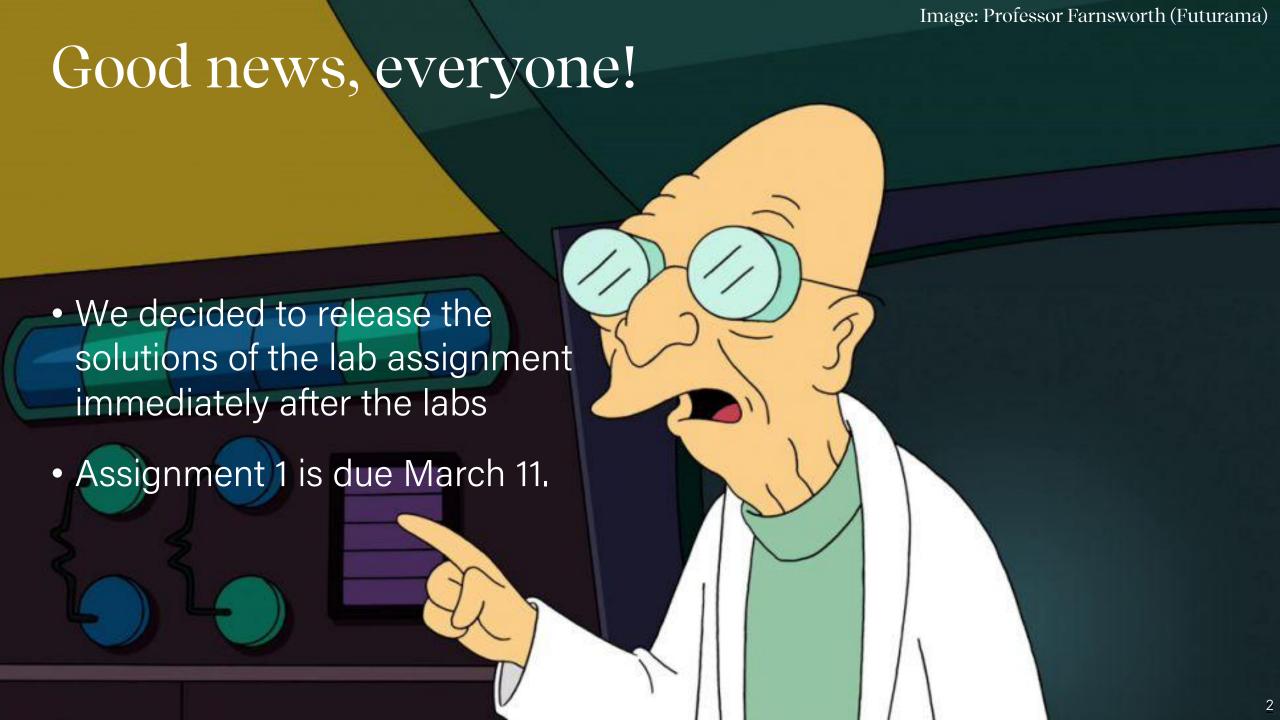
Computer ystems & rogramming

Lecture #7 – Arrays and Pointers



Aykut Erdem // Koç University // Spring 2021



COMP201 Topic 4: How can we effectively manage all types of memory in our programs?

Plan for Today

- Pointers and Parameters
- Double Pointers
- Arrays in Memory
- Arrays of Pointers
- Pointer Arithmetic

Disclaimer: Slides for this lecture were borrowed from

—Nick Troccoli and Lisa Yan's Stanford CS107 class

Lecture Plan

- Pointers and Parameters
- Double Pointers
- Arrays in Memory
- Arrays of Pointers
- Pointer Arithmetic

- A *pointer* is a variable that stores a memory address.
- Because there is no pass-by-reference in C like in C++, pointers let us pass around the address of one instance of memory, instead of making many copies.
- One (8 byte) pointer can represent any size memory location!
- Pointers are also essential for allocating memory on the heap, which we will cover later.
- Pointers also let us refer to memory generically, which we will cover later.

Recap: Memory

- Memory is a big array of bytes.
- Each byte has a unique numeric index that is commonly written in hexadecimal.
- A pointer stores one of these memory addresses.

Address	Value
	•••
0x105	'\0'
0x104	'e'
0x103	'1'
0x102	'p'
0x101	'p'
0x100	'a'
	•••

Recap: Memory

- Memory is a big array of bytes.
- Each byte has a unique numeric index that is commonly written in hexadecimal.
- A pointer stores one of these memory addresses.

Address	Value
	•••
261	'\0'
260	'e'
259	'1'
258	'p'
257	'p'
256	'a'
	•••

```
int x = 2;
// Make a pointer that stores the <u>address</u> of x.
// (& means "address of")
int *xPtr = &x;
// Dereference the pointer to go to that address.
// (* means "dereference")
printf("%d", *xPtr); // prints 2
```

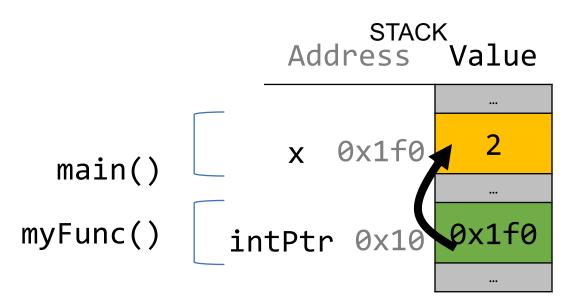
```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
     myFunc(&x);
     printf("%d", x);  // 3!
```



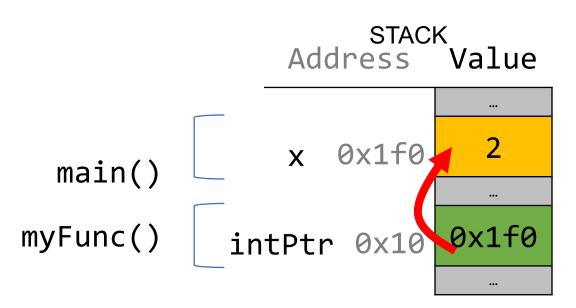
```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
     myFunc(&x);
     printf("%d", x);  // 3!
```



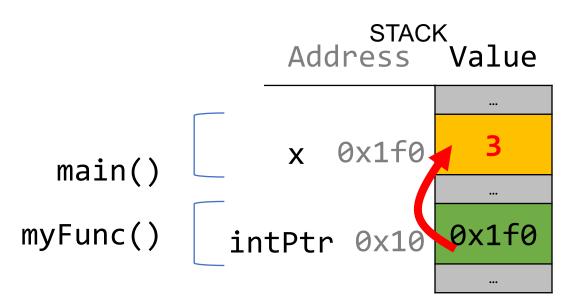
```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
     myFunc(&x);
     printf("%d", x);  // 3!
```



```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
     myFunc(&x);
     printf("%d", x);  // 3!
```



```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
    myFunc(&x);
    printf("%d", x);  // 3!
```



```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
     myFunc(&x);
     printf("%d", x);  // 3!
```



```
void myFunc(int *intPtr) {
     *intPtr = 3;
int main(int argc, char *argv[]) {
     int x = 2;
     myFunc(&x);
     printf("%d", x);  // 3!
```



When you pass a value as a parameter, C passes a copy of that value.

```
void myFunction(int x) {
     ...
}
int main(int argc, char *argv[]) {
    int num = 4;
     myFunction(num);  // passes copy of 4
}
```

When you pass a value as a parameter, C passes a copy of that value.

```
void myFunction(int *x) {
int main(int argc, char *argv[]) {
    int num = 4;
    myFunction(&num); // passes copy of e.g. 0xffed63
```

When you pass a value as a parameter, C passes a copy of that value.

```
void myFunction(char ch) {
     ...
}

int main(int argc, char *argv[]) {
     char *myStr = "Hello!";
     myFunction(myStr[1]); // passes copy of 'e'
}
```

If you are performing an operation with some input and do not care about any changes to the input, pass the data type itself.

If you are performing an operation with some input and do not care about any changes to the input, pass the data type itself.

```
void myFunction(char ch) {
    printf("%c", ch);
}
int main(int argc, char *argv[]) {
    char *myStr = "Hello!";
    myFunction(myStr[1]); // prints 'e'
}
```

If you are performing an operation with some input and do not care about any changes to the input, pass the data type itself.

```
int myFunction(int num1, int num2) {
    return x + y;
int main(int argc, char *argv[]) {
    int x = 5;
    int y = 6;
    int sum = myFunction(x, y); // returns 11
```

If you are modifying a specific instance of some value, pass the *location* of what you would like to modify.

Do I care about modifying *this* instance of my data? If so, I need to pass where that instance lives, as a parameter, so it can be modified.

If you are modifying a specific instance of some value, pass the *location* of what you would like to modify.

```
void capitalize(char *ch) {
    // modifies what is at the address stored in ch
int main(int argc, char *argv[]) {
    char letter = 'h';
    /* We don't want to capitalize any instance of 'h'.
      * We want to capitalize *this* instance of 'h'! */
    capitalize(&letter);
    printf("%c", letter); // want to print 'H';
```

If you are modifying a specific instance of some value, pass the *location* of what you would like to modify.

```
void doubleNum(int *x) {
     // modifies what is at the address stored in x
int main(int argc, char *argv[]) {
     int num = 2;
     /* We don't want to double any instance of 2.
      * We want to double *this* instance of 2! */
     doubleNum(&num);
     printf("%d", num); // want to print 4;
```

If a function takes an address (pointer) as a parameter, it can *go to* that address if it needs the actual value.

```
void capitalize(char *ch) {
    // *ch gets the character stored at address ch.
    char newChar = toupper(*ch);

    // *ch = goes to address ch and puts newChar there.
    *ch = newChar;
}
```

If a function takes an address (pointer) as a parameter, it can *go to* that address if it needs the actual value.

```
void capitalize(char *ch) {
    /* go to address ch and put the capitalized version
    * of what is at address ch there. */
    *ch = toupper(*ch);
}
```

If a function takes an address (pointer) as a parameter, it can *go to* that address if it needs the actual value.

```
void capitalize(char *ch) {
    // this capitalizes the address ch! ②
    char newChar = toupper(ch);

    // this stores newChar in ch as an address! ②
    ch = newChar;
}
```

char *

- A char * is technically a pointer to a <u>single character</u>.
- We commonly use **char** * as string by having the character it points to be followed by more characters and ultimately a null terminator.
- A char * could also just point to a single character (not a string).

String Behavior #7: If we change characters in a string parameter, these changes will persist outside of the function.

When we pass a **char** * string as a parameter, C makes a *copy* of the address stored in the **char** *, and passes it to the function. This means they both refer to the same memory location.

```
void myFunc(char *myStr) {
    ...
}
int main(int argc, char *argv[]) {
    char *str = "apple";
    myFunc(str);
    ...
}
```

```
STACK
                Address Value
  main()
              str 0xfff0
                           0x10
                           0x10
            myStr
                   0xff0
myFunc()
```

```
STACK
When we pass a char array as a parameter, C
                                                            Address
makes a copy of the address of the first array
element, and passes it (as a char *) to the
                                                                       '\0'
                                                               0x105
function.
                                                               0x104
                                                                       '1'
void myFunc(char *myStr) {
                                                               0x103
                                             main()
                                                               0x102
                                                               0x101
int main(int argc, char *argv[]) {
      char str[6];
      strcpy(str, "apple");
      myFunc(str);
                                           myFunc()
                                                                      0x100
```

```
STACK
When we pass a char array as a parameter, C
                                                           Address
makes a copy of the address of the first array
element, and passes it (as a char *) to the
function.
                                                                      '\0'
                                                              0x105
                                                              0x104
void myFunc(char *myStr) {
                                                                       '1'
                                                              0x103
                                            main()
                                                              0x102
                                                              0x101
int main(int argc, char *argv[]) {
      char str[6];
      strcpy(str, "apple");
      // equivalent
      char *strAlt = str;
      myFunc(strAlt);
                                          myFunc()
                                                                     0x100
```

```
STACK
This means if we modify characters in
                                                          Address
myFunc, the changes will persist back in
main!
                                                                    '\0'
                                                            0x105
                                                             0x104
void myFunc(char *myStr) {
                                                                     '1'
     myStr[4] = 'y';
                                                             0x103
                                           main()
                                                             0x102
                                                             0x101
int main(int argc, char *argv[]) {
      char str[6];
                                                             0x100
      strcpy(str, "apple");
     myFunc(str);
      printf("%s", str); // apply
                                         myFunc()
                                                     myStr
                                                                   0x100
```

```
STACK
This means if we modify characters in
                                                          Address
myFunc, the changes will persist back in
main!
                                                                     '\0'
                                                             0x105
                                                             0x104
void myFunc(char *myStr) {
                                                                     '1'
     myStr[4] = 'y';
                                                             0x103
                                           main()
                                                             0x102
                                                             0x101
int main(int argc, char *argv[]) {
     char str[6];
                                                             0x100
     strcpy(str, "apple");
     myFunc(str);
     printf("%s", str);
                          // apply
                                         myFunc()
                                                     myStr
                                                                    0x100
```

Exercise 1

We want to write a function that prints out the square of a number. What should go in each of the blanks?

```
void printSquare(__?__) {
    int square = __?__ * __?__;
    printf("%d", square);
int main(int argc, char *argv[]) {
    int num = 3;
    printSquare( ? ); // should print 9
```

We want to write a function that prints out the square of a number. What should go in each of the blanks?

```
void printSquare(int x) {
   int square = x * x;
   printf("%d", square);
}
```

We are performing a calculation with some input and do not care about any changes to the input, so we pass the data type itself.

```
int main(int argc, char *argv[]) {
   int num = 3;
   printSquare(num); // should print 9
}
```

We want to write a function that prints out the square of a number. What should go in each of the blanks?

```
void printSquare(int x) {
    x = x * x;
    printf("%d", x);
}
```

We are performing a calculation with some input and do not care about any changes to the input, so we pass the data type itself.

```
int main(int argc, char *argv[]) {
   int num = 3;
   printSquare(num); // should print 9
}
```

We want to write a function that flips the case of a letter. What should go in each of the blanks?

```
void flipCase(__?__) {
      if (isupper(___?__)) {
      __?__ = __?__;
} else if (islower(__?__)) {
int main(int argc, char *argv[]) {
      char ch = 'g';
      flipCase(___?__);
      printf("%c", ch);  // want this to print 'G'
```

We want to write a function that flips the case of a letter. What should go in each of the blanks?

```
We are modifying a specific
void flipCase(char *letter) {
                                          instance of the letter, so we pass the
     if (isupper(*letter)) {
                                          location of the letter we would like
           *letter = tolower(*letter);
      } else if (islower(*letter)) {
                                          to modify.
           *letter = toupper(*letter);
int main(int argc, char *argv[]) {
     char ch = 'g';
     flipCase(&ch);
     printf("%c", ch);  // want this to print 'G'
```

Pointers Summary

- If you are performing an operation with some input and do not care about any changes to the input, pass the data type itself.
- If you are modifying a specific instance of some value, pass the location of what you would like to modify.
- If a function takes an address (pointer) as a parameter, it can *go to* that address if it needs the actual value.

Pointers Summary

• **Tip:** setting a function parameter equal to a new value usually doesn't do what you want. Remember that this is setting the function's *own copy* of the parameter equal to some new value.

```
void doubleNum(int x) {
    x = x * x;  // modifies doubleNum's own copy!
}

void advanceStr(char *str) {
    str += 2;  // modifies advanceStr's own copy!
}
```

Lecture Plan

- Pointers and Parameters
- Double Pointers
- Arrays in Memory
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Sometimes, we would like to modify a string's pointer itself, rather than just the characters it points to. E.g. we want to write a function **skipSpaces** that modifies a string pointer to skip past any initial spaces. What should go in each of the blanks?

```
void skipSpaces(__?__) {
    ...
}
int main(int argc, char *argv[]) {
    char *str = " hello";
    skipSpaces(__?__);
    printf("%s", str); // should print "hello"
}
```

Sometimes, we would like to modify a string's pointer itself, rather than just the characters it points to. E.g. we want to write a function **skipSpaces** that modifies a string pointer to skip past any initial spaces. What should go in each of the blanks?

```
void skipSpaces(char **strPtr) {
    ...
}

We are modifying a specific
instance of the string pointer, so we
pass the location of the string
pointer we would like to modify.
    char *str = " hello";
    skipSpaces(&str);
    printf("%s", str); // should print "hello"
}
```

Sometimes, we would like to modify a string's pointer itself, rather than just the characters it points to. E.g. we want to write a function **skipSpaces** that modifies a string pointer to skip past any initial spaces. What should go in each of the blanks?

```
void skipSpaces(char *strPtr) {
    ...
}

This advances skipSpace's own copy of the string pointer, not the instance in main.

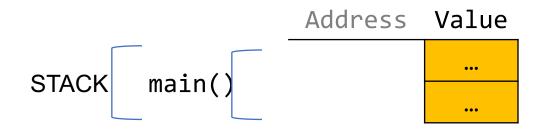
int main(int argc, char *argv[]) {
    char *str = " hello";
    skipSpaces(str);
    printf("%s", str); // should print "hello"
}
```

Demo: Skip Spaces

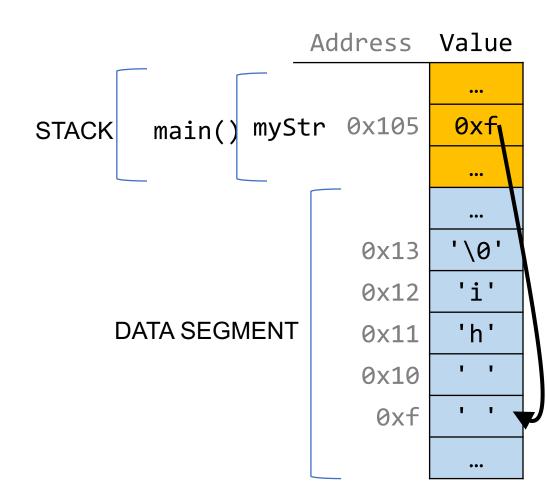


skip_spaces.c

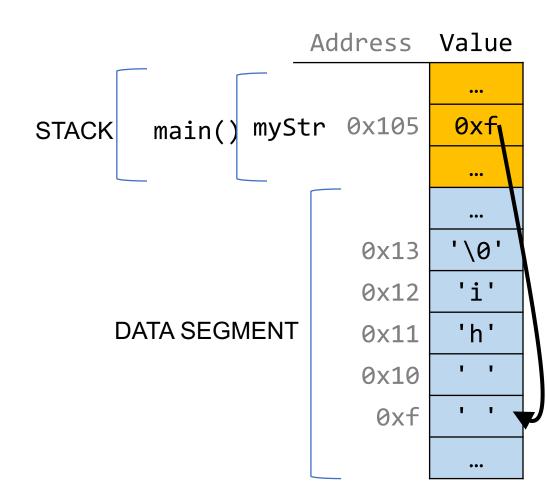
```
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
}
int main(int argc, char *argv[]) {
    char *myStr = " hi";
    skipSpaces(&myStr);
    printf("%s\n", myStr); // hi
    return 0;
}
```



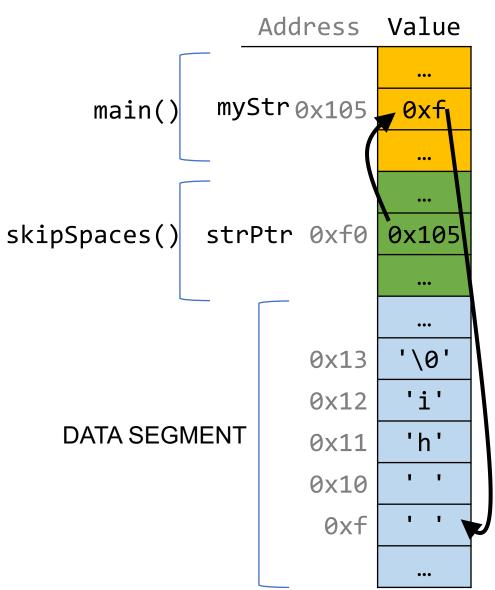
```
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
}
int main(int argc, char *argv[]) {
    char *myStr = " hi";
    skipSpaces(&myStr);
    printf("%s\n", myStr); // hi
    return 0;
}
```



```
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
}
int main(int argc, char *argv[]) {
    char *myStr = " hi";
    skipSpaces(&myStr);
    printf("%s\n", myStr); // hi
    return 0;
}
```



```
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
                                         STACK
int main(int argc, char *argv[]) {
    char *myStr = " hi";
    skipSpaces(&myStr);
    printf("%s\n", myStr);
                                 // hi
    return 0;
```

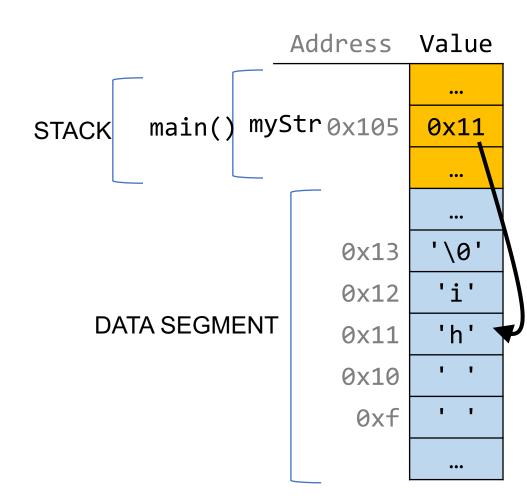


```
Address Value
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
                                                                   myStrox105
                                                          main()
                                                                                0xf
                                         STACK
int main(int argc, char *argv[]) {
    char *myStr = " hi";
                                                                  strPtr 0xf0
                                                                               0x105
    skipSpaces(&myStr);
                                                  skipSpaces()
                                                               numSpaces 0xe8
    printf("%s\n", myStr);
                                  // hi
    return 0;
                                                                                '\0'
                                                                          0x13
                                                                                'i'
                                                                         0x12
                                                        DATA SEGMENT
                                                                          0x11
                                                                          0x10
                                                                           0xf
```

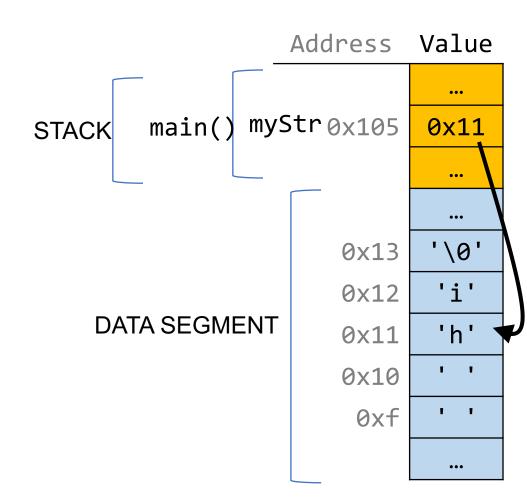
```
Address Value
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
                                                                   myStrox105
                                                          main()
                                                                                0xf
                                         STACK
int main(int argc, char *argv[]) {
    char *myStr = " hi";
                                                                  strPtr 0xf0
                                                                               0x105
    skipSpaces(&myStr);
                                                  skipSpaces()
                                                               numSpaces 0xe8
    printf("%s\n", myStr);
                                  // hi
    return 0;
                                                                                '\0'
                                                                         0x13
                                                                                'i'
                                                                         0x12
                                                        DATA SEGMENT
                                                                         0x11
                                                                         0x10
                                                                           0xf
```

```
Address Value
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
                                                                   myStrox105
                                                          main()
                                          STACK
int main(int argc, char *argv[]) {
    char *myStr = " hi";
                                                                  strPtr 0xf0
                                                                               0x105
    skipSpaces(&myStr);
                                                  skipSpaces()
                                                               numSpaces 0xe8
    printf("%s\n", myStr);
                                  // hi
    return 0;
                                                                                '\0'
                                                                          0x13
                                                                                'i'
                                                                         0x12
                                                        DATA SEGMENT
                                                                          0x11
                                                                          0x10
                                                                                . .
                                                                           0xf
```

```
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
}
int main(int argc, char *argv[]) {
    char *myStr = " hi";
    skipSpaces(&myStr);
    printf("%s\n", myStr); // hi
    return 0;
}
```



```
void skipSpaces(char **strPtr) {
    int numSpaces = strspn(*strPtr, " ");
    *strPtr += numSpaces;
}
int main(int argc, char *argv[]) {
    char *myStr = " hi";
    skipSpaces(&myStr);
    printf("%s\n", myStr); // hi
    return 0;
}
```



Making Copies

```
Address Value
void skipSpaces(char *strPtr) {
    int numSpaces = strspn(strPtr, " ");
    strPtr += numSpaces;
                                                                     myStr<sub>0x105</sub>
                                                            main()
                                          STACK
int main(int argc, char *argv[]) {
    char *myStr = " hi";
                                                     skipSpaces()
                                                                    strPtr 0xf0
    skipSpaces(myStr);
                               myFunc myFunc
    printf("%s\n", myStr);
                                        hi
    return 0;
                                                                           0x13
                                                                           0x12
                                                         DATA SEGMENT
                                                                           0x11
                                                                           0x10
                                                                             0xf
```

0xf

0xf

'\0'

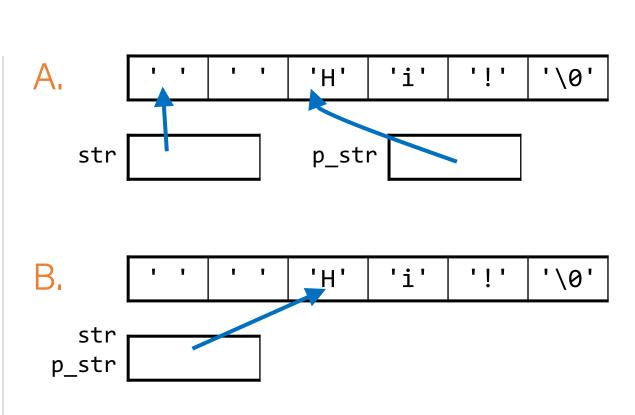
'i'

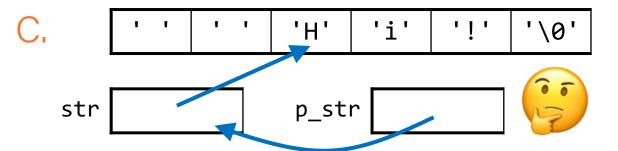
'h'

Skip spaces

```
1 void skip_spaces(char **p_str) {
     int num = strspn(*p_str, " ");
     *p_str = *p_str + num;
   int main(int argc, char *argv[]){
     char *str = " Hi!";
     skip_spaces(&str);
    printf("%s", str); // "Hi!"
     return 0;
10 }
```

What diagram most accurately depicts program state at Line 4 (before skip_spaces returns to main)?

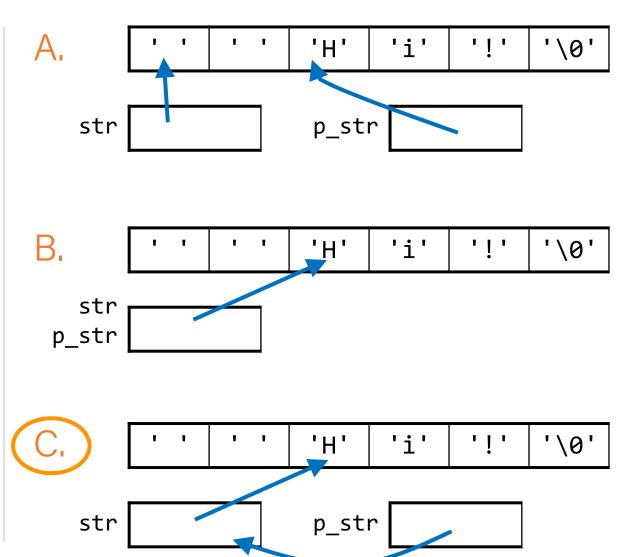




Skip spaces

```
1 void skip_spaces(char **p_str) {
     int num = strspn(*p_str, " ");
     *p_str = *p_str + num;
   int main(int argc, char *argv[]){
     char *str = " Hi!";
     skip_spaces(&str);
    printf("%s", str); // "Hi!"
     return 0;
10 }
```

What diagram most accurately depicts program state at Line 4 (before skip spaces returns to main)?



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- Arrays in Memory
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- Pointer Arithmetic

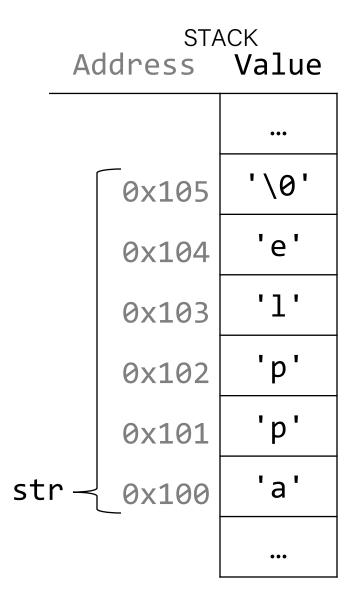
Arrays

When you declare an array, contiguous memory is allocated on the stack to store the contents of the entire array.

```
char str[6];
strcpy(str, "apple");
```

The array variable (e.g. **str**) is not a pointer; it refers to the entire array contents. In fact, **sizeof** returns the size of the entire array!

```
int arrayBytes = sizeof(str);  // 6
```



Arrays

An array variable refers to an entire block of memory. You cannot reassign an existing array to be equal to a new array.

```
int nums[] = {1, 2, 3};
int nums2[] = {4, 5, 6, 7};
nums = nums2; // not allowed!
```

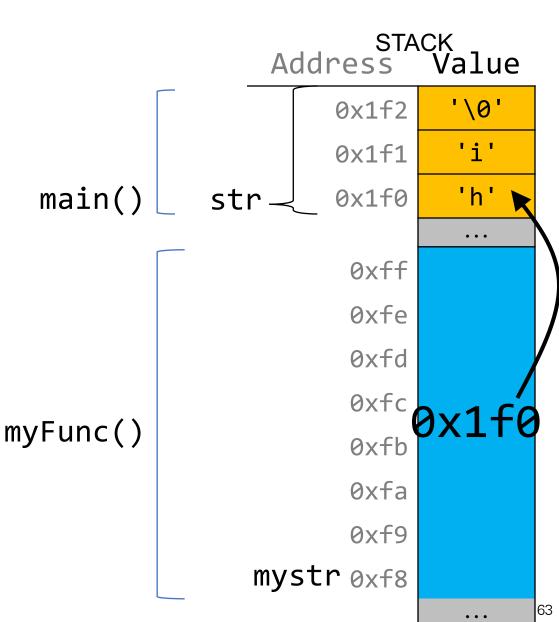
An array's size cannot be changed once you create it; you must create another new array instead.

Arrays as Parameters

When you pass an **array** as a parameter, C makes a *copy of the address of the first array element*, and passes it (a pointer) to the function.

```
void myFunc(char *myStr) {
    ...
}

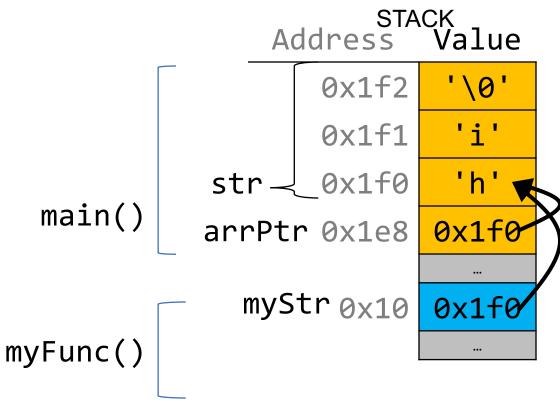
int main(int argc, char *argv[]) {
    char str[3];
    strcpy(str, "hi");
    myFunc(str);
    ...
}
```



Arrays as Parameters

When you pass an **array** as a parameter, C makes a *copy of the address of the first array element and* passes it (a pointer) to the function.

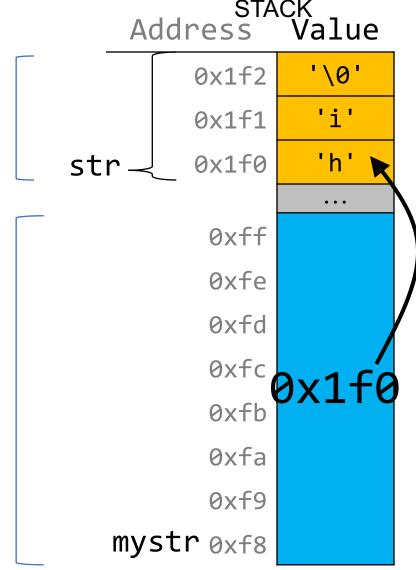
```
void myFunc(char *myStr) {
int main(int argc, char *argv[]) {
     char str[3];
     strcpy(str, "hi");
     // equivalent
     char *arrPtr = str;
     myFunc(arrPtr);
```



Arrays as Parameters

This also means we can no longer get the full size of the array using **sizeof**, because now it is just a pointer.

```
main()
void myFunc(char *myStr) {
     int size = sizeof(myStr); // 8
int main(int argc, char *argv[]) {
     char str[3];
     strcpy(str, "hi");
                                      myFunc()
     int size = sizeof(str); // 3
     myFunc(str);
```

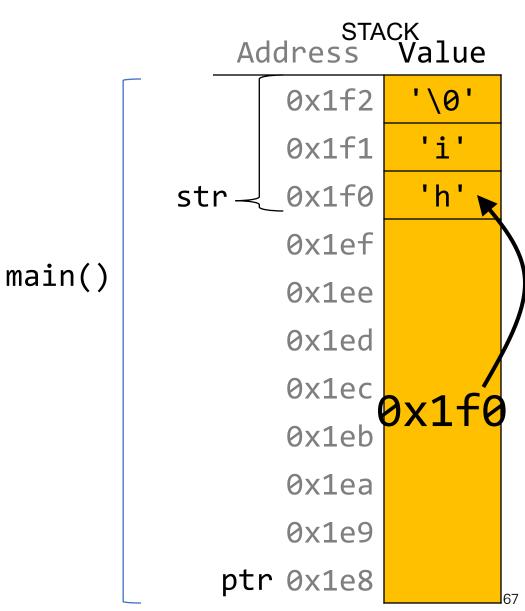


sizeof returns the size of an array, or 8 for a pointer. Therefore, when we pass an array as a parameter, we can no longer use **sizeof** to get its full size.

Arrays and Pointers

```
You can also make a pointer equal to an array; it will point to the first element in that array.
```

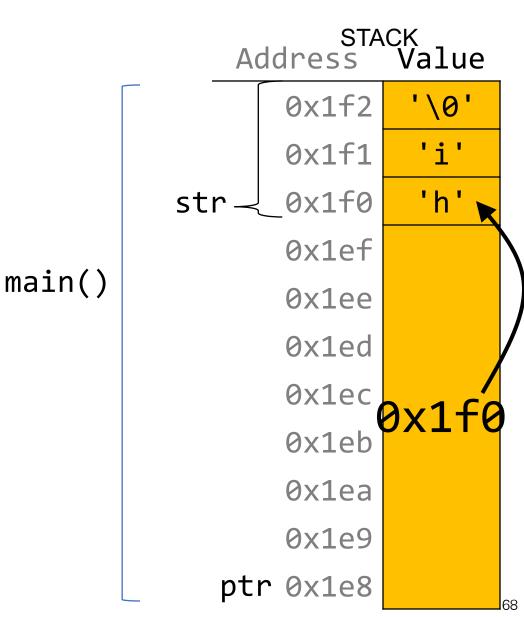
```
int main(int argc, char *argv[]) {
    char str[3];
    strcpy(str, "hi");
    char *ptr = str;
    ...
```



Arrays and Pointers

You can also make a pointer equal to an array; it will point to the first element in that array.

```
int main(int argc, char *argv[]) {
     char str[3];
     strcpy(str, "hi");
     char *ptr = str;
     // equivalent
     char *ptr = &str[0];
     // equivalent, but avoid
     char *ptr = &str;
```



Lecture Plan

- Pointers and Parameters
- Double Pointers
- Arrays in Memory
- Arrays of Pointers
- Pointer Arithmetic

Arrays Of Pointers

You can make an array of pointers to e.g. group multiple strings together:

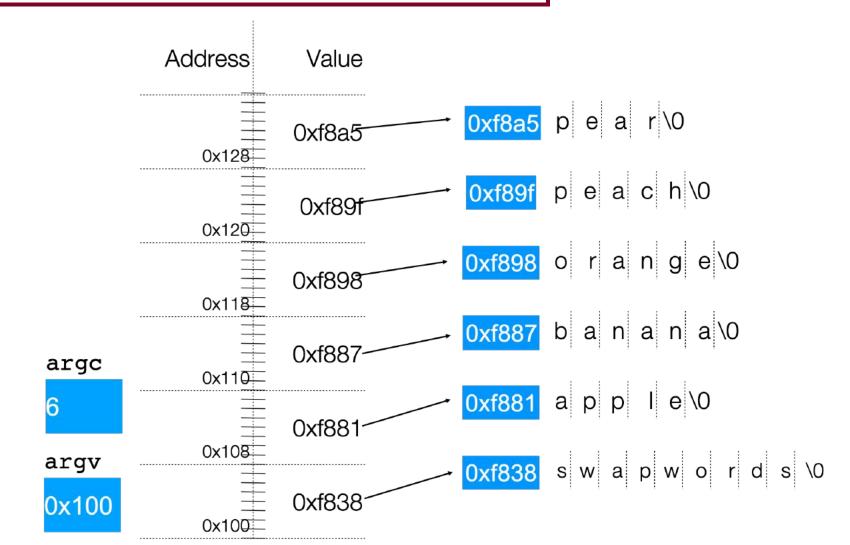
```
char *stringArray[5]; // space to store 5 char *s
```

This stores 5 **char *s**, not all of the characters for 5 strings!

```
char *str0 = stringArray[0];  // first char *
```

Arrays Of Pointers

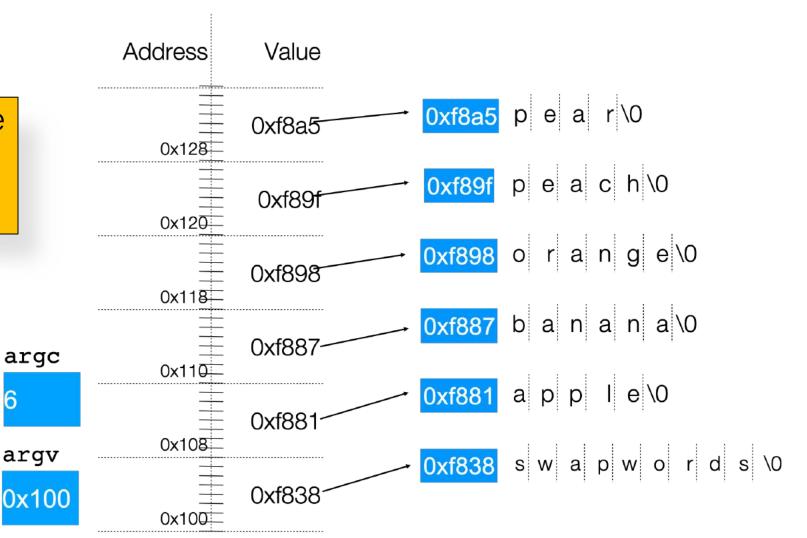
./swapwords apple banana orange peach pear



Arrays Of Pointers

./swapwords apple banana orange peach pear

What is the value of argv[2] in this diagram?



Lecture Plan

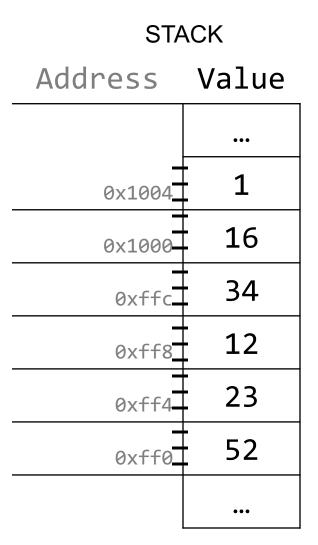
- Pointers and Parameters
- Double Pointers
- Arrays in Memory
- Arrays of Pointers
- Pointer Arithmetic

When you do pointer arithmetic, you are adjusting the pointer by a certain *number of places* (e.g. characters).

DATA SEGMENT Address Value '\0' 0xff5 'e' 0xff4 '1' 0xff3 'p' 0xff2 'p' 0xff1 'a' 0xff0

Pointer arithmetic does *not* work in bytes. Instead, it works in the *size of the type it points to*.

```
// nums points to an int array
int *nums = ...
                        // e.g. 0xff0
int *nums1 = nums + 1; // e.g. 0xff4
int *nums3 = nums + 3; // e.g. 0xffc
printf("%d", *nums);
                        // 52
printf("%d", *nums1);  // 23
printf("%d", *nums3);
                     // 34
```

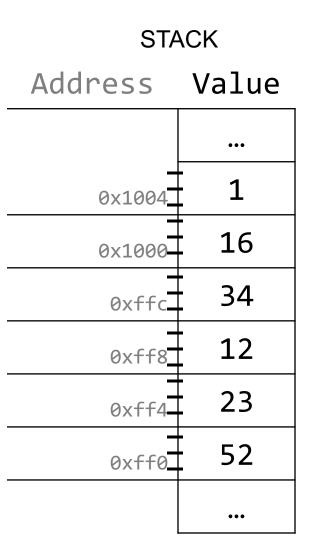


When you use bracket notation with a pointer, you are actually performing pointer arithmetic and dereferencing:

```
char *str = "apple";// e.g. 0xff0
// both of these add two places to str,
// and then dereference to get the char there.
// E.g. get memory at 0xff2.
                                  // 'p'
char thirdLetter = str[2];
char thirdLetter = *(str + 2);  // 'p'
```

Address	Value
	•••
0xff5	'\0'
0xff4	'e'
0xff3	'1'
0xff2	'p'
0xff1	'p'
0xff0	'a'
	•••

Pointer arithmetic with two pointers does *not* give the byte difference. Instead, it gives the number of places they differ by.



String Behavior #6: Adding an offset to a C string gives us a substring that many places past the first character.

How does the code know how many bytes it should look at once it visits an address?

How does the code know how many bytes it should add when performing pointer arithmetic?

```
int nums[] = \{1, 2, 3\};
// How does it know to add 4 bytes here?
int *intPtr = nums + 1;
char str[6];
strcpy(str, "COMP201");
// How does it know to add 1 byte here?
char *charPtr = str + 1;
```

- At compile time, C can figure out the sizes of different data types, and the sizes of what they point to.
- For this reason, when the program runs, it knows the correct number of bytes to address or add/subtract for each data type.

Array indexing is "syntactic sugar" for pointer arithmetic:

Pointer arithmetic **does not work in bytes**; it works on the type it points to. On **int*** addresses scale by **sizeof(int)**, on **char*** scale by **sizeof(char)**.

• This means too-large/negative subscripts will compile ☺ arr[99]

You can use either syntax on either pointer or array.

Recap

- Pointers and Parameters
- Double Pointers
- Arrays in Memory
- Arrays of Pointers
- Pointer Arithmetic

Next Time: pointer arithmetic, dynamically allocated memory