

Verifying Low-Level Cryptographic Code: HACL*

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Outline

- Last week:
 - Side-Channel Attacks
 - Statically preventing them through noninterference
- Today:
 - Back to verifying implementations (and F^*)
 - Reasoning about low-level code
 - Proof engineering to scale verification

Reminder: The F* Proof Assistant



- A functional programming language
- With support for dependent types, refinement types, effects, ...
- Semi-automated verification by relying on SMT solving
- Extraction to OCaml, F#, C (under certain conditions)



- Try it online at <https://fstar-lang.org/tutorial/>
- Or install it locally: <https://github.com/FStarLang/FStar>

Reminder: The F* Effect System

- Separates between
 - Total functions: **Tot** t
 - Ghost functions: **GTot** t
 - Possibly non-terminating functions: **Dv** t
- Can include refinements for specifications

```
val factorial (n:int) : Pure int (requires n ≥ 0) (ensures fun y -> y ≥ 0)

val append_length (#a:Type) (l1 l2: list a) : Ghost unit
  (requires True)
  (ensures fun _ -> length l1 + length l2 == length (append l1 l2))
```

Stateful F* Programs

- F* provides a built-in effect for modeling and reasoning about stateful programs:

`ST t (requires fun h -> pre h) (ensures fun h0 r h1 -> post h0 r h1)`

- Reason about state using a standard Hoare logic (requires/ensures)
- `ST` models a state with garbage-collected references
- This model is in a partial correctness setting:
 - `Pure t <: ST t`, and `Div t <: ST t`

Stateful Programs: An Example

```
val incr (r:ref int) : ST unit  
  (requires fun h -> True)  
  (ensures fun h0 v h1 -> 1 + sel h0 r == sel h1 r)
```

```
let incr (r:ref int) = r := !r + 1
```

Specifying the Heap

```
val heap : Type
```

```
val ref : Type -> Type
```

```
val sel : #a:Type -> heap -> ref a -> GTot a
```

```
effect ST (a: Type) (pre: heap -> Type) (post: heap -> a -> heap -> Type) = ...
```

Heap Operations

```
val (!) (r:ref int) : ST int  
    (requires fun h -> True)  
    (ensures fun h0 v h1 -> h0 == h1  $\wedge$  sel h0 r == v)
```

```
val (:=) (r:ref int) (v: int) : ST unit  
    (requires fun h -> True)  
    (ensures fun h0 _ h1 -> sel h1 r == v)
```


Reasoning about Framing

```
val swap (r1 r2:ref int) : ST unit
  (requires fun h -> True)
  (ensures fun h0 _ h1 ->
    sel h0 r1 == sel h1 r2  $\wedge$  sel h0 r2 == sel h1 r1)
```

```
let swap r1 r2 =
  let v1 = !r1 in let v2 = !r2 in
  r1 := v2; r2 := v1
```

- Correct? What about aliasing? What part of memory does a write impact?

The Modifies Clause

```
val addr_of : #a:Type -> ref a -> GTot nat
```

```
let modifies (s:set nat) (h0 h1 : heap) = forall a (r:ref a).  
    not (addr_of r `mem` s) ==> sel h1 r == sel h0 r
```

```
val (:=) (r:ref int) (v: int) : ST unit  
    (requires fun h -> True)  
    (ensures fun h0 _ h1 ->  
        modifies {addr_of r} h0 h1 ∧  
        sel h1 r == v)
```

The Modifies Clause

```
val addr_of : #a:Type -> ref a -> GTot nat
```

```
let modifies (s:set nat) (h0 h1 : heap) = forall a (r:ref a).  
    not (addr_of r `mem` s) ==> sel h1 r == sel h0 r
```

```
val (:=) (r:ref int) (v: int) : ST unit  
    (requires fun h -> True)  
    (ensures fun h0 _ h1 ->  
        modifies !{r} h0 h1 ∧  
        sel h1 r == v)
```

Lighter notation for location sets

Applying the Modifies Clause, Intuitively

```
val swap (r1 r2:ref int) : ST unit
  (requires fun h -> addr_of r1 <> addr_of r2)
  (ensures fun h0 _ h1 ->
    sel h0 r1 == sel h1 r2  $\wedge$  sel h0 r2 == sel h1 r1)
```

```
let swap r1 r2 =
  let v1 = !r1 in let v2 = !r2 in // Does not modify memory
  r1 := v2;           // Only modifies location r1, r2 is left unchanged
  r2 := v1            // Only modifies location r2, r1 is left unchanged
```

Monadic Effects

- The ST effect can be seen as a state monad, with a bind operator

$G \vdash e1 : \text{ST } t1 \text{ (requires (fun } h0 \rightarrow \text{pre } h0)) \text{ (ensures (fun } h0 \text{ } x1 \text{ } h1 \rightarrow \text{post } h0 \text{ } x1 \text{ } h1))}$

$G, x1:t1 \vdash e2 : \text{ST } t2$

$\text{(requires (fun } h1 \rightarrow \text{exists } h0. \text{post } h0 \text{ } x1 \text{ } h1))}$

$\text{(ensures (fun } h1 \text{ } x2 \text{ } h2 \rightarrow \text{post}' h1 \text{ } x2 \text{ } h2))}$

$G \vdash \text{let } x1 = e1 \text{ in } e2 : \text{ST } t2$

$\text{(requires (fun } h0 \rightarrow \text{pre}))$

$\text{(ensures (fun } h0 \text{ } x2 \text{ } h2 \rightarrow \text{exists } x1 \text{ } h1. \text{post } h0 \text{ } x1 \text{ } h1 \wedge \text{post}' h1 \text{ } x2 \text{ } h2))}$

Consequence Rule

$G \vdash e1 : ST\ t1\ (\text{requires}\ (\text{fun } h0 \rightarrow \text{pre } h0))\ (\text{ensures}\ (\text{fun } h0\ x1\ h1 \rightarrow \text{post } h0\ x1\ h1))$

$G \models \text{forall } h0. \text{pre}'\ h0 \Rightarrow \text{pre } h0$

$G \models \text{forall } h0\ x1\ h1. \text{post } h0\ x1\ h1 \Rightarrow \text{post}'\ h0\ x1\ h1$

 $G \vdash e1 : ST\ t1\ (\text{requires}\ (\text{fun } h0 \rightarrow \text{pre}'\ h0))\ (\text{ensures}\ (\text{fun } h0\ x1\ h1 \rightarrow \text{post}'\ h0\ x1\ h1))$

Monadic Effects, Example

```
let swap r1 r2 =  
  let v1 = !r1 in let v2 = !r2 in  
    (* Know (P1): exists h1 (v1, v2). h0 == h1 /\ v1 == sel h0 r1 /\ v2 == sel h0 r2 *)  
    r1 := v2;  
    (* Know (P2): exists h2 (). modifies !{r1} h1 h2 /\ sel h2 r1 == v2 *)  
    r2 := v1  
    (* Know (P3): exists h3 (). modifies !{r2} h2 h3 /\ sel h3 r2 == v1 *)
```

Monadic Effects, Example

(Pre): $\text{addr_of } r1 \neq \text{addr_of } r2$

(P1): $\text{exists } h1 (v1, v2). h0 == h1 \wedge v1 == \text{sel } h0 \ r1 \wedge v2 == \text{sel } h0 \ r2$

(P2): $\text{exists } h2 (). \text{ modifies } !\{r1\} \ h1 \ h2 \wedge \text{sel } h2 \ r1 == v2$

(P3): $\text{exists } h3 (). \text{ modifies } !\{r2\} \ h2 \ h3 \wedge \text{sel } h3 \ r2 == v1$

Goal: $\text{sel } h0 \ r1 == \text{sel } h3 \ r2 \wedge \text{sel } h0 \ r2 == \text{sel } h3 \ r1$

(P3): $\text{sel } h3 \ r2 == v1 \implies \text{sel } h0 \ r1 \text{ (P1)}$



(P2): $\text{sel } h2 \ r1 == v2 \implies \text{sel } h0 \ r2 \text{ (P1)}$

(P3) gives *modifies* $!\{r2\} \ h2 \ h3$.

By definition of *modifies* and (Pre), we derive $\text{sel } h3 \ r1 == \text{sel } h2 \ r1 \implies \text{sel } h0 \ r2$



Modifies Theory

`let` modifies s h0 h1 = `forall` r. `addr_of` r \notin s \implies `sel` h1 r == `sel` h0 r

- Transitivity:

`modifies` s1 h0 h1 \wedge `modifies` s2 h1 h2 \Rightarrow `modifies` (union s1 s2) h0 h2

- Inclusion:

$s1 \subseteq s2 \wedge$ `modifies` s1 h0 h1 \Rightarrow `modifies` s2 h0 h1

Exercises

- Stateful Sum
- Stateful Factorial

Richer Memory Models

- The stateful effect seen so far offers an OCaml-like memory model
 - A reference in scope is assumed to be live
 - References are not manually memory-managed
- We want to reason about C code:
 - Need to reason about liveness, more complex datastructures, stack vs heap, ...
- **Idea:** Keep the stateful effect, but change the underlying state to provide a C-like memory model

The Low* Framework

- Low* is a shallow embedding of a subset of C into F*

```
val memcpy (dst : buffer uint64) (src : buffer uint64)  
  : Stack unit  
  (requires  $\lambda h \rightarrow \text{length } \text{dst} == \text{length } \text{src} \wedge \text{live } h \text{ dst} \wedge \text{live } h \text{ src}$ )  
  (ensures  $\lambda h0 \_ h1 \rightarrow \text{modifies } (\text{loc\_buffer } \text{dst}) h0 h1$ )
```

Low* Machine Integers

- A model of C integers, e.g., uint32
- Specified using "mathematical" integers

`val v (n: UInt32.t) : GTot nat`

- Arithmetic operations can lead to overflow/underflow

`val add (n1 n2: UInt32.t) : Pure UInt32.t
(ensures $\lambda x \rightarrow v\ x == (v\ n1 + v\ n2) \% 2^{32}$)`

- Operations for signed integers require to avoid over/underflows

`val add (n1 n2: Int32.t) : Pure UInt32.t
(requires $(v\ n1 + v\ n2) < 2^{31}$)
(ensures $\lambda x \rightarrow v\ x == v\ n1 + v\ n2$)`

Low* Arrays: Specification

- At the core of the Low* memory model, named *buffers* for historical reasons
- Represented in memory as a sequence of values:

```
val buffer : Type -> Type
```

```
val as_seq : #a:Type -> mem -> buffer a -> GTot (seq a)
```

Low* Arrays: Core API

- Usable through an API that ensures *spatial* and *temporal memory safety*

```
val index (#a:Type) (b : buffer a) (n:UInt32.t{v n < length b})  
  : Stack a  
  (requires  $\lambda h \rightarrow \text{live } h \ b$ )  
  (ensures  $\lambda h_0 \ x \ h_1 \rightarrow h_0 == h_1 \wedge x == \text{Seq.index (as\_seq } h_0 \ b) (v \ n)$ )
```

- Very similar signature for upd

Low* Arrays: Pointer Arithmetic

- Low* allows (controlled) pointer arithmetic, to access a sub-array from a live array

```
val sub (#a:Type) (b : buffer a) (start: UInt32.t) (len: ghost UInt32.t)  
  : Stack (buffer a)  
  (requires  $\lambda h \rightarrow \text{live } h \ b \wedge v \ \text{start} + v \ \text{len} \leq \text{length } b$ )  
  (ensures  $\lambda h_0 \ x \ h_1 \rightarrow h_0 == h_1 \wedge \text{sub\_spec } b \ (v \ \text{start}) \ (v \ \text{len})$ )
```

- This corresponds in C to the operation `b + start`
- The modifies clause is also extended to reason about possible overlaps between arrays and slices

Low* Arrays: Allocation

- Low* provides functions to create new arrays (i.e., allocate) either on the heap (malloc) or on the stack
- Newly created arrays are assumed to be live, and with a location disjoint from all previously created arrays

Modeling Stack and Heap

- Instead of a monolithic memory model, the heap is divided into a tree of regions (conceptually, `mem = map region_id heap`)
- A specific subset of these regions models the *C stack*
- Two different effects: **ST** for arbitrary stateful computations, and **Stack** for computations only allocating in the current stack frame
- Clients can create a stack frame in a function using `push/pop_frame()`

Modeling Stack and Heap, Formally

```
effect Stack (a:Type) (pre: mem -> prop) (post: mem -> a -> mem -> prop) = ST a  
  (requires  $\lambda h \rightarrow \text{pre } h$ )  
  (ensures  $\lambda h_0 \times h_1 \rightarrow \text{post } h_0 \times h_1 \wedge \text{equal\_domains } h_0 \ h_1$ )
```

```
let equal_domains (m0: mem) (m1: mem) =  
  // The current top stack-frame is the same  
  m0.tip == m1.tip  $\wedge$   
  // The trees of heaps have the same shape  
  Set.equal (Map.domain m0.h) (Map.domain m1.h)  $\wedge$   
  // For each heap, the used addresses are the same  
  (forall r. Map.contains m0.h r ==>  
    Heap.equal_dom (Map.sel m0.h r) (Map.sel m1.h r))
```

A Complete (Toy) Low* Example

```
let main (): Stack Int32.t (requires  $\lambda \_ \rightarrow \text{True}$ ) (ensures  $\lambda \_ \_ \_ \rightarrow \text{True}$ ) =  
  push_frame ();  
  let b: buffer UInt32.t = alloca 0ul 8ul in  
  upd b 0ul 255ul;  
  pop_frame ();  
  0l
```



```
int32_t main(void) {  
  uint32_t b[8U] = { 0U };  
  b[0U] = 255U;  
  return (int32_t)0;  
}
```

Extracting Low* Code

- Low* code can be extracted to C through the KaRaMeL compiler (<https://github.com/FStarLang/karamel>)
- KaRaMeL recognizes Low*-specific types and functions (e.g., buffer uint8 and upd), and translates them to standard C types and operations (e.g., uint8[] and assignment)
- The resulting code can be compiled with standard C compilers, and integrated in unverified projects

The KaRaMeL Compiler: Design Goals

- Produce idiomatic, readable C code
 - Despite verification, extracted code will likely be reviewed and audited by users
- Remain as simple as possible
 - Semantic preservation is proven on paper, however the implementation is trusted, the codebase needs to remain small
- Support a pragmatic subset of C
 - We control the Low* code we want to extract, we only need a reasonable subset of features for verifying real-world code, not the entire C standard

KaRaMeL: Producing Idiomatic Code

- KaRaMeL retrieves the F* AST after ghost code erasure
- Many compilation micropasses:
 - Unused Argument Elimination (often for extra unit arguments)
 - Inductives with a single constructor become structs
 - Empty structs are removed
 - Inductives with constant constructors (e.g., type $t = A \mid B$) are extracted to enums
 - ...
- Also preserves original variable names, can preserve code comments, attempts to eliminate temporary variables, ...

Low* Extraction Limitations

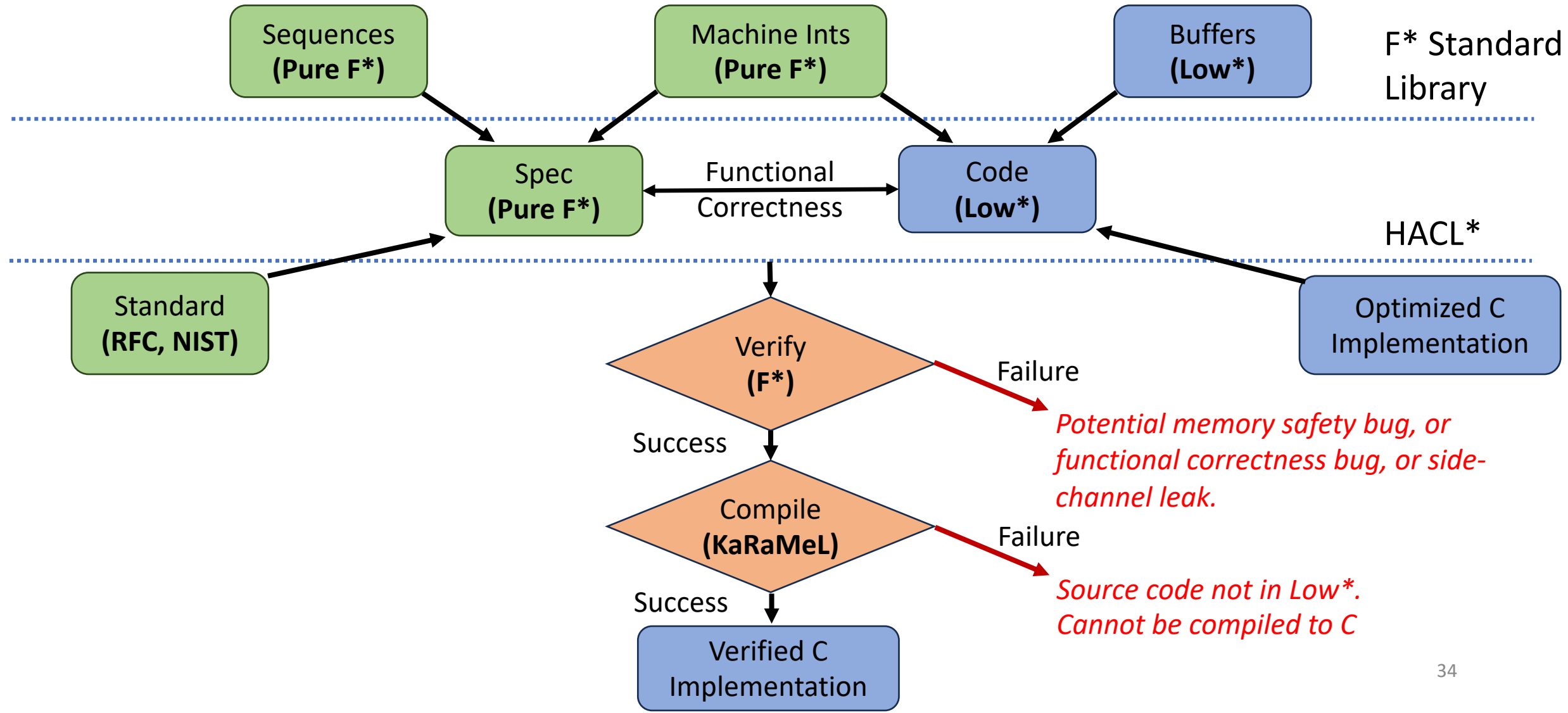
- Types with no equivalent in C (e.g., mathematical integers, sequences)
- Recursive datatypes (e.g., OCaml-style lists or trees)
- Polymorphism
 - KaRaMeL however monomorphizes code as much as possible before failing, so some *uses* of polymorphic functions and datatypes can be extracted
- Higher-order (beyond simple versions)
- Closures

All of these remain available for verification! But must be erased before reaching KaRaMeL

Using Low*: The HACL* Crypto Library

- HACL*: A verified, comprehensive cryptographic provider
- Provides guarantees about memory safety, functional correctness, resistance against side-channels
- ~150k lines of F* code compiling to ~100k lines of C (and Assembly) code
- 30+ algorithms (hashes, authenticated encryption, elliptic curves, ...)
- Integrated in Linux, Firefox, Tezos, and many more

Verification Workflow



Example: Poly1305 MAC Algorithm

- Poly1305 is a message authentication code

$$\text{poly}(k, m, w_1 \dots w_n) = (m + w_1 k^1 + \dots + w_n k^n) \% (2^{130} - 5)$$

- It authenticates a message $w_1 \dots w_n$ by:
 - Encoding it as a polynomial in the prime-field modulo $2^{130} - 5$
 - Evaluating it at point k (first part of the key)
 - Masking the result with m (second part of the key)

Specifying Poly1305

- The specification comes from the official RFC
- The specification is our **ground truth**: it needs to be as simple and easy to review as possible
- The specification also needs to be **executable**: We can then “test” it on standard test vectors
- **Solution**: We write an inefficient but straightforward implementation in Pure F*, and benefit from extraction to OCaml

Specifying Poly1305

```
let prime = pow2 130 - 5
```

```
let felem = x: nat{x < prime}
```

```
let fadd (x: felem) (y: felem) : felem = (x + y) % prime
```

```
let fmul (x: felem) (y: felem) : felem = (x * y) % prime
```

```
type key = s:seq uint8{length s == 32}
```

```
...
```

Implementing Poly1305

Several steps:

1. Create a bignum library for representing field elements
2. Optimize prime-specific field arithmetic
3. Implement Poly1305, and expose the corresponding API

Bignum Library for $\mathbb{Z}/(2^{130}-5)\mathbb{Z}$

- The numbers are too large to fit machine integers
- We use an unsaturated 44-44-42 representation
- feval allows to retrieve the corresponding mathematical number

```
type felem = b:buffer uint64{length b = 3}
```

```
let feval (h: mem) (f: felem) : GTot Spec.felem =  
  let s = as_seq h f in  
  (v s.[0] + v s.[1] * pow2 44 + v s.[2] * pow2 88) % Spec.prime
```

Implementing Field Arithmetic

```
val fadd (a b : felem) : Stack unit
  (requires  $\lambda h \rightarrow \text{live } h \ a \wedge \text{live } h \ b \wedge$ 
    disjoint a b  $\wedge$ 
    no_overflow h a b)
  (ensures  $\lambda h0 \_ h1 \rightarrow \text{modifies } (\text{loc } a) \ h0 \ h1 \wedge$ 
    feval h1 a == Spec.fadd (feval h0 a) (feval h1 a)
  )
```

This specification guarantees:

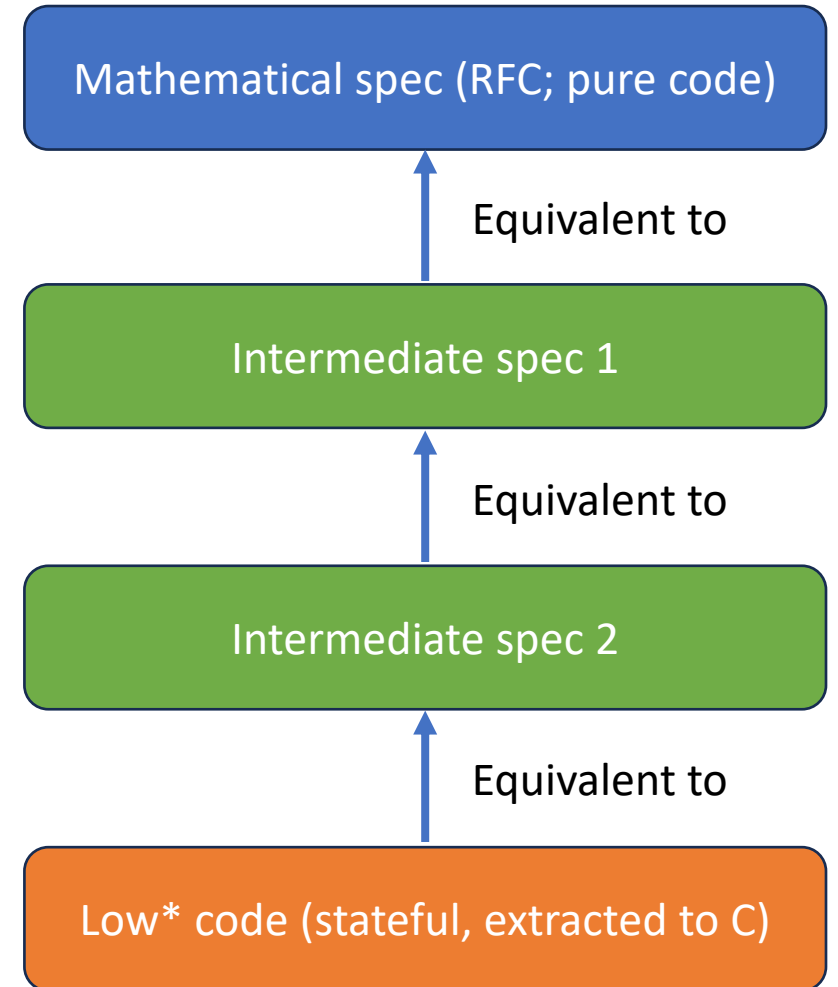
- Memory Safety
- Functional Correctness
- Side-Channel Resistance (omitted here, see last week)

Optimizing Field Arithmetic

- Many possible optimizations are purely algorithmic:
 - Replace a modular reduction by a Barrett reduction
 - Replace a modular multiplication by a Montgomery multiplication
- These are orthogonal from memory optimizations (e.g., unsaturated memory representation of bignums)
- Ideally, we want to reason about them in isolation to simplify verification

Proof by Refinement

- We write intermediate specifications
- Each layer is proven semantically equivalent to the layer above
- We can reason independently about different elements in each layer (algorithmic optimization, memory layout, aliasing, ...)



Example: Modular Exponentiation

```
let rec exp (g: int) (n: nat) = if n = 0 then 1 else g * exp g (n-1)    // Simple spec
```

```
let rec exp_opt (g:int) (n:nat) =  
  if n = 0 then 1  
  else if n % 2 = 0 then exp_opt (g*g) (n/2)  
  else g * exp_opt (g*g) (n-1/2)
```

```
let equiv_proof (g:int) (n:nat) : Lemma (exp g n == exp_opt g n)
```

- *exp* and *exp_opt* are in the pure fragment of F^* . Proving equivalence only requires reasoning about mathematical facts, not about memory

Example: Modular Exponentiation

```
val exp_opt (g:int) (n:nat) : int
```

```
type felem_spec = s: seq uint64{length s == 3}
```

```
let feval_spec (f: felem_spec) : int = (v s.[0] + v s.[1] * pow2 44 + v s.[2] * pow2 88)
```

```
let fexp_spec (f: felem_spec) (n:uint64) : felem_spec = ...
```

```
val equiv_proof (f: felem_spec) (n: uint64) : Lemma (  
    feval_spec (fexp_spec f n) == exp_opt (feval_spec f) (v n))
```

- Introduce low-level representation of integers using *mathematical sequences*

Example: Modular Exponentiation

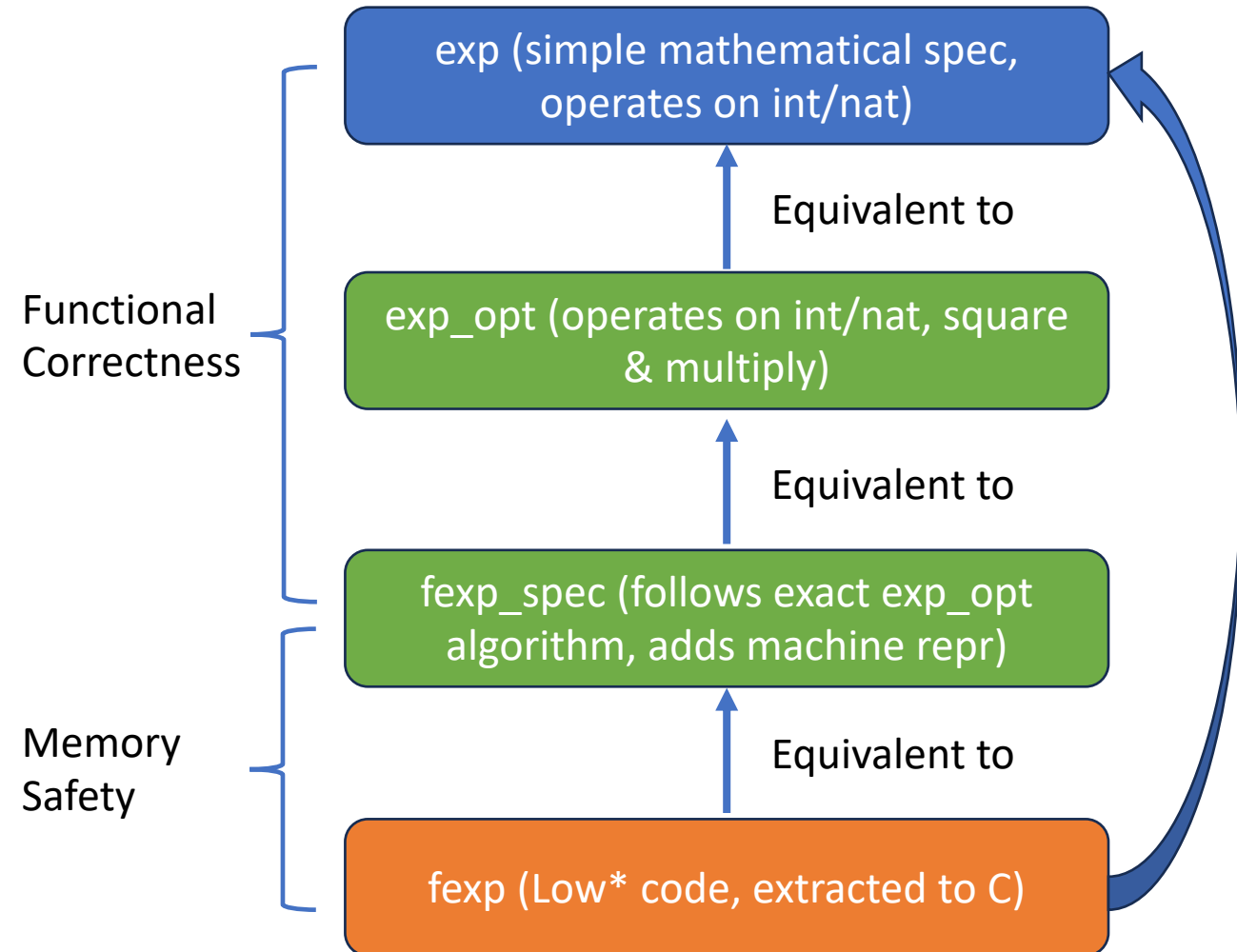
```
type felem = b:buffer uint64{length b = 3}
```

```
val fexp (a : felem) (n: uint64) : Stack unit  
  (requires  $\lambda h \rightarrow \text{live } h \ a \wedge \text{live } h \ b \wedge \text{disjoint } a \ b \wedge$   
            $\text{no\_overflow } h \ a \ b$ )  
  (ensures  $\lambda h0 \_ h1 \rightarrow \text{modifies } (\text{loc } a) \ h0 \ h1 \wedge$   
            $\text{as\_seq } h1 \ a == \text{fexp\_spec } (\text{as\_seq } h0 \ a) \ n$ )  
  )
```

- Introduce memory reasoning (aliasing, disjointness)
- The implementation of fexp closely follows the structure of fexp_spec

Modular Exponentiation: Summary

- Equivalence proofs at each layer compose to provide an end-to-end proof
- Using different layers allows to separate proofs into independent parts
- How to separate and how many layers to create is up to the proof engineer



Implementing Poly1305

```
[@"substitute"]
val poly1305_last_pass_ :
  acc:felem →
  Stack unit
  (requires (λ h → live h acc ∧ bounds (as_seq h acc) p44 p44 p42))
  (ensures (λ h0 h1 → live h0 acc ∧ bounds (as_seq h0 acc) p44 p44 p42
    ∧ live h1 acc ∧ bounds (as_seq h1 acc) p44 p44 p42
    ∧ modifies_1 acc h0 h1
    ∧ as_seq h1 acc == Hacl.Spec.Poly1305_64.poly1305_last_pass_spec_ (as_seq h0 acc)))

[@"substitute"]
let poly1305_last_pass_acc =
  let a0 = acc.(0ul) in
  let a1 = acc.(1ul) in
  let a2 = acc.(2ul) in
  let open Hacl.Bignum.Limb in
  let mask0 = gte_mask a0 Hacl.Spec.Poly1305_64.p44m5 in
  let mask1 = eq_mask a1 Hacl.Spec.Poly1305_64.p44m1 in
  let mask2 = eq_mask a2 Hacl.Spec.Poly1305_64.p42m1 in
  let mask = mask0 & ^ mask1 & ^ mask2 in
  UInt.logand_lemma_1 (v mask0); UInt.logand_lemma_1 (v mask1); UInt.logand_lemma_1 (v mask2);
  UInt.logand_lemma_2 (v mask0); UInt.logand_lemma_2 (v mask1); UInt.logand_lemma_2 (v mask2);
  UInt.logand_associative (v mask0) (v mask1) (v mask2);
  cut (v mask = UInt.ones 64 ⇒ (v a0 ≥ pow2 44 - 5 ∧ v a1 = pow2 44 - 1 ∧ v a2 = pow2 42 - 1));
  UInt.logand_lemma_1 (v Hacl.Spec.Poly1305_64.p44m5); UInt.logand_lemma_1 (v Hacl.Spec.Poly1305_64.p44m1);
  UInt.logand_lemma_1 (v Hacl.Spec.Poly1305_64.p42m1); UInt.logand_lemma_2 (v Hacl.Spec.Poly1305_64.p44m5);
  UInt.logand_lemma_2 (v Hacl.Spec.Poly1305_64.p44m1); UInt.logand_lemma_2 (v Hacl.Spec.Poly1305_64.p42m1);
  let a0' = a0 - ^ (Hacl.Spec.Poly1305_64.p44m5 & ^ mask) in
  let a1' = a1 - ^ (Hacl.Spec.Poly1305_64.p44m1 & ^ mask) in
  let a2' = a2 - ^ (Hacl.Spec.Poly1305_64.p42m1 & ^ mask) in
  upd_3 acc a0' a1' a2'
```

memory safety

math spec

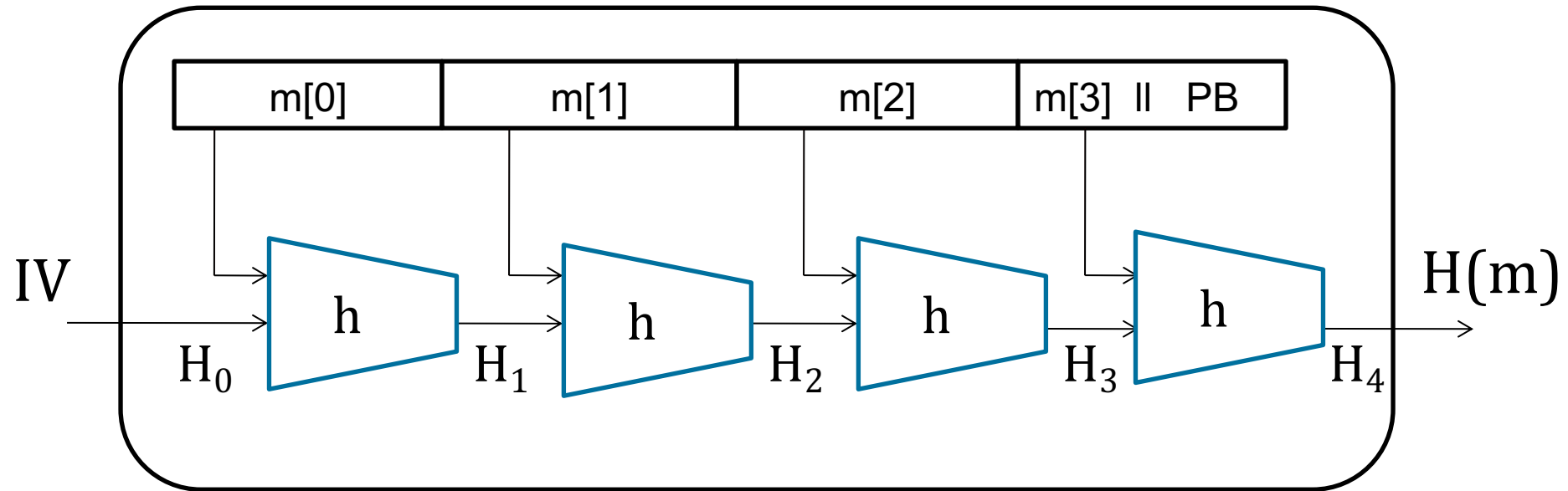
code

proof

```
static void Hacl_Impl_Poly1305_64_poly1305_last_pass(uint64_t *acc)
{
  Hacl_Bignum_Fproduct_carry_limb(acc);
  Hacl_Bignum_Modulo_carry_top(acc);
  uint64_t a0 = acc[0];
  uint64_t a10 = acc[1];
  uint64_t a20 = acc[2];
  uint64_t a0_ = a0 & (uint64_t)0xffffffff;
  uint64_t r0 = a0 >> (uint32_t)44;
  uint64_t a1_ = (a10 + r0) & (uint64_t)0xffffffff;
  uint64_t r1 = (a10 + r0) >> (uint32_t)44;
  uint64_t a2_ = a20 + r1;
  acc[0] = a0_;
  acc[1] = a1_;
  acc[2] = a2_;
  Hacl_Bignum_Modulo_carry_top(acc);
  uint64_t i0 = acc[0];
  uint64_t i1 = acc[1];
  uint64_t i0_ = i0 & (((uint64_t)1 << (uint32_t)44) - (uint64_t)1);
  uint64_t i1_ = i1 + (i0 >> (uint32_t)44);
  acc[0] = i0_;
  acc[1] = i1_;
  uint64_t a00 = acc[0];
  uint64_t a1 = acc[1];
  uint64_t a2 = acc[2];
  uint64_t mask0 = FStar_UInt64_gte_mask(a00, (uint64_t)0xffffffff);
  uint64_t mask1 = FStar_UInt64_eq_mask(a1, (uint64_t)0xffffffff);
  uint64_t mask2 = FStar_UInt64_eq_mask(a2, (uint64_t)0x3ffffffff);
  uint64_t mask = mask0 & mask1 & mask2;
  uint64_t a0_0 = a00 - ((uint64_t)0xffffffff & mask);
  uint64_t a1_0 = a1 - ((uint64_t)0xffffffff & mask);
  uint64_t a2_0 = a2 - ((uint64_t)0x3ffffffff & mask);
  acc[0] = a0_0;
  acc[1] = a1_0;
  acc[2] = a2_0;
}
```

The Need for Generic Implementations

- Families of cryptographic algorithms often share the same structure



MD5, SHA-1, SHA2-224, SHA2-256, SHA2-384, SHA2-512

The Need for Generic Implementations

- Families of cryptographic algorithms often share the same structure
- Implementing many high-quality variants is tedious and time-consuming
- Verification makes it even more costly
- Can we reason about implementations generically?

Generic SHA2 Implementations

```
let state (a : sha2_alg) = match a with  
  | SHA2_224 | SHA2_256 -> buffer uint32  
  | SHA2_384 | SHA2_512 -> buffer uint64
```

```
let bitwise_and #a (x y: state a) : state a =  
  if alg == SHA2_224 || alg == SHA2_256 then UInt32.bitwise_and x y  
  else UInt64.bitwise_and x y
```

```
let shuffle (a: sha2_alg) ... = ... bitwise_and #a x y ...
```

- We can write a generic implementation of each basic block
- We then write SHA2 functions generically

Generic SHA2 Implementations: Issues

- Naive generality leads to poor performance

```
sha2_state bitwise_and (alg:sha2_alg, x:sha2_state, y:sha2_state) {  
    if (alg == SHA2_224 | alg == SHA2_256) {  
        return UInt32.bitwise_and(x, y);  
    } else {  
        return UInt64.bitwise_and(x, y);  
    }  
}
```

- At each arithmetic operation, we now have a branching
- For performance-critical code, this is unacceptable
- We want genericity, but it must not impact performance

Reminder: The F* Normalizer

- Dependently typed proof assistants include a *normalizer* which reduces computations.

```
assert_norm (length [1; 2; 3; 4; 5; 6; 7; 8; 9; 10] == 10)
```

```
match [1; 2; 3; 4; 5; 6; 7; 8; 9; 10] with | [] -> 0 | hd :: tl -> 1 + length tl == 10    ~
```

```
1 + match [2; 3; 4; 5; 6; 7; 8; 9; 10] with | [] -> 0 | hd :: tl -> 1 + length tl == 10    ~
```

```
...
```

```
10 == 10 ~
```

```
True
```

- Requires concrete terms, cannot reduce symbolic terms

Partial Evaluation and Inlining

- We rely on two mechanisms: *compile-time inlining*, and *partial evaluation* (which uses the normalizer under the hood)

`inline_for_extraction noextract`

```
let bitwise_and #a (x y: state a) : state a =  
  if alg == SHA2_224 || alg == SHA2_256 then UInt32.bitwise_and x y  
  else UInt64.bitwise_and x y
```

```
let shuffle (a: sha2_alg) ... = ... bitwise_and #a x y ...
```

Partial Evaluation and Inlining

- We rely on two mechanisms: *compile-time inlining*, and *partial evaluation*

```
let shuffle (a: sha2_alg) ... =  
    ...  
    if alg == SHA2_224 || alg == SHA2_256 then UInt32.bitwise_and x y  
    else UInt64.bitwise_and x y  
    ...
```

Partial Evaluation and Inlining

- We rely on two mechanisms: *compile-time inlining*, and *partial evaluation*

```
inline_for_extraction noextract
```

```
let shuffle (a: sha2_alg) ... =
```

```
  ...
```

```
    if alg == SHA2_224 || alg == SHA2_256 then UInt32.bitwise_and x y
```

```
    else UInt64.bitwise_and x y
```

```
  ...
```

```
let shuffle_224 = shuffle SHA2_224
```

Partial Evaluation and Inlining

- We rely on two mechanisms: *compile-time inlining*, and *partial evaluation*

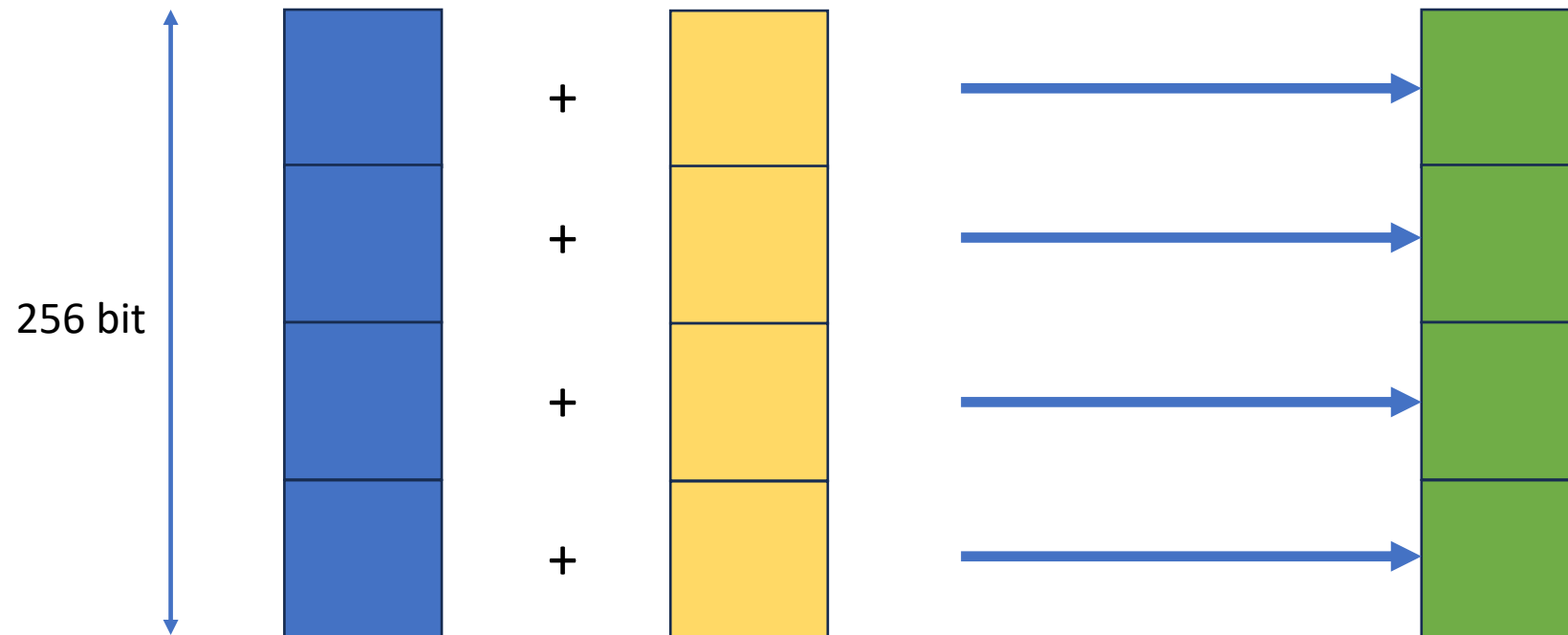
```
let shuffle_224 ... =  
  ...  
  if SHA2_224 == SHA2_224 || SHA2_224 == SHA2_256 then UInt32.bitwise_and x y  
  else UInt64.bitwise_and x y  
  ...
```



```
let shuffle_224 ... =  
  ...  
  UInt32.bitwise_and x y ...
```


SIMD Optimizations

- Modern CPUs offer SIMD (Single-instruction Multiple-Data) instructions for lightweight parallelism



SIMD Optimizations

- Crypto is highly amenable to SIMD-based optimizations
 - Process several blocks in parallel
 - Parallelize the inner block cipher in ChaCha20 (intended by designers)
 - 10-20x speedup on ChaCha20 using AVX512 SIMD parallelism
- However, SIMD instructions are platform-specific

```
master ▾  openssl / crypto / chacha / asm / chacha-x86_64.pl
1378  sub XOP_lane_ROUND {
1379  mv ($a0,$b0,$c0,$d0)=@ :
1828  sub AVX2_lane_ROUND {
1829  my ($a0,$b0,$c0,$d0)=@ ;
2486  sub AVX512ROUND {          # critical path is 14 "SIMD ticks" per round
2487      &vpadd ($a,$a,$b);
2488      &vpxord ($d,$d,$a);
```

- Maintaining optimized implementations for all platforms is hard

Verified Generic SIMD Crypto

- Similar technique as for SHA2, except, we abstract over vectorization level

```
val vec_t: w:width → Type
```

```
val (+|) : #w:width → vec_t w → vec_t w → vec_t w
```

- We then verify a generic implementation

```
let chacha20_init (w:width) (state:vec_t w) ... = ...
```

```
state.(a) <- state.(a) +| state.(b)
```

```
...
```

- And finally specialize many times

```
let chacha20_init_avx = chacha20_init 4
```

```
let chacha20_init_avx2 = chacha20_init 8
```

```
let chacha20_init_avx512 = chacha20_init 16
```

Higher-Order Combinators

- So far, this pattern applied to a parameter used for pattern-matching
- Cryptographic **constructions** frequently **combine** core operations.

Example:

- The **Merkle-Damgård construction** only requires an (abstract) compression function
- The construction consists of folding the core compression function over multiple blocks of data

Higher-Order Combinators

// Write once; this is not Low*

noextract inline_for_extraction

```
let mk_compress_blocks (a: hash_alg)
  (compress: compress_st a)
  (s: state a)
  (input: blocks)
  (n: u32 { length input = block_size a * n })
```

=

```
C.Loops.for 0u1 n (fun i ->
  compress s (Buffer.sub input (i * block_size a) (block_size a)))
```

// Specialize many times; now this is Low*

```
let compress_blocks_224 = mk_compress_blocks SHA2_224 compress_224
```

...

```
let compress_md5 = mk_compress_blocks MD5 compress_md5
```

...

Higher-Order and Partial Evaluation

- The methodology so far relies on partial evaluation and inlining

```
C.Loops.for 0ul n (fun i ->  
  compress s (Buffer.sub input (i * block_size a) (block_size a)))
```

- This would inline the entire compress function inside the loop

```
noextract inline_for_extraction  
let mk_hash (a: hash_alg)  
  (init: init_st a)  
  (compress_blocks: compress_blocks_st a)  
  (compress_last: compress_last_st a)  
  (extract: extract_st a)
```

- Worse as combinator complexity grows. We need another methodology for generic code

Encoding Functors: Associative List Example

OCaml:

```
module type Map = sig
  type k
  val find: k -> (k * 'a) list -> 'a option
end

module type EqType = sig
  type t
  val eq: t -> t -> bool end

module MkMap (E : EqType) :
  Map with type k = E.t = struct
  type k = E.t
  let find x ls =
    let b = ref true in
    let lsp = ref ls in
    while !b do
      match !lsp with
      | [] -> b := false
      | (x', _) :: tl ->
        if E.eq x x' then b := false
        else lsp := tl done;
    match !lsp with
    | [] -> None
    | (_, y) :: _ -> Some y
  end
```

Doesn't compile to C
(same with typeclasses)

Type constraint

We want a loop in the generated code

F*:

Replace with a linked list

```
type map (a : Type) = {
  k: Type;
  find: k -> list (k * a) -> ST (option a) ... }

type eq_type = {
  t: Type;
  eq: t -> t -> bool; }

let mk_map (e : eq_type) (a : Type) :
  m:map a{m.k == e.t} = {
  k = e.t;
  find = (fun x ls ->
    let b = alloc true in
    let lsp = alloc ls in
    while (fun () -> !* b)
      (fun () ->
        let ls = !* lsp in
        match ls with
        | [] -> upd b false
        | (x', _) :: tl ->
          if e.eq x x' then upd b false
          else upd lsp tl);
    match !* lsp with
    | [] -> None
    | (_, y) :: _ -> Some y) }
```

Dictionary has runtime cost

Refinement

Proofs and annotations omitted

Extraction to C?

⇒ Specialization and partial evaluation?

Zero-Cost Functors: First Attempt (i)

Generic code (F*):

```
type map (a : Type) = {
  k: Type;
  find: k -> list (k * a) -> ST (option a) ... }

type eq_type = {
  t: Type;
  eq: t -> t -> bool; }

let mk_map (e : eq_type) (a : Type) :
  m:map a{m.k == e.t} = {
  k = e.t;
  find = (fun x ls ->
    let b = alloc true in
    let lsp = alloc ls in
    while (fun () -> !* b)
      (fun () ->
        let ls = !* lsp in
        match ls with
        | [] -> upd b false
        | (x', _) :: tl ->
          if e.eq x x' then upd b false
          else upd lsp tl);
    match !* lsp with
    | [] -> None | (_, y) :: _ -> Some y) }
```

Specialization:

```
let str_eqty : eq_type = { t = string; eq = String.eq; }
let ifind = (mk_map str_eqty int).find
```

After partial evaluation: **Types are specialized**

```
let ifind (x: string) (ls: list (string * int)) option int =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () ->
      let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if String.eq x x'
        then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None | (_, y) :: _ -> Some y
```

e.eq is inlined

What happens if the code has several layers?

Zero-Cost Functors: First Attempt (ii)

Peer device for a secure channel protocol:

```
(* "Module signature" *)
type dv = {
  pid : Type;
  send : pid -> list (pid * ckey) -> bytes -> option bytes;
  recv : pid -> list (pid * ckey) -> bytes -> option bytes; }
```

```
(* "Module implementation" *)
type cipher = {
  enc : ckey -> bytes -> bytes;
  dec : ckey -> bytes -> option bytes; }

let mk_dv (m : map ckey) (c : cipher) : d:dv{d.pid == m.k} = {

  pid = m.k;

  send = (fun id dv plain ->
    match m.find id dv with
    | None -> None
    | Some sk -> Some (c.enc sk plain));

  recv = (fun id dv secret ->
    match m.find id dv with
    | None -> None
    | Some sk -> c.dec sk secret)
}
```



Zero-Cost Functors: Encoding

Parameterize with eq

```
inline_for_extraction noextract
let mk_find (k v : Type) (eq: k -> k -> bool) (x: k) (ls: list (k * v)) : option v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with | [] -> upd b false
      | (x', _) :: tl -> if eq x x' then upd b false else upd lsp tl);
  match !* lsp with | [] -> None | (_, y) :: _ -> Some y
```

```
(* Don't inline ifind *)
let ifind = mk_find i String.eq
```

Cumbersome to write and maintain

```
inline_for_extraction noextract
let mk_send (pid : Type) (find : pid -> list (pid * ckey) -> option ckey) (enc : ckey -> bytes -> bytes)
  (id : pid) (dv : list (pid * ckey)) (plain : bytes) : option bytes =
  match find id dv with
  | None -> None
  | Some sk -> Some (enc sk plain)
```

```
(* Don't inline isend *)
let isend = mk_send string ifind aes_enc

... (* mk_rcv and irec *)
```

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
let find (k v : Type) (eq: k-> k -> bool)
  (x: k) (ls: list (k * v)): option v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

What we want to get:

```
let mk_find (k v : Type) (eq: k-> k -> bool)
  (x: k) (ls: list (k * v)): option v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
val eq (k : Type): k -> k -> bool

let find (k v : Type)
  (x: k) (ls: list (k * v)): option v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq k x x' then upd b false
        else upd lsp tl);
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      | [] -> upd b false
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        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
assume val eq (k : Type): k -> k -> bool

let find (k v : Type)
  (x: k) (ls: list (k * v)): option v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq k x x' then upd b false
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      | [] -> upd b false
      | (x', _) :: tl ->
        if eq k x x' then upd b false
        else upd lsp tl);
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    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
type mindex = { k : Type; v : Type }

assume val eq (i : mindex): i.k -> i.k -> bool

let find (i : mindex) (x : i.k)
  (ls : list (i.k * i.v)) : option i.v =
  let b = alloc true in
  let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () ->
      let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
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  | [] -> None | (_, y) :: _ -> Some y
```

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  (x: i.k) (ls: list (i.k * i.v)): option i.v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

Zero-Cost Functors: Call-graph Rewriting

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```
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let find (i : minindex) (x : i.k)
  (ls : list (i.k * i.v)) : option i.v =
  let b = alloc true in
  let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () ->
      let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None | (_, y) :: _ -> Some y
```

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type minindex = { k : Type; v : Type }

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  (x: i.k) (ls: list (i.k * i.v)): option i.v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

```
%splice [ mk_find ] (specialize (`minindex) [`find ])
```

Call-graph rewriting by means
of meta-programming

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
type minindex = { k : Type; v : Type }

assume val eq (i : minindex): i.k -> i.k -> bool

let find (i : minindex) (x : i.k)
  (ls : list (i.k * i.v)) : option i.v =
  let b = alloc true in
  let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () ->
      let ls = !* lsp in
      match ls with
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```

What we want to get:

```
type minindex = { k : Type; v : Type }

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  (x: i.k) (ls: list (i.k * i.v)): option i.v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

The code is re-checked

```
%splice [ mk_find ] (specialize (`minindex) [`find ])
```

**Call-graph rewriting by means
of meta-programming**

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
type minindex = { k : Type; v : Type }

assume val eq (i : minindex): i.k -> i.k -> bool

let find (i : minindex) (x : i.k)
  (ls : list (i.k * i.v)) : option i.v =
  let b = alloc true in
  let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () ->
      let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None | (_, y) :: _ -> Some y
```

What we want to get:

```
type minindex = { k : Type; v : Type }

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  (x: i.k) (ls: list (i.k * i.v)): option i.v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

The code is re-checked

```
%splice [ mk_find ] (specialize (`minindex) [`find ])
```

Call-graph rewriting by means
of meta-programming

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
type mindex = { k : Type; v : Type }

[@ Specialize]
assume val eq (i : mindex): i.k -> i.k -> bool

[@ Eliminate]
let while_cond (b: pointer bool) (_:unit) = !*b

[@ Eliminate]
let while_body (i: mindex) (b: pointer bool)
  (lsp: list (i.k * i.v)) (x:i.k) (_:unit) =
  let ls = !* lsp in
  match ls with
  | [] -> upd b false
  | (x', _) :: tl ->
    if eq x x' then upd b false
    else upd lsp tl

[@ Specialize]
let find (i : mindex) (x : i.k)
  (ls : list (i.k * i.v)) : option i.v =
  let b = alloc true in
  let lsp = alloc ls in
  while (while_cond b) (while_body i b lsp x);
  match !* lsp with
  | [] -> None | (_, y) :: _ -> Some y
```

What we want to get:

```
type mindex = { k : Type; v : Type }

let mk_find (i: mindex) (eq: i.k-> i.k -> bool)
  (x: i.k) (ls: list (i.k * i.v)): option i.v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

The code is re-checked

```
%splice [ mk_find ] (specialize (`mindex) [`find ])
```

Call-graph rewriting by means
of meta-programming

Zero-Cost Functors: Call-graph Rewriting

What we want to write:

```
type mindex = { k : Type; v : Type }

[@ Specialize]
assume val eq (i : mindex): i.k -> i.k -> bool

[@ Eliminate]
let while_cond (b: pointer bool) (_:unit) = !*b

[@ Eliminate]
let while_body (i: mindex) (b: pointer bool)
  (lsp: list (i.k * i.v)) (x:i.k) (_:unit) =
  let ls = !* lsp in
  match ls with
  | [] -> upd b false
  | (x', _) :: tl ->
    if eq x x' then upd b false
    else upd lsp tl

[@ Specialize]
let find (i : mindex) (x : i.k)
  (ls : list (i.k * i.v)) : option i.v =
  let b = alloc true in
  let lsp = alloc ls in
  while (while_cond b) (while_body i b lsp x);
  match !* lsp with
  | [] -> None | (_, y) :: _ -> Some y
```

What we want to get:

```
type mindex = { k : Type; v : Type }

let mk_find (i: mindex) (eq: i.k-> i.k -> bool)
  (x: i.k) (ls: list (i.k * i.v)): option i.v =
  let b = alloc true in let lsp = alloc ls in
  while (fun () -> !* b)
    (fun () -> let ls = !* lsp in
      match ls with
      | [] -> upd b false
      | (x', _) :: tl ->
        if eq x x' then upd b false
        else upd lsp tl);
  match !* lsp with
  | [] -> None
  | (_, y) :: _ -> Some y
```

The code is re-checked

**Also applicable to protocol
implementations (e.g., Noise*)!**

```
%splice [ mk_find ] (specialize (`mindex) [`find ])
```

**Call-graph rewriting by means
of meta-programming**

The HPKE Example

Hybrid Public Key Encryption
draft-irtf-cfrg-hpke-06

Abstract

This document describes a scheme for hybrid public-key encryption (HPKE). This scheme provides authenticated public key encryption of arbitrary-sized plaintexts for a recipient public key. HPKE works

- Generic in three classes of algorithms
 - Authenticated Encryption with Additional Data (AEAD)
 - Key Encapsulation Mechanism (KEM)
 - Key Derivation Function (KDF)
- 24 possible ciphersuites, many more implementations

A Generic, Verified HPKE Implementation

- Abstract over algorithms to verify a generic implementation (800 lines)

```
val hpke_encrypt: cs:ciphersuite -> aead_encrypt cs -> ...
```

- Instantiate and extract each desired version/implementation (10 lines)

```
let hpke_encrypt_avx_aes = hpke_encrypt (AESGCM, ...) aes_encrypt_avx  
let hpke_encrypt_avx2_aes = hpke_encrypt (AESGCM, ...) aes_encrypt_avx2
```

- Call-graph rewriting yields a specialized, idiomatic implementation.
Calls to encrypt call directly into the corresponding AES-GCM library

Genericity: A Summary

- No performance hit due to genericity ("zero-cost abstraction")
- Reduces maintenance of verified code (only one generic implementation to maintain)
- Lowers development cost of new variants
 - Adding a new SIMD architecture only requires providing a model for basic operations (add, mul, ...) and extending a few datatypes
 - Adding a new HPKE ciphersuite only requires 10 lines of code (assuming the underlying primitives are implemented)

HACL* and Low*: Summary

- **Low***: A subset of F^* , modeling a well-behaved subset of C
- **HACL***: A comprehensive, verified cryptographic library written in Low*, yielding human-readable, high-performance C code
- Specifications are executable and directly translated from RFCs
- Proof methodology relies on successive refinements to separate verification conditions
- Engineering methodology relies on generic implementations, which are specialized at extraction-time through partial evaluation and metaprogramming