

BBM406

Fundamentals of Machine Learning

Lecture 2:
Machine Learning by Examples,
Nearest Neighbor Classifier



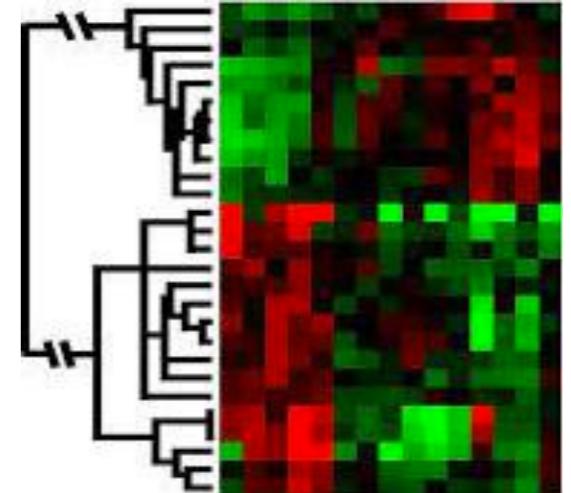
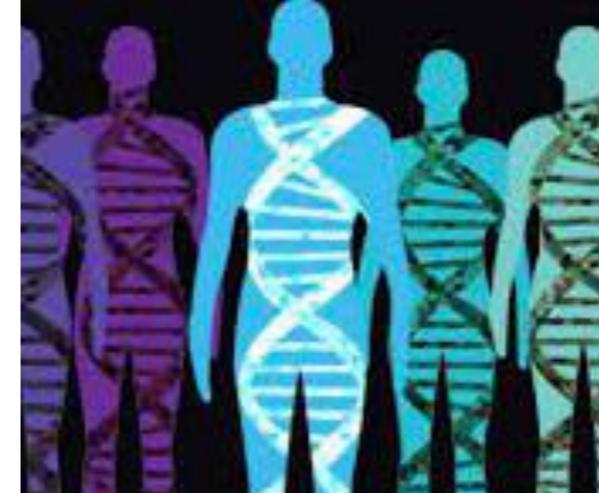
HACETTEPE
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Aykut Erdem // Hacettepe University // Fall 2019

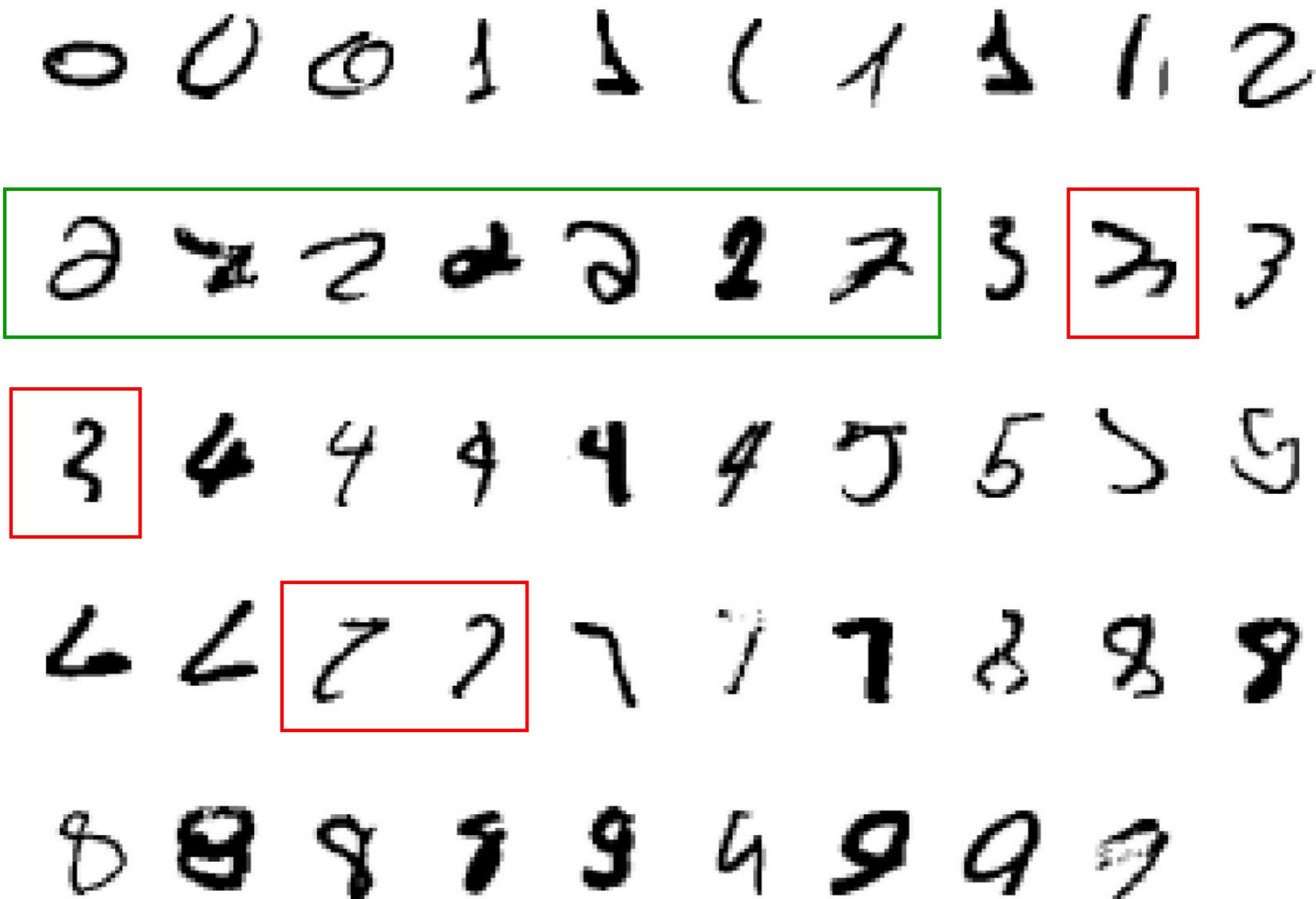
When Do We Use Machine Learning?

ML is used when:

- Human expertise does not exist (navigating on Mars)
- Humans can't explain their expertise (speech recognition)
- Models must be customized (personalized medicine)
- Models are based on huge amounts of data (genomics)



A classic example of a task that requires machine learning: It is very hard to say what makes a 2



Machine Learning (by examples)

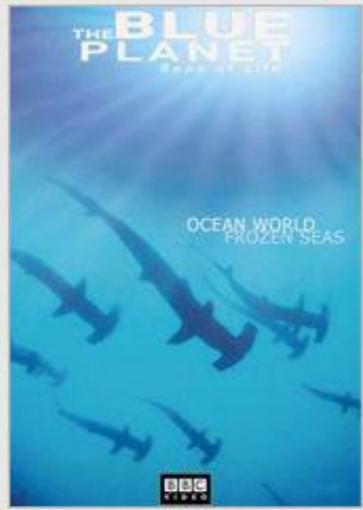
Pose Estimation



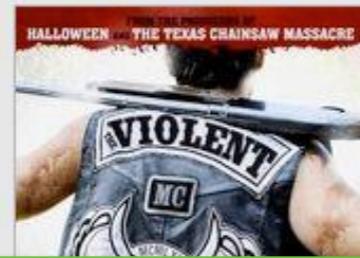
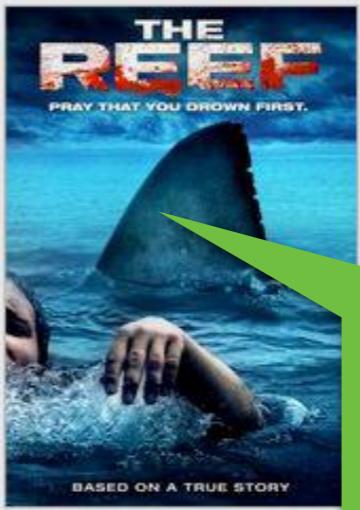
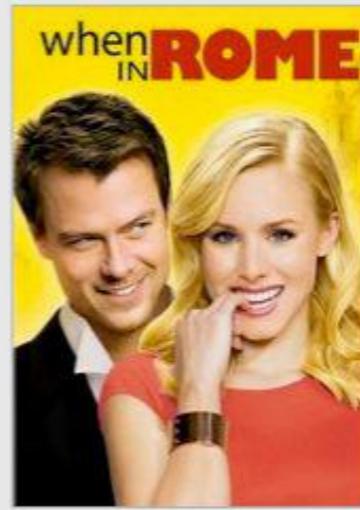
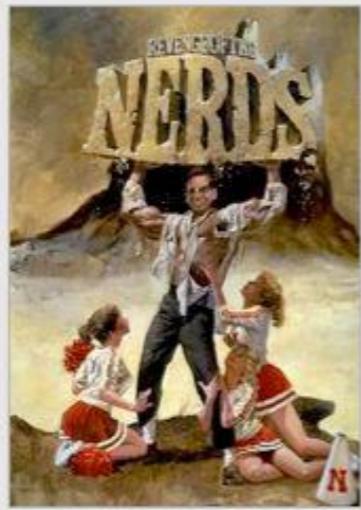
**KINECT
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SEASON TWO**

Collaborative Filtering

Recently Watched

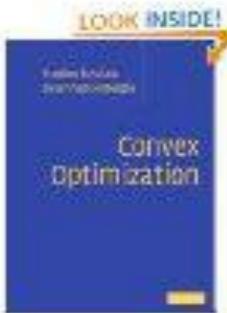


Top 10 for Alexander

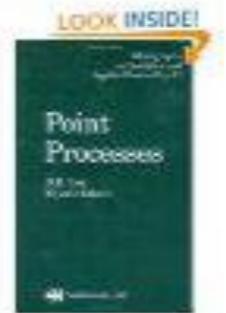


Don't mix preferences on Netflix!

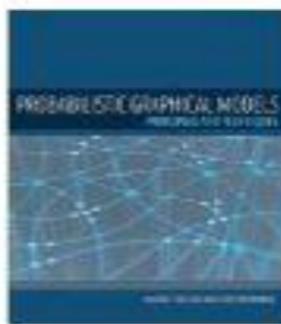
Customers Who Bought This Item Also Bought



[Convex Optimization](#) by
Stephen Boyd
 (11)
\$65.78



[Point Processes](#)
[\(Chapman & Hall / CRC Monographs on Statistics and Applied Probability\)](#) by
D.R. Cox
\$125.47



[Probabilistic Graphical Models: Principles and Techniques](#) by Daphne Koller
 (5)
\$71.52

Amazon books

Collaborative Filtering

BUSINESS
INSIDER

RETAIL

Amazon is being forced to review its website after it reportedly recommended shoppers buy items that can create explosives

Kate Taylor [✉](#) [🐦](#)

⌚ Sep. 20, 2017, 11:51 AM [🔥 6,591](#)

 FACEBOOK

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 TWITTER

 EMAIL

 PRINT

Amazon is doing some self-examination after its website suggested customers purchase potentially dangerous groupings of products.

On Wednesday, Amazon told Reuters it was "reviewing its website" after the UK's Channel 4 News reported that the e-commerce giant's algorithm suggests that shoppers pair certain items with products that can be used to create homemade explosives.

Frequently bought together



+



+



Total price: \$50.87

Add all three to Cart

Add all three to List



This chemical compound's "frequently bought together" suggestions are the necessary ingredients to create a dangerous reaction. [Amazon.com](#)

Should be careful

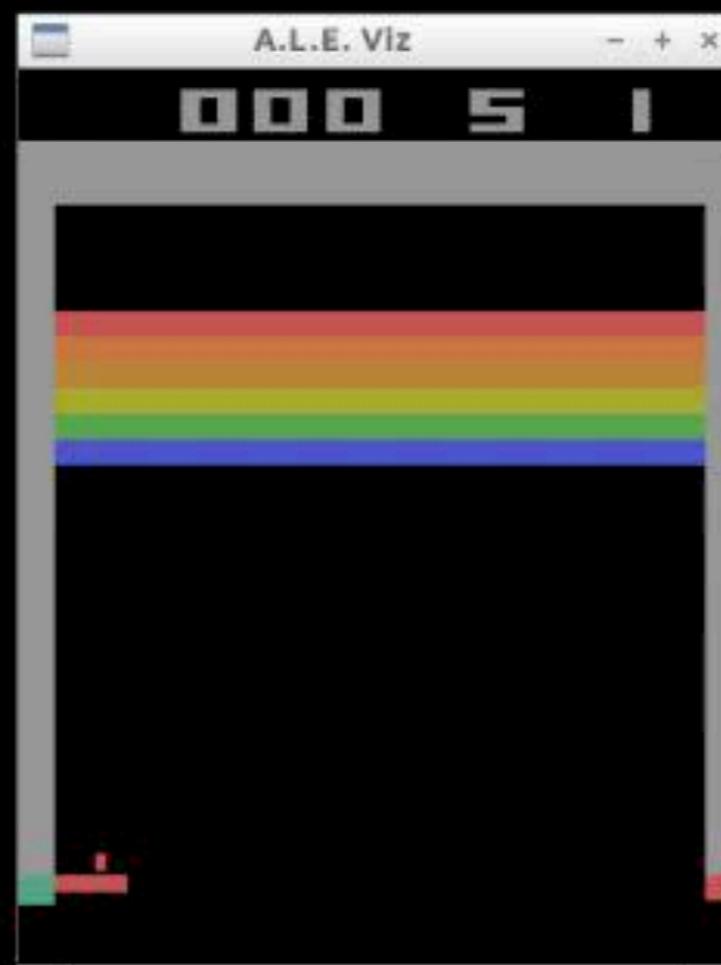
Imitation Learning in Games



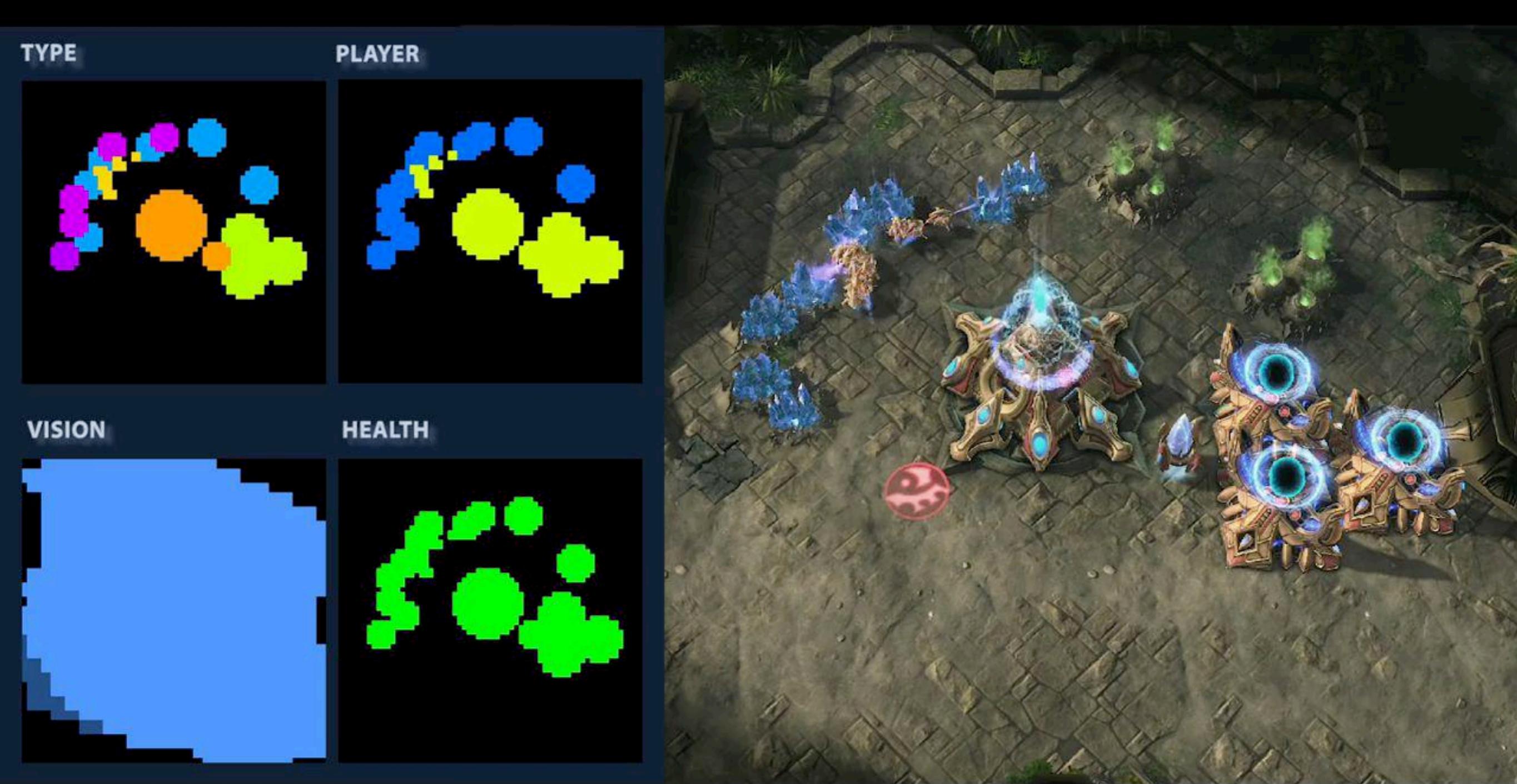
Black & White
Lionsgate Studios

Reinforcement Learning

```
Game will be controlled through named FIFO pipes.  
Size 160-210  
OK  
<type 'str'> 67200  
<type 'numpy.ndarray'> 84  
S: 1 A: 0 R: 0 D: 0  
Start  
  
action: 1  
S: 2 A: 1 R: 1 D: 0 Reward 0  
_____  
action: 1  
S: 3 A: 2 R: 2 D: 0 Reward 0  
_____  
action: 1  
S: 4 A: 3 R: 3 D: 0 Reward 0  
_____  
action NEURALNET: 3  
S: 5 A: 4 R: 4 D: 1 Reward 0  
_____  
action NEURALNET: 3  
S: 6 A: 5 R: 5 D: 2 Reward 0  
_____  
action NEURALNET: 6  
S: 7 A: 6 R: 6 D: 3 Reward 0  
_____  
action NEURALNET: 3  
S: 8 A: 7 R: 7 D: 4 Reward 0  
_____  
action NEURALNET: 6  
S: 9 A: 8 R: 8 D: 5 Reward 0  
_____  
action NEURALNET: 3
```



Reinforcement Learning



<https://www.youtube.com/watch?v=5iZlrBqDYPM>

Spam Filtering

+Alex Search Images Maps Play YouTube News Gmail Drive Calendar More ▾

Google Alex Smola 0 + Share

Gmail ▾ More ▾ ham 1–50 of 15,803

COMPOSE

<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Southwest Airlines
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	DiscountMags.com
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	support, Alex (3)
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	American Airlines AAdvan.
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Taesup, Alex, Taesup (3)

Your trip is around the corner! - You're all set for your San Jose trip! My Account | View My Itinerary Online 2:12 pm
\$3.99 Business & Finance Sale.. starts now! - Trouble Seeing This Email? View as Webpage STOP these e-nr 12:03 pm
Your order has shipped... - please send to the address below for an exchange remotesremotes.com(exchange) 7:22 am
AAdvantage eSummary - January 2013 - VIEW IN WEB BROWSER >> http://americanairlines.ed10.net/r/JC 1:17 am
Happy new year! - Hi Alex, Thanks for your condolence. I will arrive at Berkeley on 16th (wed) night. So, I car Jan 11

+Alex Search Images Maps Play YouTube News Gmail Drive Calendar More ▾

Google Alex Smola 0 + Share

Gmail ▾ More ▾ spam 1–50 of 244

COMPOSE

Delete all spam messages now (messages that have been in Spam more than 30 days will be automatically deleted)

<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	maee
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Dear Valued Customers,
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	garjeti
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Steven Cooke
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	paper18
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	First-Class Mail Service
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	garjeti
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Candy.Li
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Ronan Morgan
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	RE/MAX®
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	newsletter
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	CJCR editor
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	garjeti (2)
<input type="checkbox"/>	<input type="star"/>	<input type="more"/>	Wayne Smith

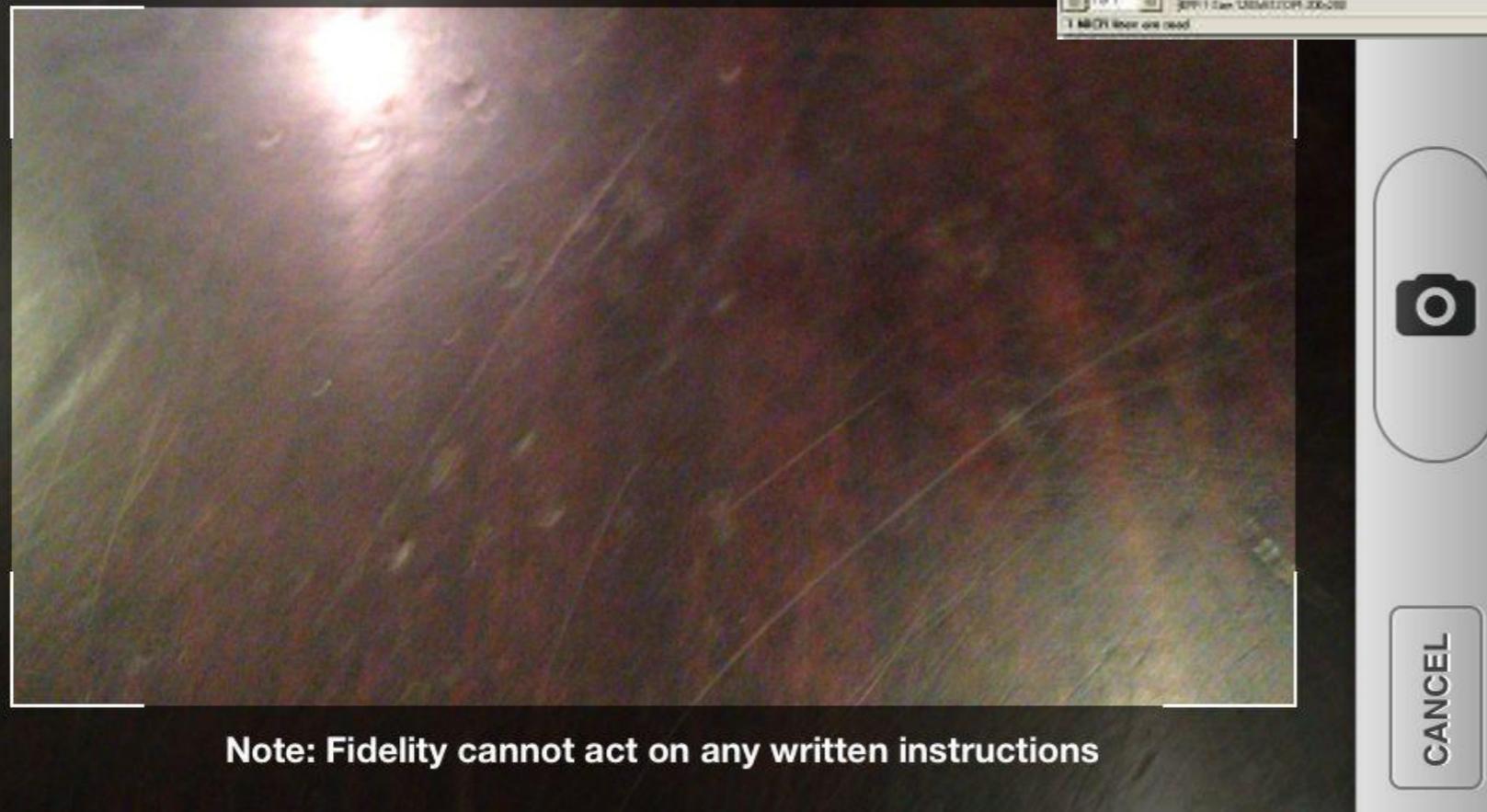
(Ei&ISTP Index)2013机械与自动化工程国际会议征文: [alex.smola@gmail.com] - 尊敬的老师, 您好 : 机械与 Jan 11
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Wayne Smith has sent you a message - Linked In Wayne Smith just sent you a message Date: 1/09/2013 ht Jan 9

Cheque Reading

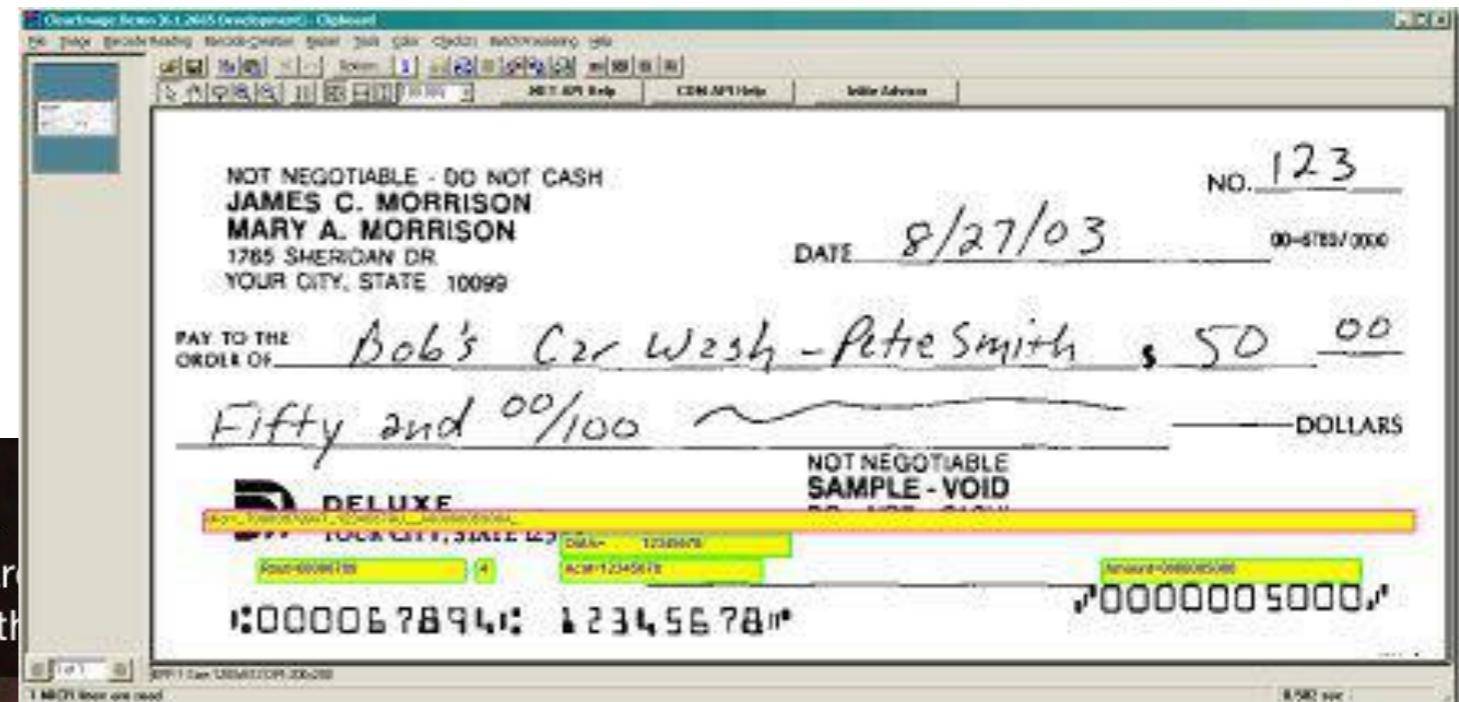
segment image

Photograph Front of Check

Place the check on a dark background in a well-lit area. Hold the camera steady and align the check's edges with the frame.

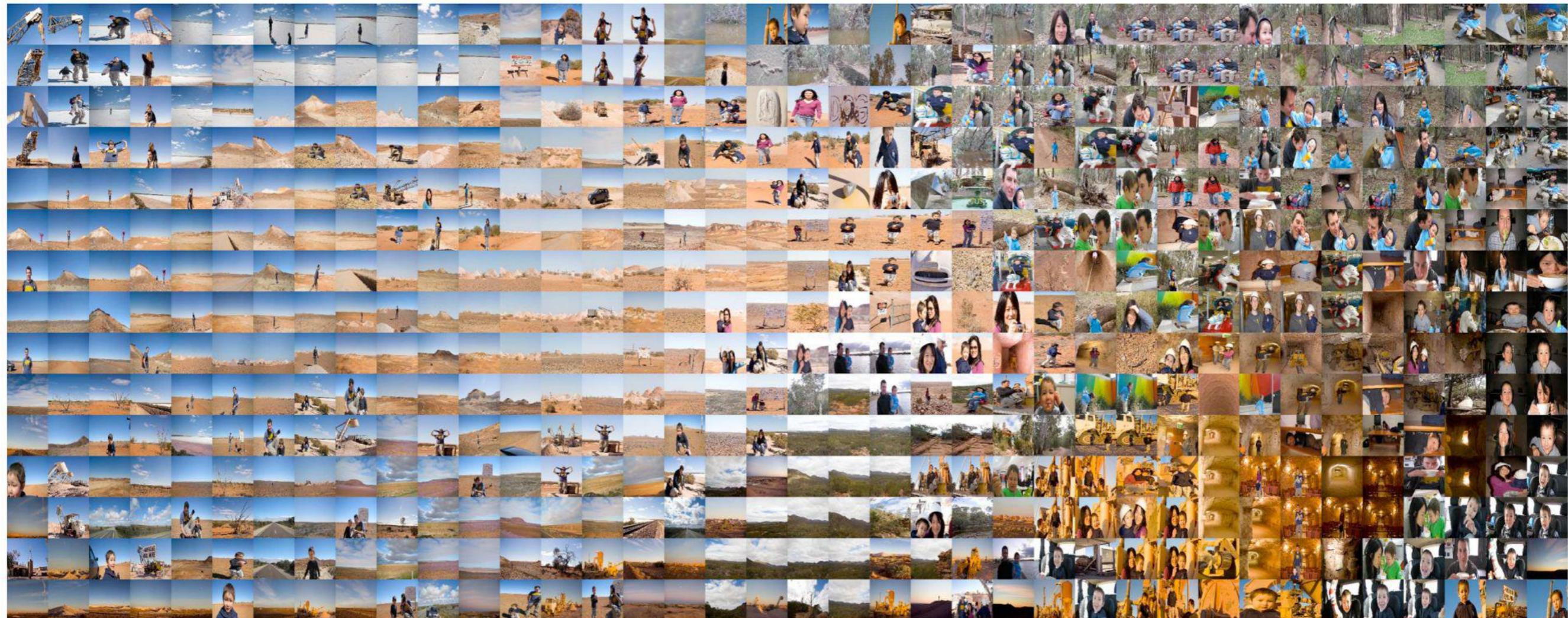


Note: Fidelity cannot act on any written instructions



recognize
handwriting

Image Layout



- Raw set of images from several cameras
- Joint layout based on image similarity

Search Ads

Google mesothelioma Alex

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About 10,600,000 results (0.25 seconds)

Ads related to mesothelioma [i](#)

Mesothelioma Symptoms - Lung cancer from Asbestos.
www.mesothelioma-lung-cancer.org/
It can take 20-30 years to develop
What Is It? Symptoms
Portal Entrance Treatments

Mesothelioma Symptoms - 101 Facts about Mesothelioma.
www.mesothelioma-answer.org/
By Anna Kaplan, M.D.
Free Mesothelioma Book - Nutrition Book - Free Mesothelioma DVDs - Asbestos

Mesothelioma Diagnosis? - Get the money you deserve fast
www.mesotheliomaclaimscenter.info/
File with **Mesothelioma** Claim Center
Mesothelioma Compensation Amounts - File a Mesothelioma Claim

Mesothelioma - Wikipedia, the free encyclopedia
en.wikipedia.org/wiki/Mesothelioma
Mesothelioma (or, more precisely, malignant **mesothelioma**) is a rare form of cancer that develops from transformed cells originating in the mesothelium, the ...
Signs and symptoms - Cause - Diagnosis - Screening

Mesothelioma Cancer Alliance | The Authority on Asbestos Cancer
www.mesothelioma.com/
Mesothelioma treatment, diagnosis and related information for patients and families.
Legal options for those diagnosed with malignant **mesothelioma**.

Ads [i](#)

Mesothelioma compensation
www.simmonsfirm.com/888-360-4189
Free Consultation with Lawyers that Focus on **Mesothelioma** Cases.

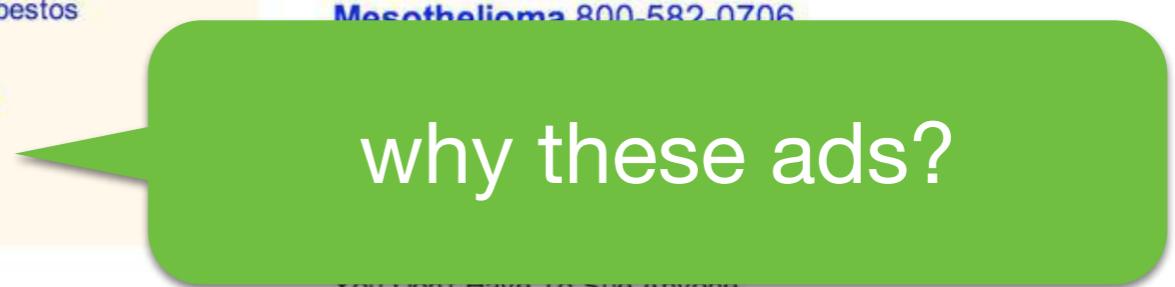
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Mesothelioma 800-582-0706

You Don't Have To Sue Anyone.
\$30 Billion Asbestos Trust Fund

Mesothelioma & Asbestos
www.navy-veterans-mesothelioma.org/
Important info for Navy Vets.
Learn About **Mesothelioma** Claims

Asbestos Exposure?
www.mesotheliomalawfirm.com/
Mesothelioma victims are entitled



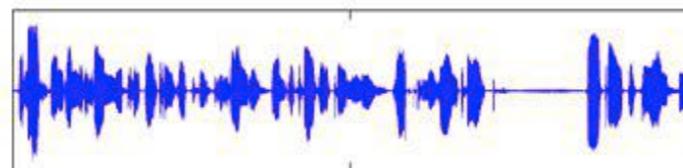
Self-Driving Cars



Image: <https://medium.com/waymo/simulation-how-one-flashing-yellow-light-turns-into-thousands-of-hours-of-experience-a7a1cb475565>

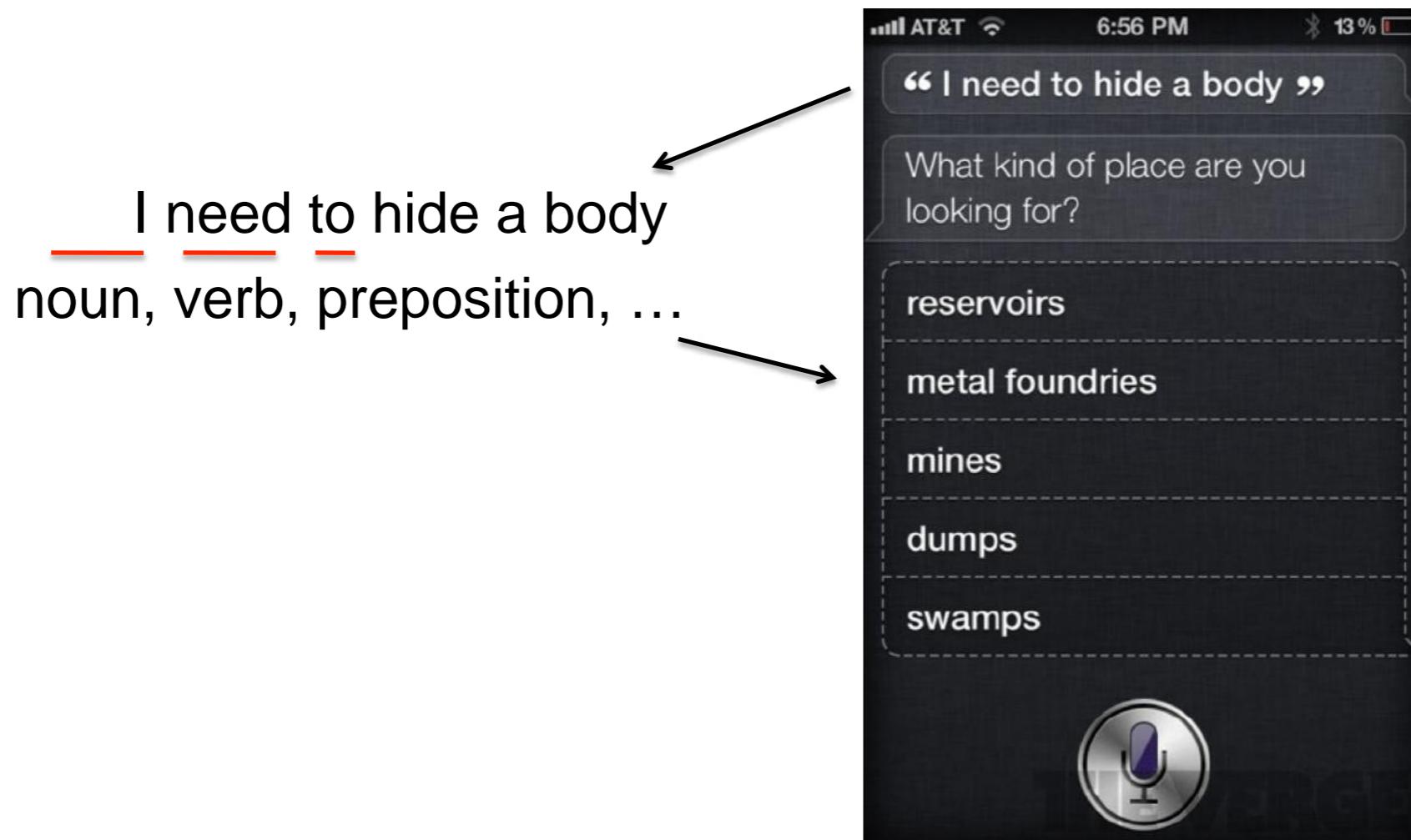
Speech Recognition

Given an audio waveform, robustly extract & recognize any spoken words

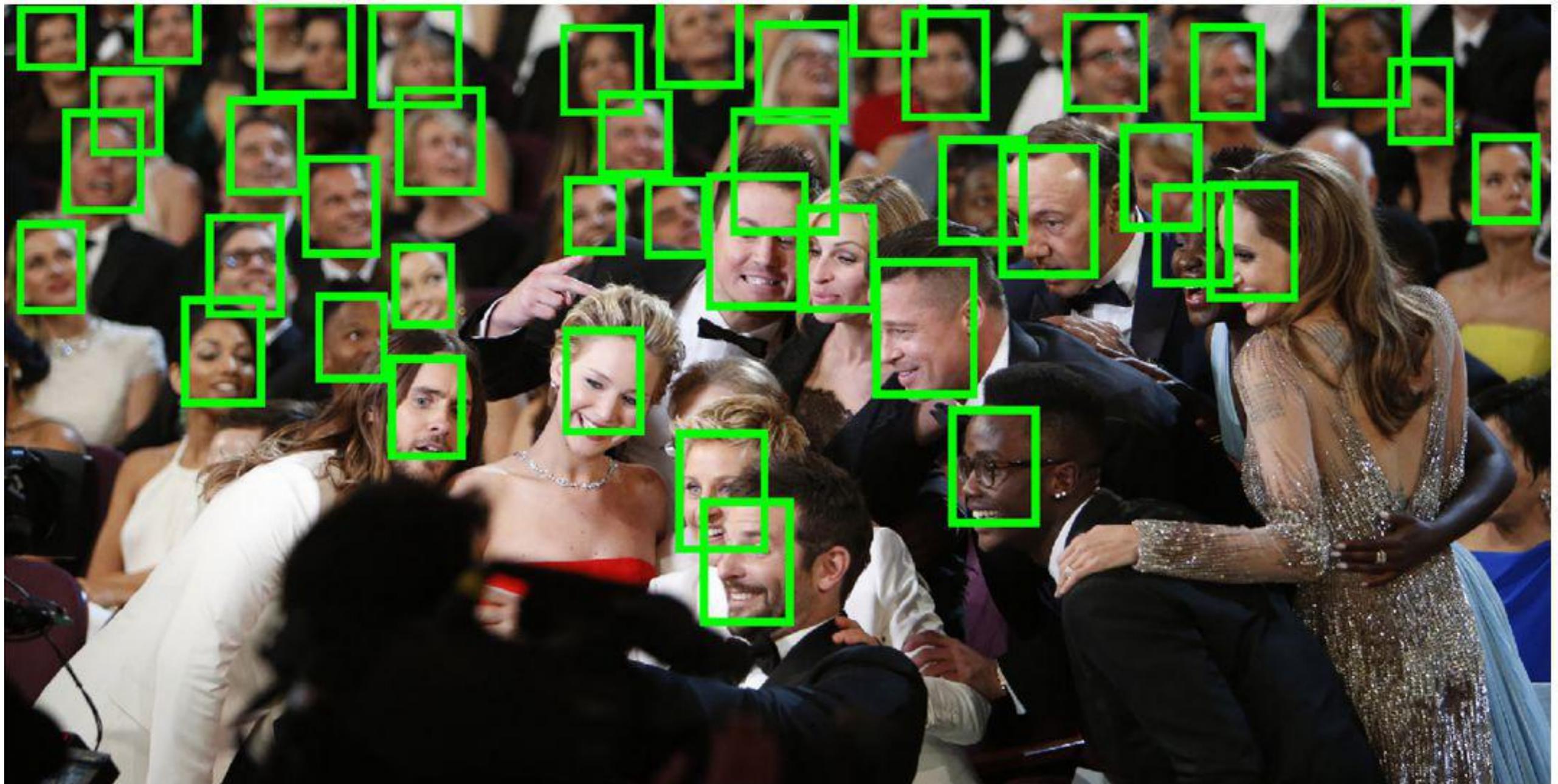


- Statistical models can be used to
 - Provide greater robustness to noise
 - Adapt to accent of different speakers
 - Learn from training

Natural Language Processing



Face Detection

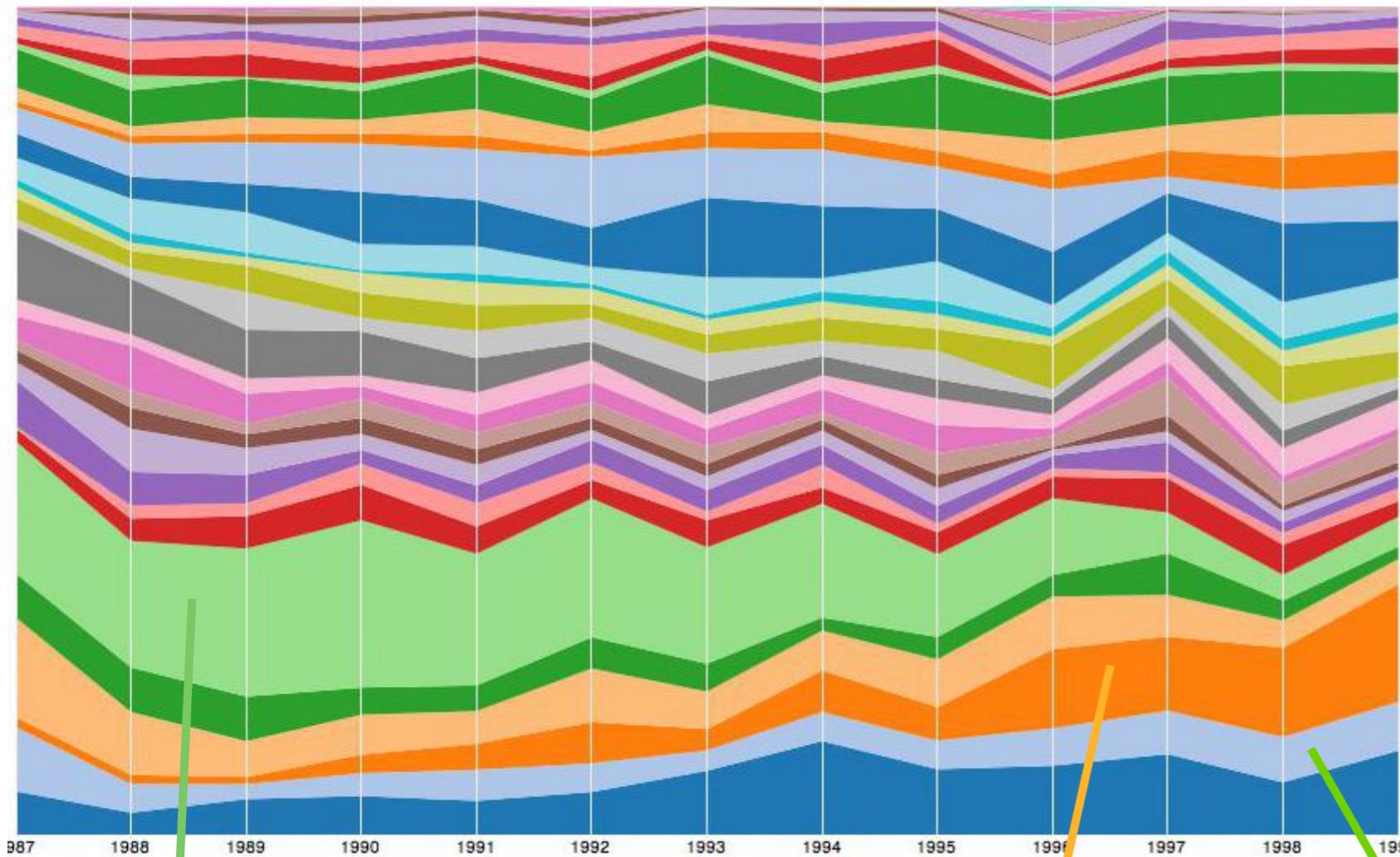


Scene Labeling via Deep Learning



[Farabet et al. ICML 2012, PAMI 2013]

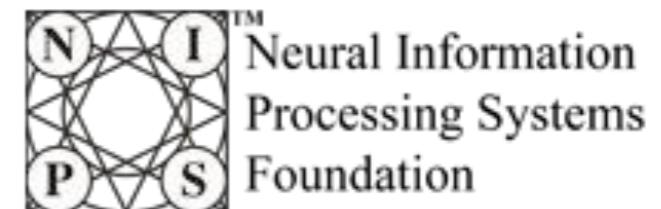
Topic Models of Text Documents



slide by Eric Sudderth
weight neural figure inputs error unit
input layer network units
weights training learning net hidden
architecture set networks output number

estimation density approach em
data model
probability mixture gaussian posterior bayesian distribution
parameters models
log likelihood prior

cell responses motion
field **cells**
receptive input model stimulus response
neurons direction orientation stimuli
spatial cortex cortical figure

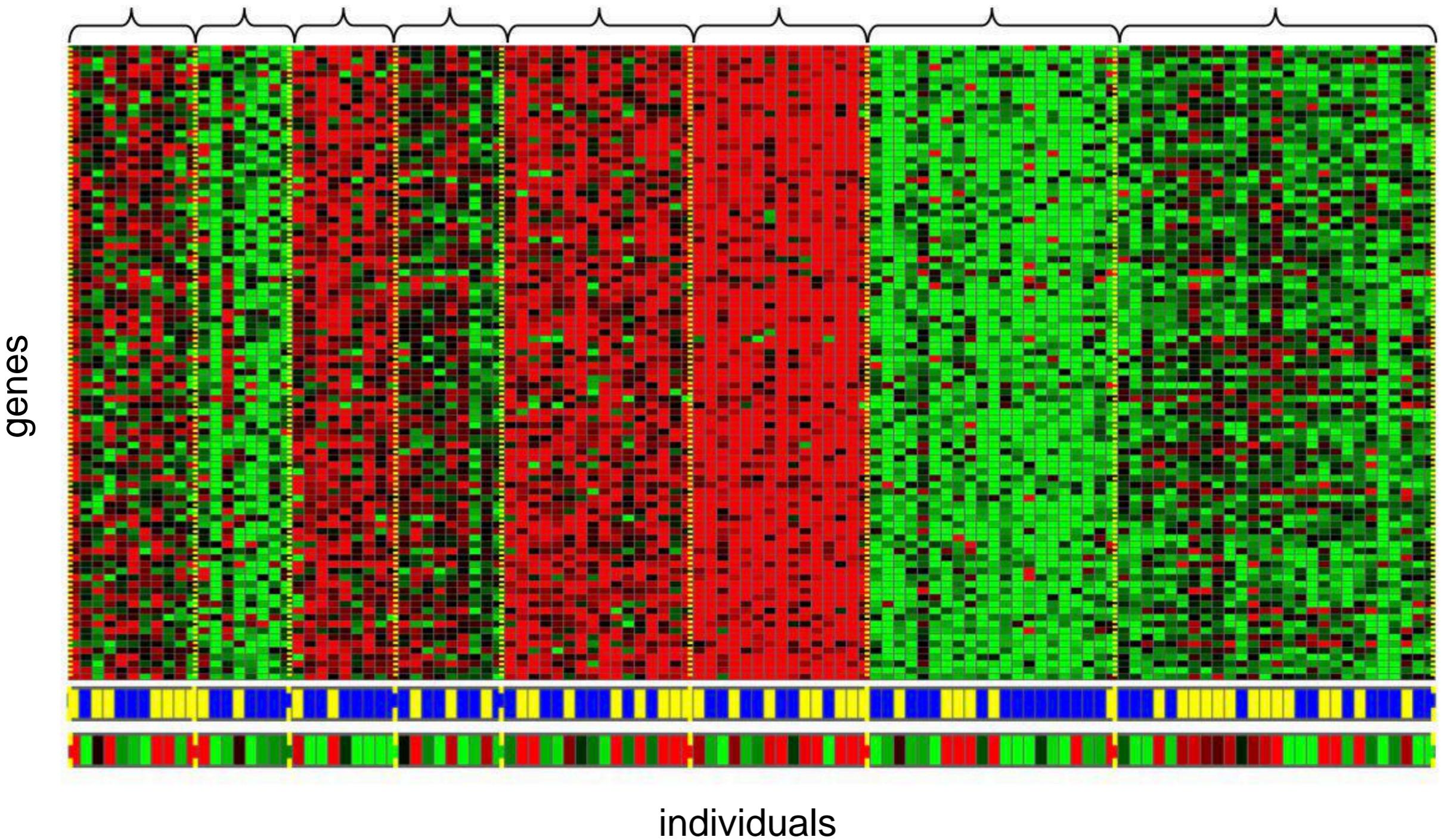


The
New York
Times

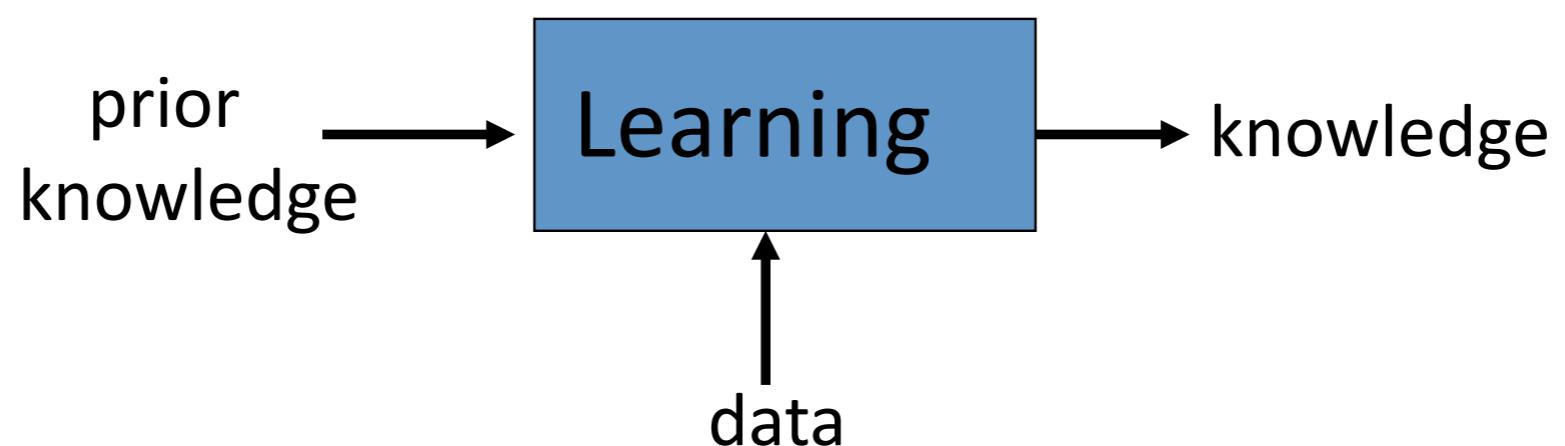


WIKIPEDIA
The Free Encyclopedia

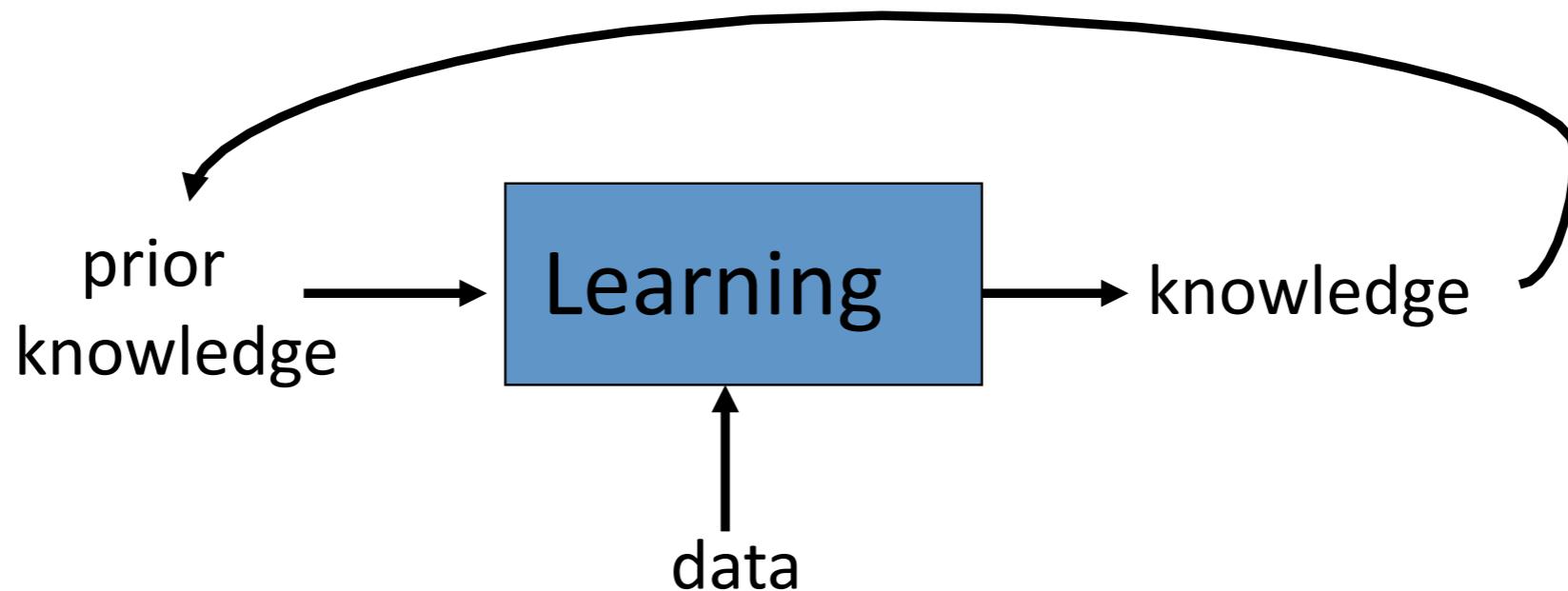
Genomics: group individuals by genetic similarity



Learning - revisited



Learning - revisited



Programming with Data

- Want adaptive robust and fault tolerant systems
- Rule-based implementation is (often)
 - difficult (for the programmer)
 - brittle (can miss many edge-cases)
 - becomes a nightmare to maintain explicitly
 - often doesn't work too well (e.g. OCR)
- Usually easy to obtain examples of what we want
IF x THEN DO y
- Collect many pairs (x_i, y_i)
- Estimate function f such that $f(x_i) = y_i$ (supervised learning)
- Detect patterns in data (unsupervised learning)

Objectives of Machine Learning

- **Algorithms:** design of efficient, accurate, and general learning algorithms to
 - deal with large-scale problems.
 - make accurate predictions (unseen examples).
 - handle a variety of different learning problems.
- **Theoretical questions:**
 - what can be learned? Under what conditions?
 - what learning guarantees can be given?
 - what is the algorithmic complexity?

Definitions and Terminology

- **Example:** an object, instance of the data used.
- **Features:** the set of attributes, often represented as a vector, associated to an example (e.g., height and weight for gender prediction).
- **Labels:** in classification, category associated to an object (e.g., positive or negative in binary classification); in regression real value.
- **Training data:** data used for training learning algorithm (often labeled data).

Definitions and Terminology (cont'd.)

- **Test data:** data used for testing learning algorithm (unlabeled data).
- **Unsupervised learning:** no labeled data.
- **Supervised learning:** uses labeled data.
- **Weakly or semi-supervised learning:** intermediate scenarios.
- **Reinforcement learning:** rewards from sequence of action.

Supervised Learning

Supervised Learning

- **Binary classification**

Given x find y in $\{-1, 1\}$

- **Multicategory classification**

Given x find y in $\{1, \dots, k\}$

often with loss

$$l(y, f(x))$$

- **Regression**

Given x find y in R (or R^d)

- **Sequence annotation**

Given sequence $x_1 \dots x_l$ find $y_1 \dots y_l$

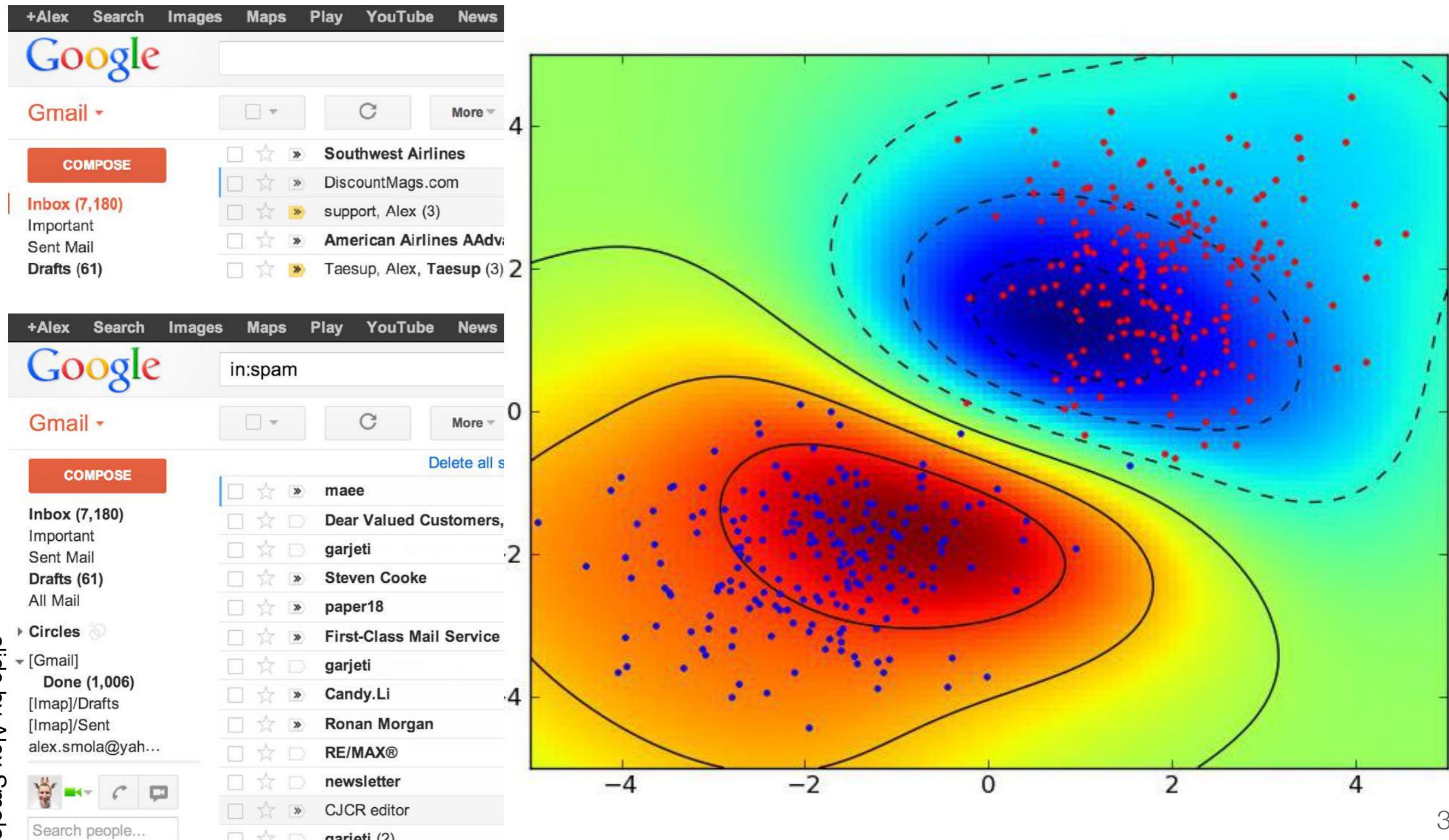
- **Hierarchical Categorization (Ontology)**

Given x find a point in the hierarchy of y (e.g. a tree)

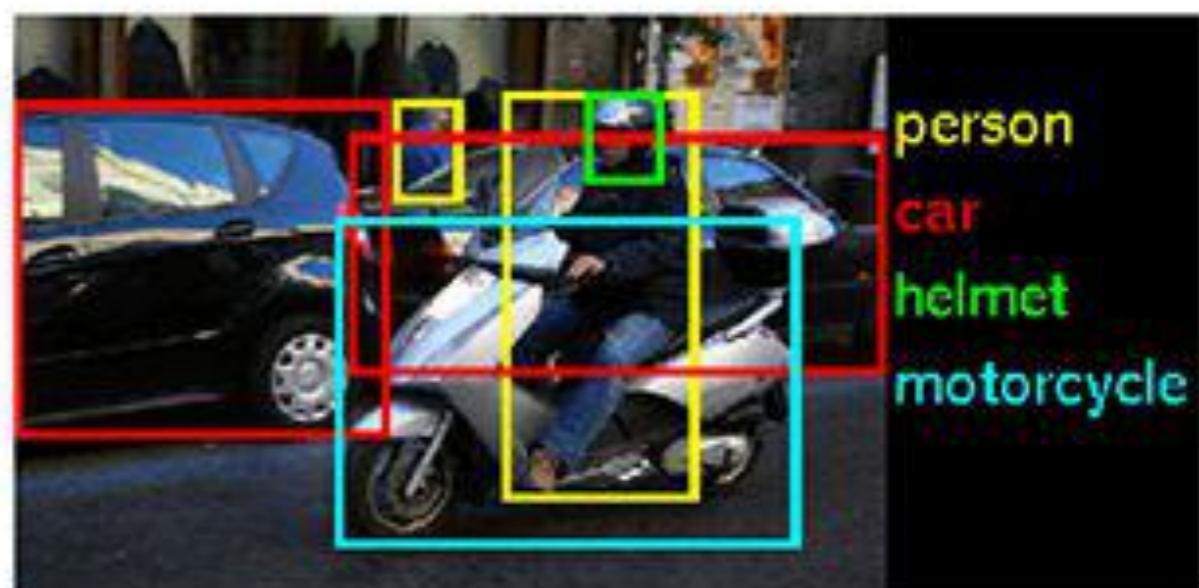
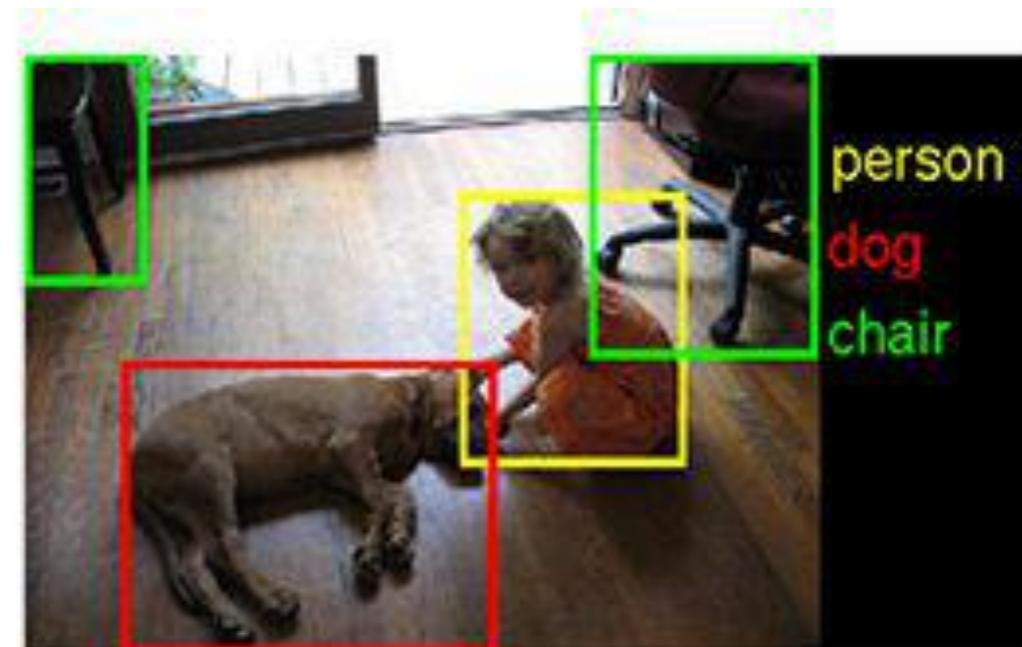
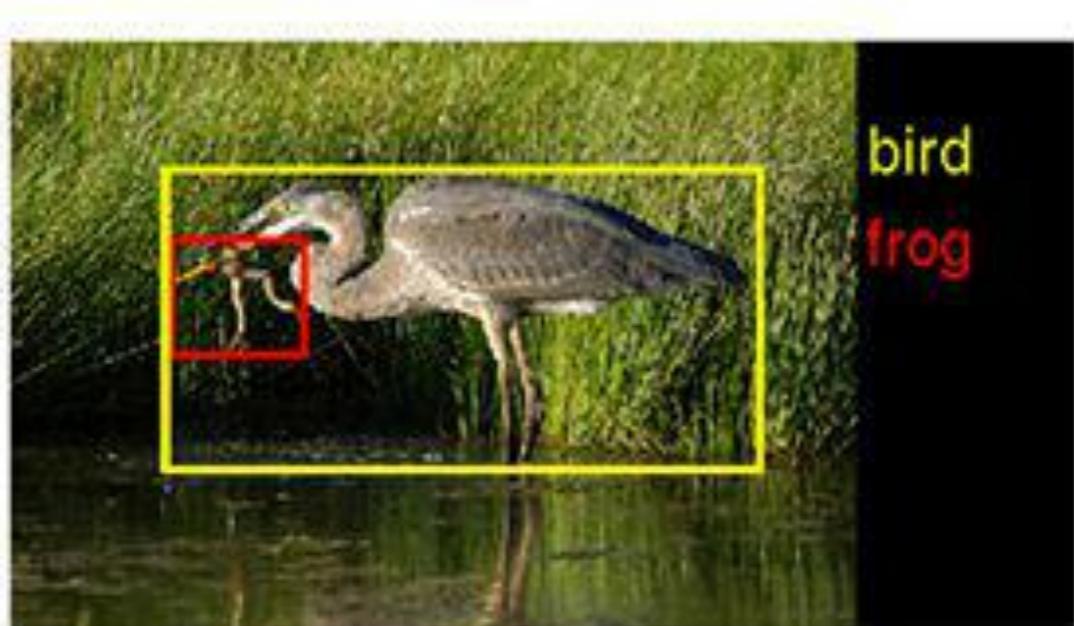
- **Prediction**

Given x_t and $y_{t-1} \dots y_1$ find y_t

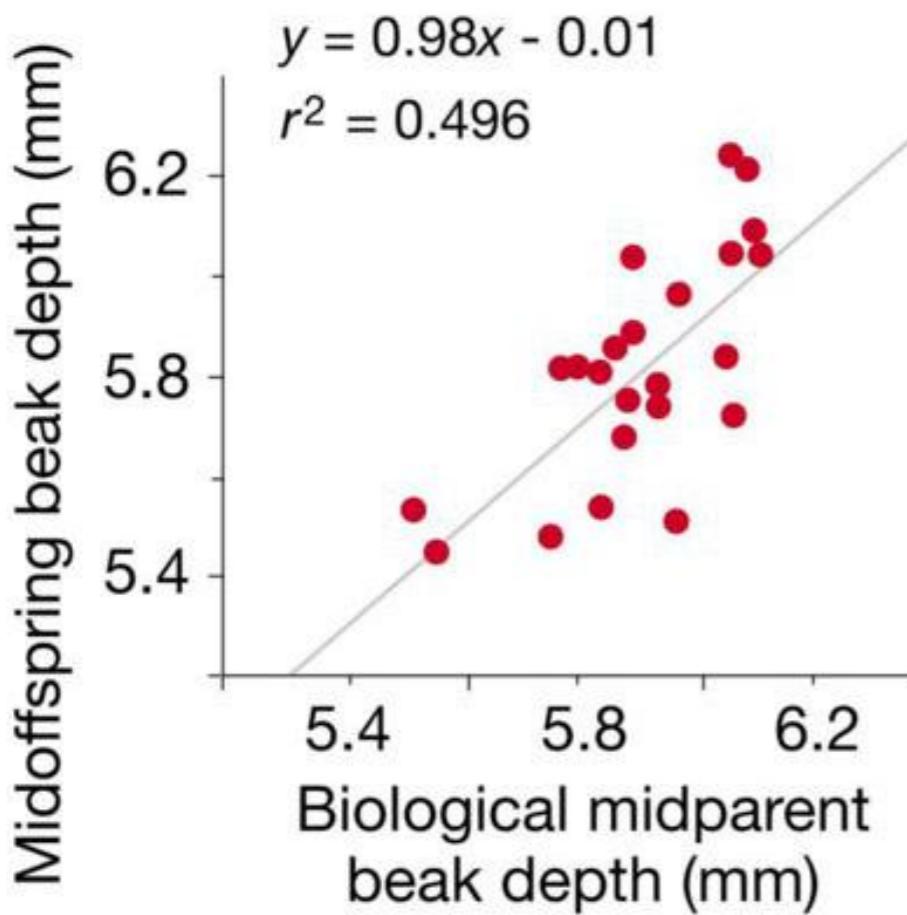
Binary Classification



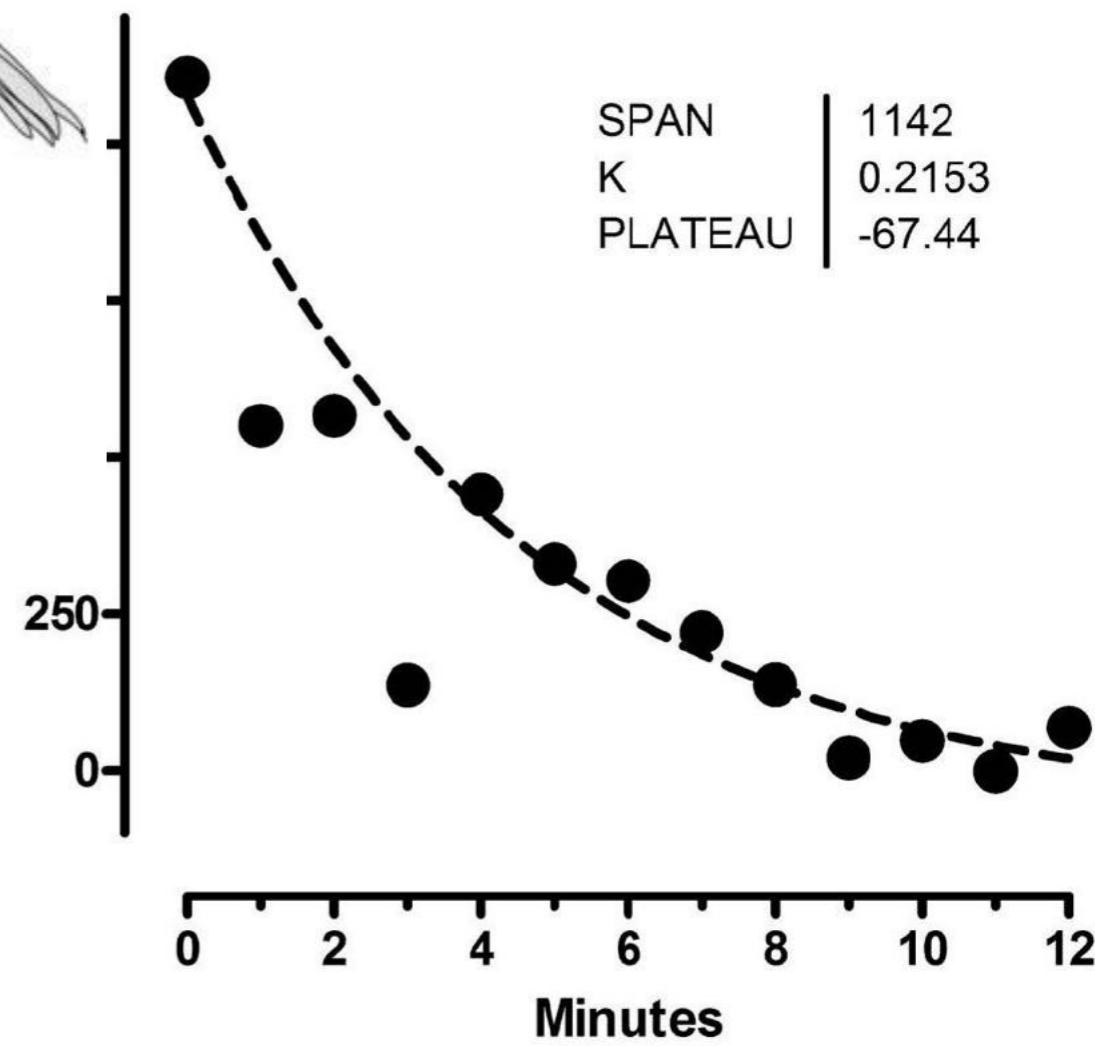
Multiclass Classification + Annotation



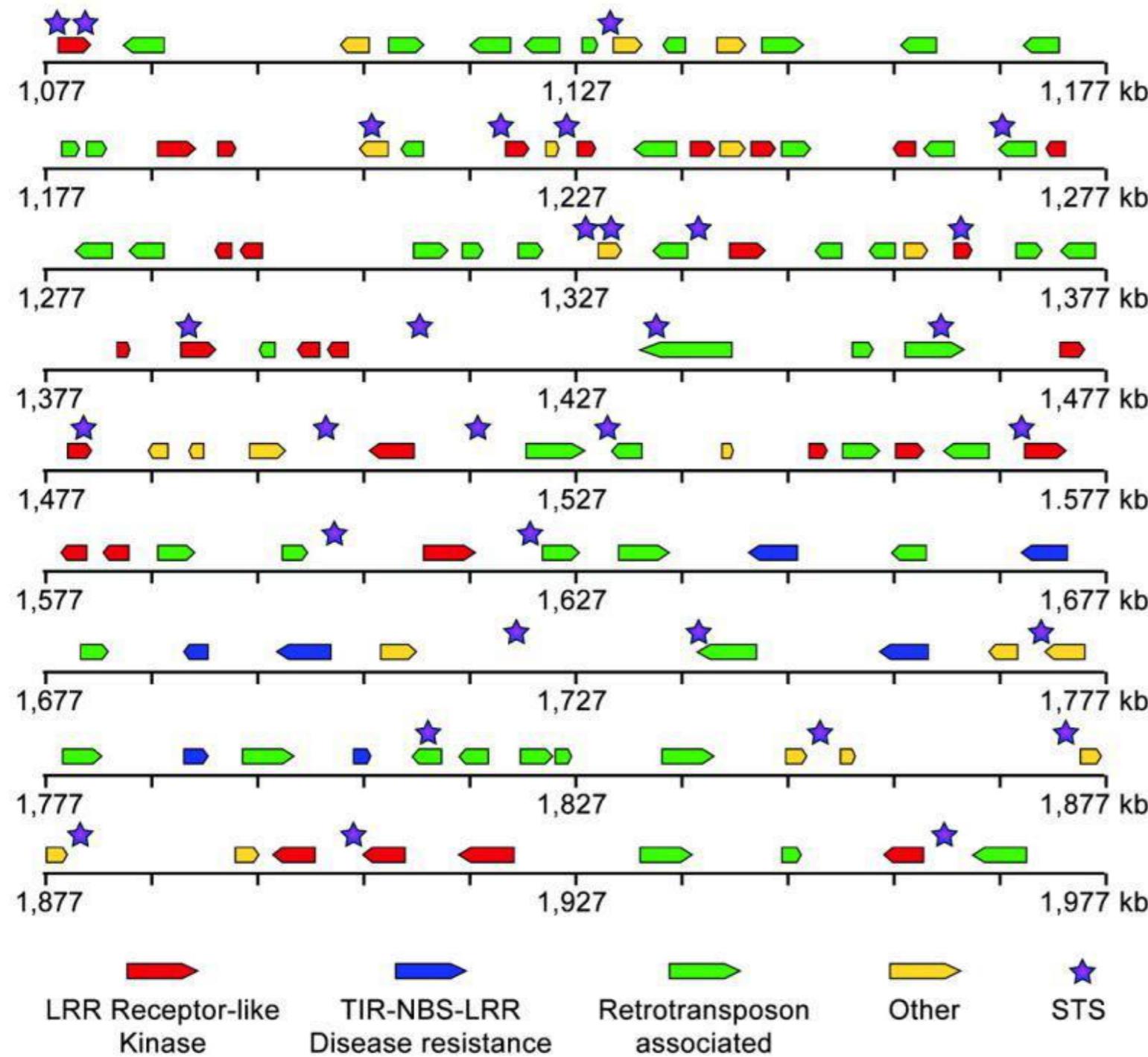
Regression



nonlinear



Sequence Annotation



given sequence

gene finding
speech recognition
activity segmentation
named entities

Ontology

dmoz open directory project In partnership with **Aol Search.**

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webpages

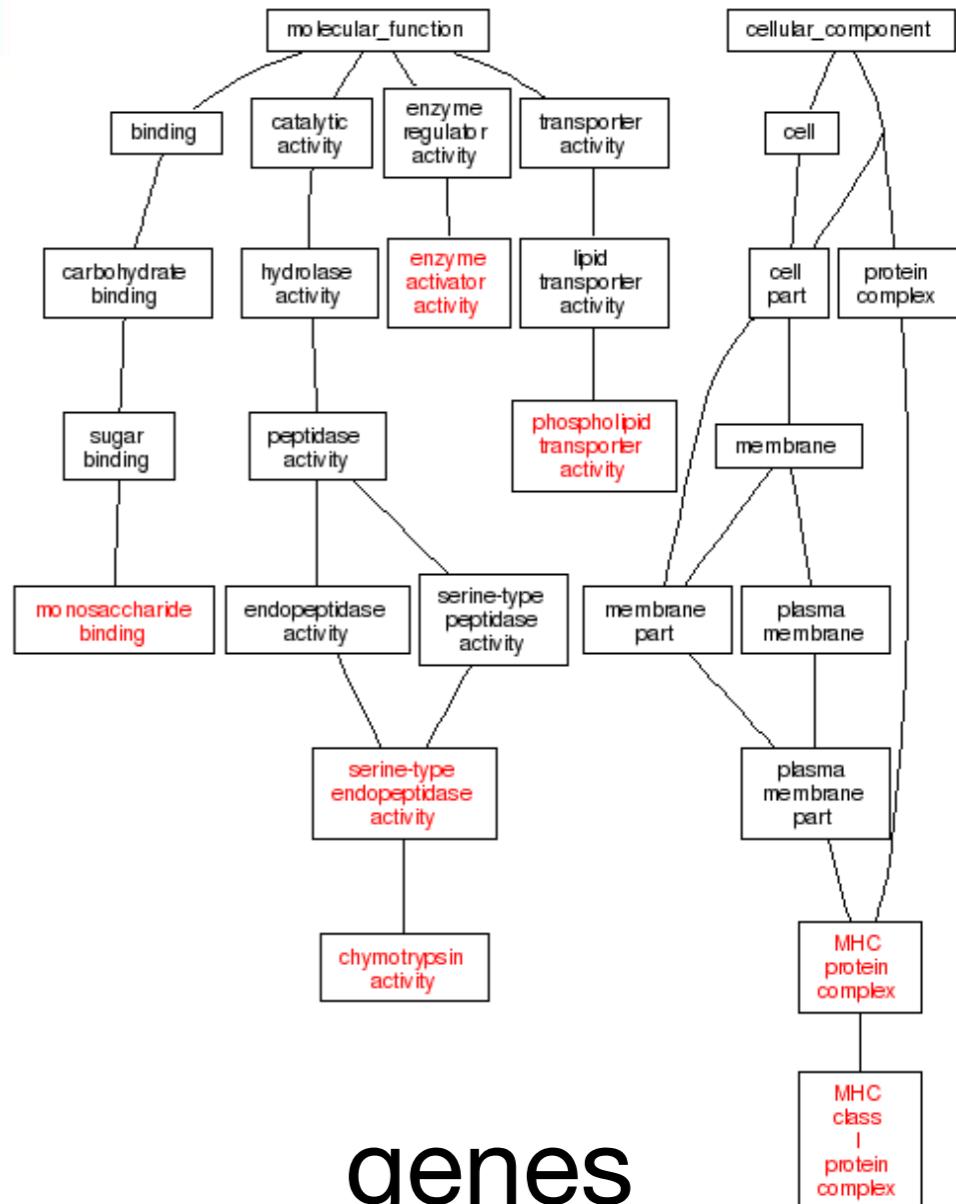
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5,114,083 sites - 96,877 editors - over 1,014,849 categories



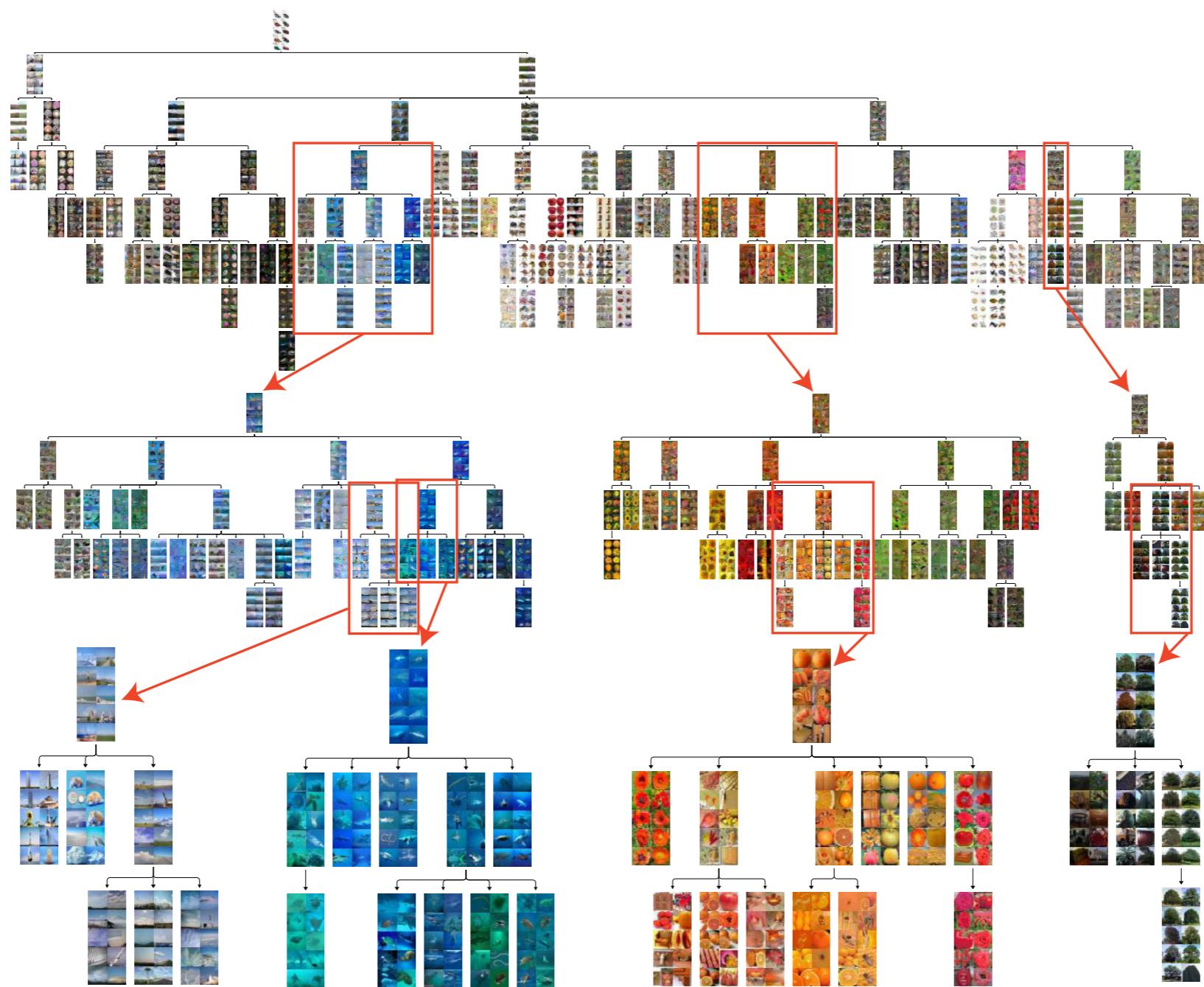
genes

Prediction



tomorrow's stock price

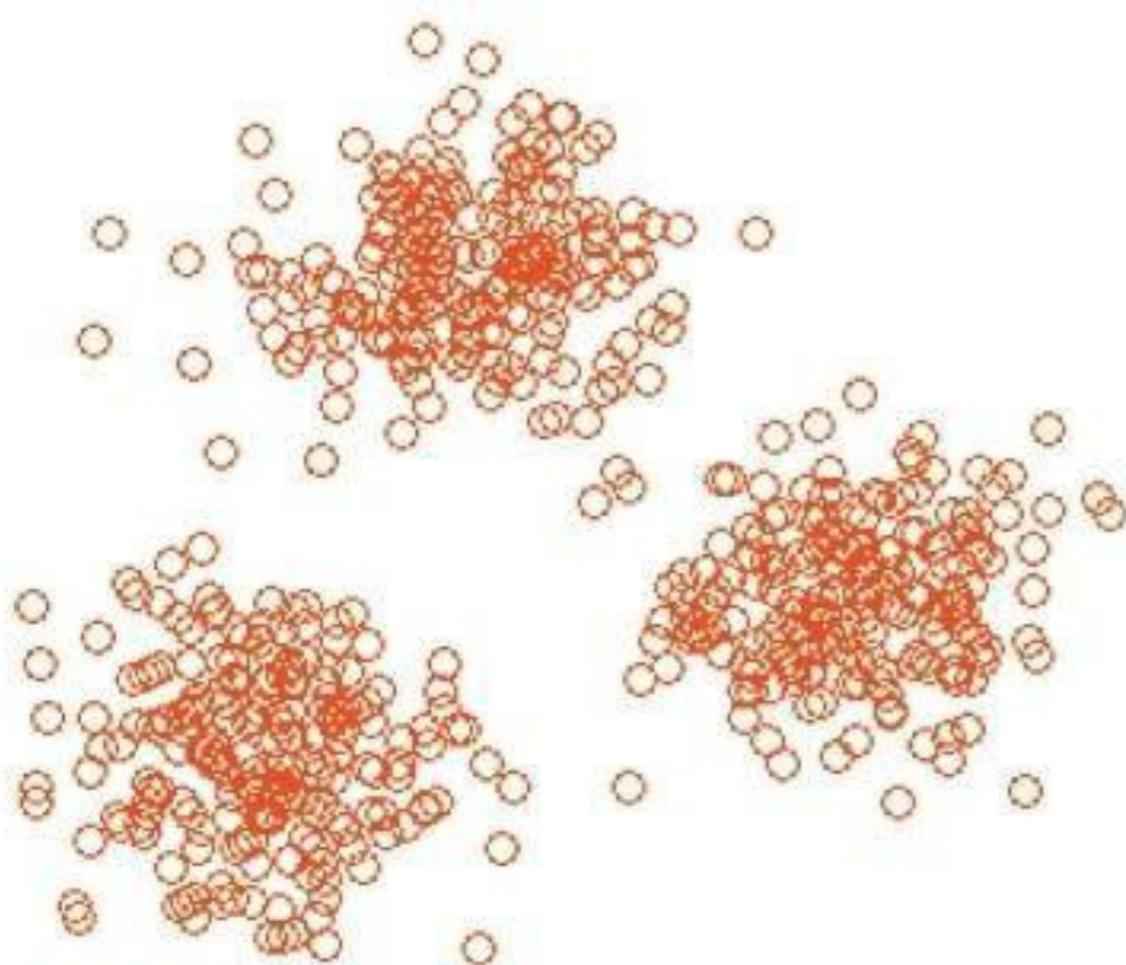
Unsupervised Learning



Unsupervised Learning

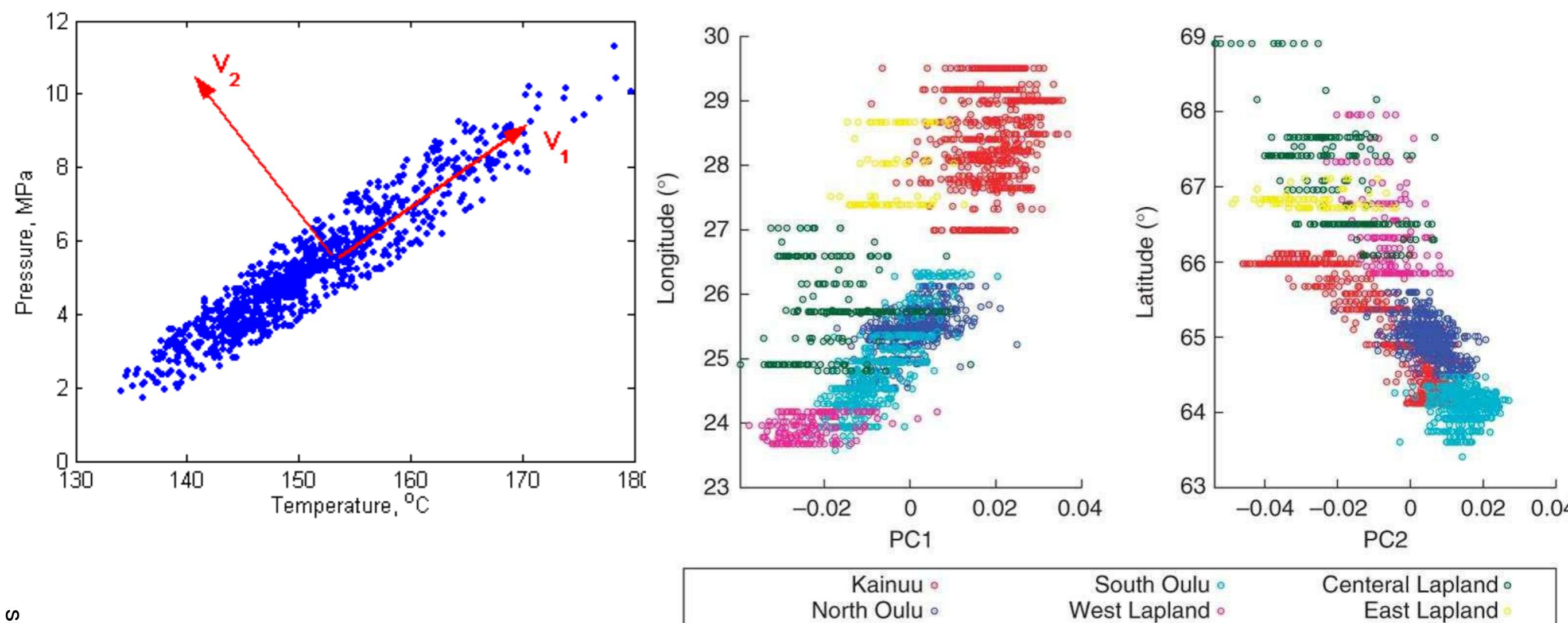
- Given data x , ask a good question ... about x or about model for x
- **Clustering**
Find a set of prototypes representing the data
- **Principal Components**
Find a subspace representing the data
- **Sequence Analysis**
Find a latent causal sequence for observations
 - Sequence Segmentation
 - Hidden Markov Model (discrete state)
 - Kalman Filter (continuous state)
- **Hierarchical representations**
- **Independent components / dictionary learning**
Find (small) set of factors for observation
- **Novelty detection**
Find the odd one out

Clustering



- Documents
- Users
- Webpages
- Diseases
- Pictures
- Vehicles
- ...

Principal Components

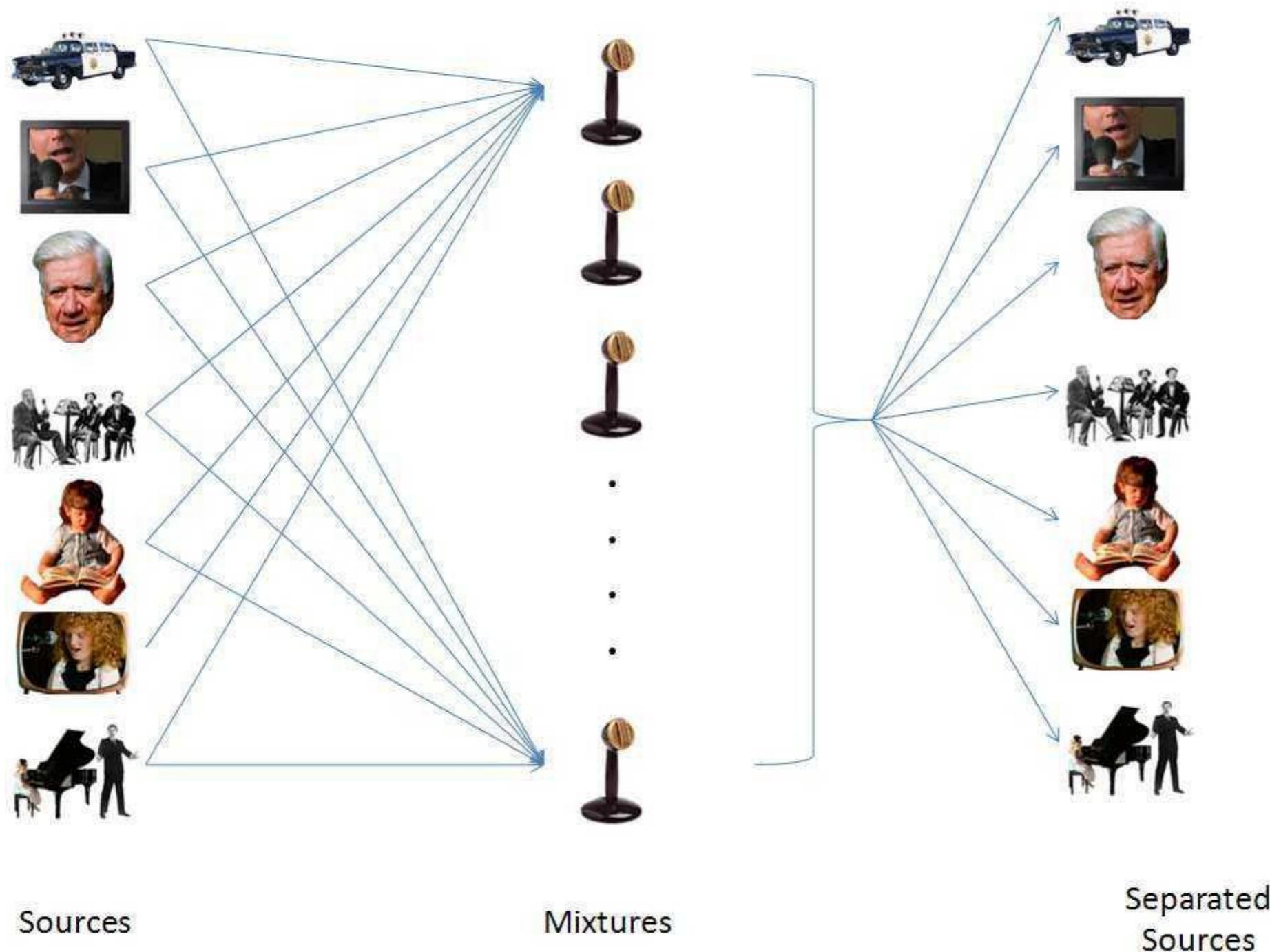


Variance component model to account for sample structure in genome-wide association studies, Nature Genetics 2010

Hierarchical Grouping

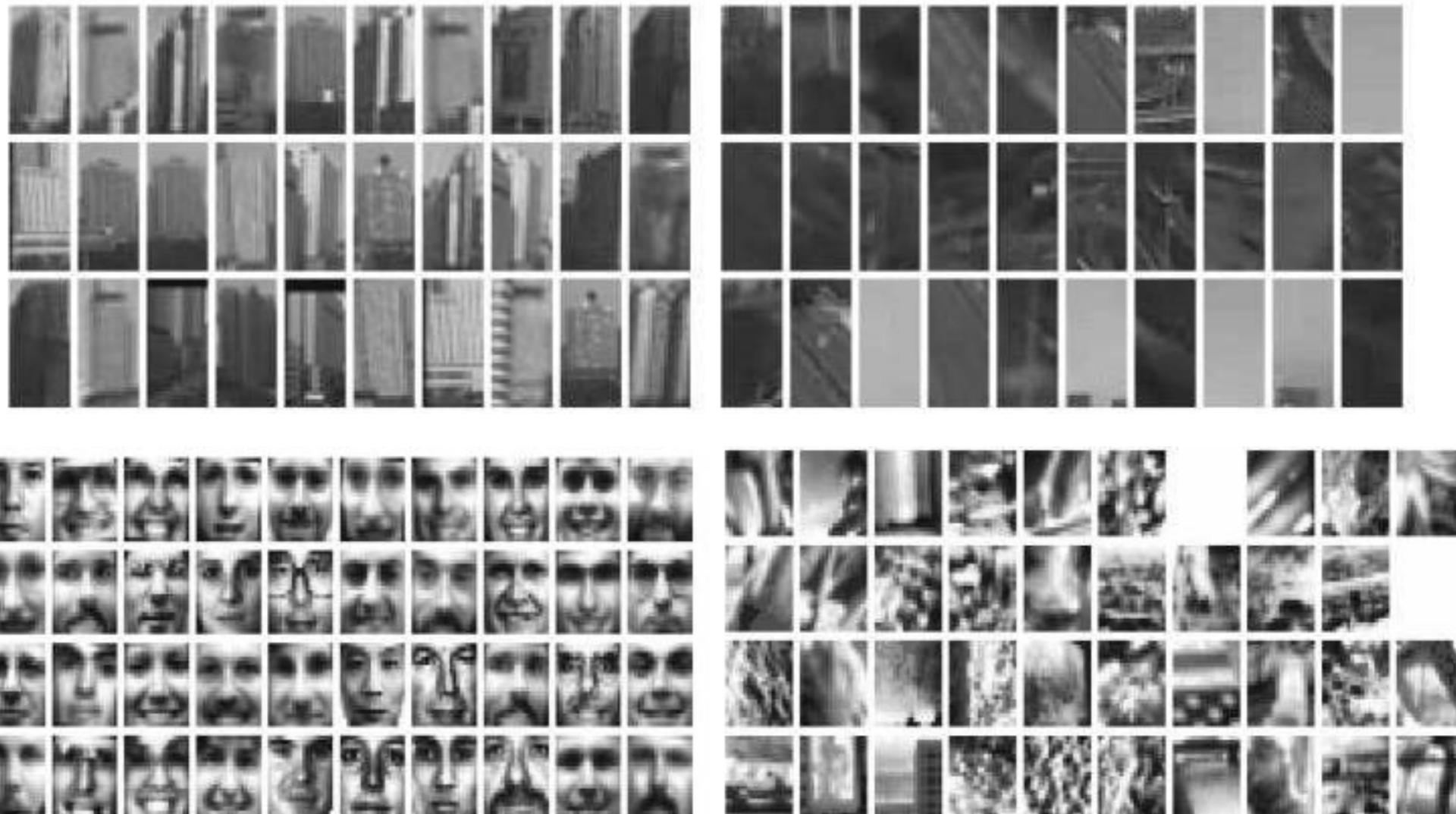


Independent Components



find them
automatically

Novelty detection



typical

atypical

Important challenges in ML

- How important is the actual learning algorithm and its tuning
- Simple versus complex algorithm
- Overfitting
- Model Selection
- Regularization

Your 1st Classifier: Nearest Neighbor Classifier

Concept Learning

- **Definition:** Acquire an operational definition of a general category of objects given *positive* and *negative* training examples.
- Also called *binary classification*, *binary supervised learning*

Concept Learning Example

	correct (complete, partial, guessing)	color (yes, no)	original (yes, no)	presentation (clear, unclear, cryptic)	binder (yes, no)	A+
1	complete	yes	yes	clear	no	yes
2	complete	no	yes	clear	no	yes
3	partial	yes	no	unclear	no	no
4	complete	yes	yes	clear	yes	yes

- **Instance Space X** : Set of all possible objects describable by attributes (often called *features*).
- **Concept c** : Subset of objects from X (c is unknown).
- **Target Function f** : Characteristic function indicating membership in c based on attributes (i.e. *label*) (f is unknown).
- **Training Data S** : Set of instances labeled with target function.

Concept Learning as Learning A Binary Function

- **Task**
 - Learn (to imitate) a function $f: X \rightarrow \{+1, -1\}$
- **Training Examples**
 - Learning algorithm is given the correct value of the function for particular inputs → training examples
 - An example is a pair (x, y) , where x is the input and $y = f(x)$ is the output of the target function applied to x .
- **Goal**
 - Find a function
$$h: X \rightarrow \{+1, -1\}$$
that approximates
$$f: X \rightarrow \{+1, -1\}$$
as well as possible.

Supervised Learning

- **Task**
 - Learn (to imitate) a function $f: X \rightarrow Y$
- **Training Examples**
 - Learning algorithm is given the correct value of the function for particular inputs → training examples
 - An example is a pair $(x, f(x))$, where x is the input and $y=f(x)$ is the output of the target function applied to x .
- **Goal**
 - Find a function
$$h: X \rightarrow Y$$
that approximates
$$f: X \rightarrow Y$$
as well as possible.

Supervised / Inductive Learning

- Given
 - examples of a function $(x, f(x))$
- Predict function $f(x)$ for new examples x
 - Discrete $f(x)$: Classification
 - Continuous $f(x)$: Regression
 - $f(x) = \text{Probability}(x)$: Probability estimation

Image Classification: a core task in Computer Vision



(assume given set of discrete labels)
{dog, cat, truck, plane, ...}



cat

The problem: semantic gap

Images are represented as
3D arrays of numbers, with
integers between [0, 255].

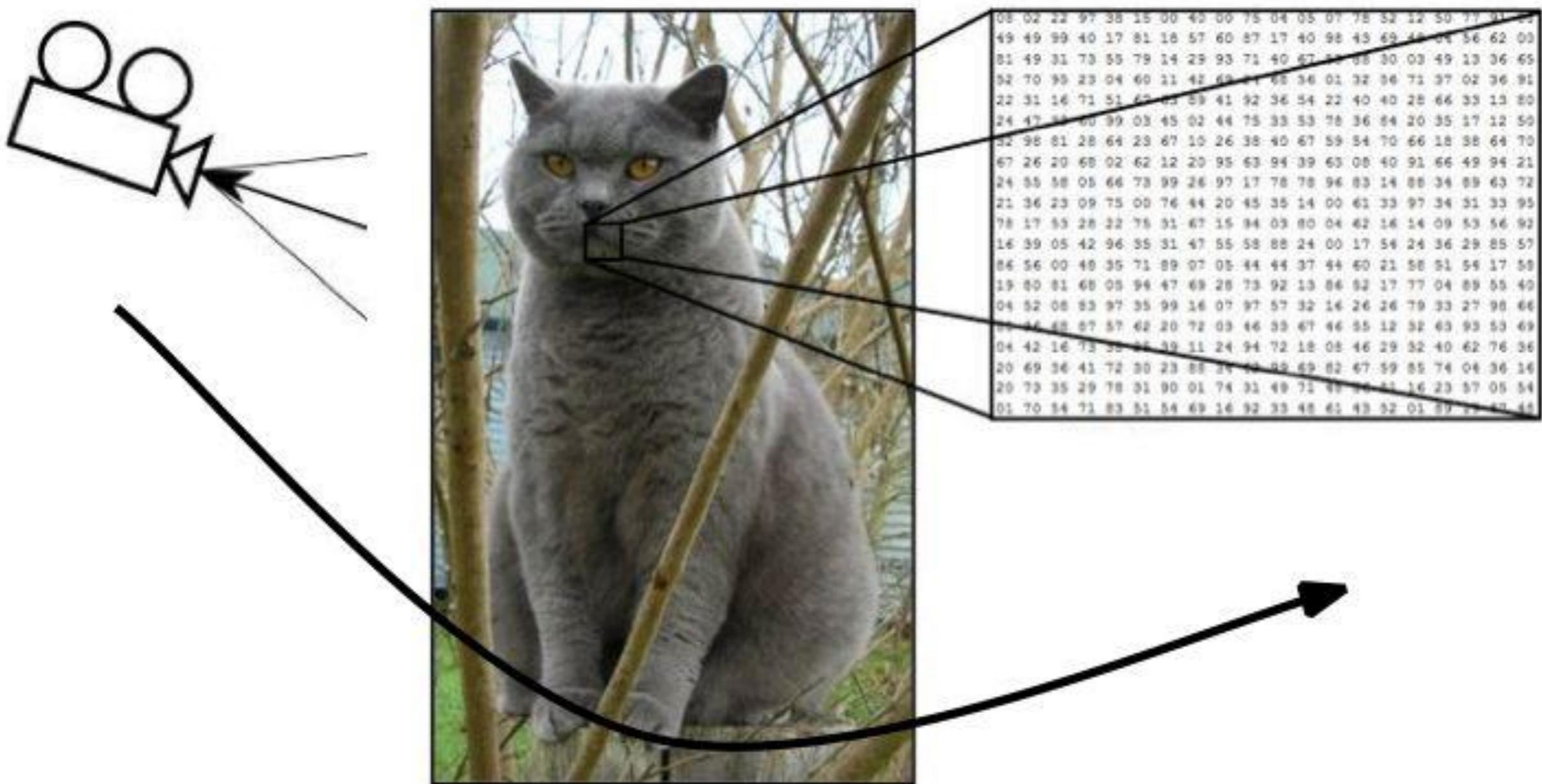
E.g.
 $300 \times 100 \times 3$
(3 for 3 color channels RGB)



08 04 22 37 38 15 00 40 00 75 04 05 07 78 52 12 50 77 81 00
49 49 99 40 17 81 18 57 60 87 17 40 98 43 69 48 01 56 62 00
81 49 31 73 55 79 14 29 93 71 40 67 50 05 30 03 49 13 36 65
52 70 95 23 04 60 11 42 62 21 48 56 01 32 56 71 37 02 36 91
22 31 16 71 51 63 03 89 41 92 36 54 22 40 40 28 66 33 13 80
24 47 39 60 99 03 45 02 44 75 33 53 78 36 54 20 35 17 12 50
32 98 81 28 64 23 67 10 26 38 40 67 59 54 70 66 18 38 64 70
67 26 20 68 02 62 12 20 95 63 94 39 63 08 40 91 66 49 94 21
24 55 58 05 66 73 99 26 97 17 78 78 96 83 14 88 34 89 63 72
21 36 23 09 75 00 76 44 20 45 35 14 00 61 33 97 34 31 33 95
78 17 53 28 22 75 31 67 15 94 03 80 04 62 16 14 09 53 56 92
16 39 05 42 96 35 31 47 85 58 88 24 00 17 54 24 36 29 85 57
86 56 00 48 35 71 89 07 05 44 44 37 44 60 21 58 51 54 17 58
19 80 81 68 05 94 47 69 28 73 92 13 86 52 17 77 04 89 55 40
04 52 08 63 97 35 99 16 07 97 57 32 16 26 24 79 33 27 98 66
00 46 69 57 57 62 20 72 03 46 33 67 46 55 12 32 63 93 53 69
04 42 16 73 16 15 39 11 24 94 72 18 08 16 29 32 40 62 76 36
20 69 36 41 72 30 23 88 34 62 99 69 82 67 59 85 74 04 36 16
20 73 35 29 78 31 90 01 74 31 49 71 99 84 81 16 23 57 05 54
01 70 54 71 83 51 54 69 16 92 33 48 61 43 52 01 89 15 47 48

What the computer sees

Challenges: Viewpoint Variation



Challenges: Illumination



Challenges: Deformation



Challenges: Occlusion



Challenges: Background clutter



Challenges: Intraclass variation



An image classifier

```
def predict(image):  
    # ????  
    return class_label
```

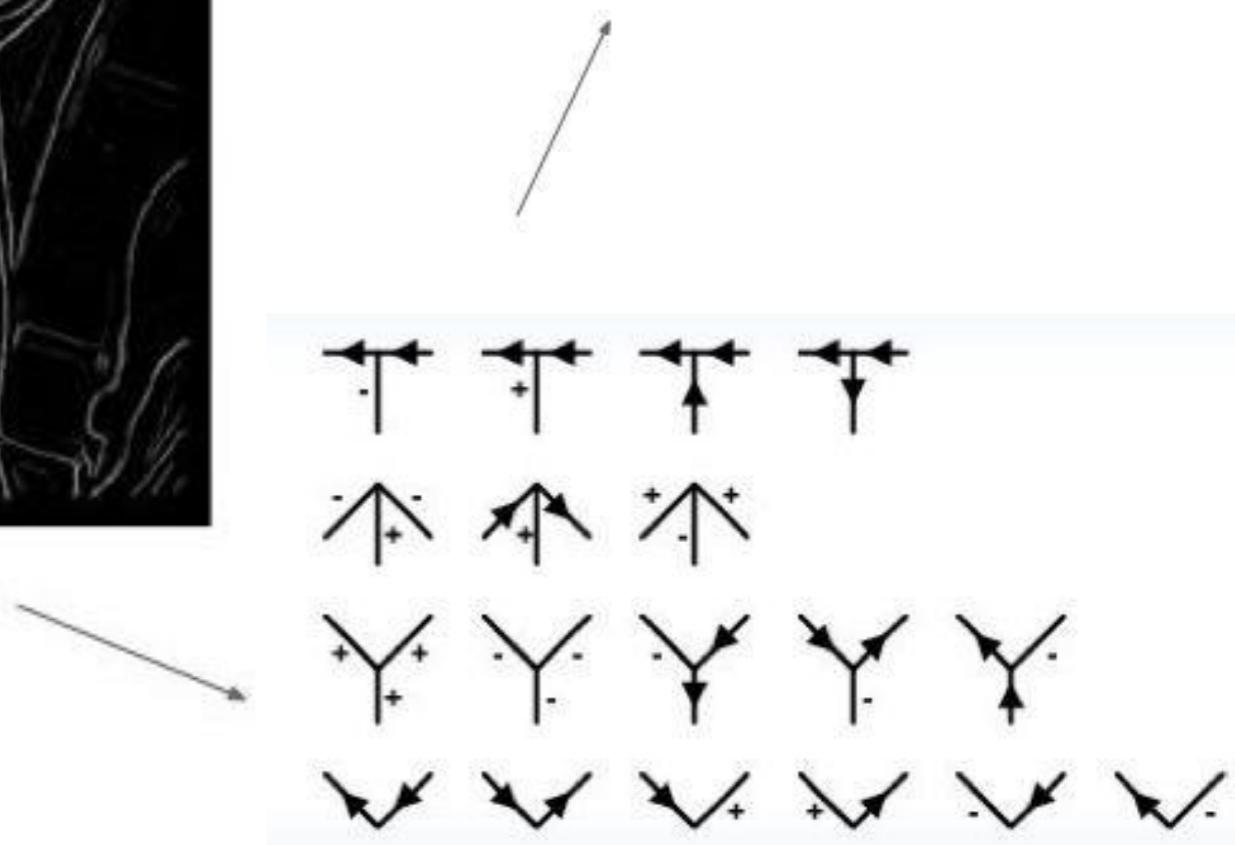
Unlike e.g. sorting a list of numbers,

no obvious way to hard-code the algorithm for
recognizing a cat, or other classes.

Attempts have been made



???



Data-driven approach:

1. Collect a dataset of images and labels
2. Use Machine Learning to train an image classifier
3. Evaluate the classifier on a withheld set of test images

Example training set

```
def train(train_images, train_labels):  
    # build a model for images -> labels...  
    return model  
  
def predict(model, test_images):  
    # predict test_labels using the model...  
    return test_labels
```



First classifier: Nearest Neighbor Classifier

```
def train(train_images, train_labels):  
    # build a model for images -> labels...  
    return model  
  
def predict(model, test_images):  
    # predict test_labels using the model...  
    return test_labels
```

Remember all training images and their labels

Predict the label of the most similar training image

Example dataset: CIFAR-10

10 labels

50,000 training images, each image is tiny: 32x32

10,000 test images.

airplane



automobile



bird



cat



deer



dog



frog



horse



ship



truck



Example dataset: CIFAR-10

10 labels

50,000 training images

10,000 test images.

airplane



automobile



bird



cat



deer



dog



frog



horse



ship



truck



For every test image (first column),
examples of nearest neighbors in rows



How do we compare the images? What is the distance metric?

L1 distance:

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$

test image				training image				pixel-wise absolute value differences			
56	32	10	18	10	20	24	17	46	12	14	1
90	23	128	133	8	10	89	100	82	13	39	33
24	26	178	200	12	16	178	170	12	10	0	30
2	0	255	220	4	32	233	112	2	32	22	108

-

=

add → 456

Nearest Neighbor classifier

```
import numpy as np

class NearestNeighbor:
    def __init__(self):
        pass

    def train(self, X, y):
        """ X is N x D where each row is an example. Y is 1-dimension of size N """
        # the nearest neighbor classifier simply remembers all the training data
        self.Xtr = X
        self.ytr = y

    def predict(self, X):
        """ X is N x D where each row is an example we wish to predict label for """
        num_test = X.shape[0]
        # lets make sure that the output type matches the input type
        Ypred = np.zeros(num_test, dtype = self.ytr.dtype)

        # loop over all test rows
        for i in xrange(num_test):
            # find the nearest training image to the i'th test image
            # using the L1 distance (sum of absolute value differences)
            distances = np.sum(np.abs(self.Xtr - X[i,:]), axis = 1)
            min_index = np.argmin(distances) # get the index with smallest distance
            Ypred[i] = self.ytr[min_index] # predict the label of the nearest example

        return Ypred
```

Nearest Neighbor classifier

remember the training data

```
import numpy as np

class NearestNeighbor:
    def __init__(self):
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    def train(self, X, y):
        """ X is N x D where each row is an example. Y is 1-dimension of size N """
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        return Ypred
```

```

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class NearestNeighbor:
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            # using the L1 distance (sum of absolute value differences)
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            min_index = np.argmin(distances) # get the index with smallest distance
            Ypred[i] = self.ytr[min_index] # predict the label of the nearest example

        return Ypred

```

Nearest Neighbor classifier

- for every test image:
- find nearest train image with L1 distance
 - predict the label of nearest training image

```

import numpy as np

class NearestNeighbor:
    def __init__(self):
        pass

    def train(self, X, y):
        """ X is N x D where each row is an example. Y is 1-dimension of size N """
        # the nearest neighbor classifier simply remembers all the training data
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            min_index = np.argmin(distances) # get the index with smallest distance
            Ypred[i] = self.ytr[min_index] # predict the label of the nearest example

        return Ypred

```

Nearest Neighbor classifier

Q: how does the classification speed depend on the size of the training data?

```

import numpy as np

class NearestNeighbor:
    def __init__(self):
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    def train(self, X, y):
        """ X is N x D where each row is an example. Y is 1-dimension of size N """
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            min_index = np.argmin(distances) # get the index with smallest distance
            Ypred[i] = self.ytr[min_index] # predict the label of the nearest example

    return Ypred

```

Nearest Neighbor classifier

Q: how does the classification speed depend on the size of the training data?
linearly :(

Aside: Approximate Nearest Neighbor

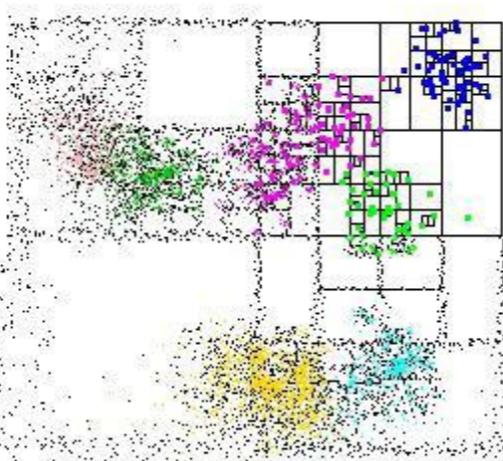
find approximate nearest neighbors quickly

ANN: A Library for Approximate Nearest Neighbor Searching

David M. Mount and Sunil Arya

Version 1.1.2

Release Date: Jan 27, 2010



What is ANN?

ANN is a library written in C++, which supports data structures and algorithms for both exact and approximate nearest neighbor searching in arbitrarily high dimensions.

In the nearest neighbor problem a set of data points in d-dimensional space is given. These points are preprocessed into a data structure, so that given any query point q , the nearest or generally k nearest points of P to q can be reported efficiently. The distance between two points can be defined in many ways. ANN assumes that distances are measured using any class of distance functions called Minkowski metrics. These include the well known Euclidean distance, Manhattan distance, and max distance.

Based on our own experience, ANN performs quite efficiently for point sets ranging in size from thousands to hundreds of thousands, and in dimensions as high as 20. (For applications in significantly higher dimensions, the results are rather spotty, but you might try it anyway.)

The library implements a number of different data structures, based on kd-trees and box-decomposition trees, and employs a couple of different search strategies.

The library also comes with test programs for measuring the quality of performance of ANN on any particular data sets, as well as programs for visualizing the structure of the geometric data structures.

FLANN - Fast Library for Approximate Nearest Neighbors

- Home
- News
- Publications
- Download
- Changelog
- Repository

What is FLANN?

FLANN is a library for performing fast approximate nearest neighbor searches in high dimensional spaces. It contains a collection of algorithms we found to work best for nearest neighbor search and a system for automatically choosing the best algorithm and optimum parameters depending on the dataset.

FLANN is written in C++ and contains bindings for the following languages: C, MATLAB and Python.

News

- (14 December 2012) Version 1.8.0 is out bringing incremental addition/removal of points to/from indexes
- (20 December 2011) Version 1.7.0 is out bringing two new index types and several other improvements.
- You can find binary installers for FLANN on the [Point Cloud Library](#) project page. Thanks to the PCL developers!
- Mac OS X users can install flann through MacPorts (thanks to Mark Moll for maintaining the Portfile)
- New release introducing an easier way to use custom distances, kd-tree implementation optimized for low dimensionality search and experimental MPI support
- New release introducing new C++ templated API, thread-safe search, save/load of indexes and more.
- The FLANN license was changed from LGPL to BSD.

How fast is it?

In our experiments we have found FLANN to be about one order of magnitude faster on many datasets (in query time), than previously available approximate nearest neighbor search software.

Publications

More information and experimental results can be found in the following papers:

- Marius Muja and David G. Lowe: "Scalable Nearest Neighbor Algorithms for High Dimensional Data". Pattern Analysis and Machine Intelligence (PAMI), Vol. 36, 2014. [\[PDF\]](#) [\[BibTeX\]](#)
- Marius Muja and David G. Lowe: "Fast Matching of Binary Features". Conference on Computer and Robot Vision (CRV) 2012. [\[PDF\]](#) [\[BibTeX\]](#)
- Marius Muja and David G. Lowe, "Fast Approximate Nearest Neighbors with Automatic Algorithm Configuration", in International Conference on Computer Vision Theory and Applications (VISAPP'09), 2009 [\[PDF\]](#) [\[BibTeX\]](#)

The choice of distance is a **hyperparameter**
common choices:

L1 (Manhattan) distance

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$

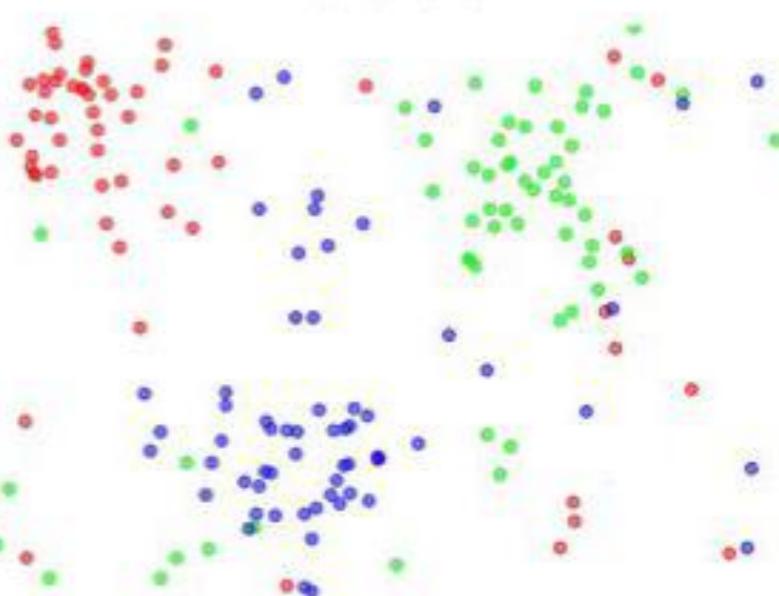
L2 (Euclidean) distance

$$d_2(I_1, I_2) = \sqrt{\sum_p (I_1^p - I_2^p)^2}$$

k-Nearest Neighbor

find the k nearest images, have them vote on the label

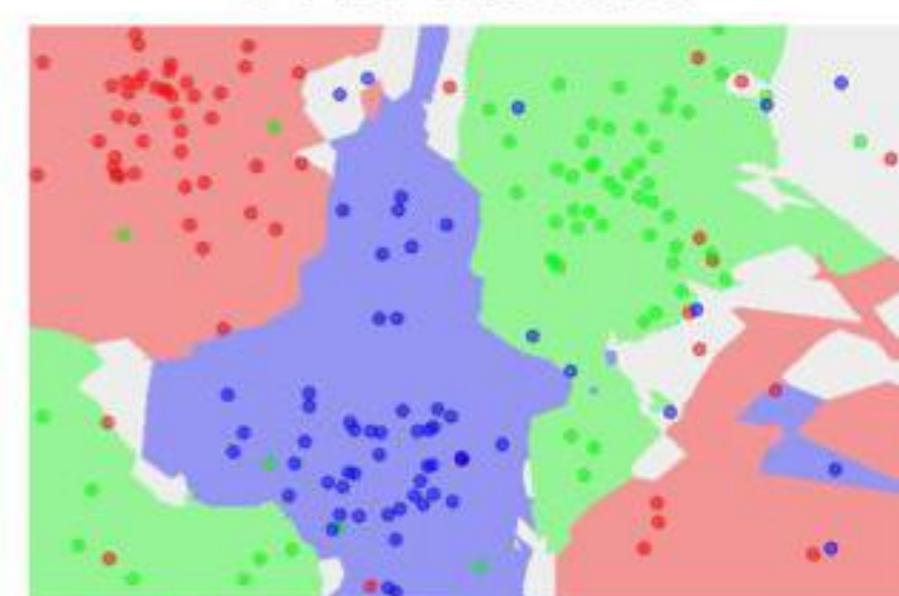
the data



NN classifier



5-NN classifier



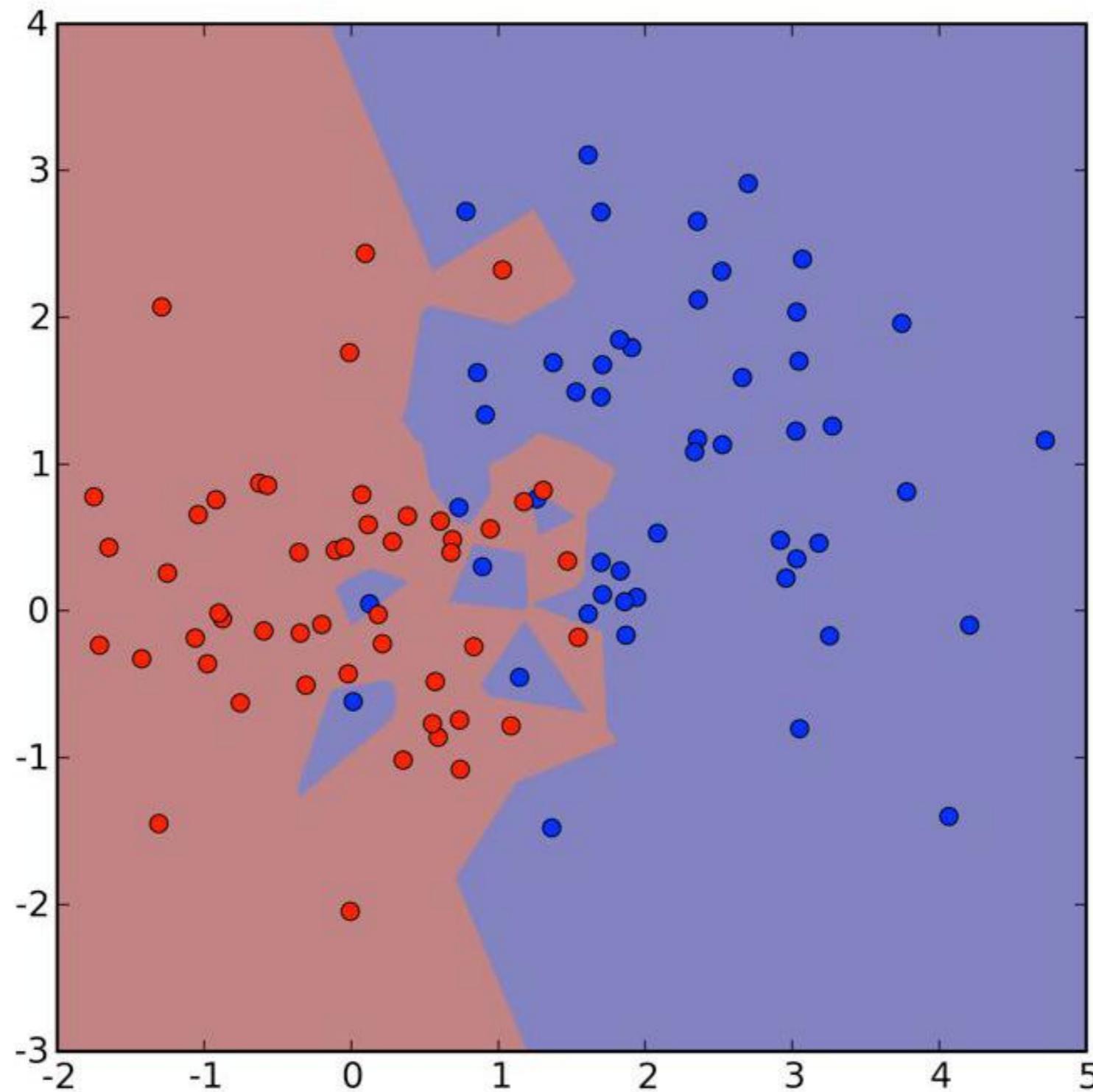
http://en.wikipedia.org/wiki/K-nearest_neighbors_algorithm

K-Nearest Neighbor (kNN)

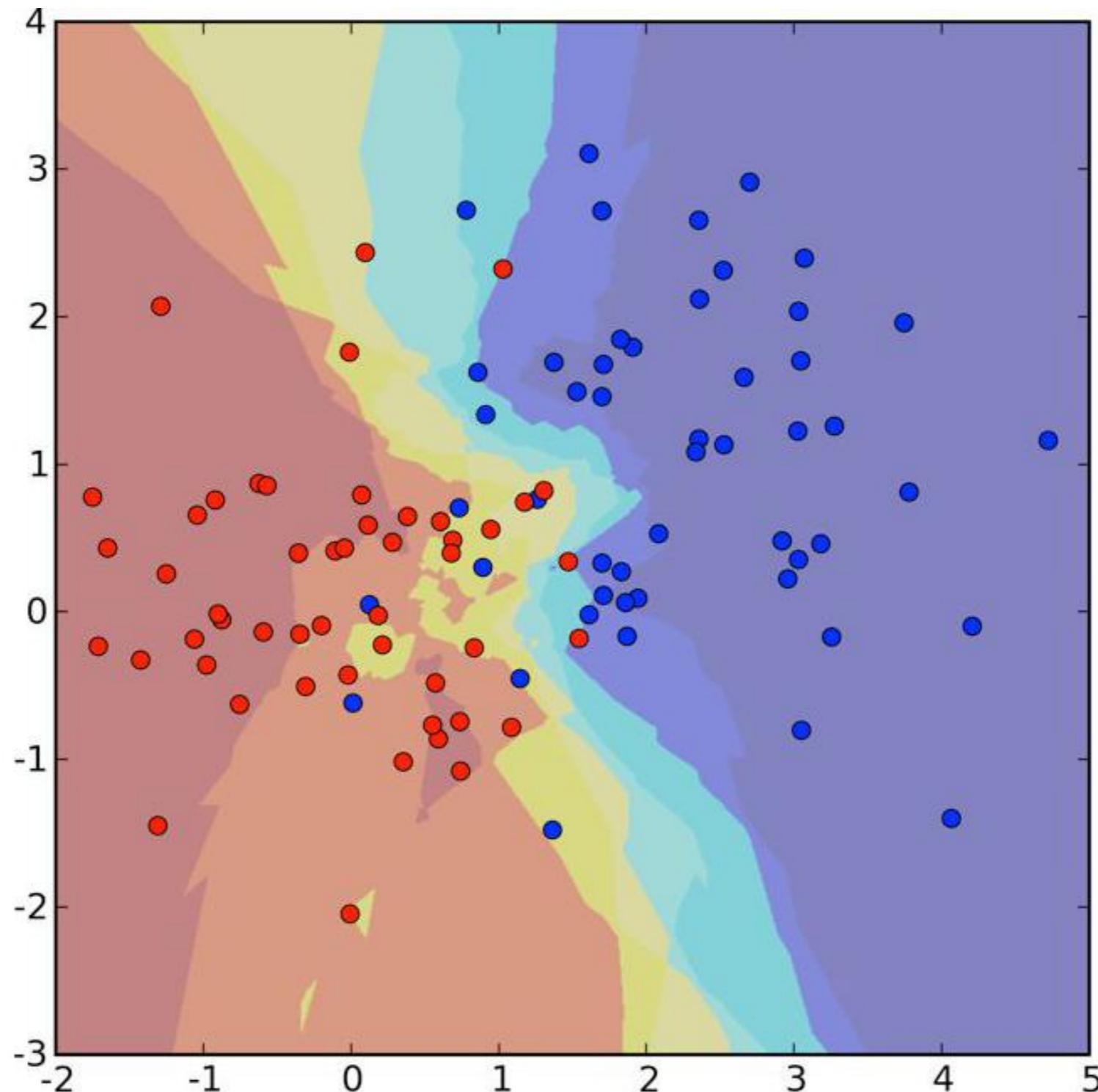
- Given: Training data $\{(x_1, y_1), \dots, (x_n, y_n)\}$
 - Attribute vectors: $x_i \in X$
 - Labels: $y_i \in Y$
- Parameter:
 - Similarity function: $K : X \times X \rightarrow R$
 - Number of nearest neighbors to consider: k
- Prediction rule
 - New example x'
 - K-nearest neighbors: k train examples with largest $K(x_i, x')$

$$h(\vec{x}') = \arg \max_{y \in Y} \left\{ \sum_{i \in knn(\vec{x}')} 1_{[y_i=y]} \right\}$$

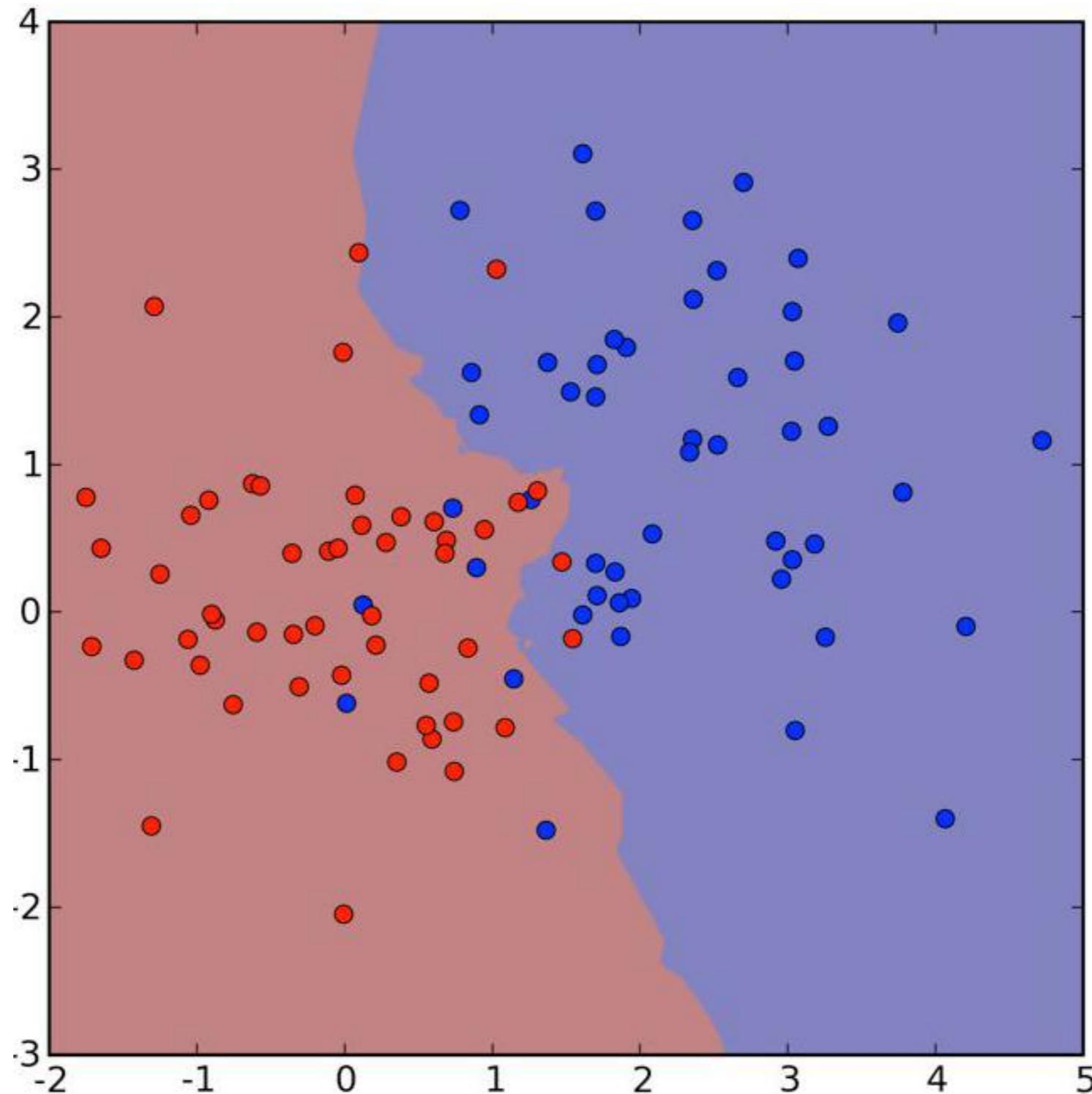
1-Nearest Neighbor



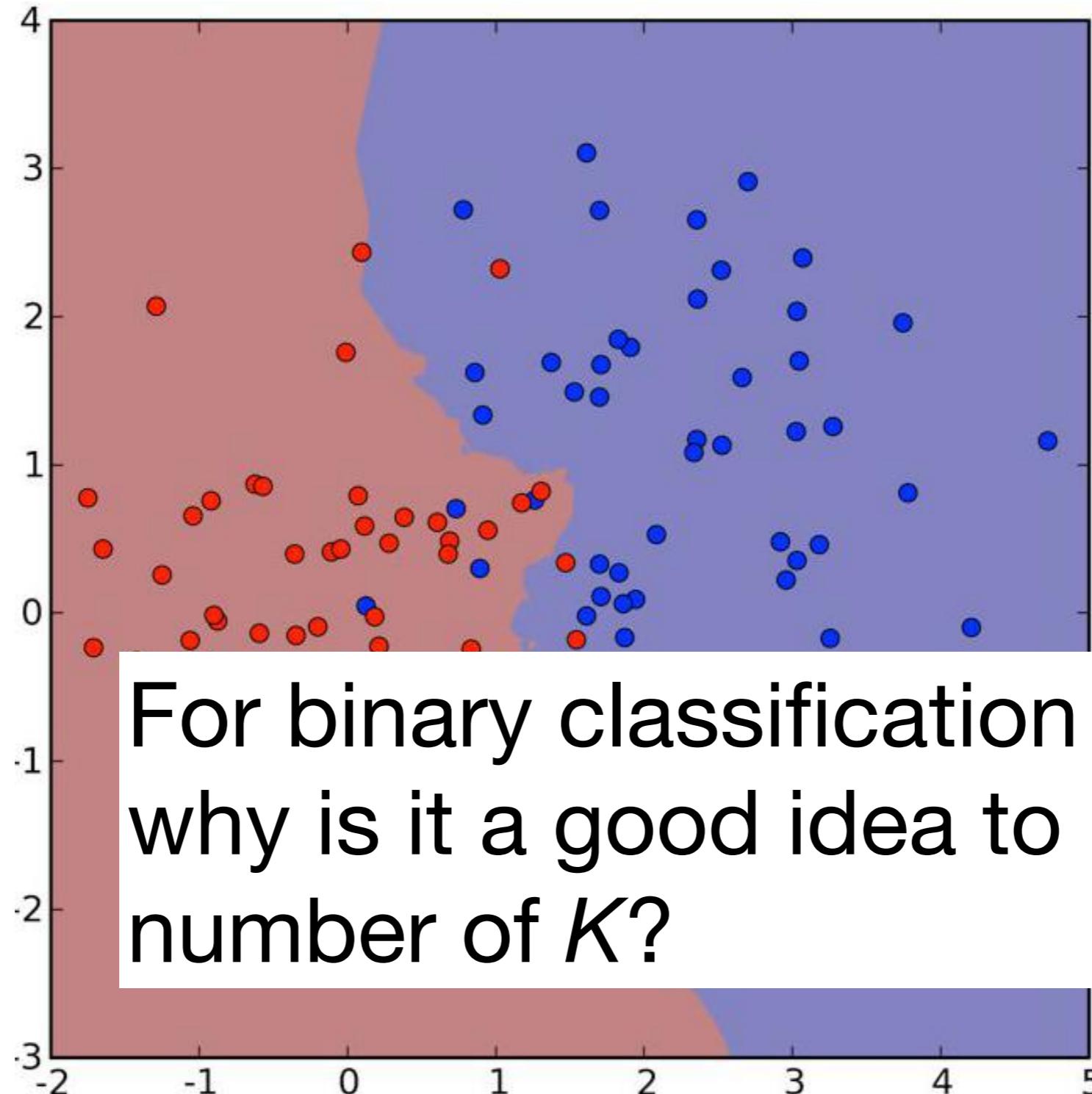
4-Nearest Neighbors



4-Nearest Neighbors Sign



4-Nearest Neighbors Sign



Example dataset: CIFAR-10

10 labels

50,000 training images

10,000 test images.

airplane



automobile



bird



cat



deer



dog



frog



horse



ship



truck



For every test image (first column),
examples of nearest neighbors in rows



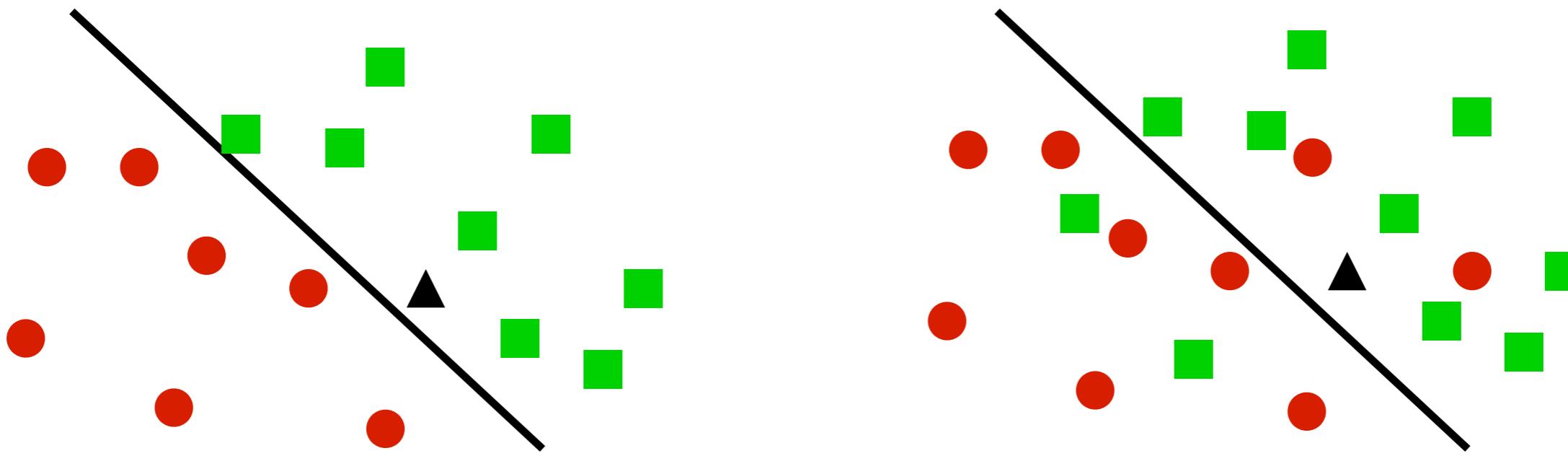
What is the best **distance** to use?

What is the best value of **k** to use?

i.e. how do we set the **hyperparameters**?

We will talk about this later!

If we get more data



- 1 Nearest Neighbor
 - Converges to perfect solution if clear separation
 - Twice the minimal error rate $2p(1-p)$ for noisy problems
- k-Nearest Neighbor
 - Converges to perfect solution if clear separation (**but needs more data**)
 - Converges to minimal error $\min(p, 1-p)$ for noisy problems if k increases

Demo

Weighted K-Nearest Neighbor

- Given: Training data $\{(x_1, y_1), \dots, (x_n, y_n)\}$
 - Attribute vectors: $x_i \in X$
 - Target attribute $y_i \in Y$
- Parameter:
 - Similarity function: $K : X \times X \rightarrow R$
 - Number of nearest neighbors to consider: k
- Prediction rule
 - New example x'
 - K-nearest neighbors: k train examples with largest $K(x_i, x')$

$$h(\vec{x}') = \arg \max_{y \in Y} \left\{ \sum_{i \in knn(\vec{x}')} 1_{[y_i=y]} K(\vec{x}_i, \vec{x}') \right\}$$

More Nearest Neighbors in Visual Data

Where in the World?

[Hays & Efros, CVPR 2008]

A nearest neighbor
recognition example



Where in the World?

[Hays & Efros, CVPR 2008]

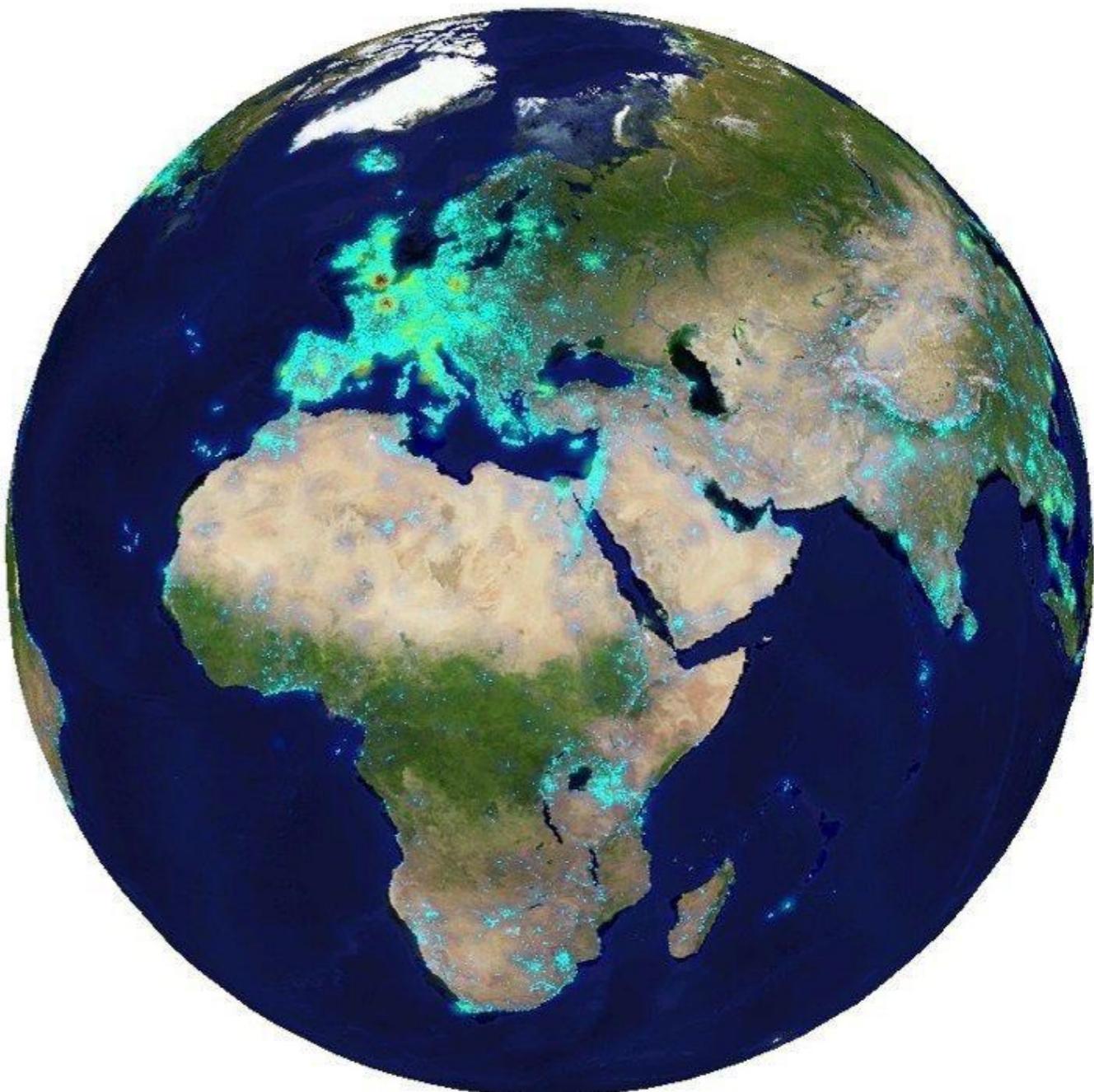


Where in the World?

[Hays & Efros, CVPR 2008]

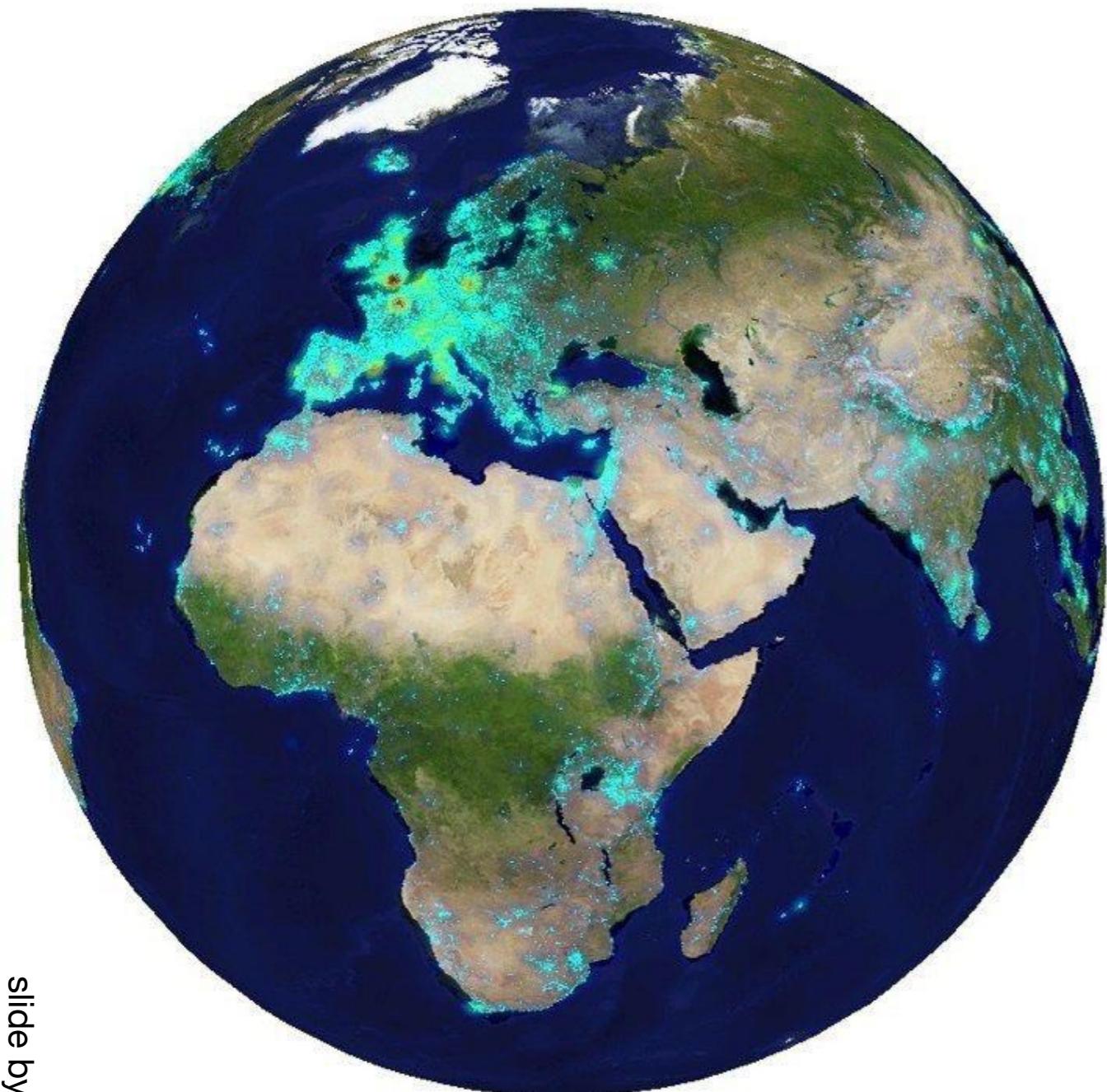


6+ million geotagged photos
by 109,788 photographers



Annotated by Flickr users

6+ million geotagged photos
by 109,788 photographers

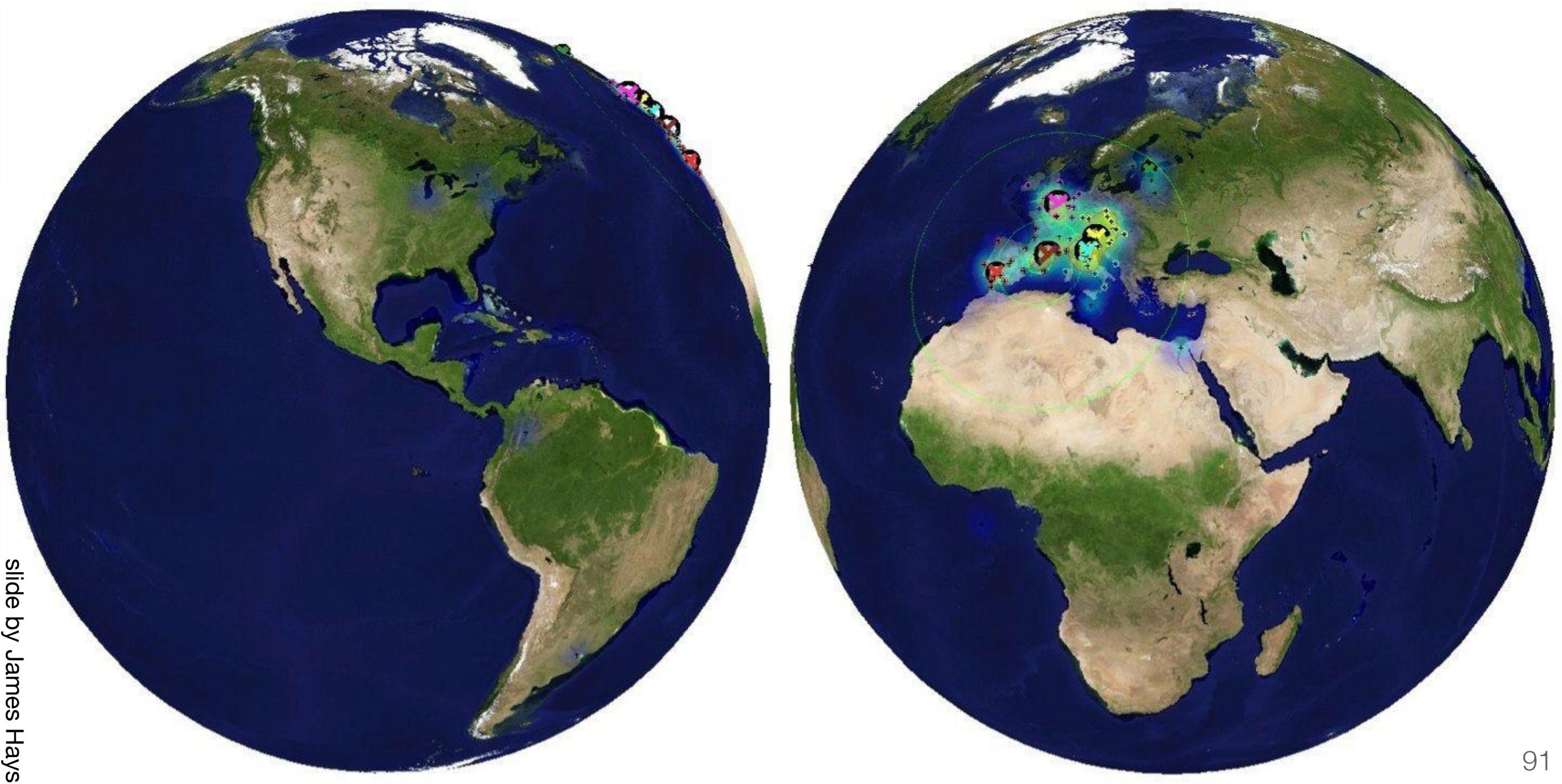
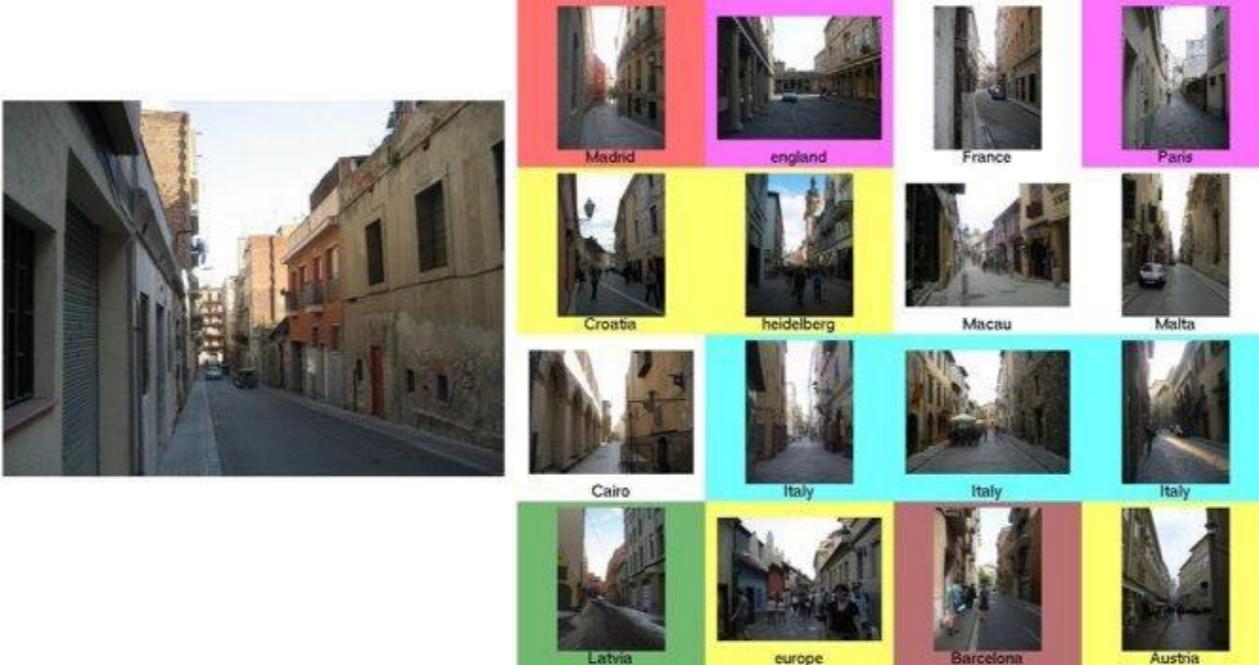


Annotated by Flickr users

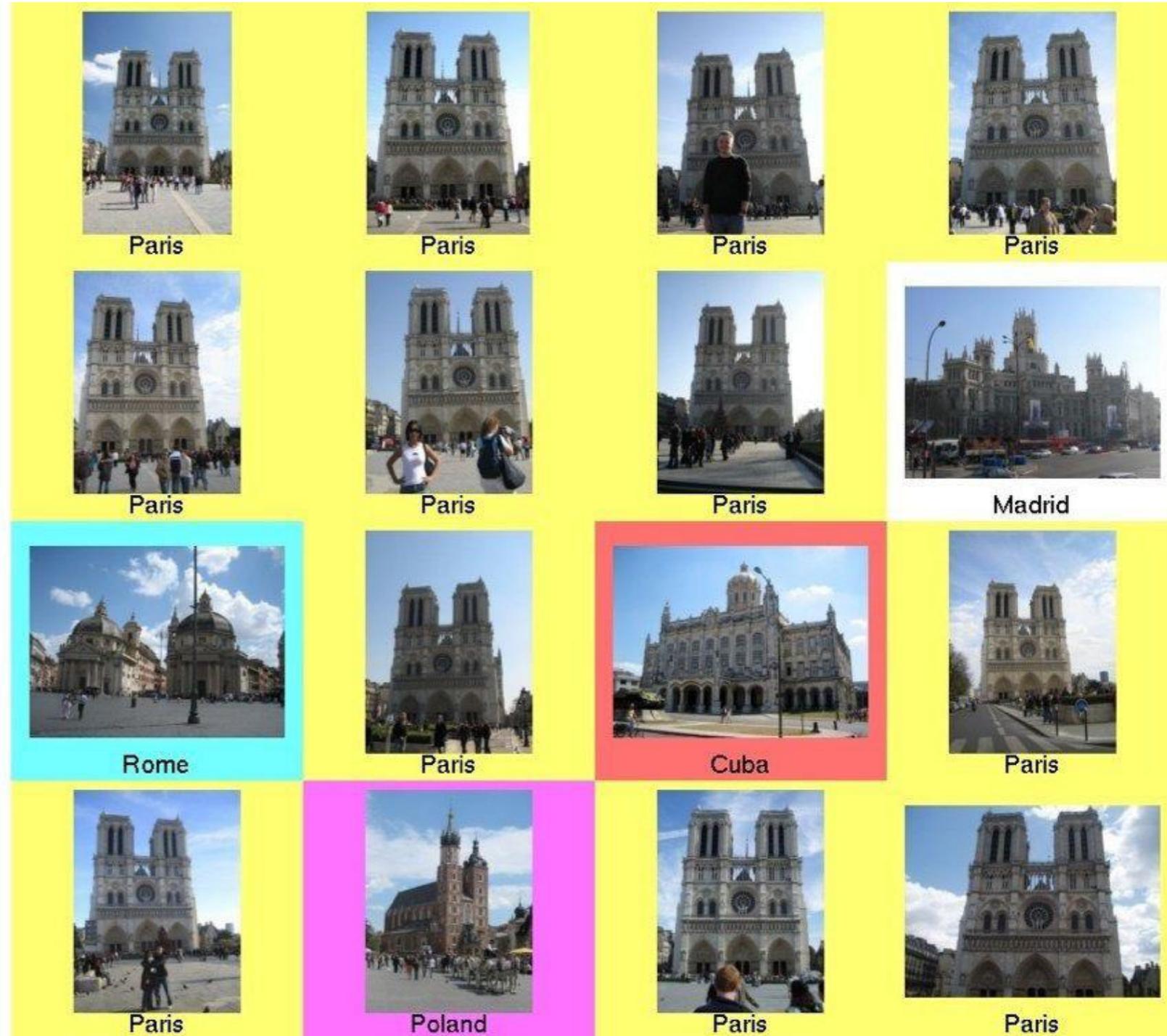
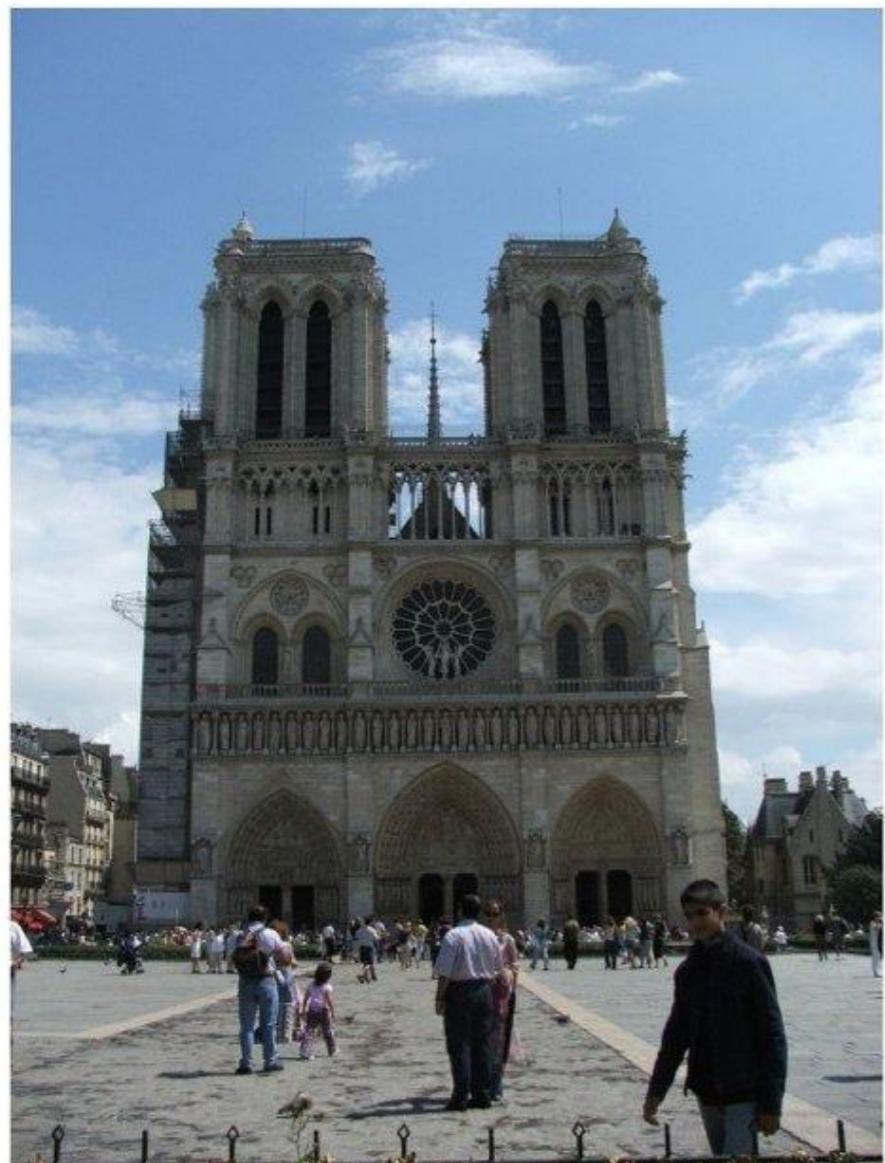


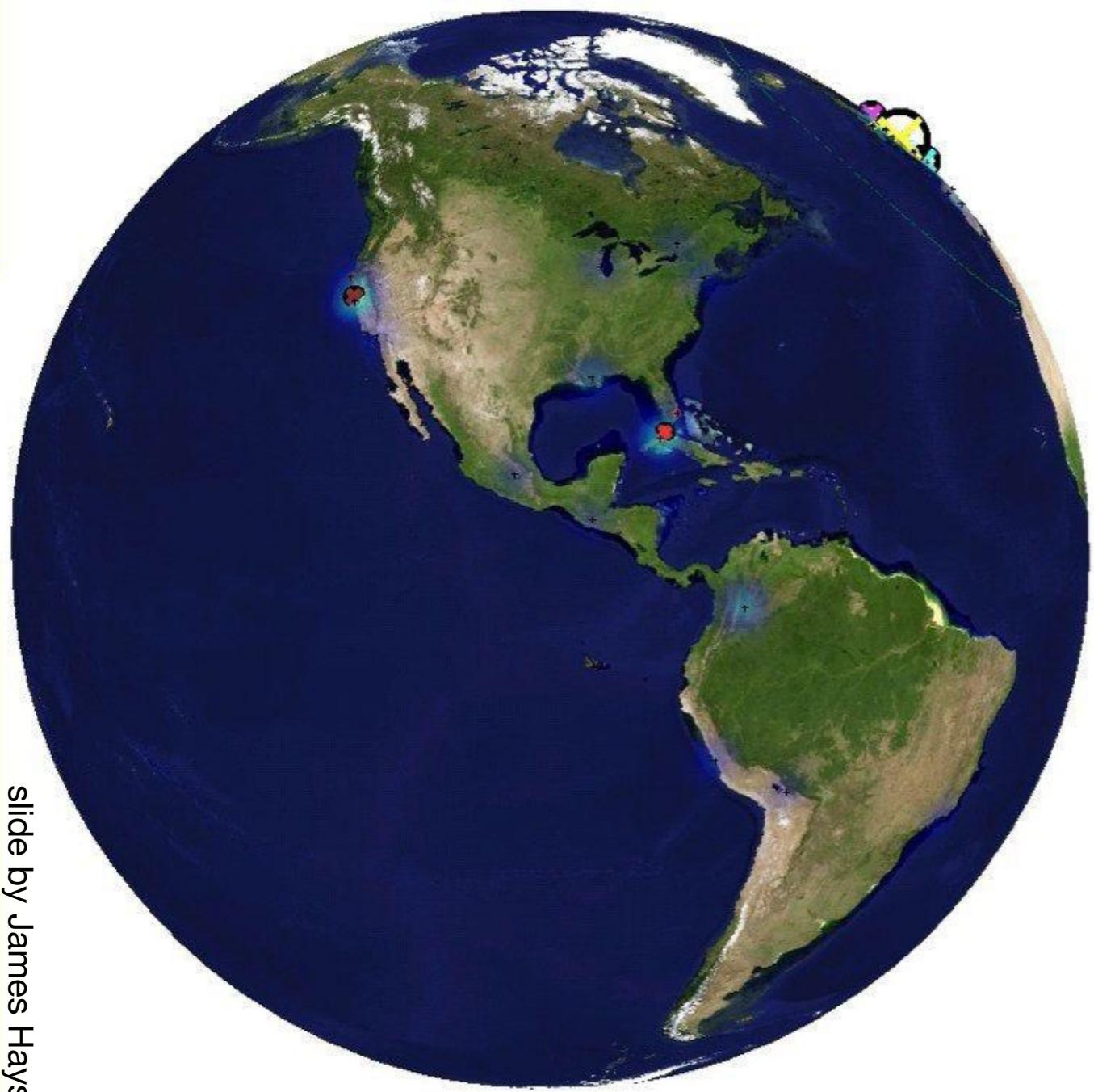
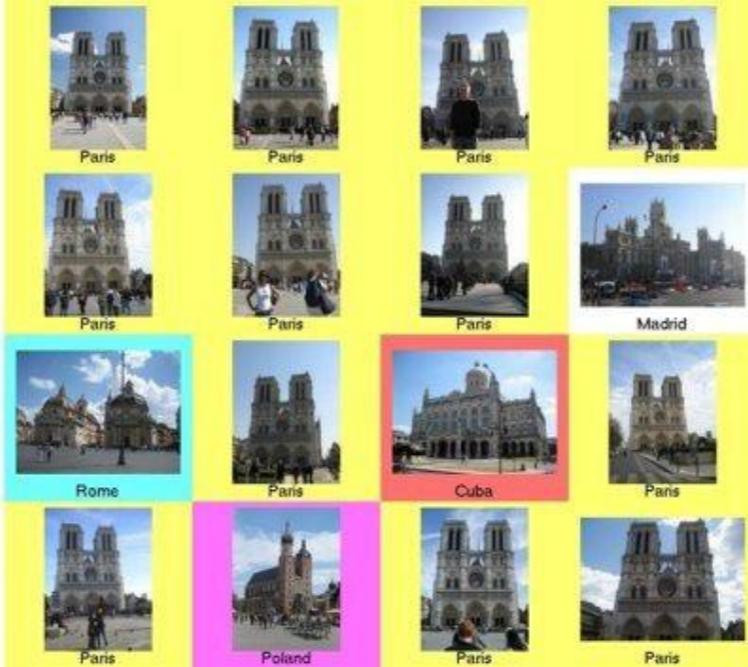
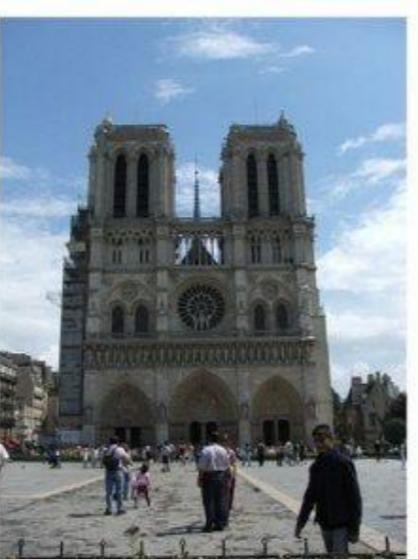
Scene Matches



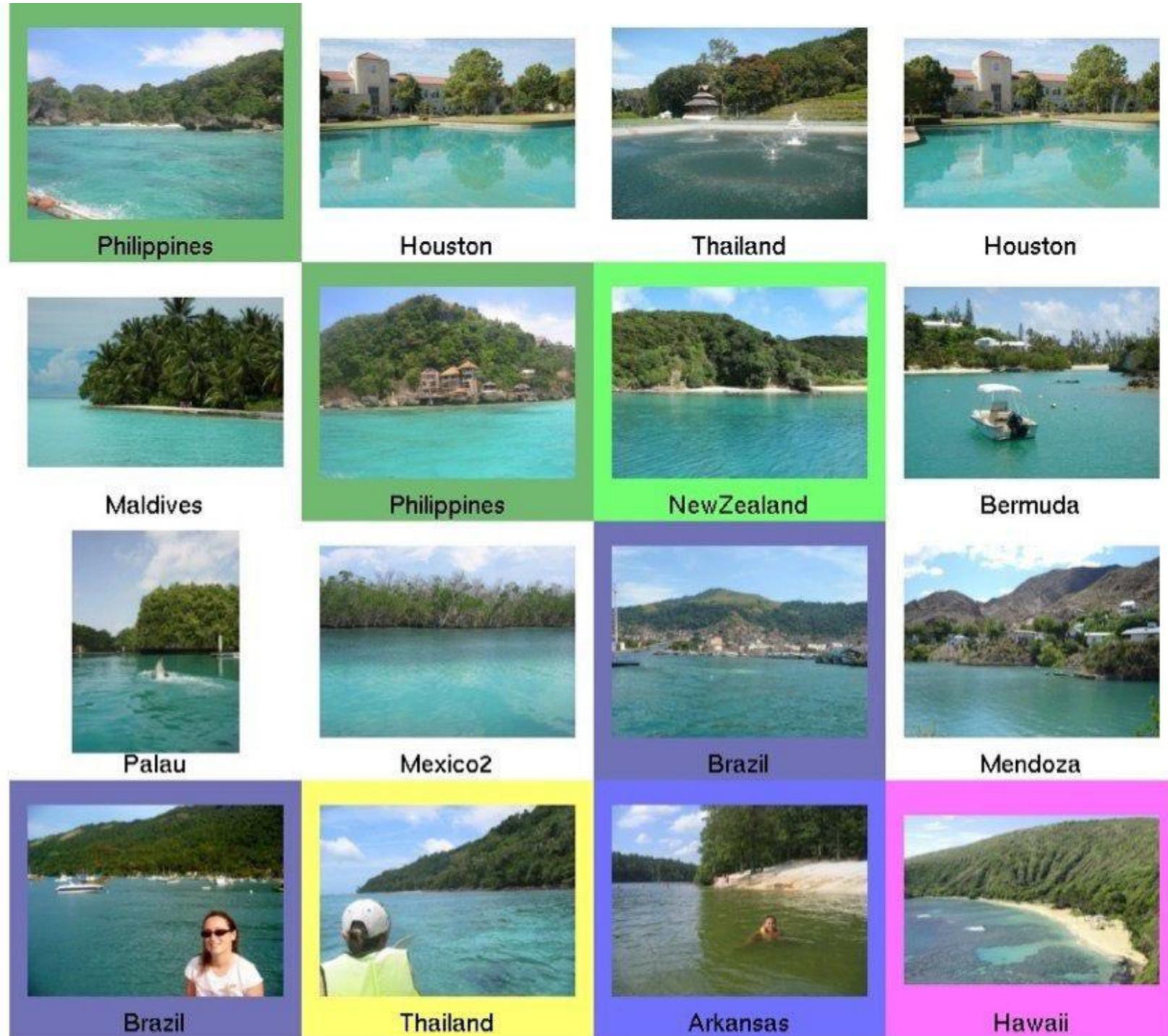


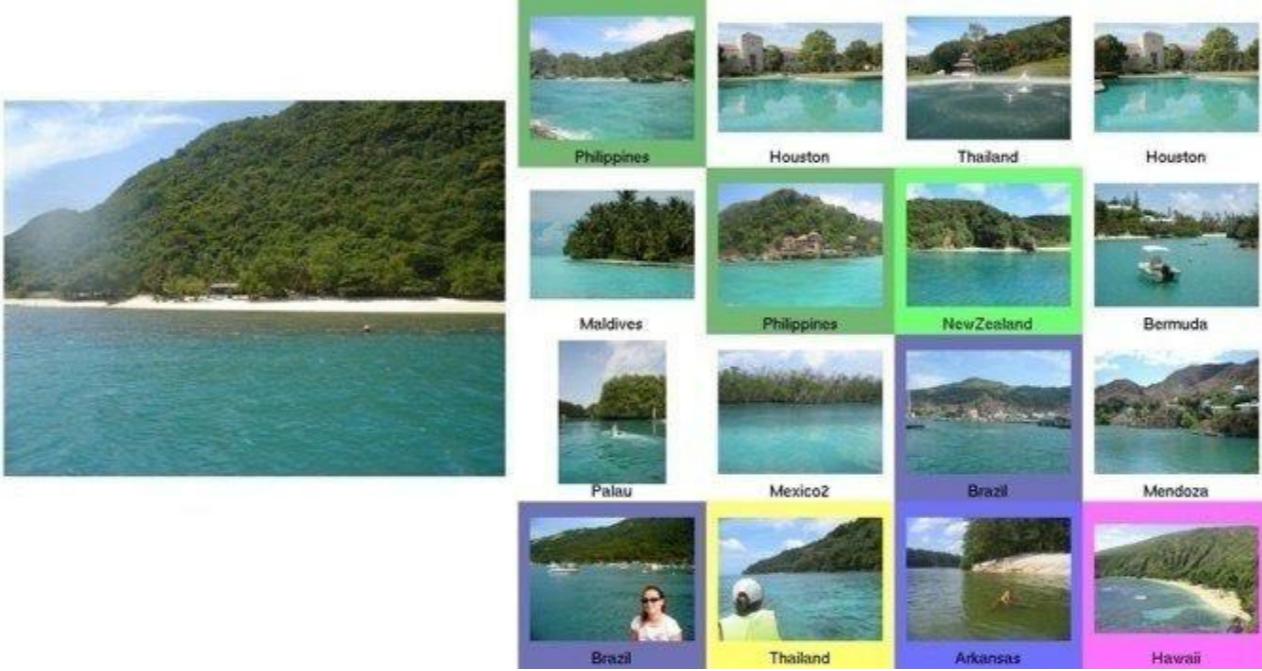
Scene Matches



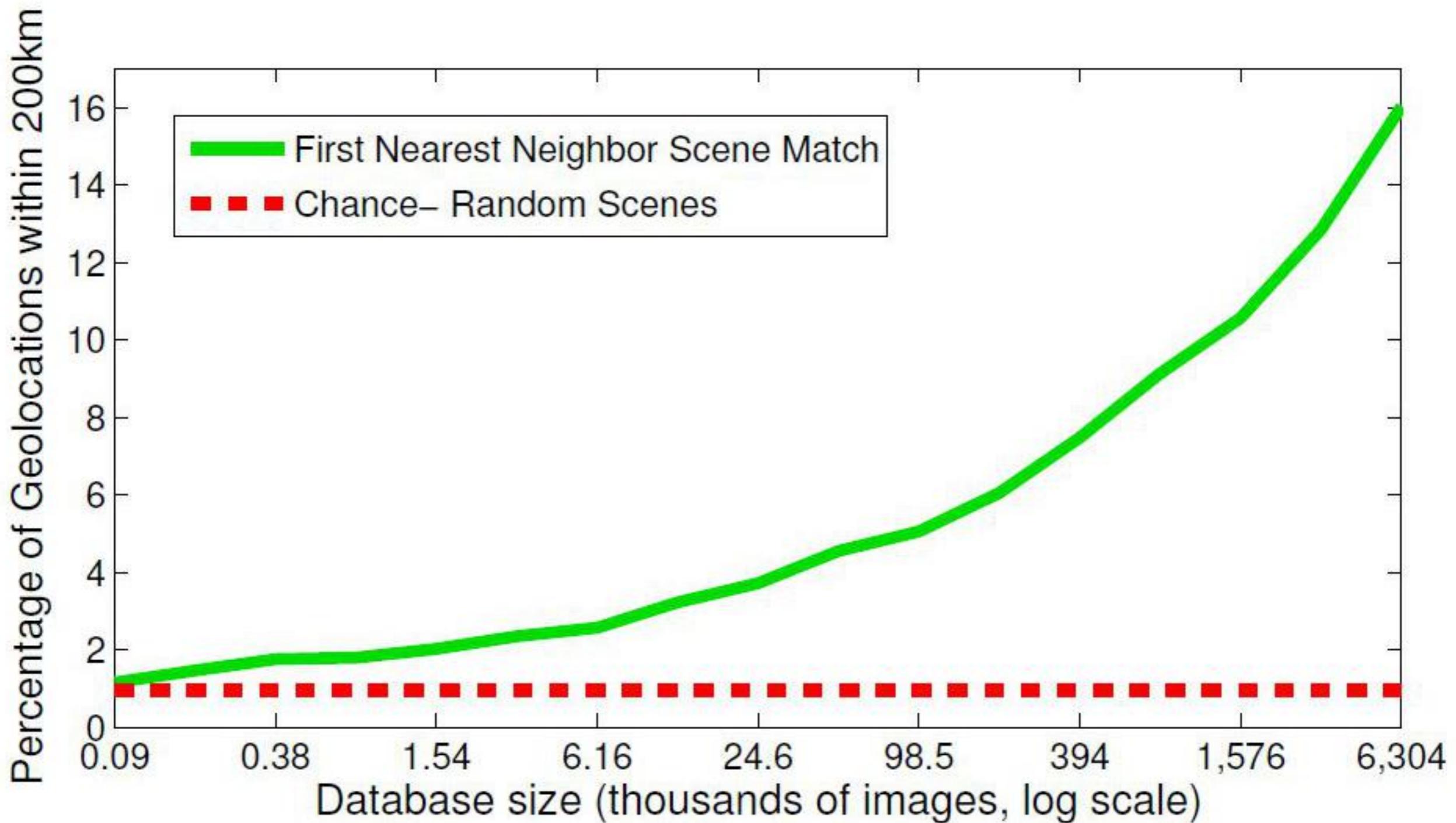


Scene Matches

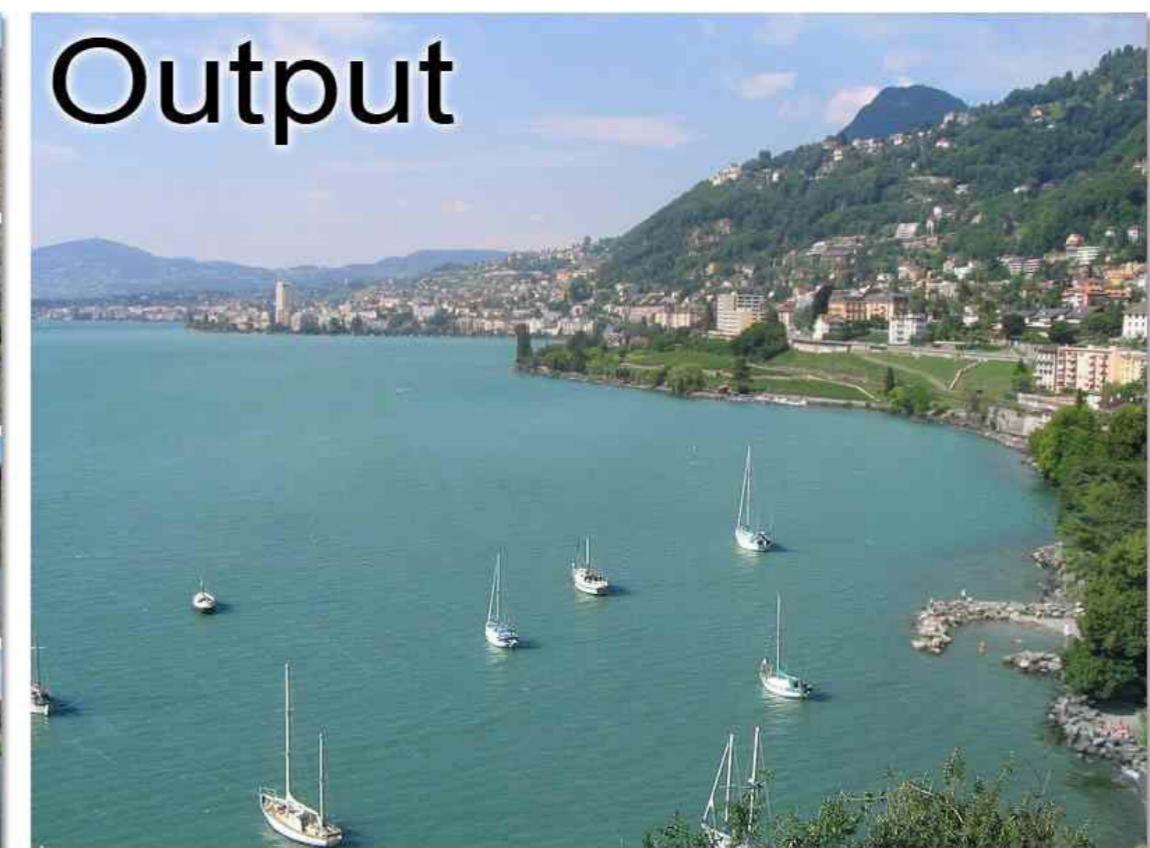
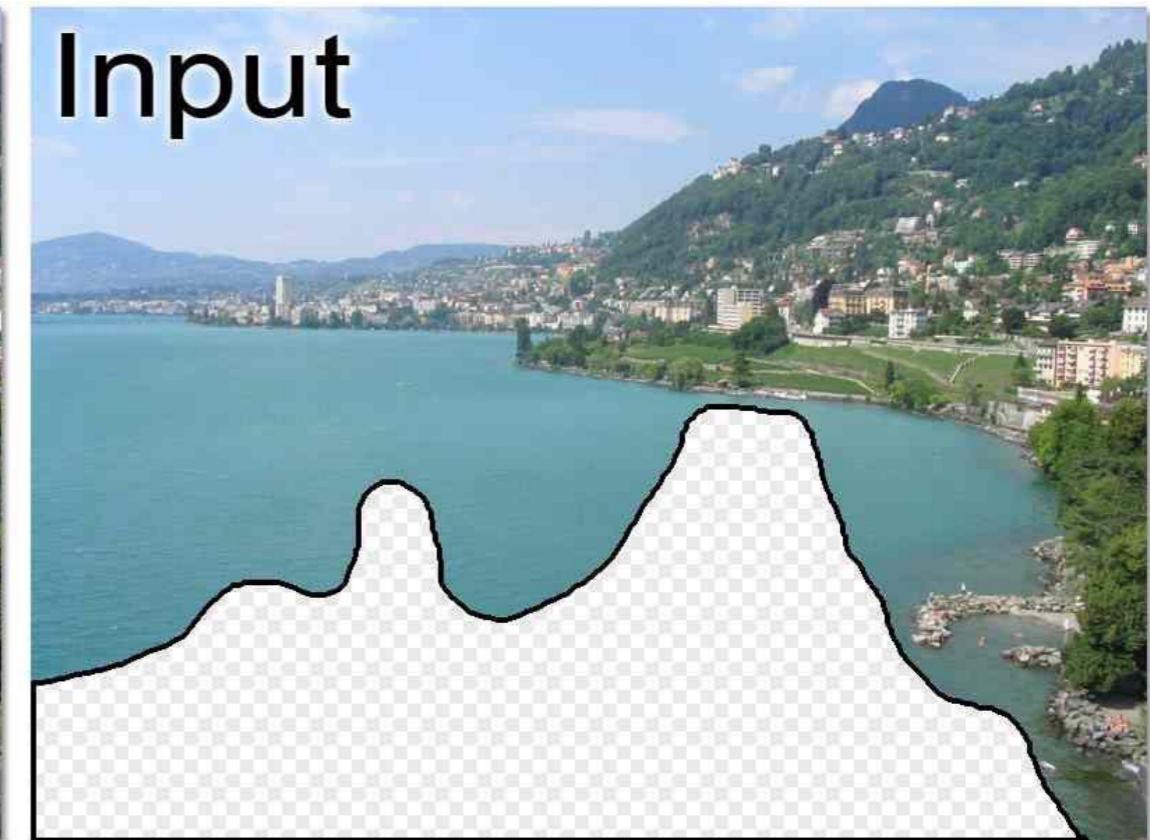


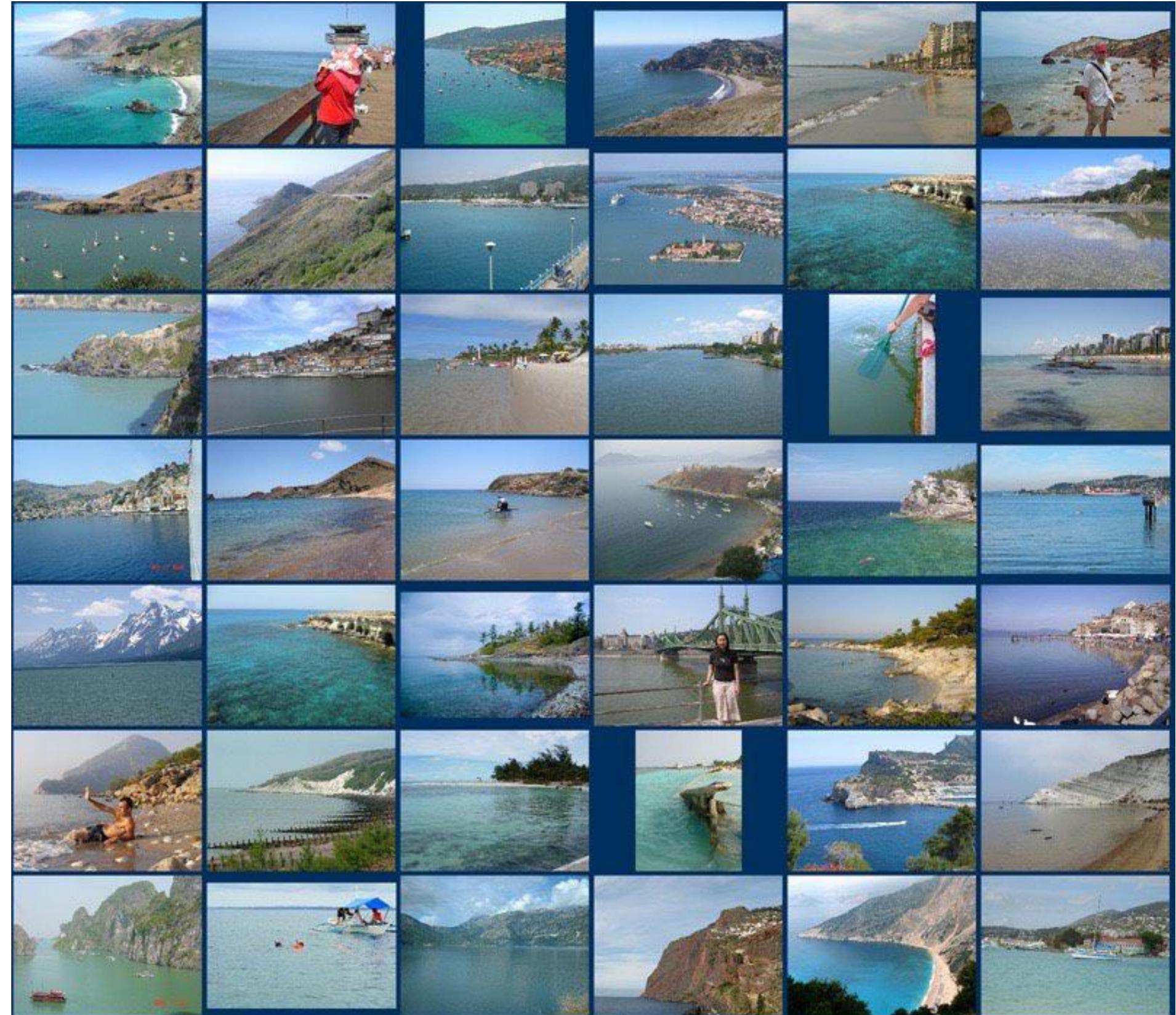
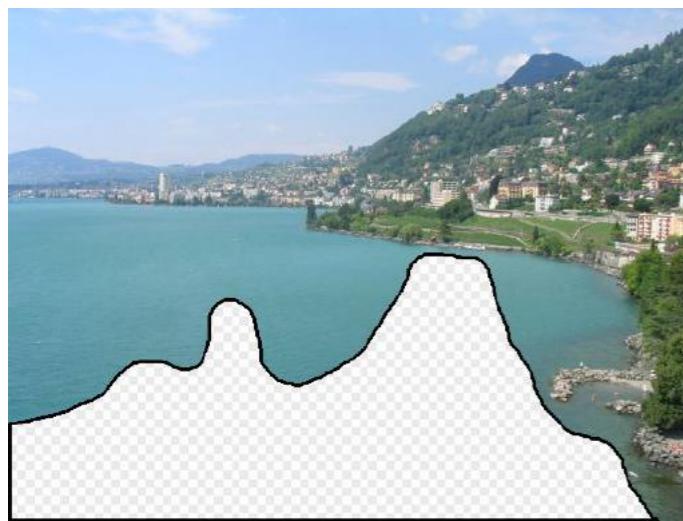


The Importance of Data



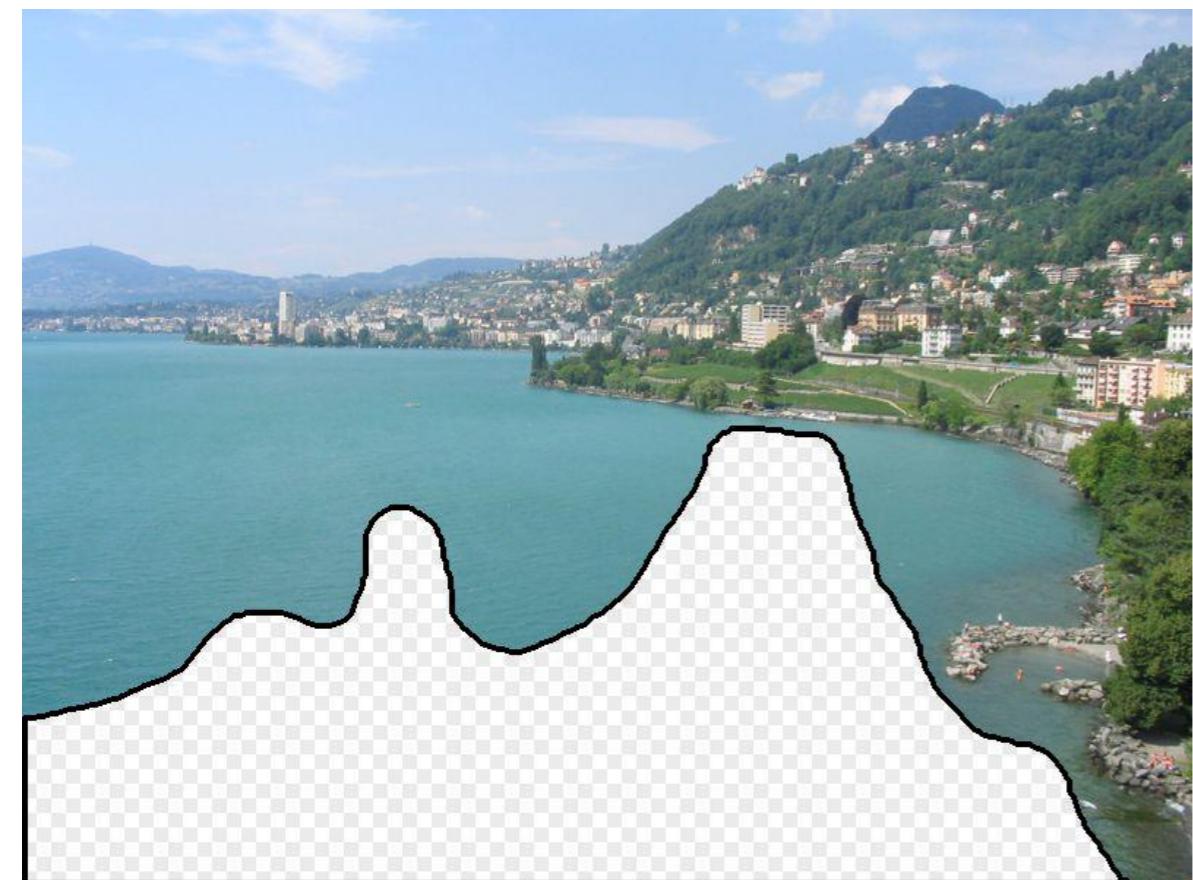
Scene Completion [Hays & Efros, SIGGRAPH07]





... 200 total

Context Matching





Graph cut + Poisson blending

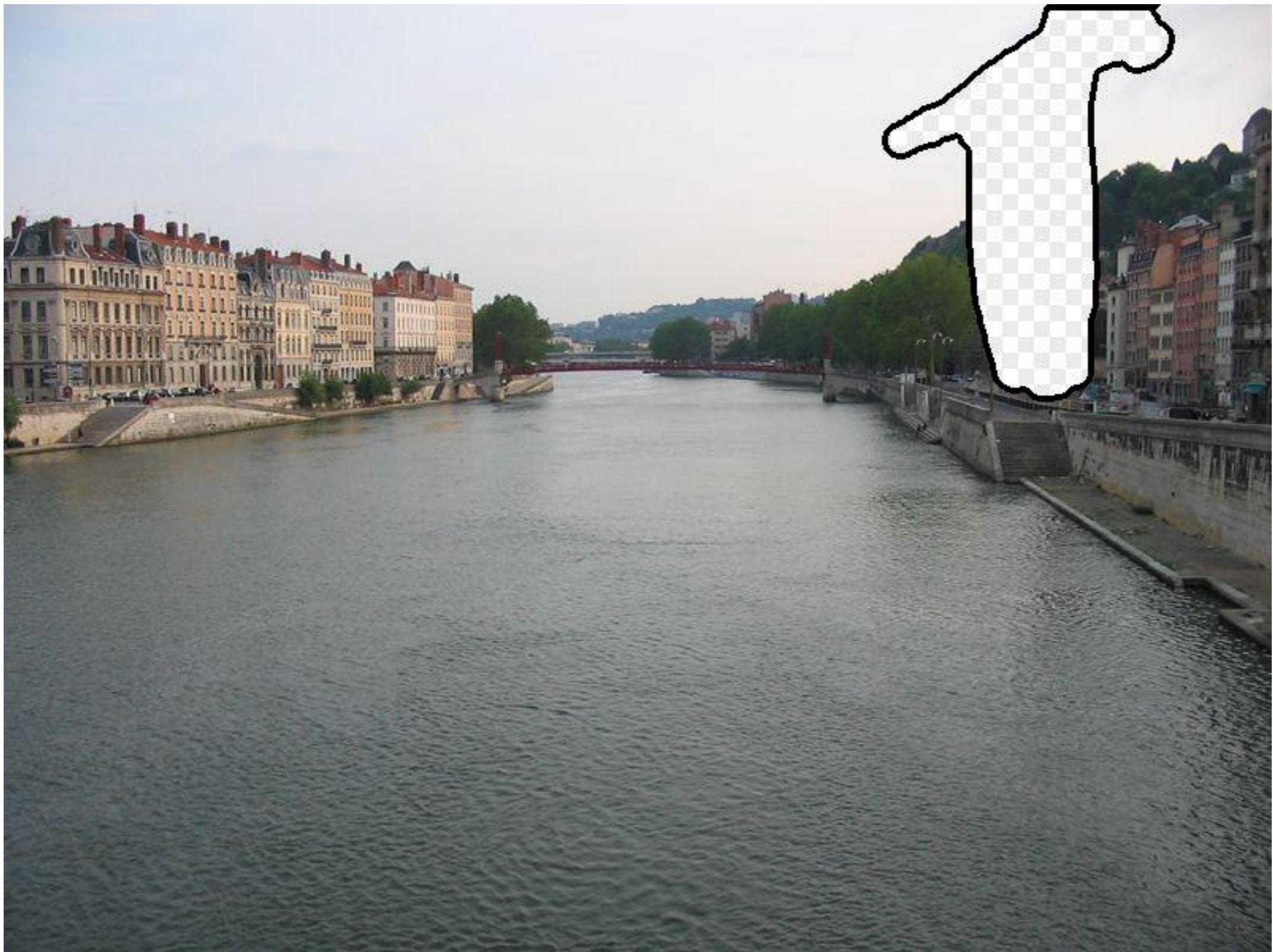
Hays and Efros, SIGGRAPH 2007













Weighted K-NN for Regression

- Given: Training data $\{(x_1, y_1), \dots, (x_n, y_n)\}$
 - Attribute vectors: $x_i \in X$
 - Target attribute $y_i \in \mathcal{R}$
- Parameter:
 - Similarity function: $K : X \times X \rightarrow \mathcal{R}$
 - Number of nearest neighbors to consider: k
- Prediction rule
 - New example x'
 - K-nearest neighbors: k train examples with largest $K(x_i, x')$

$$h(\vec{x}') = \frac{\sum_{i \in knn(\vec{x}')} y_i K(\vec{x}_i, \vec{x}')}{\sum_{i \in knn(\vec{x}')} K(\vec{x}_i, \vec{x}')}$$

Collaborative Filtering

Rating Matrix

	m_1	m_2	m_3	m_4	m_5	m_6
u_1		1	5		3	5
u_2		5	1	1	3	1
u_3		2	4		1	5
u	?	1	4	?	?	?

Recently Watched Top 10 for Thorsten

Overview of Nearest Neighbors

- Very simple method
- Retain all training data
 - Can be slow in testing
 - Finding NN in high dimensions is slow
- Metrics are very important
- Good baseline

Next Class:

Linear Regression and Least Squares