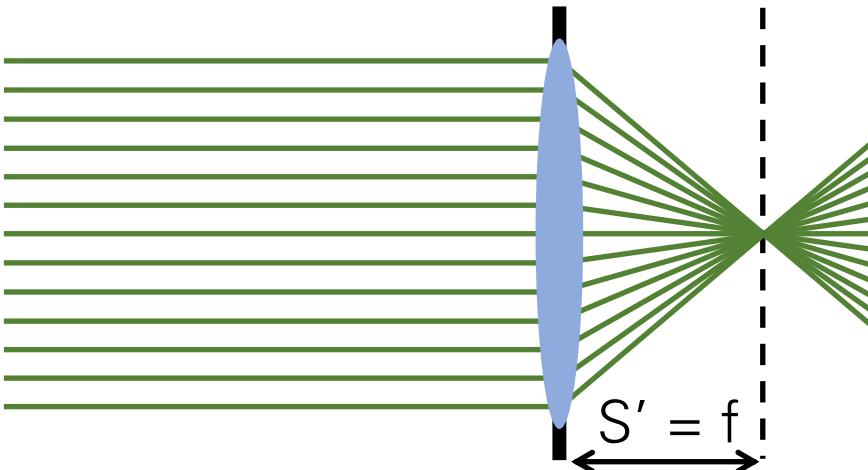
Special focus distances

$S' = f, S = ?, m = ?$

$$\frac{1}{S'} + \frac{1}{S} = \frac{1}{f}$$
$$m = \frac{S' - f}{f}$$

Special focus distances

$S' = f, S = \infty, m = 0 \rightarrow$ infinity focus (parallel rays)



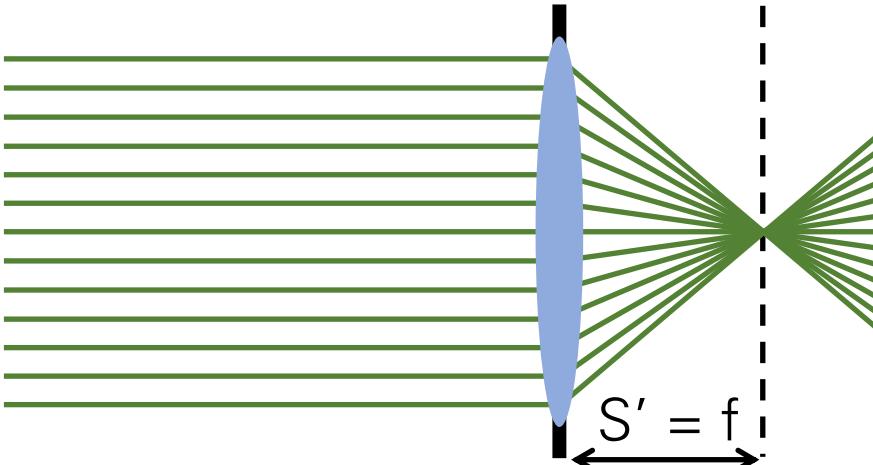
$$\frac{1}{S'} + \frac{1}{S} = \frac{1}{f}$$
$$m = \frac{S' - f}{f}$$

$S' = S = ?, m = ?$

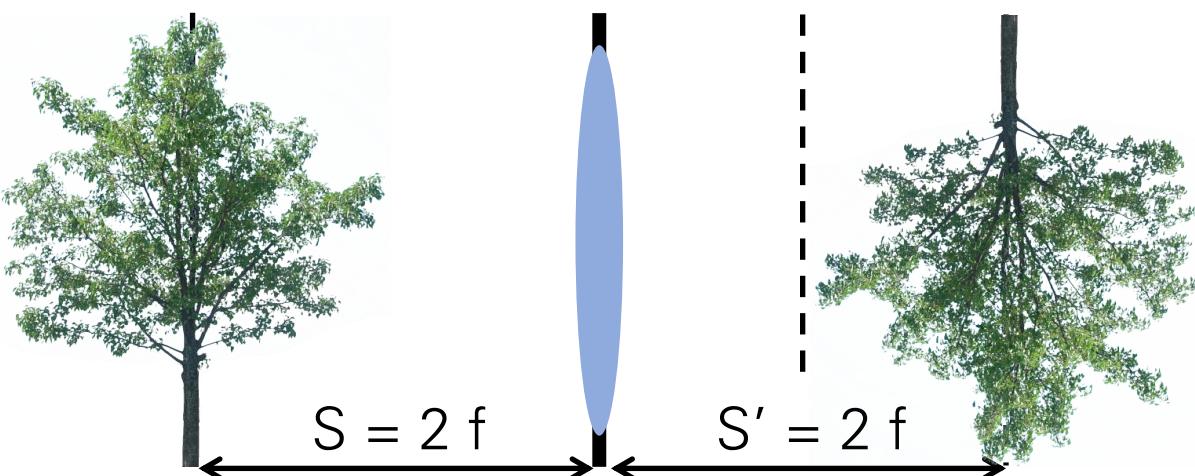
Special focus distances

$S' = f, S = \infty, m = 0 \rightarrow$ infinity focus (parallel rays)

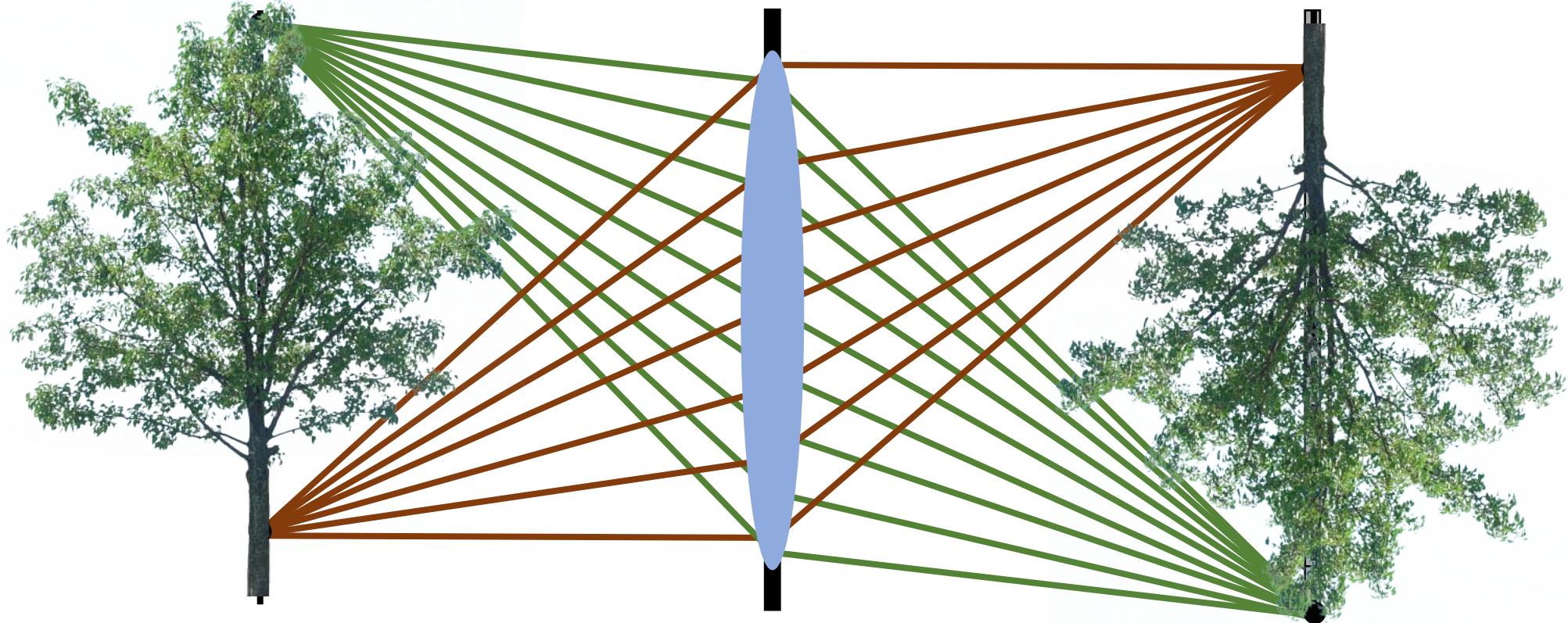
$$\frac{1}{S'} + \frac{1}{S} = \frac{1}{f}$$
$$m = \frac{S' - f}{f}$$



$S' = S = 2 f, m = 1 \rightarrow$ object is reproduced in real-life size



Free lunch?



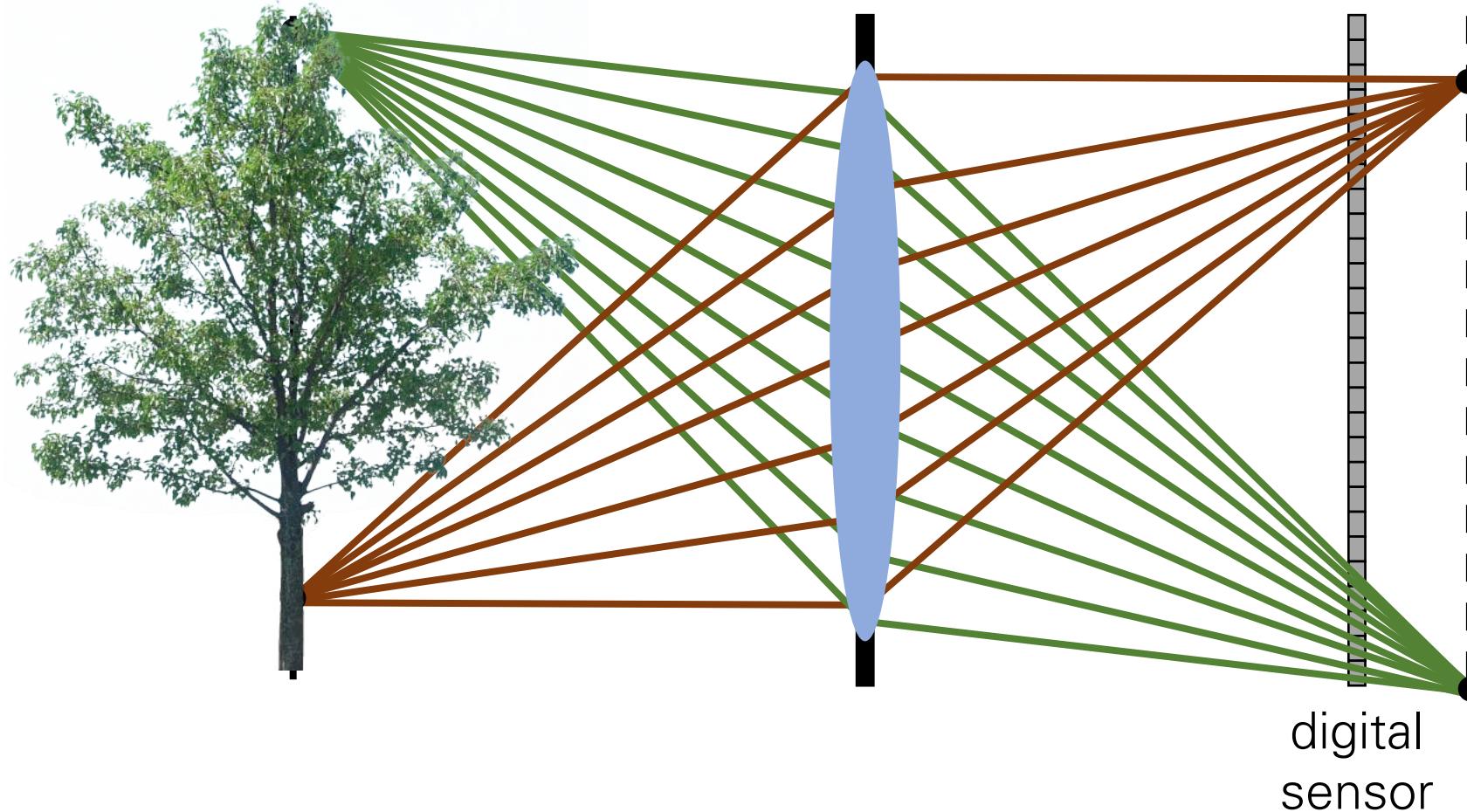
By using a lens, we simultaneously achieve:

1. Image is sharp.
2. Signal-to-noise ratio is high.

Do we lose anything by using a lens?

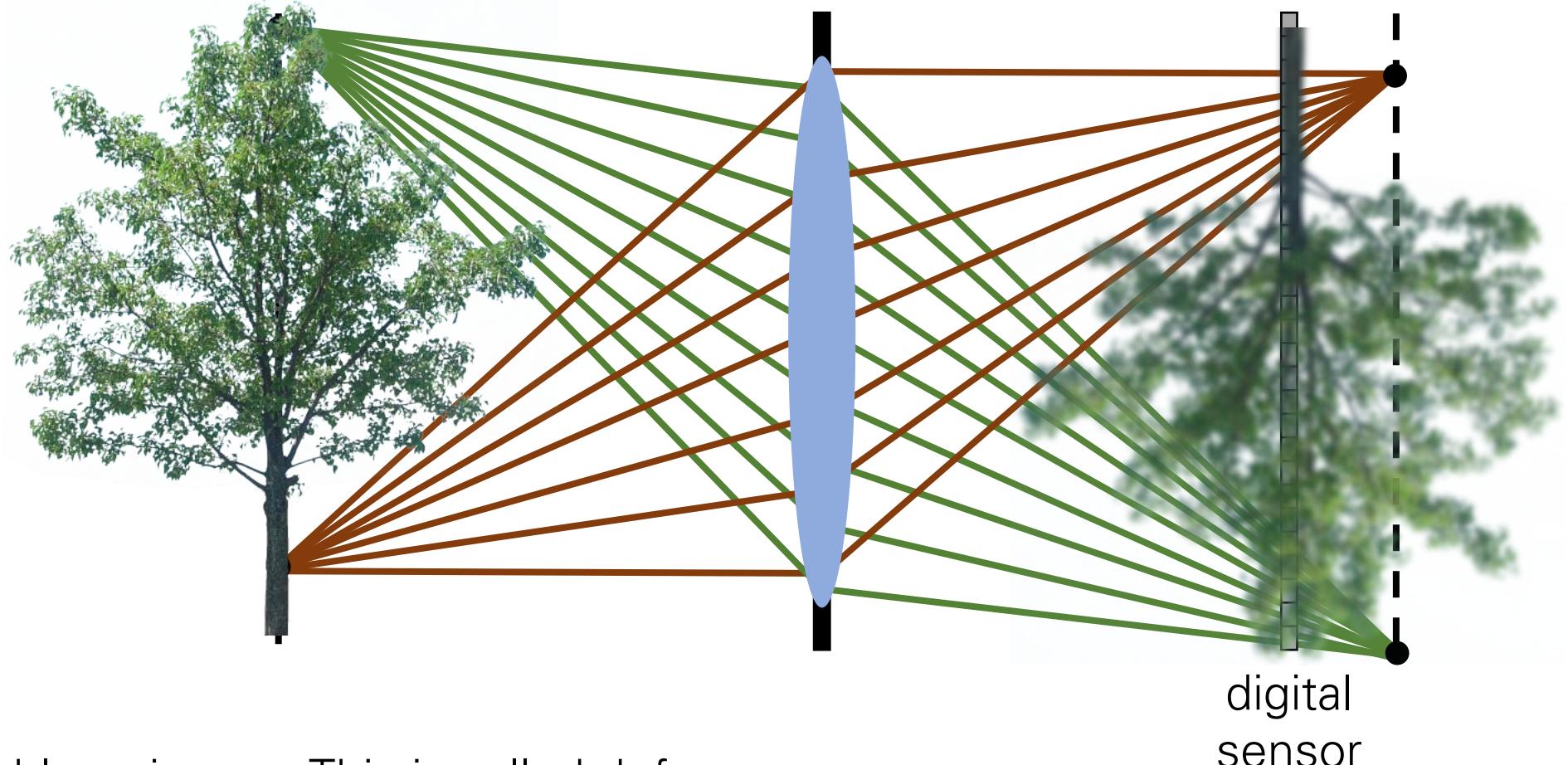
Defocus

What happens if we don't place the sensor at the focus distance?



Defocus

What happens if we don't place the sensor at the focus distance?



We get a blurry image. This is called defocus.

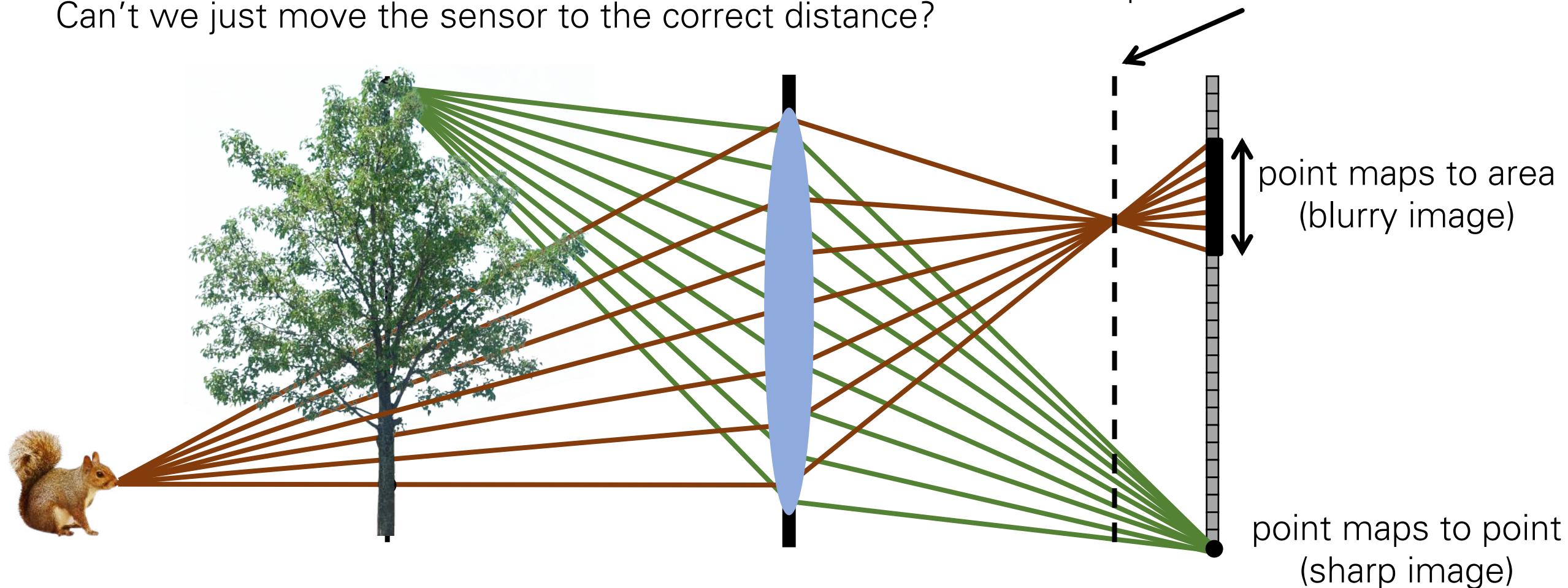
- Defocus never happens with an ideal pinhole camera.

Defocus

Can't we just move the sensor to the correct distance?

Defocus

Can't we just move the sensor to the correct distance?



Unless our scene is just one plane, part of it will always be out of focus.

How do we control what is in focus?

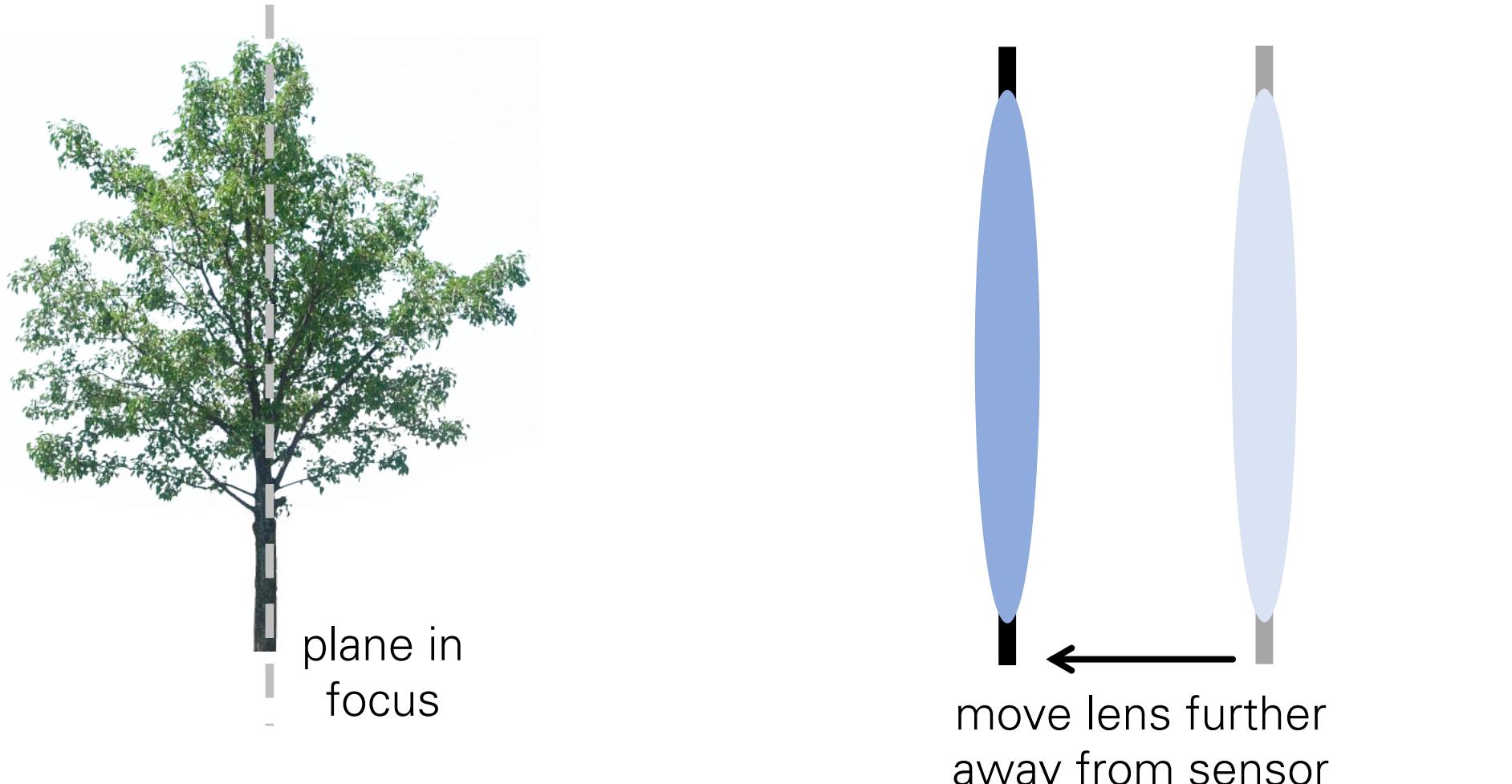
How do we control what is in focus?

We change the distance between the sensor and the lens



How do we control what is in focus?

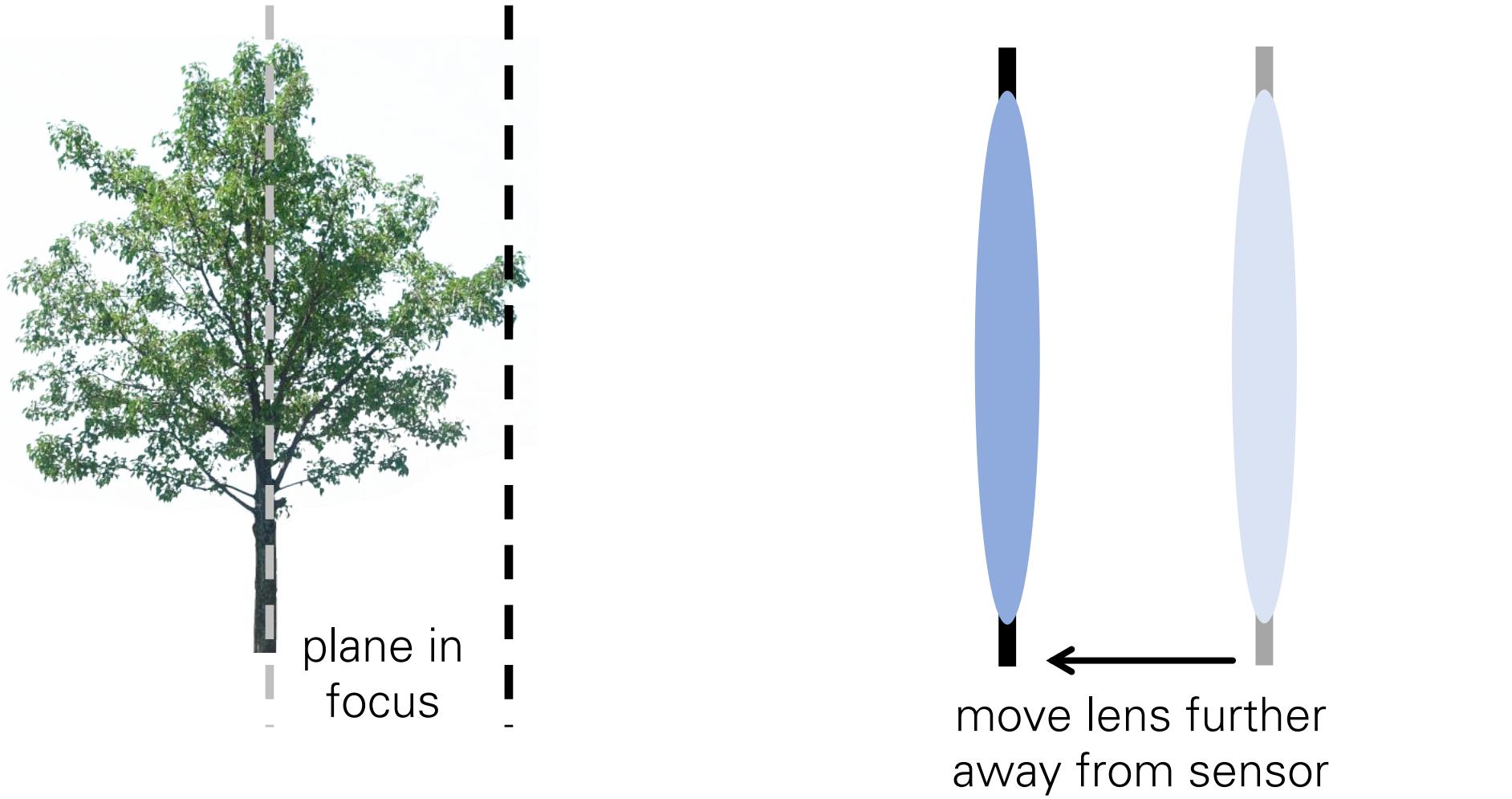
We change the distance between the sensor and the lens



- What happens to plane in focus?

How do we control what is in focus?

We change the distance between the sensor and the lens



- What happens to plane in focus? → It moves closer.

The lens on your camera

Focus ring: controls distance of lens from sensor



Demonstration

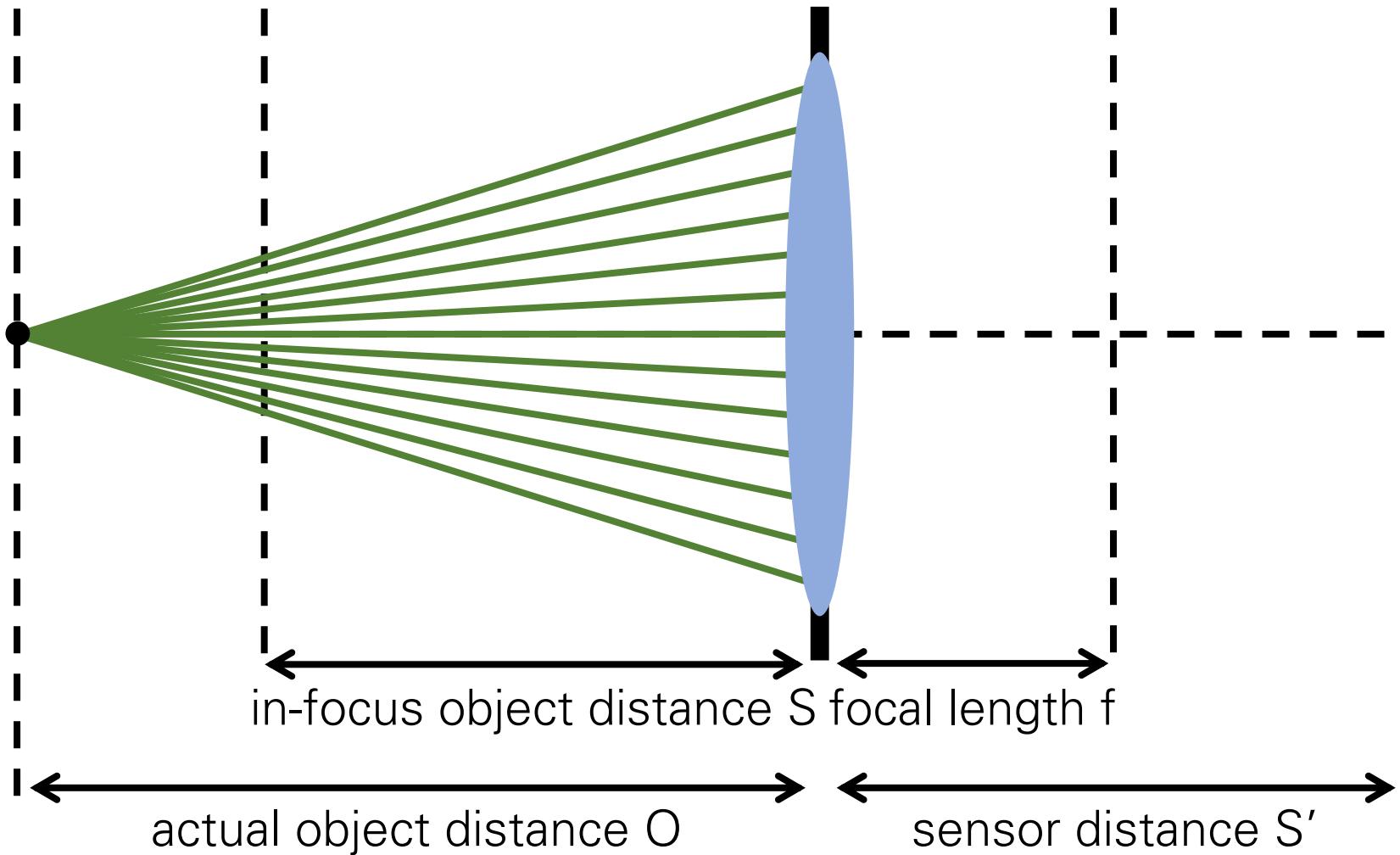


Defocus

Does that mean that lenses are only good for planar scenes?

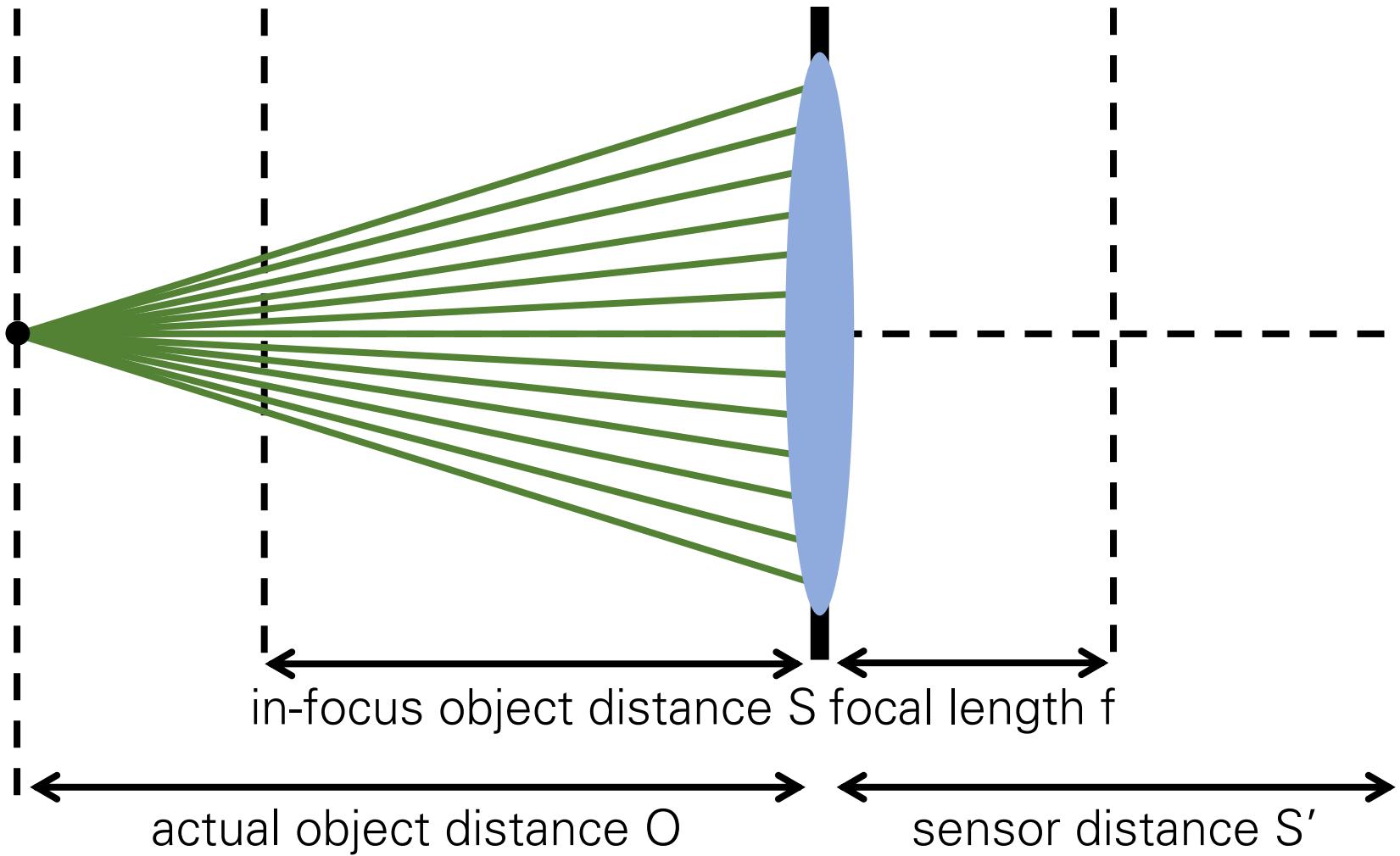
Circle of confusion

How do we find where the point will focus?



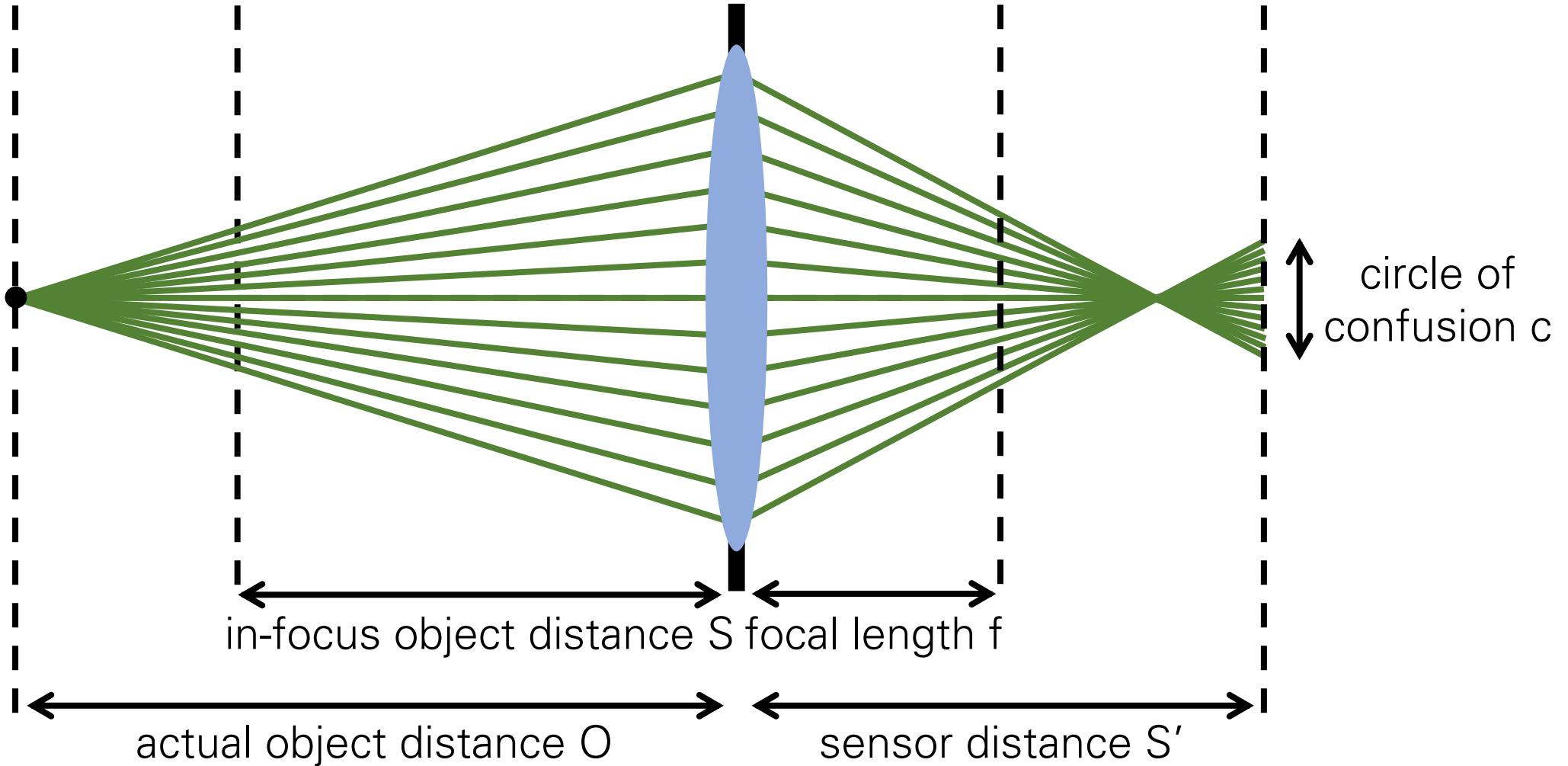
Circle of confusion

Will the point focus at a distance smaller or larger than S' ?



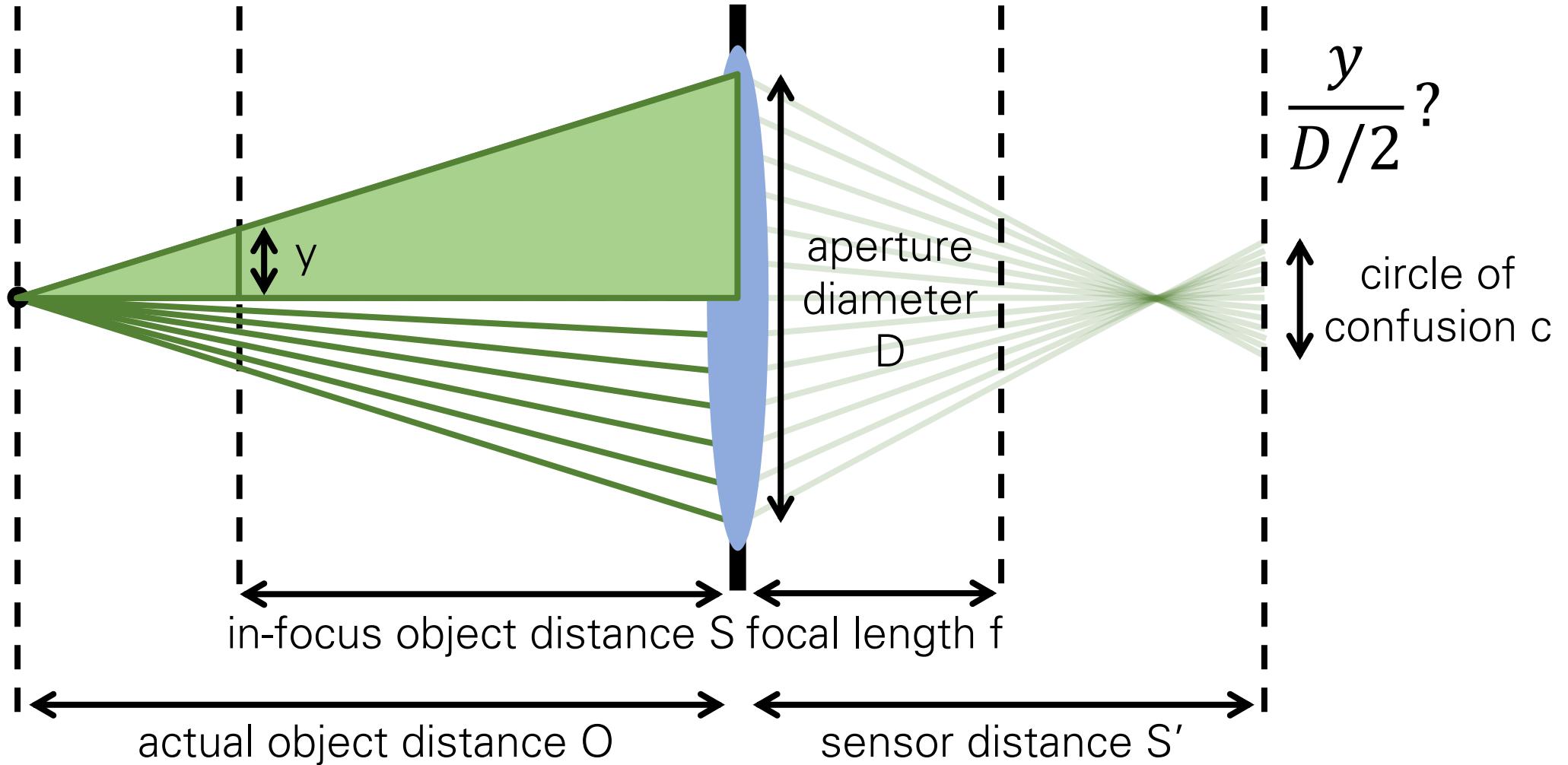
Circle of confusion

How can we compute the diameter of the circle of confusion?



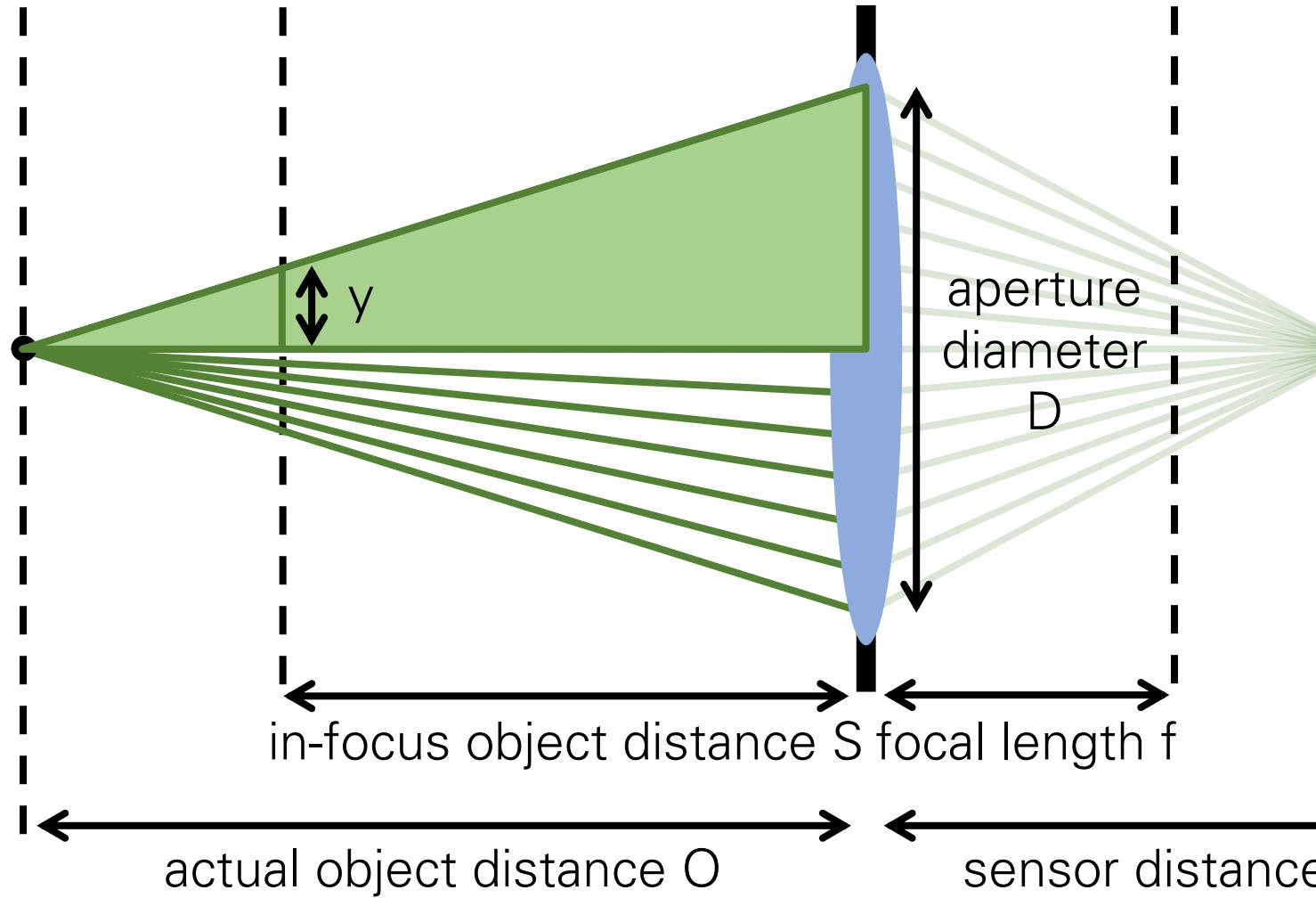
Circle of confusion

How can we compute the diameter of the circle of confusion? → Use similar triangles.



Circle of confusion

How can we compute the diameter of the circle of confusion? → Use similar triangles.



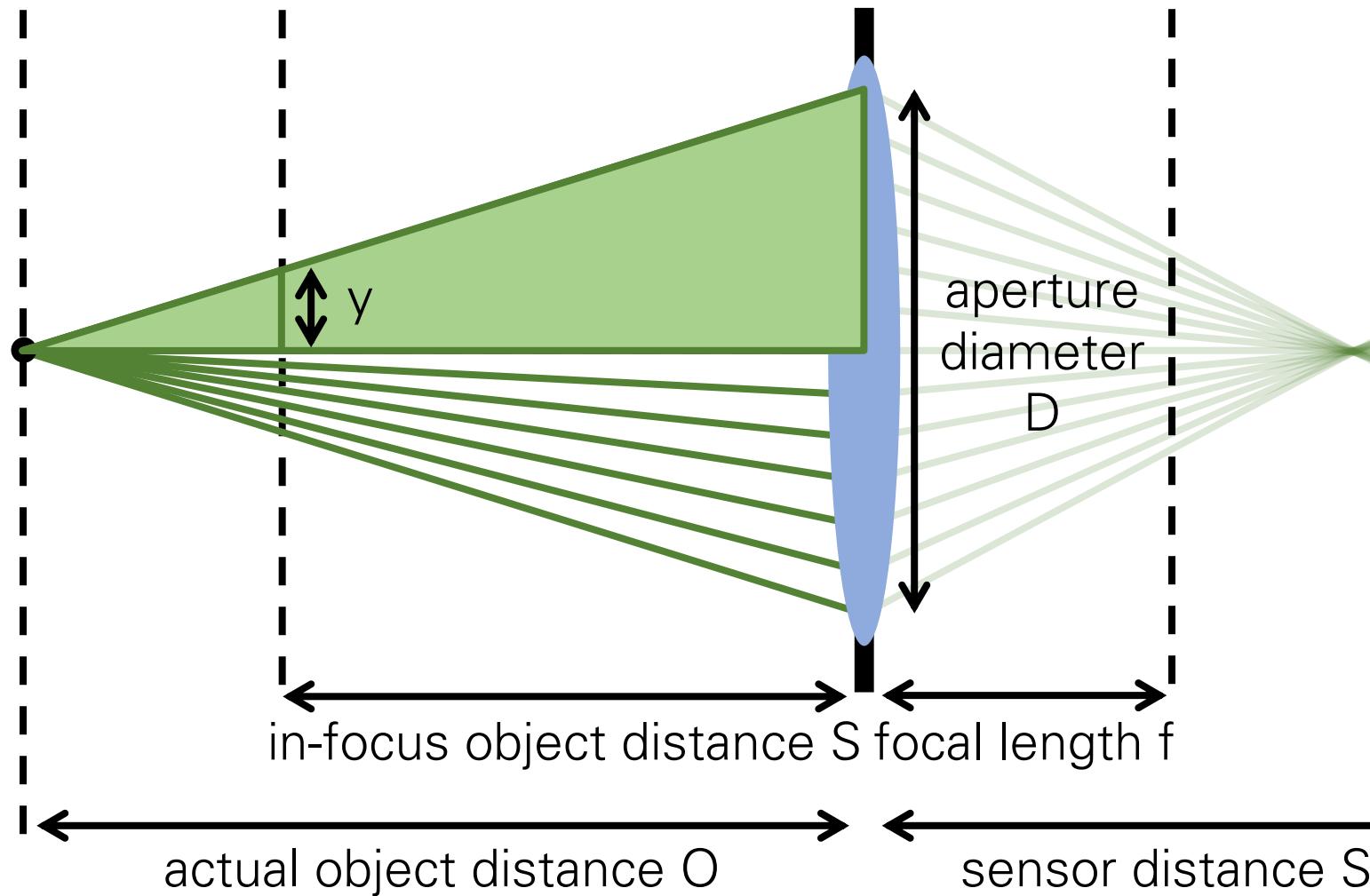
$$\frac{y}{D/2} = \frac{|O - S|}{O}$$

circle of
confusion c

$$\frac{y}{c/2} = ?$$

Circle of confusion

How can we compute the diameter of the circle of confusion? → Use similar triangles.



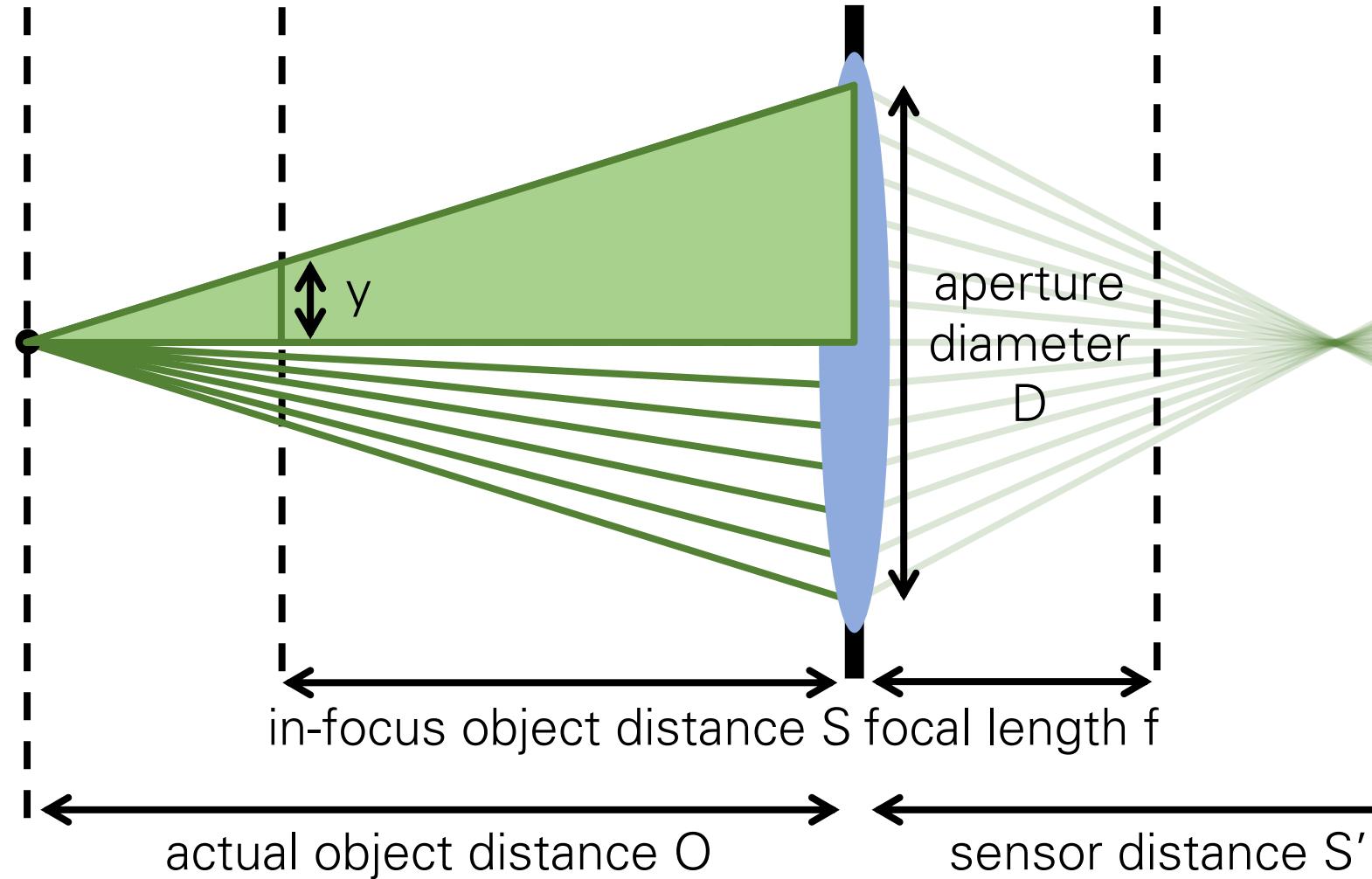
$$\frac{y}{D/2} = \frac{|O - S|}{O}$$

circle of
confusion c

$$\frac{y}{c/2} = \frac{1}{m}$$

Circle of confusion

How can we compute the diameter of the circle of confusion? → Use similar triangles.



$$\frac{y}{D/2} = \frac{|O - S|}{O}$$

circle of
confusion c

$$\frac{y}{c/2} = \frac{1}{m}$$

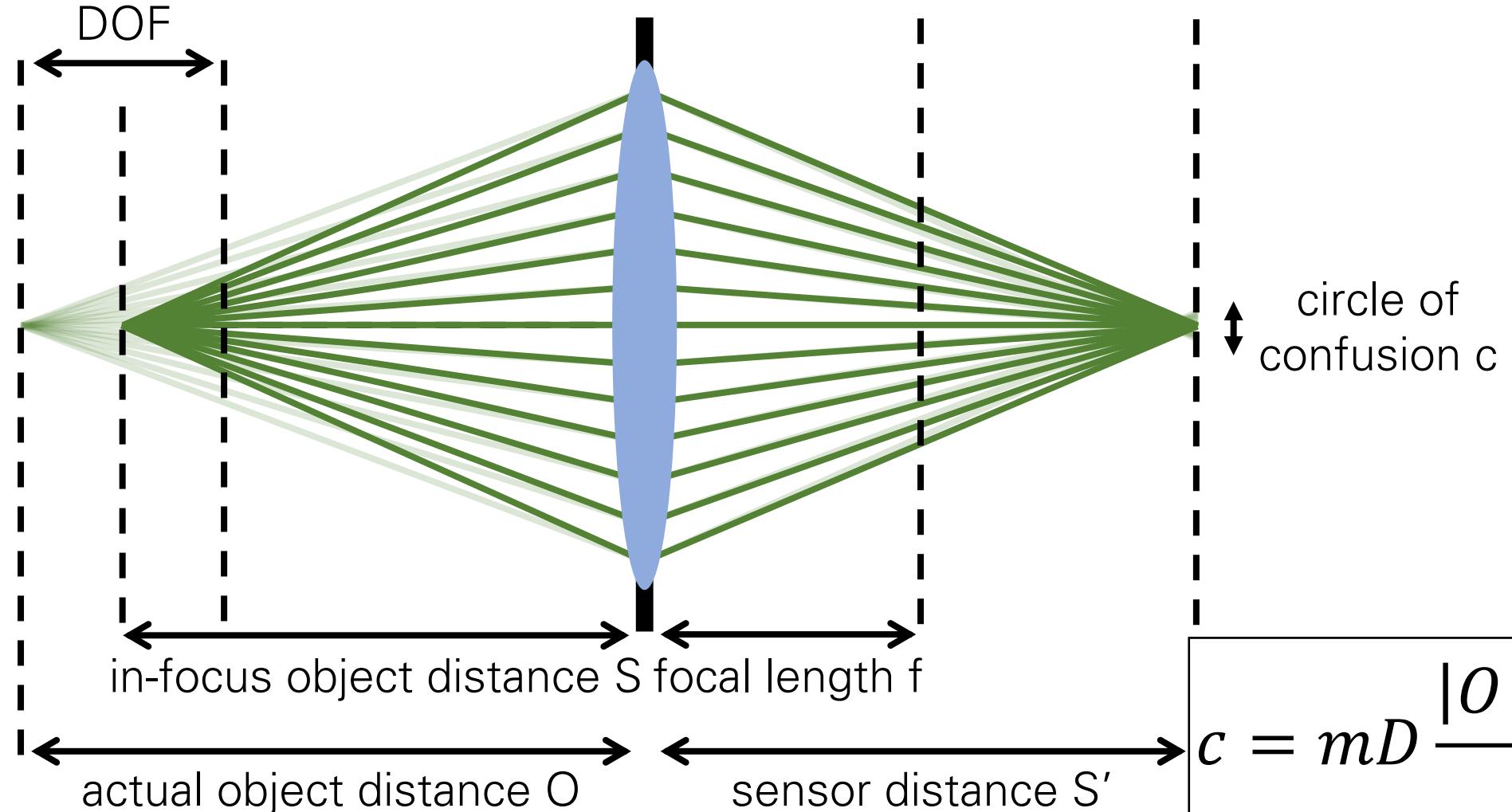
$$c = mD \frac{|O - S|}{O}$$

Depth of field

Distance from the in-focus object plane where the circle of confusion is acceptably small.

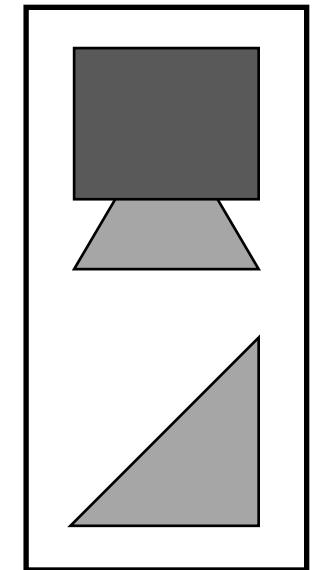
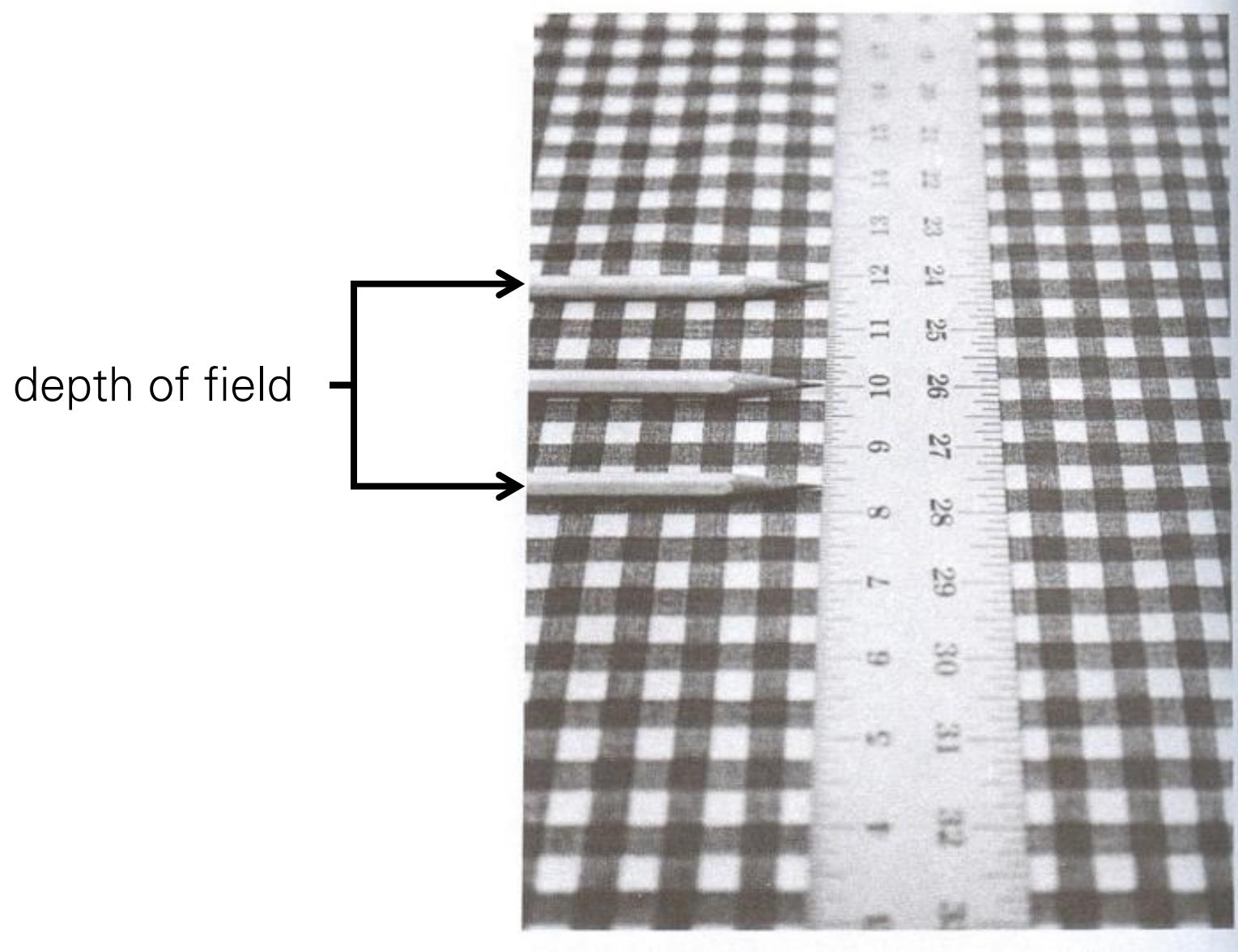
e.g., equal to
4-5 pixels

$$c < \varepsilon \Rightarrow \text{DOF} = \frac{2\varepsilon O}{mD}$$



Note: in reality,
DOF is slightly
asymmetrical.

Depth of field

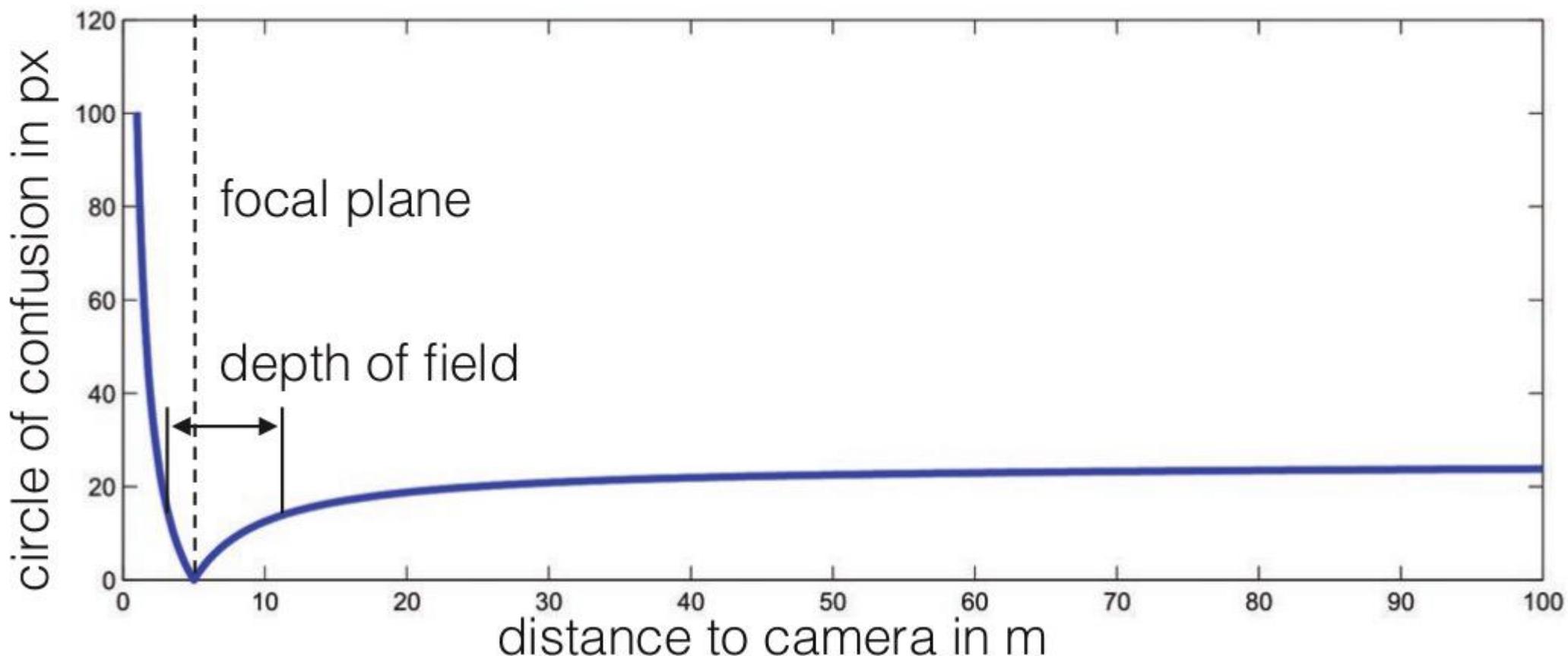


scene

Circle of confusion

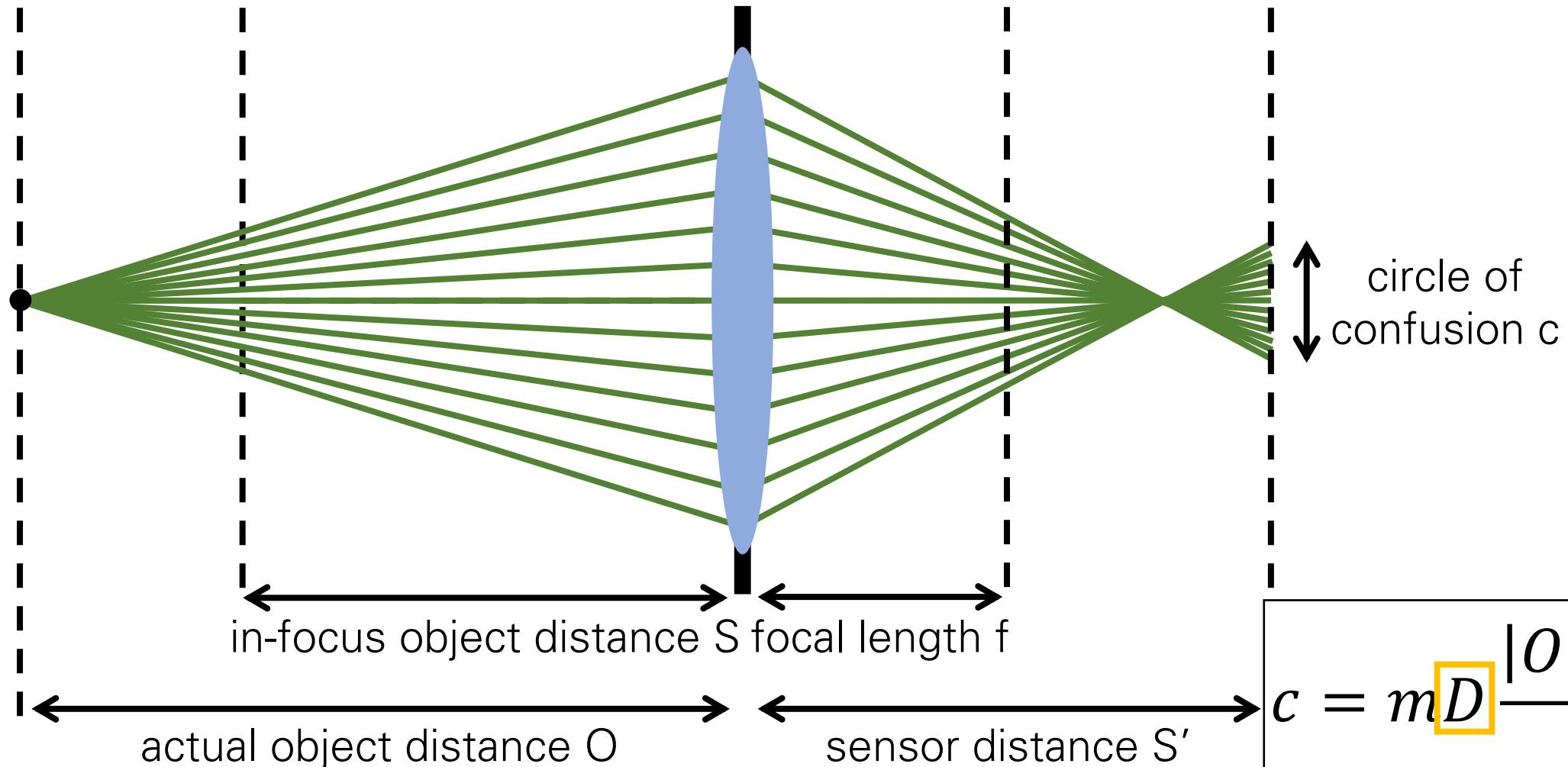
$$c = M \cdot D \cdot \frac{|S - S_1|}{S}$$

Canon 5D Mark III: f=50mm, f/2.8 (N=2.8),
focused at 5m, pixel size=7.5um



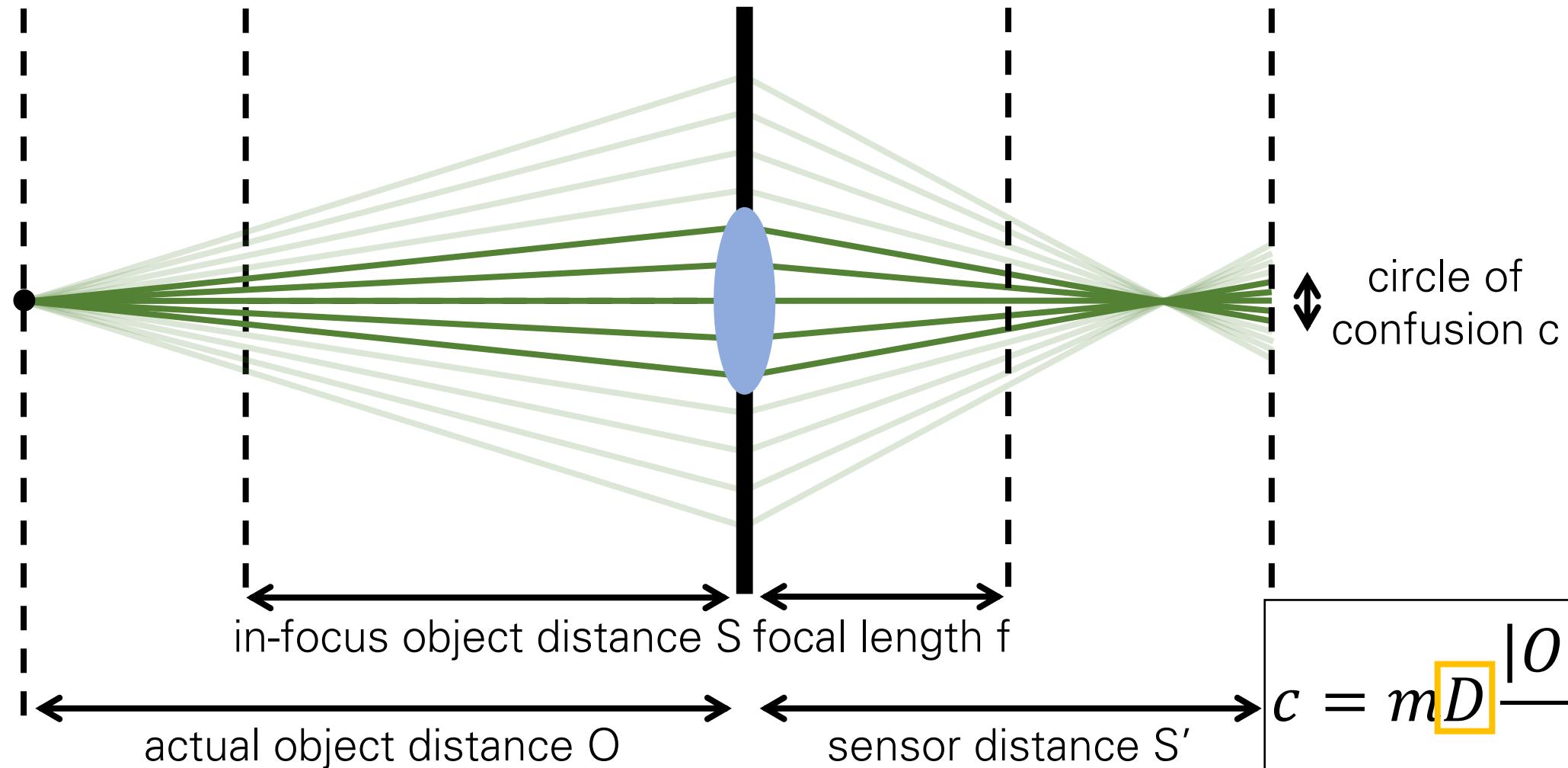
Defocus depends on aperture diameter

What happens to the circle of confusion as the aperture diameter is reduced?



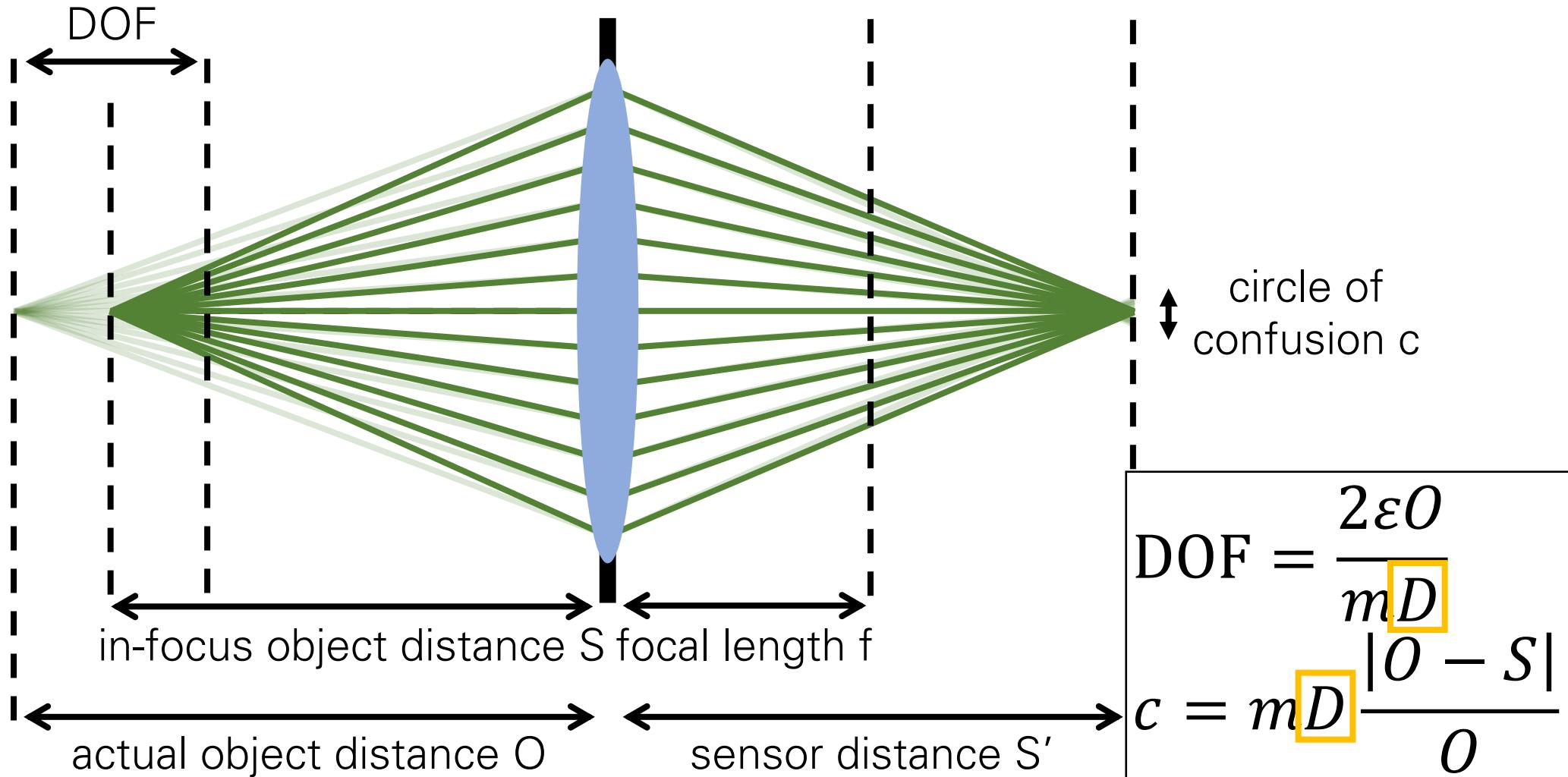
Defocus depends on aperture diameter

What happens to the circle of confusion as the aperture diameter is reduced? → It shrinks.



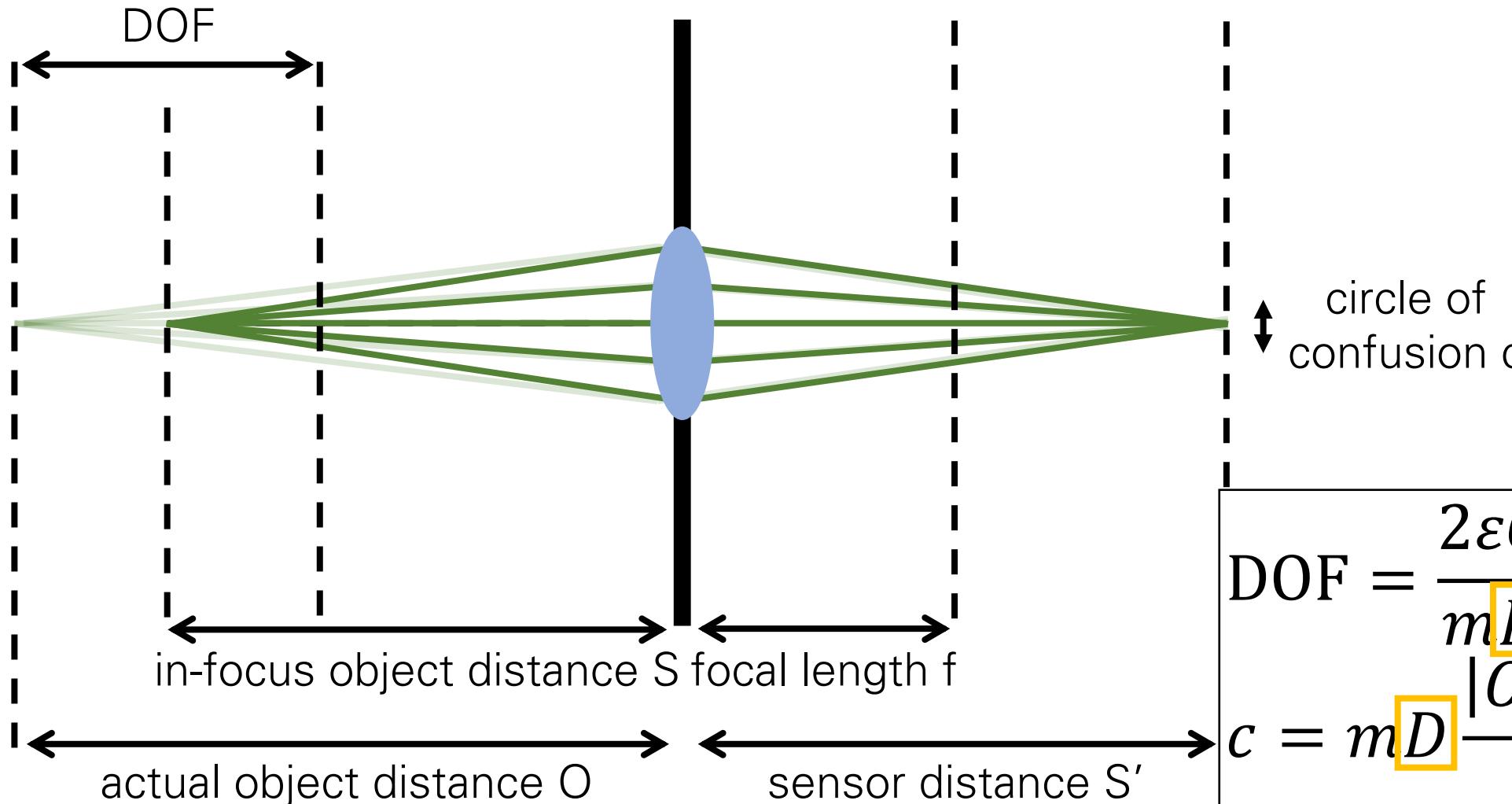
Defocus depends on aperture diameter

What happens to the depth of field as the aperture diameter is reduced?



Defocus depends on aperture diameter

What happens to the depth of field as the aperture diameter is reduced? → It expands.



Aperture size

Most lenses have apertures of variable size.

- The size of the aperture is expressed as the “f-number”: The bigger this number, the smaller the aperture.



f / 1.4



f / 2.8



f / 4



f / 8



f / 16

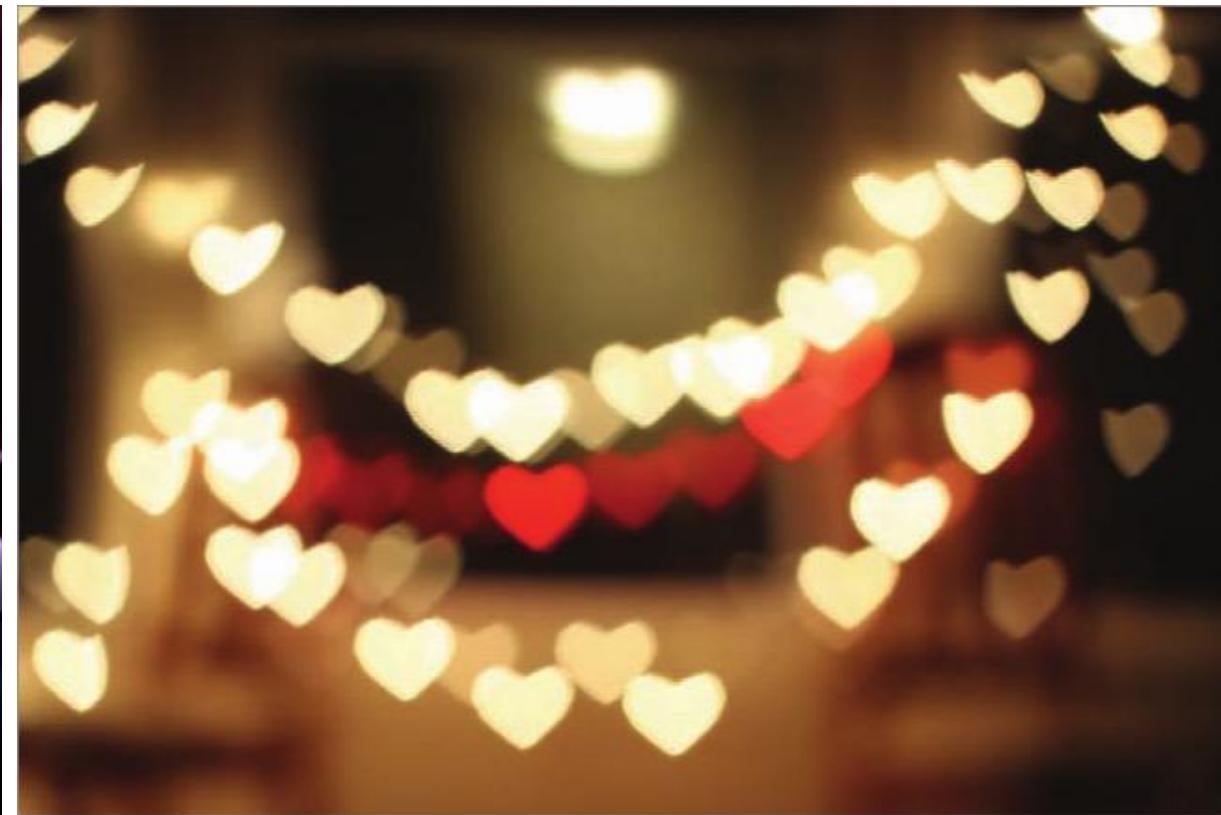
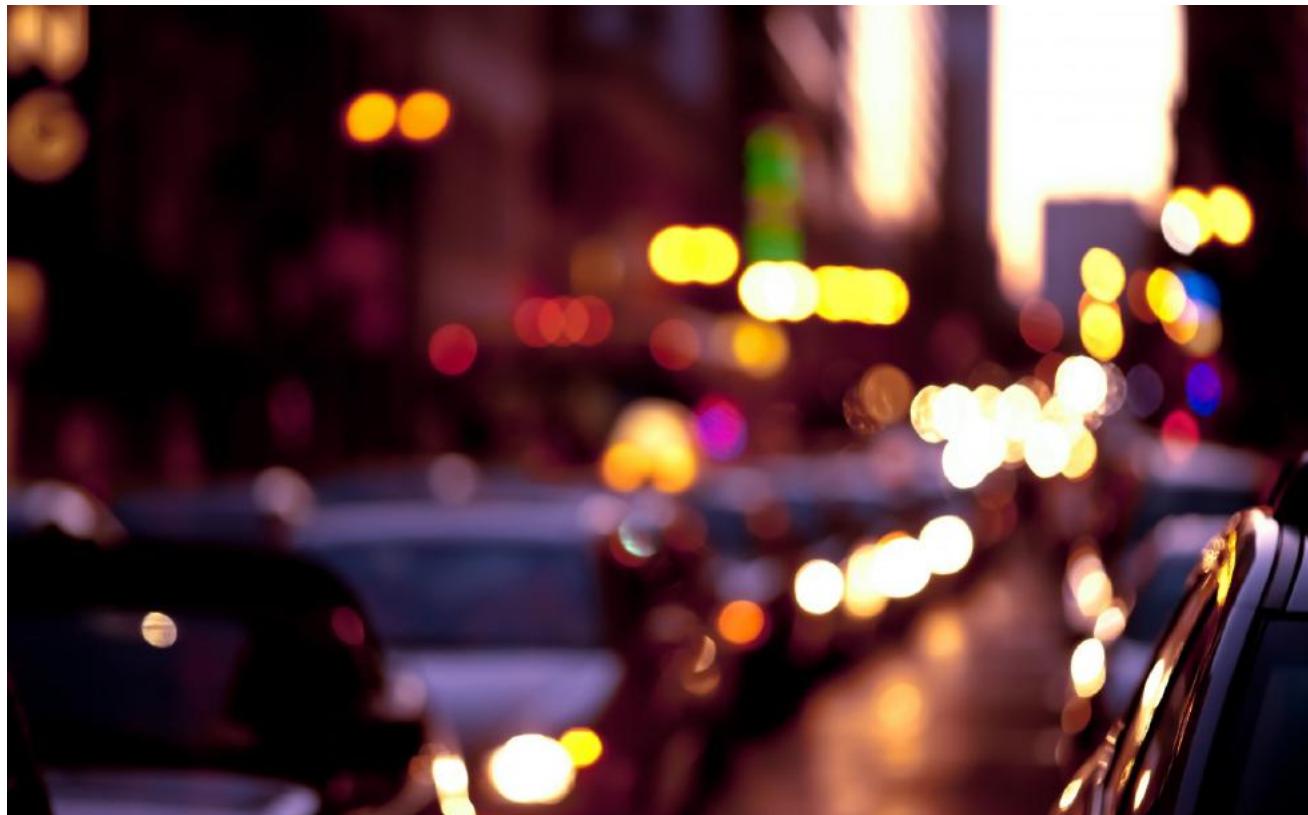
You can see the aperture by removing the lens and looking inside it.

Demonstration



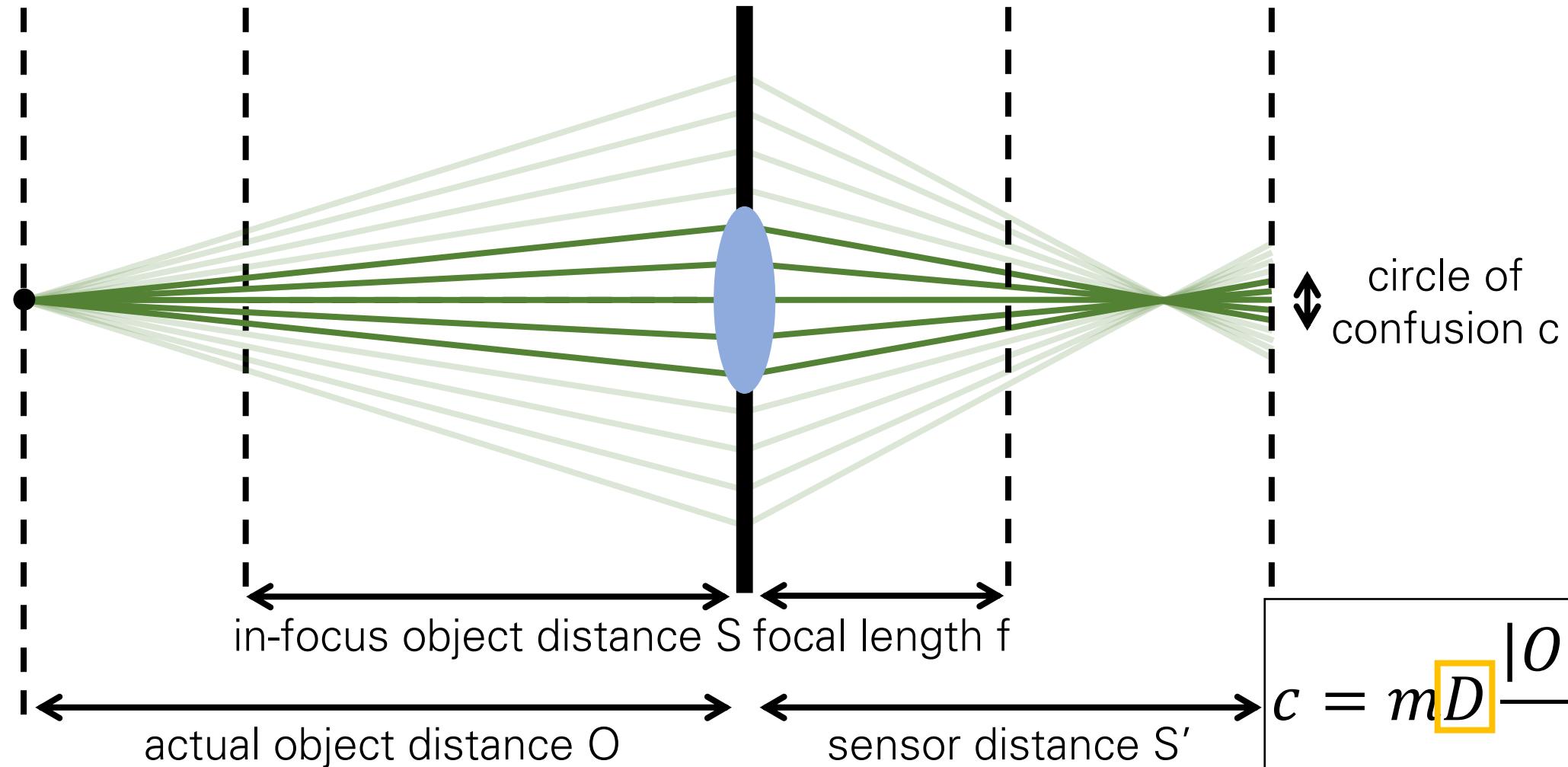
Depth of Field

Form of defocus blur is determined by shape of aperture.



Defocus depends on aperture diameter

If small aperture sizes reduce defocus blur, should we always use the smallest aperture?

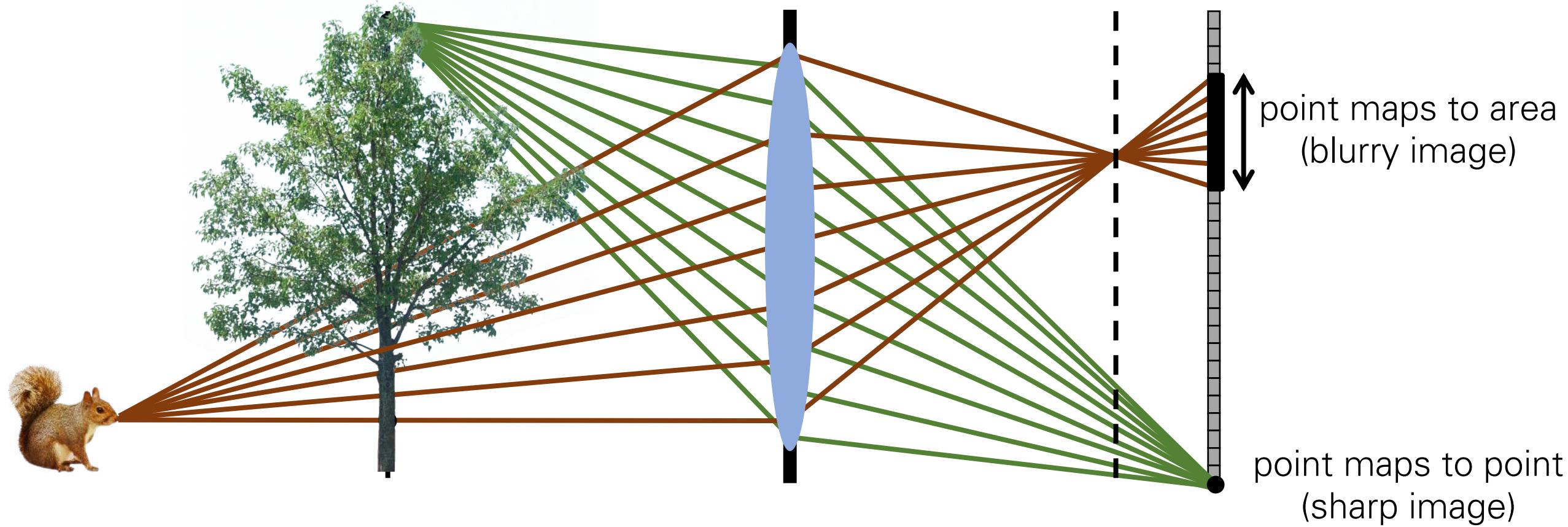


Bokeh

Sharp depth of field ("bokeh") is often desirable.

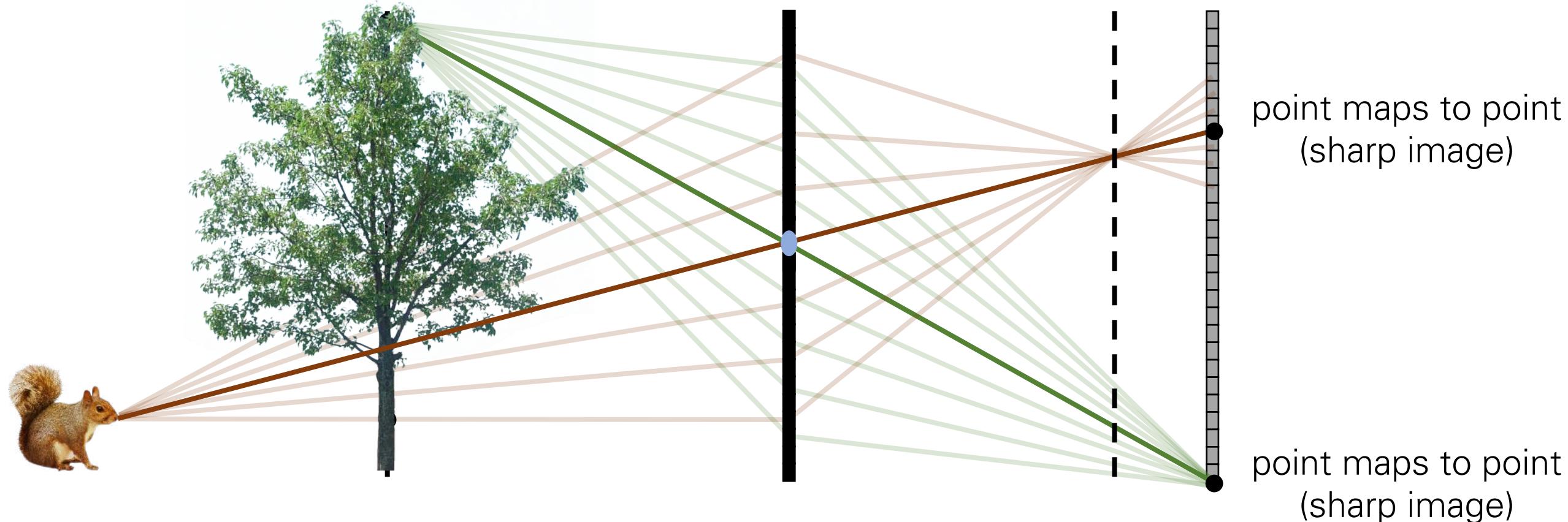


What happens as the aperture keeps getting smaller?



What happens as the aperture keeps getting smaller?

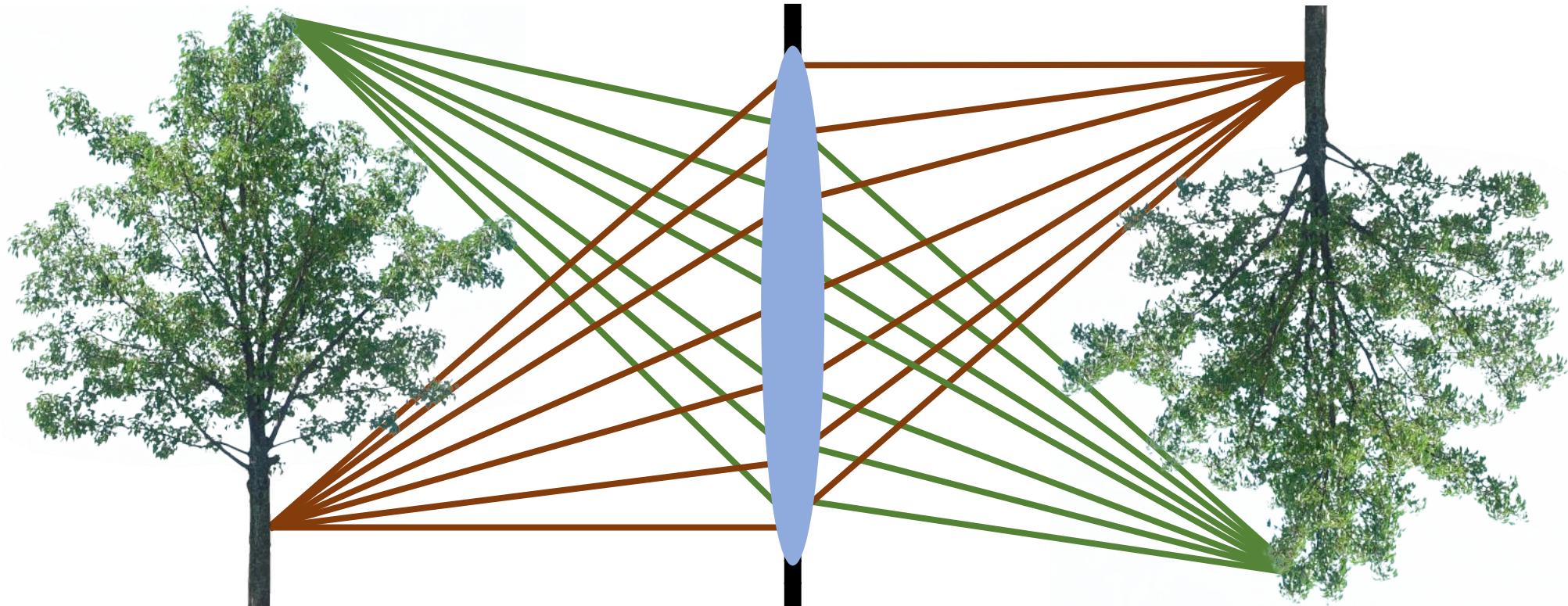
Lens becomes equivalent to a pinhole.



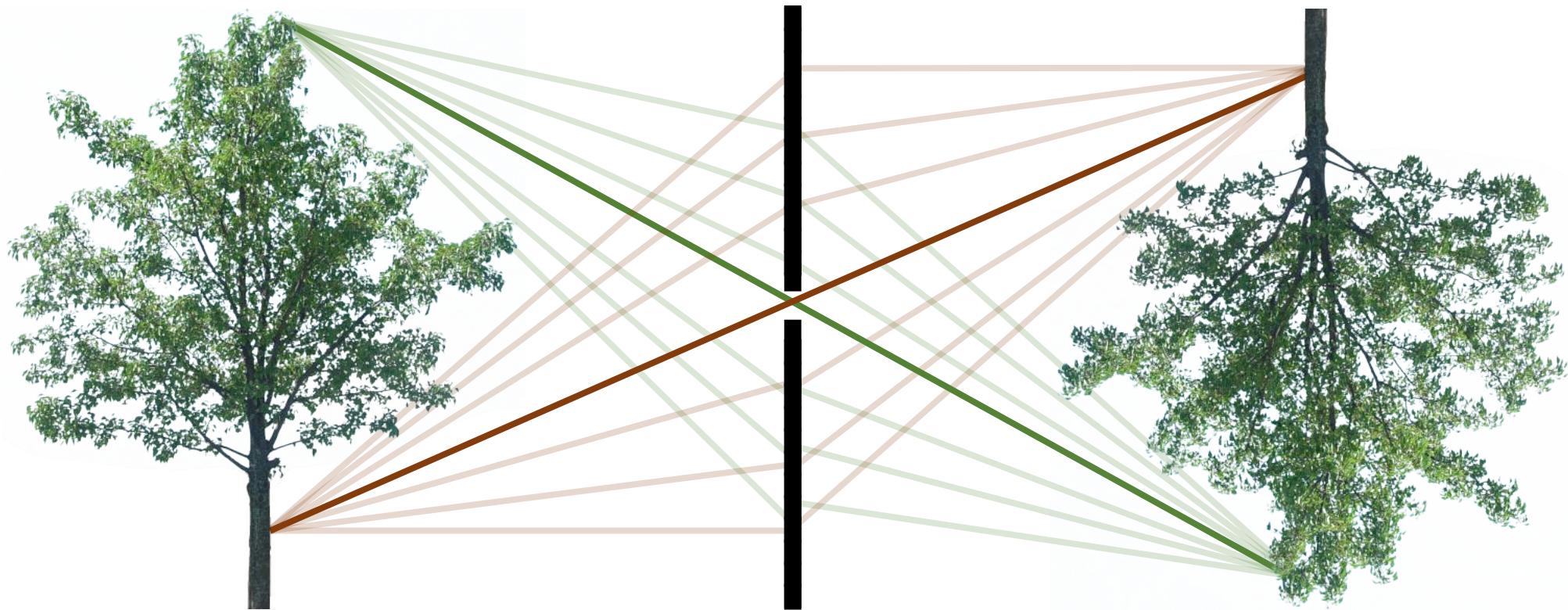
- No defocus, everything is sharp regardless of depth.
- Very little light, signal-to-noise ratio is just as bad as pinhole.

Lens camera and pinhole camera

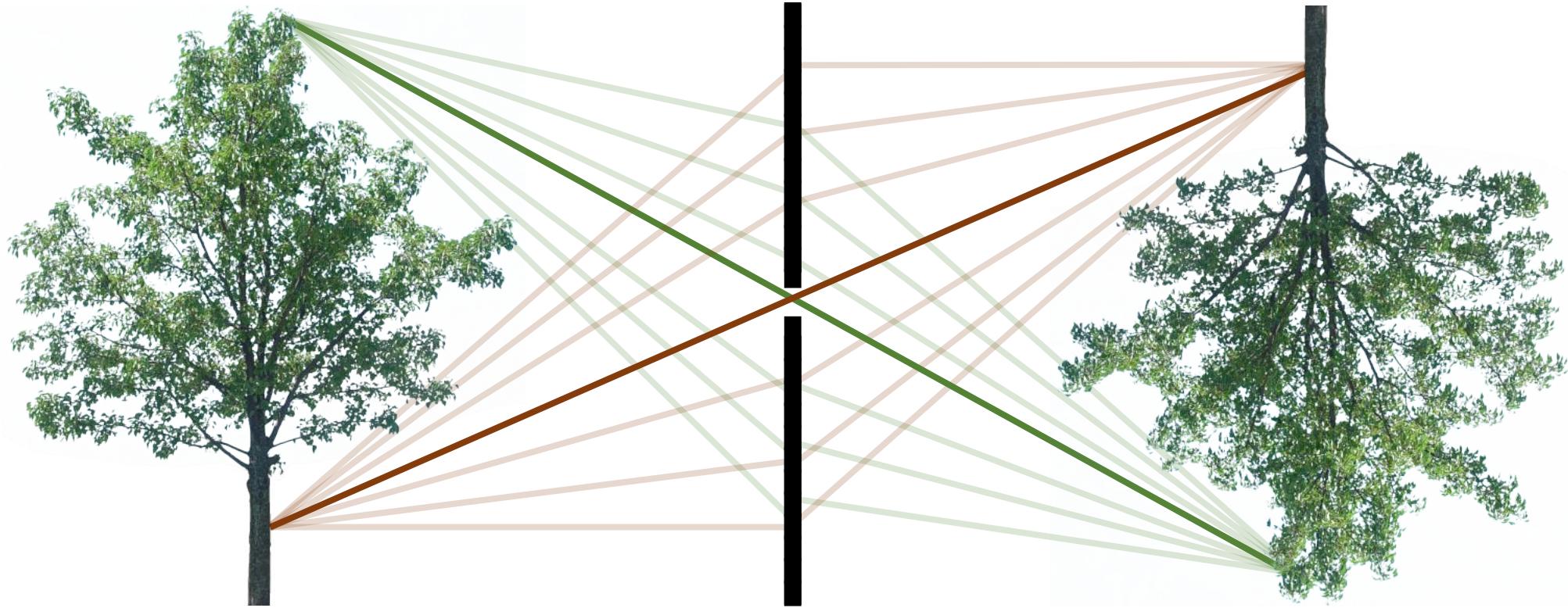
The lens camera



The pinhole camera

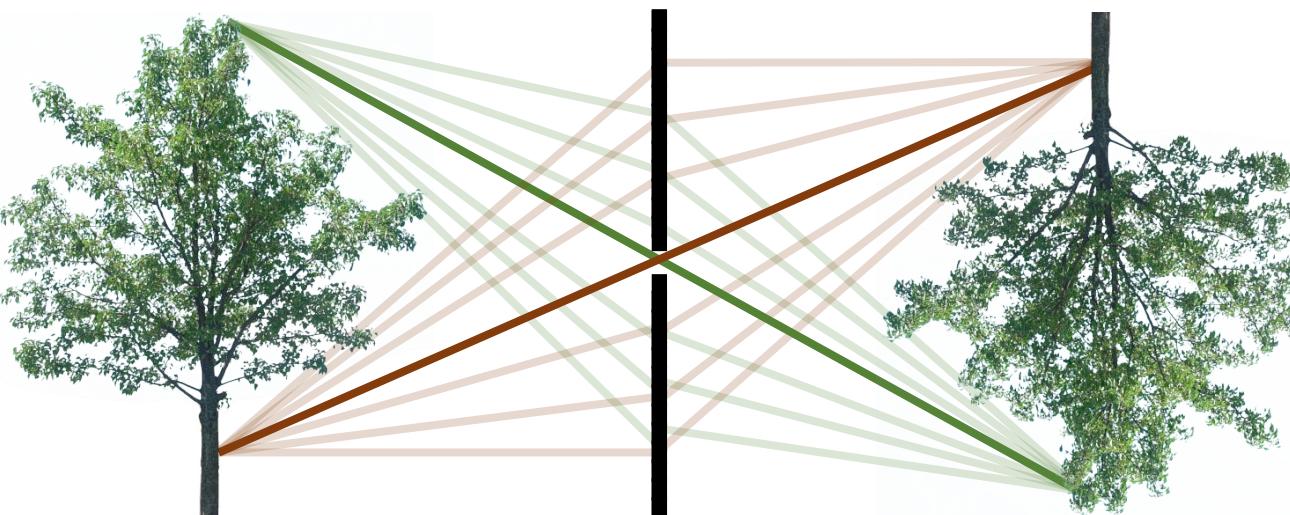
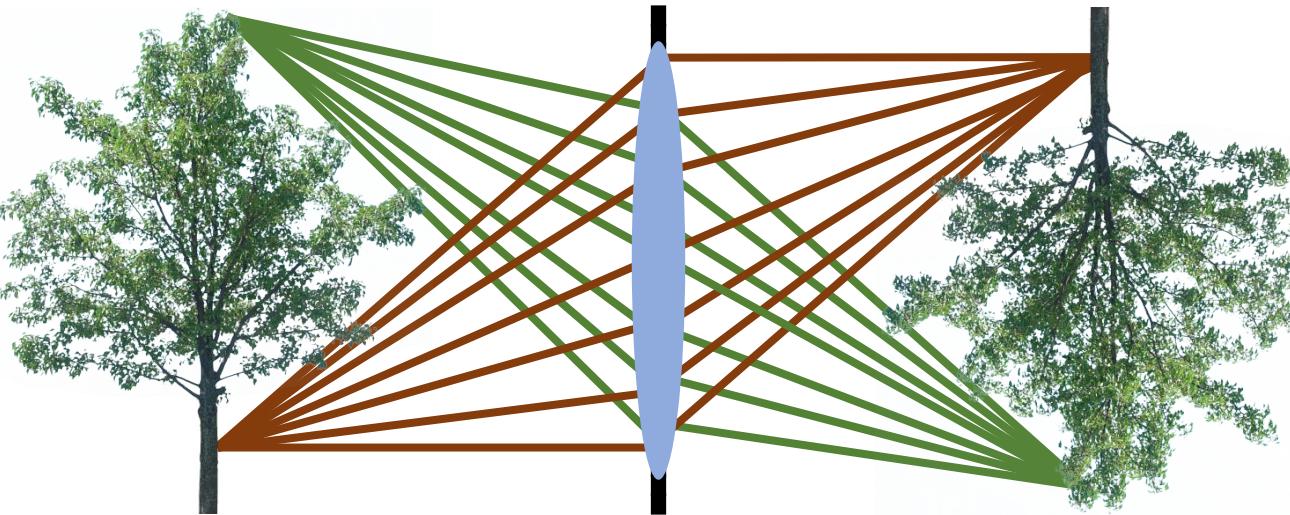


The pinhole camera



Central rays propagate in the same way for both models!

Describing both lens and pinhole cameras

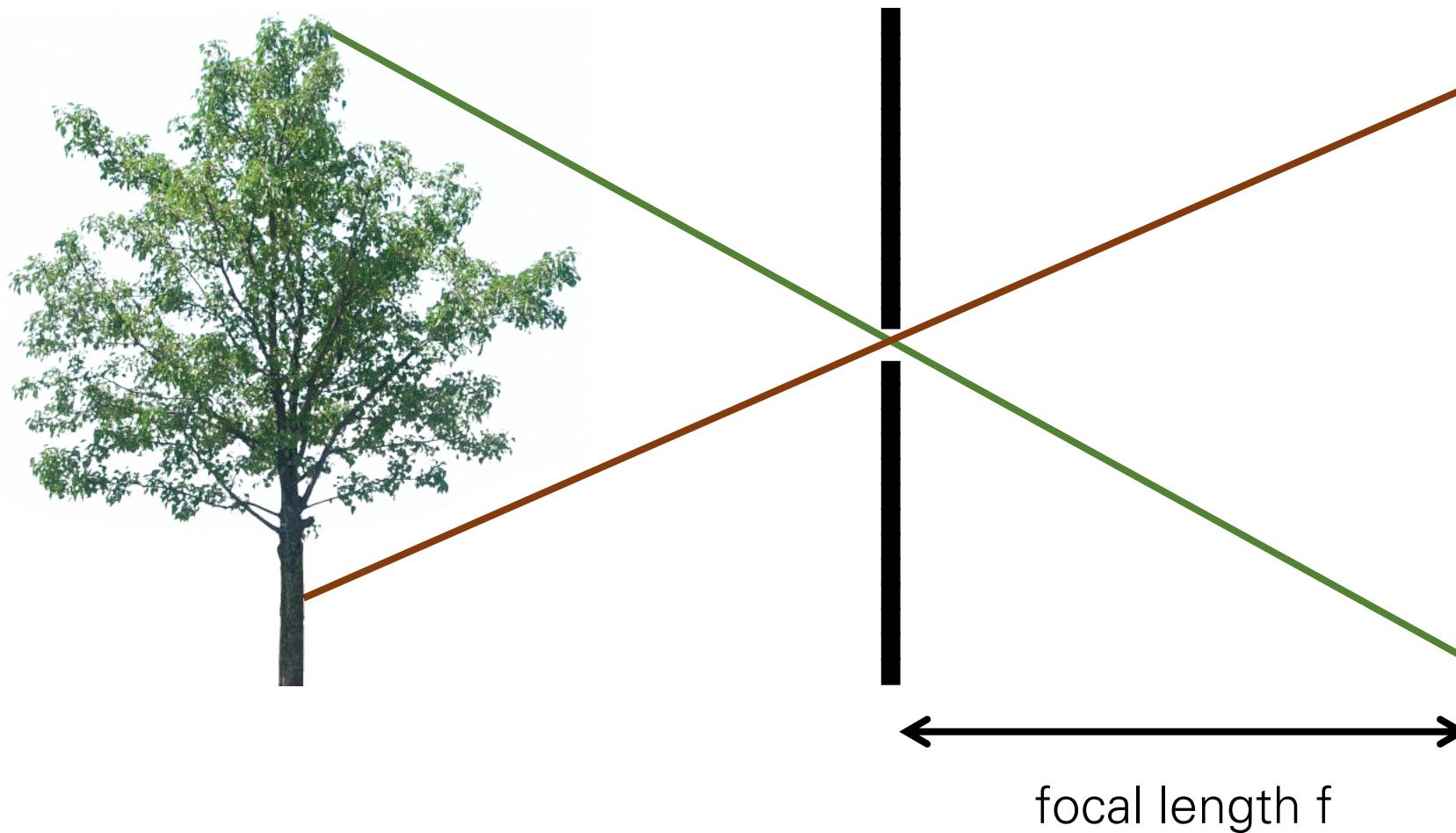


We can derive properties and descriptions that hold for both camera models if:

- We consider only central rays.
- We assume that everything of interest in the scene is within the depth of field.

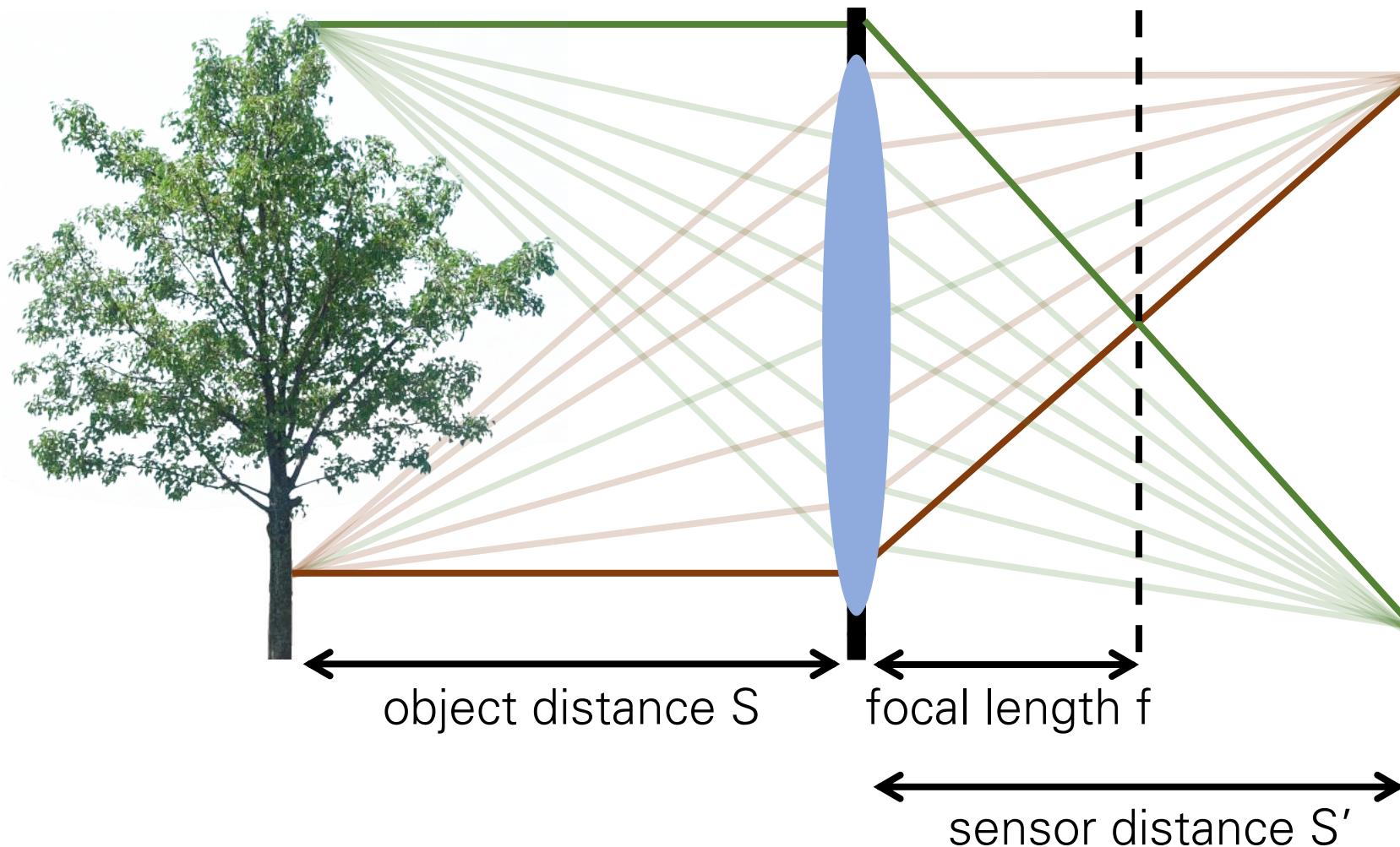
Important difference: focal length

In a pinhole camera, focal length is distance between aperture and sensor

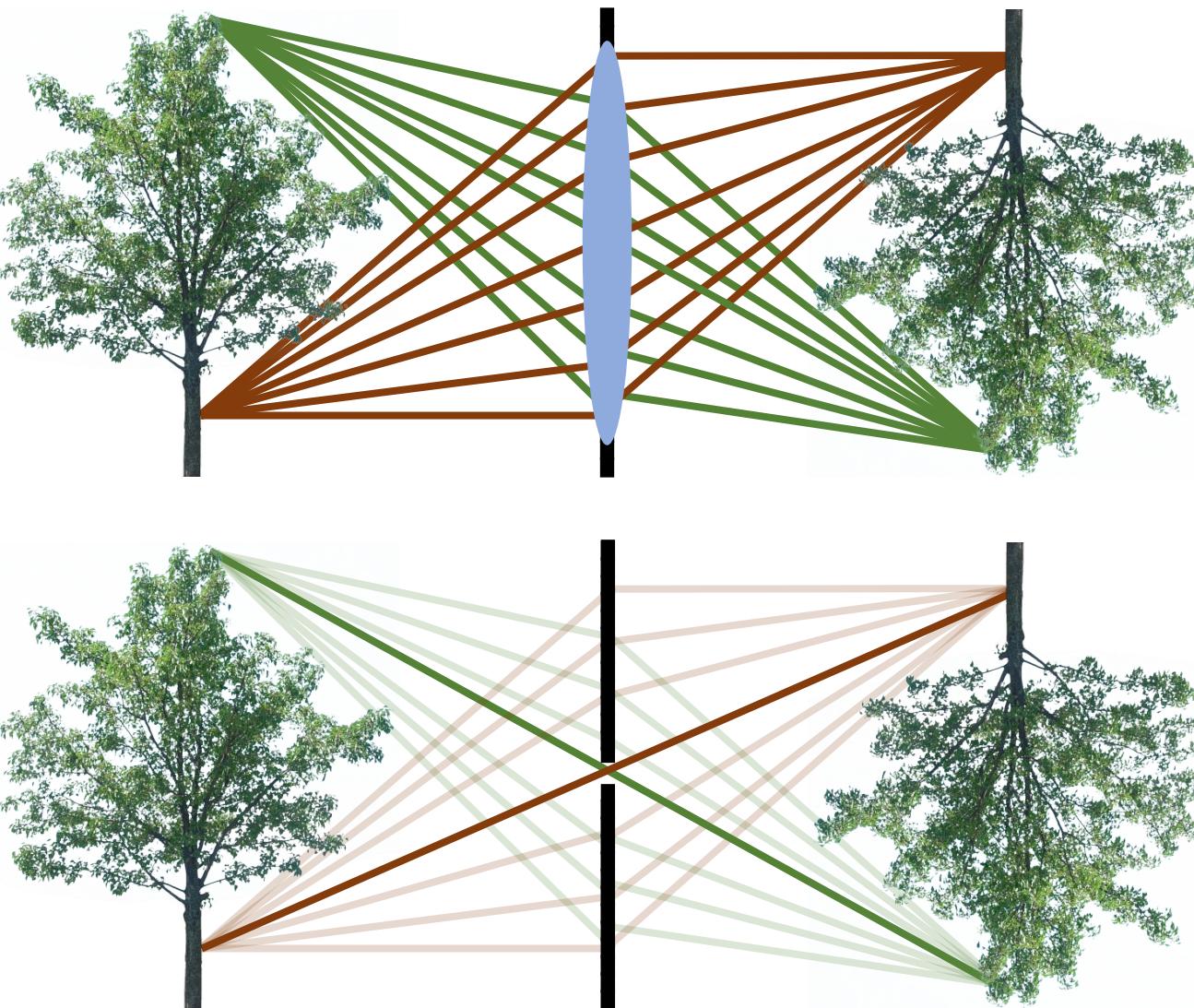


Important difference: focal length

In a lens camera, focal length is distance where parallel rays intersect



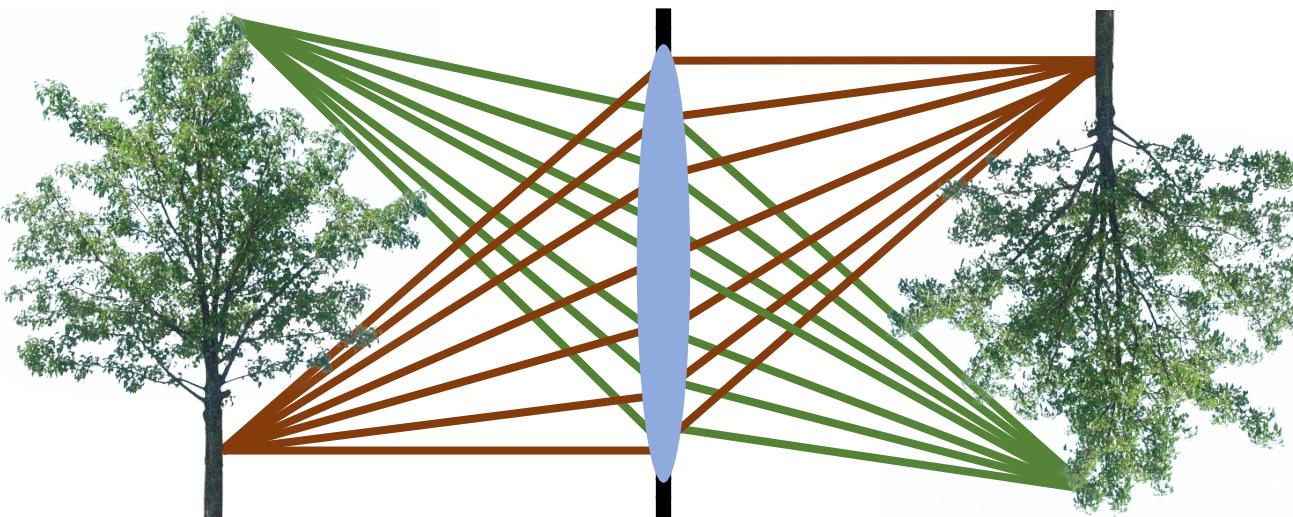
Describing both lens and pinhole cameras



We can derive properties and descriptions that hold for both camera models if:

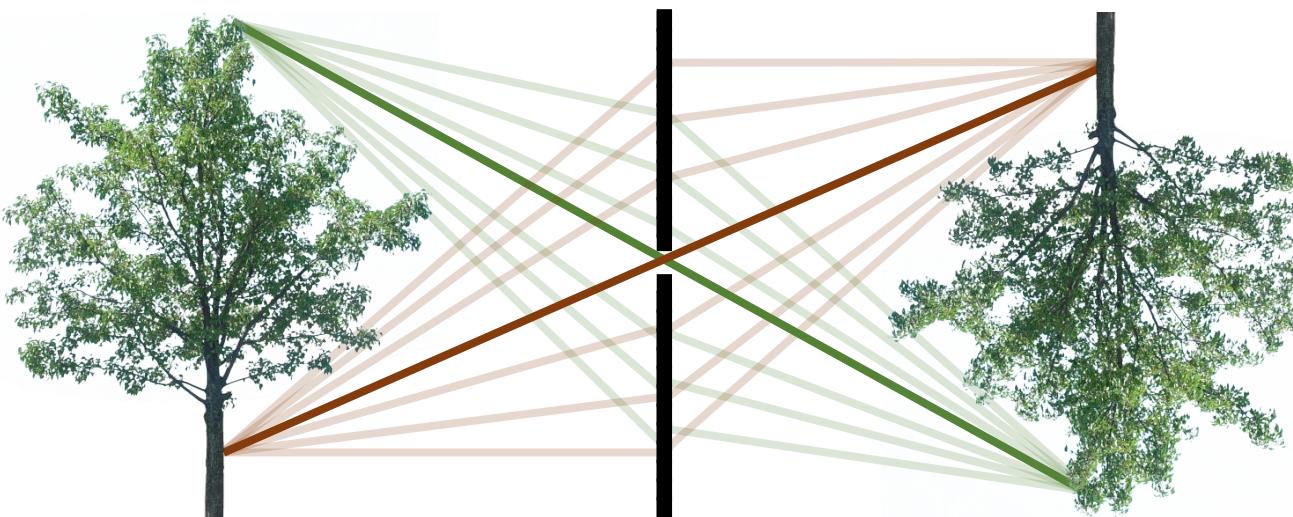
- We consider only central rays.
- We assume everything of interest in the scene is within the depth of field.
- We assume that the focus distance of the lens camera is equal to the focal length of the pinhole camera.

Effect of aperture size on lens and pinhole cameras



Doubling the aperture diameter:

- Increases light throughput by four times.
- Increases circle of confusion for out-of-focus plane by two times.
- Decreases depth of field by two times.



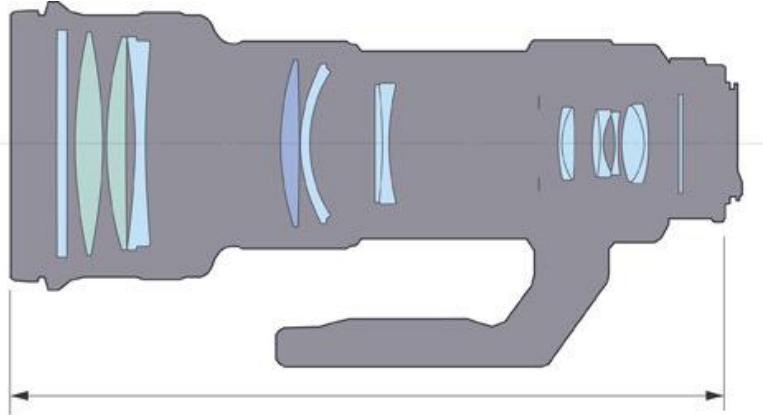
Doubling the aperture diameter:

- Increases light throughput by four times.
- Increases circle of confusion for all planes by two times.

Thin lenses are fiction!

Thin lenses are a fiction

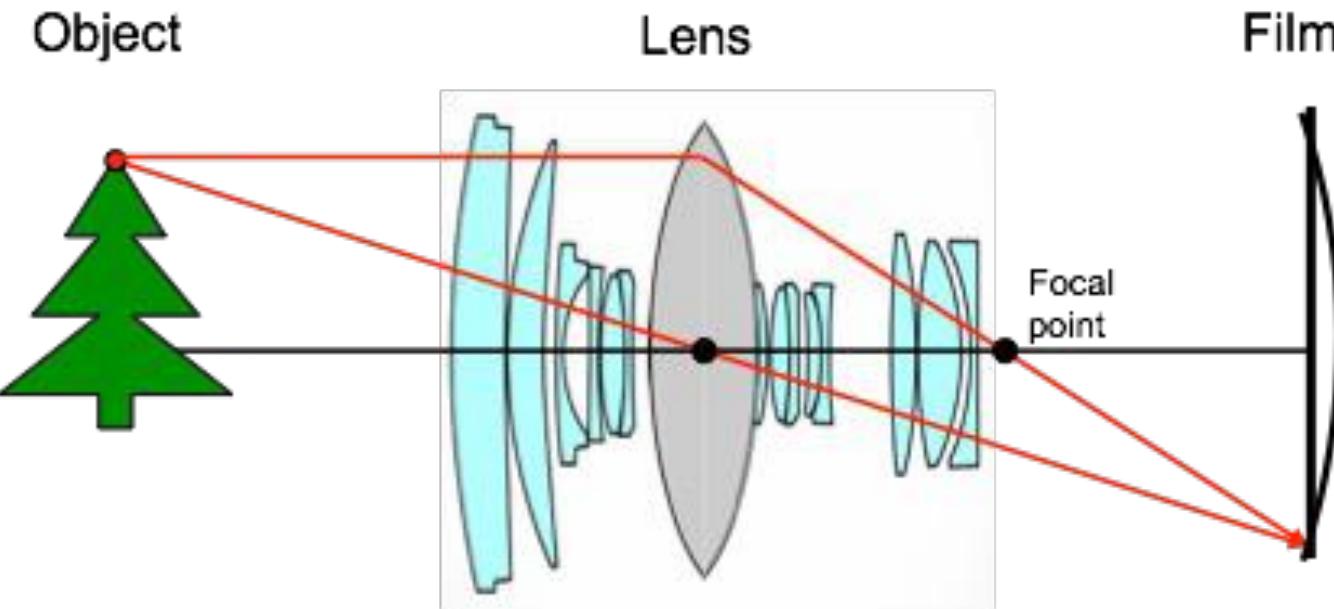
The thin lens model assumes that the lens has no thickness, but this is rarely true...



To make real lenses behave like ideal thin lenses, we have to use combinations of multiple lens elements (compound lenses).

Thin lenses are a fiction

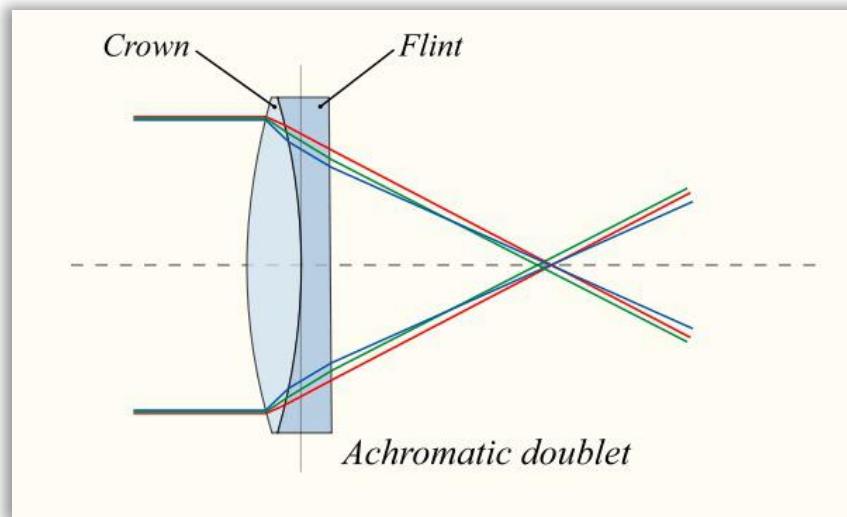
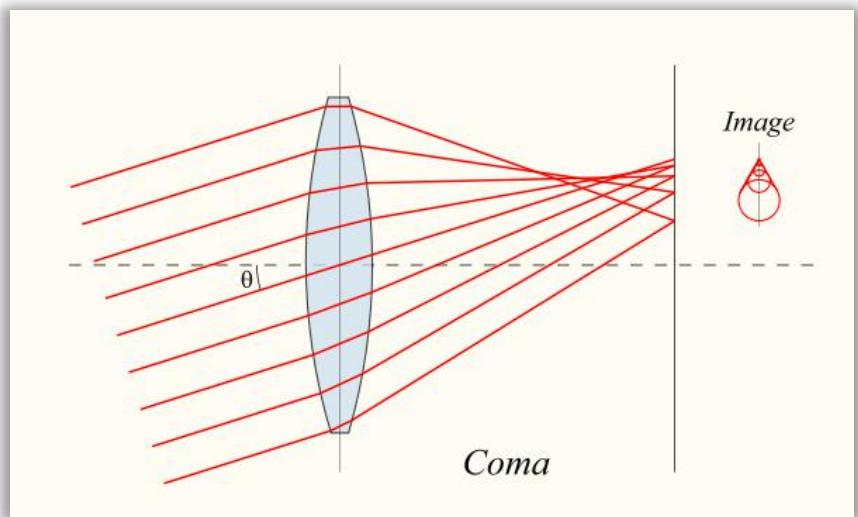
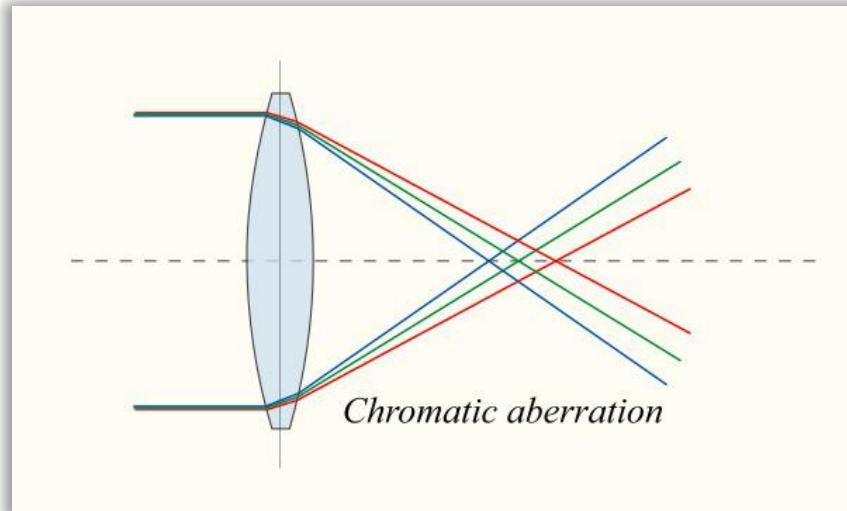
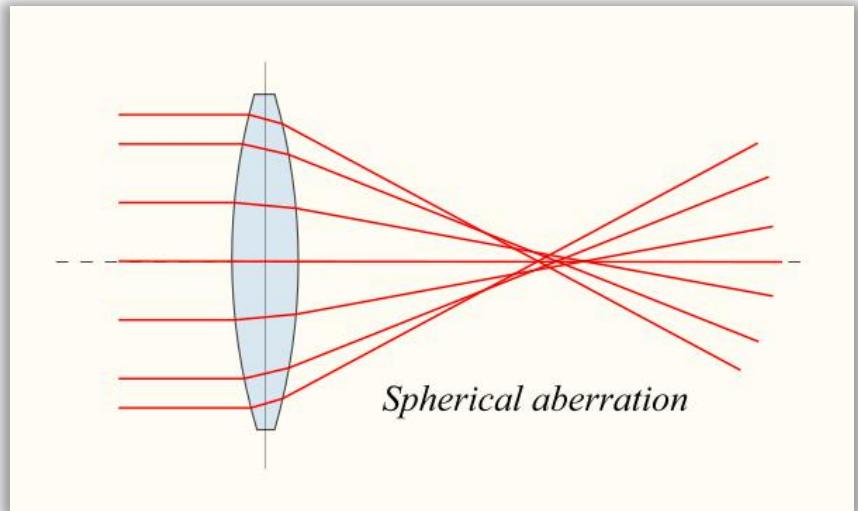
The thin lens model assumes that the lens has no thickness, but this is rarely true...



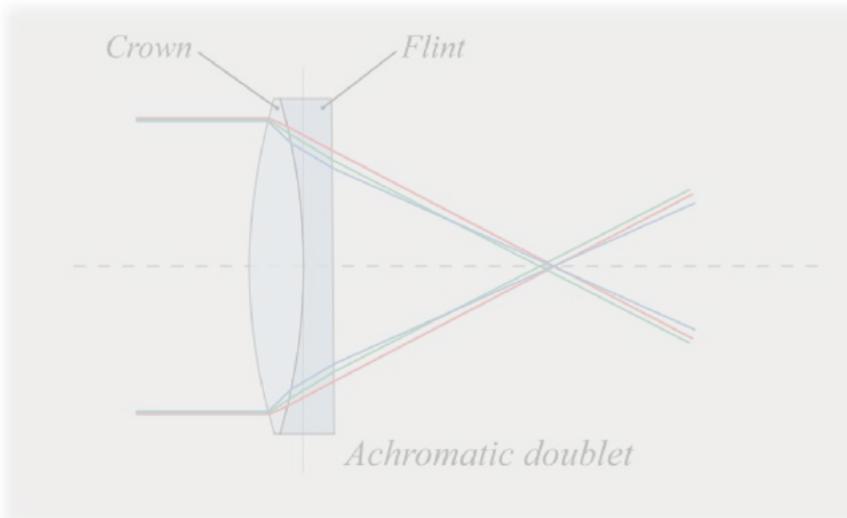
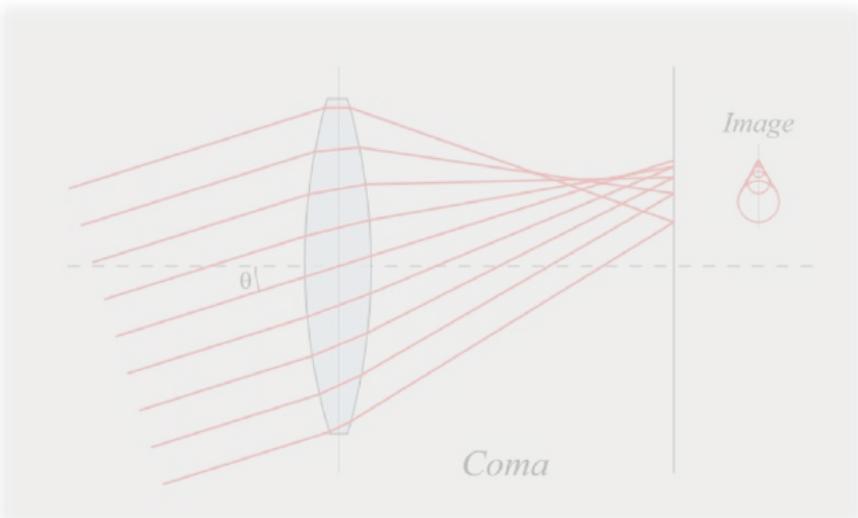
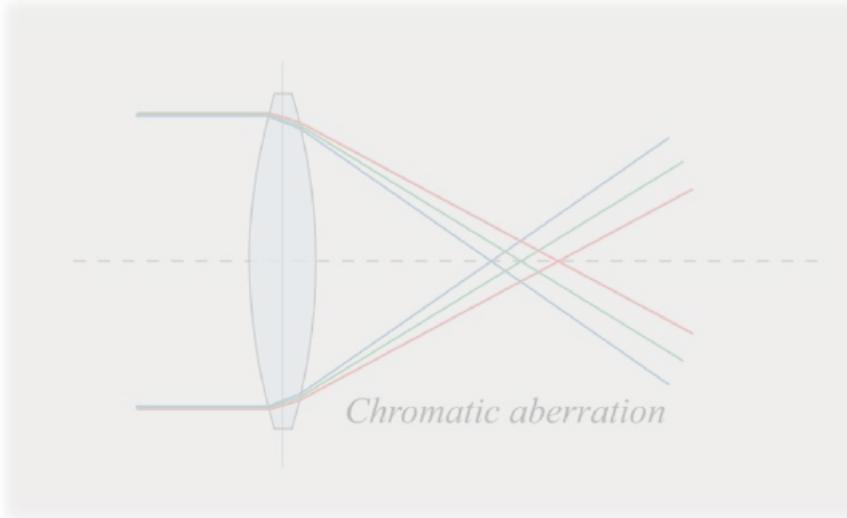
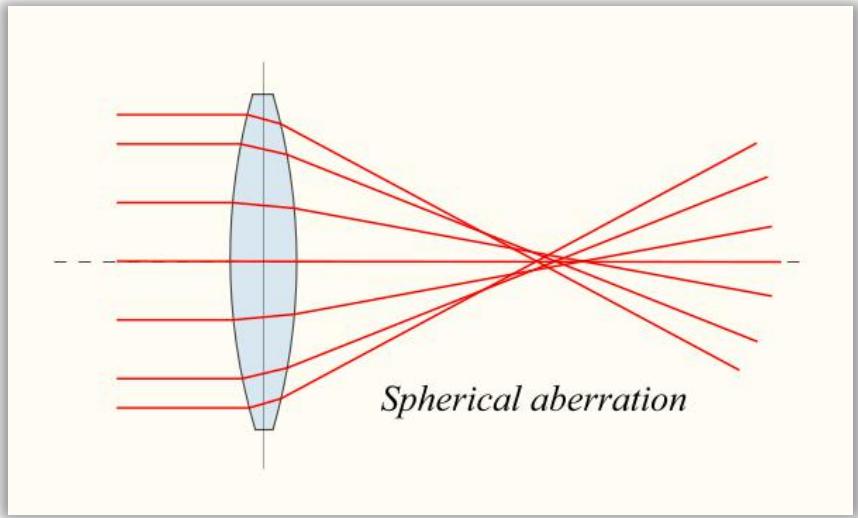
Even though we have multiple lenses, the entire optical system can be (paraxially) described using a single thin lens of some equivalent focal length and aperture number.

To make real lenses behave like ideal thin lenses, we have to use combinations of multiple lens elements (compound lenses).

Lenses - Aberrations

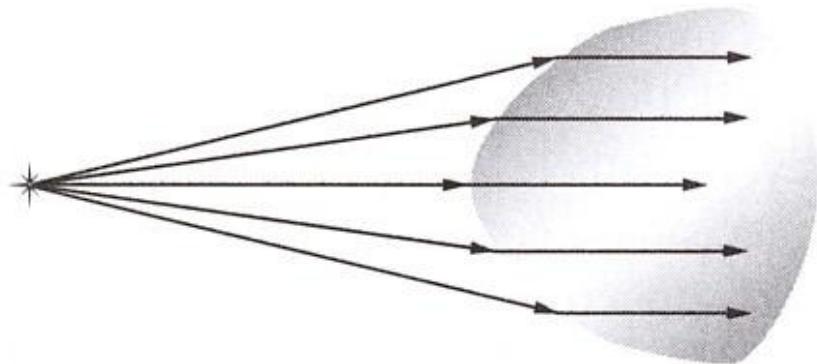


Lenses - Aberrations



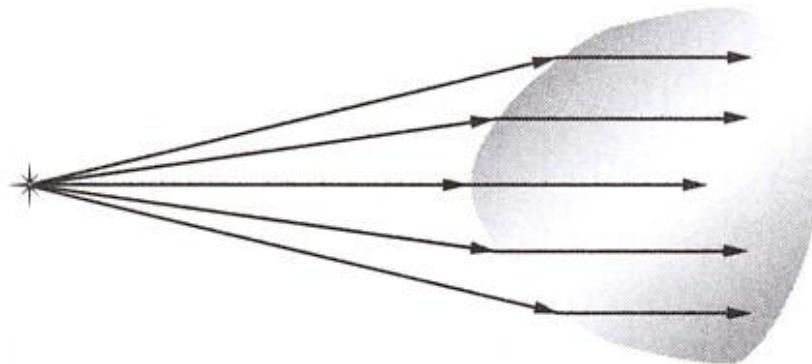
Refraction at interfaces of complicated shapes

What shape should an interface have to make parallel rays converge to a point?



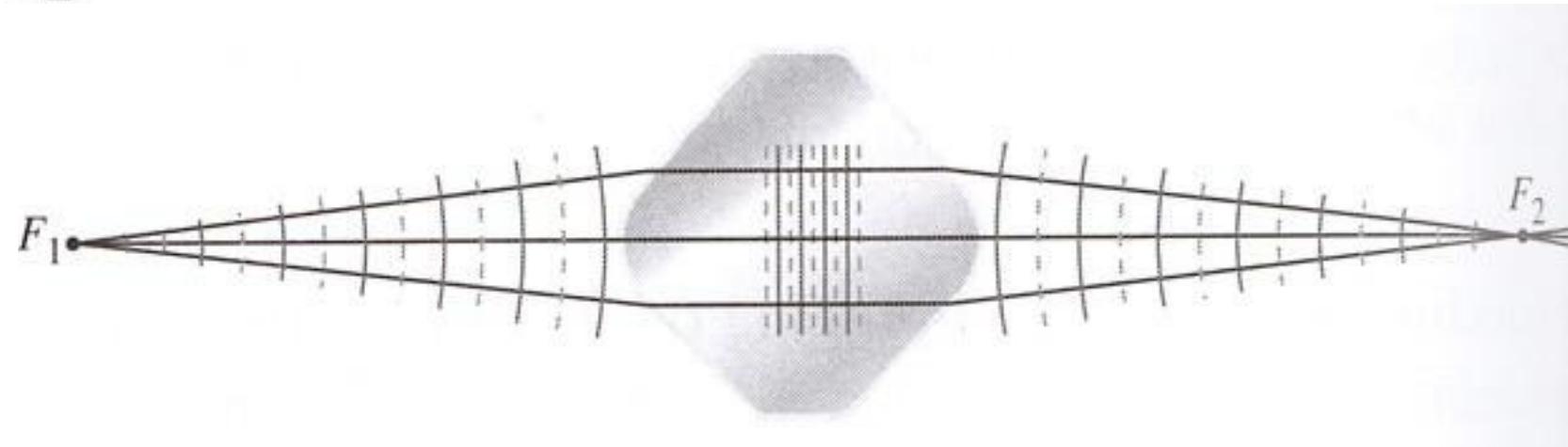
Refraction at interfaces of complicated shapes

What shape should an interface have to make parallel rays converge to a point?



Single hyperbolic interface:
point to parallel rays

Double hyperbolic interface:
point to point rays

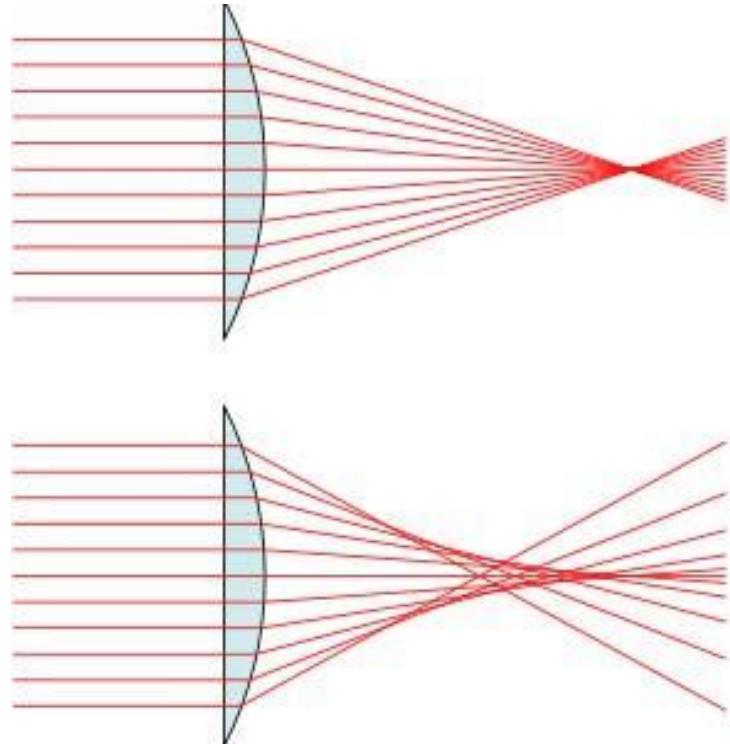


What shape should an interface have to make parallel rays converge to a point?

Spherical lenses

In practice, lenses are often made to have spherical interfaces for ease of fabrication.

- Two roughly fitting curved surfaces ground together will eventually become spherical.



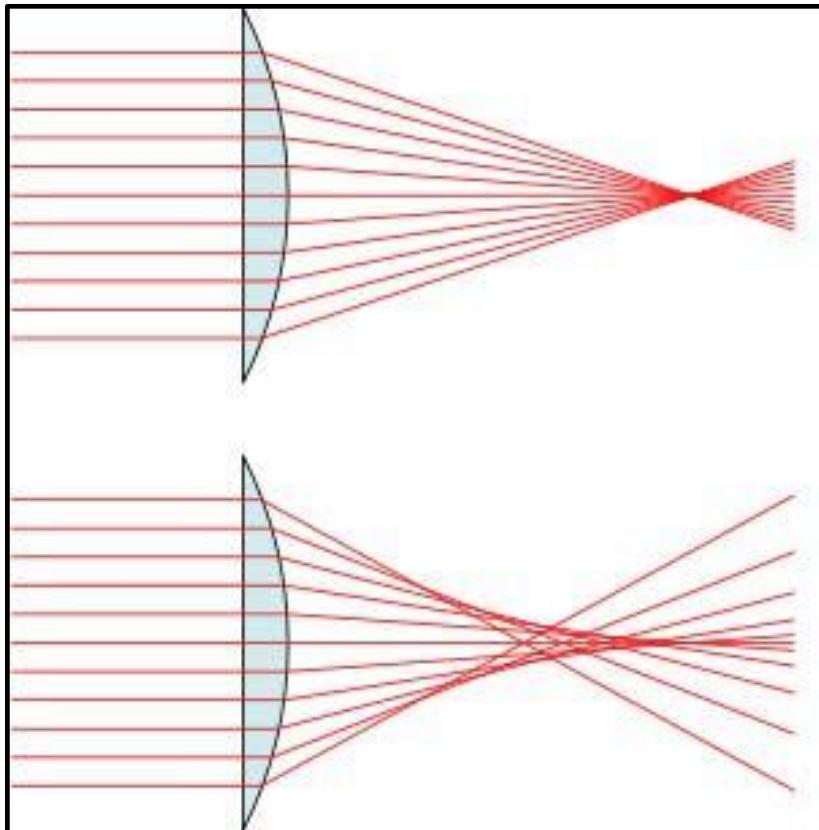
Spherical lenses don't bring parallel rays to a point.

- This is called spherical aberration.
- Approximately axial (i.e., paraxial) rays behave better.

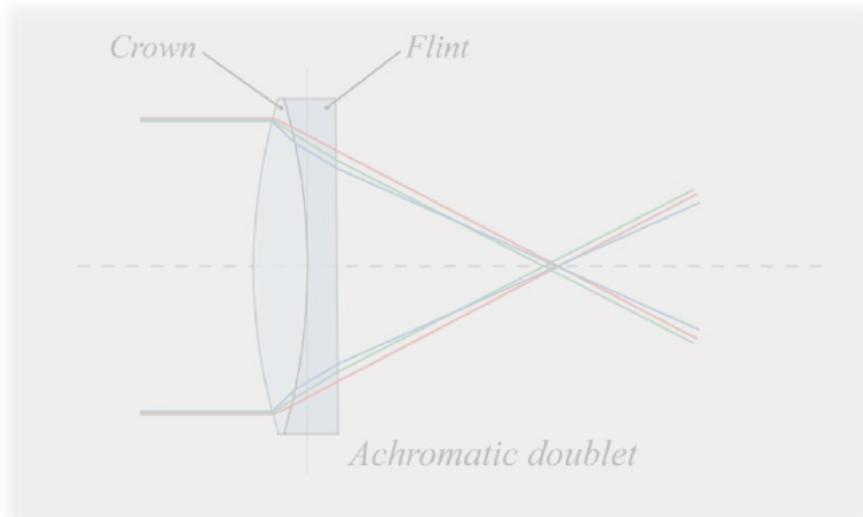
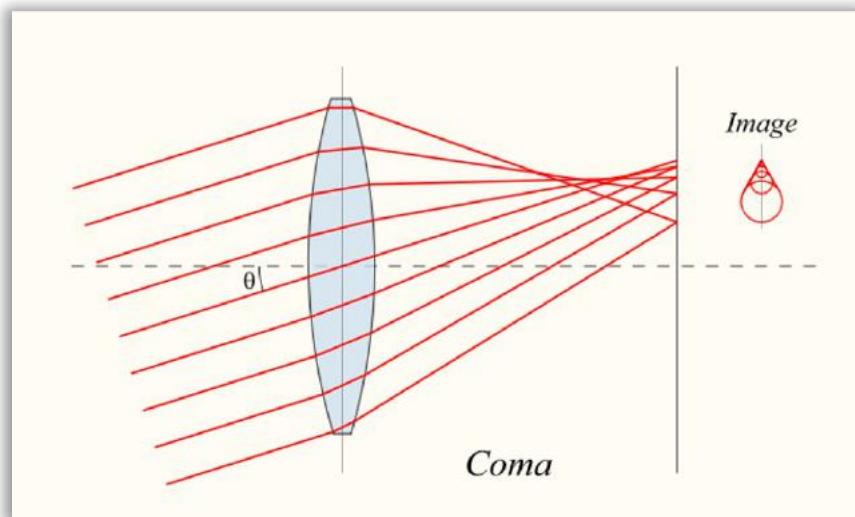
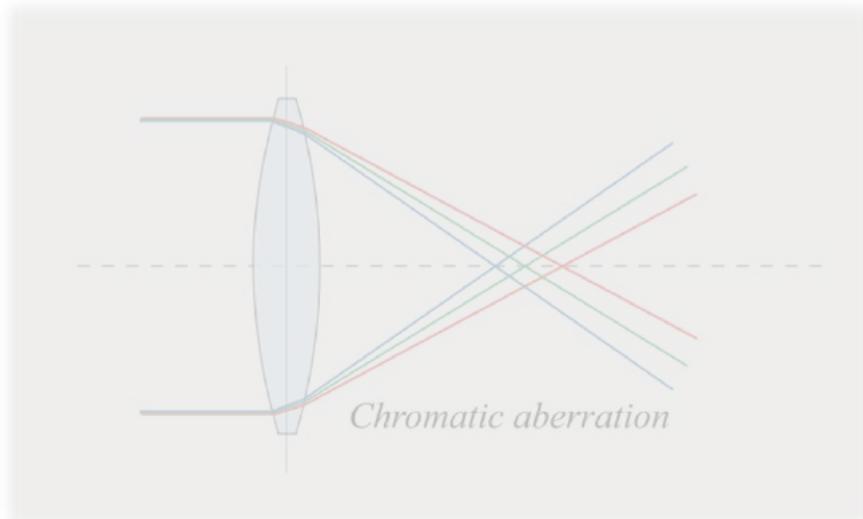
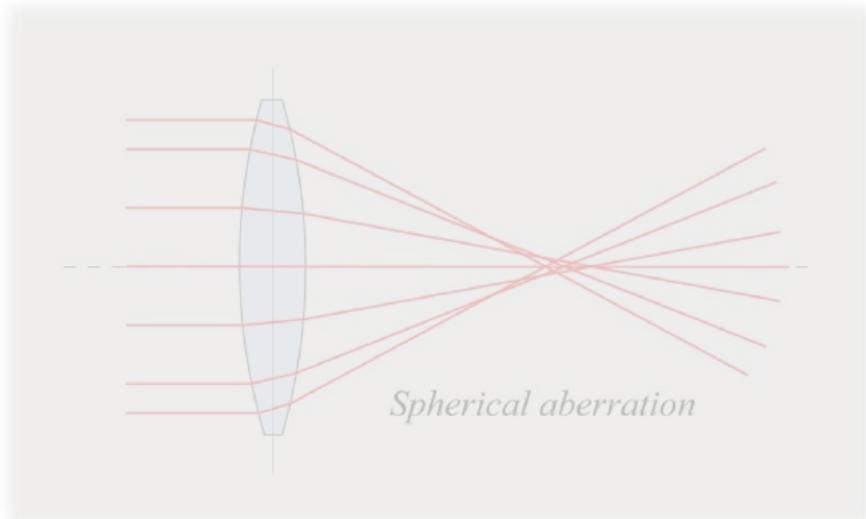
Aberrations

Deviations from ideal thin lens behavior (e.g., imperfect focus).

- Example: spherical aberration.



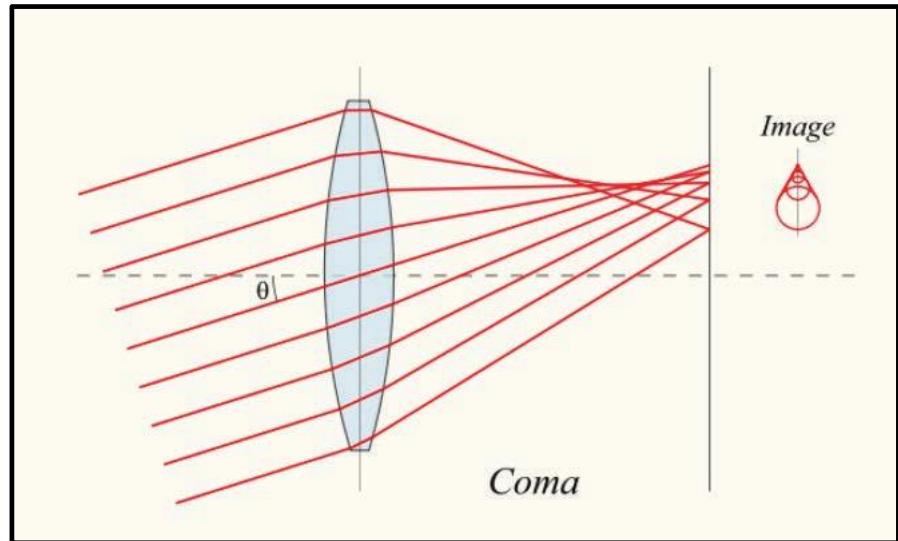
Lenses - Aberrations



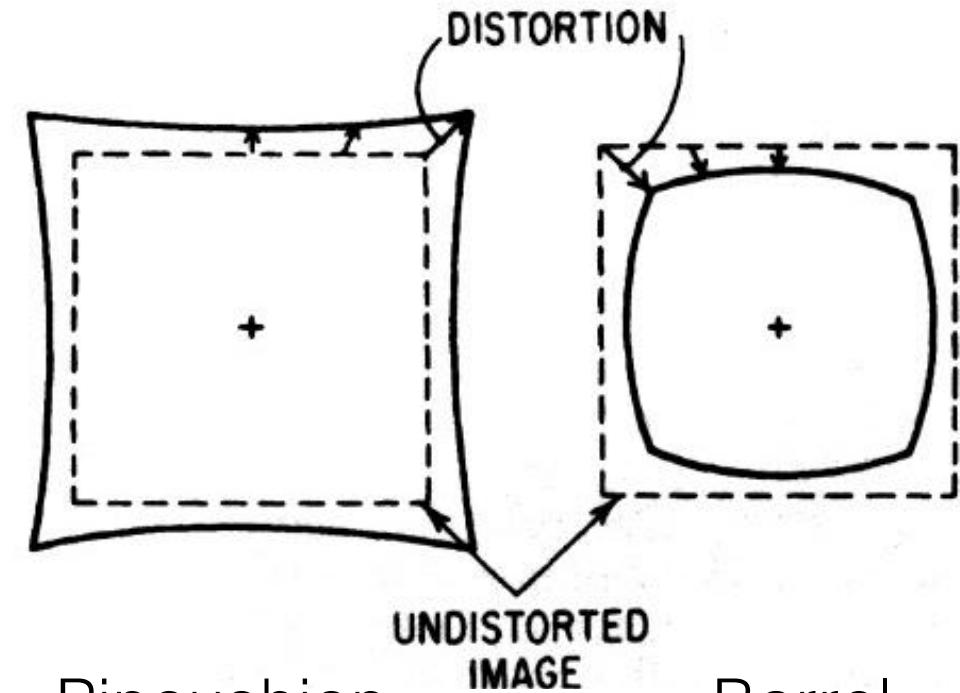
Oblique aberrations

These appear only as we move further from the center of the field of view.

- Contrast with spherical and chromatic, which appear everywhere.
- Many other examples (astigmatism, field curvature, etc.).



Coma



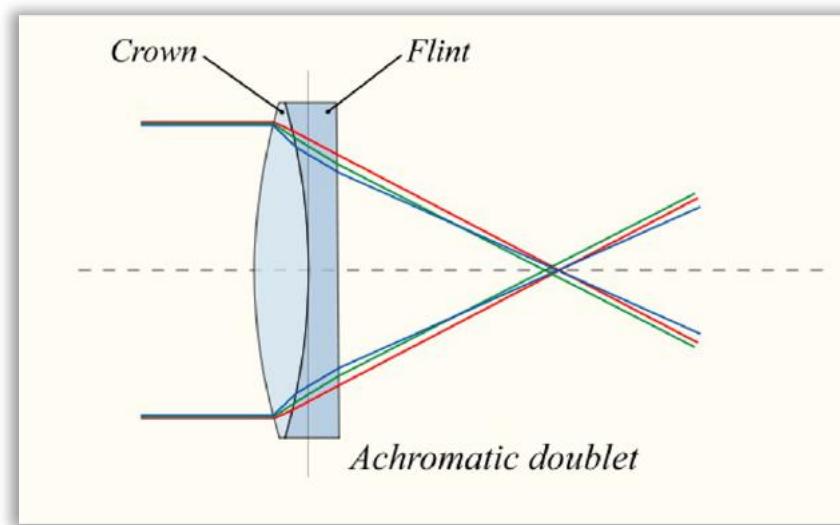
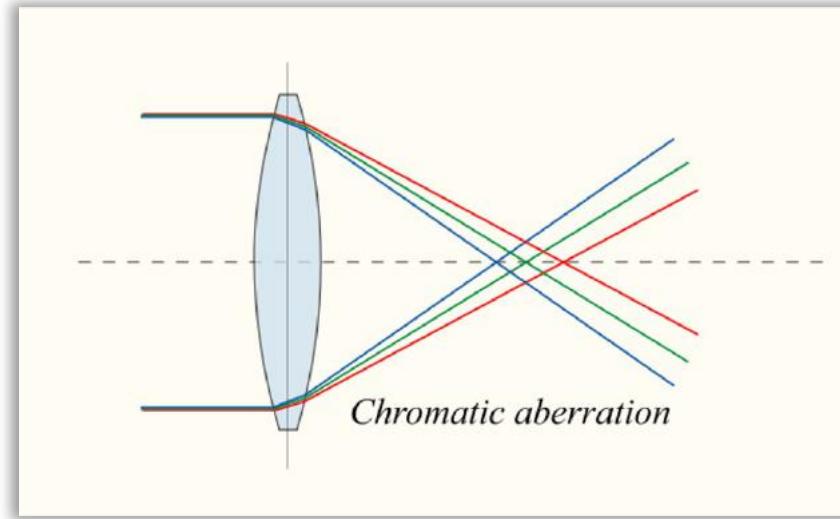
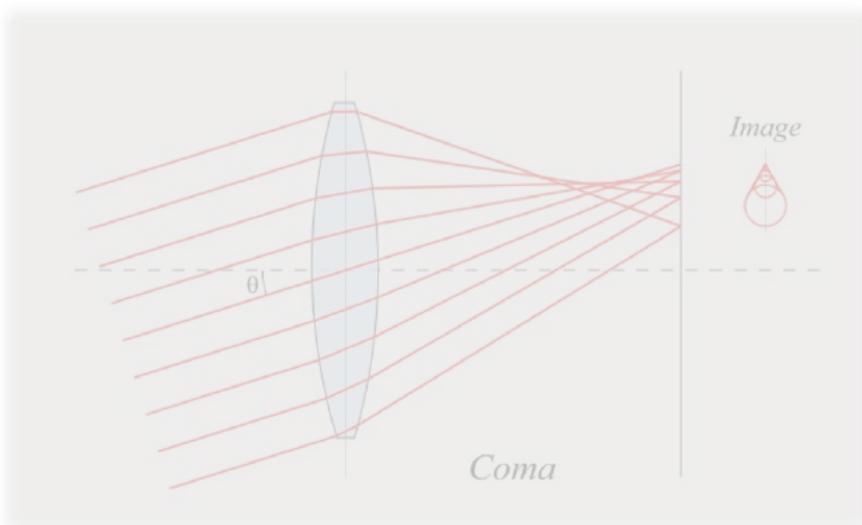
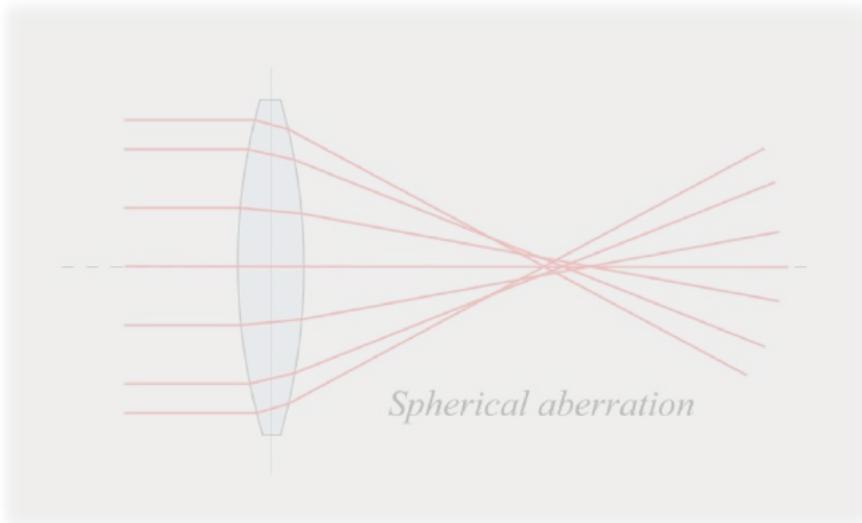
Pincushion

Barrel

Distortion example



Lenses - Aberrations

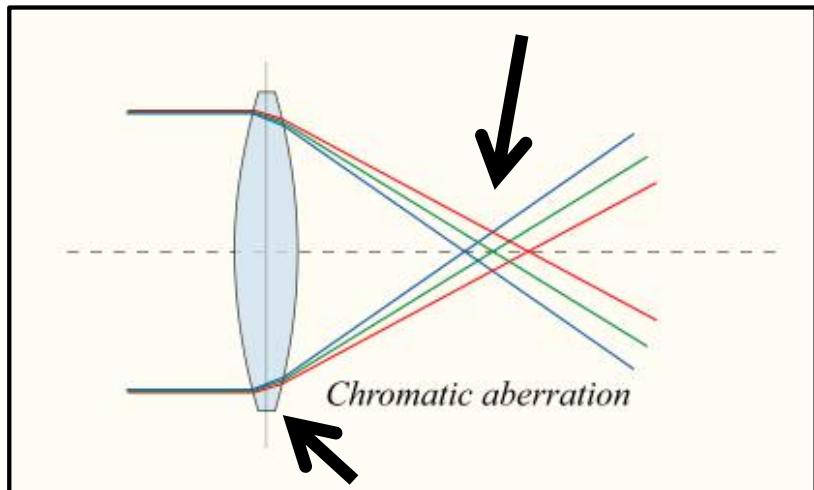


Aberrations

Deviations from ideal thin lens behavior (e.g., imperfect focus).

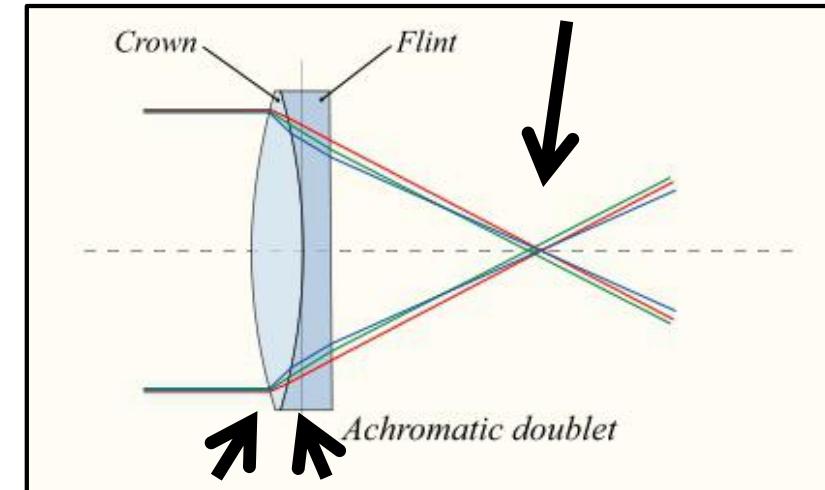
- Example: chromatic aberration.

focal length shifts with wavelength



glass has dispersion (refractive index changes with wavelength)

one lens cancels out dispersion of other



glasses of different refractive index

Using a doublet (two-element compound lens), we can reduce chromatic aberration.

Chromatic aberration examples



Field of view

Field of view

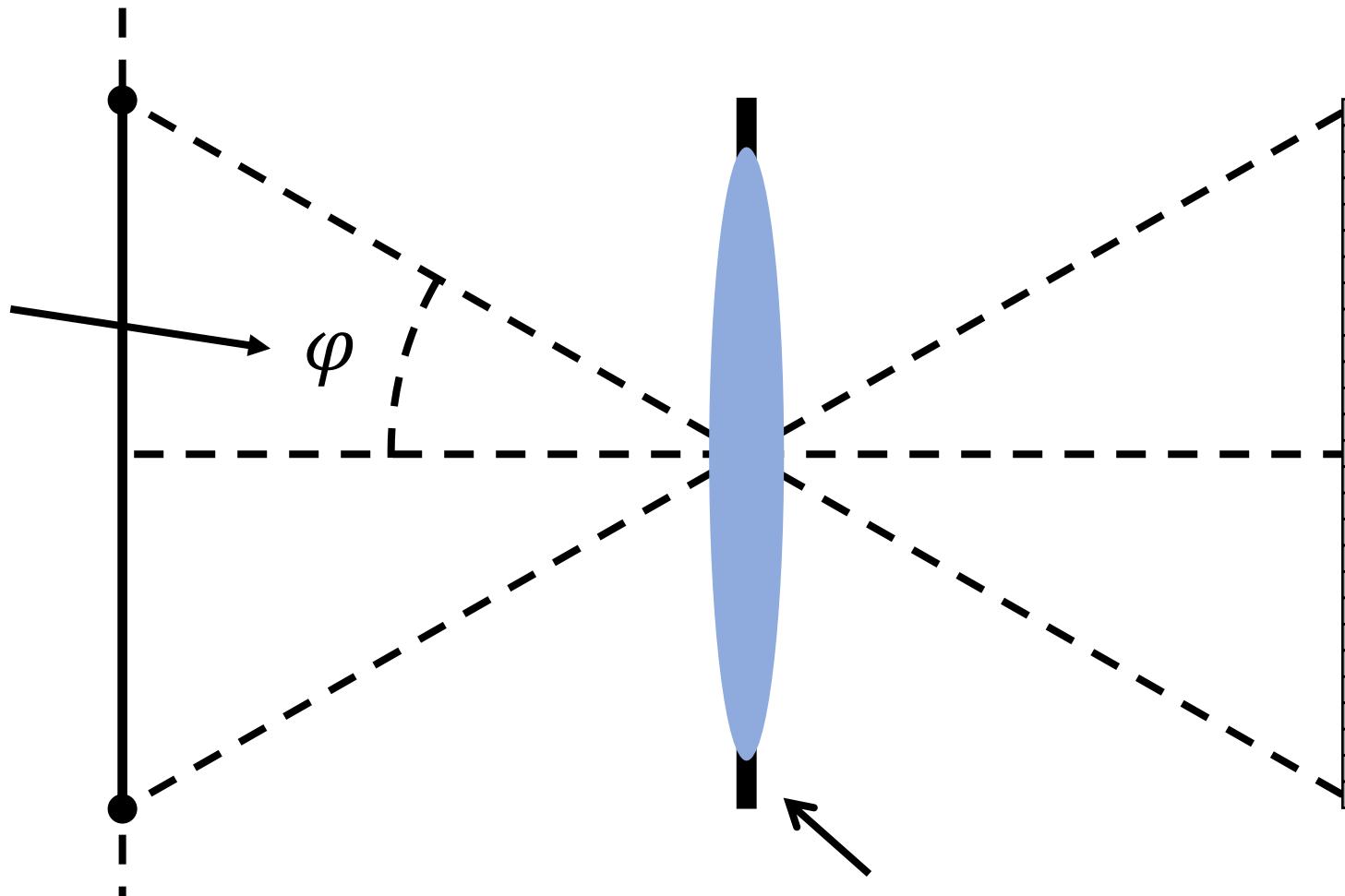
- Determines how much of scene is in frame
- Traditionally specified by focal length
 - but interpreting this number requires considering the “format,” or size of the film or sensor
- After decades of 35mm, that format is stuck in our heads
 - fields of view are usually discussed using the numbers that would be written on a lens for the 35mm format
- Changing FOV while keeping the camera fixed
 - strictly “crops” the image: relationships between objects are fixed corresponds to turning the zoom control on a modern camera

What happens as you take a closer look?



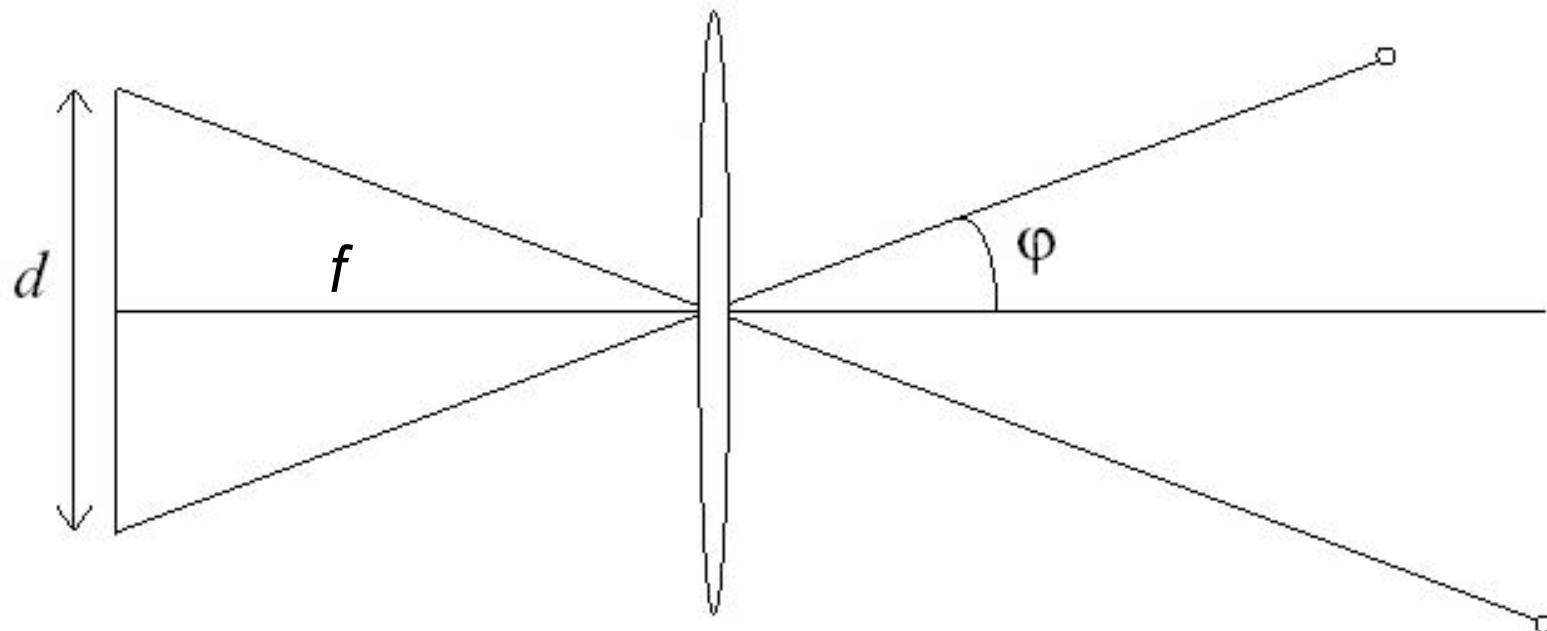
Field of view

also described
using angle of
view



Note: here I drew a lens, but I could have just as well drawn a pinhole

Field of view depends on focal length



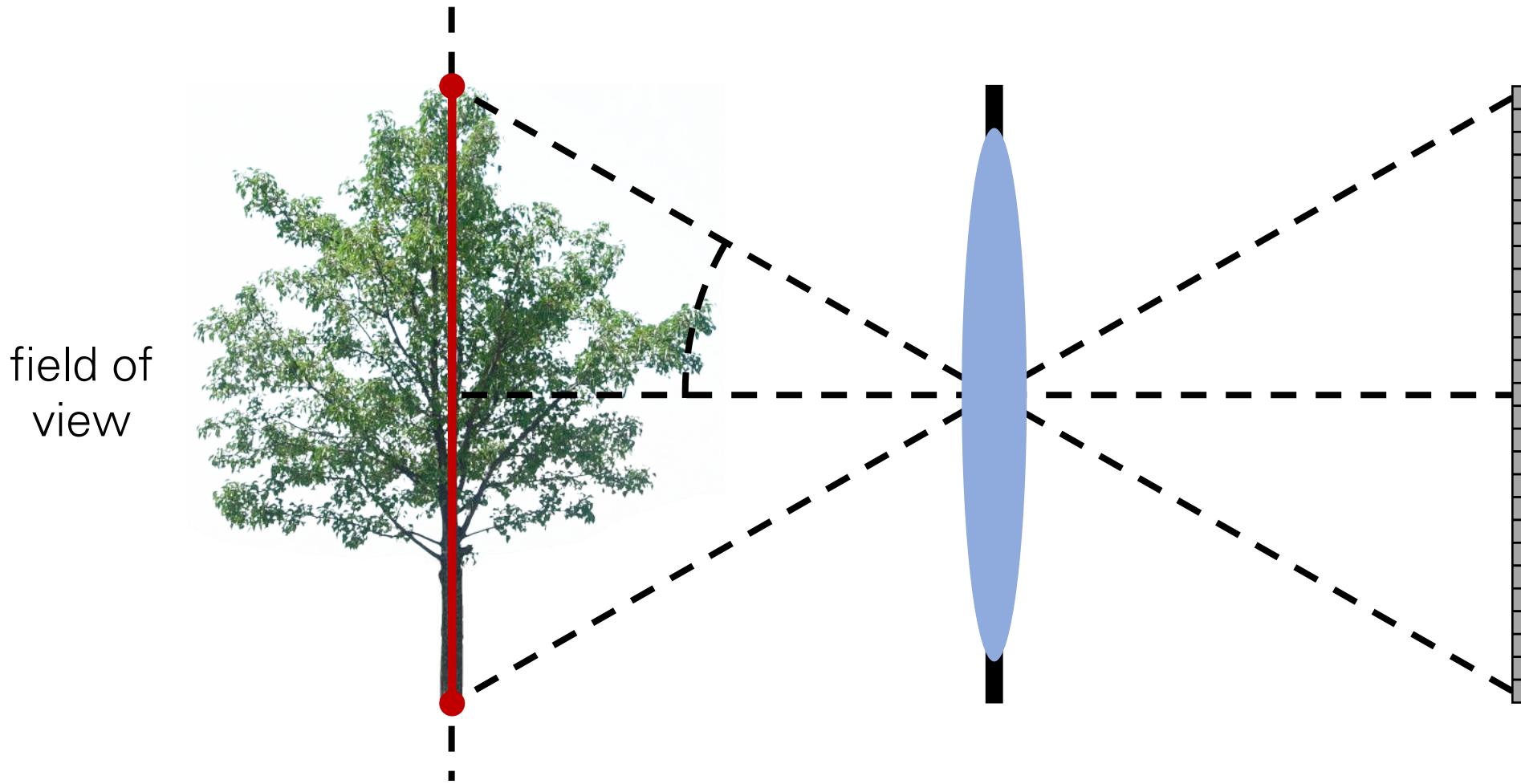
Size of field of view governed by size of the camera retina:

$$\varphi = \tan^{-1}\left(\frac{d}{2f}\right)$$

Smaller field of view = larger focal length

Field of view

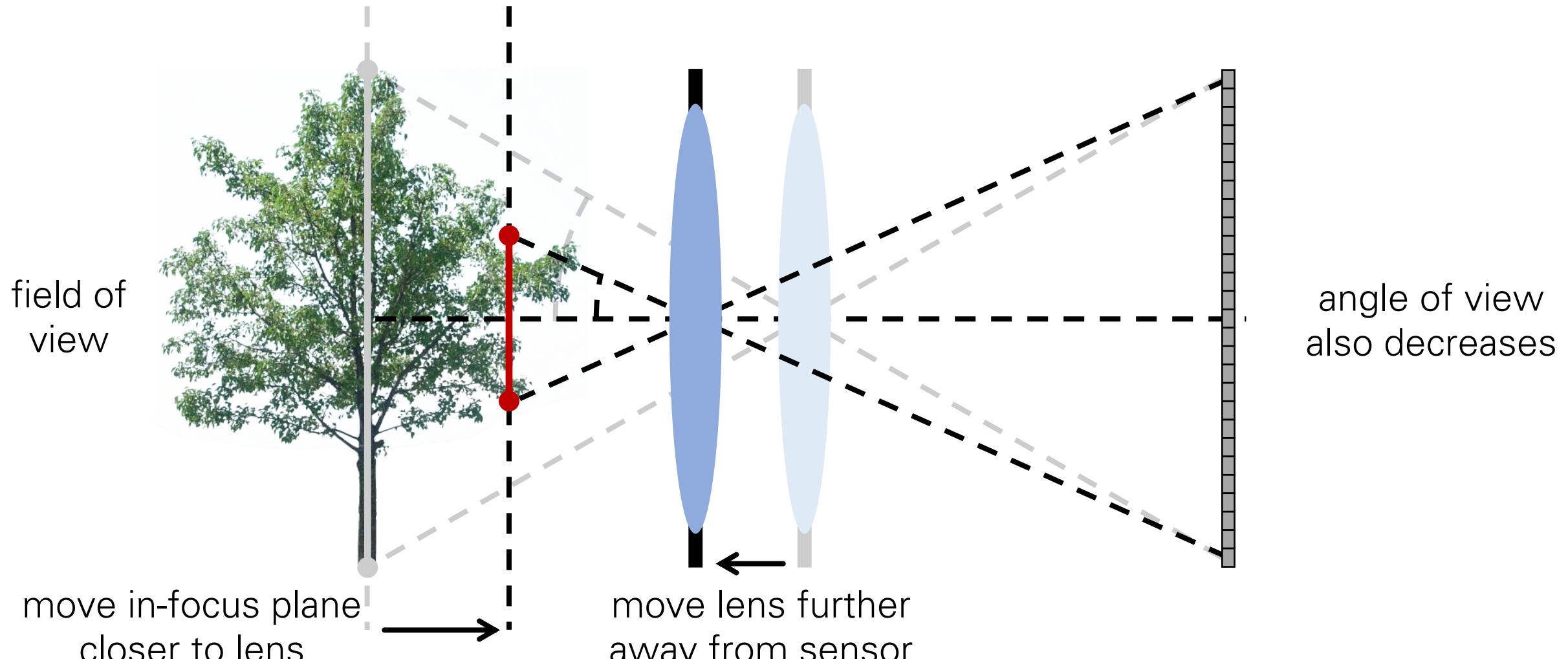
The part of the in-focus plane that gets mapped on the sensor.



- What happens to field of view as we focus closer?

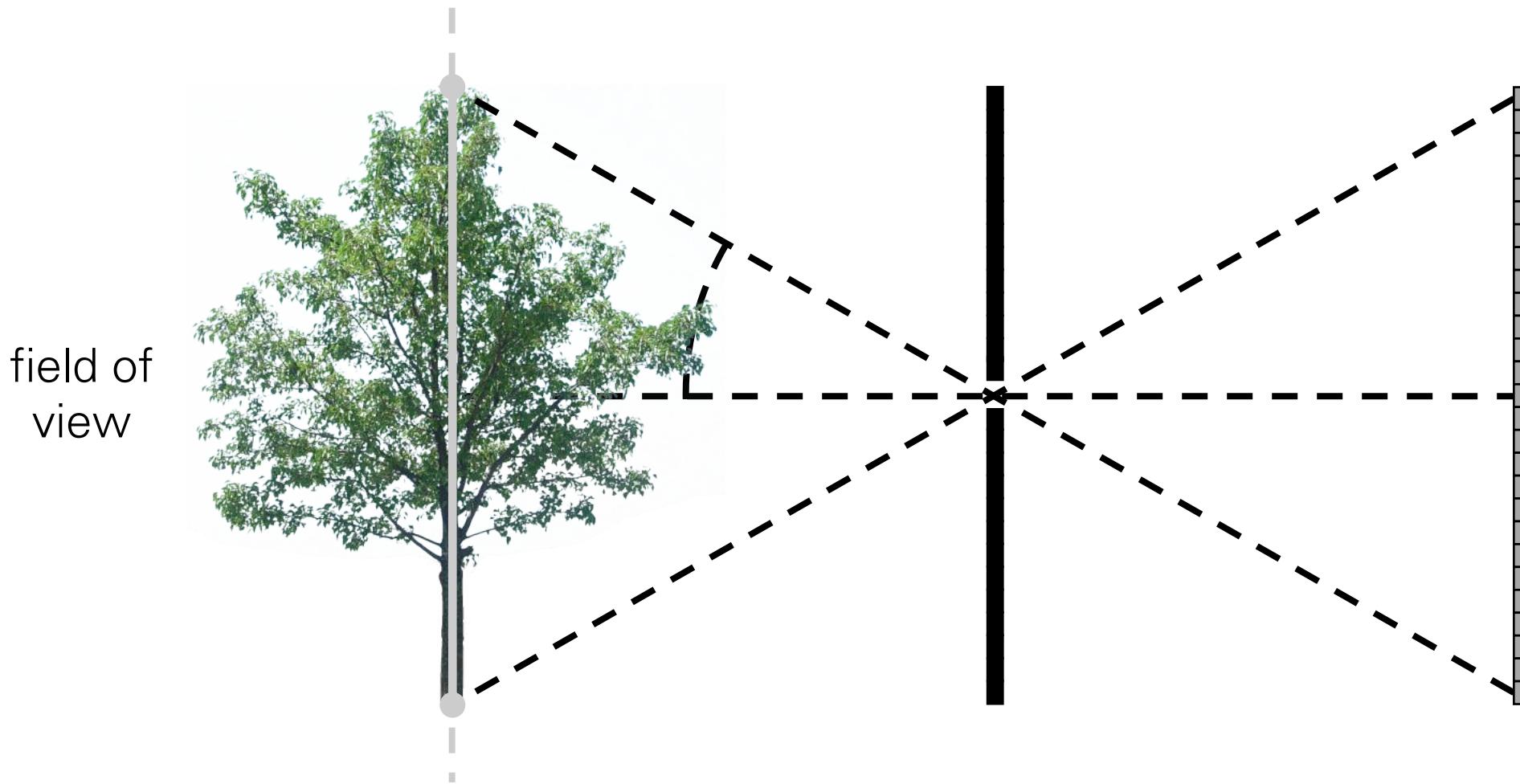
Field of view

The part of the in-focus plane that gets mapped on the sensor.



- What happens to field of view as we focus closer? → It becomes smaller.

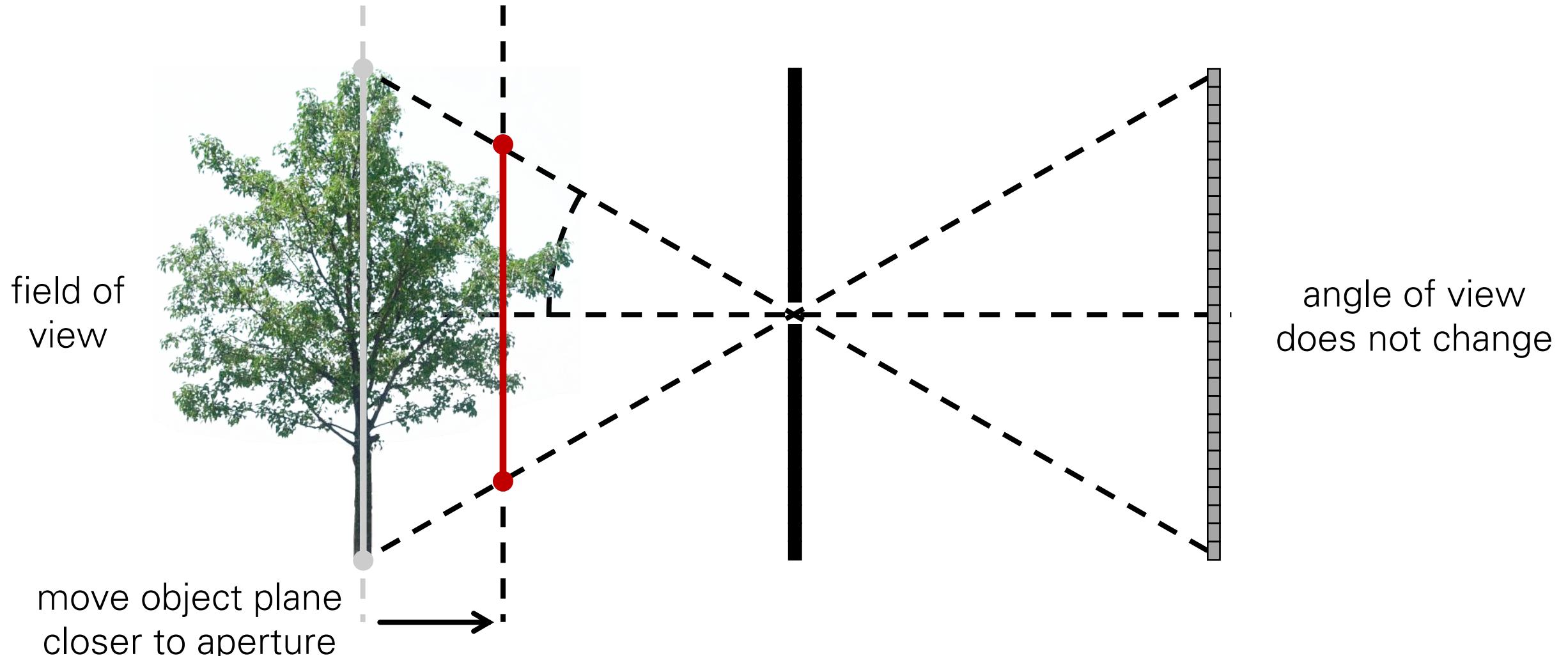
Comparison with pinhole camera



- What happens to field of view as we move closer?

Comparison with pinhole camera

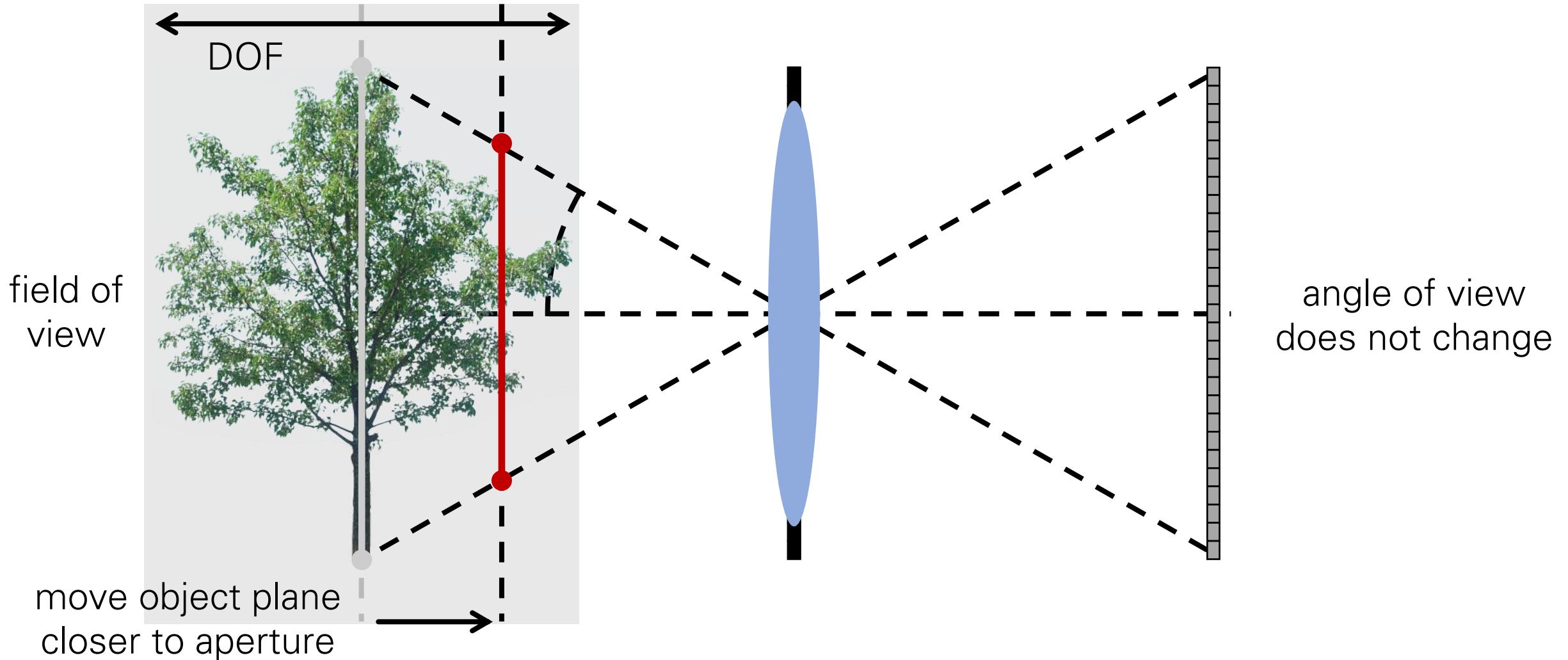
No need to refocus: we can move object closer without changing aperture-sensor distance.



- What happens to field of view as we move closer? → It becomes smaller, but amount differs.

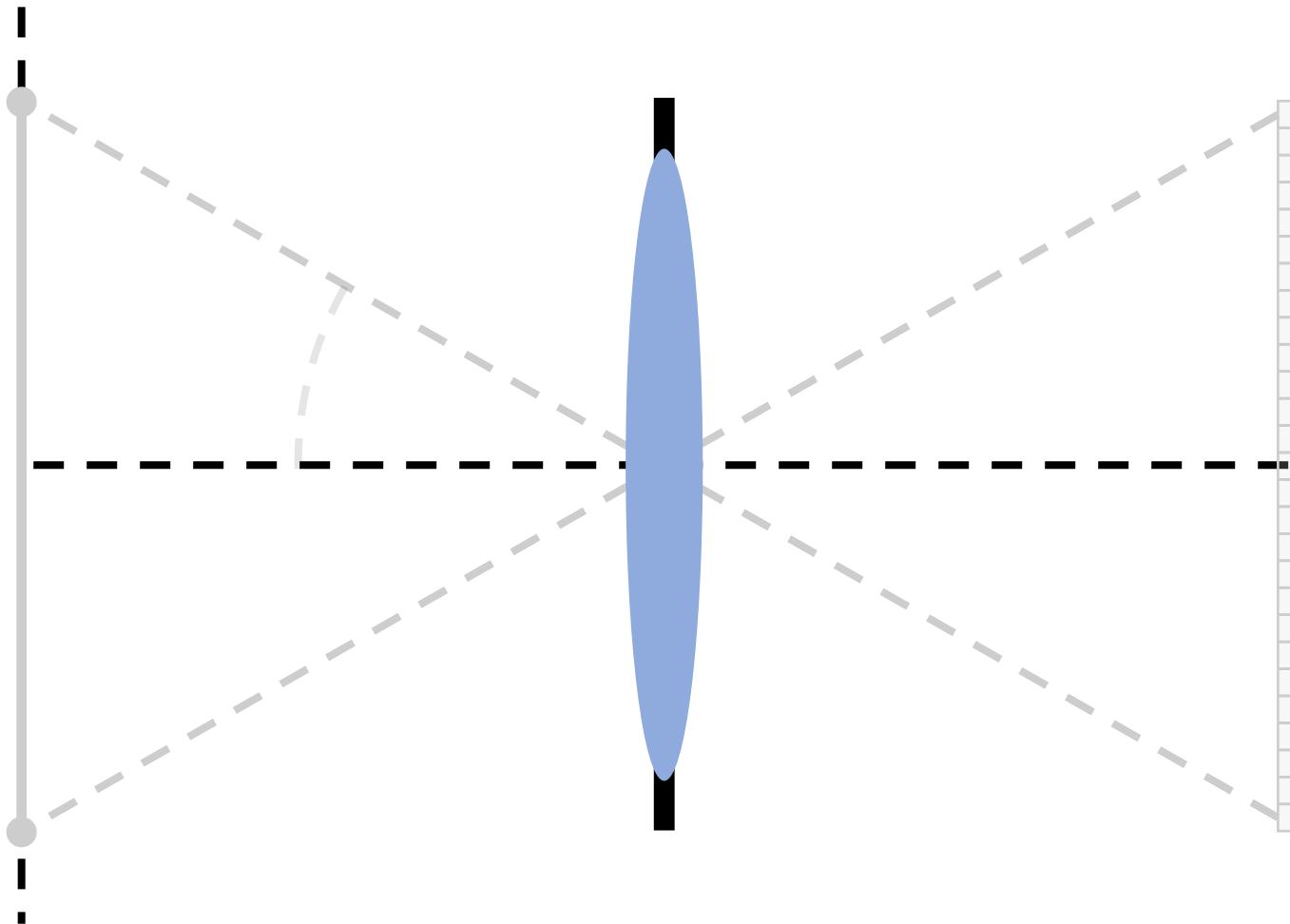
Comparison with pinhole camera

No need to refocus: we can move object closer without changing aperture-sensor distance.



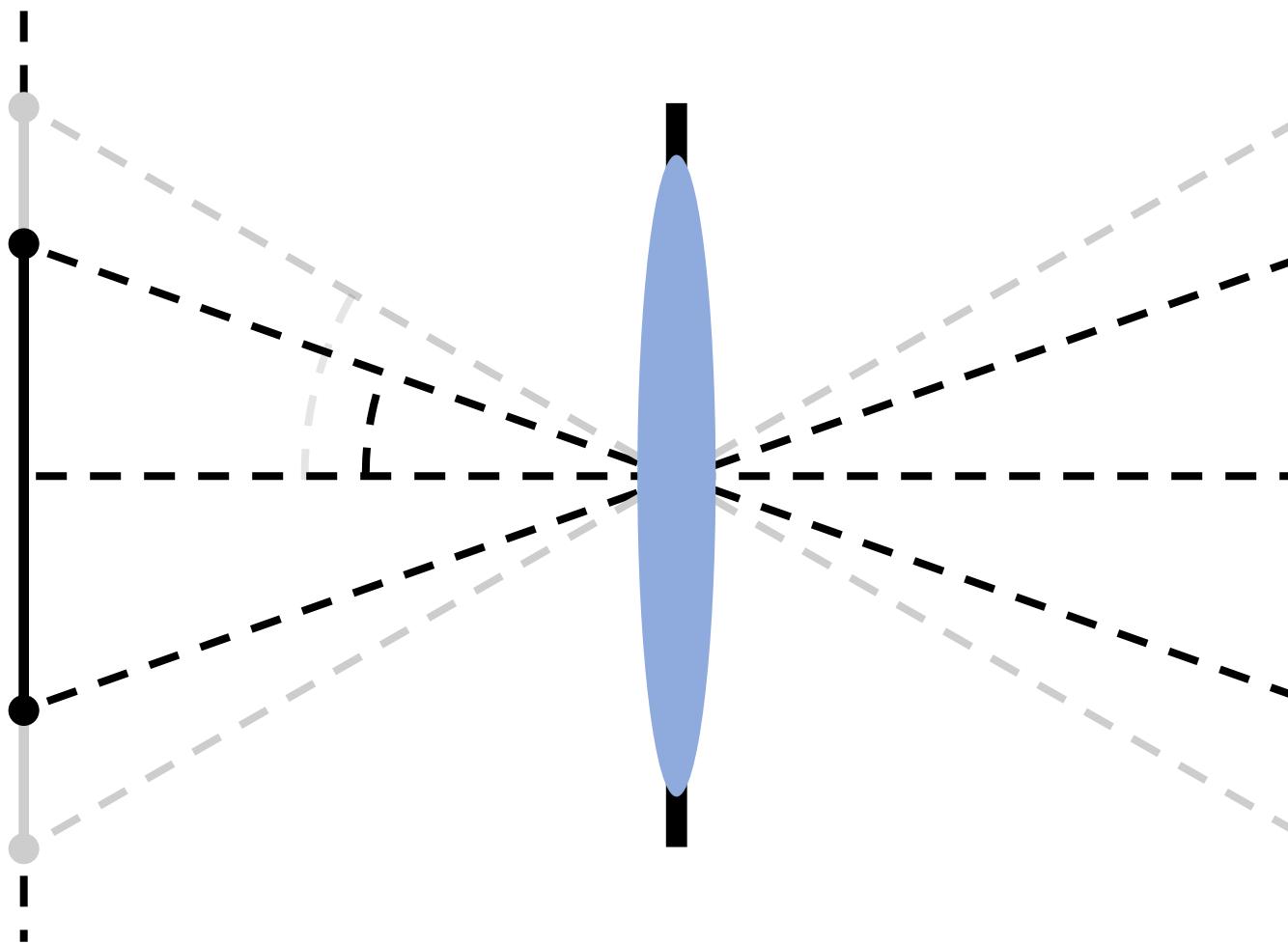
This can be done with a lens only if depth of field is large enough. Then the two behave the same.

Field of view also depends on sensor size



- What happens to field of view when we reduce sensor size?

Field of view also depends on sensor size



Lens and pinhole cameras behave the same in this case.

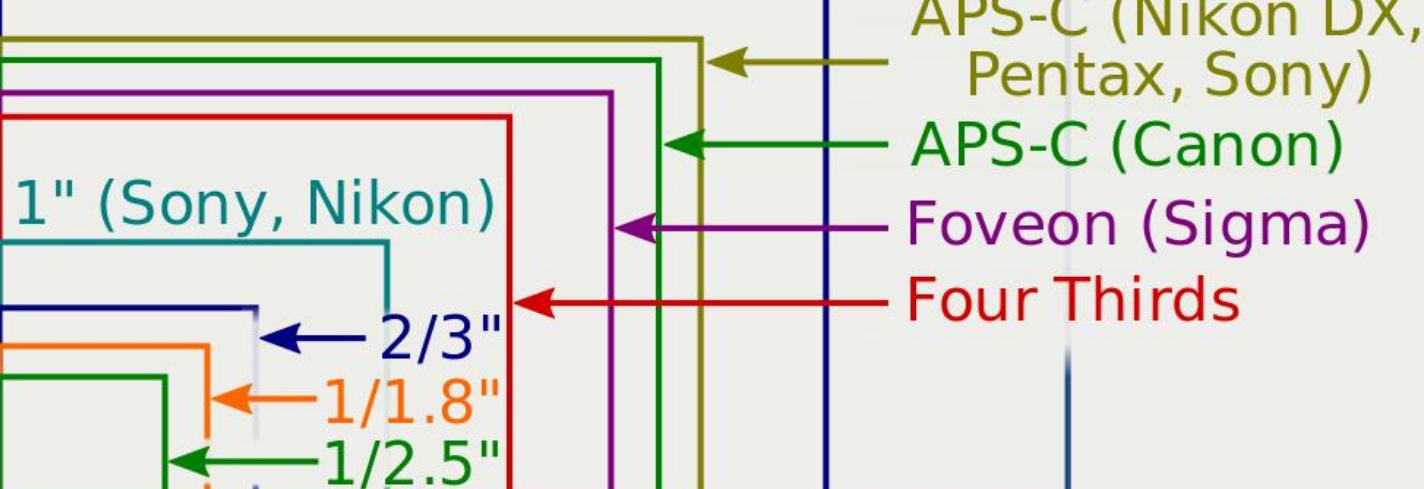
- What happens to field of view when we reduce sensor size? → It decreases.

Field of view also depends on sensor size

Medium format (Kodak KAF 39000 sensor)

35 mm "full frame"

APS-H (Canon)



- "Full frame" corresponds to standard film size.
- Digital sensors come in smaller formats due to manufacturing limitations (now mostly overcome).
- Lenses are often described in terms of field of view on film instead of focal length.
- These descriptions are invalid when not using full-frame sensor.

Crop factor

Medium format (Kodak KAF 39000 sensor)

35 mm "full frame"

APS-H (Canon)

APS-C (Nikon DX,
Pentax, Sony)

APS-C (Canon)

Foveon (Sigma)

Four Thirds

1" (Sony, Nikon)

2/3"

1/1.8"

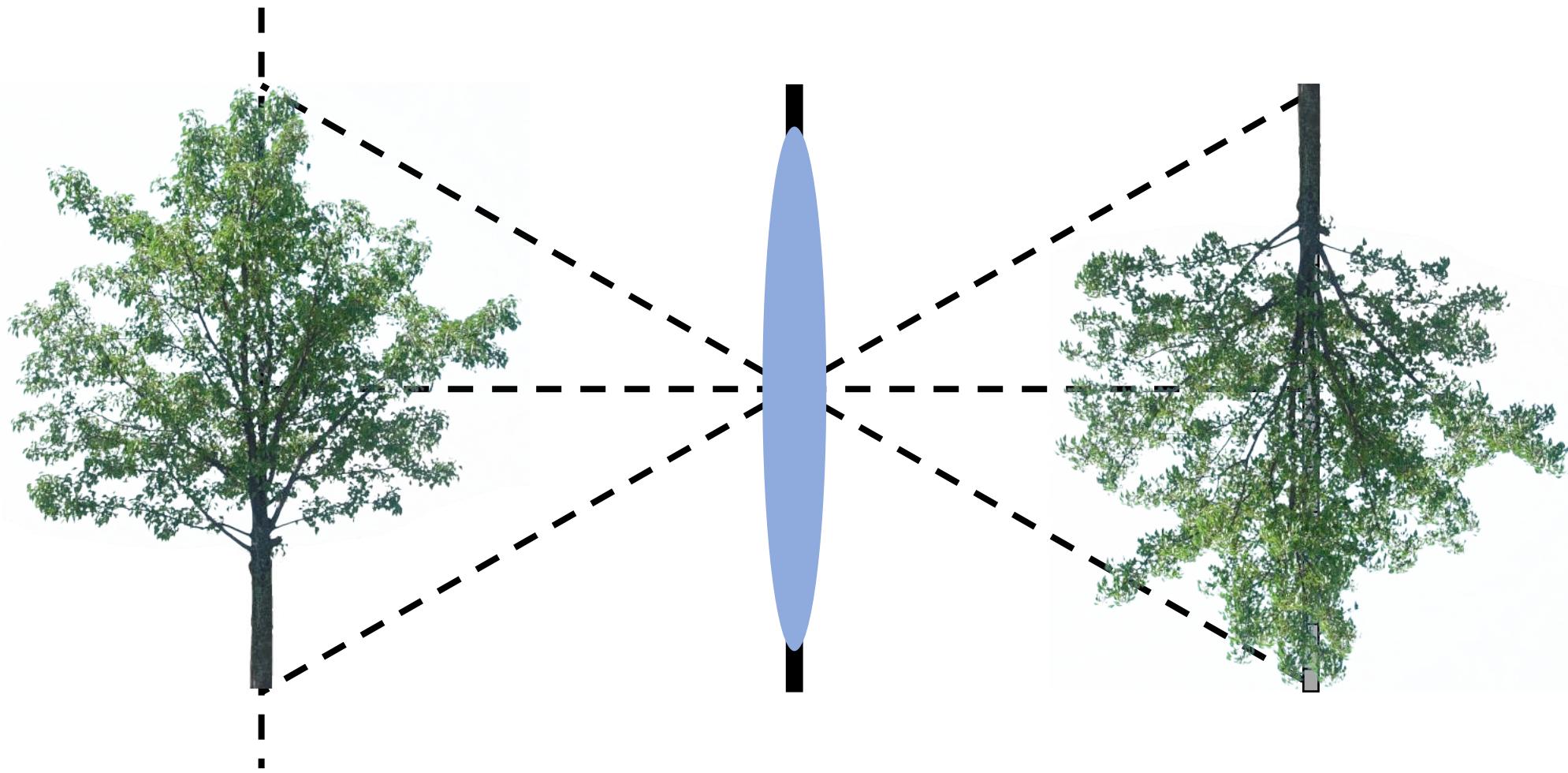
1/2.5"



How much field of view is cropped when using a sensor smaller than full frame.

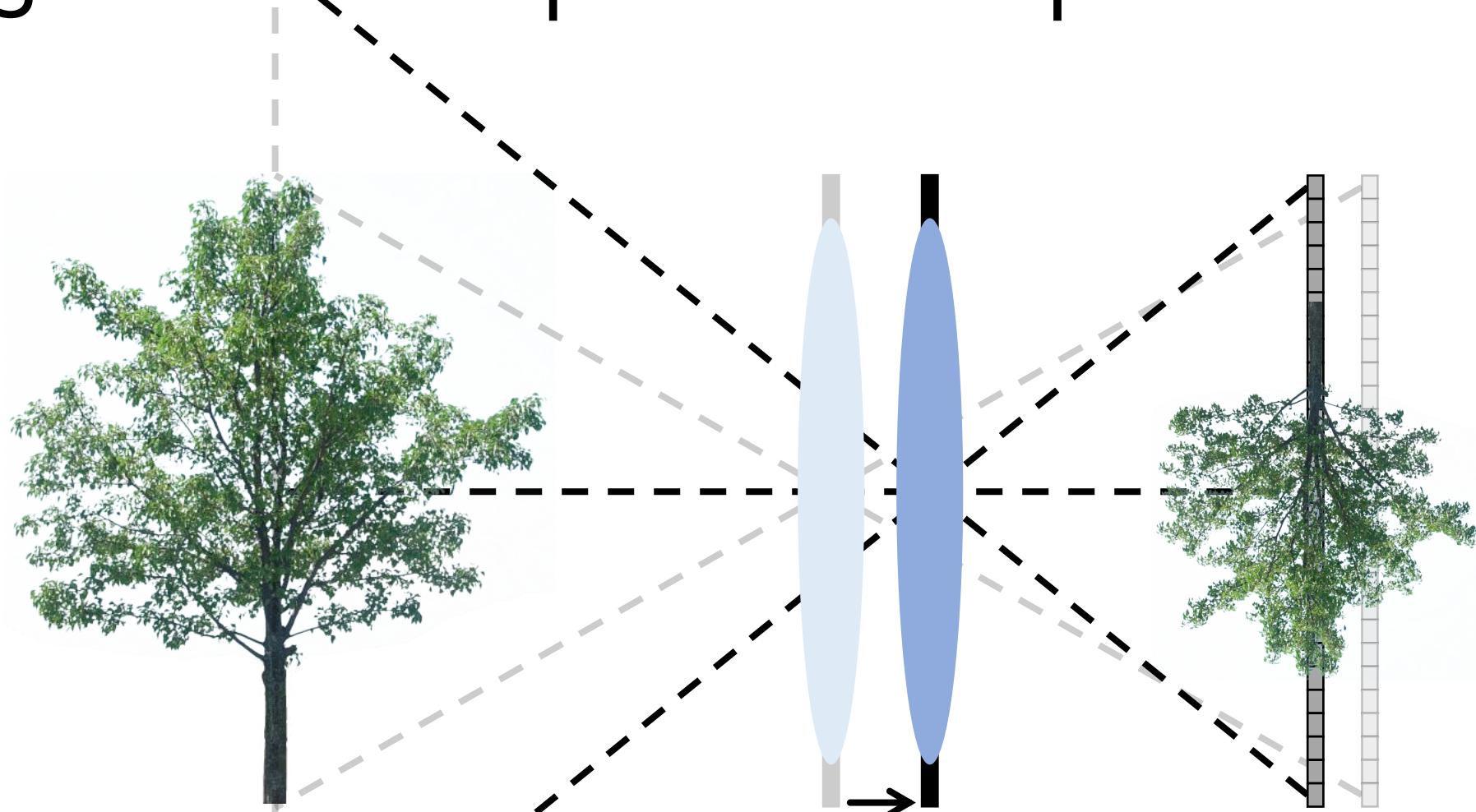
Magnification and perspective

Magnification depends on depth



- What happens to magnification as we focus further away?

Magnification depends on depth



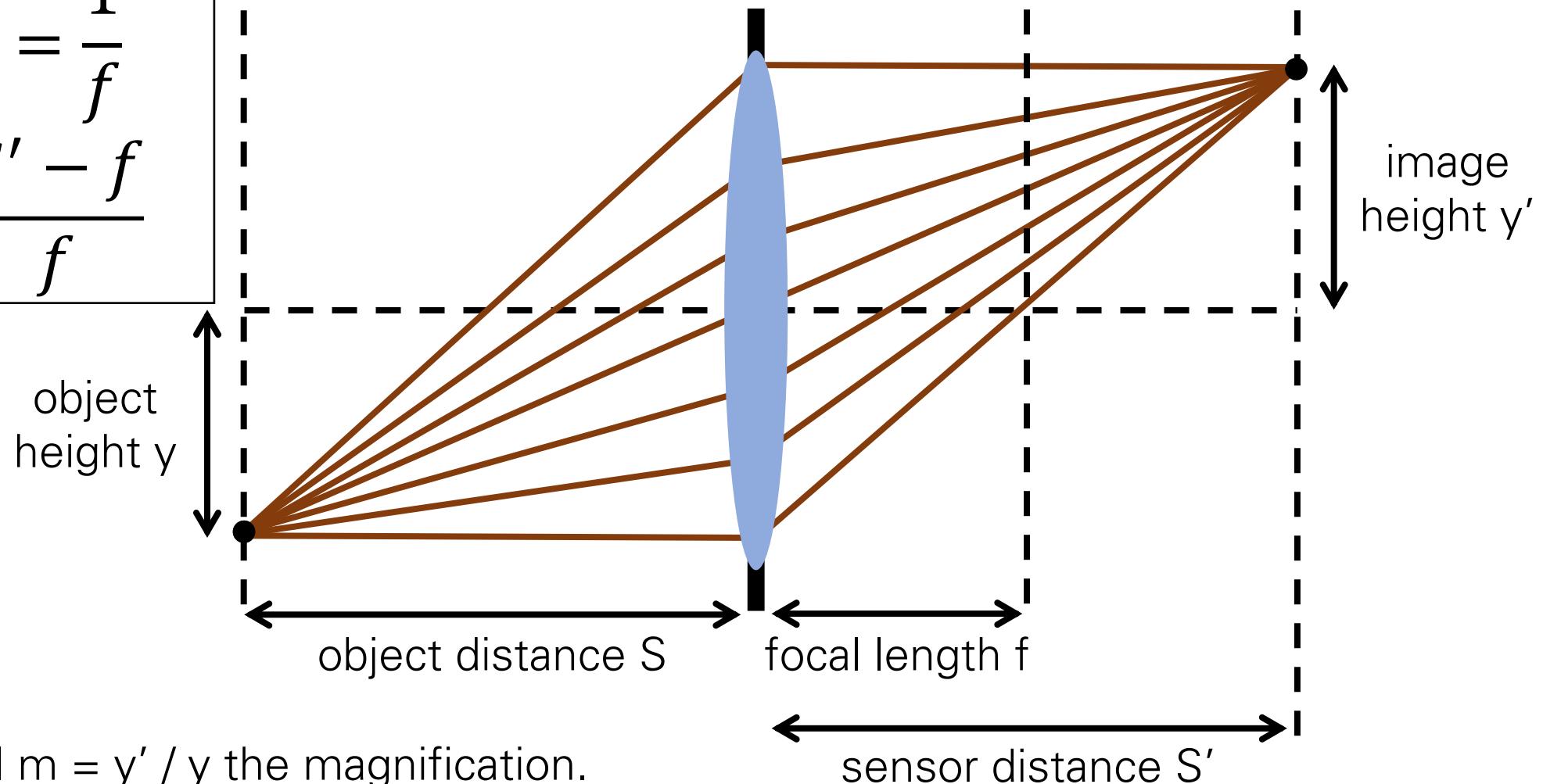
move object further
away from lens

move lens closer
to sensor

- What happens to magnification as we focus further? → It becomes smaller.

Magnification depends on depth

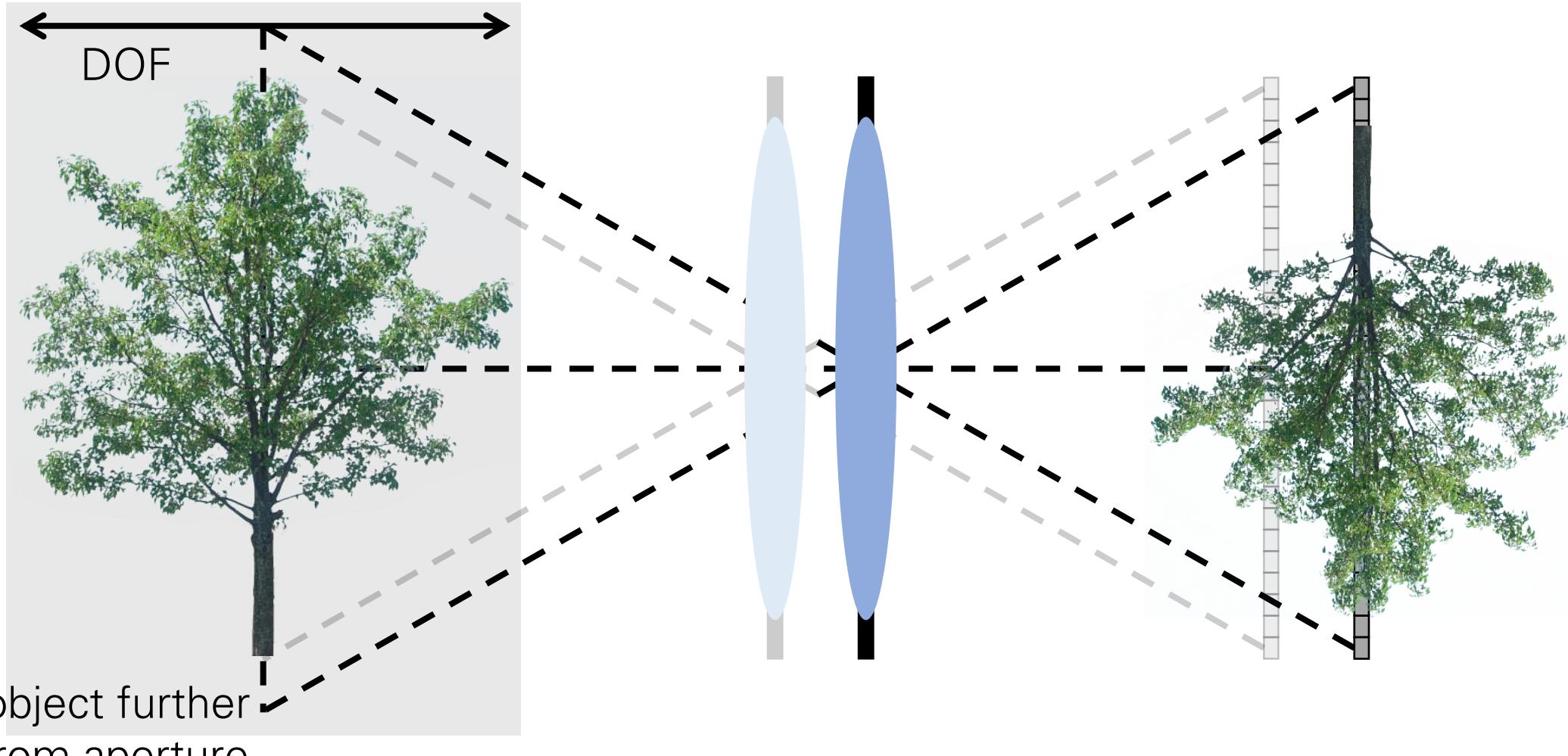
$$\frac{1}{S'} + \frac{1}{S} = \frac{1}{f}$$
$$m = \frac{S' - f}{f}$$



- We call $m = y' / y$ the magnification.

Comparison with pinhole camera

No need to refocus: we can move object further without changing aperture-sensor distance.



This can be done with a lens only if depth of field is large enough. Then the two behave the same.

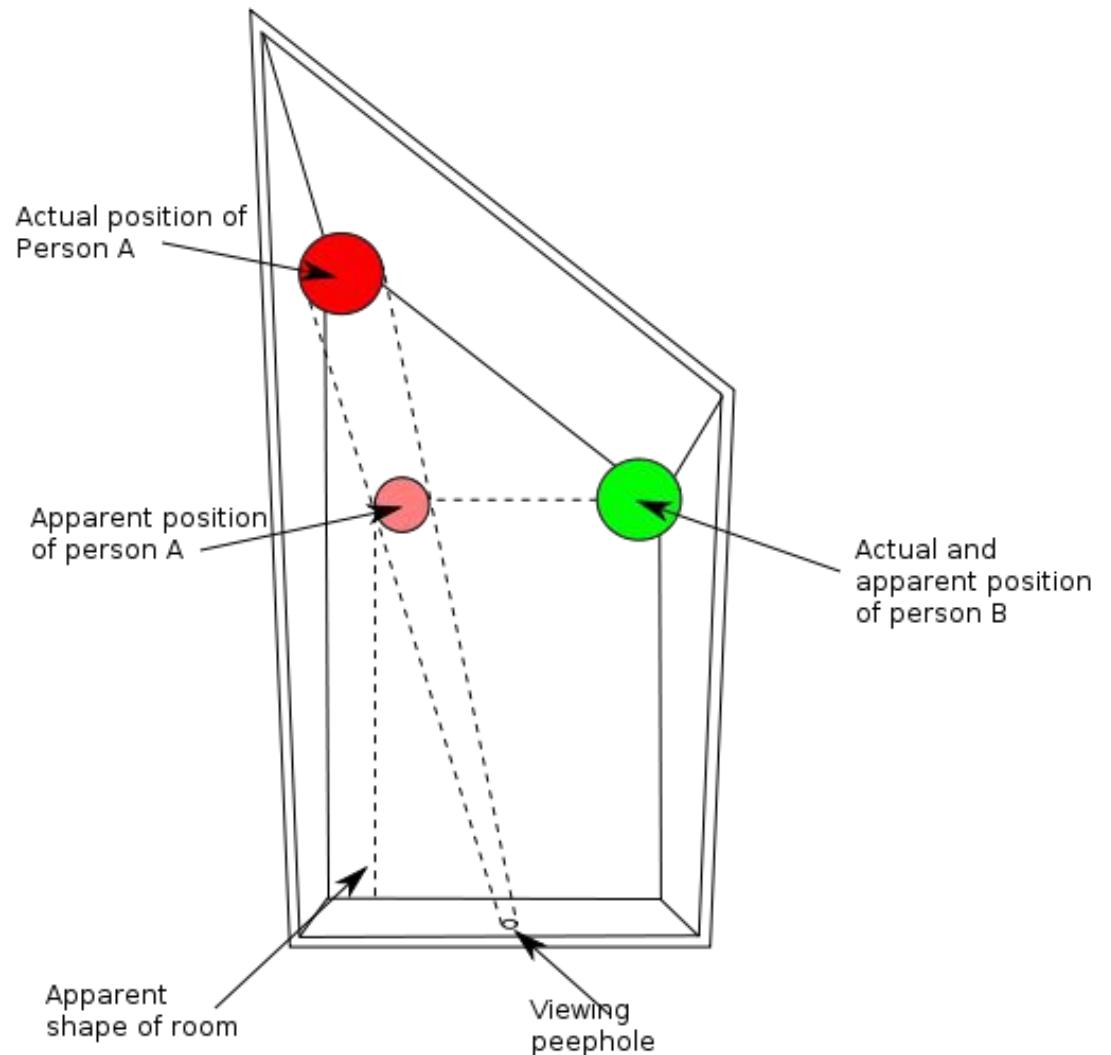
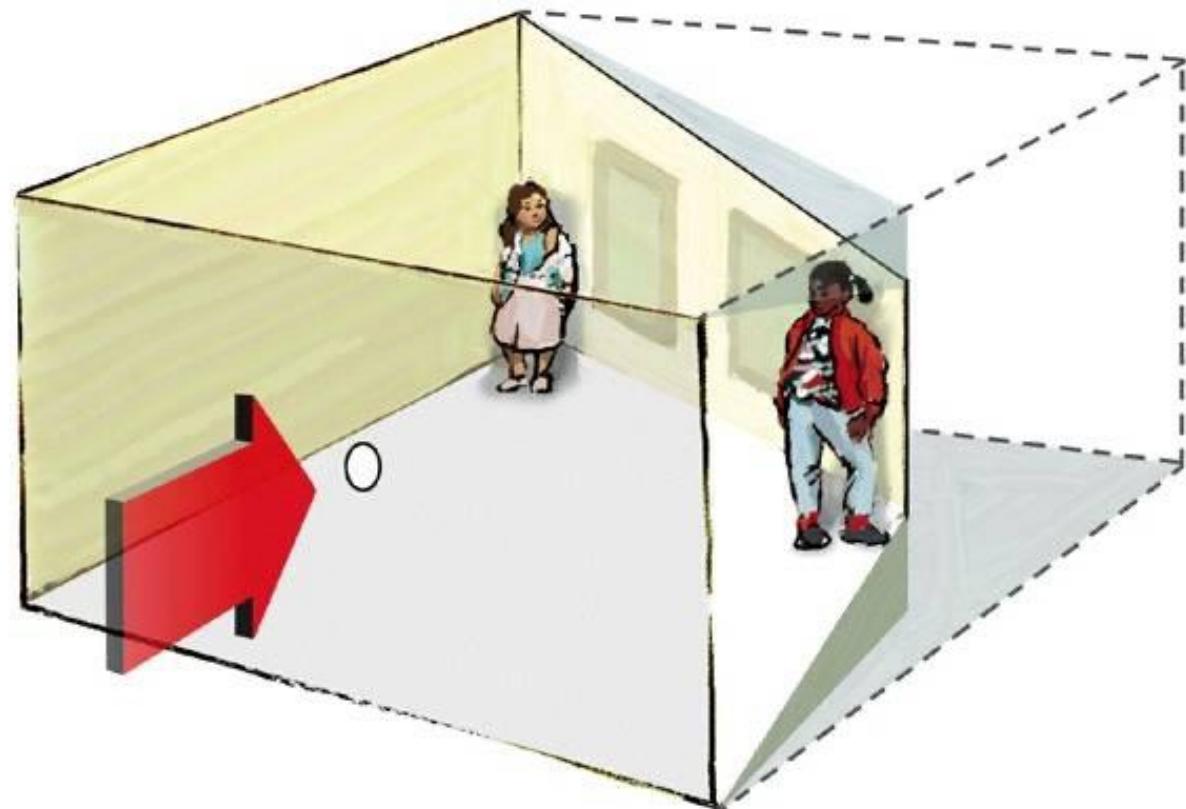
Forced perspective



The Ames room illusion



The Ames room illusion



The arrow illusion

Prof. Kokichi Sugihara has many other amazing illusions involving perspective distortion, check them out on YouTube or on his website:

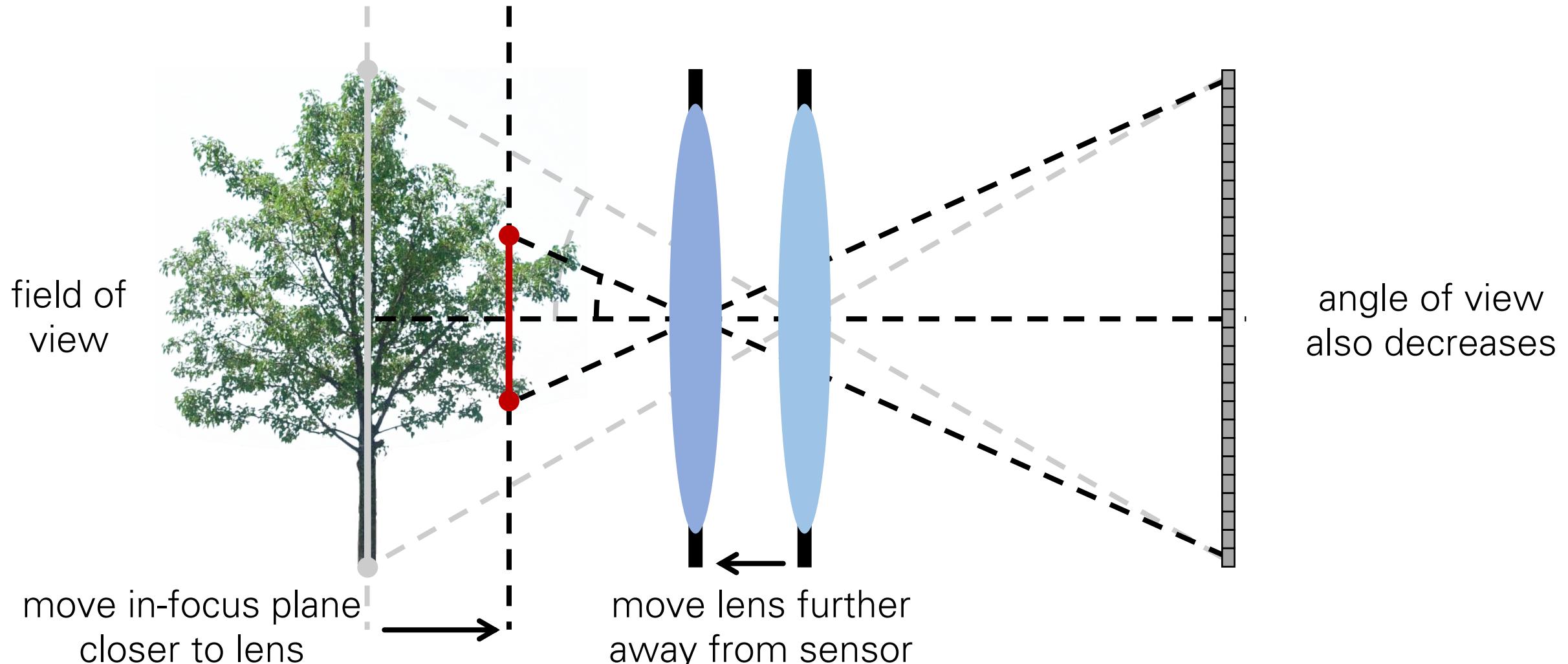
<http://www.isc.meiji.ac.jp/~kokichis/>



Zooming

Field of view

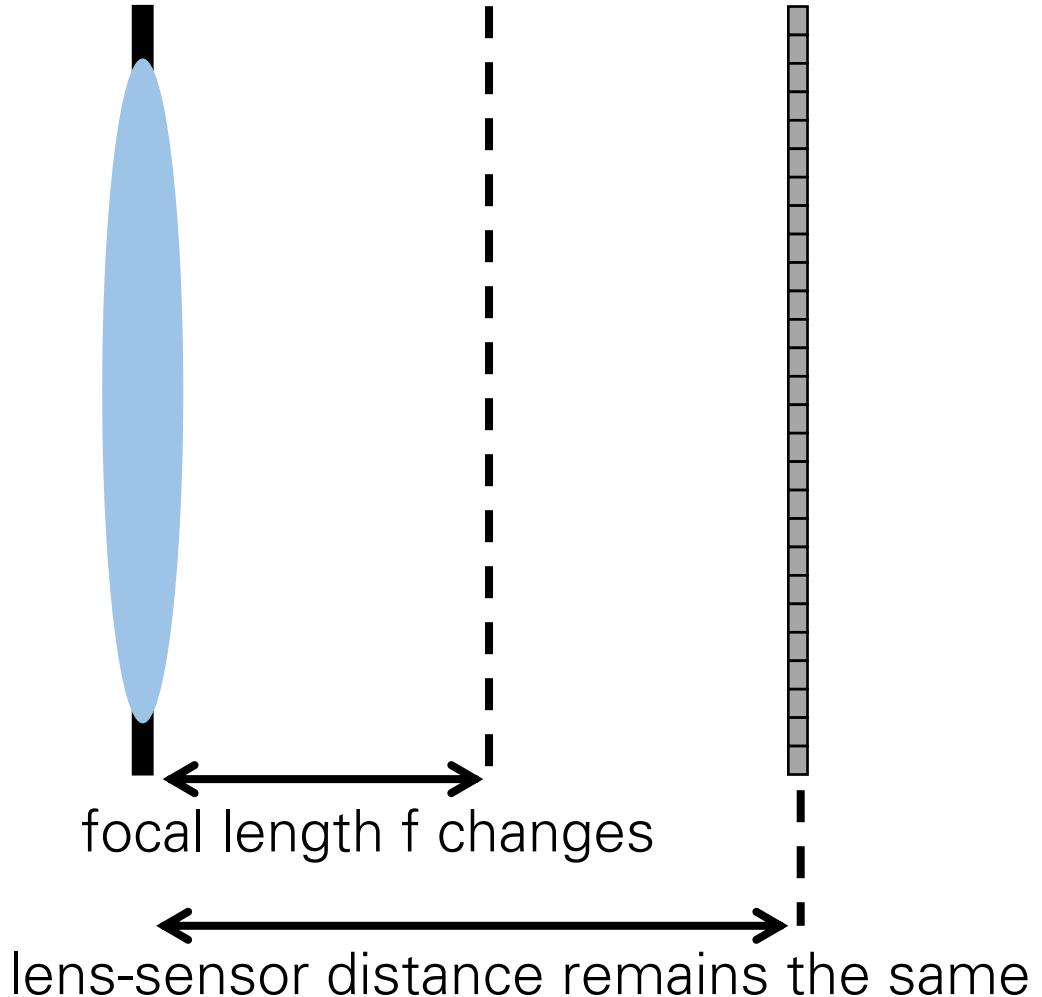
The part of the in-focus plane that gets mapped on the sensor.



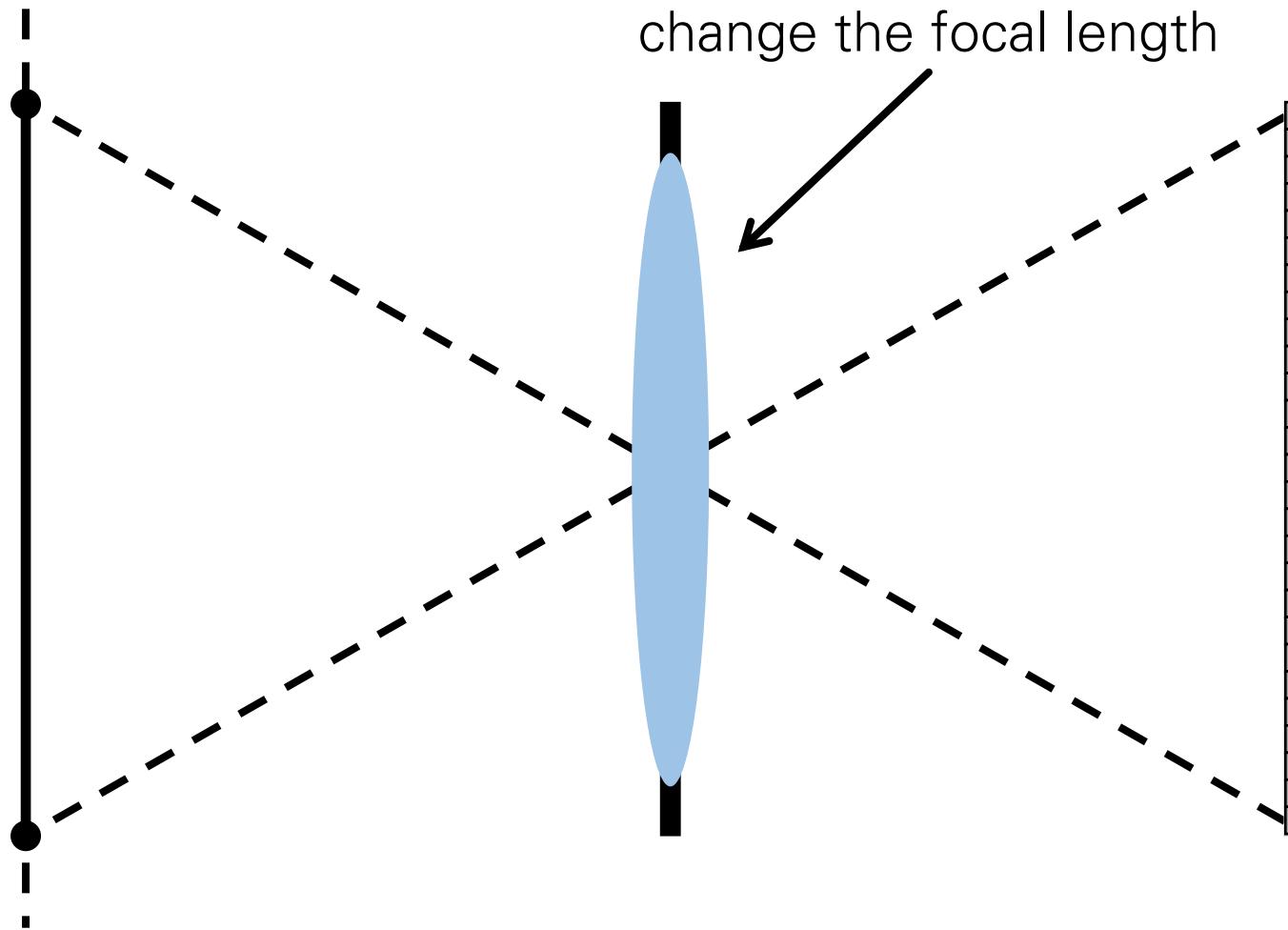
- What happens to field of view as we focus closer? → It becomes smaller.

Zooming means changing the focal length

Very different
process from
refocusing

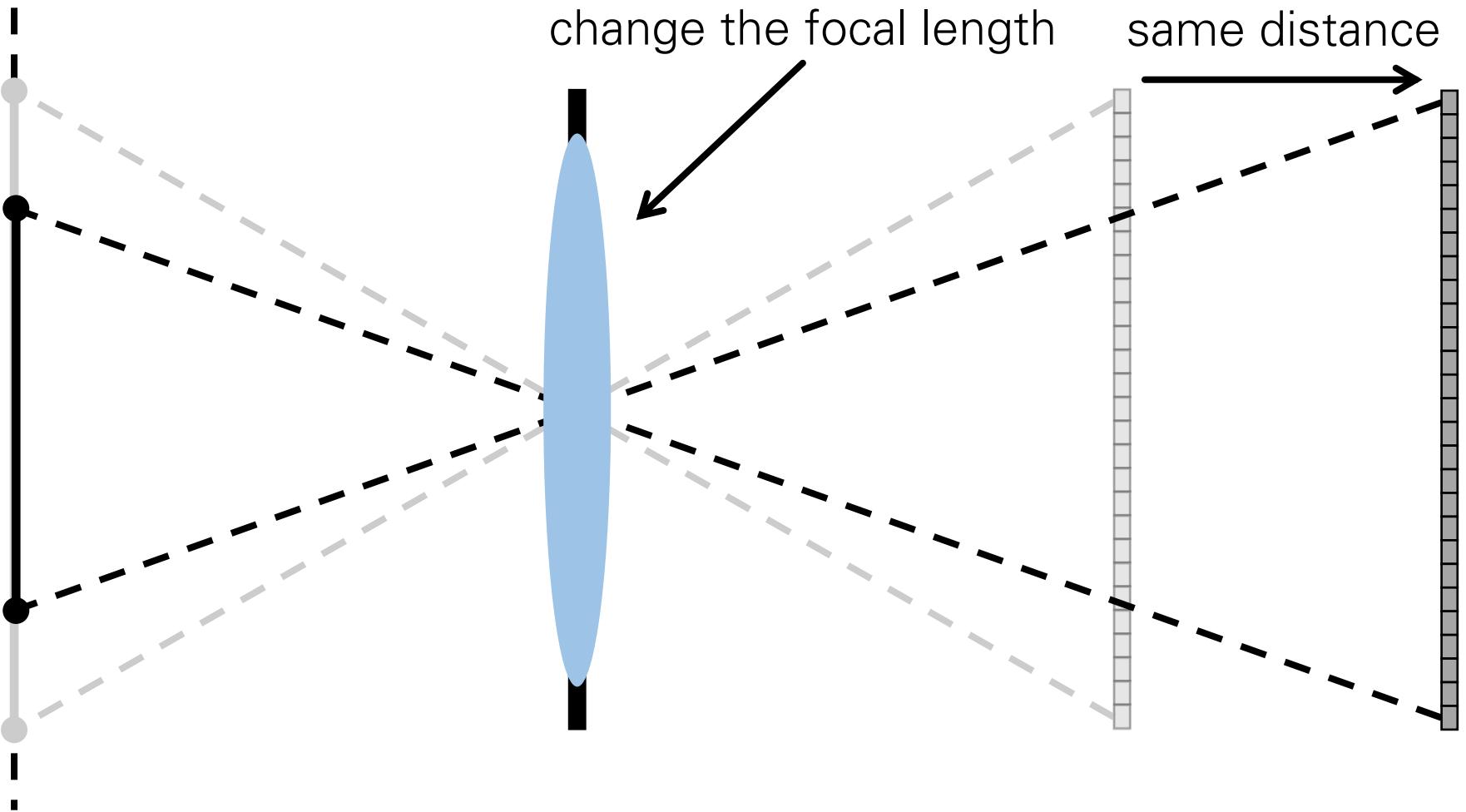


Zooming and field of view

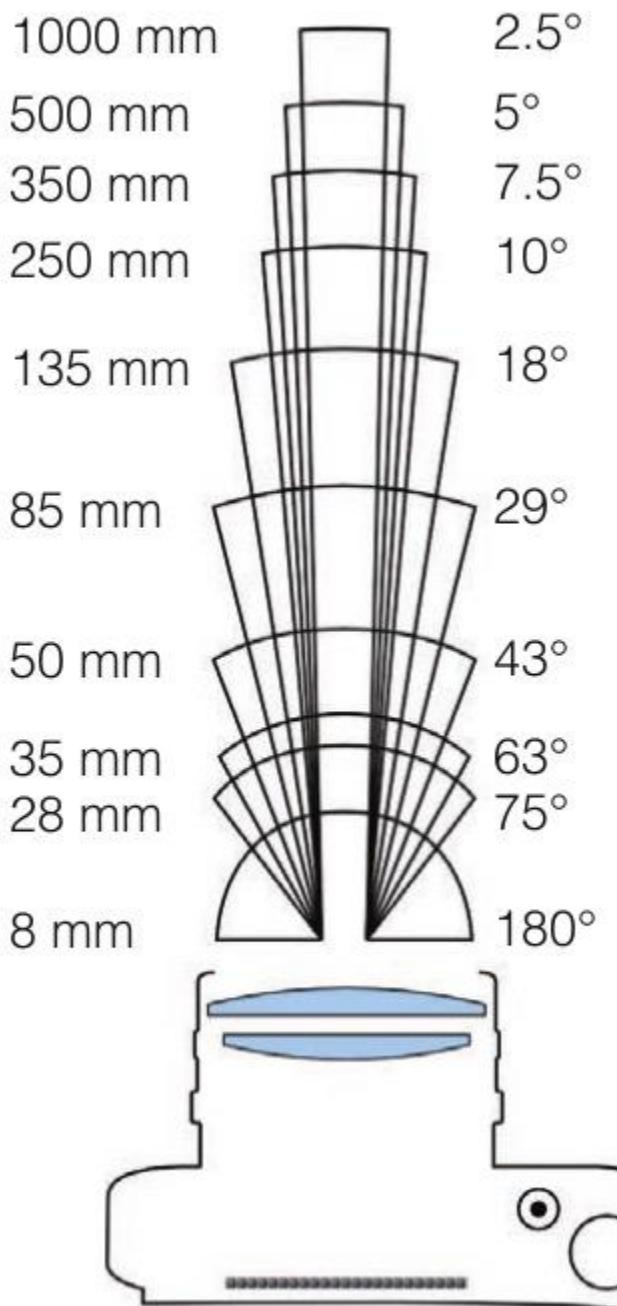


- What happens to field of view when we focus closer? → It decreases.
- What happens to field of view when we increase lens focal length?

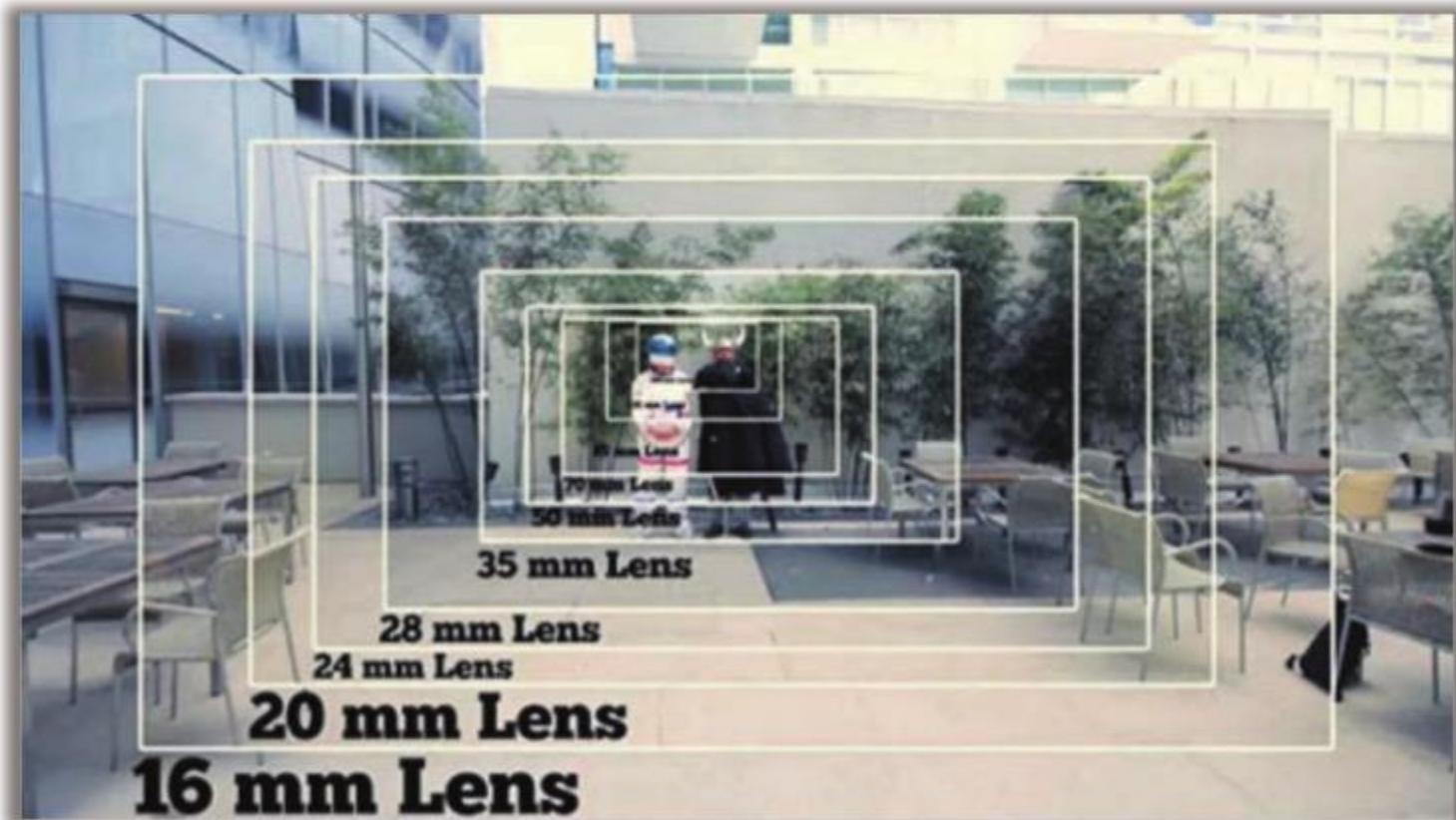
Zooming and field of view



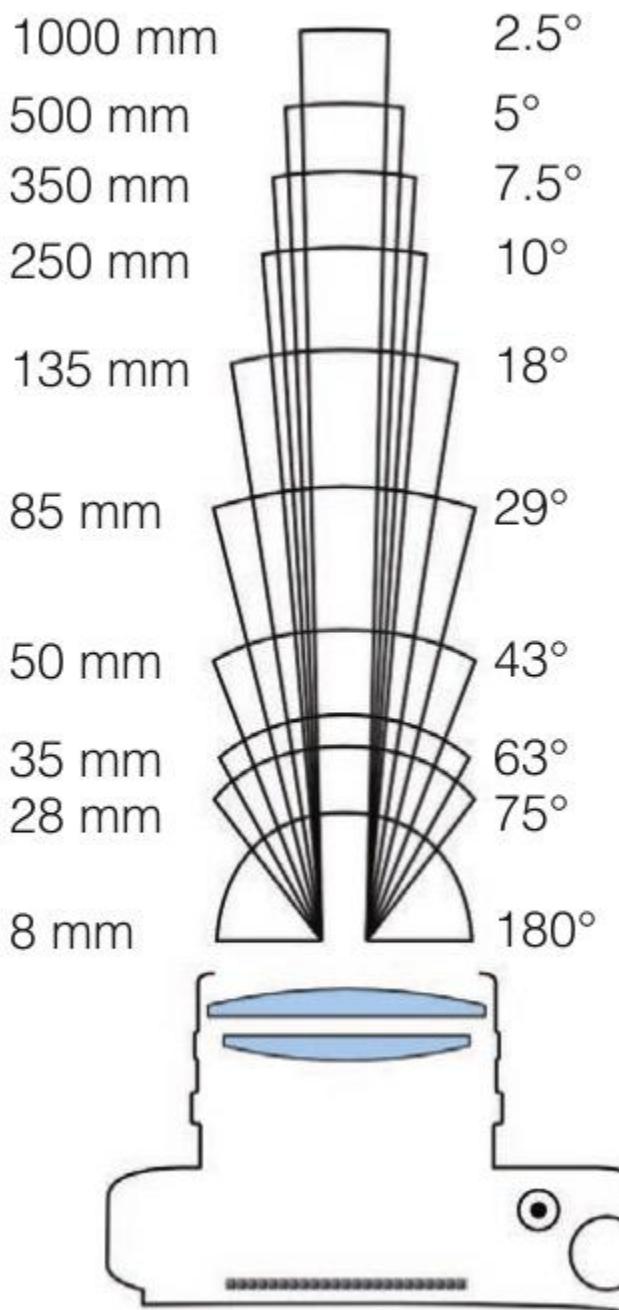
- When we increase lens focal length, field of view decreases (we “zoom in”).



Field of view

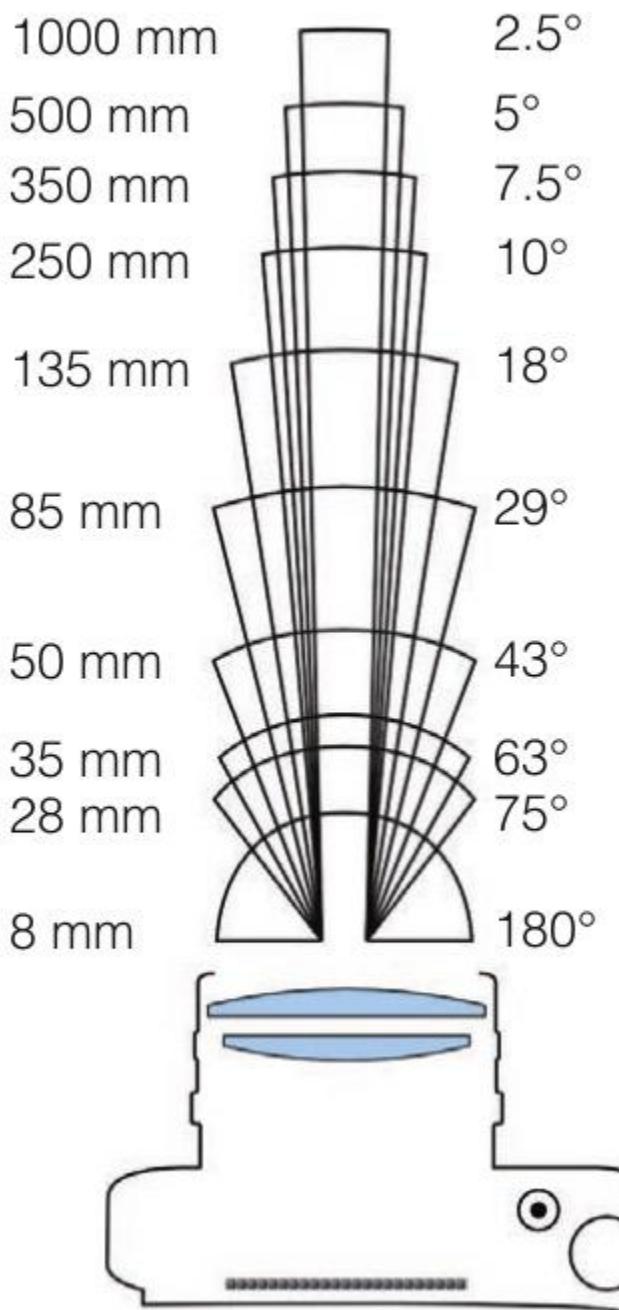


Andrew McWilliams



Field of view



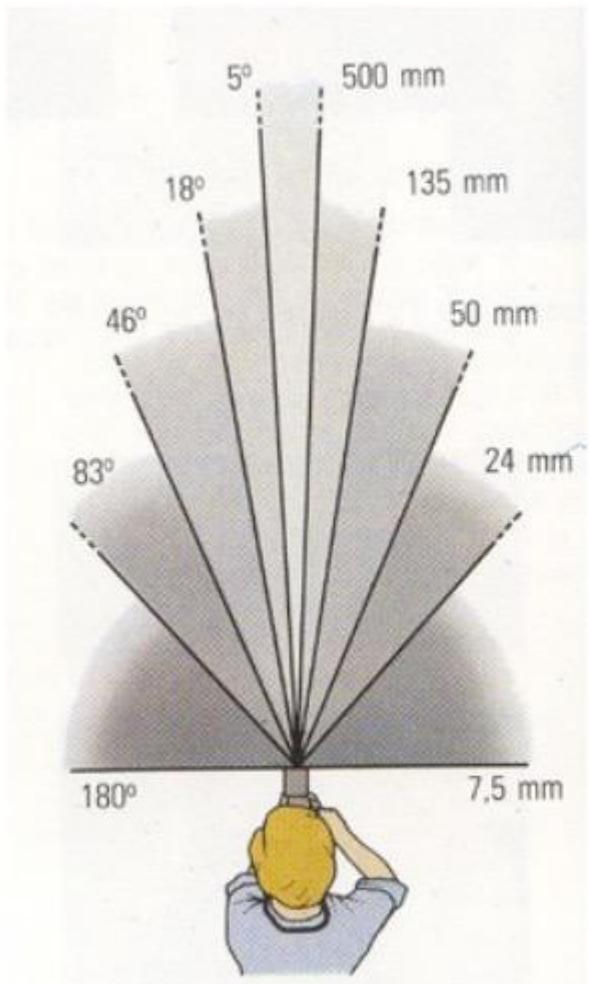


Field of view

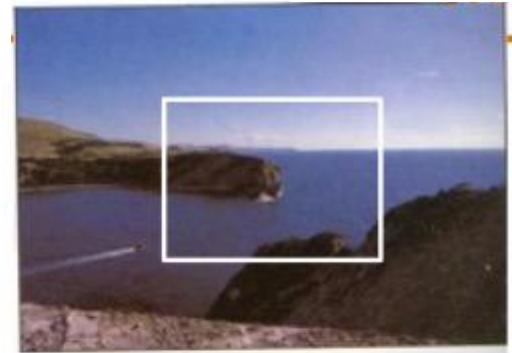


Field of view

Increasing the lens focal length is similar to cropping



$f = 25 \text{ mm}$



$f = 50 \text{ mm}$



$f = 135 \text{ mm}$



Is this effect identical to cropping?

The lens on your camera

Focus ring: controls distance of lens from sensor



Zoom ring: controls focal length of lens

Focusing versus zooming

When you turn the focus ring to bring lens further-away from the sensor:

1. The in-focus distance decreases (you need to get closer to object).
2. The field of view decreases (you see a smaller part of the object).
3. The magnification increases (same part of the object is bigger on sensor).

When you turn the zoom ring to decrease the focal length of the lens:

1. The in-focus distance increases (you need to move away from the object).
2. The field of view increases (you see a larger part of the object).
3. The magnification decreases (same part of the object is smaller on sensor).

Focusing versus zooming

When you turn the focus ring to bring lens further-away from the sensor:

1. The in-focus distance decreases (you need to get closer to object).
2. The field of view decreases (you see a smaller part of the object).
3. The magnification increases (same part of the object is bigger on sensor).

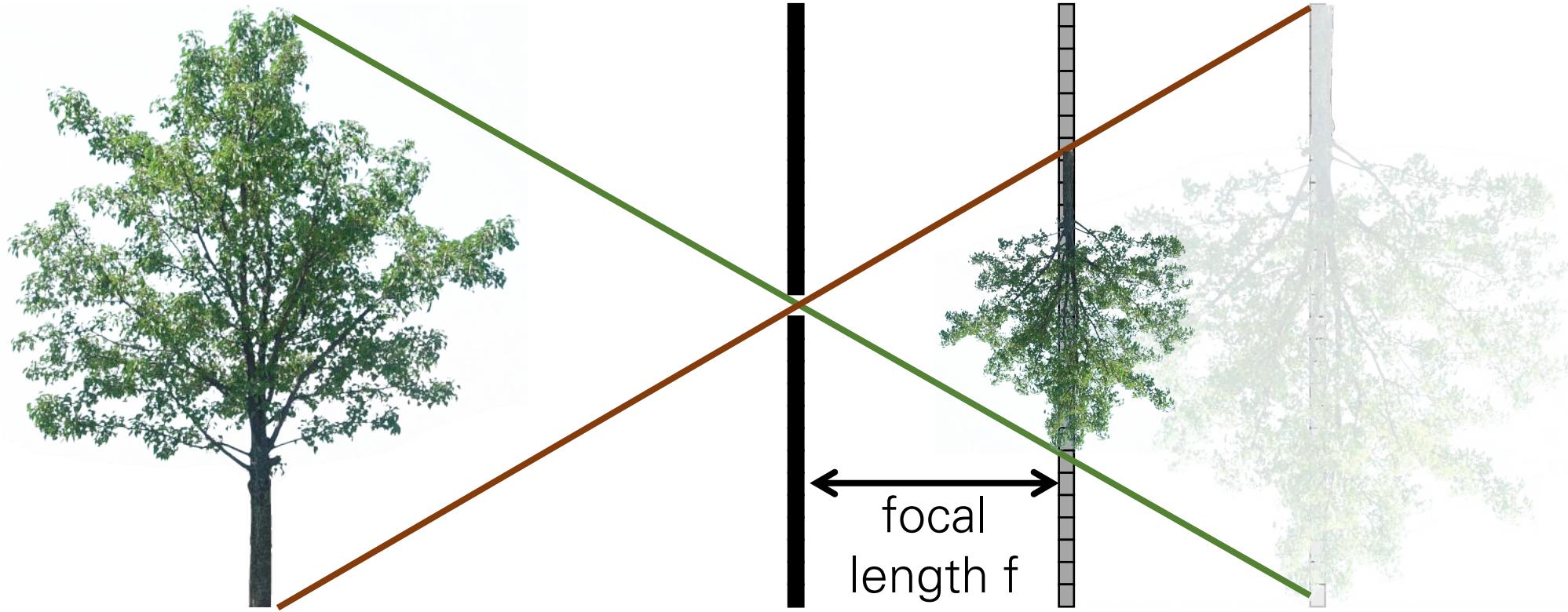
We can use both focus and zoom to cancel out their effects.

When you turn the zoom ring to decrease the focal length of the lens:

1. The in-focus distance increases (you need to move away from the object).
2. The field of view increases (you see a larger part of the object).
3. The magnification decreases (same part of the object is smaller on sensor).

What if...

real-world
object



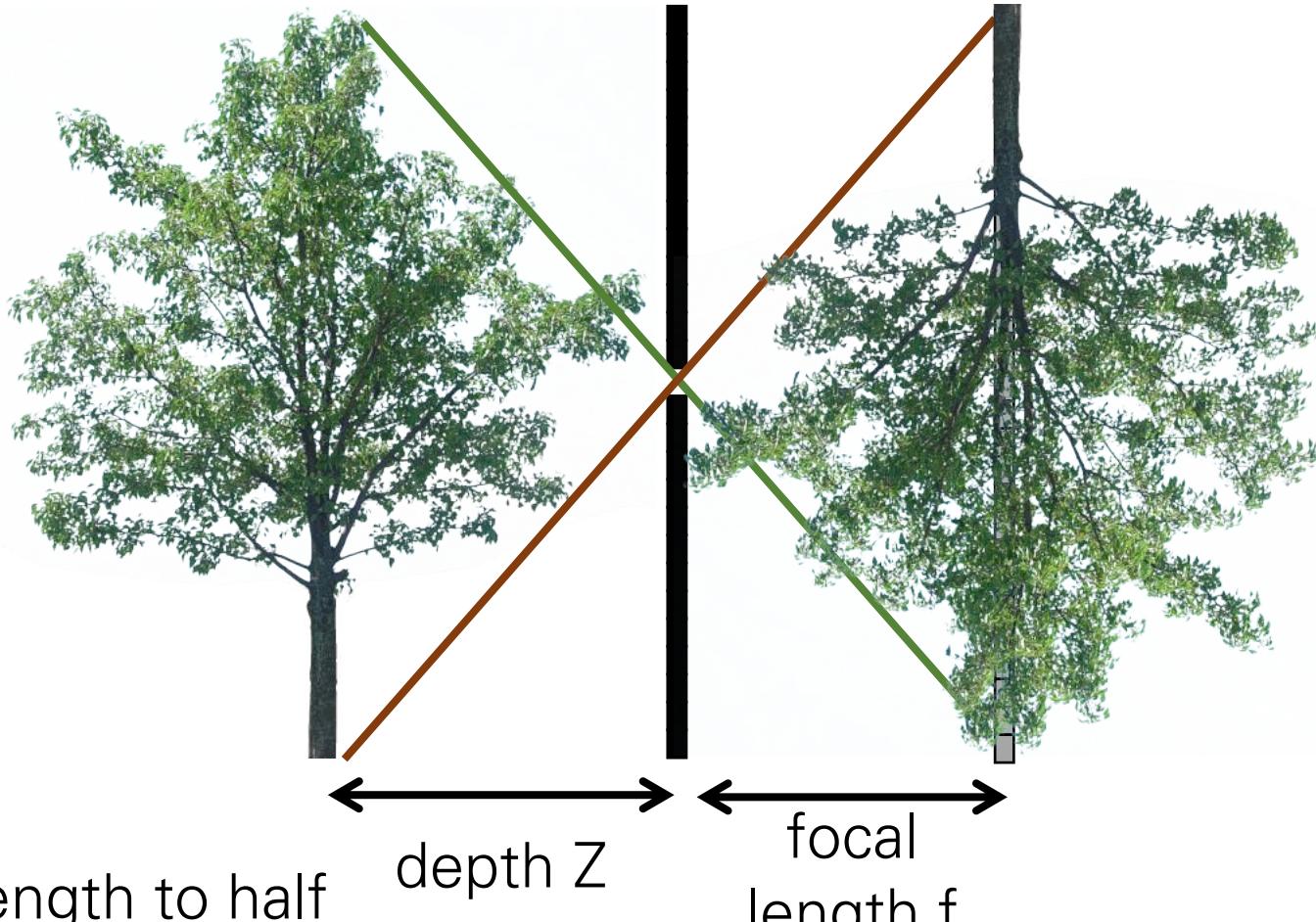
1. Set focal length to half

depth $2 Z$

focal length $2 f$

What if...

real-world
object



1. Set focal length to half
2. Set depth to half

Is this the same image
as the one we had at
focal length $2f$ and
distance $2Z$?

Similar construction can
be done with lenses,
after taking care of
refocusing.

Perspective distortion



long focal length

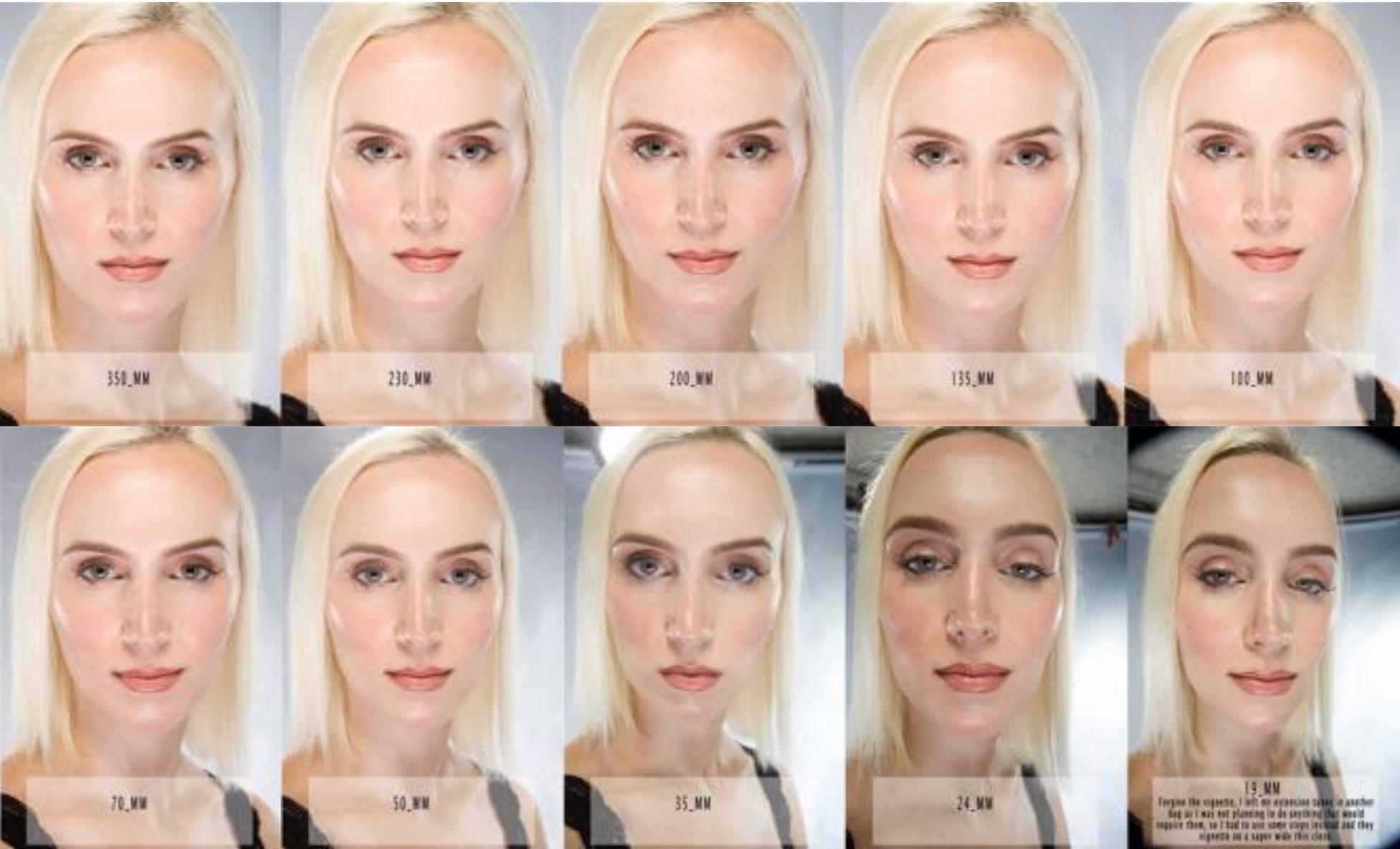


mid focal length



short focal length

Perspective distortion



What is the best focal length for portraits?

That's like asking which is better, vi or emacs...



long focal length



mid focal length



short focal length

Vertigo effect

Named after Alfred Hitchcock's movie

- also known as “dolly zoom”



Vertigo effect

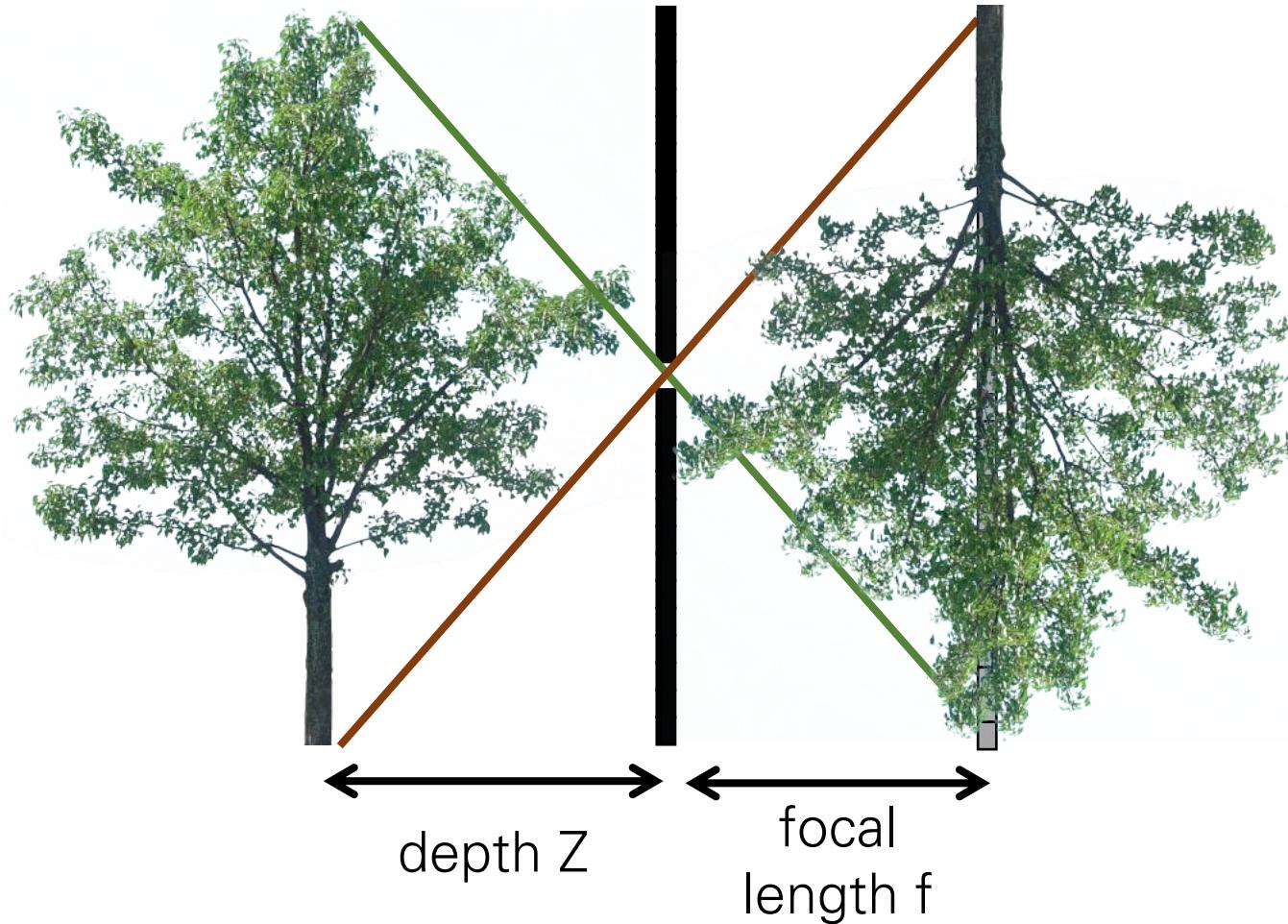


How would you
create this effect?

Orthographic camera and telecentric lenses

What if...

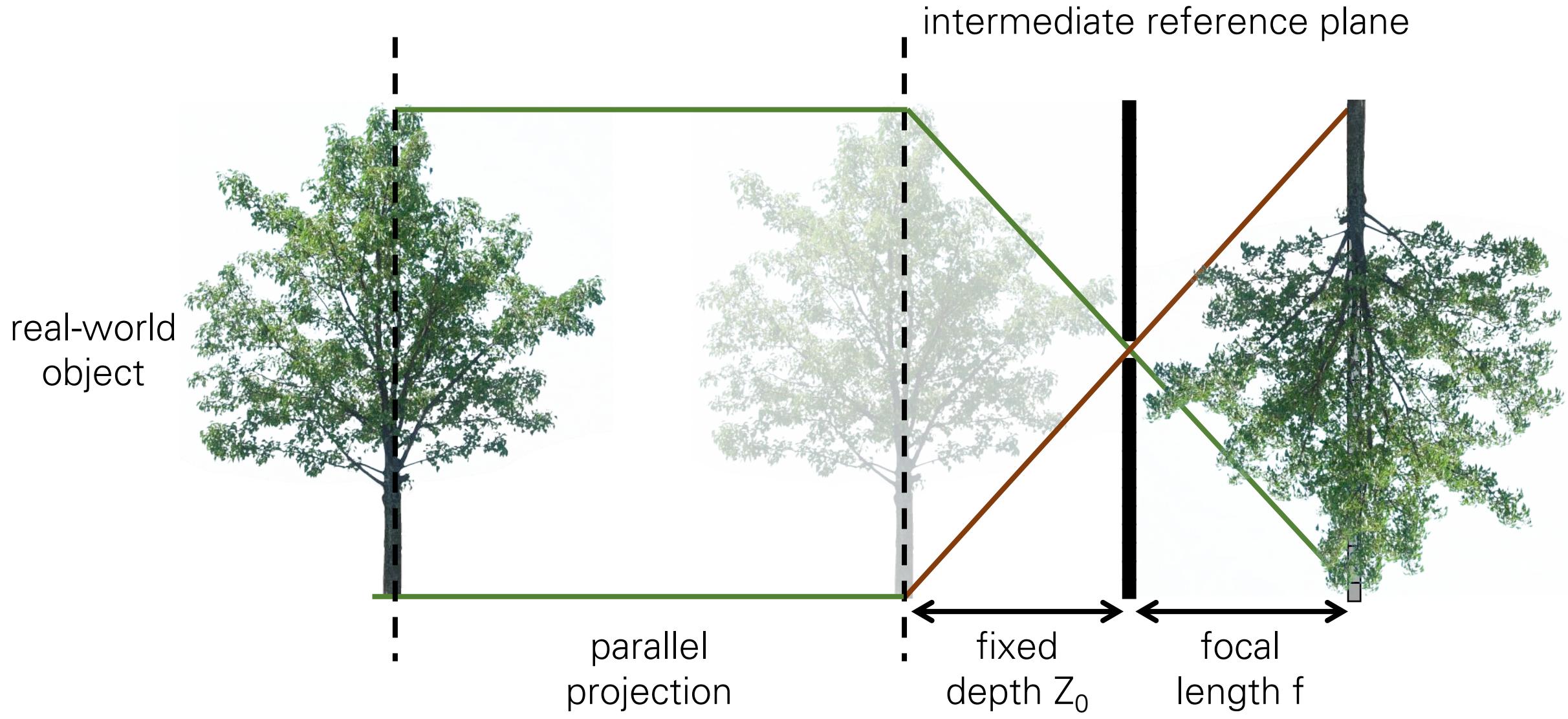
real-world
object



Continue increasing Z and f while maintaining same magnification?

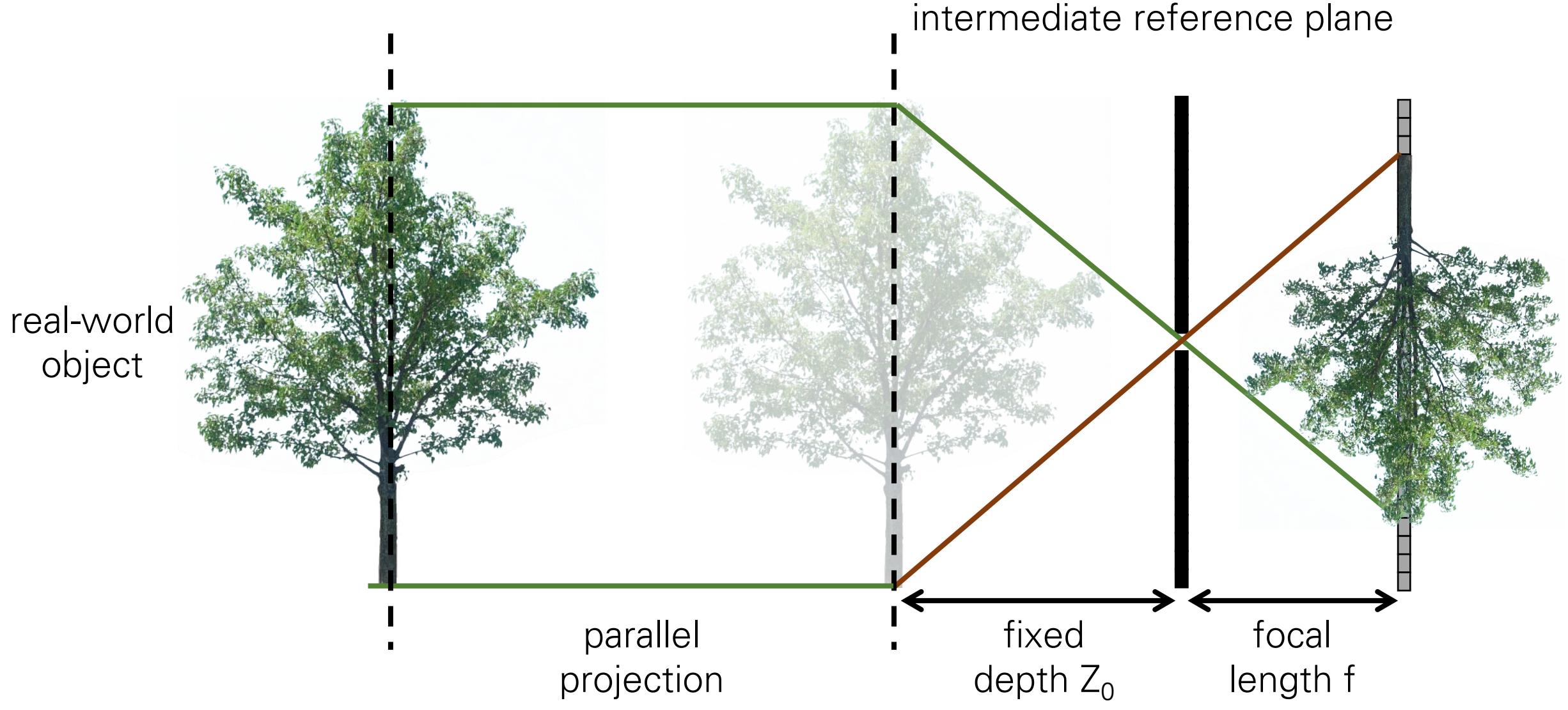
$$f \rightarrow \infty \text{ and } \frac{f}{Z} = \text{constant}$$

Orthographic camera



Depth-independent magnification $m = 1$ (real-life size).

Weak-perspective camera

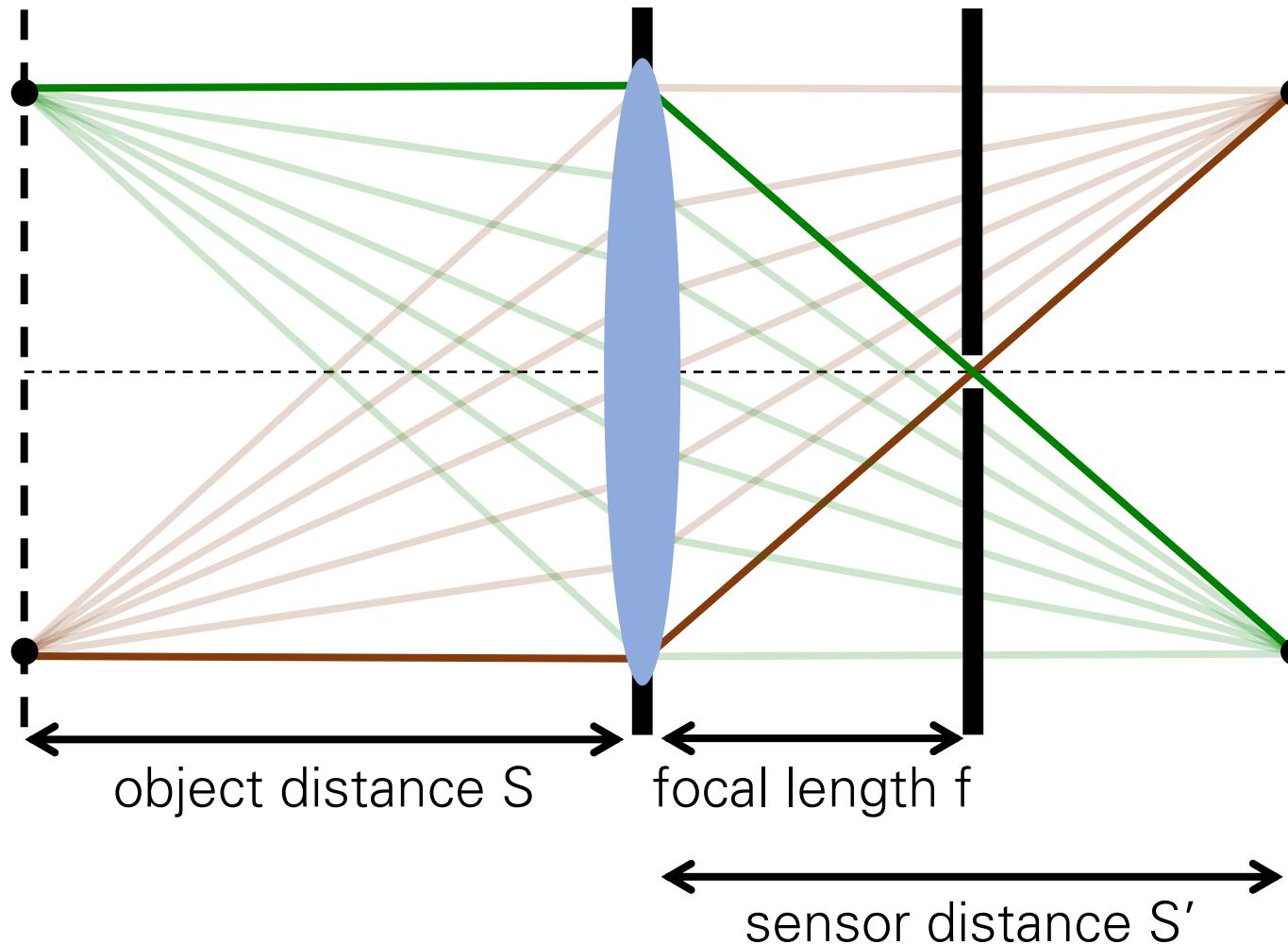


Depth-independent magnification $m = f / Z_0$.

How can we implement such a camera with lenses?

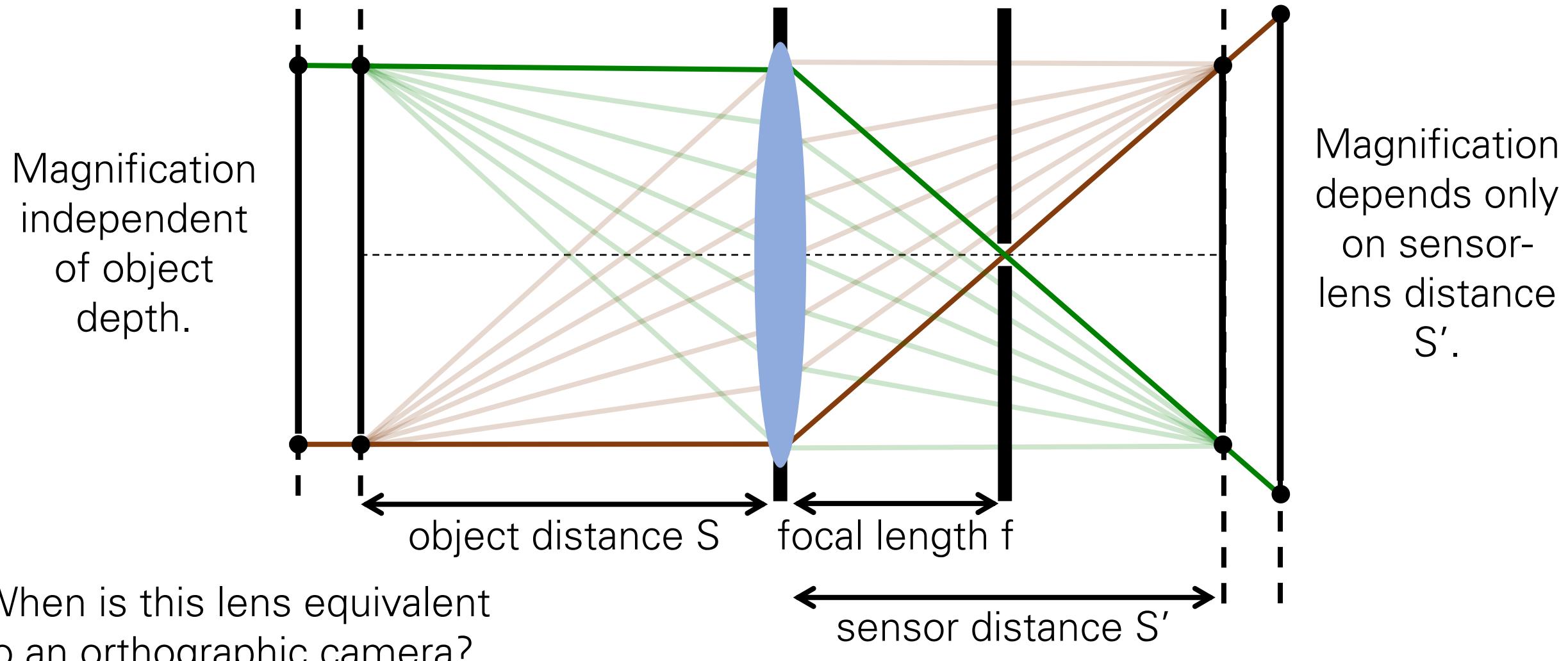
Telecentric lens

Place a pinhole at focal length, so that only rays parallel to primary ray pass through.

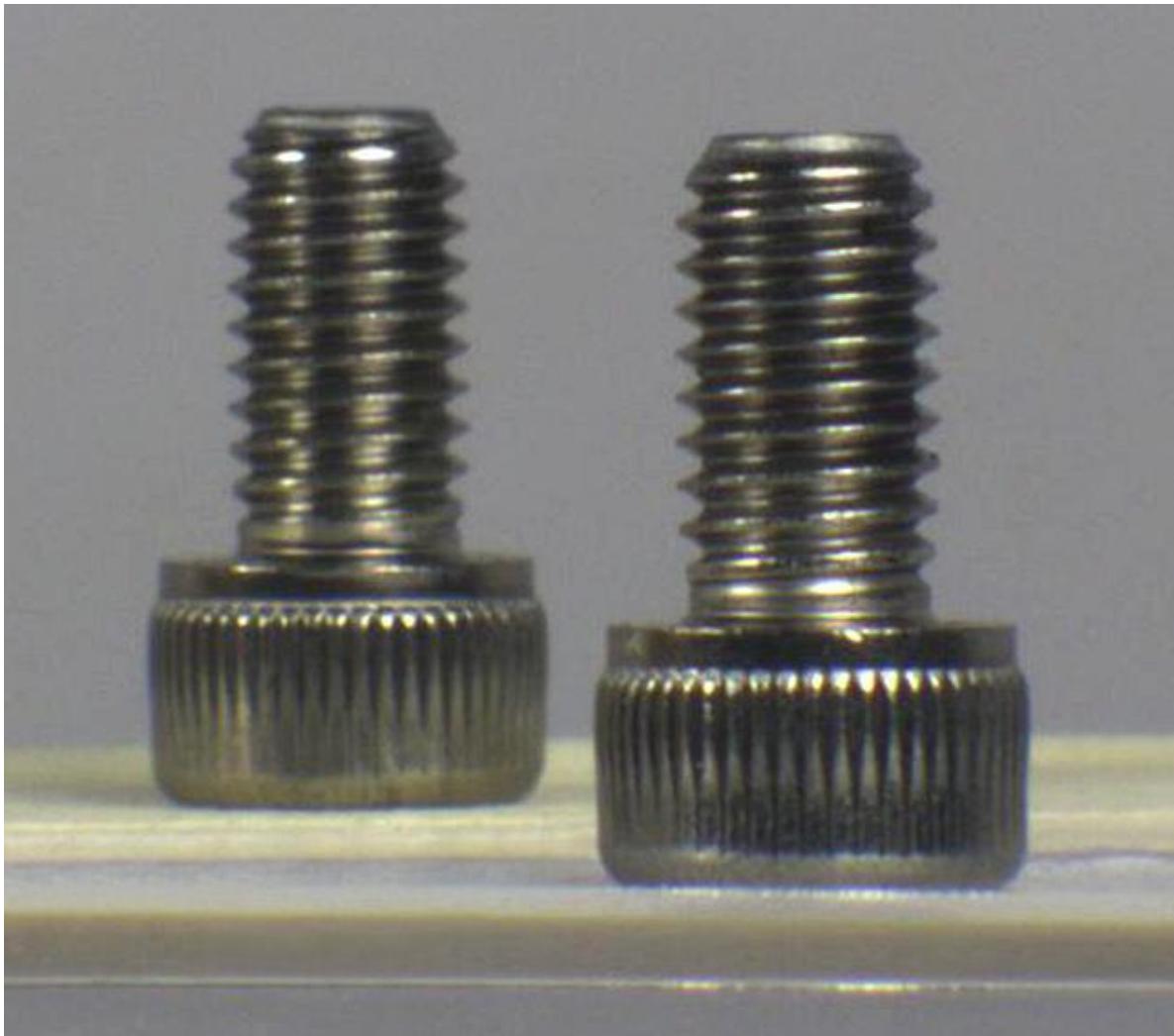


Telecentric lens

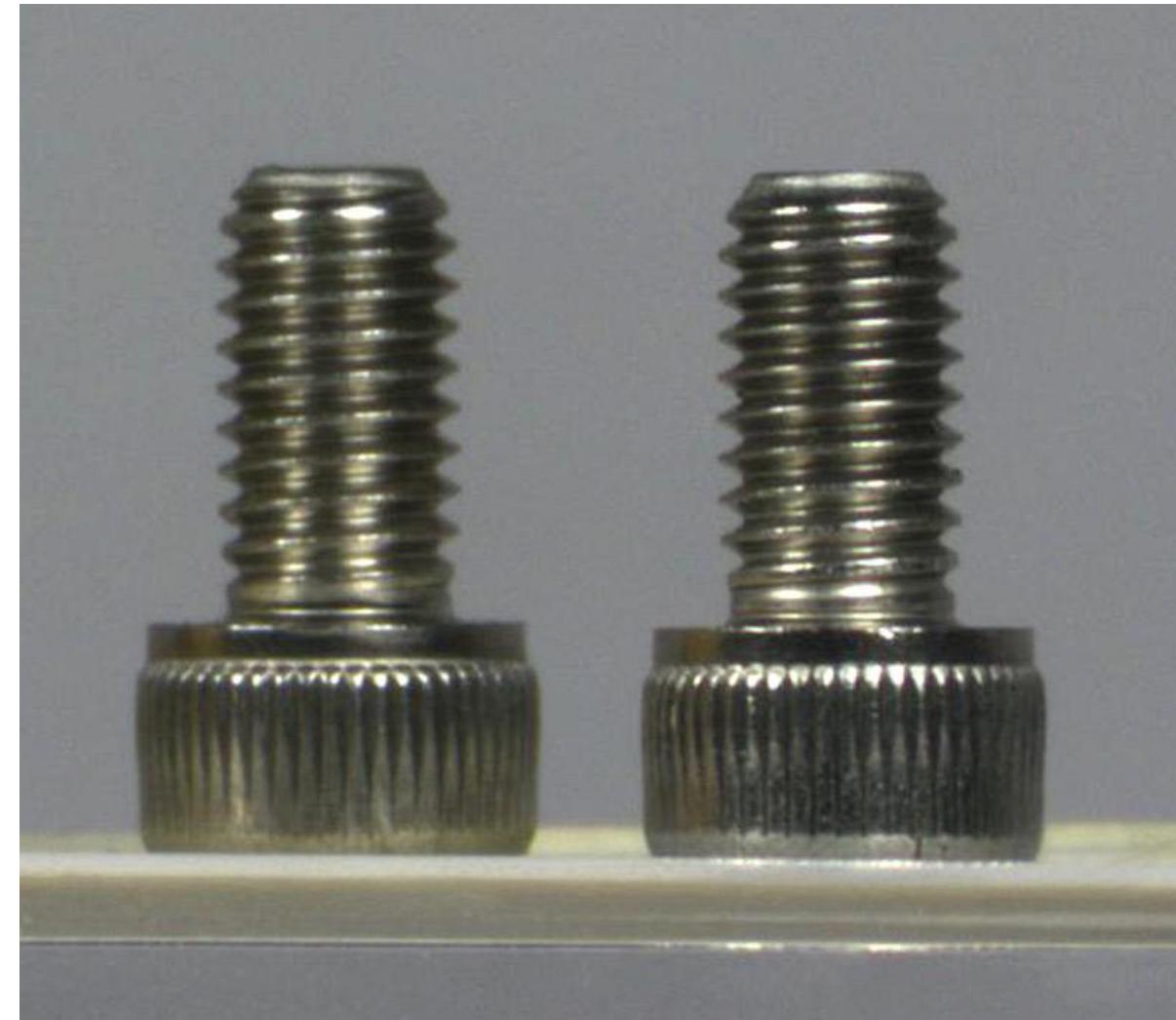
Place a pinhole at focal length, so that only rays parallel to primary ray pass through.



Regular vs elecentric lens



regular lens



telecentric lens

Next Lecture:
Digital Photography,
Noise and Color