

## About your midterm exam

- Zoom and Blackboard
- It will become active at 11:50am, and it will be released in 3 parts
  - Each contains multi-part questions
  - 30 mins to complete in one sitting
  - Backtracking allowed
- Open books, open notes. You can use your own lecture notes, lecture slides and textbook, but nothing else
- We won't take any questions during the exam. Please write "ERROR" if you think something is wrong

## Recap

- Revisiting %rip
- Calling Functions
  - The Stack
  - Passing Control
  - Passing Data
  - Local Storage
- Register Restrictions
- Pulling it all together: recursion example

## Plan for Today

- Arrays
- Structures
- Floating Point

**Disclaimer:** Slides for this lecture were borrowed from

—Randal E. Bryant and David R. O'Hallaroni's CMU 15-213 class

## Lecture Plan

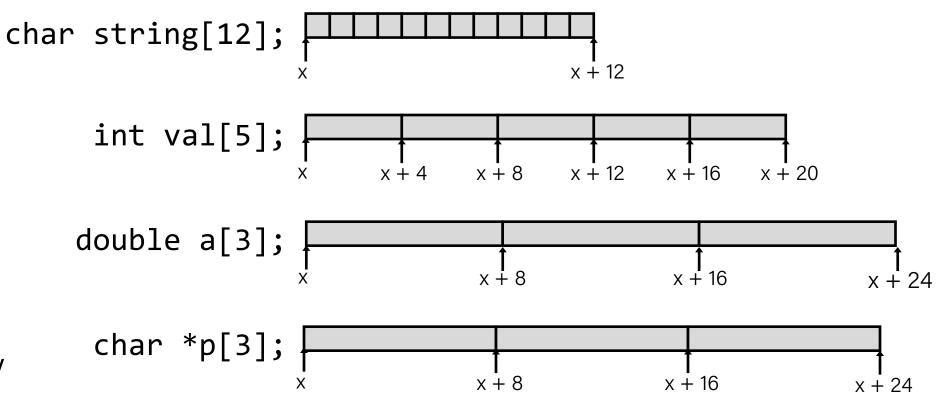
- Arrays
  - One-dimensional
  - Multi-dimensional (nested)
  - Multi-level
- Structures
- Floating Point

## Array Allocation

#### **Basic Principle**

#### T A[L];

- Array of data type T and length L
- Contiguously allocated region of L\*sizeof(T) bytes in memory



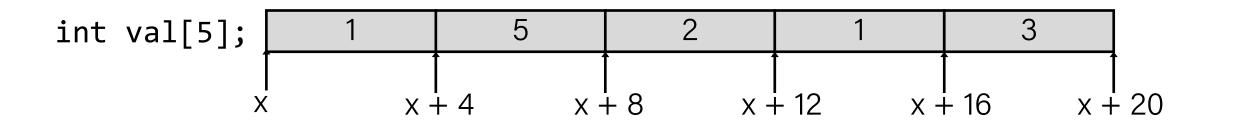
## Array Access

#### Basic Principle

T A[L];

- Array of data type T and length L
- Identifier A can be used as a pointer to array element 0: Type T\*

Reference	Туре	Value
val[4]	int	3
val	int *	X
val+1	int *	x + 4
&val[2]	int *	x + 8
val[5]	int	??
*(val+1)	int	5
val + i	int *	x + 4 i



## Array Example

```
5
#define ZLEN 5
                               zip_dig cmu;
typedef int zip_dig[ZLEN];
                                               16
                                                     20
                                                            24
                                                                  28
zip_dig cmu = \{1,5,2,1,3\};
                               zip_dig mit;
zip_dig mit = \{0,2,1,3,9\};
                                               36
                                                     40
                                                                  48
                                                                         52
zip_dig ku = \{3,4,4,5,0\};
                                zip_dig ku;
```

- Declaration "zip\_dig cmu" equivalent to "int cmu[5]"
- Example arrays were allocated in successive 20 byte blocks
  - Not guaranteed to happen in general

36

56

76

9

64

60

56

68

## Array Accessing Example

```
int get_digit
  (zip_dig z, int digit)
{
  return z[digit];
}
```

```
zip_dig ku; 3 4 4 5 0
16 20 24 28 32 3

# %rdi = z
# %rsi = digit
movl (%rdi,%rsi,4), %eax # z[digit]
```

- Register %rdi contains starting address of array
- Register %rsi contains array index
- Desired digit at %rdi + 4\*%rsi
- Use memory reference (%rdi, %rsi, 4)

## Array Loop Example

```
void zincr(zip_dig z) {
    size_t i;
    for (i=0; i<ZLEN; i++)
    z[i]++;
}</pre>
```

```
# %rdi = z
 movl $0, %eax
                       # i = 0
                        # goto middle
 jmp
        .L3
.L4:
                        # loop:
 addl $1, (%rdi,%rax,4) # z[i]++
 addq $1, %rax
                        # i++
.L3:
                        # middle
 cmpq $4, %rax
                        # i:4
                        # if <=, goto loop</pre>
 jbe .L4
 rep; ret
```

## Multidimensional (Nested) Arrays

#### **Declaration**

T A[R][C];

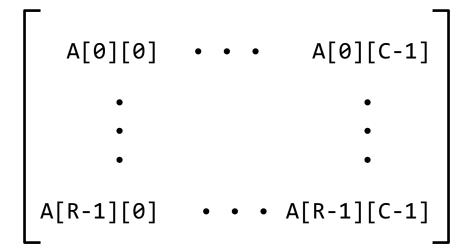
- 2D array of data type T
- R rows, C columns
- Type T element requires
   K bytes

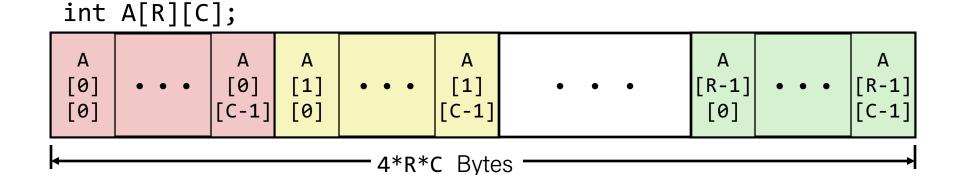
#### **Array Size**

• *R* \* *C* \* *K* bytes

#### Arrangement

Row-Major Ordering





## Nested Array Example

```
#define PCOUNT 4
zip_dig pgh[PCOUNT] =
{{1, 5, 2, 0, 6},
{1, 5, 2, 1, 3},
{1, 5, 2, 1, 7},
{1, 5, 2, 2, 1, 7};
```

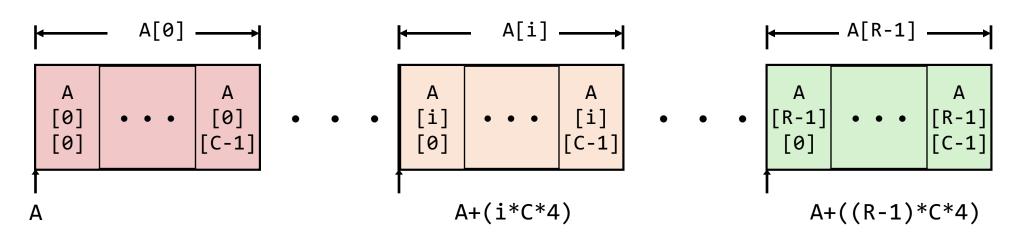
- "zip\_dig pgh[4]" equivalent to "int pgh[4][5]"
  - Variable pgh: array of 4 elements, allocated contiguously
  - Each element is an array of 5 int's, allocated contiguously
- "Row-Major" ordering of all elements in memory

## Nested Array Row Access

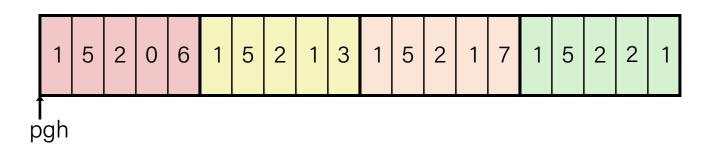
#### **Row Vectors**

- A[i] is array of C elements
- Each element of type T requires K bytes
- Starting address  $\mathbf{A} + i * (C * K)$

#### int A[R][C];



## Nested Array Row Access Code



#### **Row Vector**

- pgh[index] is array of 5 int's
- Starting address pgh+20\*index

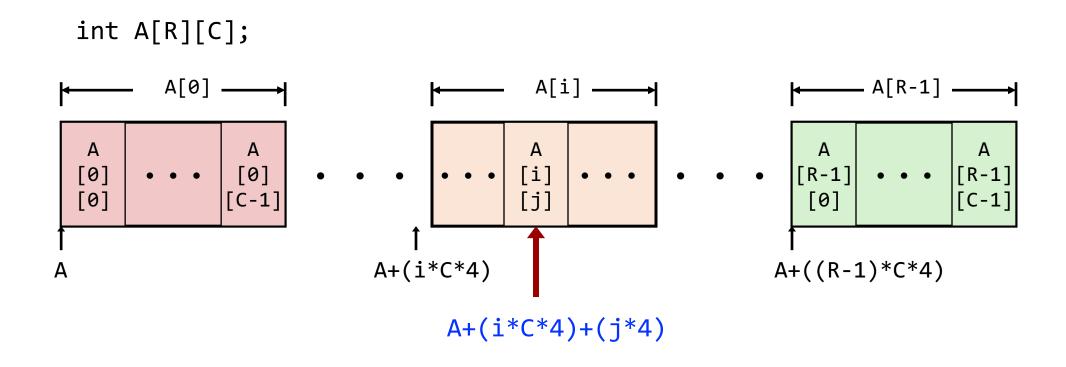
#### **Machine Code**

- Computes and returns address
- Compute as pgh+4\*(index+4\*index)

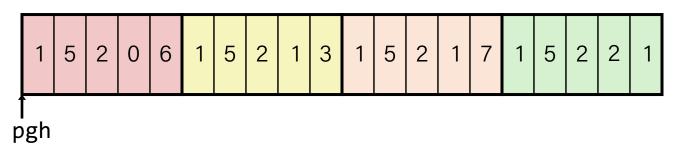
## Nested Array Element Access

#### **Array Elements**

- A[i][j] is element of type T, which requires K bytes
- Address A + i \* (C \* K) + j \* K = A + (i \* C + j) \* K



## Nested Array Element Access Code



```
int get_pgh_digit
    (int index, int dig)
{
    return pgh[index][dig];
}
leaq (%rdi,%rdi,4), %rax # 5*index
# 5*index+dig
movl pgh(,%rsi,4), %eax # M[pgh + 4*(5*index+dig)]
# M[pgh + 4*(5*index+dig
```

#### **Array Elements**

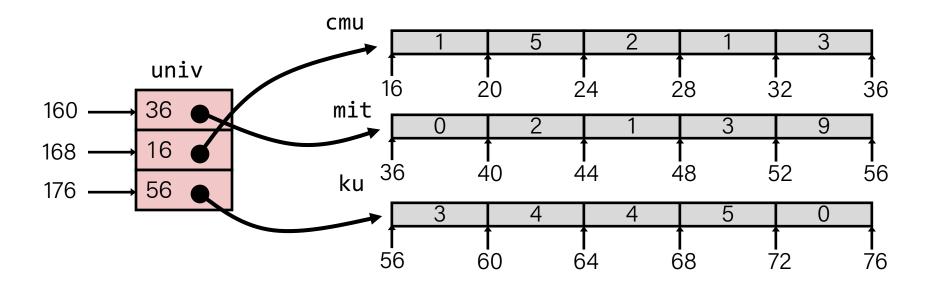
- pgh[index][dig] is int
- Address: pgh + 20\*index + 4\*dig
  - = pgh + 4\*(5\*index + dig)

## Multi-Level Array Example

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig ku = { 3, 4, 4, 5, 0 };

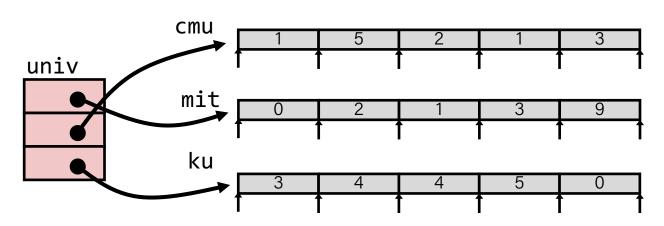
#define UCOUNT 3
int *univ[UCOUNT] = {mit, cmu, ku};
```

- Variable univ denotes array of 3 elements
- Each element is a pointer
  - 8 bytes
- Each pointer points to array of int's



## Element Access in Multi-Level Array

```
int get_univ_digit
  (size_t index, size_t digit)
{
  return univ[index][digit];
}
```



```
salq $2, %rsi # 4*digit
addq univ(,%rdi,8), %rsi # p = univ[index] + 4*digit
movl (%rsi), %eax # return *p
ret
```

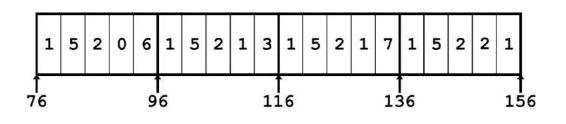
#### Computation

- Element access Mem[Mem[univ+8\*index]+4\*digit]
- Must do two memory reads
  - First get pointer to row array
  - Then access element within array

## Array Element Accesses

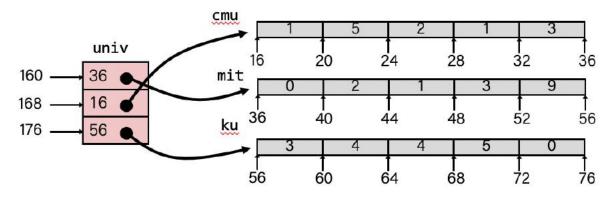
#### **Nested array**

```
int get_pgh_digit
  (size_t index, size_t digit)
{
  return pgh[index][digit];
}
```



#### Multi-level array

```
int get_univ_digit
  (size_t index, size_t digit)
{
  return univ[index][digit];
}
```



Accesses looks similar in C, but address computations very different:

Mem[pgh+20\*index+4\*digit]

Mem[Mem[univ+8\*index]+4\*digit]

### N × N Matrix Code

#### **Fixed dimensions**

 Know value of N at compile time

## Variable dimensions, explicit indexing

 Traditional way to implement dynamic arrays

## Variable dimensions, implicit indexing

Now supported by gcc

### 16 × 16 Matrix Access

```
/* Get element a[i][j] */
int fix ele(fix matrix a, size_t i, size_t j) {
 return a[i][j];
# a in %rdi, i in %rsi, j in %rdx
salq $6, %rsi
                # 64*i
addq %rsi, %rdi # a + 64*i
movl (%rdi,%rdx,4), %eax # M[a + 64*i + 4*j]
ret
```

#### **Array Elements**

- Address A + i \* (C \* K) + j \* K
- C = 16, K = 4

### n x n Matrix Access

```
/* Get element a[i][j] */
int var_ele(size_t n, int a[n][n], size_t i, size_t j) {
  return a[i][j];
}
```

#### **Array Elements**

- Address A + i \* (C \* K) + j \* K
- C = 16, K = 4
- Must perform integer multiplication

## Practice 1: Reverse Engineering

```
#define M ??
#define N ??

long P[M][N];
long Q[N][M];
long sum_elem(long i, long j)
{
    return P[i][j] + Q[j][i];
}
```

```
# long sum_elem(long i, long j)
# in %rdi, j in %rsi
1 sum_element:
    leaq 0(,%rdi,8), %rdx
                               Compute 8*i
    subq %rdi, %rdx
                               Compute 7*i
    addq %rsi, %rdx
                               Compute 7*i+j
    leaq (%rsi,%rsi,4), %rax
5
                               Compute 5*j
    addq %rax, %rdi
                               Compute i+5*j
   movq Q(,%rdi,8), %rax
                               Retrieve M[Q+8*(5*j+i)]
                               Add M[P+8*(7*i+j)]
8
    add P(,%rdx,8), %rax
9
    ret
```

#### What is the value of M and N?

M = 5 and N = 7



## Lecture Plan

- Arrays
- Structures
  - Allocation
  - Access
  - Alignment
- Floating Point

## Structure Representation

- Structure represented as block of memory
  - Big enough to hold all of the fields
- Fields ordered according to declaration
  - Even if another ordering could yield a more compact representation
- Compiler determines overall size + positions of fields
  - Machine-level program has no understanding of the structures in the source code

## Generating Pointer to Structure Member

```
struct rec {
    int a[4];
    size_t i;
    struct rec *next;
};
```

# r r+4\*idx a i next 0 16 24 32

## **Generating Pointer to Array Element**

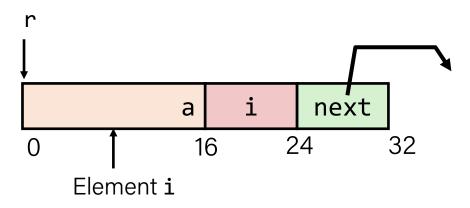
- Offset of each structure member determined at compile time
- Compute as r + 4\*idx

```
int *get_ap
  (struct rec *r, size_t idx)
{
  return &r->a[idx];
}
```

```
# r in %rdi, idx in %rsi
leaq (%rdi,%rsi,4), %rax
ret
```

## Following Linked List

```
struct rec {
    int a[4];
    int i;
    struct rec *next;
};
void set_val (struct rec *r, int val) {
  while (r) {
    int i = r \rightarrow i;
    r-a[i] = val;
    r = r \rightarrow next;
```



Register	Value
%rdi	r
%esi	val

```
.L11:
                               # loop:
                               # i = M[r+16]
 movslq 16(%rdi), %rax
         %esi, (%rdi,%rax,4)
                               \# M[r+4*i] = val
 movl
        24(%rdi), %rdi
                               \# r = M[r+24]
 movq
 testq
         %rdi, %rdi
                               #
                                  Test r
 jne
         .L11
                                   if !=0 goto loop
```

## Practice 2: Reverse Engineering

## Fill in the blanks by inspecting the assembly code generated by gcc.



```
struct test {
   short *p;
   struct {
      short x;
      short y;
   } s;
   struct test *next;
void st init(struct test *st) {
   st->s.y = \underline{st->s.x};
   st->p = &(st->s.y);
   st->next = <u>st</u>
```

```
# void st_init(struct test *st)
# st in %rdi
1 st_init:
2   movl 8(%rdi), %eax   Get st->s.x
3   movl %eax, 10(%rdi)   Save in st->s.y
4   leaq 10(%rdi), %rax   Compute &(st->s.y)
5   movq %rax, (%rdi)   Store in st->p
6   movq %rdi, 12(%rdi)   Store st in st->next
7   ret
```

```
0 8 10 12 20 p s.x s.y next
```

## Structures & Alignment

#### **Unaligned Data**

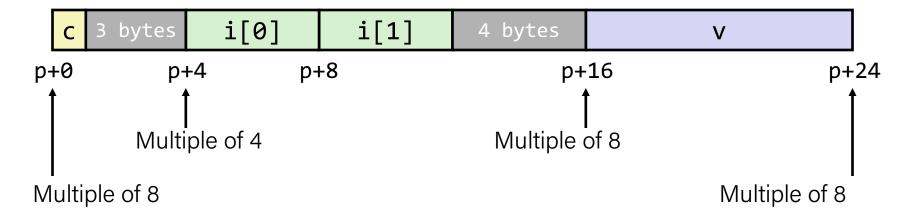
```
    c
    i[0]
    i[1]
    v

    p
    p+1
    p+5
    p+9
    p+17
```

```
struct S1 {
  char c;
  int i[2];
  double v;
} *p;
```

#### **Aligned Data**

- Primitive data type requires K bytes
- Address must be multiple of K



## Alignment Principles

#### **Aligned Data**

- Primitive data type requires K bytes
- Address must be multiple of K
- Required on some machines; advised on x86-64

#### **Motivation for Aligning Data**

- Memory accessed by (aligned) chunks of 4 or 8 bytes (system dependent)
  - Inefficient to load or store datum that spans quad word boundaries
  - Virtual memory trickier when datum spans 2 pages

#### Compiler

Inserts gaps in structure to ensure correct alignment of fields

## Specific Cases of Alignment (x86-64)

- 1 byte: char, ...
  - no restrictions on address
- 2 bytes: short, ...
  - lowest 1 bit of address must be 02
- 4 bytes: int, float, ...
  - lowest 2 bits of address must be 002
- 8 bytes: double, long, char \*, ...
  - lowest 3 bits of address must be 0002
- 16 bytes: long double (GCC on Linux)
  - lowest 4 bits of address must be 00002

## Satisfying Alignment with Structures

#### Within structure:

Must satisfy each element's alignment requirement

#### **Overall structure placement**

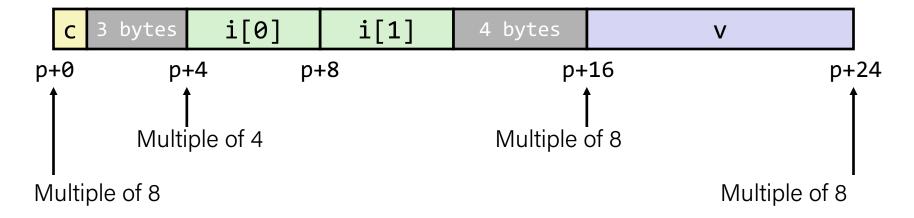
- Each structure has alignment requirement K
  - K = Largest alignment of any element
- Initial address & structure length must be multiples of K

#### **Example:**

• K = 8, due to **double** element

```
char c;
int i[2];
double v;
} *p;
```

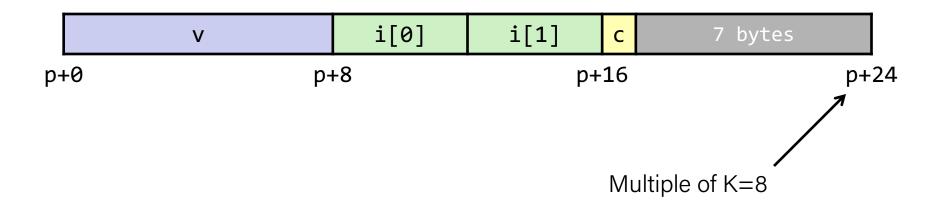
struct S1 {



## Meeting Overall Alignment Requirement

- For largest alignment requirement K
- Overall structure must be multiple of K

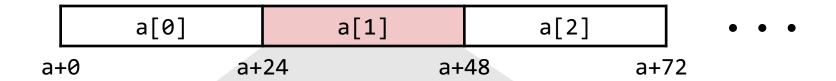
```
struct S2 {
  double v;
  int i[2];
  char c;
} *p;
```

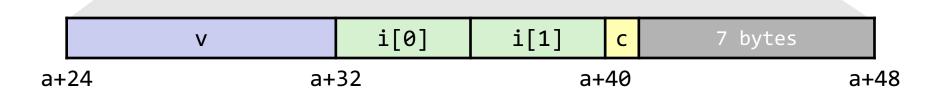


## Arrays of Structures

- Overall structure length multiple of K
- Satisfy alignment requirement for every element

```
struct S2 {
  double v;
  int i[2];
  char c;
} a[10];
```





## Accessing Array Elements

- Compute array offset 12\*idx
  - sizeof(S3), including alignment spacers
- Element j is at offset 8 within structure
- Assembler gives offset a+8 (resolved during linking)

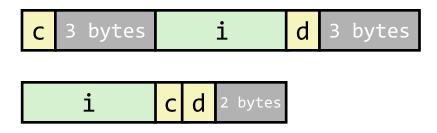
```
struct S3 {
   short i;
   float v;
   short j;
} a[10];
```

## Saving Space

Put large data types first

```
struct S4 {
    char c;
    int i;
    char c;
    char d;
} *p;
struct S5 {
    int i;
    char c;
    char d;
} *p;
```

Effect (K=4)



## Practice 3: Alignment



Determine the offset of each field, the total size of the structure, and its alignment requirement for x86-64.

```
struct mystruct {
   int *a;
   float b;
   char c;
   short d;
   long e;
   double f;
   int g;
   char *h;
```

Field	*a	b	C	d	е	f	g	*h	Total	Alignment
Size	8	4	1	2	8	8	4	8	40	0
Offset	$\cap$	Q	12	1/1	16	24	32	36	48	Ø
Oliset	U	O	12	14	10	<b>4</b>	52	30	•	padded to satisfy ent requirement

#### Rearranged structure with minimum wasted space:

Field	*a	h	f	е	b	g	d	C	Total	Alignment
Size	8	8	8	8	4	4	2	1	10	0
Offset	0	8	16	24	32	36	40	42	48	O noddod to ootiof
									-	padded to satisfy ent requirement

### Lecture Plan

- Arrays
  - One-dimensional
  - Multi-dimensional (nested)
  - Multi-level
- Structures
- Floating Point

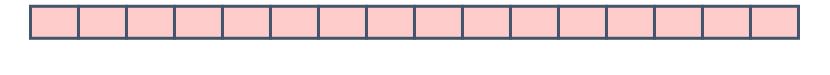
## Background

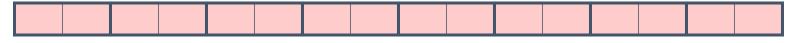
- History
  - x87 FP
    - Legacy, very ugly
  - Streaming SIMD Extensions (SSE) FP
    - SIMD: single instruction, multiple data
    - Special case use of vector instructions
  - AVX FP
    - Newest version
    - Similar to SSE
    - Documented in book

## Programming with SSE3

#### XMM Registers

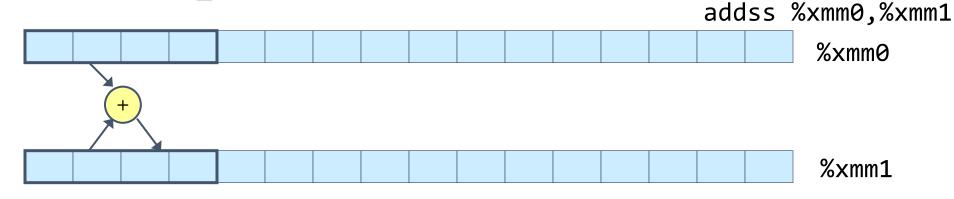
- 16 total, each 16 bytes
- 16 single-byte integers
- 8 16-bit integers
- 4 32-bit integers
- 4 single-precision floats
- 2 double-precision floats
- 1 single-precision float
- 1 double-precision float



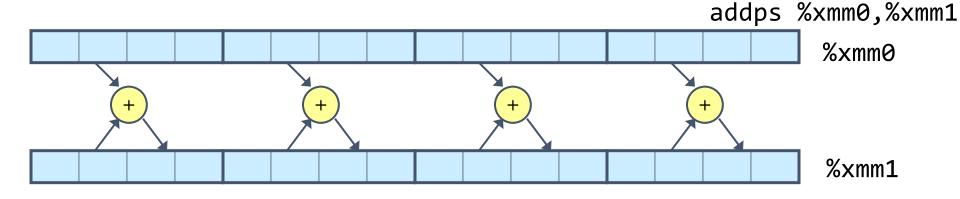


## Scalar & SIMD Operations

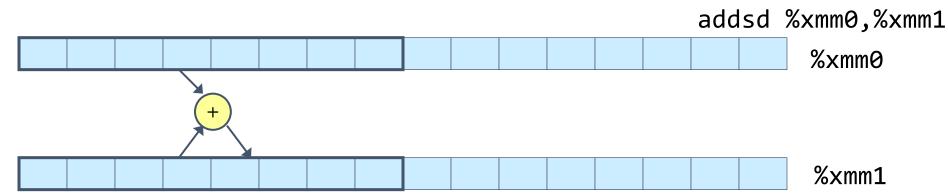
Scalar Operations: Single Precision



SIMD
 Operations:
 Single
 Precision



Scalar Operations: Double Precision



#### FP Basics

- Arguments passed in %xmm0, %xmm1, ...
- Result returned in %xmm0
- All XMM registers caller-saved

```
float fadd(float x, float y) {
    return x + y;
}
```

```
double dadd(double x, double y) {
    return x + y;
}
```

```
# x in %xmm0, y in %xmm1
addss %xmm1, %xmm0
ret
```

```
# x in %xmm0, y in %xmm1
addsd %xmm1, %xmm0
ret
```

## FP Memory Referencing

- Integer (and pointer) arguments passed in regular registers
- FP values passed in XMM registers
- Different mov instructions to move between XMM registers, and between memory and XMM registers

## Other Aspects of FP Code

- Lots of instructions
  - Different operations, different formats, ...
- Floating-point comparisons
  - Instructions ucomiss and ucomisd
  - Set condition codes CF, ZF, and PF
- Using constant values
  - Set XMM0 register to 0 with instruction xorpd %xmm0, %xmm0
  - Others loaded from memory

## Recap

- Arrays
- Structures
- Floating Point

That's it for assembly!

Next time: security vulnerabilities, memory hierarchy