



DS&A Crash Course Review



# Arrays

- Arrays must be contiguous in memory
- Static arrays have a fixed size
- Dynamic arrays solve our space problem if we fill up the array with values and are the default for many languages such as Javascript or Python
- Whenever a dynamic array needs to be resized when adding new elements, it is  $O(n)$ . However, the amortized time complexity is  $O(1)$ .

Operations	Big-O Time
Read/ Write ith element	$O(1)$
Insert / Remove End	$O(1)$
Insert Middle or Beginning	$O(n)$
Remove Middle or Beginning	$O(n)$



# Array Algorithms

- Stacks
  - LIFO (last in, first out)
  - useful for when you are working with something in reverse order or need to do some backtracking
- Fixed Sliding Window
  - useful for when you're interested in the contents of a range
- Variable Sliding Window
  - useful when we want to find a min/max range for certain conditions
- Two Pointers
  - useful when we want are interested in two specific indices or values

Operations	Big-O Time
Push	$O(1)$
Pop	$O(1)$
Peek	$O(1)$



# Hash Sets / Maps

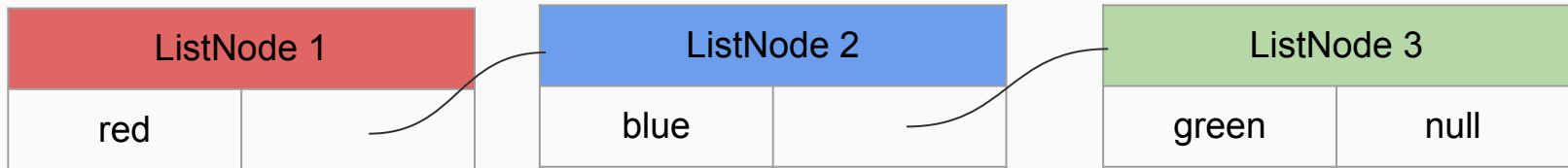
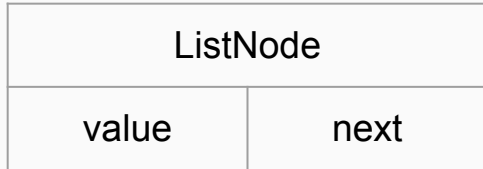
- Sets are a hash-like list of values
  - Useful when we need to keep track of unique values that should only appear once and do not need to be assigned to indices
- Maps and Objects store key-value pairs
  - maps are useful over objects when we want to use data types besides strings as keys

Operations	Big-O Time
Insert value	$O(1)$
Remove value	$O(1)$
Search value	$O(1)$



# Linked Lists

- Linked lists are made up of “list nodes”
- Each of these nodes encapsulate at minimum 2 components
  - Value
  - Pointer(s) to other nodes
- Linked lists are not contiguous in memory and instead use pointers to different parts of memory



# Linked Lists (cont.)

- \*\*\*Linked lists have great runtimes, but although reading, writing, and creating new values is technically  $O(1)$ , we often need to traverse the list to find the node (which is  $O(n)$ ).

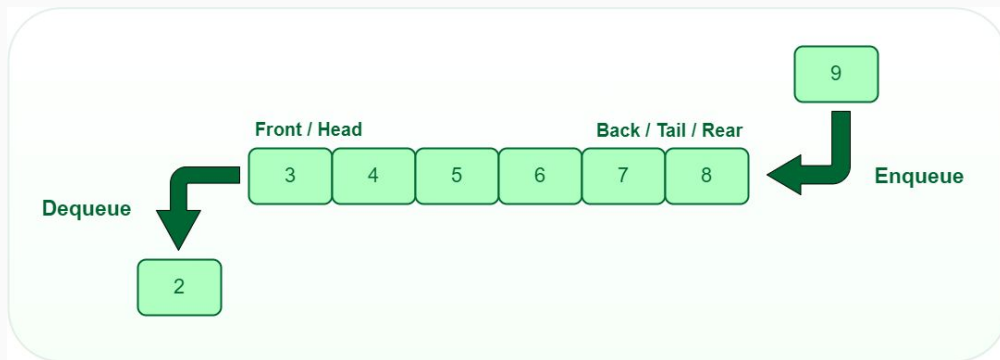
Operations	Big-O Time
Read/ Write ith element***	$O(1)$
Insert / Remove End	$O(1)$
Insert Middle or Beginning***	$O(1)$
Remove Middle or Beginning	$O(1)$



# Queues

- FIFO (first in, first out)
- Because we can add/remove nodes at the beginning of a Linked List in  $O(1)$  time, it is actually more efficient to create a queue this way versus an array.

Operations	Big-O Time
Enqueue	$O(1)$
Dequeue	$O(1)$

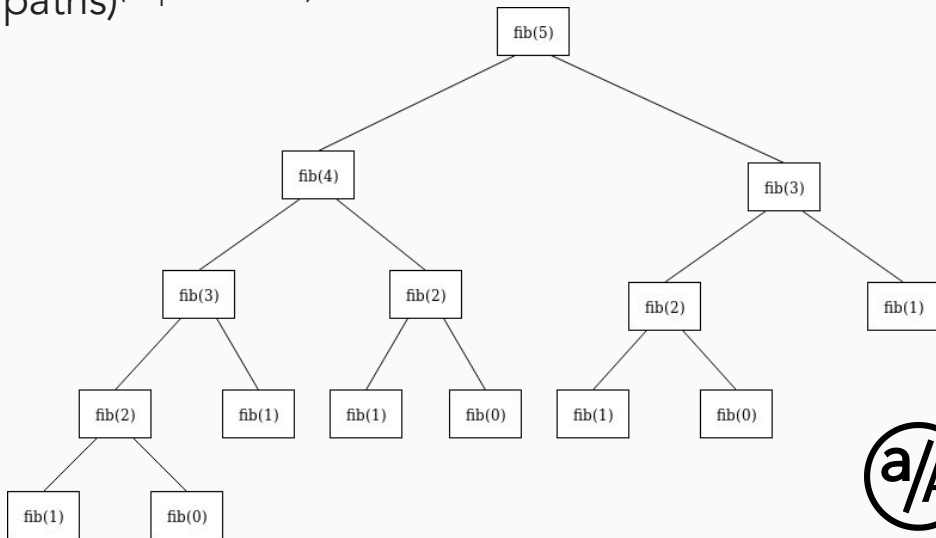


# Recursion

- Single-path recursive functions usually run in  $O(n)$  where  $n$  is the depth of the stack
- Recursion naturally uses a call stack, so it's perfect for DFS (which uses a stack)
- Multi-path recursive functions can be analyzed with the following formula:

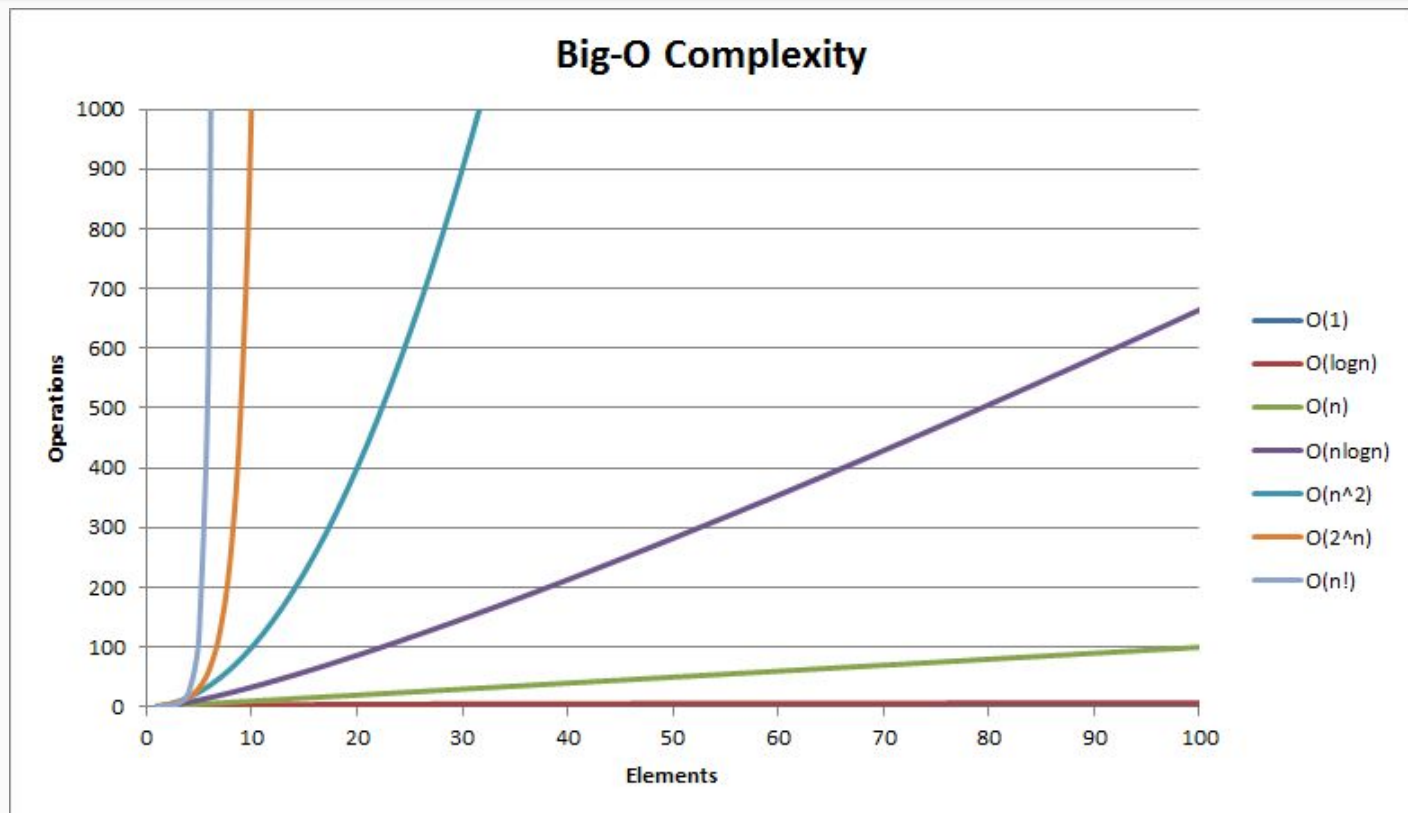
(# of paths)<sup>(depth of stack)</sup>

Operations	Big-O Time
Traverse	$O(P^D)$





# Big O Chart



# Amortized Complexity

- In most cases, we care about worst case scenarios
- However, amortized complexity is when the worst case scenario happens so infrequently that it's more useful to consider the average case scenario
  - Examples
    - Dynamic array push: worst case  $O(n)$ , amortized  $O(1)$
    - Quick sort: worst case  $O(n)$ , amortized  $O(\log(n))$



# Binary Search

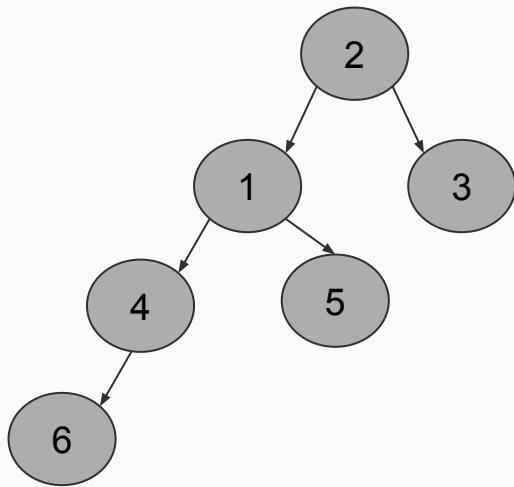
- Recursively cut input size by half to find something quickly
- Very efficient and one of the few algorithms that can run in  $O(\log(n))$

Operations	Big-O Time
Search	$O(\log(n))$



# Binary Trees

- Made up of nodes with left and right pointers
- Connected nodes have “parent-child” relationship.
- **leaf node** - A node without a child.
- **root** - A node without a parent.
- A node is an **ancestor** to **descendant** nodes.
- **height** - how far a node is from the leaf nodes.
- **depth** - how far a node from the root node.
- Binary search trees are sorted trees that allow for efficient searching



# Depth First Search

- Searches as deep into one path as possible before searching a different path
- 3 types (process node at diff times):

- In-order traversal
- Pre-order traversal
- Post-order traversal

Operations	Big-O Time
Search tree	$O(n)$

- Utilizes a stack

- This makes recursion perfect since recursion inherently uses a stack via the call stack!

```
var inorderTraversal = function(root) {  
  if (!root) return;  
  inorderTraversal(root.left);  
  console.log(root.val)  
  inorderTraversal(root.right);  
};
```

```
var preorderTraversal = function(root) {  
  if (!root) return;  
  console.log(root.val)  
  inorderTraversal(root.left);  
  inorderTraversal(root.right);  
};
```

```
var postorderTraversal = function(root) {  
  if (!root) return;  
  inorderTraversal(root.left);  
  inorderTraversal(root.right);  
  console.log(root.val)  
};
```



# Breadth First Search (BFS)

- Searches through nodes level by level
- We process nodes closest to the root first
- This algorithm is very useful when finding shortest paths or when dealing with layers
- Utilizes a queue
  - Because recursion uses a stack, we always want to just run BFS iteratively
- Steps
  - Add the root to the queue
  - Shift out a "current node" from the queue
  - Process current node
  - Push current node's children into the queue
  - Repeat process until queue is empty

Operations	Big-O Time
Search tree	$O(n)$



# Backtracking

- Backtracking is where we solve problems recursively by “building candidates” and then abandon those candidates (“backtrack”) once we determine that candidate can no longer yield a valid solution.
- Most common type of problem that can be solved with backtracking is “find all possible ways to do something”
- Backtracking problems run in exponential runtime.

```
// let curr represent the thing you are building  
// it could be an array or a combination of variables
```

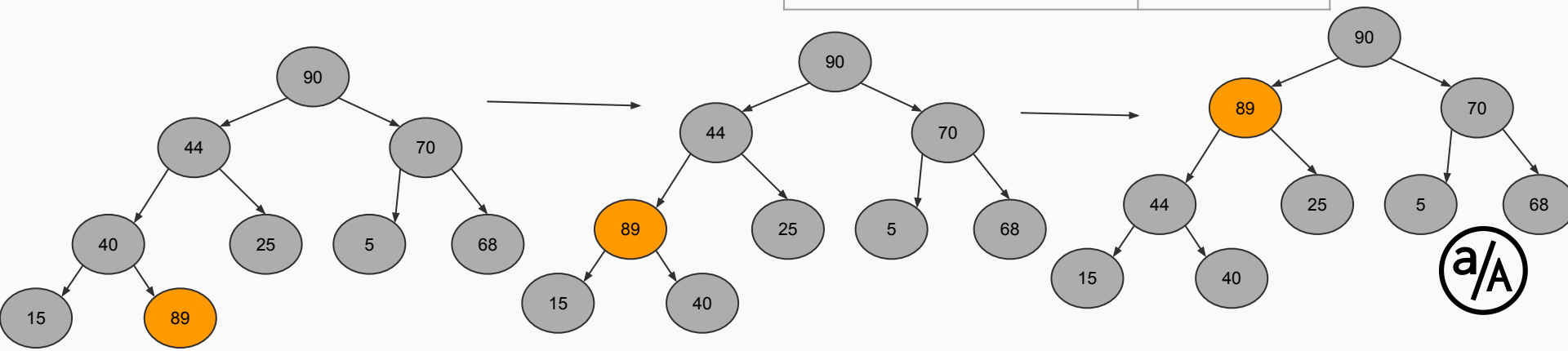
```
function backtrack(curr) {  
  if (base case) {  
    Increment or add to answer  
    return  
  }  
  
  for (iterate over input) {  
    Modify curr  
    backtrack(curr)  
    Undo whatever modification was done to curr  
  }  
}
```



# Heaps / Priority Queues

- A partially ordered complete binary tree that is useful for efficiently finding minimum or maximum values

Operations	Big-O Time
Push	$O(\log(n))$
Poll	$O(\log(n))$
Heapify	$O(n)$
Peek	$O(1)$





# Graphs

- A graph is simply a group of connected nodes
  - subsets of graphs include linked lists and trees
- Graphs can be **directed** or **undirected**, referring to whether edges point one way or both ways
- Graphs can be **disconnected**
- $E \leq V^2$ , where  $E$  = edges and  $V$  = vertices
- Ways to represent graphs:
  - Matrix
  - Adjacency Matrix
  - Adjacency List



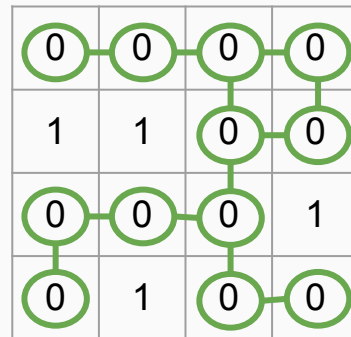
# Matrices

- Graphs represented as a 2D array
- Typically an 4-directional undirected graph, but it can also be 8-directional
- Coordinates represented with row and column indices
  - We can find values by using `grid[row][col]`
  - Some also use `x` and `y`, but I recommend against this because I've seen many people get confused during mock interviews.
- Commonly used for path representation

```
grid = [ [0, 0, 0, 0],  
         [1, 1, 0, 0],  
         [0, 0, 0, 1],  
         [0, 1, 0, 0] ]
```

0 = free

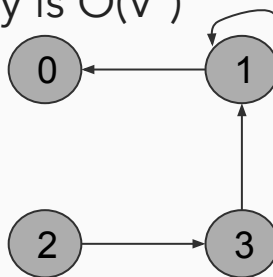
1 = blocked



# Adjacency Matrices

- The cells of a adjacency matrix are NOT nodes
- Instead, the indices represent vertices, and the values in the cells represent edges between vertices
- Always a square since both sides represent vertices
- Rare because it is space inefficient. Complexity is  $O(V^2)$
- Examples

- $\text{adjMatrix}[1][2] === 1$ 
  - An edge exists from vertex 1 to vertex 2
- $\text{adjMatrix}[2][1] === 1$ 
  - An edge exists from vertex 2 to vertex 1
  - Order matters!!
- $\text{adjMatrix}[0][1] === 0$ 
  - No edge exists from vertex 0 to vertex 1
- $\text{adjMatrix}[1][1] === 1$ 
  - There exists a self looping edge at vertex 1



$\text{adjMatrix} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 \end{bmatrix}$

	0	1	2	3
0	0	0	0	0
1	1	1	0	0
2	0	0	0	1
3	0	1	0	0



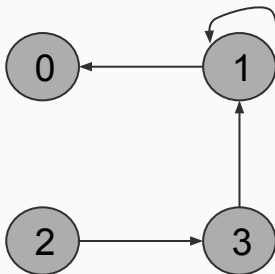
# Adjacency Lists

- Very common way to represent a graph
- Uses nodes, similar to linked lists or trees
- Unlike linked lists or trees, there is no predefined number of connected neighbors
- We can represent neighbors in an array or set
- Much more space efficient than adjacency matrix since we only represent nodes that actually exist.
- Sometimes may have to build the adjacency list ourselves

```
class GraphNode {  
    constructor(val) {  
        this.val = val;  
        this.neighbors = [];  
    }  
}
```

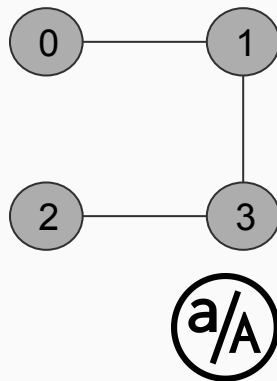
directed graph:

```
graph = {  
    0: [],  
    1: [0,1],  
    2: [3],  
    3: [1]  
}
```



undirected graph:

```
graph = {  
    0: [1],  
    1: [0,3],  
    2: [3],  
    3: [1,2]  
}
```



# Questions?

