

# **Acing UTME Maths**

A Comprehensive Guide with Past Questions and Solutions

**By**

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# Dedication and Acknowledgements

This work is dedicated to our families, whose unwavering support has been our greatest strength throughout this journey. Their constant encouragement and belief in our abilities have fueled our passion and perseverance in creating this resource.

We would also like to express our sincere gratitude to the following individuals and institutions for their invaluable contributions:

- Our mentors and teachers, who instilled in us a love for mathematics and equipped us with the knowledge and skills needed to succeed.
- The examiners and administrators of the UTME, whose dedication to educational standards ensures a fair and effective assessment process.
- Our colleagues and friends, who provided feedback and support throughout the development of this book.
- The wider academic community, whose research and publications have laid the foundation for our understanding of mathematics.

We are truly grateful for the collective effort that has made this book possible. We hope that it will be a valuable resource for students preparing for the UTME and beyond.

## A Note on Preparation

This book was meticulously prepared using the  $\text{\LaTeX}$  document processing system, a powerful tool for typesetting high-quality scientific and mathematical texts. The diagrams herein were crafted using the TikZ package. We extend our thanks to the developers of the  $\text{\LaTeX}$  system and the numerous packages that made this work possible.

## About the Authors

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# Preface

Welcome to “Acing UTME Maths”, a comprehensive guide designed to help you conquer the upcoming UTME Maths exam. This book provides you with a wealth of past questions, detailed solutions, and insightful strategies to enhance your understanding and preparation.

This book is organized into chapters that follow the official UTME Maths syllabus, covering all key topics and subtopics. Each chapter includes a variety of past questions carefully selected to reflect the types and difficulty levels encountered in the actual exam.

In addition to past questions, we have provided detailed solutions that explain the reasoning behind each step and highlight common mistakes to avoid. We encourage you to work through these solutions carefully and utilize them as learning tools to improve your problem-solving skills.

Furthermore, we have incorporated valuable strategies throughout the book, offering tips and techniques to maximize your efficiency and performance on the exam. These strategies will help you manage your time effectively, approach different question types confidently, and overcome any challenges you may encounter.

We are confident that “Acing UTME Maths” will be your ultimate companion on your journey to success. By diligently working through the material and utilizing the resources provided, you will gain the knowledge, skills, and confidence needed to achieve your desired score on the UTME Mathematics exam.

Best of luck!

Ayodeji Adesegun and Chimobi Nwafor

# Chapter 1

## Number and Numeration

### 1.1 Number Bases

#### 1.1.1 Questions

- The number 25 when converted from the tens and units base to the binary base (base 2) is:
  - 10011
  - 1111011
  - 111000
  - 11001
  - 110011
  - $M102_5$
  - $M2002_5$
  - $M3024_5$
- A woman bought 4 bags of rice at  $N56$  per bag and 3 tins of milk at  $N4$  per tin. What is the total cost of the items she bought?
  - $N245$
  - $N242$
  - $N236$
  - $N341$
  - $N338$
- Evaluate  $212_3 - 121_3 + 222_3$ .
  - $313_3$
  - $1000_3$
  - $1020_3$
  - $1222_3$
  - $1213_3$
- A trader in a country where the currency 'MONT' ( $M$ ) is in base five bought  $103_5$  oranges at  $M14_5$  each. If he sold the oranges at  $M24_5$  each, what would be his gain?
  - $M103_5$
  - $M1030_5$
  - $M102_5$
  - $M2002_5$
  - $M3024_5$
- Find  $x$  if  $(x_4)^2 = (100100)_2$ .
  - 6
  - 12
  - 100
  - 210
  - 10042
- Convert  $241_5$  to base 8.
  - $71_8$
  - $107_8$
  - $176_8$
  - $241_8$
- In the equation  $\frac{11_2}{x_2} = \frac{1000_2}{x_2 + 101_2}$ , solve for  $x$ .
  - 101
  - 11
  - 110
  - 111
  - 10
- $4243_5 - 12x4_5 = y344_5$ . What is the difference between  $x$  and  $y$ ?
  - 4
  - 2
  - 1

- D. 3  
E. 5
9. In base ten, the number  $101101_2$  equals:  
A. 15  
B. 45  
C. 23  
D. 12
10. Convert the number 39 to base 2.  
A. 100111  
B. 111001  
C. 110111  
D. 111111  
E. 100101
11. Find  $n$  if  $34_n = 10110_2$ .  
A. 5  
B. 6  
C. 7  
D. 8  
E. 9
12. If  $2_9 \times (Y3)_9 = 3_5 \times (Y3)_5$ , find the value of  $Y$ .  
A. 4  
B. 3  
C. 2  
D. 1  
E. 5
13. Simplify  $213_4 \times 23_4$ .  
A.  $10321_4$   
B.  $12231_4$   
C.  $13221_4$   
D.  $10311_4$   
E.  $13021_4$
14.  $55_x + 52_x = 77_{10}$ , find  $x$ .  
A. 5  
B. 6  
C. 7  
D. 8  
E. 10
15. If  $x_{10} = 23_5$ , find  $x$ .  
A. 15  
B. 12  
C. 14  
D. 13  
E. 16
16. Find the sum of  $25_6, 52_6, 43_6$  in base 8.  
A. 411  
B. 141  
C. 114  
D. 417
17. If  $2A3_3 = 77_8$ , find  $A$ .  
A. 1  
B. 2  
C. 0  
D. 4
18. Evaluate  $(202_3)^2 - (112_3)^2$ .  
A. 21112  
B. 21121  
C. 21011  
D. 21120
19. If  $321_4$  is divided by  $23_4$  and leaves a remainder  $r$ , what is the value of  $r$ ?  
A. 4  
B. 2  
C. 3  
D. 0  
E. 1
20. Convert  $521_{10}$  to a number in base 5.  
A.  $1404_5$   
B.  $4041_5$   
C.  $4140_5$   
D.  $4014_5$   
E.  $4104_5$
21. If  $6R7_8 = 511_9$ , find  $R$ .  
A. 6  
B. 5  
C. 3  
D. 2  
E. 8

22. Find the value of  $x$  if  $121_x + 112_x = 30_{10}$ .
- A. 5  
B. 7  
C.  $-\frac{9}{2}$   
D. 3  
E. 4
23. Evaluate  $(1011_2)^2 - 1012_2$ .
- A.  $110000_2$   
B.  $110000_2$   
C.  $101011_2$   
D.  $110110_2$
24. Add  $1101_2$ ,  $11011_2$  and  $111_2$ .
- A.  $110110_2$   
B.  $101011_2$   
C.  $111011_2$   
D.  $101010_2$   
E.  $110011_2$
25. Find the value of  $m$  if  $13_m + 24_m = 41_m$ .
- A. 8  
B. 5  
C. 4  
D. 6  
E. 3
26. If  $125_x = 20_{10}$ , find  $x$ .
- A. 2  
B. 3  
C. 4  
D. 6  
E. 5
27. If  $(K2)_6 \times 3_6 = 3_5(K4)_5$ , what is the value of  $k$ ?
- A. 2  
B. 1  
C. 3  
D. 4  
E. 5
28. Find  $P$ , if  $451_6 - P_7 = 305_6$ .
- A.  $116_7$   
B.  $62_7$   
C.  $611_7$   
D.  $142_7$
29. The sum of four numbers is  $1214_5$ . What is the average expressed in base 5?
- A. 141  
B. 411  
C. 417  
D. 114  
E. 471
30. If  $(1P03)_4 = 115_{10}$ , find  $P$ .
- A. 2  
B. 0  
C. 1  
D. 4  
E. 3
31. If  $(P344)_6 - (23P2)_6 = (2PP2)_6$ , find the digit  $P$ .
- A. 1  
B. 2  
C. 3  
D. 4  
E. 5
32.  $4243_5 - (12X4)_5 = Y344$ . What is the difference between  $X$  and  $Y$ ?
- A. 1  
B. 2  
C. 3  
D. 4  
E. 5
33. Convert  $67_{10}$  to base 2.
- A.  $1000011_2$   
B.  $1000101_2$   
C.  $1100011_2$   
D.  $1010011_2$
34. Evaluate  $1101_2 + 1011_2$ .
- A.  $11000_2$   
B.  $10110_2$   
C.  $11010_2$   
D.  $11100_2$
35. If  $432_x = 156_{10}$ , find  $x$ .



- A. 5  
B. 6  
C. 7  
D. 8
36. Convert  $1234_5$  to base 10.  
A. 194  
B. 189  
C. 204  
D. 214
37. Simplify  $321_4 + 132_4$ .  
A.  $1123_4$   
B.  $1213_4$   
C.  $1203_4$   
D.  $1130_4$
38. If  $101_x + 11_x = 1000_x$ , find  $x$ .  
A. 2  
B. 3  
C. 4  
D. 5
39. Evaluate  $10110_2 - 1101_2$ .  
A.  $1001_2$   
B.  $1011_2$   
C.  $111_2$   
D.  $1111_2$
40. Convert  $255_{10}$  to base 16.  
A.  $FF_{16}$   
B.  $FE_{16}$   
C.  $EF_{16}$   
D.  $F0_{16}$
41. If  $212_3 \times 2_3 = x_3$ , find  $x$ .  
A.  $1201_3$   
B.  $1101_3$   
C.  $2021_3$   
D.  $1011_3$
42. Find  $n$  if  $144_n = 100_{10}$ .  
A. 6  
B. 7  
C. 8  
D. 9
43. Convert  $345_6$  to base 8.  
A.  $215_8$   
B.  $225_8$   
C.  $205_8$   
D.  $235_8$
44. Evaluate  $111_2 \times 101_2$ .  
A.  $100011_2$   
B.  $110011_2$   
C.  $100111_2$   
D.  $101011_2$
45. If  $54_x = 34_{10}$ , find  $x$ .  
A. 5  
B. 6  
C. 7  
D. 8
46. Simplify  $2134_5 + 3421_5$ .  
A.  $11110_5$   
B.  $11010_5$   
C.  $10110_5$   
D.  $11210_5$
47. Convert  $1000000_2$  to base 10.  
A. 64  
B. 128  
C. 32  
D. 256
48. If  $ABC_{16} = x_{10}$ , where  $A = 10, B = 11, C = 12$ , find  $x$ .  
A. 2748  
B. 2847  
C. 2784  
D. 2874
49. Evaluate  $1010_2 \div 10_2$ .  
A.  $101_2$   
B.  $110_2$   
C.  $100_2$   
D.  $111_2$
50. If  $234_x + 123_x = 412_x$ , find  $x$ .

- A. 5  
B. 6  
C. 7  
D. 8
51. Convert  $72_{10}$  to base 8.  
A.  $110_8$   
B.  $100_8$   
C.  $111_8$   
D.  $120_8$
52. Simplify  $444_5 - 232_5$ .  
A.  $212_5$   
B.  $202_5$   
C.  $222_5$   
D.  $112_5$
53. If  $1011_2 \times x_2 = 101101_2$ , find  $x$ .  
A.  $11_2$   
B.  $101_2$   
C.  $111_2$   
D.  $1001_2$
54. Convert  $1010101_2$  to base 10.  
A. 85  
B. 95  
C. 75  
D. 65
55. Evaluate  $432_5 \times 3_5$ .  
A.  $2341_5$   
B.  $2441_5$   
C.  $2141_5$   
D.  $2041_5$
56. If  $3x4_5 = 59_{10}$ , find  $x$ .  
A. 1  
B. 2  
C. 3  
D. 4
57. Convert  $156_{10}$  to base 7.  
A.  $312_7$   
B.  $315_7$   
C.  $321_7$   
D.  $314_7$
58. Simplify  $11011_2 + 10111_2 + 1101_2$ .  
A.  $110001_2$   
B.  $111001_2$   
C.  $101001_2$   
D.  $110101_2$
59. If  $x_4 \times 23_4 = 132_4$ , find  $x$ .  
A.  $2_4$   
B.  $3_4$   
C.  $10_4$   
D.  $11_4$
60. Evaluate  $10000_2 - 1111_2$ .  
A.  $1_2$   
B.  $10_2$   
C.  $11_2$   
D.  $1_2$
61. Convert  $1A3_{16}$  to base 10.  
A. 419  
B. 429  
C. 439  
D. 449
62. If  $201_x - 102_x = 22_x$ , find  $x$ .  
A. 3  
B. 4  
C. 5  
D. 6
63. Simplify  $2103_4 + 3012_4$ .  
A.  $11121_4$   
B.  $12111_4$   
C.  $11211_4$   
D.  $10321_4$
64. Convert  $500_{10}$  to base 9.  
A.  $615_9$   
B.  $605_9$   
C.  $625_9$   
D.  $616_9$
65. If  $110_2 \times 11_2 \times 10_2 = x_2$ , find  $x$ .  
A.  $100100_2$

- B.  $101100_2$   
 C.  $110100_2$   
 D.  $111100_2$
66. Evaluate  $543_6 - 254_6$ .  
 A.  $245_6$   
 B.  $255_6$   
 C.  $235_6$   
 D.  $225_6$
67. If  $1x2_3 + 201_3 = 1010_3$ , find  $x$ .  
 A. 0  
 B. 1  
 C. 2  
 D. 3
68. Convert  $1111111_2$  to base 10.  
 A. 127  
 B. 128  
 C. 255  
 D. 256
69. Simplify  $3421_5 \times 2_5$ .  
 A.  $13342_5$   
 B.  $14342_5$   
 C.  $12342_5$   
 D.  $13442_5$
70. If  $x_8 + 37_8 = 100_8$ , find  $x$ .  
 A.  $40_8$   
 B.  $41_8$   
 C.  $50_8$   
 D.  $51_8$
71. Convert  $200_{10}$  to base 6.  
 A.  $532_6$   
 B.  $542_6$   
 C.  $552_6$   
 D.  $512_6$
72. Evaluate  $111_2 + 111_2 + 111_2$ .  
 A.  $10101_2$   
 B.  $10011_2$   
 C.  $11001_2$   
 D.  $10111_2$
73. If  $43_x \times 2_x = 136_x$ , find  $x$ .  
 A. 5  
 B. 6  
 C. 7  
 D. 8
74. Convert  $3E7_{16}$  to base 10.  
 A. 997  
 B. 999  
 C. 987  
 D. 1007
75. Simplify  $1234_5 - 432_5$ .  
 A.  $302_5$   
 B.  $402_5$   
 C.  $312_5$   
 D.  $412_5$
76. If  $1101_2 \div x_2 = 11_2$ , find  $x$ .  
 A.  $10_2$   
 B.  $11_2$   
 C.  $100_2$   
 D.  $101_2$
77. Evaluate  $321_4 \times 12_4$ .  
 A.  $10302_4$   
 B.  $11302_4$   
 C.  $10202_4$   
 D.  $11202_4$
78. Convert  $1000_{10}$  to base 12.  
 A.  $6B4_{12}$   
 B.  $6A4_{12}$   
 C.  $694_{12}$   
 D.  $684_{12}$
79. If  $x2x_3 = 50_{10}$ , find  $x$ .  
 A. 1  
 B. 2  
 C. 0  
 D. 3
80. Simplify  $10111_2 - 1010_2 - 101_2$ .  
 A.  $1000_2$   
 B.  $1100_2$

- C.  $1010_2$   
D.  $1110_2$
81. Convert  $777_8$  to base 10.  
A. 511  
B. 521  
C. 501  
D. 531
82. If  $1x0_4 + 201_4 = 1011_4$ , find  $x$ .  
A. 0  
B. 1  
C. 2  
D. 3
83. Evaluate  $432_5 + 143_5 + 321_5$ .  
A.  $1401_5$   
B.  $1341_5$   
C.  $1441_5$   
D.  $1301_5$
84. Convert  $11001100_2$  to base 16.  
A.  $CC_{16}$   
B.  $CD_{16}$   
C.  $DC_{16}$   
D.  $DD_{16}$
85. If  $210_x \times 2_x = 1120_x$ , find  $x$ .  
A. 3  
B. 4  
C. 5  
D. 6
86. Simplify  $654_7 - 365_7$ .  
A.  $256_7$   
B.  $266_7$   
C.  $356_7$   
D.  $246_7$
87. Convert  $128_{10}$  to base 4.  
A.  $2000_4$   
B.  $1000_4$   
C.  $10000_4$   
D.  $3000_4$
88. If  $11x_4 = 23_{10}$ , find  $x$ .  
A. 1  
B. 2  
C. 3  
D. 0
89. Evaluate  $1111_2 \times 1111_2$ .  
A.  $11100001_2$   
B.  $11010001_2$   
C.  $11001001_2$   
D.  $11110001_2$
90. Convert  $343_5$  to base 10.  
A. 98  
B. 88  
C. 108  
D. 93
91. If  $x4_6 + 25_6 = 103_6$ , find  $x$ .  
A. 3  
B. 4  
C. 5  
D. 2
92. Simplify  $10101_2 + 11_2$ .  
A.  $11000_2$   
B.  $10111_2$   
C.  $11001_2$   
D.  $11010_2$
93. Convert  $99_{10}$  to base 3.  
A.  $10200_3$   
B.  $10020_3$   
C.  $10100_3$   
D.  $11000_3$
94. If  $231_x - 112_x = 114_x$ , find  $x$ .  
A. 5  
B. 6  
C. 7  
D. 8
95. Evaluate  $2413_5 + 1324_5$ .  
A.  $4242_5$   
B.  $4342_5$   
C.  $4142_5$

- D.  $4442_5$
96. Convert  $1024_{10}$  to base 2.
- A.  $10000000000_2$   
 B.  $100000000_2$   
 C.  $1000000000_2$   
 D.  $10000000_2$
97. The equation  $100_x \div 10_x = 10_x$  is true for all values of  $x$  except:
- A.  $x = 1$   
 B.  $x = 2$   
 C.  $x = 0$   
 D. Never true
98. Simplify  $333_4 + 222_4 + 111_4$ .
- A.  $1222_4$
- B.  $1332_4$   
 C.  $1232_4$   
 D.  $2222_4$
99. Convert  $B4_{16}$  to base 2.
- A.  $10110100_2$   
 B.  $10101100_2$   
 C.  $11010100_2$   
 D.  $10110010_2$
100. Solve for  $x$  in the equation  $23_x = 15_{10}$ .
- A. 5  
 B. 6  
 C. 7  
 D. 8

## 1.2 Fraction and Decimals

### 1.2.1 Questions

1. The sum of  $3\frac{7}{8}$  and  $1\frac{1}{3}$  is greater than the difference between  $\frac{3}{8}$  and  $1\frac{2}{3}$  by?
- A.  $3\frac{2}{3}$       C.  $8\frac{1}{8}$       E.  $5\frac{1}{4}$   
 B.  $1\frac{1}{2}$       D.  $3\frac{11}{12}$
2. After getting a rise of 15%, a man's new monthly salary is N 345. How much per month did he earn before the increase?
- A. N360      C. N293.25      E. N396.75  
 B. N300      D. N330
3. Find correct to 3 significant figures, the value of  $\sqrt{41830}$
- A. 647      C. 205      E. 6470  
 B. 2050      D. 647
4. 12 men complete a job in 9 days. How many men working at the same rate, would be required to complete the job in 6 days?
- A. 24      C. 8      E. 18  
 B. 9      D. 12
5. Simplify  $2\frac{5}{12} - 1\frac{7}{8} \times \frac{6}{5}$ .
- A.  $\frac{11}{30}$       C.  $\frac{1}{6}$       E.  $\frac{13}{20}$   
 B.  $\frac{9}{4}$       D.  $\frac{5}{3}$
6. By selling an article for N45.00 a man makes a profit of 8%. For how much should he have sold it in order to make a profit of 32%?
- A. N59.00      C. N180.00      E. N42.00  
 B. N55.00      D. N63.00
7. Which of the following fractions is less than one-third?
- A.  $\frac{4}{11}$       C.  $\frac{15}{44}$       E.  $\frac{6}{14}$   
 B.  $\frac{122}{383}$       D.  $\frac{22}{63}$
8. The ratio of the price of loaf of bread to the price of a packet of sugar in 1975 was  $a : x$ . In 1980, the price of a loaf of bread went up by 25% and that of a packet of sugar by 10%. Their new ratio is now ?
- A.  $50a : 44x$       C.  $40a : 44x$       E.  $44a : 55x$   
 B.  $44a : 50x$       D.  $55a : 44x$

9. Simplify:  $1 + \frac{2}{3 + \frac{4}{5 + \frac{6}{7}}}$
- A.  $\frac{7}{95}$   
 B.  $\frac{177}{95}$   
 C.  $\frac{233}{151}$   
 D.  $\frac{17}{10}$   
 E.  $\frac{3}{10}$
10. Evaluate and correct to 4 decimal places  $827.51 \times 0.015$ .
- A. 124.1265  
 B. 8.8415  
 C. 12.4127  
 D. 12.4120  
 E. 124.1265
11. A micrometer is defined as one millionth of a millimeter. A length of 12, 000 micrometer may be represented as
- A. 0.000012m  
 B. 0.12m  
 C. 0.00000012m  
 D. 0.00000000012m  
 E. 0.0000012m
12. The difference between  $4\frac{5}{7}$  and  $2\frac{1}{4}$  is greater than the sum of  $\frac{1}{14}$  and  $1\frac{1}{2}$  by?
- A.  $\frac{27}{28}$   
 B.  $\frac{23}{28}$   
 C.  $\frac{50}{56}$   
 D.  $\frac{48}{56}$   
 E.  $\frac{24}{48}$
13. When a dealer sells a bicycle for N81, he makes a profit of 8%. What did he pay for the bicycle.
- A. N75  
 B. N75.52  
 C. N74.52  
 D. N87.48  
 E. N73
14. A man and wife went to buy an article costing N400. The woman had 10% of the cost and the man 40% of the remainder. How much did they have altogether?
- A. N186  
 B. N184  
 C. N200  
 D. N144  
 E. N100
15. A sum of money invested at 5% per annum simple interest amount to N285.20 after 3 years. How long will it take the same sum to amount to N434.00 at  $7\frac{1}{2}\%$  per annum simple interest?
- A. 10 years  
 B. 12 years  
 C.  $7\frac{1}{2}$  years  
 D. 14 years  
 E. 5 years
16. A construction company is owned by two partners A and B and it is agreed that their profit will be divided in ratio 4 : 5, at the end of the year, B received N5, 000 more than A. What is the total profit of the company for the year?
- A. N45, 000  
 B. N30, 000  
 C. N150, 000  
 D. N25, 000  
 E. N30, 000
17. The diameter of metal rod is measured as 23.40cm to 4 significant figures. What is the maximum error in the measurement?
- A. 0.0004cm  
 B. 0.05cm  
 C. 0.005cm  
 D. 0.5cm  
 E. 0.45cm
18. Simplify:  $3 - \frac{2}{\frac{4}{5} + \frac{1}{2}}$

- A.  $1\frac{9}{10}$   
 B.  $1\frac{3}{10}$   
 C.  $1\frac{3}{4}$   
 D.  $-1$   
 E.  $1$
19. Given that  $x : y = \frac{1}{3} : \frac{1}{2}$  and  $\psi : \theta = \frac{2}{5} : \frac{4}{7}$ , find  $x : \theta$ .
- A.  $20 : 21$   
 B.  $7 : 15$   
 C.  $3 : 20$   
 D.  $2 : 35$   
 E.  $4 : 105$
20. If N560 is shared in the ratio  $7 : 2 : 1$ , what is the smallest share?
- A. N392  
 B. N113.40  
 C. N56.00  
 D. N87.48  
 E. N126.41
21. Simplify:  $\frac{1}{2} + \frac{1}{2 + \frac{1}{2 - \frac{1}{4 + \frac{1}{5}}}}$
- A.  $\frac{169}{190}$   
 B.  $-\frac{1}{3}$   
 C.  $\frac{13}{15}$   
 D.  $-\frac{3}{4}$   
 E.  $-\frac{14}{27}$
22.  $22\frac{1}{2}\%$  of the Nigerian Naira equals  $17\frac{1}{10}\%$  of a foreign currency  $M$ . What is the conversion rate of  $M$  to Naira?
- A.  $2\frac{11}{57}$  Naria  
 B.  $1\frac{18}{57}$  Naria  
 C.  $\frac{15}{59}$  Naria  
 D.  $\frac{15}{57}$  Naria  
 E.  $38\frac{1}{4}$  Naria
23. Divide the LCM of 48, 64, and 80 by their HCF.
- A. 30  
 B. 48  
 C. 52  
 D. 20  
 E. 60
24. A sum of money was invested at 8% per annum simple interest. If after 4 years the money amounts to N330.00, find the amount originally invested.
- A. N150  
 B. N200  
 C. N165  
 D. N180  
 E. N250
25.  $P$  sold his bicycle to  $Q$  at a profit of 10%.  $Q$  sold to  $R$  for N209 at a loss of 5%. How much did the bicycle cost  $P$ ?
- A. N150  
 B. N205  
 C. N180  
 D. N196  
 E. N200
26. Find the smallest number by which 252 can be multiplied to obtain a perfect square.
- A. 2  
 B. 3  
 C. 5  
 D. 7  
 E. 9
27. Find the reciprocal of:  $\frac{\frac{2}{3}}{\frac{1}{2} + \frac{1}{3}}$
- A.  $\frac{4}{5}$   
 B.  $\frac{2}{5}$   
 C.  $\frac{6}{9}$   
 D.  $\frac{5}{4}$

- E.  $\frac{3}{4}$
28. Three boys shared some oranges, the first received  $\frac{1}{3}$  of the oranges, the second received  $\frac{2}{3}$  of the remainder, if the third boy received the remaining 12 oranges. How many oranges did they share?
- A. 48  
B. 72  
C. 54  
D. 42  
E. 60
29. Udoh deposited N150.00 in the bank. At the end of 5 years, the simple interest on the principal was N55.00. At what rate per annum was the interest paid
- A.  $7\frac{1}{3}\%$   
B.  $5\%$   
C.  $11\%$   
D.  $3\frac{1}{2}\%$   
E.  $4\frac{2}{5}\%$
30. A number of pencil were shared among Desmond, Florence, and Kevin in ratio 2 : 3 : 5 respectively. If Desmond got 5, how many were shared out?
- A. 30  
B. 15  
C. 25  
D. 20  
E. 35
31. Find the least length of a rod which can be cut into exactly equal strips, each of 40 cm or 48 cm in length.
- A. 240 cm  
B. 480 cm  
C. 360 cm  
D. 120 cm  
E. 480 cm
32. A rectangular lawn has an area of 1815 square yards. If its length is 50 metres, find its width in meters. Given that 1 metre equals 1.1 yard.
- A. 30.00 m  
B. 33.00 m  
C. 32.00 m  
D. 39.93 m  
E. 36.45 m
33. Reduce each number to two significant figures and then evaluate  $\frac{0.021741 \times 1.2047}{0.023789}$
- A. 0.8  
B. 1.2  
C. 1.1  
D. 0.9  
E. 0.6
34. A cinema hall contains a certain number of people. If  $27\frac{1}{2}\%$  are children,  $47\frac{1}{2}\%$  are men and 84 are women, find the number of men in the hall
- A. 133  
B. 84  
C. 63  
D. 113
35. A woman buys 270 oranges for N1,800 and sells at 5 for N40. What is her profit?
- A. N 1,620  
B. N 630  
C. N 360  
D. N 2,160
36. If a car travels 120km on 45 litres of petrol, how much petrol is needed for a journey of 600km?
- A. 720 litres  
B. 225 litres  
C. 960 litres  
D. 160 litres
37. Simplify  $1 - \left(\frac{1}{7} \times 3\frac{1}{2}\right) \div \frac{3}{4}$
- A. 2  
B. 1  
C.  $\frac{1}{3}$   
D.  $\frac{2}{3}$
38. Evaluate:  $\frac{12.02 \times 20.06}{26.04 \times 60.06}$ , correct to 3 significant figures
- A. 0.154  
B. 0.155  
C. 0.158



- D. 0.157
39. Evaluate:  $\frac{0.8 \times 0.43 \times 0.031}{0.05 \times 0.72 \times 0.021}$ , correct to 3 significant figures
- A. 14.1  
B. 14.09  
C. 14.12  
D. 14.11
40. A man bought a car for N500,000 and was able to sell it for N350,000, what was his percentage loss?
- A. 50%  
B. 30%  
C. 70%  
D. 60%
41. Simplify:  $1\frac{2}{3} + 4\frac{1}{4} + 1\frac{5}{12}$
- A.  $4\frac{1}{3}$   
B.  $4\frac{2}{3}$   
C.  $4\frac{12}{17}$   
D.  $4\frac{3}{17}$
42. A man donates 16% of his monthly net earning to the church. If it amounts to N4,500, what is his monthly income?
- A. N40,500  
B. N52,000  
C. N52,500  
D. N45,000
43. If a student measured the length of a table to be 2.30 m insted of 2.50 m. What was his percentage error in measuring the length?
- A. 7%  
B. 10%  
C. 9%  
D. 8%
44. A man bought a second-hand photocopy machine for 34,000. He serviced it at a cost of N2,000 and then sold it at a profit of 15%. What was the selling price?
- A. 37,550  
B. 40,000  
C. 41,400  
D. 42,400
45. A student spent  $\frac{1}{5}$  of his allowance on books,  $\frac{1}{3}$  of the remainder on food and kept the rest for contingencies. What fraction was kept?
- A.  $\frac{8}{15}$   
B.  $\frac{4}{5}$   
C.  $\frac{2}{3}$   
D.  $\frac{7}{15}$
46. If  $p : q = \frac{2}{3} : \frac{5}{6}$  and  $\frac{3}{4} : \frac{1}{2}$ , find  $p : q : r$
- A. 12 : 15 : 10  
B. 10 : 15 : 24  
C. 9 : 10 : 15  
D. 12 : 15 : 16
47. Simplify:  $\frac{3\frac{2}{3} \times \frac{5}{6} \times \frac{2}{3}}{\frac{11}{25} \times \frac{3}{4} \times \frac{2}{27}}$
- A.  $4\frac{1}{3}$   
B. 30  
C.  $5\frac{2}{3}$   
D. 50
48. A man earns N3,500 per month out of which he spend 15% on his children's education. If he spends additional N1,950 on food, how much does he have left?
- A. N2,975  
B. N1,950  
C. N525  
D. N1025
49. Evaluate  $\frac{21}{9}$  to 3 significant figures
- A. 2.30  
B. 2.31  
C. 2.32  
D. 2.33
50. A girl shares a number of apples in the ratio 5 : 3 : 2. If the highest share is 40, find the smallest share.
- A. 74

- B. 38  
C. 36  
D. 16
51. Calculate the time taken for N3,000 to earn N600 at 8% simple interest.
- A. 3 years  
B.  $2\frac{1}{2}$  years  
C.  $1\frac{1}{2}$  years  
D.  $3\frac{1}{2}$  years
52. Find the tax on an income of N20,000 if no tax is paid on the first N10,000 and tax is paid at N50 and in N1,000 on the next N5,000 and at N55 and N1000 on the remainder.
- A. N225  
B. N525  
C. N552  
D. N500
53. The time taken to do a piece of work is inversely proportional to the number of men employed. If it takes 30 men to do a piece of work in 6 days, how many men are required to do the work in 4 days?
- A. 35  
B. 45  
C. 25  
D. 60
54. Three boys shared oranges. The first received  $\frac{1}{3}$  of the oranges and the second received  $\frac{2}{3}$  of the remainder. If the third boy received the remaining 12 oranges, how much oranges did they share?
- A. 42  
B. 60  
C. 54  
D. 48
55. A farmer planted 5,000 grains of maize and harvested 5,000 cobs, each bearing 500 grains. What is the ratio of the number of grains sowed to the number harvested?
- A. 1 : 5,000  
B. 1 : 25,000  
C. 1 : 500  
D. 1 : 250,000
56. Evaluate:  $\frac{0.21 \times 0.072 \times 0.00054}{0.006 \times 1.68 \times 0.063}$
- A. 0.1286  
B. 0.01285  
C. 0.01286  
D. 0.1285
57. A man's initial salary is N540 a month and increases after a period of six months by N36 a month. Find his salary in the eight month of the third year.
- A. 828  
B. 756  
C. 720  
D. 684
58. Find correct to 3 decimal places:
- $$\left(\frac{1}{0.05}\right) \div \left(\frac{1}{5.005}\right) - (0.05 \times 2.05)$$
- A. 99.998  
B. 9.998  
C. 98.999  
D. 89.899
59. Express  $62 \div 3$  as a decimal correct to 3 significant figures.
- A. 20.667  
B. 20.6  
C. 20.7  
D. 20.67
60. Factory *P* produces 20,000 bags of cement per day while factory *Q* produces 15,000 bags per day. If *P* reduces production by 5% and *Q* increases production by 5% determine the effective loss in the number of bags produced per day by the two factories
- A. 750  
B. 250  
C. 1000  
D. 1250
61. If 3 gallons of spirit containing 20% water are added to 5 gallons of another spirit containing 15% water, what percentage of the mixture is water?
- A.  $2\frac{4}{5}$   
B.  $18\frac{7}{8}$

- C.  $18\frac{1}{8}$   
D.  $16\frac{7}{8}$
62. The radius of a circle is given as 5cm subject to an error of 0.1cm. What is the percentage error in the area of the circle?
- A.  $\frac{1}{4}$   
B.  $\frac{1}{25}$   
C. 25  
D. 4
63. A man invested a sum of N280.00 partly at 5% and partly at 4%. If the total interest is N12.8 per annum, find the amount invested at 5%.
- A. N120  
B. N160  
C. N200  
D. N140
64. Evaluate  $\frac{3524}{0.05}$  correct to 3 significant figures
- A. 70000  
B. 70480  
C. 705  
D. 70500
65. If N225 yields N27 in  $x$  years simple interest at the rate of 4% per annum, find  $x$
- A. 12  
B. 4  
C. 27  
D. 3
66. A man's initial salary is N540 a month and increases after each period of six months by N36 a month. Find his salary in the eighth month of the third year.
- A. N756  
B. N648  
C. N720  
D. N828
67.  $\frac{1}{3} \div \left[ \frac{5}{7} \left( \frac{9}{10} - 1 + \frac{3}{4} \right) \right]$
- A.  $\frac{13}{24}$   
B.  $\frac{39}{28}$   
C.  $\frac{28}{39}$   
D.  $\frac{84}{13}$
68. Two sisters, Taiwo and Kehinde, own a store. The ratio of Taiwo's share to Kehinde's is 11 : 9. Later Kehinde sells  $\frac{2}{3}$  of her share to Taiwo for N720. Find the value of the store.
- A. 1080  
B. 3000  
C. 3600  
D. 2400
69. A tax payer has allowed  $\frac{1}{8}$ th of his income tax free, and pays 20% on the remainder. If he pays N490 tax, what is his income?
- A. N2450  
B. N2800  
C. N3920  
D. N560
70. A basket contains green, black and blue balls in the ratio 5 : 2 : 1. If there are 10 blue balls, find the corresponding new ratio when 10 green and 10 black balls are removed from the basket
- A. 1 : 1 : 1  
B. 4 : 2 : 1  
C. 5 : 1 : 1  
D. 4 : 1 : 1
71. The prime factors of 2, 520 are:
- A. 2, 3, 5, 7  
B. 2, 9, 5  
C. 2, 3, 7, 9  
D. 2, 9, 7
72. Simplify:  $\frac{2}{3} + \frac{3}{4} - \frac{5}{6}$
- A.  $\frac{7}{12}$   
B.  $\frac{5}{12}$   
C.  $\frac{11}{12}$   
D.  $\frac{1}{2}$

73. A man sells a radio for N1,200 at a loss of 20%. How much did he buy it?
- A. N1,500  
B. N1,440  
C. N1,000  
D. N960
74. Express 0.0462 in standard form.
- A.  $4.62 \times 10^{-2}$   
B.  $4.62 \times 10^{-3}$   
C.  $46.2 \times 10^{-3}$   
D.  $4.62 \times 10^2$
75. If  $\frac{2}{3}$  of a number is 30, what is  $\frac{3}{5}$  of that number?
- A. 27  
B. 20  
C. 45  
D. 25
76. A discount of 15% on the marked price of an article amounts to N450. What is the marked price?
- A. N3,000  
B. N3,500  
C. N2,500  
D. N4,000
77. Evaluate:  $(0.6)^2 - (0.4)^2$
- A. 0.2  
B. 0.4  
C. 0.52  
D. 0.36
78. A worker's salary was increased by 25%. If his new salary is N2,500, what was his old salary?
- A. N2,000  
B. N2,250  
C. N1,875  
D. N3,125
79. Simplify:  $\frac{0.0324 \times 0.00064}{0.48 \times 0.012}$
- A. 0.0036  
B. 0.036  
C. 0.36  
D. 3.6
80. What is the simple interest on N5,000 for 3 years at 4% per annum?
- A. N600  
B. N500  
C. N650  
D. N750
81. If  $x : y = 2 : 3$  and  $y : z = 4 : 5$ , find  $x : z$ .
- A. 8 : 15  
B. 10 : 15  
C. 8 : 12  
D. 6 : 15
82. Express  $\frac{5}{8}$  as a decimal.
- A. 0.625  
B. 0.650  
C. 0.725  
D. 0.525
83. A man bought 20 articles at N50 each and sold them at N60 each. What is his percentage profit?
- A. 10%  
B. 20%  
C. 15%  
D. 25%
84. Evaluate:  $2.5 \times 0.04 \times 0.5$
- A. 0.05  
B. 0.5  
C. 0.005  
D. 5.0
85. The HCF of 72, 96 and 108 is
- A. 12  
B. 24  
C. 18  
D. 36
86. Simplify:  $3\frac{1}{4} \div 1\frac{1}{2}$
- A.  $2\frac{1}{6}$   
B.  $1\frac{5}{6}$   
C.  $2\frac{1}{2}$

- D.  $4\frac{7}{8}$
87. A sum of N8,000 is invested at 5% compound interest per annum. What is the amount after 2 years?
- A. N8,820  
B. N8,800  
C. N8,640  
D. N9,000
88. Express 0.0000375 in standard form.
- A.  $3.75 \times 10^{-5}$   
B.  $3.75 \times 10^{-4}$   
C.  $37.5 \times 10^{-6}$   
D.  $3.75 \times 10^5$
89. If  $\frac{3}{4}$  of a class are girls and  $\frac{2}{3}$  of the girls are tall, what fraction of the class are tall girls?
- A.  $\frac{1}{2}$   
B.  $\frac{5}{12}$   
C.  $\frac{2}{3}$   
D.  $\frac{1}{4}$
90. A man earns N15,000 monthly. If 12% is deducted for tax, how much does he take home?
- A. N13,200  
B. N13,800  
C. N14,000  
D. N13,500
91. Evaluate:  $\sqrt{0.0169}$
- A. 0.13  
B. 0.013  
C. 1.3  
D. 0.0013
92. Simplify:  $\frac{3}{7} \times \frac{14}{9} \div \frac{2}{3}$
- A. 1  
B. 2  
C.  $\frac{1}{2}$   
D. 3
93. What percentage of 250 is 75?
- A. 30%  
B. 25%  
C. 20%  
D. 35%
94. The LCM of 12, 18, and 24 is
- A. 72  
B. 144  
C. 48  
D. 36
95. A man bought a car for N800,000 and sold it for N920,000. What is his percentage gain?
- A. 15%  
B. 12%  
C. 20%  
D. 10%
96. Express  $2\frac{3}{5}$  as a decimal.
- A. 2.6  
B. 2.3  
C. 2.5  
D. 2.8
97. If N1,200 amounts to N1,440 in 2 years at simple interest, what is the rate per annum?
- A. 10%  
B. 12%  
C. 8%  
D. 15%
98. Simplify:  $\left(\frac{2}{3}\right)^2 + \left(\frac{1}{4}\right)^2$
- A.  $\frac{25}{36}$   
B.  $\frac{17}{36}$   
C.  $\frac{73}{144}$   
D.  $\frac{65}{144}$
99. A bag of rice costs N8,000. If the price increases by 12.5%, what is the new price?
- A. N9,000  
B. N9,500  
C. N8,500  
D. N10,000

100. Evaluate:  $4.8 \div 0.06$

A. 80

B. 8

C. 800

D. 0.8

## Chapter 2

# Algebra

## 2.1 Factorization and Remainder Theorem

### 2.1.1 Questions

1. If the function  $f$  is defined by  $f(x+2) = 2x^2 + 7x - 5$ , find  $f(-1)$ .
  - A.  $-8$
  - B.  $4$
  - C.  $10$
  - D.  $-10$
2. Factorize  $a^2x - b^2y - b^2x + a^2y$ .
  - A.  $(y-x)(a-b)(a+b)$
  - B.  $(a-b)(x+y)$
  - C.  $(x-y)(a-b)$
  - D.  $(x+y)(a-b)(a+b)$
3. If  $x-1$  and  $x+1$  are both factors of the equation  $x^3 + px^2 + qx + 6 = 0$ , evaluate  $p$  and  $q$ .
  - A.  $-6, -1$
  - B.  $1, -1$
  - C.  $6, 1$
  - D.  $6, -6$
4. If  $f(x) = \frac{1}{x-1} + \frac{x-1}{x^2-1}$ , find  $f(1-x)$ .
  - A.  $\frac{1}{x} + \frac{1}{x-2}$
  - B.  $-\frac{1}{x} - \frac{1}{x-2}$
  - C.  $x + \frac{1}{2x-1}$
  - D.  $\frac{1}{x} + \frac{1}{x^2-1}$
  - E.  $-\frac{1}{x} - \frac{1}{2x-1}$
5. Multiply  $(x+3y+5)$  by  $(2x^2+5y+2)$ .
  - A.  $2x^3 + 3x^2y + 10xy^2 + 13y + 10x^2 + 2x + 10$
  - B.  $2x^3 + 2x^2y + 10xy + 10y^2 + 31y + 5x^2 + 2x + 10$
  - C.  $2x^3 + 6x^2y + 5xy + 10y^2 + 13y + 5x^2 + 2x + 10$
  - D.  $2x^3 + 6x^2y + 5xy + 15y^2 + 31y + 5x^2 + 2x + 10$
  - E.  $2x^3 + 3x^2y + 5xy + 10y^2 + 13y + 5x^2 + 2x + 10$
6. If  $kx^3 + 10x^2 + lx - 3$  is divisible by  $(x-1)$  and when it is divided by  $(x+2)$  the remainder is 27, find the constants  $k$  and  $l$ .
  - A.  $k = -7, l = -15$
  - B.  $k = \frac{-21}{5}, l = \frac{-61}{5}$
  - C.  $k = -15, l = -7$
  - D.  $k = -\frac{5}{3}, l = \frac{19}{5}$
  - E.  $k = -\frac{5}{3}, l = -\frac{19}{3}$
7. Factorize  $3x^3 + 4x^2 - 13x + 6$  completely, given that  $x-1$  is a factor.
  - A.  $(x-1)(x-3)(x+2)$
  - B.  $(x-1)(x-3)(3x+2)$
  - C.  $(x-1)(x-2)(x+3)$
  - D.  $(x-1)(x+3)(3x+2)$
  - E.  $(x-1)(x+3)(3x-2)$
8. Multiply  $x^2 + x + 1$  by  $x^2 - x + 1$ .
  - A.  $x^4 + 3x^2 + x + 1$
  - B.  $x^4 + 4x^2 - 6x + 1$

- C.  $x^4 + 4x^2 + 1$   
 D.  $x^4 - x^3 - x^2 + x + 1$   
 E.  $x^4 - 6x^2 - 4x + 1$
9. If  $x = 1$  is a root of the equation  $x^3 - 2x^2 - 5x + 6$ , find the other roots.  
 A. -3 and 2  
 B. 1 and 3  
 C. -2 and 2  
 D. 3 and -2  
 E. -3 and 1
10. If  $x + 2$  and  $x - 1$  are factors of the expression  $lx^3 + 2kx^2 + 24$ , find the values of  $l$  and  $k$ .  
 A.  $l = -6, k = -9$   
 B.  $l = -2, k = -1$   
 C.  $l = -2, k = 1$   
 D.  $l = 0, k = 1$   
 E.  $l = 6, k = 0$
11. Factorize completely:  $81a^4 - 16b^4$ .  
 A.  $(3a + 2b)(2a - 3b)(9a^2 + 4b^2)$   
 B.  $(3a - 2b)(2a - 3b)(9a^2 - 4b^2)$   
 C.  $(3a - 2b)(3a - 2b)(9a^2 + 4b^2)$   
 D.  $(3a - 2b)(2a - 3b)(4a^2 - 9b^2)$   
 E.  $(3a - 2b)(3a + 2b)(9a^2 + 4b^2)$
12. The factor which is common to all three binomial expressions  $4a^2 - 9b^2$ ,  $8a^2 + 27b^3$ ,  $(4a + 6b)^2$  is:  
 A.  $4a - 6b$   
 B.  $4a + 6b$   
 C.  $2a - 3b$   
 D.  $2a + 3b$   
 E.  $3a - 2b$
13. If  $x - 2$  and  $x + 1$  are factors of the expression  $x^3 + px^2 + qx + 1$ , find  $p + q$ .  
 A. -3  
 B. 0  
 C.  $-\frac{17}{3}$   
 D.  $-\frac{2}{3}$   
 E. 3
14. The factors of  $9 - (x^2 - 3x - 1)^2$  are:  
 A.  $(x - 4)(x - 1)(x - 1)(x + 2)$   
 B.  $(x - 4)(x + 1)(x - 2)(x - 1)$   
 C.  $(x - 2)(x + 2)(x + 1)(x + 4)$   
 D.  $(x - 2)(x + 2)(x + 1)(x - 1)$   
 E.  $(x - 4)(x - 3)(x - 2)(x + 1)$
15. If  $f(x - 2) = 4x^2 + x + 7$ , find  $f(1)$ .  
 A. 27  
 B. 7  
 C. 17  
 D. 46  
 E. 12
16. If  $g(y) = \frac{y - 3}{11} + \frac{11}{y^2 - 9}$  what is  $g(y + 3)$ ?  
 A.  $\frac{y}{11} + \frac{11}{y(y + 5)}$   
 B.  $\frac{y + 30}{11} + \frac{11}{y(y + 3)}$   
 C.  $\frac{y}{11} + \frac{11}{y(y + 3)}$   
 D.  $\frac{y + 3}{11} + \frac{11}{y(y - 6)}$
17. Factorize completely  $3a + 125a^3$ .  
 A.  $(2a + 5x)(4 + 10ax + 25ax^2)$   
 B.  $(2a + 5x^2)(4 + 25ax)$   
 C.  $a(2 + 5x)(4 - 10x + 25ax^2)$   
 D.  $a(2 + 5x)(4 + 10ax + 25ax^2)$
18. Factorize  $x^2 + 2a + ax + 2x$ .  
 A.  $(x^2 - 1)(x + a)$   
 B.  $(x + 2)(x + a)$   
 C.  $(x + 2a)(x + 3)$   
 D.  $(x + 2a)(x - 1)$
19. The graphical method of solving the equation  $x^3 + 3x^2 + 4x - 28 = 0$  is by drawing the graphs of the curves:  
 A.  $y = x^3$  and  $y = 3x^2 + x - 28$   
 B.  $y = x^3 + 3x^2 + 4x$  and  $y = 28$   
 C.  $y = x^3 + 3x^2 + 4x - 28$  and the line  $y = \frac{28}{x}$   
 D.  $y = x^2 + 3x + 4$  and  $y = \frac{28}{x}$   
 E.  $y = x^2 + 3x + 4$  and line  $y = 28x$
20. Factorize  $(4a + 3)^2 - (3a - 2)^2$ .  
 A.  $(x + 2a)(x - 1)$



- B.  $(x + 1)(x + 2a)$   
 C.  $(x + 2)(x + a)$   
 D.  $(x^2 - 1)(x + a)$
21. If  $x^3 - 12x - 16 = 0$  has  $x - 2$  as a solution, then the equation has:  
 A. 3 roots all different  
 B.  $x - 4$  as a solution also  
 C. 3 roots all equal  
 D. 3 roots with two equal and the third different  
 E. only one root
22. The expression  $x^3 - 4x^2 + cx + d$  is such that  $x + 1$  is a factor and its value is 1 when  $x$  is  $-2$ . Find  $c$  and  $d$ .  
 A.  $c = -4$  and  $d = 9$   
 B.  $c = 20$  and  $d = 9$   
 C.  $c = -20$  and  $d = 15$   
 D.  $c = -20$  and  $d = -15$   
 E.  $c = 20$  and  $d = -15$
23. What factor is common to all the expressions  $x + 1$ ,  $2x^2 + x + 1$ , and  $x^2 - 1$ ?  
 A.  $x + 1$   
 B. 1  
 C. No common factor  
 D.  $2x - 1$   
 E.  $x$
24. Factorize completely:  $(x^2 + x)^2 - (2x + 2)^2$ .  
 A.  $(x + y)(x + 2)(x - 2)$   
 B.  $(x + 1)^2(x + 2)(x - 2)$   
 C.  $(x + y)^2(y - 2)^2$   
 D.  $(x + 1)^2(x + 2)^2$
25. If  $f(x) = 2x^2 + 5x + 3$ , find  $f(x + 1)$ .  
 A.  $2x^2 - x + 10$   
 B.  $2x^2 - x$   
 C.  $4x^2 + 3x + 12$   
 D.  $4x^2 + 3x + 2$
26. If one factor of  $x^3 - 8^{-1}$  is  $x - 2^{-1}$ , the other factor is:  
 A.  $x^2 + 2^{-1}x - 4^{-1}$   
 B.  $x^2 - 2^{-1}x - 4^{-1}$   
 C.  $x^2 - 2^{-1}x - 4^{-1}$   
 D.  $x^2 + 4^{-1}x - 2^{-1}$
27. Factorize  $9(x + y)^2 - 4(x - y)^2$ .  
 A.  $(x + y)(5x + y)$   
 B.  $(x + y)^2$   
 C.  $5(x + y)^2$   
 D.  $(x + 5y)(5x - y)$
28. Factorize  $4a^2 - 12ab - c^2 + 9b^2$ .  
 A.  $(2a + 3b - c)(2a + 3b + c)$   
 B.  $4a(a - 3b) + (3b - c)^2$   
 C.  $(2a - 3b - c)(2a - 3b + c)$   
 D.  $4a(a - 3b) + (3b + c)^2$
29. What are the values of  $k$  and  $l$  respectively if  $\frac{1}{2}(3y - 4x)^2 = (8x^2 + kxy + ly^2)$ .  
 A.  $12, \frac{9}{2}$   
 B.  $-12, \frac{9}{2}$   
 C.  $6, 9$   
 D.  $-6, 9$
30. If  $f(x - 4) = x^2 + 2x + 3$ , find  $f(2)$ .  
 A. 11  
 B. 6  
 C. 51  
 D. 27
31. Factorize completely:  $y^3 - 4xy + xy^3 - 4y$ .  
 A.  $y(1 - x)(y + 2)(y - 2)$   
 B.  $y(1 + x)(y - 2)(y - 2)$   
 C.  $(y + xy)(y + 2)(y - 2)$   
 D.  $(y + xy)(y + 2)(y - 2)$
32. If  $g(x) = x^2 + 3x + 4$ , find  $g(x + 1) - g(x)$ .  
 A.  $2(x + 2)$   
 B.  $(x + 2)$   
 C.  $(2x + 1)$   
 D.  $x^2 + 4$
33. Factorize:  $m^3 - 2m^2 - m + 2$ .  
 A.  $(m + 1)(m + 1)(m + 2)$   
 B.  $(m^2 + 1)(m - 2)$   
 C.  $(m^2 + 2)(m - 1)$   
 D.  $(m - 2)(m + 1)(m - 1)$
34. Which of the following is a factor of  $rs + tr - pt - ps$ ?

- A.  $(p - s)$   
 B.  $(r - p)$   
 C.  $(s - p)$   
 D.  $(r + p)$
35. If  $x + 1$  is a factor of  $x^3 + 3x^2 + kx + 4$ , find the value of  $k$ .  
 A.  $-6$   
 B.  $6$   
 C.  $8$   
 D.  $-8$
36. Factorize:  $9p^2 - q^2 + 6qr - 9r^2$ .  
 A.  $(3p - 3q + r)(3p - q)$   
 B.  $(6p - 3q - 3r)(3p - q - 4r)$   
 C.  $(3p - 3q + r)(3p - q - 3r)$   
 D.  $(3p - 3q + r)(3p - q + 4r)$
37. If a function is defined by  $f(x + 1) = 3x^2 - x + 4$ , find  $f(0)$ .  
 A.  $6$   
 B.  $8$   
 C.  $0$   
 D.  $2$   
 E.  $4$
38. If  $f(x + 2) = 3x^2 + 4x + 1$ , find the value of  $f(1)$ .  
 A.  $32$   
 B.  $40$   
 C.  $8$   
 D.  $32$   
 E.  $21$
39. Factorize:  $6x^2 - 14x - 12$ .  
 A.  $2(x + 3)(3x - 2)$   
 B.  $2(x - 3)(3x + 2)$   
 C.  $6(x - 2)(x + 1)$   
 D.  $6(x + 2)(x - 1)$   
 E.  $(3x + 4)(2x + 3)$
40. Factorize:  $abx^2 + 8y - 4bx - 2axy$ .  
 A.  $(ax - 4)(bx - 2y)$   
 B.  $(bx - 4)(ax - 2y)$   
 C.  $(ax + b)(x - 8y)$   
 D.  $(x - 2y)(abx - 4)$   
 E.  $(ax - 2y)(by - 4)$
41. Factorize:  $1 - (a - b)^2$ .  
 A.  $(1 + a + b)(1 - a - b)$   
 B.  $(1 - a + b)(1 + a - b)$   
 C.  $(1 + a - b)(1 - a + b)$   
 D.  $(1 - a - b)(1 - a + b)$   
 E.  $(1 - a + b)(1 + a + b)$
42. Which of the following is a factor of  $15 + 7x - 2x^2$ ?  
 A.  $x + 3$   
 B.  $x - 5$   
 C.  $x + 5$   
 D.  $x - 3$
43. Divide the expression  $x^3 + 7x^2 - x - 7$  by  $-1 + x^2$ .  
 A.  $x + 7$   
 B.  $-x^3 + 7x^2 - x - 7$   
 C.  $x - 7$   
 D.  $-x^2 + 7x + 7$
44. Find a positive value of  $p$  if the expression  $2x^2 - px + p$  leaves a remainder 6 when divided by  $x - p$ .  
 A.  $1$   
 B.  $2$   
 C.  $3$   
 D.  $4$
45. When the expression  $pm^2 + qm + 1$  is divided by  $(m - 1)$ , it has a remainder of 2 and when divided by  $(m + 1)$  the remainder is 4, find  $p$  and  $q$  respectively.  
 A.  $-2, 3$   
 B.  $2, -1$   
 C.  $-1, 2$   
 D.  $3, -2$
46. Factorize:  $r^2 - r(2p + q) + 2pq$ .  
 A.  $(r - q)(r - 2p)$   
 B.  $(r - 2q)(2r - p)$   
 C.  $(2r - p)(r + p)$   
 D.  $(r - p)(r + q)$
47. Divide  $2x^3 + 11x^2 + 17x + 6$  by  $2x + 1$ .  
 A.  $x^2 + 5x + 6$   
 B.  $x^2 - 5x + 6$   
 C.  $2x^2 + 5x + 6$

- D.  $x^2 + 5x + 6$
48. Factorize completely:  $x^2 + 2xy + y^2 + 3x + 3y - 18$ .
- A.  $(x + y + 6)(x + y - 3)$   
 B.  $(x - y - 6)(x - y + 3)$   
 C.  $(x - y + 6)(x - y - 3)$   
 D.  $(x + y - 6)(x + y + 3)$
49. Divide  $4x^3 - 3x + 1$  by  $2x - 1$ .
- A.  $2x^2 - x + 1$   
 B.  $2x^2 + x - 1$   
 C.  $2x^2 - x - 1$   
 D.  $2x^2 + x + 1$
50. If  $(x - 1)$ ,  $(x + 1)$  and  $(x - 2)$  are factors of the polynomial  $ax^3 + bx^2 + cx - 1$ , find  $a$ ,  $b$ , and  $c$  respectively.
- A.  $-\frac{1}{2}, 1, \frac{1}{2}$   
 B.  $\frac{1}{2}, 1, \frac{1}{2}$   
 C.  $\frac{1}{2}, -1, \frac{1}{2}$   
 D.  $\frac{1}{2}, 1, 1\frac{1}{2}$
51. Factorize:  $4x^2 - 9y^2 + 20x + 25$ .
- A.  $(2x - 3y + 5)(2x - 3y - 5)$   
 B.  $(2x - 3y + 5)(2x + 3y + 5)$   
 C.  $(2x + 3y - 5)(2x + 3y + 5)$   
 D.  $(2x + 3y - 5)(2x - 3y - 5)$   
 E.  $(2x - 3y + 5)(2x - 3y - 5)$
52. Divide  $a^{3x} - 26a^{2x} + 156a^x - 216$  by  $a^{2x} - 24a^x + 108$ .
- A.  $a^x + 2$   
 B.  $a^x - 2$   
 C.  $a^x - 18$   
 D.  $a^x - 6$
53. Find the values of  $x$  where the curve  $y = x^3 + 2x^2 - 5x - 6$  crosses the  $x$ -axis:
- A. 2, -1 and -3  
 B. 2, 1 and 3  
 C. 2, 1 and -3  
 D. 2, -1 and 3
54. The polynomial whose roots are  $\frac{4}{3}$  and  $-\frac{3}{5}$  is:
- A.  $15x^2 - 11x - 12$   
 B.  $12x^2 + 11x - 15$   
 C.  $12x^2 - x - 12$   
 D.  $15x^2 + 11x - 12$
55. If  $9x^2 + 6xy + 4y^2$  is a factor of  $27x^3 - 8y^3$ , find the other factor.
- A.  $2y + 3x$   
 B.  $2y - 3x$   
 C.  $3x + 2y$   
 D.  $3x - 2y$
56. Factorize completely:  $\frac{x^3 + 3x^2 - 10x}{2x^2 - 8}$ .
- A.  $\frac{x(x - 5)}{2(x - 2)}$   
 B.  $\frac{x(x - 5)}{2(x + 2)}$   
 C.  $\frac{x(x + 5)}{2(x + 2)}$   
 D.  $\frac{x^2 + 5}{2x + 4}$
57. Find the remainder when  $3x^3 + 5x^2 + 11x - 4$  is divided by  $x + 3$ .
- A. 1  
 B. 4  
 C. -4  
 D. -1
58. Factorize completely:  $ac - 2bc + a^2 + 4b^2$ .
- A.  $(a - 2b)(c + a - 2b)$   
 B.  $(a - 2b)(c - a + 2b)$   
 C.  $(a - 2b)(c + a + 2b)$   
 D.  $(a - 2b)(c - a - 2b)$
59. Factorize  $2y^2 - 15xy + 18x^2$ .
- A.  $(2y - 3x)(y + 6x)$   
 B.  $(2y - 3x)(y - 6x)$   
 C.  $(3y + 2x)(y - 6x)$   
 D.  $(2y + 3x)(y - 6x)$
60. Find the value of  $k$  if  $y - 1$  is a factor of  $y^3 + 4y^2 + ky - 6$ .
- A. -6  
 B. -4  
 C. 0

- D. 1
61. Divide  $6x^2 + 13x + 5$  by  $2x + 1$ .
- A.  $3x - 5$   
 B.  $3x + 5$   
 C.  $5x - 3$   
 D.  $5x + 3$
62. The polynomial whose roots are  $-2$ ,  $-1$  and  $3$  is:
- A.  $x^3 - 7x + 6$   
 B.  $x^3 + 7x - 6$   
 C.  $x^3 - 7x - 6$   
 D.  $x^3 + 7x + 6$
63. Find the value of  $k$  if the expression  $kx^3 + x^2 - 5x - 2$  leaves a remainder of  $2$  when divided by  $2x + 1$ .
- A.  $10$   
 B.  $-8$   
 C.  $-10$   
 D.  $8$
64. Find the roots of  $x^3 - 2x^2 - 5x + 6 = 0$ .
- A.  $-1, -2, 3$   
 B.  $-1, 2, -3$   
 C.  $1, 2, -3$   
 D.  $1, -2, 3$
65. Factorize:  $2t^2 + t - 15$ .
- A.  $(t + 3)(2t - 5)$   
 B.  $(2t + 3)(t - 5)$   
 C.  $(t + 3)(t - 5)$   
 D.  $(2t - 3)(t + 5)$
66. If  $2x^2 - kx - 12$  is divisible by  $x - 4$ , find the value of  $k$ .
- A.  $4$   
 B.  $5$   
 C.  $6$   
 D.  $7$
67. Solve for  $x$  in the equation  $x^3 - x + 5 = 0$ .
- A.  $-1, 1, -5$   
 B.  $1, 1, 5$   
 C.  $1, 1, -5$   
 D.  $1, -1, 5$
68. Find the remainder when  $x^3 - 2x^2 + 3x - 3$  is divided by  $x^2 + 1$ .
- A.  $2x - 1$   
 B.  $x + 3$   
 C.  $2x + 1$   
 D.  $3x - 3$
69. Find the remainder when  $2x^3 - 11x^2 + 8x - 1$  is divided by  $x + 3$ .
- A.  $-871$   
 B.  $-781$   
 C.  $-187$   
 D.  $-178$
70. Factorize:  $(2x+3y)^2 + 2(2x+3y)(2x-3y) + (2x-3y)^2$ .
- A.  $16x^2$   
 B.  $18x^2$   
 C.  $12x^2$   
 D. none of the above
71. Factorize:  $45a^3b + 5ab^3 - 30a^2b^2$ .
- A.  $5ab(3a - b)^2$   
 B.  $7ab(5a - b)^2$   
 C.  $5ab(5a - b)^2$   
 D. none of the above
72. Find the factors of  $(a - b)^3 + (b - c)^3 + (c - a)^3$ .
- A.  $3(a + b)(b + c)(c + a)$   
 B.  $3(a - b)(b - c)(c - a)$   
 C.  $5(a - b)(b - c)(c - a)$   
 D.  $5(a + b)(b - c)(c - a)$
73. Factorize:  $a^2 + \frac{1}{a^2} + 3 - 2a - \frac{2}{a}$ .
- A.  $\left(a + \frac{1}{a} - 1\right)\left(a - \frac{1}{a} + 1\right)$   
 B.  $\left(a + \frac{1}{a} + 1\right)\left(a + \frac{1}{a} + 1\right)$   
 C.  $\left(a + \frac{1}{a} + 1\right)\left(a + \frac{1}{a} - 1\right)$   
 D.  $\left(a + \frac{1}{a} - 1\right)\left(a + \frac{1}{a} - 1\right)$
74. Resolve into factors:  $9(3x + 5y)^2 - 12(3x + 5y)(2x + 3y) + 4(2x + 3y)^2$ .

- A.  $(5x + 9y)$   
 B.  $(5x - 9y)^2$   
 C.  $(7x + 9y)^2$   
 D. None of the above
75. Factorize:  $(a - b + c)^2 + (b - c + a)^2 + 2(a - b + c)(b - c + a)$ .  
 A.  $6a^2$   
 B.  $4a^2$   
 C.  $8a^2$   
 D.  $10a^2$
76. Resolve into factors:  $81x^2y^2 - 108xyz + 36z^2$ .  
 A.  $(6xy + 9z)^2$   
 B.  $(9xy - 7z)^2$   
 C.  $(9xy + 6z)^2$   
 D.  $(6xy - 7z)^2$
77. What value should  $a$  possess so that  $x + 1$  may be a factor of the polynomial  

$$f(x) = 2x^3 - ax^2 - (2a - 3)x + 2$$
  
 A. 3  
 B. 2  
 C. -2  
 D. none of the above
78. If  $(x - 2)$  is a factor of the polynomial  $x^3 - 2ax^2 + ax - 1$ , find the value of  $a$ .  
 A.  $\frac{5}{6}$   
 B.  $\frac{7}{6}$   
 C.  $\frac{11}{6}$   
 D. none of the above
79. The remainder when  $6p^3 - p^2 - 47p + 30$  is divided by  $p - 3$  is:  
 A. 21  
 B. 63  
 C. 18  
 D. 42
80. Factorize:  $k^2 - 2kp + p^2$ .  
 A.  $(k + p)^2$   
 B.  $(k - p)^2$   
 C.  $k^2 - p^2$   
 D.  $k^2 + p^2$
81. If  $x + 1$  is a factor of  $x^3 + 3x^2 + mx + 4$ , find the value of  $m$ .  
 A. 8  
 B. -6  
 C. 6  
 D. -8
82. Divide the expression  $x^3 + 7x^2 - x - 7$  by  $x^2 - 1$ .  
 A.  $x - 1$   
 B.  $x + 1$   
 C.  $x - 7$   
 D.  $x + 7$
83. If  $x + a$  is a factor of the polynomial  $x^3 + ax^2 - 2x + a + 4$ , find the value of  $a$ .  
 A.  $-\frac{4}{3}$   
 B.  $\frac{4}{3}$   
 C.  $\frac{2}{3}$   
 D.  $-\frac{2}{3}$
84. Resolve into factors:  $16x^2 - 72xy + 81y^2 - 12x + 27y$ .  
 A.  $(6x - 7y)(6x - 7y - 5)$   
 B.  $(6x - 7y)(6x - 7y + 5)$   
 C.  $(4x + 9y)(4x + 9y + 3)$   
 D.  $(4x - 9y)(4x - 9y - 3)$
85. Resolve into factors:  $16(x - y)^2 - 9(x + y)^2$ .  
 A.  $(x - 5y)(5x - y)$   
 B.  $(x + 7y)(7x + y)$   
 C.  $(x - 7y)(7x - y)$   
 D.  $(x + 5y)(5x + y)$
86. Factorize the expression:  $a^2 + \frac{1}{4} + a$ .  
 A.  $\left(a + \frac{1}{2}\right)\left(a - \frac{1}{2}\right)$   
 B.  $\left(a + \frac{1}{2}\right)^2$   
 C.  $\left(a + \frac{1}{2}\right)^3$   
 D.  $\left(a + \frac{1}{2}\right) \cdot a$
87. Resolve into factors:  $(a + b)^2 - 2(a^2 - b^2) + (a - b)^2$ .

- A.  $6b^2$   
 B.  $4b^2$   
 C.  $2b^2$   
 D.  $8b^2$
88. Factorize the expression:  $(a+b)^2 - 14c(a+b) + 49c^2$ .  
 A.  $(a-b-9c)^3$   
 B.  $(a+b+9c)^2$   
 C.  $(a+b-7c)^2$   
 D. none of the above
89. When a polynomial  $f(x)$  is divided by  $x-3$  and  $x+6$ , the respective remainders are 7 and 22. What is the remainder when  $f(x)$  is divided by  $(x-3)(x+6)$ ?  
 A.  $-\frac{5}{3}x + 12$   
 B.  $-\frac{7}{3}x + 14$   
 C.  $-\frac{5}{3}x + 16$   
 D.  $-\frac{7}{3}x + 12$
90. When  $4x^3 - ax^2 + bx + 4$  is divided by  $x-2$  and  $x+1$ , the respective remainders are 20 and -13. Find the values of  $a$  and  $b$ .  
 A.  $a = 3, b = 2$   
 B.  $a = 9, b = 8$   
 C.  $a = 7, b = 6$   
 D.  $a = 5, b = 4$
91. When  $(x^3 - 2x^2 + px - q)$  is divided by  $x^2 - 2x - 3$  the remainder is  $(x - 6)$ . The values of  $p$  and  $q$  are:  
 A.  $p = -2, q = -6$   
 B.  $p = 2, q = -6$   
 C.  $p = 2, q = 6$   
 D.  $p = -2, q = 6$
92. If  $(x-1)$  is a factor of  $ax^3 + bx^2 - 36x + 22$  and  $2^b = 64^a$ , find  $a$  and  $b$ .  
 A.  $a = 4, b = 16$   
 B.  $a = 6, b = 24$   
 C.  $a = 2, b = 12$   
 D.  $a = 8, b = 16$
93. If  $2apq = (p+q)^2 - (p-q)^2$ , then the value of  $a$  is:  
 A. 1  
 B. 2  
 C. 4  
 D. 8
94. What is the value of  $\frac{(a^2 + b^2)(a-b) - (a-b)^3}{a^2b - ab^2}$ ?  
 A. -1  
 B. -2  
 C. 1  
 D. 2
95. Find the values of  $m$  and  $n$  in the polynomial  $2x^3 + mx^2 + nx - 14$ , such that  $(x-1)$  and  $(x+2)$  are its factors.  
 A.  $m = 4, n = 5$   
 B.  $m = 9, n = 3$   
 C.  $m = 6, n = 7$   
 D. none of the above
96. Divide the polynomial  $4y^3 - 3y^2 + 2y - 4$  by  $y+2$  and find the quotient and remainder.  
 A.  $4y^2 - 11y + 24, -52$   
 B.  $6y^2 - 13y + 36, -64$   
 C.  $4y^2 + 13y - 24, 52$   
 D. none of the above
97. Suppose that  $b$  and  $c$  are constants and  

$$(x+2)(x+b) = x^2 + cx + 6$$
  
 what is  $c$ ?  
 A. -5  
 B. -3  
 C. -1  
 D. 3  
 E. 5
98. Simplify the expression:  $x^3 + 3x + \frac{3}{x} + \frac{1}{x^3}$ .  
 A.  $\left(x - \frac{1}{3}\right)^3$   
 B.  $\left(x - \frac{1}{x}\right)^3$   
 C.  $\left(x - \frac{3}{x}\right)^3$   
 D.  $\left(x + \frac{1}{x}\right)^3$
99. If  $(x^{3/2} - xy^{1/2} + x^{1/2}y - y^{3/2})$  is divided by  $(x^{1/2} - y^{1/2})$ , the quotient is:  
 A.  $x^{1/2} + y^{1/2}$   
 B.  $x^2 - y^2$

C.  $x - y$

D.  $x + y$

100. Let  $f(x) = a_0x^n + a_1x^{n-1} + a_2x^{n-2} + \cdots + a_{n-1}x + a_n$ , where  $a_0, a_1, a_2, \dots, a_n$  are constants. If  $f(x)$  is divided by  $ax - b$ , then the remainder is:

A.  $f\left(\frac{b}{a}\right)$

B.  $f\left(\frac{-b}{a}\right)$

C.  $f\left(\frac{a}{b}\right)$

D.  $f\left(\frac{-a}{b}\right)$

## 2.2 Indices and Standard Form

### 2.2.1 Questions

1. If  $(25)^{x-1} = 64\left(\frac{5}{2}\right)^6$ , then  $x$  has the value:

A. 7

B. 4

C. 32

D. 5

E. 64

2. Simplify:  $\frac{5^x \times 25^{x-1}}{125^{x+1}}$ .

A.  $5^{x+2}$

B.  $5^{2x-1}$

C.  $5^{x+1}$

D.  $5^3$

E.  $5^{-5}$

3. Express  $37.05 \times 0.0042$  in standard form.

A.  $15.561 \times 10^2$

B.  $1.556 \times 10^1$

C.  $1.5561 \times 10^{-4}$

D.  $1.5561 \times 10^{-1}$

E.  $1.5561 \times 10^2$

4. Simplify:  $\sqrt[3]{(64r^{-6})^{\frac{1}{2}}}$

A.  $\frac{1}{2r}$

B.  $\frac{2}{r}$

C. 2

D.  $\frac{1}{2}$

5. What are the values of  $y$  that satisfy this equation:

$$9^y - 4(3^y) + 3 = 0$$

A. -1 and 0

B. 1 and 3

C. 0 and 1

D. -1 and 1

6. Simplify:  $\frac{9^{\frac{1}{3}} \times 27^{-\frac{1}{2}}}{3^{-\frac{1}{6}} \times 3^{-\frac{2}{3}}}$

A.  $\frac{1}{3}$

B.  $\frac{1}{9}$

C. 3

D. 1

E. 9

7. If  $\sqrt{3^x} = \sqrt[3]{9}$

A.  $\frac{3}{4}$

B.  $\frac{4}{3}$

C.  $\frac{1}{3}$

D.  $\frac{2}{3}$

E.  $\frac{1}{2}$

8. Find the value of  $\left(4^{\frac{1}{2}}\right)^6$

A. 6

B. 2

C. 1

D. 4

E. 8

9. Simplify:  $\frac{3(2^{n-1}) - 4(2^{n-1})}{2^{n+1} - 2^n}$

- A.  $-2^{n-1}$
- B.  $2^{n+1}$
- C.  $-2^1$
- D.  $-2^{-1}$

10. Evaluate:  $\frac{27^{\frac{1}{3}} - 8^{\frac{2}{3}}}{16^{\frac{2}{4}} \times 2}$

- A.  $-\frac{1}{8}$
- B.  $\frac{21}{7}$
- C.  $\frac{23}{5}$
- D.  $-\frac{23}{5}$
- E.  $-\frac{23}{6}$

11. If  $\frac{4^{x+3}}{16^{2x-3}} = 1$ , find  $x$

- A. 1
- B. -1
- C. -3
- D. 3
- E. -3

12. Evaluate without using tables:  $(0.008)^{-\frac{1}{3}} \times (0.16)^{-\frac{3}{2}}$

- A.  $\frac{8}{625}$
- B. 8
- C.  $\frac{625}{8}$
- D.  $\frac{1}{8}$

13. Simplify:  $\frac{3^n - 3^{n-1}}{3^3 \times 3^n - 27 \times 3^{n-1}}$

- A. 0
- B.  $\frac{1}{27}$
- C.  $3^n - 3^{n-1}$
- D. 1
- E.  $\frac{2}{27}$

14. Evaluate and leave your answer in standard form:

$$\sqrt{\frac{0.0048 \times 0.81 \times 10^{-7}}{0.027 \times 0.04 \times 10^6}}$$

- A.  $6 \times 10^{-14}$
- B.  $6 \times 10^{-7}$
- C.  $6 \times 10^7$
- D.  $6 \times 10^{14}$

15. If  $3^{2y} - 6(3^y) = 27$ , find  $y$ .

- A. 3
- B. -1
- C. 2
- D. -3
- E. 1

16. If it is given that  $5^{x+1} + 5^x = 150$ , then the value of  $x$  is equal to:

- A. 2
- B. 3
- C.  $\frac{1}{2}$
- D. 1
- E. 4

17. Given that  $10^{2n+1} = 0.0000001$ , find  $n$ .

- A. -7
- B. -6
- C.  $-\frac{3}{4}$
- D. 4
- E. -4

18. The result of dividing  $\left(\frac{x^a}{x^b}\right)^{a-b}$  by  $\left(\frac{x^{a+b}}{x^{a-b}}\right)^{\frac{a^2}{b}}$  is:

- A.
- B.
- C.
- D.

19. If  $\sqrt[3]{81} = 3^x$ , find the value of  $x$ .

- A.  $\frac{4}{3}$
- B.  $-\frac{4}{3}$
- C.  $\frac{3}{4}$



D.  $-\frac{3}{4}$

20. Simplify:  $\frac{x(x+1)^{-\frac{1}{2}} - (x+1)^{\frac{1}{2}}}{(x+1)^{\frac{1}{2}}}$ .

A.  $\frac{1}{x+1}$

B.  $-\frac{1}{x+1}$

C.  $\frac{1}{x}$

D.  $-\frac{1}{\sqrt{x+1}}$

21. Express in standard form:

$$\frac{0.8 \times 0.8 \times 0.8 - 0.5 \times 0.5 \times 0.5}{0.8 \times 0.8 + 0.8 \times 0.5 + 0.5 \times 0.5}$$

A.  $8 \times 10^{-1}$

B.  $4 \times 10^{-1}$

C.  $3 \times 10^{-1}$

D.  $1.3 \times 10^{-1}$

22. Express in standard form:

$$\frac{69842 \times 69842 - 30158 \times 30158}{69842 - 30158}$$

A.  $3.0158 \times 10^{-4}$

B.  $10^{-4}$

C.  $6.9842 \times 10^{-5}$

D.  $10^{-5}$

E.  $10^5$

23. The value of  $\frac{9^2 \times 18^4}{3^{16}}$  is:

A.  $\frac{2}{3}$

B.  $\frac{4}{9}$

C.  $\frac{32}{243}$

D.  $\frac{16}{81}$

24. If  $m$  and  $n$  are whole numbers such that  $m^n = 121$ , then  $(m-1)^{n+1}$  is:

A. 10

B.  $10^2$

C.  $10^3$

D.  $10^4$

25. Simplify:  $\frac{a^{\frac{1}{2}} + a^{-\frac{1}{2}}}{1-a} + \frac{1-a^{\frac{1}{2}}}{1+\sqrt{a}}$ .

A.  $\frac{a}{a-1}$

B.  $\frac{a-1}{2}$

C.  $\frac{2}{a-1}$

D.  $\frac{2}{1-a}$

26. Simplify:  $\left(\frac{1}{64}\right)^0 + (64)^{-\frac{1}{2}} + (-32)^{\frac{4}{3}}$ .

A.  $17\frac{1}{8}$

B.  $11\frac{7}{8}$

C.  $17\frac{3}{8}$

D.  $17\frac{7}{8}$

27. If  $\left(\frac{x}{y}\right)^{5a-3} = \left(\frac{y}{x}\right)^{17-3a}$ , what is the value of  $a$ ?

A.  $-7$

B.  $-5$

C. 0

D. 3

28. Evaluate:  $\frac{(0.064 - 0.008)(0.16 - 0.04)}{(0.16 + 0.08 + 0.04)(0.4 + 0.2)^3}$ .

A.  $\frac{1}{3}$

B. 3

C.  $\frac{3}{2}$

D.  $\frac{2}{3}$

29. The value of  $\left[\left(\sqrt[n]{x^2}\right)^{n/2}\right]^2$  is:

A.  $\frac{1}{x^2}$

B.  $x$

C.  $x^2$

D.  $x^{\frac{n}{2}}$

30. Solve for  $x$  if  $3^x - 3^{x-1} = 486$ .
- A. 5  
B. 6  
C. 7  
D. 9
31. If  $5\sqrt{5} \times 5^3 \div 5^{-\frac{3}{2}} = 5^{a+2}$ , then the value of  $a$  is:
- A. 4  
B. 5  
C. 6  
D. 8
32. If  $(\sqrt{3})^5 \times 9^2 = 3^n \times 3\sqrt{3}$ , find  $n$ .
- A. 2  
B. 3  
C. 4  
D. 5
33. The value of  $\frac{243^{\frac{n}{5}} \times 3^{2n+1}}{9^n \times 3^{n-1}}$  is:
- A. 3  
B. 6  
C. 9  
D. 12
34. If  $k^a k^b k^c = 1$ , then the value of  $a^3 + b^3 + c^3$  is:
- A. 9  
B.  $a + b + c$   
C.  $abc$   
D.  $3abc$
35. The value of  $\frac{81^{3.6} \times 9^{2.7}}{81^{4.2} \times 3}$  is:
- A. 3  
B. 6  
C. 9  
D. 8.2
36. Simplify:  $\frac{6^{2n+1} \times 9^n \times 4^{2n}}{18^n \times 2^n \times 12^{2n}}$ .
- A.  $3^{2n}$   
B.  $3 \times 2^{n+1}$   
C.  $2n$   
D. 6  
E. 1
37. Solve the system of equations:  $2^{x+y} = 32$  and  $3^{3y-x} = 27$ . Find  $(x, y)$ .
- A.  $(-3, 2)$   
B.  $(-3, -2)$   
C.  $(3, 2)$   
D.  $(2, 2)$   
E.  $(3, -2)$
38. Evaluate:  $256^{\frac{3}{4}} \times 256^{-\frac{1}{4}}$ .
- A. 4  
B. 8  
C. 16  
D. 64
39. If  $8^x = \frac{1}{4}$ , find the value of  $x$ .
- A.  $-\frac{2}{3}$   
B.  $-\frac{1}{2}$   
C.  $\frac{1}{3}$   
D.  $\frac{2}{3}$
40. Simplify:  $\frac{2^{-3} \times 8^2}{4^{-1}}$ .
- A. 16  
B. 32  
C. 64  
D. 128
41. If  $27^{x+2} = 9^{2x-3}$ , find  $x$ .
- A. 9  
B. 12  
C. 15  
D. 18
42. Evaluate:  $(0.25)^{-\frac{1}{2}}$ .
- A.  $\frac{1}{4}$   
B.  $\frac{1}{2}$   
C. 2  
D. 4
43. Express 0.000215 in standard form.

- A.  $2.15 \times 10^{-4}$   
B.  $2.15 \times 10^{-3}$   
C.  $21.5 \times 10^{-5}$   
D.  $2.15 \times 10^4$
44. If  $2^{x-1} \times 4^{x+1} = 8^x$ , find  $x$ .  
A. 1  
B. 2  
C. 3  
D. 4
45. Simplify:  $\frac{16^{\frac{3}{4}} \times 2^3}{4^{\frac{1}{2}}}$ .  
A. 8  
B. 16  
C. 32  
D. 64
46. If  $(0.5)^{1-x} = 8$ , find  $x$ .  
A. -4  
B. -2  
C. 2  
D. 4
47. Express in standard form:  $\frac{0.00056 \times 3500}{0.07 \times 0.004}$ .  
A.  $7 \times 10^3$   
B.  $7 \times 10^2$   
C.  $7 \times 10^{-3}$   
D.  $7 \times 10^{-2}$
48. Evaluate:  $27^{\frac{2}{3}} - 16^{\frac{3}{4}}$ .  
A. 1  
B. 2  
C. 3  
D. 4
49. If  $5^{2x-3} = 125$ , find  $x$ .  
A. 2  
B. 3  
C. 4  
D. 5
50. Simplify:  $(81)^{\frac{3}{4}} \times (81)^{-\frac{1}{4}}$ .  
A. 3  
B. 9  
C. 27  
D. 81
51. Express 3,450,000 in standard form.  
A.  $3.45 \times 10^5$   
B.  $3.45 \times 10^6$   
C.  $34.5 \times 10^5$   
D.  $345 \times 10^4$
52. If  $\frac{9^x}{3^{2x-1}} = 27$ , find  $x$ .  
A. 1  
B. 2  
C. 3  
D. 4
53. Evaluate:  $\left(\frac{1}{125}\right)^{-\frac{2}{3}}$   
A. 5  
B. 25  
C. 125  
D. 625
54. Simplify:  $2^{n+1} - 2^n$   
A.  $2^n$   
B.  $2^{n-1}$   
C. 2  
D. 1
55. If  $4^{x+1} = 8^{x-2}$ , find  $x$   
A. 5  
B. 6  
C. 7  
D. 8
56. Express 0.000000482 in standard form  
A.  $4.82 \times 10^{-7}$   
B.  $4.82 \times 10^{-6}$   
C.  $48.2 \times 10^{-8}$   
D.  $482 \times 10^{-9}$
57. Evaluate:  $\frac{8^{\frac{2}{3}} \times 4^{\frac{1}{2}}}{2^3}$   
A.  $\frac{1}{2}$   
B. 1

- C. 2  
D. 4
58. If  $2^x + 2^{x+1} = 48$ , find  $x$   
A. 3  
B. 4  
C. 5  
D. 6
59. Simplify:  $\frac{625^{\frac{1}{4}} \times 125^{\frac{1}{3}}}{5^2}$   
A. 1  
B. 5  
C. 25  
D. 125
60. Express in standard form:  $(3.5 \times 10^4) \times (2 \times 10^{-3})$   
A.  $7 \times 10^1$   
B.  $7 \times 10^{-1}$   
C.  $7 \times 10^2$   
D.  $7 \times 10^7$
61. If  $16^{x-\frac{1}{2}} = 4^{2x}$ , find  $x$   
A. -1  
B.  $-\frac{1}{2}$   
C.  $\frac{1}{2}$   
D. 1
62. Evaluate:  $49^{\frac{1}{2}} - 32^{\frac{2}{5}}$   
A. 1  
B. 2  
C. 3  
D. 4
63. Simplify:  $\frac{3^{n+2} - 3^n}{3^{n+1}}$   
A.  $\frac{8}{3}$   
B. 2  
C. 3  
D. 8
64. If  $\sqrt[3]{8^x} = 4$ , find  $x$   
A. 1  
B. 2  
C. 3  
D. 4
65. Express  $\frac{7200000}{0.0024}$  in standard form  
A.  $3 \times 10^9$   
B.  $3 \times 10^{10}$   
C.  $3 \times 10^8$   
D.  $3 \times 10^7$
66. Evaluate:  $(64)^{-\frac{2}{3}} + (27)^{-\frac{1}{3}}$   
A.  $\frac{1}{3}$   
B.  $\frac{5}{12}$   
C.  $\frac{7}{12}$   
D. 1
67. If  $25^{1-x} = \frac{1}{125}$ , find  $x$   
A.  $\frac{5}{2}$   
B.  $\frac{3}{2}$   
C. 2  
D.  $\frac{7}{2}$
68. Simplify:  $(8^{-1} \times 2^5)^2$   
A. 4  
B. 8  
C. 16  
D. 32
69. Express in standard form:  $\frac{8.4 \times 10^6}{2.1 \times 10^{-3}}$   
A.  $4 \times 10^9$   
B.  $4 \times 10^8$   
C.  $4 \times 10^{10}$   
D.  $4 \times 10^3$
70. If  $3^{2x+1} = 27^{x-1}$ , find  $x$   
A. -2  
B. -3  
C. -4  
D. -5

71. Evaluate:  $\left(\frac{16}{81}\right)^{-\frac{3}{4}}$

A.  $\frac{8}{27}$

B.  $\frac{27}{8}$

C.  $\frac{2}{3}$

D.  $\frac{3}{2}$

72. Simplify:  $5^{n-1} + 5^{n+1}$

A.  $\frac{26}{5} \times 5^n$

B.  $26 \times 5^{n-1}$

C.  $5^{2n}$

D.  $2 \times 5^n$

73. If  $\sqrt{32^x} = 8$ , find  $x$

A.  $\frac{3}{5}$

B.  $\frac{2}{5}$

C.  $\frac{4}{5}$

D.  $\frac{1}{5}$

74. Express  $562,000 \times 0.00003$  in standard form

A.  $1.686 \times 10^1$

B.  $1.686 \times 10^{-1}$

C.  $16.86 \times 10^0$

D.  $1.686 \times 10^2$

75. Evaluate:  $100^{\frac{3}{2}} - 64^{\frac{1}{2}}$

A. 992

B. 936

C. 1000

D. 994

76. If  $7^{x+2} = \frac{1}{49}$ , find  $x$

A. -4

B. -3

C. -2

D. -1

77. Simplify:  $\frac{2^{2n} \times 4^n}{8^n}$

A. 1

B. 2

C.  $2^n$

D.  $4^n$

78. Express in standard form:  $\sqrt{0.000144}$

A.  $1.2 \times 10^{-2}$

B.  $1.2 \times 10^{-1}$

C.  $12 \times 10^{-3}$

D.  $1.2 \times 10^{-3}$

79. If  $4^{3x-2} = 64^{x+1}$ , find  $x$

A. 2

B. 3

C. 4

D. 5

80. Evaluate:  $(0.04)^{-\frac{3}{2}}$

A. 125

B. 25

C. 5

D. 625

81. Simplify:  $\frac{(x^2)^3 \times x^{-4}}{x^3}$

A.  $x$

B.  $x^{-1}$

C.  $x^2$

D.  $x^{-2}$

82. If  $9^{x-1} = 3^{x+3}$ , find  $x$

A. 3

B. 4

C. 5

D. 6

83. Express in standard form:  $\frac{0.0081 \times 0.012}{0.027}$

A.  $3.6 \times 10^{-3}$

B.  $3.6 \times 10^{-2}$

C.  $36 \times 10^{-4}$

D.  $3.6 \times 10^{-4}$

84. Evaluate:  $243^{\frac{2}{5}} \times 32^{\frac{3}{5}}$

A. 48

- B. 54  
C. 72  
D. 36
85. If  $2^{x-y} = 8$  and  $2^{x+y} = 32$ , find  $x$   
A. 3  
B. 4  
C. 5  
D. 6
86. Simplify:  $\frac{a^{\frac{1}{3}} \times a^{\frac{2}{3}}}{a^{-\frac{1}{2}}}$   
A.  $a^{\frac{1}{2}}$   
B.  $a^{\frac{3}{2}}$   
C.  $a^2$   
D.  $a$
87. If  $\sqrt[4]{16^x} = 8$ , find  $x$   
A. 2  
B. 3  
C. 4  
D. 5
88. Express in standard form:  $(6 \times 10^5) \div (3 \times 10^{-2})$   
A.  $2 \times 10^7$   
B.  $2 \times 10^6$   
C.  $2 \times 10^3$   
D.  $2 \times 10^{-7}$
89. Evaluate:  $125^{\frac{2}{3}} - 36^{\frac{1}{2}}$   
A. 13  
B. 19  
C. 21  
D. 25
90. If  $5^{2x} - 7(5^x) + 10 = 0$ , find  $x$   
A. 0 or 1  
B. 1 or 2  
C. 0 or 2  
D. 1 or  $\log_5 2$
91. Simplify:  $\frac{10^{n+2} - 10^n}{99 \times 10^n}$   
A. 1  
B. 10
- C.  $\frac{1}{10}$   
D. 99
92. If  $(0.125)^x = 8$ , find  $x$   
A. -1  
B. -2  
C. -3  
D. 3
93. Express in standard form:  $\sqrt{6.4 \times 10^{-5}}$   
A.  $8 \times 10^{-3}$   
B.  $8 \times 10^{-2}$   
C.  $2.53 \times 10^{-3}$   
D.  $2.53 \times 10^{-2}$
94. Evaluate:  $\left(27^{\frac{1}{3}} + 8^{\frac{1}{3}}\right)^2$   
A. 25  
B. 49  
C. 64  
D. 81
95. If  $3^{x+1} + 3^{x-1} = 90$ , find  $x$   
A. 2  
B. 3  
C. 4  
D. 5
96. Simplify:  $\left(\frac{125}{8}\right)^{-\frac{2}{3}} \times \left(\frac{25}{4}\right)^{\frac{1}{2}}$   
A. 1  
B. 2  
C. 3  
D. 4
97. If  $2^a = 3$  and  $2^b = 5$ , find  $2^{2a+b}$   
A. 15  
B. 30  
C. 45  
D. 60
98. Express  $\frac{72 \times 10^{-5} \times 25 \times 10^3}{18 \times 10^{-2}}$  in standard form  
A.  $1 \times 10^1$   
B.  $1 \times 10^2$   
C.  $1 \times 10^3$

D.  $1 \times 10^4$

99. If  $4^{x+2} - 4^x = 240$ , find  $x$

- A. 1
- B. 2
- C. 3
- D. 4

100. Simplify:  $\frac{(2^{n+1})^2 \times 4^{n-1}}{8^n}$

- A. 2
- B. 4
- C. 8
- D.  $2^n$

## 2.3 Surds

### 2.3.1 Questions

1. Simplify:  $\sqrt{50}$

- A.  $5\sqrt{2}$
- B.  $2\sqrt{5}$
- C.  $10\sqrt{2}$
- D.  $25\sqrt{2}$

2. Simplify:  $\sqrt{75} + \sqrt{12}$

- A.  $7\sqrt{3}$
- B.  $5\sqrt{3} + 2\sqrt{3}$
- C.  $\sqrt{87}$
- D.  $8\sqrt{3}$

3. Rationalize the denominator:  $\frac{6}{\sqrt{3}}$

- A.  $2\sqrt{3}$
- B.  $3\sqrt{2}$
- C.  $6\sqrt{3}$
- D.  $\sqrt{18}$

4. Simplify:  $\sqrt{128}$

- A.  $8\sqrt{2}$
- B.  $4\sqrt{8}$
- C.  $16\sqrt{2}$
- D.  $2\sqrt{32}$

5. Evaluate:  $(\sqrt{5})^2$

- A. 25
- B. 5
- C. 10
- D.  $\sqrt{25}$

6. Simplify:  $\sqrt{18} - \sqrt{8}$

- A.  $\sqrt{10}$

B.  $\sqrt{2}$

C.  $2\sqrt{2}$

D.  $3\sqrt{2} - 2\sqrt{2}$

7. Multiply:  $\sqrt{3} \times \sqrt{12}$

- A. 6
- B.  $3\sqrt{4}$
- C.  $\sqrt{36}$
- D.  $2\sqrt{6}$

8. Rationalize:  $\frac{10}{\sqrt{5}}$

- A.  $2\sqrt{5}$
- B.  $5\sqrt{2}$
- C.  $\sqrt{20}$
- D.  $10\sqrt{5}$

9. Simplify:  $3\sqrt{8} + 2\sqrt{2}$

- A.  $5\sqrt{10}$
- B.  $8\sqrt{2}$
- C.  $5\sqrt{2}$
- D.  $6\sqrt{2} + 2\sqrt{2}$

10. Express in simplest form:  $\sqrt{200}$

- A.  $10\sqrt{2}$
- B.  $20\sqrt{2}$
- C.  $100\sqrt{2}$
- D.  $2\sqrt{100}$

11. Simplify:  $\frac{\sqrt{48}}{\sqrt{3}}$

- A. 4
- B. 16
- C.  $\sqrt{16}$

- D.  $2\sqrt{4}$
12. Evaluate:  $\sqrt{2} \times \sqrt{8}$
- A. 4  
B.  $\sqrt{16}$   
C.  $2\sqrt{4}$   
D.  $\sqrt{10}$
13. Simplify:  $\sqrt{45} - \sqrt{20}$
- A.  $\sqrt{25}$   
B.  $\sqrt{5}$   
C.  $3\sqrt{5} - 2\sqrt{5}$   
D.  $5\sqrt{5}$
14. Rationalize:  $\frac{8}{\sqrt{2}}$
- A.  $4\sqrt{2}$   
B.  $8\sqrt{2}$   
C.  $2\sqrt{8}$   
D.  $16\sqrt{2}$
15. Simplify:  $2\sqrt{27} + \sqrt{12}$
- A.  $8\sqrt{3}$   
B.  $6\sqrt{3} + 2\sqrt{3}$   
C.  $7\sqrt{3}$   
D.  $9\sqrt{3}$
16. Express  $\sqrt{72}$  in simplest surd form
- A.  $6\sqrt{2}$   
B.  $8\sqrt{3}$   
C.  $9\sqrt{2}$   
D.  $12\sqrt{6}$
17. Multiply and simplify:  $\sqrt{6} \times \sqrt{24}$
- A. 12  
B.  $\sqrt{144}$   
C.  $6\sqrt{4}$   
D.  $2\sqrt{36}$
18. Rationalize the denominator:  $\frac{15}{\sqrt{3}}$
- A.  $5\sqrt{3}$   
B.  $3\sqrt{5}$   
C.  $15\sqrt{3}$   
D.  $\sqrt{75}$
19. Simplify:  $\sqrt{98} + \sqrt{32}$
- A.  $11\sqrt{2}$   
B.  $7\sqrt{2} + 4\sqrt{2}$   
C.  $\sqrt{130}$   
D.  $9\sqrt{2}$
20. Evaluate:  $\frac{\sqrt{50}}{\sqrt{2}}$
- A. 5  
B. 25  
C.  $\sqrt{25}$   
D. 10
21. Simplify:  $4\sqrt{5} - 2\sqrt{5}$
- A.  $2\sqrt{5}$   
B.  $6\sqrt{5}$   
C.  $2\sqrt{0}$   
D.  $8\sqrt{5}$
22. Expand and simplify:  $(\sqrt{3} + 2)(\sqrt{3} - 2)$
- A. -1  
B. 1  
C.  $3 - 4$   
D. 7
23. Rationalize:  $\frac{12}{\sqrt{6}}$
- A.  $2\sqrt{6}$   
B.  $6\sqrt{2}$   
C.  $\sqrt{24}$   
D.  $12\sqrt{6}$
24. Simplify:  $\sqrt{180}$
- A.  $6\sqrt{5}$   
B.  $9\sqrt{2}$   
C.  $3\sqrt{20}$   
D.  $18\sqrt{10}$
25. Evaluate:  $\sqrt{7} \times \sqrt{7}$
- A. 7  
B. 14  
C. 49  
D.  $\sqrt{14}$
26. Simplify:  $\sqrt{125} - \sqrt{45}$



- A.  $2\sqrt{5}$   
B.  $5\sqrt{5} - 3\sqrt{5}$   
C.  $8\sqrt{5}$   
D.  $\sqrt{80}$
27. Rationalize:  $\frac{20}{\sqrt{10}}$   
A.  $2\sqrt{10}$   
B.  $10\sqrt{2}$   
C.  $\sqrt{200}$   
D.  $20\sqrt{10}$
28. Simplify:  $3\sqrt{12} + 4\sqrt{3}$   
A.  $10\sqrt{3}$   
B.  $6\sqrt{3} + 4\sqrt{3}$   
C.  $7\sqrt{15}$   
D.  $12\sqrt{3}$
29. Express in simplest form:  $\sqrt{162}$   
A.  $9\sqrt{2}$   
B.  $6\sqrt{3}$   
C.  $81\sqrt{2}$   
D.  $3\sqrt{18}$
30. Multiply:  $\sqrt{10} \times \sqrt{40}$   
A. 20  
B.  $\sqrt{400}$   
C.  $10\sqrt{4}$   
D.  $4\sqrt{100}$
31. Rationalize the denominator:  $\frac{18}{\sqrt{2}}$   
A.  $9\sqrt{2}$   
B.  $2\sqrt{9}$   
C.  $18\sqrt{2}$   
D.  $\sqrt{162}$
32. Simplify:  $\sqrt{300}$   
A.  $10\sqrt{3}$   
B.  $3\sqrt{100}$   
C.  $30\sqrt{10}$   
D.  $100\sqrt{3}$
33. Evaluate:  $\frac{\sqrt{72}}{\sqrt{8}}$   
A. 3  
B. 9  
C.  $\sqrt{9}$   
D. 6
34. Simplify:  $5\sqrt{2} + 3\sqrt{2}$   
A.  $8\sqrt{2}$   
B.  $15\sqrt{4}$   
C.  $8\sqrt{4}$   
D.  $\sqrt{64}$
35. Expand:  $(\sqrt{5} + 1)^2$   
A.  $6 + 2\sqrt{5}$   
B.  $5 + 1$   
C. 26  
D. 6
36. Rationalize:  $\frac{24}{\sqrt{8}}$   
A.  $3\sqrt{8}$   
B.  $6\sqrt{2}$   
C.  $8\sqrt{3}$   
D.  $12\sqrt{2}$
37. Simplify:  $\sqrt{112}$   
A.  $4\sqrt{7}$   
B.  $7\sqrt{4}$   
C.  $8\sqrt{14}$   
D.  $56\sqrt{2}$
38. Multiply and simplify:  $\sqrt{5} \times \sqrt{20}$   
A. 10  
B.  $5\sqrt{4}$   
C.  $\sqrt{100}$   
D. 20
39. Simplify:  $\sqrt{147} - \sqrt{27}$   
A.  $4\sqrt{3}$   
B.  $7\sqrt{3} - 3\sqrt{3}$   
C.  $\sqrt{120}$   
D.  $10\sqrt{3}$
40. Rationalize:  $\frac{14}{\sqrt{7}}$   
A.  $2\sqrt{7}$   
B.  $7\sqrt{2}$

- C.  $\sqrt{98}$   
D.  $14\sqrt{7}$
41. Simplify:  $2\sqrt{18} + 3\sqrt{2}$   
A.  $9\sqrt{2}$   
B.  $6\sqrt{2} + 3\sqrt{2}$   
C.  $5\sqrt{20}$   
D.  $11\sqrt{2}$
42. Express in simplest form:  $\sqrt{242}$   
A.  $11\sqrt{2}$   
B.  $121\sqrt{2}$   
C.  $2\sqrt{121}$   
D.  $22\sqrt{11}$
43. Evaluate:  $\frac{\sqrt{108}}{\sqrt{3}}$   
A. 6  
B. 36  
C.  $\sqrt{36}$   
D.  $3\sqrt{4}$
44. Simplify:  $7\sqrt{3} - 2\sqrt{3}$   
A.  $5\sqrt{3}$   
B.  $9\sqrt{3}$   
C.  $5\sqrt{0}$   
D.  $14\sqrt{6}$
45. Expand and simplify:  $(\sqrt{2} + 3)(\sqrt{2} - 3)$   
A. -7  
B.  $2 - 9$   
C. 11  
D. -5
46. Rationalize:  $\frac{30}{\sqrt{5}}$   
A.  $6\sqrt{5}$   
B.  $5\sqrt{6}$   
C.  $\sqrt{180}$   
D.  $30\sqrt{5}$
47. Simplify:  $\sqrt{245}$   
A.  $7\sqrt{5}$   
B.  $5\sqrt{7}$   
C.  $49\sqrt{5}$   
D.  $\sqrt{49 \times 5}$
48. Multiply:  $\sqrt{15} \times \sqrt{15}$   
A. 15  
B. 30  
C. 225  
D.  $\sqrt{30}$
49. Simplify:  $\sqrt{192} - \sqrt{48}$   
A.  $4\sqrt{3}$   
B.  $8\sqrt{3} - 4\sqrt{3}$   
C.  $\sqrt{144}$   
D.  $12\sqrt{3}$
50. Rationalize:  $\frac{16}{\sqrt{4}}$   
A. 8  
B.  $4\sqrt{4}$   
C.  $16\sqrt{4}$   
D. 32
51. Simplify:  $4\sqrt{20} + 2\sqrt{5}$   
A.  $10\sqrt{5}$   
B.  $8\sqrt{5} + 2\sqrt{5}$   
C.  $6\sqrt{25}$   
D.  $20\sqrt{5}$
52. Express in simplest form:  $\sqrt{288}$   
A.  $12\sqrt{2}$   
B.  $144\sqrt{2}$   
C.  $2\sqrt{144}$   
D.  $24\sqrt{3}$
53. Evaluate:  $\frac{\sqrt{125}}{\sqrt{5}}$   
A. 5  
B. 25  
C.  $\sqrt{25}$   
D. 15
54. Simplify:  $9\sqrt{7} + 4\sqrt{7}$   
A.  $13\sqrt{7}$   
B.  $36\sqrt{14}$   
C.  $13\sqrt{14}$   
D.  $\sqrt{169 \times 7}$
55. Expand:  $(\sqrt{6} + 2)^2$

- A.  $10 + 4\sqrt{6}$   
 B.  $6 + 4$   
 C. 40  
 D. 8
56. Rationalize:  $\frac{21}{\sqrt{3}}$   
 A.  $7\sqrt{3}$   
 B.  $3\sqrt{7}$   
 C.  $21\sqrt{3}$   
 D.  $\sqrt{147}$
57. Simplify:  $\sqrt{343}$   
 A.  $7\sqrt{7}$   
 B.  $49\sqrt{7}$   
 C.  $\sqrt{49 \times 7}$   
 D.  $343\sqrt{1}$
58. Multiply and simplify:  $\sqrt{8} \times \sqrt{18}$   
 A. 12  
 B.  $\sqrt{144}$   
 C.  $2\sqrt{36}$   
 D.  $4\sqrt{9}$
59. Simplify:  $\sqrt{175} + \sqrt{63}$   
 A.  $8\sqrt{7}$   
 B.  $5\sqrt{7} + 3\sqrt{7}$   
 C.  $\sqrt{238}$   
 D.  $15\sqrt{7}$
60. Rationalize:  $\frac{25}{\sqrt{5}}$   
 A.  $5\sqrt{5}$   
 B.  $25\sqrt{5}$   
 C.  $\sqrt{125}$   
 D. 125
61. Simplify:  $5\sqrt{32} - 2\sqrt{2}$   
 A.  $18\sqrt{2}$   
 B.  $20\sqrt{2} - 2\sqrt{2}$   
 C.  $3\sqrt{30}$   
 D.  $8\sqrt{2}$
62. Express in simplest form:  $\sqrt{392}$   
 A.  $14\sqrt{2}$   
 B.  $196\sqrt{2}$   
 C.  $2\sqrt{196}$   
 D.  $28\sqrt{7}$
63. Evaluate:  $\frac{\sqrt{200}}{\sqrt{8}}$   
 A. 5  
 B. 25  
 C.  $\sqrt{25}$   
 D. 10
64. Simplify:  $6\sqrt{11} - 2\sqrt{11}$   
 A.  $4\sqrt{11}$   
 B.  $8\sqrt{11}$   
 C.  $4\sqrt{0}$   
 D.  $12\sqrt{22}$
65. Expand and simplify:  $(\sqrt{10} + 1)(\sqrt{10} - 1)$   
 A. 9  
 B.  $10 - 1$   
 C. 11  
 D. -9
66. Rationalize:  $\frac{35}{\sqrt{7}}$   
 A.  $5\sqrt{7}$   
 B.  $7\sqrt{5}$   
 C.  $\sqrt{245}$   
 D.  $35\sqrt{7}$
67. Simplify:  $\sqrt{450}$   
 A.  $15\sqrt{2}$   
 B.  $225\sqrt{2}$   
 C.  $2\sqrt{225}$   
 D.  $9\sqrt{50}$
68. Multiply:  $\sqrt{6} \times \sqrt{54}$   
 A. 18  
 B.  $\sqrt{324}$   
 C.  $6\sqrt{9}$   
 D.  $3\sqrt{36}$
69. Simplify:  $\sqrt{243} - \sqrt{48}$   
 A.  $5\sqrt{3}$   
 B.  $9\sqrt{3} - 4\sqrt{3}$   
 C.  $\sqrt{195}$

- D.  $13\sqrt{3}$
70. Rationalize:  $\frac{40}{\sqrt{10}}$
- A.  $4\sqrt{10}$   
 B.  $10\sqrt{4}$   
 C.  $\sqrt{160}$   
 D.  $40\sqrt{10}$
71. Simplify:  $3\sqrt{50} + 4\sqrt{2}$
- A.  $19\sqrt{2}$   
 B.  $15\sqrt{2} + 4\sqrt{2}$   
 C.  $7\sqrt{52}$   
 D.  $12\sqrt{100}$
72. Express in simplest form:  $\sqrt{500}$
- A.  $10\sqrt{5}$   
 B.  $250\sqrt{2}$   
 C.  $5\sqrt{100}$   
 D.  $100\sqrt{5}$
73. Evaluate:  $\frac{\sqrt{180}}{\sqrt{5}}$
- A. 6  
 B. 36  
 C.  $\sqrt{36}$   
 D.  $3\sqrt{4}$
74. Simplify:  $10\sqrt{3} + 5\sqrt{3}$
- A.  $15\sqrt{3}$   
 B.  $50\sqrt{9}$   
 C.  $15\sqrt{6}$   
 D.  $\sqrt{675}$
75. Expand:  $(\sqrt{11} + 3)^2$
- A.  $20 + 6\sqrt{11}$   
 B.  $11 + 9$   
 C. 121  
 D. 14
76. Rationalize:  $\frac{42}{\sqrt{6}}$
- A.  $7\sqrt{6}$   
 B.  $6\sqrt{7}$   
 C.  $42\sqrt{6}$   
 D.  $\sqrt{252}$
77. Simplify:  $\sqrt{512}$
- A.  $16\sqrt{2}$   
 B.  $256\sqrt{2}$   
 C.  $2\sqrt{256}$   
 D.  $8\sqrt{64}$
78. Multiply and simplify:  $\sqrt{12} \times \sqrt{27}$
- A. 18  
 B.  $\sqrt{324}$   
 C.  $6\sqrt{9}$   
 D.  $3\sqrt{36}$
79. Simplify:  $\sqrt{320} + \sqrt{80}$
- A.  $12\sqrt{5}$   
 B.  $8\sqrt{5} + 4\sqrt{5}$   
 C.  $\sqrt{400}$   
 D.  $20\sqrt{5}$
80. Rationalize:  $\frac{48}{\sqrt{12}}$
- A.  $4\sqrt{12}$   
 B.  $12\sqrt{4}$   
 C.  $4\sqrt{3}$   
 D.  $8\sqrt{3}$
81. Simplify:  $6\sqrt{45} - 3\sqrt{5}$
- A.  $15\sqrt{5}$   
 B.  $18\sqrt{5} - 3\sqrt{5}$   
 C.  $3\sqrt{40}$   
 D.  $21\sqrt{5}$
82. Express in simplest form:  $\sqrt{578}$
- A.  $17\sqrt{2}$   
 B.  $289\sqrt{2}$   
 C.  $2\sqrt{289}$   
 D.  $34\sqrt{17}$
83. Evaluate:  $\frac{\sqrt{243}}{\sqrt{3}}$
- A. 9  
 B. 81  
 C.  $\sqrt{81}$   
 D. 27
84. Simplify:  $8\sqrt{13} + 7\sqrt{13}$

- A.  $15\sqrt{13}$   
B.  $56\sqrt{26}$   
C.  $15\sqrt{26}$   
D.  $\sqrt{3575}$
85. Expand and simplify:  $(\sqrt{7} + 4)(\sqrt{7} - 4)$   
A.  $-9$   
B.  $7 - 16$   
C.  $23$   
D.  $-7$
86. Rationalize:  $\frac{56}{\sqrt{8}}$   
A.  $7\sqrt{8}$   
B.  $14\sqrt{2}$   
C.  $8\sqrt{7}$   
D.  $28\sqrt{2}$
87. Simplify:  $\sqrt{605}$   
A.  $11\sqrt{5}$   
B.  $121\sqrt{5}$   
C.  $5\sqrt{121}$   
D.  $\sqrt{121 \times 5}$
88. Multiply:  $\sqrt{11} \times \sqrt{44}$   
A.  $22$   
B.  $\sqrt{484}$   
C.  $11\sqrt{4}$   
D.  $2\sqrt{121}$
89. Simplify:  $\sqrt{363} - \sqrt{27}$   
A.  $8\sqrt{3}$   
B.  $11\sqrt{3} - 3\sqrt{3}$   
C.  $\sqrt{336}$   
D.  $14\sqrt{3}$
90. Rationalize:  $\frac{4}{\sqrt{3} + 1}$   
A.  $2\sqrt{3} - 2$   
B.  $2(\sqrt{3} - 1)$   
C.  $4\sqrt{3} - 4$   
D.  $\sqrt{3} - 1$
91. Simplify:  $\frac{1}{\sqrt{5} - 2}$   
A.  $\sqrt{5} + 2$   
B.  $\frac{\sqrt{5} + 2}{5}$   
C.  $5 + 2$   
D.  $\sqrt{5} - 2$
92. Evaluate:  $(\sqrt{8} + \sqrt{2})(\sqrt{8} - \sqrt{2})$   
A.  $6$   
B.  $8 - 2$   
C.  $10$   
D.  $4$
93. Rationalize:  $\frac{6}{\sqrt{7} - \sqrt{3}}$   
A.  $\frac{3(\sqrt{7} + \sqrt{3})}{2}$   
B.  $\sqrt{7} + \sqrt{3}$   
C.  $3\sqrt{7} + 3\sqrt{3}$   
D.  $6(\sqrt{7} + \sqrt{3})$
94. Simplify:  $\sqrt{12} + \sqrt{27} - \sqrt{75}$   
A.  $0$   
B.  $-2\sqrt{3}$   
C.  $2\sqrt{3}$   
D.  $\sqrt{3}$
95. Evaluate:  $\frac{\sqrt{98} - \sqrt{32}}{\sqrt{2}}$   
A.  $3$   
B.  $7 - 4$   
C.  $11$   
D.  $\sqrt{33}$
96. Rationalize:  $\frac{10}{\sqrt{6} + \sqrt{2}}$   
A.  $\frac{5(\sqrt{6} - \sqrt{2})}{2}$   
B.  $5\sqrt{6} - 5\sqrt{2}$   
C.  $\sqrt{6} - \sqrt{2}$   
D.  $10(\sqrt{6} - \sqrt{2})$
97. Simplify:  $(\sqrt{5} + \sqrt{3})^2$   
A.  $8 + 2\sqrt{15}$   
B.  $5 + 3$   
C.  $64$   
D.  $8 + \sqrt{15}$

98. Evaluate:  $\frac{\sqrt{72} + \sqrt{50}}{\sqrt{2}}$

A. 11

B.  $6 + 5$

C.  $\sqrt{61}$

D. 8

99. Rationalize:  $\frac{8}{\sqrt{5} + \sqrt{3}}$

A.  $4(\sqrt{5} - \sqrt{3})$

B.  $8\sqrt{5} - 8\sqrt{3}$

C.  $\sqrt{5} - \sqrt{3}$

D.  $2(\sqrt{5} - \sqrt{3})$

100. Simplify and rationalize the expression  $\frac{2}{\sqrt{3} - \sqrt{2}}$ .

A.  $\sqrt{3} - \sqrt{2}$

B.  $2\sqrt{3} - 2\sqrt{2}$

C.  $2\sqrt{3} + 2\sqrt{2}$

D.  $\sqrt{3} + \sqrt{2}$

## 2.4 Logarithms

### 2.4.1 Questions

1. Evaluate:  $\log_2 8$ .

A. 2

B. 3

C. 4

D. 8

2. If  $\log_{10} 2 = 0.3010$ , find  $\log_{10} 20$ .

A. 0.6020

B. 1.3010

C. 2.3010

D. 6.020

3. Simplify:  $\log_5 125$ .

A. 1

B. 2

C. 3

D. 5

4. If  $\log_x 81 = 4$ , find  $x$ .

A. 3

B. 4

C. 9

D. 27

5. Evaluate:  $\log_3 1$ .

A. 0

B. 1

C. 3

D. undefined

6. Simplify:  $\log_7 49 + \log_7 7$ .

A. 1

B. 2

C. 3

D. 4

7. If  $\log_{10} 5 = 0.6990$ , find  $\log_{10} 50$ .

A. 0.3010

B. 1.3010

C. 1.6990

D. 3.4950

8. Evaluate:  $\log_4 64$ .

A. 2

B. 3

C. 4

D. 16

9. Simplify:  $\log_2 32 - \log_2 4$ .

A. 2

B. 3

C. 4

D. 8

10. If  $\log_5 x = 3$ , find  $x$ .

A. 8

B. 15

C. 25

D. 125

11. Evaluate:  $2\log_3 9$ .

- A. 2  
B. 3  
C. 4  
D. 6
12. Simplify:  $\log_6 36 + \log_6 1$ .  
A. 0  
B. 1  
C. 2  
D. 3
13. If  $\log_{10} 3 = 0.4771$ , find  $\log_{10} 30$ .  
A. 0.9542  
B. 1.4771  
C. 4.771  
D. 14.313
14. Evaluate:  $\log_8 512$ .  
A. 2  
B. 3  
C. 4  
D. 64
15. Simplify:  $\log_5 25 \times \log_5 5$ .  
A. 1  
B. 2  
C. 3  
D. 5
16. If  $\log_2 x = 5$ , find  $x$ .  
A. 10  
B. 25  
C. 32  
D. 64
17. Evaluate:  $\log_{10} 100$ .  
A. 1  
B. 2  
C. 10  
D. 100
18. Simplify:  $\log_3 81 - \log_3 9$ .  
A. 1  
B. 2  
C. 3  
D. 4
19. If  $\log_{10} 2 = 0.3010$ , find  $\log_{10} 8$ .  
A. 0.6020  
B. 0.9030  
C. 2.408  
D. 8.030
20. Evaluate:  $\log_9 729$ .  
A. 2  
B. 3  
C. 4  
D. 81
21. Simplify:  $3 \log_2 4$ .  
A. 2  
B. 4  
C. 6  
D. 8
22. If  $\log_x 16 = 2$ , find  $x$ .  
A. 2  
B. 4  
C. 8  
D. 32
23. Evaluate:  $\log_5 1$ .  
A. 0  
B. 1  
C. 5  
D. undefined
24. Simplify:  $\log_4 16 + \log_4 4$ .  
A. 2  
B. 3  
C. 4  
D. 5
25. If  $\log_{10} 7 = 0.8451$ , find  $\log_{10} 70$ .  
A. 1.6902  
B. 1.8451  
C. 8.451  
D. 59.157
26. Evaluate:  $\log_6 216$ .  
A. 2

- B. 3  
C. 4  
D. 36
27. Simplify:  $\log_7 343 - \log_7 49$ .  
A. 0  
B. 1  
C. 2  
D. 7
28. If  $\log_3 x = 4$ , find  $x$ .  
A. 12  
B. 27  
C. 64  
D. 81
29. Evaluate:  $\log_{10} 1000$ .  
A. 2  
B. 3  
C. 10  
D. 100
30. Simplify:  $2 \log_5 5 + \log_5 25$ .  
A. 2  
B. 3  
C. 4  
D. 5
31. If  $\log_x 27 = 3$ , find  $x$ .  
A. 3  
B. 9  
C. 27  
D. 81
32. Evaluate:  $\log_2 \frac{1}{8}$ .  
A. -3  
B. -2  
C.  $\frac{1}{3}$   
D. 3
33. Simplify:  $\log_3 27 + \log_3 3$ .  
A. 2  
B. 3  
C. 4  
D. 9
34. If  $\log_{10} 4 = 0.6021$ , find  $\log_{10} 400$ .  
A. 1.2042  
B. 1.6021  
C. 2.6021  
D. 240.84
35. Evaluate:  $\log_5 \frac{1}{25}$ .  
A. -2  
B. -1  
C.  $\frac{1}{2}$   
D. 2
36. Simplify:  $\log_8 64 - \log_8 8$ .  
A. 0  
B. 1  
C. 2  
D. 8
37. If  $\log_4 x = 3$ , find  $x$ .  
A. 12  
B. 16  
C. 64  
D. 81
38. Evaluate:  $3 \log_3 3$ .  
A. 1  
B. 3  
C. 9  
D. 27
39. Simplify:  $\log_2 16 + \log_2 2$ .  
A. 3  
B. 4  
C. 5  
D. 32
40. If  $\log_{10} 6 = 0.7782$ , find  $\log_{10} 60$ .  
A. 1.5564  
B. 1.7782  
C. 7.782



- D. 46.692
41. Evaluate:  $\log_{10} \frac{1}{100}$ .
- A. -2  
B. -1  
C.  $\frac{1}{2}$   
D. 2
42. Simplify:  $\log_9 81 + \log_9 9$ .
- A. 2  
B. 3  
C. 4  
D. 9
43. If  $\log_7 x = 2$ , find  $x$ .
- A. 14  
B. 49  
C. 98  
D. 343
44. Evaluate:  $\log_3 \frac{1}{27}$ .
- A. -3  
B. -2  
C.  $\frac{1}{3}$   
D. 3
45. Simplify:  $2 \log_4 4 + \log_4 16$ .
- A. 2  
B. 3  
C. 4  
D. 6
46. If  $\log_{10} 8 = 0.9031$ , find  $\log_{10} 800$ .
- A. 1.8062  
B. 2.9031  
C. 9.031  
D. 722.48
47. Evaluate:  $\log_6 \frac{1}{36}$ .
- A. -2  
B. -1  
C.  $\frac{1}{2}$
- D. 2
48. Simplify:  $\log_{10} 1000 - \log_{10} 10$ .
- A. 1  
B. 2  
C. 3  
D. 100
49. If  $\log_2 x = 6$ , find  $x$ .
- A. 8  
B. 12  
C. 32  
D. 64
50. Evaluate:  $4 \log_2 2$ .
- A. 2  
B. 4  
C. 8  
D. 16
51. Simplify:  $\log_5 125 + \log_5 5$ .
- A. 2  
B. 3  
C. 4  
D. 5
52. If  $\log_x 125 = 3$ , find  $x$ .
- A. 5  
B. 25  
C. 125  
D. 625
53. Evaluate:  $\log_4 \frac{1}{16}$ .
- A. -2  
B. -1  
C.  $\frac{1}{4}$   
D. 4
54. Simplify:  $\log_7 49 + \log_7 7$ .
- A. 2  
B. 3  
C. 4  
D. 7
55. If  $\log_{10} 9 = 0.9542$ , find  $\log_{10} 900$ .

- A. 1.9084  
B. 2.9542  
C. 9.542  
D. 858.78
56. Evaluate:  $\log_8 \frac{1}{64}$ .  
A. -2  
B. -1  
C.  $\frac{1}{2}$   
D. 2
57. Simplify:  $\log_3 243 - \log_3 27$ .  
A. 1  
B. 2  
C. 3  
D. 9
58. If  $\log_6 x = 3$ , find  $x$ .  
A. 18  
B. 36  
C. 216  
D. 1296
59. Evaluate:  $\log_{10} \frac{1}{1000}$ .  
A. -3  
B. -2  
C.  $\frac{1}{3}$   
D. 3
60. Simplify:  $3 \log_5 5 + \log_5 1$ .  
A. 1  
B. 2  
C. 3  
D. 5
61. If  $\log_x 64 = 3$ , find  $x$ .  
A. 2  
B. 4  
C. 8  
D. 16
62. Evaluate:  $\log_9 \frac{1}{81}$ .  
A. -2  
B. -1  
C.  $\frac{1}{2}$   
D. 2
63. Simplify:  $\log_2 64 + \log_2 4$ .  
A. 6  
B. 8  
C. 10  
D. 256
64. If  $\log_8 x = 2$ , find  $x$ .  
A. 16  
B. 64  
C. 128  
D. 512
65. Evaluate:  $5 \log_3 3$ .  
A. 3  
B. 5  
C. 15  
D. 243
66. Simplify:  $\log_6 216 - \log_6 36$ .  
A. 0  
B. 1  
C. 2  
D. 6
67. If  $\log_{10} x = 2$ , find  $x$ .  
A. 2  
B. 10  
C. 20  
D. 100
68. Evaluate:  $\log_7 \frac{1}{343}$ .  
A. -3  
B. -2  
C.  $\frac{1}{3}$   
D. 3
69. Simplify:  $2 \log_6 6 + \log_6 36$ .  
A. 2  
B. 3

- C. 4  
D. 6
70. If  $\log_5 x = 4$ , find  $x$ .  
A. 20  
B. 125  
C. 625  
D. 3125
71. Evaluate:  $\log_{10} \sqrt{10}$ .  
A.  $\frac{1}{2}$   
B. 1  
C. 2  
D. 5
72. Simplify:  $\log_4 256 - \log_4 16$ .  
A. 1  
B. 2  
C. 3  
D. 4
73. If  $\log_x 32 = 5$ , find  $x$ .  
A. 2  
B. 4  
C. 8  
D. 16
74. Evaluate:  $\log_5 \frac{1}{125}$ .  
A. -3  
B. -2  
C.  $\frac{1}{3}$   
D. 3
75. Simplify:  $\log_8 512 + \log_8 8$ .  
A. 3  
B. 4  
C. 5  
D. 8
76. If  $\log_9 x = 2$ , find  $x$ .  
A. 18  
B. 81  
C. 162  
D. 729
77. Evaluate:  $\log_{10} \sqrt[3]{10}$ .  
A.  $\frac{1}{3}$   
B. 1  
C. 3  
D. 10
78. Simplify:  $3 \log_2 2 + 2 \log_2 4$ .  
A. 5  
B. 6  
C. 7  
D. 8
79. If  $\log_3 x = 5$ , find  $x$ .  
A. 15  
B. 81  
C. 243  
D. 729
80. Evaluate:  $\log_{10} 0.01$ .  
A. -2  
B. -1  
C. 0.01  
D. 2
81. Simplify:  $\log_5 625 - \log_5 25$ .  
A. 1  
B. 2  
C. 3  
D. 5
82. If  $\log_x 1000 = 3$ , find  $x$ .  
A. 10  
B. 100  
C. 333  
D. 1000
83. Evaluate:  $\log_{10} \sqrt[4]{10}$ .  
A.  $\frac{1}{4}$   
B. 1  
C. 2.5  
D. 4
84. Simplify:  $\log_7 2401 - \log_7 343$ .

- A. 0  
B. 1  
C. 2  
D. 7
85. If  $\log_4 x = 4$ , find  $x$ .  
A. 16  
B. 64  
C. 128  
D. 256
86. Evaluate:  $\log_{10} 0.001$ .  
A. -3  
B. -2  
C. 0.001  
D. 3
87. Simplify:  $2 \log_3 9 + \log_3 3$ .  
A. 3  
B. 4  
C. 5  
D. 9
88. If  $\log_{10} x = -1$ , find  $x$ .  
A. 0.01  
B. 0.1  
C. 1  
D. 10
89. Evaluate:  $\log_2 \sqrt{8}$ .  
A.  $\frac{3}{2}$   
B. 2  
C. 3  
D. 4
90. Simplify:  $\log_9 729 + \log_9 9$ .  
A. 3  
B. 4  
C. 5  
D. 9
91. If  $\log_7 x = 3$ , find  $x$ .  
A. 21  
B. 49  
C. 147  
D. 343
92. Evaluate:  $\log_{10} 0.0001$ .  
A. -4  
B. -3  
C. 0.0001  
D. 4
93. Simplify:  $3 \log_4 4 + \log_4 64$ .  
A. 4  
B. 5  
C. 6  
D. 8
94. If  $\log_{10} x = -2$ , find  $x$ .  
A. 0.001  
B. 0.01  
C. 0.1  
D. 1
95. Evaluate:  $\log_3 \sqrt{27}$ .  
A.  $\frac{3}{2}$   
B. 2  
C. 3  
D. 9
96. Simplify:  $\log_{10} 10000 - \log_{10} 100$ .  
A. 1  
B. 2  
C. 3  
D. 100
97. If  $\log_2 x = 7$ , find  $x$ .  
A. 14  
B. 64  
C. 128  
D. 256
98. Evaluate:  $\log_{10} \sqrt{100}$ .  
A.  $\frac{1}{2}$   
B. 1  
C. 2  
D. 10

99. Simplify:  $\log_6 1296 - \log_6 216$ .

- A. 0
- B. 1
- C. 2
- D. 6

100. If  $\log_{10} 2 = 0.3010$  and  $\log_{10} 3 = 0.4771$ , evaluate  $\log_{10} 18$ .

- A. 1.2552
- B. 1.2551
- C. 1.7781
- D. 1.7782

## Chapter 3

# Geometry

### 3.1 Circle Geometry

#### 3.1.1 Questions

1. A chord of length 24 cm is drawn in a circle of radius 13 cm. Calculate the distance of the chord from the center.  
A. 5 cm  
B. 7 cm  
C. 9 cm  
D. 11 cm
2. Two chords  $AB$  and  $CD$  intersect at point  $E$  inside a circle. If  $AE = 4$  cm,  $EB = 6$  cm and  $CE = 3$  cm, find  $ED$ .  
A. 6 cm  
B. 8 cm  
C. 10 cm  
D. 12 cm
3. A tangent from an external point  $P$  to a circle with center  $O$  and radius 5 cm has length 12 cm. Find the distance  $OP$ .  
A. 7 cm  
B. 11 cm  
C. 13 cm  
D. 17 cm
4. In a circle, a chord subtends an angle of  $60^\circ$  at the center. If the radius is 10 cm, find the length of the chord.  
A. 5 cm  
B. 8 cm  
C. 10 cm  
D. 12 cm
5. An arc of a circle subtends an angle of  $120^\circ$  at the center. If the radius is 7 cm, what angle does it subtend at the circumference?  
A.  $30^\circ$   
B.  $45^\circ$   
C.  $60^\circ$   
D.  $90^\circ$
6. Two tangents from an external point to a circle are 8 cm each. If the angle between them is  $60^\circ$ , find the radius of the circle.  
A. 4 cm  
B.  $4\sqrt{3}$  cm  
C. 8 cm  
D.  $8\sqrt{3}$  cm
7. In a cyclic quadrilateral  $ABCD$ ,  $\angle A = 70^\circ$  and  $\angle C = 110^\circ$ . Find  $\angle B$ .  
A.  $70^\circ$   
B.  $90^\circ$   
C.  $110^\circ$   
D.  $180^\circ$
8. A chord of a circle is 16 cm long and is 6 cm from the center. Calculate the radius of the circle.  
A. 8 cm  
B. 10 cm  
C. 12 cm  
D. 14 cm

9. Two circles with radii 4 cm and 6 cm touch externally. Calculate the distance between their centers.  
A. 2 cm  
B. 5 cm  
C. 10 cm  
D. 12 cm
10. A chord of length 20 cm subtends an angle of  $90^\circ$  at the center of a circle. Find the radius.  
A. 10 cm  
B.  $10\sqrt{2}$  cm  
C. 15 cm  
D. 20 cm
11. In a circle with center  $O$ , a chord  $AB$  is 12 cm long. If the perpendicular from  $O$  to  $AB$  is 8 cm, find the radius.  
A. 9 cm  
B. 10 cm  
C. 11 cm  
D. 12 cm
12. Two tangents are drawn from point  $P$  to a circle with center  $O$ . If the angle between the tangents is  $80^\circ$ , find  $\angle POQ$  where  $Q$  is one point of tangency.  
A.  $40^\circ$   
B.  $50^\circ$   
C.  $80^\circ$   
D.  $100^\circ$
13. A cyclic quadrilateral has angles  $x$ ,  $2x$ ,  $3x$ , and  $4x$ . Find the largest angle.  
A.  $72^\circ$   
B.  $108^\circ$   
C.  $120^\circ$   
D.  $144^\circ$
14. In a circle, an inscribed angle is  $40^\circ$ . Find the central angle subtending the same arc.  
A.  $20^\circ$   
B.  $40^\circ$   
C.  $60^\circ$   
D.  $80^\circ$
15. Two chords  $PQ$  and  $RS$  of a circle intersect at  $T$  outside the circle. If  $PT = 6$  cm,  $TQ = 4$  cm and  $RT = 8$  cm, find  $TS$ .  
A. 2 cm  
B. 3 cm  
C. 4 cm  
D. 5 cm
16. A tangent to a circle makes an angle of  $30^\circ$  with a chord drawn from the point of contact. Find the angle subtended by the chord at the center.  
A.  $60^\circ$   
B.  $90^\circ$   
C.  $120^\circ$   
D.  $150^\circ$
17. In a circle of radius 15 cm, a chord is 18 cm long. Calculate its distance from the center.  
A. 6 cm  
B. 9 cm  
C. 12 cm  
D. 15 cm
18. Two circles with radii 8 cm and 3 cm touch internally. Find the distance between their centers.  
A. 3 cm  
B. 5 cm  
C. 8 cm  
D. 11 cm
19. A chord of a circle subtends an angle of  $144^\circ$  at the center. What angle does it subtend at a point on the minor arc?  
A.  $36^\circ$   
B.  $72^\circ$   
C.  $108^\circ$   
D.  $144^\circ$
20. In a cyclic quadrilateral  $PQRS$ ,  $\angle P = 85^\circ$ . Find  $\angle R$ .  
A.  $85^\circ$   
B.  $95^\circ$   
C.  $105^\circ$   
D.  $175^\circ$
21. A tangent and a chord meet at a point on a circle, making an angle of  $50^\circ$ . Find the angle in the alternate segment.  
A.  $25^\circ$   
B.  $40^\circ$   
C.  $50^\circ$

- D.  $100^\circ$
22. Two parallel chords in a circle have lengths 16 cm and 12 cm. If the radius is 10 cm, find the distance between the chords (both on the same side of center).
- A. 2 cm  
B. 4 cm  
C. 6 cm  
D. 8 cm
23. A circle passes through the vertices of a square with side 8 cm. Find the radius of the circle.
- A. 4 cm  
B.  $4\sqrt{2}$  cm  
C. 8 cm  
D.  $8\sqrt{2}$  cm
24. In a circle, a chord  $AB = 14$  cm and its perpendicular distance from center  $O$  is  $7\sqrt{3}$  cm. Find the radius.
- A. 12 cm  
B. 14 cm  
C. 16 cm  
D. 18 cm
25. Two secants are drawn from point  $P$  to a circle. If the external parts are 4 cm and 5 cm and one whole secant is 12 cm, find the other whole secant.
- A. 9 cm  
B. 9.6 cm  
C. 10 cm  
D. 11 cm
26. A cyclic trapezium has parallel sides of lengths 10 cm and 6 cm. If the radius is 5 cm, find the length of one of the non-parallel sides.
- A. 4 cm  
B. 5 cm  
C. 6 cm  
D. 8 cm
27. In a circle with radius  $r$ , two parallel chords are on opposite sides of the center. If their lengths are 16 cm and 12 cm and  $r = 10$  cm, find the distance between them.
- A. 10 cm  
B. 12 cm  
C. 14 cm  
D. 16 cm
28. A chord subtends an angle of  $120^\circ$  at the center of a circle with radius 6 cm. Find the area of the minor segment.
- A.  $(12\pi - 9\sqrt{3}) \text{ cm}^2$   
B.  $(9\pi - 9\sqrt{3}) \text{ cm}^2$   
C.  $(6\pi - 9\sqrt{3}) \text{ cm}^2$   
D.  $(12\pi - 18\sqrt{3}) \text{ cm}^2$
29. From an external point, two tangents are drawn to a circle of radius 5 cm. If each tangent is 12 cm long, find the distance between the points of tangency.
- A. 8.46 cm  
B. 9.23 cm  
C. 10 cm  
D. 12 cm
30. In a circle, an angle in a semicircle is:
- A.  $45^\circ$   
B.  $60^\circ$   
C.  $90^\circ$   
D.  $180^\circ$
31. A chord of length 8 cm is at distance 3 cm from center. Another chord is at distance 4 cm. Find its length.
- A. 4 cm  
B. 6 cm  
C.  $2\sqrt{9}$  cm  
D.  $2\sqrt{9}$  cm
32. Two circles of equal radii 5 cm each intersect such that each passes through the center of the other. Find the length of the common chord.
- A. 5 cm  
B.  $5\sqrt{2}$  cm  
C.  $5\sqrt{3}$  cm  
D. 10 cm
33. In a cyclic quadrilateral, two opposite angles are  $(3x + 10)^\circ$  and  $(2x + 20)^\circ$ . Find  $x$ .
- A.  $30^\circ$   
B.  $35^\circ$   
C.  $40^\circ$   
D.  $45^\circ$
34. A tangent to a circle of radius 7 cm from point  $P$  is 24 cm long. Find  $OP$ .
- A. 17 cm



- B. 20 cm  
C. 25 cm  
D. 31 cm
35. In a circle, a chord  $AB = 10$  cm subtends an angle of  $60^\circ$  at the center. Find the radius.
- A. 5 cm  
B. 8 cm  
C. 10 cm  
D. 12 cm
36. Two chords  $AB$  and  $CD$  of a circle intersect at right angles at point  $E$  inside the circle. If  $AE = 3$  cm,  $EB = 4$  cm and  $CE = 2$  cm, find  $ED$ .
- A. 5 cm  
B. 6 cm  
C. 7 cm  
D. 8 cm
37. A circle has diameter 26 cm. A chord parallel to the diameter is 24 cm long. Find its distance from the diameter.
- A. 3 cm  
B. 4 cm  
C. 5 cm  
D. 6 cm
38. In a cyclic quadrilateral  $ABCD$ ,  $\angle DAB = 65^\circ$  and  $\angle ABC = 75^\circ$ . Find  $\angle BCD$ .
- A.  $105^\circ$   
B.  $115^\circ$   
C.  $125^\circ$   
D.  $140^\circ$
39. The angle between a tangent and a chord drawn from the point of contact is  $35^\circ$ . Find the angle subtended by the chord at the center.
- A.  $35^\circ$   
B.  $55^\circ$   
C.  $70^\circ$   
D.  $110^\circ$
40. A chord of a circle is equal to its radius. Find the angle subtended by the chord at the center.
- A.  $30^\circ$   
B.  $45^\circ$   
C.  $60^\circ$   
D.  $90^\circ$
41. Two tangents from external point  $T$  touch a circle at  $A$  and  $B$ . If  $\angle ATB = 50^\circ$  and radius is 6 cm, find  $TA$ .
- A.  $6 \tan 25^\circ$  cm  
B.  $6/\tan 25^\circ$  cm  
C.  $6 \sin 25^\circ$  cm  
D.  $6/\sin 25^\circ$  cm
42. In a circle with center  $O$  and radius 10 cm, two chords  $AB$  and  $CD$  are each 12 cm long. Find the distance between them if they are on the same side.
- A. 0 cm  
B. 8 cm  
C. 12 cm  
D. 16 cm
43. A cyclic quadrilateral has three angles  $80^\circ$ ,  $95^\circ$ , and  $105^\circ$ . Find the fourth angle.
- A.  $70^\circ$   
B.  $75^\circ$   
C.  $80^\circ$   
D.  $85^\circ$
44. Two circles with radii 9 cm and 4 cm intersect. The distance between their centers is 10 cm. Find the length of the common chord.
- A. 6 cm  
B. 7.2 cm  
C. 8 cm  
D. 9.6 cm
45. A secant and a tangent are drawn from external point  $P$  to a circle. If the tangent is 8 cm and the external part of the secant is 4 cm, find the whole secant.
- A. 12 cm  
B. 16 cm  
C. 18 cm  
D. 20 cm
46. In a circle, a chord  $PQ$  is 16 cm long and subtends angle  $90^\circ$  at center  $O$ . Find the area of triangle  $POQ$ .
- A.  $32 \text{ cm}^2$   
B.  $48 \text{ cm}^2$   
C.  $64 \text{ cm}^2$   
D.  $72 \text{ cm}^2$

47. Two parallel chords of lengths 6 cm and 8 cm are on opposite sides of center in a circle of radius 5 cm. Find distance between them.
- A. 6 cm  
B. 7 cm  
C. 8 cm  
D. 9 cm
48. The angle in the alternate segment equals the angle between:
- A. Two chords  
B. Two radii  
C. A tangent and a chord  
D. Two tangents
49. In a circle of radius 13 cm, a chord  $AB = 24$  cm. Find the angle subtended by the chord at center.
- A.  $67.4^\circ$   
B.  $112.6^\circ$   
C.  $134.8^\circ$   
D.  $157.4^\circ$
50. A circle is inscribed in an equilateral triangle of side 12 cm. Find the radius of the circle.
- A.  $2\sqrt{3}$  cm  
B.  $3\sqrt{3}$  cm  
C.  $4\sqrt{3}$  cm  
D.  $6\sqrt{3}$  cm
51. Two chords intersect inside a circle at point  $M$ . If the segments of one chord are 5 cm and 7 cm, and one segment of other is 10 cm, find the other segment.
- A. 3.5 cm  
B. 4 cm  
C. 4.5 cm  
D. 5 cm
52. In a cyclic quadrilateral, if one angle is three times another and their sum is  $180^\circ$ , find the smaller angle.
- A.  $30^\circ$   
B.  $45^\circ$   
C.  $60^\circ$   
D.  $90^\circ$
53. A tangent of length 15 cm is drawn from point  $P$  to circle with radius 8 cm. Find the angle between the tangent and the line joining  $P$  to the center.
- A.  $28.1^\circ$   
B.  $32.0^\circ$   
C.  $58.0^\circ$   
D.  $62.0^\circ$
54. In a circle, a diameter  $AB = 20$  cm. A chord  $CD$  perpendicular to  $AB$  at point  $E$  where  $AE = 4$  cm. Find  $CD$ .
- A. 12 cm  
B. 14 cm  
C. 16 cm  
D. 18 cm
55. Two circles touch externally. The sum of their radii is 15 cm and distance between centers is 15 cm. If one radius is 9 cm, find the other.
- A. 4 cm  
B. 5 cm  
C. 6 cm  
D. 7 cm
56. A chord subtends angle  $\theta$  at center and angle  $\alpha$  at circumference. The relationship is:
- A.  $\theta = \alpha$   
B.  $\theta = 2\alpha$   
C.  $\alpha = 2\theta$   
D.  $\theta + \alpha = 180^\circ$
57. In a circle with radius  $r$ , a chord of length  $r\sqrt{3}$  is drawn. Find the angle it subtends at center.
- A.  $60^\circ$   
B.  $90^\circ$   
C.  $120^\circ$   
D.  $150^\circ$
58. Two tangents from point  $P$  make angle  $60^\circ$  with each other. If radius is 5 cm, find  $OP$ .
- A. 5 cm  
B. 10 cm  
C.  $5\sqrt{3}$  cm  
D.  $10\sqrt{3}$  cm
59. A cyclic quadrilateral has consecutive angles in ratio  $2 : 3 : 4 : x$ . Find  $x$ .
- A. 3  
B. 4  
C. 5

- D. 6
60. In circle with center  $O$ , chord  $AB = 8$  cm and  $\angle AOB = 90^\circ$ . Find radius.
- A. 4 cm  
B.  $4\sqrt{2}$  cm  
C. 6 cm  
D. 8 cm
61. Two circles of radii 7 cm and 5 cm touch internally. Their common tangent divides the line joining centers in ratio:
- A. 5 : 7  
B. 7 : 5  
C. 2 : 5  
D. 5 : 2
62. A chord is 12 cm from center of circle with radius 13 cm. Find its length.
- A. 5 cm  
B. 8 cm  
C. 10 cm  
D. 12 cm
63. In a cyclic trapezium  $ABCD$  with  $AB \parallel CD$ , if  $\angle A = 70^\circ$ , find  $\angle C$ .
- A.  $70^\circ$   
B.  $90^\circ$   
C.  $110^\circ$   
D.  $140^\circ$
64. From external point, secant and tangent are drawn. If tangent is 12 cm and internal part of secant is 9 cm, find external part.
- A. 6 cm  
B. 7 cm  
C. 8 cm  
D. 9 cm
65. A regular hexagon is inscribed in circle of radius 8 cm. Find side of hexagon.
- A. 4 cm  
B. 6 cm  
C. 8 cm  
D. 10 cm
66. Angle between tangent and radius at point of contact is:
- A.  $0^\circ$   
B.  $45^\circ$   
C.  $60^\circ$   
D.  $90^\circ$
67. Two chords  $AB = 10$  cm and  $CD = 24$  cm are in circle of radius 13 cm. Find sum of their distances from center.
- A. 10 cm  
B. 12 cm  
C. 17 cm  
D. 20 cm
68. In cyclic quadrilateral, diagonal divides it into two triangles. If angles of one triangle are  $40^\circ$ ,  $60^\circ$ ,  $80^\circ$ , find angle opposite to  $80^\circ$  in other triangle.
- A.  $40^\circ$   
B.  $60^\circ$   
C.  $80^\circ$   
D.  $100^\circ$
69. A circle passes through vertices of rectangle with sides 6 cm and 8 cm. Find diameter.
- A. 7 cm  
B. 10 cm  
C. 12 cm  
D. 14 cm
70. Chord  $AB$  of circle with center  $O$  and radius 5 cm has length 8 cm. Point  $M$  is midpoint of  $AB$ . Find  $OM$ .
- A. 2 cm  
B. 3 cm  
C. 4 cm  
D. 5 cm
71. Two tangents from external point are 6 cm and 8 cm long. This is:
- A. Possible  
B. Impossible  
C. Possible only if radii differ  
D. None of these
72. A chord subtends  $45^\circ$  at center. Angle at major arc is:
- A.  $22.5^\circ$   
B.  $45^\circ$   
C.  $67.5^\circ$

- D.  $90^\circ$
73. In circle, perpendicular from center to chord bisects:
- A. The chord
  - B. The arc
  - C. The angle at center
  - D. All of these
74. Tangents from external point to circle are:
- A. Unequal
  - B. Equal
  - C. Parallel
  - D. Perpendicular
75. A cyclic quadrilateral with all sides equal is a:
- A. Rectangle
  - B. Rhombus
  - C. Square
  - D. Trapezium
76. In circle of radius 10 cm, chord at 6 cm from center has length:
- A. 8 cm
  - B. 12 cm
  - C. 14 cm
  - D. 16 cm
77. Two circles touch externally. Line through point of contact passes through:
- A. One center only
  - B. Both centers
  - C. Neither center
  - D. Midpoint of line joining centers
78. Angle subtended by diameter at circumference is:
- A.  $45^\circ$
  - B.  $60^\circ$
  - C.  $90^\circ$
  - D.  $180^\circ$
79. Common chord of two intersecting circles is:
- A. Parallel to line joining centers
  - B. Perpendicular to line joining centers
  - C. Equal to sum of radii
  - D. Equal to difference of radii
80. In cyclic quadrilateral, product of diagonals equals:
- A. Sum of products of opposite sides
  - B. Difference of products of opposite sides
  - C. Product of adjacent sides
  - D. Twice the area
81. A chord of length  $2r$  in circle of radius  $r$  is:
- A. Impossible
  - B. The diameter
  - C. Any chord
  - D. The radius
82. Maximum number of common tangents to two circles touching externally is:
- A. 1
  - B. 2
  - C. 3
  - D. 4
83. In circle, equal chords are:
- A. Equidistant from center
  - B. At different distances from center
  - C. Parallel
  - D. Perpendicular
84. Angle in semicircle is always:
- A. Acute
  - B. Right
  - C. Obtuse
  - D. Reflex
85. Two chords  $AB$  and  $CD$  intersect at  $E$ .  $AE \times EB$  equals:
- A.  $CE + ED$
  - B.  $CE - ED$
  - C.  $CE \times ED$
  - D.  $CE/ED$
86. Radius of circle inscribed in right triangle with legs 3 cm and 4 cm is:
- A. 1 cm
  - B. 1.5 cm
  - C. 2 cm
  - D. 2.5 cm
87. Circle circumscribing square of side  $a$  has radius:

- A.  $a/2$   
 B.  $a/\sqrt{2}$   
 C.  $a\sqrt{2}/2$   
 D.  $a\sqrt{2}$
88. Tangent to circle is perpendicular to:  
 A. Chord  
 B. Diameter  
 C. Radius at point of contact  
 D. Another tangent
89. In circle of radius 13 cm, two parallel chords of lengths 10 cm and 24 cm are on same side. Distance between them is:  
 A. 7 cm  
 B. 10 cm  
 C. 12 cm  
 D. 17 cm
90. Angle between two tangents from external point is  $60^\circ$ . Angle between radii to points of tangency is:  
 A.  $60^\circ$   
 B.  $90^\circ$   
 C.  $120^\circ$   
 D.  $150^\circ$
91. A chord divides circle into two parts. Angle subtended by smaller arc at center is  $100^\circ$ . Angle at circumference on larger arc is:  
 A.  $50^\circ$   
 B.  $80^\circ$   
 C.  $100^\circ$   
 D.  $130^\circ$
92. Locus of centers of circles passing through two fixed points is:  
 A. Circle  
 B. Perpendicular bisector of line joining points  
 C. Line joining points  
 D. Parallel line
93. Circle inscribed in equilateral triangle of side  $a$  has radius:  
 A.  $a/2\sqrt{3}$   
 B.  $a/\sqrt{3}$   
 C.  $a\sqrt{3}/6$   
 D.  $a\sqrt{3}/3$
94. Two chords intersect inside circle. One is divided into segments 3 cm and 8 cm. Other is 12 cm. One segment of second chord is:  
 A. 2 cm  
 B. 4 cm  
 C. 6 cm  
 D. 8 cm
95. Cyclic quadrilateral with two adjacent right angles is a:  
 A. Square  
 B. Rectangle  
 C. Trapezium  
 D. Impossible
96. Maximum distance between two points on circle of radius  $r$  is:  
 A.  $r$   
 B.  $r\sqrt{2}$   
 C.  $2r$   
 D.  $\pi r$
97. In circle, angle between tangent and chord equals angle in:  
 A. Semicircle  
 B. Alternate segment  
 C. Same segment  
 D. Minor segment
98. Number of tangents from external point to circle:  
 A. 0  
 B. 1  
 C. 2  
 D. Infinite
99. Circle touching all sides of triangle is called:  
 A. Circumcircle  
 B. Incircle  
 C. Excircle  
 D. Concentric circle
100. The angle formed by a diameter at any point on the circumference is:  
 A.  $45^\circ$   
 B.  $90^\circ$   
 C.  $180^\circ$   
 D.  $360^\circ$

## 3.2 Mensuration

### 3.2.1 Questions

- Calculate the arc length of a sector with radius 14 cm and central angle  $45^\circ$ . (Take  $\pi = 22/7$ ).  
A. 9 cm  
B. 11 cm  
C. 13 cm  
D. 15 cm
- Find the area of a sector with radius 7 cm and angle  $60^\circ$  at the center. (Take  $\pi = 22/7$ ).  
A.  $25.67 \text{ cm}^2$   
B.  $28.33 \text{ cm}^2$   
C.  $30.25 \text{ cm}^2$   
D.  $32.50 \text{ cm}^2$
- The volume of a cylinder with radius 7 cm and height 10 cm is: (Take  $\pi = 22/7$ ).  
A.  $1540 \text{ cm}^3$   
B.  $1100 \text{ cm}^3$   
C.  $770 \text{ cm}^3$   
D.  $440 \text{ cm}^3$
- Calculate the curved surface area of a cone with radius 7 cm and slant height 10 cm. (Take  $\pi = 22/7$ ).  
A.  $110 \text{ cm}^2$   
B.  $154 \text{ cm}^2$   
C.  $220 \text{ cm}^2$   
D.  $280 \text{ cm}^2$
- Find the surface area of a sphere with radius 7 cm. (Take  $\pi = 22/7$ ).  
A.  $308 \text{ cm}^2$   
B.  $462 \text{ cm}^2$   
C.  $616 \text{ cm}^2$   
D.  $770 \text{ cm}^2$
- A sector has arc length 22 cm and radius 7 cm. Find the angle in radians.  
A.  $\pi/7$   
B.  $\pi/2$   
C.  $\pi$   
D.  $2\pi$
- Calculate the volume of a cone with base radius 6 cm and height 8 cm. (Take  $\pi = 22/7$ ).  
A.  $301.71 \text{ cm}^3$   
B.  $352.00 \text{ cm}^3$   
C.  $402.29 \text{ cm}^3$   
D.  $452.57 \text{ cm}^3$
- The total surface area of a cylinder with radius 7 cm and height 5 cm is: (Take  $\pi = 22/7$ ).  
A.  $308 \text{ cm}^2$   
B.  $440 \text{ cm}^2$   
C.  $528 \text{ cm}^2$   
D.  $616 \text{ cm}^2$
- Find the volume of a sphere with diameter 14 cm. (Take  $\pi = 22/7$ ).  
A.  $1437.33 \text{ cm}^3$   
B.  $1372.00 \text{ cm}^3$   
C.  $1230.67 \text{ cm}^3$   
D.  $1100.50 \text{ cm}^3$
- A sector has perimeter 32 cm and radius 10 cm. Find the arc length.  
A. 10 cm  
B. 12 cm  
C. 14 cm  
D. 16 cm
- Calculate the area of a sector with arc length 11 cm and radius 7 cm.  
A.  $35.5 \text{ cm}^2$   
B.  $38.5 \text{ cm}^2$   
C.  $41.5 \text{ cm}^2$   
D.  $44.5 \text{ cm}^2$
- The slant height of a cone with radius 5 cm and vertical height 12 cm is:  
A. 10 cm  
B. 11 cm  
C. 13 cm  
D. 15 cm
- Find the total surface area of a cone with base radius 7 cm and slant height 10 cm. (Take  $\pi = 22/7$ ).

- A.  $308 \text{ cm}^2$   
B.  $374 \text{ cm}^2$   
C.  $440 \text{ cm}^2$   
D.  $506 \text{ cm}^2$
14. A cylinder has volume  $1540 \text{ cm}^3$  and radius 7 cm. Find its height. (Take  $\pi = 22/7$ ).
- A. 8 cm  
B. 10 cm  
C. 12 cm  
D. 14 cm
15. Calculate the volume of a hemisphere with radius 7 cm. (Take  $\pi = 22/7$ ).
- A.  $616.00 \text{ cm}^3$   
B.  $718.67 \text{ cm}^3$   
C.  $821.33 \text{ cm}^3$   
D.  $924.00 \text{ cm}^3$
16. A sector has angle  $120^\circ$  and arc length 44 cm. Find the radius. (Take  $\pi = 22/7$ ).
- A. 18 cm  
B. 21 cm  
C. 24 cm  
D. 27 cm
17. The curved surface area of a cylinder is  $880 \text{ cm}^2$  and radius is 7 cm. Find height. (Take  $\pi = 22/7$ ).
- A. 15 cm  
B. 18 cm  
C. 20 cm  
D. 22 cm
18. Find the total surface area of a sphere with radius 3.5 cm. (Take  $\pi = 22/7$ ).
- A.  $110 \text{ cm}^2$   
B.  $132 \text{ cm}^2$   
C.  $154 \text{ cm}^2$   
D.  $176 \text{ cm}^2$
19. A cone has total surface area  $704 \text{ cm}^2$ , radius 7 cm. Find slant height. (Take  $\pi = 22/7$ ).
- A. 20 cm  
B. 25 cm  
C. 28 cm  
D. 32 cm
20. Calculate the arc length subtending angle  $\pi/3$  radians in circle of radius 21 cm. (Take  $\pi = 22/7$ ).
- A. 18 cm  
B. 20 cm  
C. 22 cm  
D. 24 cm
21. A cylinder has height equal to its diameter. If radius is 7 cm, find volume. (Take  $\pi = 22/7$ ).
- A.  $2156 \text{ cm}^3$   
B.  $2310 \text{ cm}^3$   
C.  $2464 \text{ cm}^3$   
D.  $2618 \text{ cm}^3$
22. Find area of segment of circle with radius 7 cm and central angle  $90^\circ$ . (Take  $\pi = 22/7$ ).
- A.  $12.5 \text{ cm}^2$   
B.  $13.5 \text{ cm}^2$   
C.  $14.5 \text{ cm}^2$   
D.  $15.5 \text{ cm}^2$
23. The volume of a cone is  $1232 \text{ cm}^3$  and height is 24 cm. Find radius. (Take  $\pi = 22/7$ ).
- A. 5 cm  
B. 6 cm  
C. 7 cm  
D. 8 cm
24. A sector of angle  $60^\circ$  has area  $462 \text{ cm}^2$ . Find radius. (Take  $\pi = 22/7$ ).
- A. 18 cm  
B. 20 cm  
C. 21 cm  
D. 24 cm
25. Calculate curved surface area of hemisphere with radius 14 cm. (Take  $\pi = 22/7$ ).
- A.  $1100 \text{ cm}^2$   
B.  $1232 \text{ cm}^2$   
C.  $1364 \text{ cm}^2$   
D.  $1496 \text{ cm}^2$
26. A cylinder and cone have equal base and height. If cylinder volume is  $300 \text{ cm}^3$ , find cone volume.
- A.  $75 \text{ cm}^3$   
B.  $100 \text{ cm}^3$   
C.  $150 \text{ cm}^3$

- D.  $200 \text{ cm}^3$
27. Find the volume of cone with base circumference 44 cm and height 12 cm. (Take  $\pi = 22/7$ ).
- A.  $588 \text{ cm}^3$   
 B.  $616 \text{ cm}^3$   
 C.  $644 \text{ cm}^3$   
 D.  $672 \text{ cm}^3$
28. A sector has radius 10 cm and area  $50 \text{ cm}^2$ . Find angle in radians.
- A. 0.5  
 B. 1.0  
 C. 1.5  
 D. 2.0
29. Calculate total surface area of hemisphere with diameter 14 cm. (Take  $\pi = 22/7$ ).
- A.  $396 \text{ cm}^2$   
 B.  $462 \text{ cm}^2$   
 C.  $528 \text{ cm}^2$   
 D.  $594 \text{ cm}^2$
30. The ratio of volumes of sphere and cylinder with same radius and height equal to diameter is:
- A. 1 : 2  
 B. 2 : 3  
 C. 3 : 4  
 D. 4 : 3
31. A cone has volume  $308 \text{ cm}^3$  and base area  $154 \text{ cm}^2$ . Find height. (Take  $\pi = 22/7$ ).
- A. 4 cm  
 B. 5 cm  
 C. 6 cm  
 D. 7 cm
32. Find arc length of sector with area  $77 \text{ cm}^2$  and radius 7 cm. (Take  $\pi = 22/7$ ).
- A. 20 cm  
 B. 22 cm  
 C. 24 cm  
 D. 26 cm
33. A cylinder has total surface area  $1936 \text{ cm}^2$  and radius 14 cm. Find height. (Take  $\pi = 22/7$ ).
- A. 6 cm  
 B. 8 cm  
 C. 10 cm  
 D. 12 cm
34. Calculate volume of sphere inscribed in cube of side 6 cm. (Take  $\pi = 22/7$ ).
- A.  $113.14 \text{ cm}^3$   
 B.  $123.43 \text{ cm}^3$   
 C.  $133.71 \text{ cm}^3$   
 D.  $144.00 \text{ cm}^3$
35. A cone and sphere have equal radius  $r$ . If cone height is  $4r$ , ratio of their volumes is:
- A. 1 : 1  
 B. 1 : 2  
 C. 2 : 1  
 D. 3 : 4
36. Find the sector angle if arc length equals radius of 7 cm.
- A. 0.5 radians  
 B. 1 radian  
 C. 1.5 radians  
 D. 2 radians
37. A cylinder has height 10 cm and total surface area  $880 \text{ cm}^2$ . Find radius. (Take  $\pi = 22/7$ ).
- A. 6 cm  
 B. 7 cm  
 C. 8 cm  
 D. 9 cm
38. Calculate volume of cone with slant height 25 cm and base diameter 14 cm. (Take  $\pi = 22/7$ ).
- A.  $1232 \text{ cm}^3$   
 B.  $1320 \text{ cm}^3$   
 C.  $1408 \text{ cm}^3$   
 D.  $1496 \text{ cm}^3$
39. A sector has perimeter 60 cm and angle 2 radians. Find radius.
- A. 12 cm  
 B. 14 cm  
 C. 15 cm  
 D. 16 cm
40. The surface area of sphere is  $2464 \text{ cm}^2$ . Find diameter. (Take  $\pi = 22/7$ ).



- A. 24 cm  
B. 26 cm  
C. 28 cm  
D. 30 cm
41. A cone has curved surface area  $550 \text{ cm}^2$  and slant height 25 cm. Find radius. (Take  $\pi = 22/7$ ).  
A. 5 cm  
B. 6 cm  
C. 7 cm  
D. 8 cm
42. Calculate area of major sector if minor sector has area  $50 \text{ cm}^2$  and circle radius is 10 cm. (Take  $\pi = 22/7$ ).  
A.  $264.29 \text{ cm}^2$   
B.  $274.29 \text{ cm}^2$   
C.  $284.29 \text{ cm}^2$   
D.  $294.29 \text{ cm}^2$
43. A cylinder and sphere have equal surface areas. If sphere radius is  $r$ , find cylinder radius (height =  $2r$ ).  
A.  $r/2$   
B.  $2r/3$   
C.  $r$   
D.  $2r$
44. Find the volume of largest cone that can be carved from cube of side 14 cm. (Take  $\pi = 22/7$ ).  
A.  $718.67 \text{ cm}^3$   
B.  $796.44 \text{ cm}^3$   
C.  $874.22 \text{ cm}^3$   
D.  $952.00 \text{ cm}^3$
45. A sector with angle  $\theta$  radians and radius  $r$  has perimeter  $P$ . Express  $\theta$  in terms of  $P$  and  $r$ .  
A.  $(P - 2r)/r$   
B.  $(P + 2r)/r$   
C.  $(P - r)/2r$   
D.  $(P + r)/2r$
46. Calculate the ratio of curved surface areas of cone and hemisphere with equal base radius.  
A.  $l : r$   
B.  $l : 2r$   
C.  $2l : r$   
D.  $l^2 : 2r^2$
47. A cylinder has diameter 14 cm and height 20 cm. Find cost of painting at Rs. 2 per  $\text{cm}^2$ . (Take  $\pi = 22/7$ ).  
A. Rs. 2156  
B. Rs. 2464  
C. Rs. 2772  
D. Rs. 3080
48. Find volume of sphere whose surface area is  $5544 \text{ cm}^2$ . (Take  $\pi = 22/7$ ).  
A.  $38808 \text{ cm}^3$   
B.  $40824 \text{ cm}^3$   
C.  $42840 \text{ cm}^3$   
D.  $44856 \text{ cm}^3$
49. A sector has area  $A$  and arc length  $l$ . Express radius in terms of  $A$  and  $l$ .  
A.  $2A/l$   
B.  $A/2l$   
C.  $l/2A$   
D.  $2l/A$
50. Two cones have equal base. Heights are in ratio 3 : 4. Ratio of volumes is:  
A. 3 : 4  
B. 9 : 16  
C. 27 : 64  
D. 4 : 3
51. Calculate perimeter of sector with radius 21 cm and angle  $60^\circ$ . (Take  $\pi = 22/7$ ).  
A. 56 cm  
B. 60 cm  
C. 64 cm  
D. 68 cm
52. A cone has volume  $V$  and base area  $A$ . Find height.  
A.  $3V/A$   
B.  $V/3A$   
C.  $A/3V$   
D.  $V/A$
53. The volume of cylinder is  $3080 \text{ cm}^3$  and curved surface area is  $1540 \text{ cm}^2$ . Find radius. (Take  $\pi = 22/7$ ).  
A. 5 cm  
B. 6 cm  
C. 7 cm

- D. 8 cm
54. Find angle of sector if its area is  $1/8$  of circle area.
- A.  $30^\circ$   
B.  $36^\circ$   
C.  $45^\circ$   
D.  $60^\circ$
55. A sphere and cube have equal surface areas. If cube side is  $a$ , find sphere radius.
- A.  $a/\sqrt{\pi}$   
B.  $a\sqrt{3/2\pi}$   
C.  $a\sqrt{6/4\pi}$   
D.  $a\sqrt{3/\pi}$
56. Calculate total surface area of solid consisting of hemisphere on cylinder. Both have radius 7 cm and cylinder height 10 cm. (Take  $\pi = 22/7$ ).
- A.  $902 \text{ cm}^2$   
B.  $968 \text{ cm}^2$   
C.  $1034 \text{ cm}^2$   
D.  $1100 \text{ cm}^2$
57. A cone is cut parallel to base at half height. Ratio of volumes of top cone to original cone is:
- A. 1 : 2  
B. 1 : 4  
C. 1 : 8  
D. 1 : 16
58. Find arc length subtending angle  $5\pi/6$  in circle of radius 12 cm. (Take  $\pi = 22/7$ ).
- A. 29.14 cm  
B. 31.43 cm  
C. 33.71 cm  
D. 36.00 cm
59. A cylinder has volume  $V$  and height  $h$ . Find radius.
- A.  $\sqrt{V/\pi h}$   
B.  $\sqrt{V\pi h}$   
C.  $\sqrt{Vh/\pi}$   
D.  $\sqrt{\pi V/h}$
60. Calculate volume of cone formed by rolling sector of angle  $120^\circ$  and radius 18 cm. (Take  $\pi = 22/7$ ).
- A.  $263.03 \text{ cm}^3$   
B.  $293.03 \text{ cm}^3$   
C.  $323.03 \text{ cm}^3$   
D.  $353.03 \text{ cm}^3$
61. Two spheres have radii in ratio 2 : 3. Ratio of their surface areas is:
- A. 2 : 3  
B. 4 : 9  
C. 8 : 27  
D. 16 : 81
62. A sector has radius 14 cm and perimeter 50 cm. Find its area. (Take  $\pi = 22/7$ ).
- A.  $140 \text{ cm}^2$   
B.  $154 \text{ cm}^2$   
C.  $168 \text{ cm}^2$   
D.  $182 \text{ cm}^2$
63. Calculate slant height of cone whose volume is  $308 \text{ cm}^3$ , base radius 7 cm. (Take  $\pi = 22/7$ ).
- A. 10 cm  
B. 11 cm  
C. 12 cm  
D. 13 cm
64. A hemisphere and cone have equal base and height. Ratio of their volumes is:
- A. 1 : 1  
B. 2 : 1  
C. 3 : 2  
D. 4 : 3
65. Find the volume of largest sphere that can fit in cube of edge 10 cm. (Take  $\pi = 22/7$ ).
- A.  $523.81 \text{ cm}^3$   
B.  $552.38 \text{ cm}^3$   
C.  $580.95 \text{ cm}^3$   
D.  $609.52 \text{ cm}^3$
66. A sector area is  $A$ , radius is  $r$ , and angle is  $\theta$  radians. Which is correct?
- A.  $A = r^2\theta/2$   
B.  $A = r\theta/2$   
C.  $A = 2r^2\theta$   
D.  $A = r^2\theta$
67. Calculate cost of painting cylindrical pillar of diameter 0.7 m and height 4 m at Rs. 15 per  $\text{m}^2$ . (Take  $\pi = 22/7$ ).

- A. Rs. 126  
B. Rs. 132  
C. Rs. 138  
D. Rs. 144
68. Two cones have equal volume and base. Heights are in ratio 4 : 9. This is:  
A. Possible  
B. Impossible  
C. Possible only if radii differ  
D. Insufficient information
69. Find radius of sphere whose volume equals sum of volumes of two spheres of radii 3 cm and 4 cm.  
A. 5 cm  
B. 6 cm  
C. 7 cm  
D.  $\sqrt{91}$  cm
70. A sector of radius  $r$  and angle  $\theta$  is bent to form cone. The radius of cone base is:  
A.  $r\theta/\pi$   
B.  $r\theta/2\pi$   
C.  $2r\theta/\pi$   
D.  $r/\theta$
71. Calculate total surface area of cone with base diameter 10 cm and height 12 cm. (Take  $\pi = 22/7$ ).  
A.  $282.86 \text{ cm}^2$   
B.  $292.86 \text{ cm}^2$   
C.  $302.86 \text{ cm}^2$   
D.  $312.86 \text{ cm}^2$
72. A cylinder has volume  $5544 \text{ cm}^3$  and total surface area  $1848 \text{ cm}^2$ . Find height. (Take  $\pi = 22/7$ ).  
A. 16 cm  
B. 18 cm  
C. 20 cm  
D. 22 cm
73. Two cylinders have equal height. Radii are in ratio 2 : 3. Ratio of volumes is:  
A. 2 : 3  
B. 4 : 9  
C. 8 : 27  
D. 6 : 9
74. Find perimeter of segment with radius 14 cm and central angle  $90^\circ$ . (Take  $\pi = 22/7$ ).  
A. 41.81 cm  
B. 43.81 cm  
C. 45.81 cm  
D. 47.81 cm
75. A sphere is melted to form cylinder of same radius. If cylinder height is  $h$  and sphere radius is  $r$ , then:  
A.  $h = 4r/3$   
B.  $h = 3r/4$   
C.  $h = 2r/3$   
D.  $h = r$
76. Calculate volume of cone whose curved surface area is  $4070 \text{ cm}^2$  and slant height 37 cm. (Take  $\pi = 22/7$ ).  
A.  $12320 \text{ cm}^3$   
B.  $13440 \text{ cm}^3$   
C.  $14560 \text{ cm}^3$   
D.  $15680 \text{ cm}^3$
77. Two spheres have volumes in ratio 8 : 27. Ratio of their radii is:  
A. 2 : 3  
B. 4 : 9  
C. 8 : 27  
D. 16 : 81
78. A sector of angle  $216^\circ$  has radius 25 cm. Find perimeter. (Take  $\pi = 22/7$ ).  
A. 141.43 cm  
B. 143.43 cm  
C. 145.43 cm  
D. 147.43 cm
79. Find height of cone whose volume and curved surface area are numerically equal. If radius is 7 cm: (Take  $\pi = 22/7$ ).  
A. 21 cm  
B. 24 cm  
C. 27 cm  
D. 30 cm
80. A cylinder, cone, and hemisphere have equal base and height (diameter for hemisphere). Ratio of volumes is:  
A. 1 : 2 : 3  
B. 2 : 3 : 4

- C. 3 : 1 : 2  
D. 6 : 2 : 4
81. Calculate area of largest circle that can be inscribed in sector of radius 12 cm and angle  $60^\circ$ . (Take  $\pi = 22/7$ ).  
A.  $28.27 \text{ cm}^2$   
B.  $30.86 \text{ cm}^2$   
C.  $33.45 \text{ cm}^2$   
D.  $36.04 \text{ cm}^2$
82. A sphere of radius 6 cm is dropped into cylindrical vessel of radius 8 cm containing water. Find rise in water level.  
A. 3.5 cm  
B. 4.0 cm  
C. 4.5 cm  
D. 5.0 cm
83. Find volume of hollow cylinder with external radius 8 cm, internal radius 6 cm, and height 7 cm. (Take  $\pi = 22/7$ ).  
A.  $528 \text{ cm}^3$   
B.  $568 \text{ cm}^3$   
C.  $608 \text{ cm}^3$   
D.  $616 \text{ cm}^3$
84. A cone and hemisphere have equal base radii. If volumes are equal, ratio of cone height to radius is:  
A. 1 : 1  
B. 2 : 1  
C. 1 : 2  
D. 3 : 2
85. Calculate the area enclosed between two concentric circles of radii 14 cm and 21 cm. (Take  $\pi = 22/7$ ).  
A.  $770 \text{ cm}^2$   
B.  $825 \text{ cm}^2$   
C.  $880 \text{ cm}^2$   
D.  $935 \text{ cm}^2$
86. A sector is rolled into cone. If sector has angle  $120^\circ$  and radius 9 cm, find curved surface area of cone. (Take  $\pi = 22/7$ ).  
A.  $84.86 \text{ cm}^2$   
B.  $88.29 \text{ cm}^2$   
C.  $91.71 \text{ cm}^2$   
D.  $95.14 \text{ cm}^2$
87. Two cones have equal slant height. Base radii are in ratio 3 : 5. Ratio of curved surface areas is:  
A. 3 : 5  
B. 9 : 25  
C. 27 : 125  
D. 6 : 10
88. Find volume of sphere circumscribing cylinder with radius 3 cm and height 8 cm. (Take  $\pi = 22/7$ ).  
A.  $523.81 \text{ cm}^3$   
B.  $552.38 \text{ cm}^3$   
C.  $580.95 \text{ cm}^3$   
D.  $609.52 \text{ cm}^3$
89. A sector has area  $154 \text{ cm}^2$  and perimeter 44 cm. Find radius. (Take  $\pi = 22/7$ ).  
A. 5 cm  
B. 6 cm  
C. 7 cm  
D. 8 cm
90. Calculate total surface area of solid hemisphere placed on cylinder. Both have radius 7 cm, cylinder height 13 cm. (Take  $\pi = 22/7$ ).  
A.  $1012 \text{ cm}^2$   
B.  $1078 \text{ cm}^2$   
C.  $1144 \text{ cm}^2$   
D.  $1210 \text{ cm}^2$
91. A cone's slant height is twice its base radius. If volume is  $1232 \text{ cm}^3$ , find slant height. (Take  $\pi = 22/7$ ).  
A. 24 cm  
B. 26 cm  
C. 28 cm  
D. 30 cm
92. Calculate the volume of a square-based pyramid with base side 10 cm and height 12 cm.  
A.  $400 \text{ cm}^3$   
B.  $600 \text{ cm}^3$   
C.  $800 \text{ cm}^3$   
D.  $1200 \text{ cm}^3$
93. Find the area of a trapezoid with parallel sides 10 cm and 15 cm, and height 8 cm.  
A.  $80 \text{ cm}^2$   
B.  $100 \text{ cm}^2$

- C.  $120 \text{ cm}^2$   
D.  $200 \text{ cm}^2$
94. Calculate the total surface area of a cube with side length 5 cm.  
A.  $125 \text{ cm}^2$   
B.  $150 \text{ cm}^2$   
C.  $100 \text{ cm}^2$   
D.  $75 \text{ cm}^2$
95. A rectangular tank measures 4 m by 3 m by 2 m. Find its volume.  
A.  $12 \text{ m}^3$   
B.  $24 \text{ m}^3$   
C.  $48 \text{ m}^3$   
D.  $9 \text{ m}^3$
96. Find the curved surface area of a cylinder with radius 3.5 cm and height 10 cm. (Take  $\pi = 22/7$ ).  
A.  $110 \text{ cm}^2$   
B.  $220 \text{ cm}^2$   
C.  $330 \text{ cm}^2$   
D.  $440 \text{ cm}^2$
97. Calculate the surface area of a sphere with diameter 14 cm. (Take  $\pi = 22/7$ ).  
A.  $154 \text{ cm}^2$   
B.  $308 \text{ cm}^2$   
C.  $616 \text{ cm}^2$   
D.  $1232 \text{ cm}^2$
98. Find the area of a circle with radius 10 cm. (Use  $\pi = 3.14$ ).  
A.  $31.4 \text{ cm}^2$   
B.  $62.8 \text{ cm}^2$   
C.  $314 \text{ cm}^2$   
D.  $100 \text{ cm}^2$
99. A cone has base radius 5 cm and vertical height 12 cm. Find its slant height.  
A. 11 cm  
B. 13 cm  
C. 15 cm  
D. 17 cm
100. Calculate the volume of a sphere with radius 3 cm. (Take  $\pi = 3.142$ ).  
A.  $113.11 \text{ cm}^3$   
B.  $37.70 \text{ cm}^3$   
C.  $50.27 \text{ cm}^3$   
D.  $150.82 \text{ cm}^3$

### 3.3 Loci

#### 3.3.1 Questions

- The locus of a point  $P$  such that it is always 5 cm from a fixed point  $O$  is a:
  - Straight line
  - Circle of radius 5 cm
  - Pair of parallel lines
  - Perpendicular bisector
- Points  $A$  and  $B$  are 8 cm apart. The locus of points equidistant from  $A$  and  $B$  is:
  - A circle passing through  $A$  and  $B$
  - The perpendicular bisector of  $AB$
  - A line parallel to  $AB$
  - An angle bisector
- The locus of points at a constant distance of 3 cm from a straight line  $l$  consists of:
  - Two parallel lines, each 3 cm from  $l$
  - A circle of radius 3 cm
  - A single line perpendicular to  $l$
  - Four lines forming a square
- Two lines  $AB$  and  $CD$  intersect at point  $O$ . The locus of points equidistant from both lines is:
  - A circle centered at  $O$
  - The perpendicular bisector of  $AB$
  - The pair of angle bisectors of the angles formed at  $O$
  - A line parallel to  $AB$
- A point  $P$  moves such that its distance from a fixed point  $Q$  is always 7 cm. What is the locus of  $P$ ?
  - A sphere of radius 7 cm
  - A circle of radius 7 cm centered at  $Q$
  - A straight line through  $Q$
  - Two parallel lines 7 cm apart
- Points  $X$  and  $Y$  are 10 cm apart. How many points are exactly 6 cm from  $X$  and equidistant from  $X$  and  $Y$ ?
  - 0

- B. 1  
C. 2  
D. 4
7. The locus of the center of a circle that rolls without slipping along a straight line is:  
A. A circle  
B. A straight line parallel to the given line  
C. A curve called a cycloid  
D. A perpendicular line
8. A point  $M$  is equidistant from two fixed points  $P$  and  $Q$  which are 12 cm apart. If  $M$  is also 8 cm from  $P$ , what is the distance from  $M$  to  $Q$ ?  
A. 4 cm  
B. 8 cm  
C. 12 cm  
D. 20 cm
9. The locus of points in a plane that are 4 cm from a fixed point  $O$  and also 4 cm from another fixed point  $P$  where  $OP = 6$  cm consists of:  
A. 0 points  
B. 1 point  
C. 2 points  
D. Infinitely many points
10. A ladder of length 5 m leans against a wall with its foot on the ground. As the ladder slides down, the locus of its midpoint is:  
A. A straight line  
B. A circle  
C. A quarter circle  
D. A parabola
11. Two points  $A$  and  $B$  are 14 cm apart. The locus of point  $P$  such that  $\angle APB = 90^\circ$  is:  
A. A straight line  
B. A circle with  $AB$  as diameter  
C. The perpendicular bisector of  $AB$   
D. Two circles
12. The locus of points at a distance of 5 cm from a circle of radius 3 cm centered at  $O$  consists of:  
A. A single circle of radius 8 cm  
B. Two concentric circles of radii 2 cm and 8 cm  
C. A circle of radius 5 cm  
D. An ellipse
13. A point  $P$  moves such that it is always equidistant from two parallel lines  $l_1$  and  $l_2$  that are 10 cm apart. The locus of  $P$  is:  
A. A line parallel to both  $l_1$  and  $l_2$ , midway between them  
B. A circle  
C. The perpendicular bisector of the distance between  $l_1$  and  $l_2$   
D. Two lines perpendicular to  $l_1$  and  $l_2$
14. Points  $R$  and  $S$  are 6 cm apart. How many points are 4 cm from  $R$  and 5 cm from  $S$ ?  
A. 0  
B. 1  
C. 2  
D. 3
15. The locus of the vertex of a right angle that moves such that its arms always pass through two fixed points  $A$  and  $B$  is:  
A. A straight line  
B. A circle with  $AB$  as diameter  
C. The perpendicular bisector of  $AB$   
D. An ellipse
16. A point  $Q$  is 8 cm from a fixed point  $O$ . How many points are 5 cm from  $O$  and equidistant from  $Q$  and  $O$ ?  
A. 0  
B. 1  
C. 2  
D. 4
17. The locus of points that are 3 cm from a line segment  $AB$  of length 8 cm forms:  
A. Two parallel line segments  
B. A rectangle with semicircular ends (a stadium shape)  
C. A circle  
D. An ellipse
18. Two intersecting lines form four angles at their intersection point  $O$ . If a point  $P$  is equidistant from both lines, then  $P$  lies on:  
A. A circle centered at  $O$   
B. One of the two angle bisectors  
C. A line perpendicular to one of the given lines  
D. The perpendicular bisector of  $O$
19. Points  $M$  and  $N$  are 20 cm apart. The number of points that are 12 cm from  $M$  and also 12 cm from  $N$  is:  
A. 0  
B. 1  
C. 2  
D. 4
20. A point moves such that the sum of its distances from two fixed points  $F_1$  and  $F_2$  is constant. The locus is:  
A. A circle  
B. An ellipse with foci at  $F_1$  and  $F_2$   
C. A hyperbola  
D. The perpendicular bisector of  $F_1F_2$
21. The locus of centers of all circles passing through two given points  $A$  and  $B$  is:  
A. A circle with center at the midpoint of  $AB$   
B. The perpendicular bisector of  $AB$

- C. A line parallel to  $AB$   
D. A circle with  $AB$  as diameter
22. A point  $P$  is equidistant from two points  $A$  and  $B$  where  $AB = 16$  cm. If  $PA = 10$  cm, then  $PB$  equals:  
A. 6 cm  
B. 10 cm  
C. 16 cm  
D. 26 cm
23. The locus of points at a perpendicular distance of 6 cm from a straight line is:  
A. A single line parallel to the given line  
B. Two lines parallel to the given line, one on each side  
C. A circle of radius 6 cm  
D. A perpendicular line
24. Points  $C$  and  $D$  are 9 cm apart. How many points are 5 cm from  $C$  and 6 cm from  $D$ ?  
A. 0  
B. 1  
C. 2  
D. 3
25. A point  $P$  moves such that it is always twice as far from point  $A$  as it is from point  $B$ , where  $AB = 12$  cm. The locus of  $P$  is:  
A. A straight line  
B. A circle  
C. An ellipse  
D. A hyperbola
26. The locus of points equidistant from three non-collinear points  $A$ ,  $B$ , and  $C$  is:  
A. The circumcenter of triangle  $ABC$   
B. The centroid of triangle  $ABC$   
C. The incenter of triangle  $ABC$   
D. The orthocenter of triangle  $ABC$
27. A circle of radius 4 cm is centered at point  $O$ . How many points are 7 cm from  $O$  and also 3 cm from the circle?  
A. 0  
B. 1  
C. 2  
D. 4
28. Two points  $E$  and  $F$  are 5 cm apart. The locus of points  $P$  such that  $PE = 2 \cdot PF$  forms:  
A. A straight line  
B. A circle (Circle of Apollonius)  
C. The perpendicular bisector of  $EF$   
D. Two parallel lines
29. The locus of the midpoint of all chords of a circle that are parallel to a given chord is:  
A. A diameter perpendicular to the given chord  
B. A chord parallel to the given chord  
C. A circle concentric with the given circle  
D. The center of the circle
30. A point  $P$  is 10 cm from a line  $l$  and also 10 cm from a point  $Q$  that is 8 cm from line  $l$ . How many such points  $P$  are possible?  
A. 1  
B. 2  
C. 3  
D. 4
31. The locus of points that are 4 cm from a given point and also 4 cm from a given line (not passing through the point) can have:  
A. At most 1 point  
B. At most 2 points  
C. At most 3 points  
D. At most 4 points
32. Points  $G$  and  $H$  are 15 cm apart. The number of points that are 10 cm from  $G$  and equidistant from  $G$  and  $H$  is:  
A. 0  
B. 1  
C. 2  
D. 3
33. A point moves such that the difference of its distances from two fixed points is constant. The locus is:  
A. A circle  
B. An ellipse  
C. A hyperbola  
D. A parabola
34. The locus of points in a plane at a distance of 5 cm from a circle of radius 3 cm and lying outside the circle is:  
A. A circle of radius 2 cm  
B. A circle of radius 8 cm  
C. An annulus between radii 3 cm and 8 cm  
D. Two circles of radii 2 cm and 8 cm
35. Two perpendicular lines intersect at point  $O$ . The locus of points equidistant from these two lines forms:  
A. A circle centered at  $O$   
B. Two perpendicular lines bisecting the angles at  $O$   
C. Four lines  
D. A square
36. A point  $P$  is equidistant from the sides of an angle. The locus of  $P$  is:  
A. The angle bisector  
B. A circle  
C. A parallel line  
D. The perpendicular bisector

37. Points  $J$  and  $K$  are 18 cm apart. How many points are 10 cm from  $J$  and 10 cm from  $K$ ?
- 0
  - 1
  - 2
  - 4
38. The locus of the center of a circle of radius  $r$  that rolls on the outside of a fixed circle of radius  $R$  is:
- A circle of radius  $R$
  - A circle of radius  $R + r$
  - A circle of radius  $R - r$
  - A straight line
39. A point is 12 cm from point  $A$  and 5 cm from point  $B$  where  $AB = 13$  cm. How many such points exist?
- 0
  - 1
  - 2
  - Infinitely many
40. The locus of points from which tangents of equal length can be drawn to a circle is:
- A line perpendicular to the radius
  - Any point outside the circle
  - A concentric circle
  - The center of the circle
41. A point  $P$  moves such that its distance from a fixed line  $l$  is always equal to its distance from a fixed point  $F$  not on  $l$ . The locus of  $P$  is:
- A circle
  - An ellipse
  - A parabola
  - A hyperbola
42. Points  $L$  and  $M$  are 7 cm apart. How many points are 4 cm from  $L$  and also 4 cm from  $M$ ?
- 0
  - 1
  - 2
  - 3
43. The locus of points at a distance of 2 cm from a square of side 6 cm forms:
- A larger square
  - A square with rounded corners
  - A circle
  - An octagon
44. A point  $P$  is such that  $PA^2 + PB^2 = k$  where  $A$  and  $B$  are fixed points and  $k$  is constant. The locus of  $P$  is:
- A straight line
  - A circle
  - An ellipse
  - A parabola
45. Two parallel lines  $m$  and  $n$  are 12 cm apart. The locus of points that are 5 cm from  $m$  and 7 cm from  $n$  consists of:
- 0 points
  - 1 line
  - 2 lines
  - 4 lines
46. A point moves such that it is always 3 cm closer to point  $A$  than to point  $B$  where  $AB = 10$  cm. The locus is:
- A circle
  - The perpendicular bisector of  $AB$
  - A line parallel to  $AB$
  - A hyperbola
47. The locus of the center of a circle that touches two parallel lines is:
- A line perpendicular to both given lines
  - A line parallel to both given lines, midway between them
  - A circle
  - Two parallel lines
48. Points  $N$  and  $O$  are 20 cm apart. How many points are 15 cm from  $N$  and 15 cm from  $O$ ?
- 0
  - 1
  - 2
  - 4
49. A point  $P$  moves such that the ratio  $\frac{PA}{PB} = 2$  where  $A$  and  $B$  are fixed points 9 cm apart. The locus of  $P$  is:
- A straight line
  - A circle
  - An ellipse
  - The perpendicular bisector of  $AB$
50. The locus of points that are 6 cm from point  $O$  and also lie on a circle of radius 10 cm centered at  $O$  consists of:
- 0 points
  - 1 point
  - Infinitely many points
  - The entire circle of radius 10 cm
51. A line segment  $PQ$  of length 8 cm moves such that  $P$  always lies on line  $l_1$  and  $Q$  always lies on line  $l_2$  where  $l_1 \perp l_2$ . The locus of the midpoint of  $PQ$  is:
- A straight line
  - A quarter circle of radius 4 cm
  - A circle of radius 4 cm
  - An ellipse
52. Points  $R$  and  $S$  are 11 cm apart. The number of points that are 7 cm from  $R$  and 8 cm from  $S$  is:
- 0



- B. 1  
C. 2  
D. 3
53. The locus of points equidistant from two concentric circles of radii 4 cm and 8 cm is:  
A. A circle of radius 6 cm  
B. A circle of radius 12 cm  
C. The perpendicular bisector  
D. No such locus exists
54. A point  $P$  is 5 cm from a line  $l$ . How many points are 3 cm from  $P$  and 3 cm from line  $l$ ?  
A. 1  
B. 2  
C. 3  
D. 4
55. The locus of the vertices of all right-angled triangles on the same base is:  
A. A straight line  
B. A circle with the base as diameter  
C. The perpendicular bisector of the base  
D. Two circles
56. Points  $T$  and  $U$  are 16 cm apart. How many points are 10 cm from  $T$  and equidistant from  $T$  and  $U$ ?  
A. 0  
B. 1  
C. 2  
D. 3
57. A point moves such that the product of its distances from two fixed points is constant. The locus is:  
A. A circle  
B. An ellipse  
C. A cassinian oval  
D. A hyperbola
58. The locus of points that are 3 cm from a fixed point  $O$  and also 3 cm from a fixed line  $l$  that is 5 cm from  $O$  consists of:  
A. 0 points  
B. 1 point  
C. 2 points  
D. 4 points
59. Two lines intersect at  $60^\circ$ . The locus of points 4 cm from the point of intersection and equidistant from both lines consists of:  
A. 2 points  
B. 4 points  
C. 6 points  
D. 8 points
60. A circle of radius 5 cm rolls along a straight line without slipping. The locus of a point on the circumference of the circle is:  
A. A straight line parallel to the given line  
B. A circle  
C. A cycloid  
D. A sine wave
61. Points  $V$  and  $W$  are 13 cm apart. The locus of points  $P$  such that  $\angle VPW = 90^\circ$  is:  
A. A straight line perpendicular to  $VW$   
B. A circle with  $VW$  as diameter  
C. The perpendicular bisector of  $VW$   
D. Two circles
62. The locus of points in a plane such that the sum of squares of distances from two fixed points is constant forms:  
A. A straight line  
B. A circle  
C. An ellipse  
D. A hyperbola
63. A point  $P$  is equidistant from two intersecting lines that meet at  $45^\circ$ . If  $P$  is 6 cm from the point of intersection, how many such points exist?  
A. 2  
B. 4  
C. 6  
D. 8
64. The locus of the midpoints of all chords of length 8 cm in a circle of radius 5 cm is:  
A. The center of the circle only  
B. A circle of radius 3 cm  
C. A circle of radius 4 cm  
D. A straight line
65. Points  $X$  and  $Y$  are 24 cm apart. How many points are 15 cm from  $X$  and 20 cm from  $Y$ ?  
A. 0  
B. 1  
C. 2  
D. 3
66. A point moves such that its distance from point  $A$  is always half its distance from point  $B$  where  $AB = 12$  cm. The locus is:  
A. A straight line  
B. A circle  
C. The perpendicular bisector of  $AB$   
D. A parabola
67. The locus of centers of all circles of radius 3 cm that touch a given line  $l$  is:  
A. A single line parallel to  $l$   
B. Two lines parallel to  $l$ , each 3 cm away  
C. A circle  
D. The line  $l$  itself
68. A point  $P$  is 8 cm from point  $A$  and 6 cm from point  $B$  where  $AB = 10$  cm. How many such points  $P$  exist?

- A. 0  
B. 1  
C. 2  
D. Infinitely many
69. The locus of points at a distance of 4 cm from a line segment  $AB$  of length 6 cm and lying in the same plane consists of:  
A. Two parallel line segments only  
B. A rectangle  
C. A stadium shape (rectangle with semicircular ends)  
D. A circle
70. Points  $Z$  and  $A_1$  are 30 cm apart. The number of points that are 18 cm from  $Z$  and 18 cm from  $A_1$  is:  
A. 0  
B. 1  
C. 2  
D. 4
71. A square  $ABCD$  has side length 8 cm. The locus of points equidistant from all four vertices is:  
A. The center of the square only  
B. A circle passing through all vertices  
C. The perpendicular bisectors of all sides  
D. Four points
72. The locus of points that are 5 cm from a circle of radius 5 cm and lie inside the circle is:  
A. A circle of radius 0 cm (the center only)  
B. A circle of radius 10 cm  
C. No such points exist  
D. The entire interior of the circle
73. A point  $P$  moves such that  $2 \cdot PA = 3 \cdot PB$  where  $A$  and  $B$  are fixed points. The locus of  $P$  is:  
A. A straight line  
B. A circle (Apollonius circle)  
C. The perpendicular bisector of  $AB$   
D. An ellipse
74. Two perpendicular lines  $l_1$  and  $l_2$  intersect at point  $O$ . The locus of points that are 7 cm from  $O$  and equidistant from  $l_1$  and  $l_2$  consists of:  
A. 2 points  
B. 4 points  
C. 6 points  
D. 8 points
75. Points  $B_1$  and  $C_1$  are 14 cm apart. How many points are 9 cm from  $B_1$  and 10 cm from  $C_1$ ?  
A. 0  
B. 1  
C. 2  
D. 3
76. A point moves such that its distance from a fixed point is equal to its distance from a fixed circle (not containing the point). The locus is:  
A. A circle  
B. An ellipse  
C. A parabola  
D. A conic section depending on the configuration
77. The locus of the center of a circle of radius 4 cm that touches a fixed circle of radius 6 cm externally is:  
A. A circle of radius 2 cm  
B. A circle of radius 6 cm  
C. A circle of radius 10 cm  
D. A circle of radius 4 cm
78. A point  $P$  is 12 cm from a line  $l$  and also 13 cm from a point  $Q$  that is 5 cm from line  $l$ . How many such points  $P$  are possible?  
A. 0  
B. 1  
C. 2  
D. 4
79. Points  $D_1$  and  $E_1$  are 25 cm apart. The locus of points equidistant from  $D_1$  and  $E_1$  and also 20 cm from  $D_1$  consists of:  
A. 0 points  
B. 1 point  
C. 2 points  
D. 4 points
80. The locus of points from which the angle subtended by a line segment  $AB$  is  $60^\circ$  forms:  
A. Two circular arcs on opposite sides of  $AB$   
B. A complete circle  
C. The perpendicular bisector of  $AB$   
D. Two straight lines
81. A triangle  $ABC$  has  $AB = 10$  cm,  $BC = 8$  cm, and  $AC = 6$  cm. The locus of points equidistant from all three sides is:  
A. The circumcenter  
B. The centroid  
C. The incenter  
D. The orthocenter
82. Points  $F_1$  and  $G_1$  are 21 cm apart. How many points are 13 cm from  $F_1$  and 13 cm from  $G_1$ ?  
A. 0  
B. 1  
C. 2  
D. 4
83. The locus of points at which a line segment subtends a constant angle  $\alpha$  (where  $0^\circ < \alpha < 180^\circ$ ) forms:  
A. Two straight lines  
B. Two circular arcs

- C. A complete circle  
D. An ellipse
84. A point  $P$  moves such that  $3 \cdot PA = 4 \cdot PB$  where  $A$  and  $B$  are 14 cm apart. The locus is:  
A. A straight line  
B. A circle  
C. A parabola  
D. An ellipse
85. The locus of midpoints of all line segments of length 12 cm with endpoints on two parallel lines 8 cm apart is:  
A. A line parallel to the given lines  
B. Two lines parallel to the given lines  
C. A region between two parallel lines  
D. The entire plane
86. Points  $H_1$  and  $I_1$  are 17 cm apart. The number of points that are 10 cm from  $H_1$  and 10 cm from  $I_1$  is:  
A. 0  
B. 1  
C. 2  
D. 4
87. A point moves such that the sum of its distances from two perpendicular lines is constant and equals 10 cm. The locus is:  
A. A circle  
B. A square  
C. A straight line  
D. A line segment
88. The locus of the vertex of an isosceles triangle with a fixed base  $AB$  and constant vertical angle  $\alpha$  is:  
A. The perpendicular bisector of  $AB$   
B. A circle passing through  $A$  and  $B$   
C. Two circular arcs  
D. A straight line through  $A$  and  $B$
89. Points  $J_1$  and  $K_1$  are 28 cm apart. How many points are 16 cm from  $J_1$  and 20 cm from  $K_1$ ?  
A. 0  
B. 1  
C. 2  
D. 3
90. A point  $P$  is such that the angle  $\angle APB = 45^\circ$  where  $A$  and  $B$  are fixed points 10 cm apart. The complete locus of  $P$  consists of:  
A. One circular arc  
B. Two circular arcs on opposite sides of  $AB$   
C. A complete circle  
D. Two semicircles
91. The locus of centers of all circles passing through a fixed point  $P$  and having radius  $r$  is:  
A. A point  
B. A circle of radius  $r$  centered at  $P$   
C. A line through  $P$   
D. The entire plane
92. Points  $L_1$  and  $M_1$  are 32 cm apart. The locus of points equidistant from  $L_1$  and  $M_1$  and also 25 cm from  $L_1$  consists of:  
A. 0 points  
B. 1 point  
C. 2 points  
D. 4 points
93. A rectangle has length 12 cm and width 5 cm. The locus of points equidistant from all four vertices is:  
A. The center of the rectangle only  
B. A circle  
C. The diagonals of the rectangle  
D. Four points
94. The locus of points whose distance from a fixed point  $O$  is twice their distance from a fixed line  $l$  (where  $O$  is not on  $l$ ) is:  
A. A circle  
B. An ellipse  
C. A parabola  
D. A hyperbola
95. Points  $N_1$  and  $O_1$  are 19 cm apart. How many points are 12 cm from  $N_1$  and 12 cm from  $O_1$ ?  
A. 0  
B. 1  
C. 2  
D. 4
96. A circle has center  $O$  and radius 8 cm. The locus of midpoints of all chords of the circle that have length 12 cm is:  
A. The center  $O$  only  
B. A circle of radius  $2\sqrt{7}$  cm  
C. A circle of radius 6 cm  
D. A circle of radius 4 cm
97. A point moves such that it is always 4 cm from a fixed line and also 4 cm from a fixed point on that line. The locus consists of:  
A. 0 points  
B. 1 point  
C. 2 points  
D. 3 points
98. The locus of the center of a circle that passes through two fixed points  $A$  and  $B$  and has radius  $r$  (where  $r > \frac{AB}{2}$ ) is:  
A. A single point  
B. The perpendicular bisector of  $AB$   
C. A circle centered at the midpoint of  $AB$   
D. Two points on the perpendicular bisector of  $AB$

99. Points  $P_1$  and  $Q_1$  are 26 cm apart. The number of points that are 17 cm from  $P_1$  and equidistant from  $P_1$  and  $Q_1$  is:
- 0
  - 1
  - 2
  - 3
100. A point  $P$  moves in a plane such that the absolute difference of its distances from two fixed points is zero. The locus of  $P$  is:
- A straight line
  - A circle
  - The perpendicular bisector of the line joining the two points
  - A single point

## 3.4 Trigonometry

### 3.4.1 Questions

- In a right-angled triangle, if the opposite side is 5 cm and the hypotenuse is 13 cm, what is  $\sin \theta$ ?
  - $\frac{5}{12}$
  - $\frac{5}{13}$
  - $\frac{12}{13}$
  - $\frac{13}{5}$
- A right-angled triangle has an adjacent side of 7 cm and a hypotenuse of 25 cm. Find  $\cos \theta$ .
  - $\frac{7}{24}$
  - $\frac{7}{25}$
  - $\frac{24}{25}$
  - $\frac{25}{7}$
- If  $\tan \theta = \frac{3}{4}$ , find the value of  $\sin \theta$ .
  - $\frac{3}{4}$
  - $\frac{3}{5}$
  - $\frac{4}{5}$
  - $\frac{5}{3}$
- In a right-angled triangle with opposite side 8 cm and adjacent side 15 cm, find  $\tan \theta$ .
  - $\frac{8}{15}$
  - $\frac{15}{8}$
  - $\frac{8}{17}$
  - $\frac{15}{17}$
- A man standing 20 m from a building observes the top at an angle of elevation of  $30^\circ$ . What is the height of the building?
  - 10 m
  - $\frac{20}{\sqrt{3}}$  m
  - $20\sqrt{3}$  m
  - 40 m
- If  $\sin \theta = \frac{12}{13}$ , find  $\cos \theta$ .
  - $\frac{5}{13}$
  - $\frac{12}{5}$
  - $\frac{13}{12}$
  - $\frac{13}{5}$
- In triangle  $ABC$ ,  $a = 7$  cm,  $b = 8$  cm, and  $\angle C = 60^\circ$ . Find the length of side  $c$  using the cosine rule.
  - $\sqrt{57}$  cm
  - $\sqrt{85}$  cm
  - 9 cm
  - $\sqrt{113}$  cm
- A triangle has sides  $a = 5$  cm,  $b = 7$  cm, and  $c = 8$  cm. Find  $\cos A$ .
  - $\frac{3}{4}$
  - $\frac{7}{8}$
  - $\frac{19}{28}$
  - $\frac{5}{7}$
- From the top of a cliff 50 m high, the angle of depression to a boat is  $25^\circ$ . How far is the boat from the base of the cliff?
  - $50 \tan 25^\circ$  m
  - $\frac{50}{\tan 25^\circ}$  m
  - $50 \sin 25^\circ$  m
  - $\frac{50}{\cos 25^\circ}$  m
- In triangle  $PQR$ ,  $p = 10$  cm,  $\angle Q = 45^\circ$ , and  $\angle R = 60^\circ$ . Find the length of side  $q$  using the sine rule.
  - $\frac{10\sqrt{2}}{\sqrt{3}}$  cm
  - $\frac{10}{\sqrt{2}}$  cm
  - $\frac{10\sqrt{3}}{\sqrt{2}}$  cm
  - $10\sqrt{6}$  cm
- If  $\cos \theta = \frac{5}{13}$ , find  $\tan \theta$ .
  - $\frac{5}{12}$
  - $\frac{12}{5}$
  - $\frac{12}{13}$
  - $\frac{13}{12}$
- A ladder 10 m long leans against a wall making an angle of  $60^\circ$  with the ground. How high up the wall does the ladder reach?
  - 5 m
  - $5\sqrt{3}$  m

- C.  $10\sqrt{3}$  m  
D.  $\frac{10}{\sqrt{3}}$  m
13. Find the area of a triangle with sides  $a = 6$  cm,  $b = 8$  cm, and included angle  $C = 30^\circ$ .  
A.  $12 \text{ cm}^2$   
B.  $24 \text{ cm}^2$   
C.  $48 \text{ cm}^2$   
D.  $12\sqrt{3} \text{ cm}^2$
14. Solve for  $\theta$  in the range  $0^\circ \leq \theta \leq 360^\circ$ :  $\sin \theta = \frac{1}{2}$ .  
A.  $30^\circ, 150^\circ$   
B.  $60^\circ, 120^\circ$   
C.  $30^\circ, 330^\circ$   
D.  $45^\circ, 135^\circ$
15. A ship sails from port on a bearing of  $060^\circ$  for 30 km. How far east has the ship traveled?  
A. 15 km  
B.  $15\sqrt{3}$  km  
C.  $30 \sin 60^\circ$  km  
D.  $30 \cos 60^\circ$  km
16. If  $\sin \theta + \cos \theta = 1$ , and  $0^\circ \leq \theta \leq 90^\circ$ , find  $\theta$ .  
A.  $0^\circ$  or  $90^\circ$   
B.  $30^\circ$   
C.  $45^\circ$   
D.  $60^\circ$
17. In triangle  $ABC$ ,  $a = 12$  cm,  $b = 9$  cm, and  $\angle A = 80^\circ$ . Find  $\angle B$  using the sine rule.  
A.  $\sin^{-1} \left( \frac{9 \sin 80^\circ}{12} \right)$   
B.  $\sin^{-1} \left( \frac{12 \sin 80^\circ}{9} \right)$   
C.  $\cos^{-1} \left( \frac{9}{12} \right)$   
D.  $80^\circ - \sin^{-1} \left( \frac{9}{12} \right)$
18. If  $\tan \theta = 1$ , find all values of  $\theta$  in the range  $0^\circ \leq \theta \leq 360^\circ$ .  
A.  $45^\circ, 225^\circ$   
B.  $30^\circ, 210^\circ$   
C.  $60^\circ, 240^\circ$   
D.  $90^\circ, 270^\circ$
19. A tree casts a shadow 15 m long when the angle of elevation of the sun is  $40^\circ$ . Find the height of the tree.  
A.  $15 \sin 40^\circ$  m  
B.  $15 \cos 40^\circ$  m  
C.  $15 \tan 40^\circ$  m  
D.  $\frac{15}{\tan 40^\circ}$  m
20. Find the value of  $\sin^2 30^\circ + \cos^2 30^\circ$ .  
A.  $\frac{1}{2}$   
B.  $\frac{3}{4}$   
C. 1  
D.  $\frac{\sqrt{3}}{2}$
21. In triangle  $XYZ$ ,  $x = 15$  cm,  $y = 20$  cm, and  $z = 25$  cm. Find  $\angle Z$ .  
A.  $30^\circ$   
B.  $60^\circ$   
C.  $90^\circ$   
D.  $120^\circ$
22. A man 1.8 m tall observes the top of a pole at an angle of elevation of  $50^\circ$ . If he is standing 12 m from the pole, find the height of the pole.  
A.  $12 \tan 50^\circ$  m  
B.  $(12 \tan 50^\circ + 1.8)$  m  
C.  $(12 \sin 50^\circ + 1.8)$  m  
D.  $\frac{12}{\tan 50^\circ}$  m
23. If  $\cos \theta = -\frac{1}{2}$  and  $90^\circ < \theta < 180^\circ$ , find  $\theta$ .  
A.  $120^\circ$   
B.  $135^\circ$   
C.  $150^\circ$   
D.  $210^\circ$
24. Two sides of a triangle are 8 cm and 11 cm, and the included angle is  $70^\circ$ . Find the area of the triangle.  
A.  $44 \sin 70^\circ \text{ cm}^2$   
B.  $88 \sin 70^\circ \text{ cm}^2$   
C.  $44 \cos 70^\circ \text{ cm}^2$   
D.  $22 \sin 70^\circ \text{ cm}^2$
25. From point  $P$ , the angle of elevation to the top of a tower is  $35^\circ$ . From point  $Q$ , 50 m closer to the tower, the angle is  $55^\circ$ . Find the height of the tower.  
A.  $\frac{50 \tan 35^\circ \tan 55^\circ}{\tan 55^\circ - \tan 35^\circ}$  m  
B.  $50 \tan 35^\circ$  m  
C.  $50 \tan 55^\circ$  m  
D.  $\frac{50}{\tan 35^\circ + \tan 55^\circ}$  m
26. Solve for  $\theta$ :  $2 \sin \theta = \sqrt{3}$ , where  $0^\circ \leq \theta \leq 360^\circ$ .  
A.  $60^\circ, 120^\circ$   
B.  $30^\circ, 150^\circ$   
C.  $45^\circ, 135^\circ$   
D.  $60^\circ, 300^\circ$
27. A plane flies on a bearing of  $135^\circ$  for 100 km. How far south has it traveled?  
A. 50 km  
B.  $50\sqrt{2}$  km  
C.  $100 \sin 45^\circ$  km  
D.  $100 \cos 45^\circ$  km
28. In triangle  $DEF$ ,  $d = 13$  cm,  $e = 14$  cm, and  $f = 15$  cm. Find  $\cos D$  using the cosine rule.  
A.  $\frac{2}{5}$   
B.  $\frac{3}{5}$   
C.  $\frac{4}{5}$   
D.  $\frac{16}{21}$
29. If  $\tan \theta = -\sqrt{3}$  and  $180^\circ < \theta < 270^\circ$ , find  $\theta$ .

- A.  $210^\circ$   
 B.  $240^\circ$   
 C.  $225^\circ$   
 D.  $300^\circ$
30. A tower stands on level ground. From a point 40 m away, the angle of elevation to the top is  $28^\circ$ . Find the height of the tower.  
 A.  $40 \sin 28^\circ$  m  
 B.  $40 \cos 28^\circ$  m  
 C.  $40 \tan 28^\circ$  m  
 D.  $\frac{40}{\sin 28^\circ}$  m
31. Find the value of  $\sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$ .  
 A.  $\frac{1}{2}$   
 B.  $\frac{\sqrt{3}}{2}$   
 C. 1  
 D.  $\frac{1}{\sqrt{2}}$
32. In triangle  $ABC$ ,  $a = 10$  cm,  $b = 14$  cm, and  $\angle C = 45^\circ$ . Find side  $c$ .  
 A.  $2\sqrt{37}$  cm  
 B.  $\sqrt{296 - 140\sqrt{2}}$  cm  
 C. 12 cm  
 D.  $\sqrt{100 + 196}$  cm
33. A ship sails from port  $A$  on a bearing of  $N30^\circ E$  for 60 km to port  $B$ . How far north of  $A$  is port  $B$ ?  
 A. 30 km  
 B.  $30\sqrt{3}$  km  
 C.  $60 \sin 30^\circ$  km  
 D.  $60 \cos 30^\circ$  km
34. Solve for  $\theta$ :  $\cos \theta = 0$ , where  $0^\circ \leq \theta \leq 360^\circ$ .  
 A.  $0^\circ, 180^\circ$   
 B.  $90^\circ, 270^\circ$   
 C.  $0^\circ, 360^\circ$   
 D.  $45^\circ, 225^\circ$
35. The area of a triangle is  $36 \text{ cm}^2$ . If two sides are 9 cm and 10 cm, find the included angle.  
 A.  $\sin^{-1}\left(\frac{4}{5}\right)$   
 B.  $\sin^{-1}\left(\frac{3}{5}\right)$   
 C.  $\cos^{-1}\left(\frac{4}{5}\right)$   
 D.  $\tan^{-1}\left(\frac{4}{5}\right)$
36. If  $\sin \theta = \frac{3}{5}$  and  $\theta$  is acute, find  $\cos \theta + \tan \theta$ .  
 A.  $\frac{7}{5}$   
 B.  $\frac{19}{20}$   
 C.  $\frac{23}{20}$   
 D.  $\frac{9}{5}$
37. From a lighthouse 75 m high, the angle of depression to a ship is  $18^\circ$ . How far is the ship from the base of the lighthouse?  
 A.  $75 \tan 18^\circ$  m  
 B.  $\frac{75}{\tan 18^\circ}$  m  
 C.  $75 \sin 18^\circ$  m  
 D.  $\frac{75}{\sin 18^\circ}$  m
38. In triangle  $PQR$ ,  $p = 7$  cm,  $q = 24$  cm, and  $r = 25$  cm. Find  $\sin R$ .  
 A.  $\frac{7}{25}$   
 B.  $\frac{24}{25}$   
 C.  $\frac{7}{24}$   
 D. 1
39. Solve for  $\theta$ :  $2 \cos \theta + 1 = 0$ , where  $0^\circ \leq \theta \leq 360^\circ$ .  
 A.  $60^\circ, 300^\circ$   
 B.  $120^\circ, 240^\circ$   
 C.  $135^\circ, 225^\circ$   
 D.  $150^\circ, 210^\circ$
40. A plane flies from town  $A$  on a bearing of  $240^\circ$  for 80 km. How far west of  $A$  is the plane?  
 A. 40 km  
 B.  $40\sqrt{3}$  km  
 C.  $80 \sin 60^\circ$  km  
 D.  $80 \cos 60^\circ$  km
41. In triangle  $ABC$ ,  $a = 9$  cm,  $c = 12$  cm, and  $\angle B = 120^\circ$ . Find side  $b$  using the cosine rule.  
 A. 15 cm  
 B.  $\sqrt{261}$  cm  
 C. 21 cm  
 D.  $3\sqrt{37}$  cm
42. If  $\sin \theta = -\frac{\sqrt{2}}{2}$  and  $270^\circ < \theta < 360^\circ$ , find  $\theta$ .  
 A.  $225^\circ$   
 B.  $270^\circ$   
 C.  $300^\circ$   
 D.  $315^\circ$
43. A rope from the top of a flagpole to a point on the ground 8 m from its base makes an angle of  $65^\circ$  with the ground. Find the height of the flagpole.  
 A.  $8 \sin 65^\circ$  m  
 B.  $8 \cos 65^\circ$  m  
 C.  $8 \tan 65^\circ$  m  
 D.  $\frac{8}{\cos 65^\circ}$  m
44. Find the value of  $\tan 45^\circ + \tan 30^\circ$ .  
 A.  $1 + \frac{1}{\sqrt{3}}$   
 B.  $\frac{\sqrt{3}+1}{\sqrt{3}}$   
 C.  $\sqrt{3} + 1$   
 D.  $\frac{2}{\sqrt{3}}$
45. In triangle  $PQR$ ,  $p = 16$  cm,  $q = 12$  cm, and  $r = 20$  cm. Find  $\angle Q$ .  
 A.  $30^\circ$   
 B.  $37^\circ$

- C.  $53^\circ$   
D.  $90^\circ$
46. Two ships leave a port at the same time. One sails on a bearing of  $040^\circ$  at 15 km/h, the other on a bearing of  $130^\circ$  at 20 km/h. How far apart are they after 2 hours?
- A.  $10\sqrt{13}$  km  
B.  $20\sqrt{13}$  km  
C. 30 km  
D. 50 km
47. Solve for  $\theta$ :  $\sin^2 \theta = \frac{3}{4}$ , where  $0^\circ \leq \theta \leq 180^\circ$ .
- A.  $30^\circ, 150^\circ$   
B.  $45^\circ, 135^\circ$   
C.  $60^\circ, 120^\circ$   
D.  $90^\circ$
48. A vertical pole stands on a slope that makes an angle of  $10^\circ$  with the horizontal. From a point 30 m down the slope, the angle of elevation to the top of the pole is  $25^\circ$ . Find the height of the pole.
- A.  $30 \sin 15^\circ$  m  
B.  $30 \sin 25^\circ$  m  
C.  $30 \tan 15^\circ$  m  
D.  $30 \sin 35^\circ$  m
49. If  $\cos A = \frac{3}{5}$  and  $\cos B = \frac{5}{13}$  where  $A$  and  $B$  are acute, find  $\sin(A + B)$ .
- A.  $\frac{56}{65}$   
B.  $\frac{63}{65}$   
C.  $\frac{16}{65}$   
D.  $\frac{48}{65}$
50. The area of triangle  $ABC$  is  $50 \text{ cm}^2$ . If  $a = 10$  cm and  $b = 13$  cm, find the possible values of  $\angle C$ .
- A.  $\sin^{-1}\left(\frac{10}{13}\right)$  or  $180^\circ - \sin^{-1}\left(\frac{10}{13}\right)$   
B.  $\sin^{-1}\left(\frac{5}{13}\right)$  or  $180^\circ - \sin^{-1}\left(\frac{5}{13}\right)$   
C.  $\sin^{-1}\left(\frac{10}{13}\right)$  only  
D.  $90^\circ$
51. From the top of a building 80 m high, the angles of depression to two cars on opposite sides of the building are  $30^\circ$  and  $45^\circ$ . Find the distance between the cars.
- A.  $80(1 + \sqrt{3})$  m  
B. 160 m  
C.  $80\sqrt{3}$  m  
D.  $80(\sqrt{3} - 1)$  m
52. Solve for  $\theta$ :  $\tan^2 \theta = 3$ , where  $0^\circ \leq \theta \leq 360^\circ$ .
- A.  $60^\circ, 120^\circ, 240^\circ, 300^\circ$   
B.  $30^\circ, 150^\circ, 210^\circ, 330^\circ$   
C.  $45^\circ, 135^\circ, 225^\circ, 315^\circ$   
D.  $60^\circ, 240^\circ$  only
53. In triangle  $XYZ$ ,  $x = 7$  cm,  $y = 10$  cm, and  $\angle Z = 75^\circ$ . Find the area of the triangle.
- A.  $35 \sin 75^\circ \text{ cm}^2$   
B.  $70 \sin 75^\circ \text{ cm}^2$   
C.  $35 \cos 75^\circ \text{ cm}^2$   
D.  $\frac{35 \sin 75^\circ}{2} \text{ cm}^2$
54. A plane flies from airport  $A$  to airport  $B$  on a bearing of  $110^\circ$  for 200 km. What is the eastward displacement?
- A.  $200 \sin 20^\circ$  km  
B.  $200 \cos 20^\circ$  km  
C.  $200 \sin 70^\circ$  km  
D.  $200 \cos 70^\circ$  km
55. If  $\sin \theta = \frac{7}{25}$  and  $90^\circ < \theta < 180^\circ$ , find  $\tan \theta$ .
- A.  $-\frac{7}{24}$   
B.  $\frac{7}{24}$   
C.  $-\frac{24}{7}$   
D.  $\frac{24}{7}$
56. In triangle  $ABC$ ,  $a = 11$  cm,  $\angle B = 50^\circ$ , and  $\angle C = 70^\circ$ . Find side  $b$  using the sine rule.
- A.  $\frac{11 \sin 50^\circ}{\sin 60^\circ}$  cm  
B.  $\frac{11 \sin 60^\circ}{\sin 50^\circ}$  cm  
C.  $\frac{11 \sin 70^\circ}{\sin 50^\circ}$  cm  
D.  $11 \sin 50^\circ$  cm
57. A ladder 6 m long rests against a vertical wall. If the foot of the ladder is 2 m from the wall, find the angle the ladder makes with the ground.
- A.  $\cos^{-1}\left(\frac{1}{3}\right)$   
B.  $\sin^{-1}\left(\frac{1}{3}\right)$   
C.  $\cos^{-1}\left(\frac{2}{3}\right)$   
D.  $\sin^{-1}\left(\frac{2}{3}\right)$
58. Find all values of  $\theta$  in the range  $0^\circ \leq \theta \leq 360^\circ$  such that  $2 \cos^2 \theta = 1$ .
- A.  $45^\circ, 135^\circ, 225^\circ, 315^\circ$   
B.  $60^\circ, 120^\circ, 240^\circ, 300^\circ$   
C.  $30^\circ, 150^\circ, 210^\circ, 330^\circ$   
D.  $0^\circ, 90^\circ, 180^\circ, 270^\circ$
59. Two sides of a triangle are 15 cm and 18 cm, enclosing an angle of  $100^\circ$ . Find the third side.
- A.  $\sqrt{549 + 540 \cos 80^\circ}$  cm  
B.  $\sqrt{549 - 540 \cos 80^\circ}$  cm  
C.  $\sqrt{549 - 540 \cos 100^\circ}$  cm  
D.  $\sqrt{549 + 540 \cos 100^\circ}$  cm
60. A man walks 5 km on a bearing of  $N60^\circ W$ . How far west has he walked?
- A. 2.5 km  
B.  $2.5\sqrt{3}$  km  
C.  $5 \sin 60^\circ$  km  
D.  $5 \cos 60^\circ$  km
61. If  $\tan \theta = \frac{5}{12}$  and  $\theta$  is acute, find  $\sec \theta$ .

- A.  $\frac{12}{13}$   
 B.  $\frac{13}{12}$   
 C.  $\frac{5}{13}$   
 D.  $\frac{13}{5}$
62. Solve for  $\theta$ :  $\sin \theta \cos \theta = \frac{1}{4}$ , where  $0^\circ \leq \theta \leq 90^\circ$ .  
 A.  $30^\circ$   
 B.  $45^\circ$   
 C.  $60^\circ$   
 D. No solution in the given range
63. In triangle  $DEF$ ,  $d = 20$  cm,  $e = 21$  cm, and  $f = 29$  cm. Find  $\sin F$ .  
 A.  $\frac{20}{29}$   
 B.  $\frac{21}{29}$   
 C.  $\frac{420}{841}$   
 D. 1
64. From a point on level ground, the angle of elevation to the top of a tower is  $40^\circ$ . After walking 50 m toward the tower, the angle is  $60^\circ$ . Find the height of the tower.  
 A.  $\frac{50 \tan 40^\circ \tan 60^\circ}{\tan 60^\circ - \tan 40^\circ}$  m  
 B.  $50 \tan 40^\circ$  m  
 C.  $50 \tan 60^\circ$  m  
 D.  $25(\tan 40^\circ + \tan 60^\circ)$  m
65. If  $\cos \theta = \frac{8}{17}$  and  $\theta$  is in the fourth quadrant, find  $\sin \theta$ .  
 A.  $\frac{15}{17}$   
 B.  $-\frac{15}{17}$   
 C.  $\frac{8}{15}$   
 D.  $-\frac{8}{15}$
66. The bearing of point  $B$  from point  $A$  is  $125^\circ$ . Find the bearing of  $A$  from  $B$ .  
 A.  $235^\circ$   
 B.  $305^\circ$   
 C.  $055^\circ$   
 D.  $215^\circ$
67. In triangle  $ABC$ ,  $b = 8$  cm,  $c = 10$  cm, and  $\angle A = 90^\circ$ . Find  $\sin B$ .  
 A.  $\frac{4}{5}$   
 B.  $\frac{3}{5}$   
 C.  $\frac{5}{8}$   
 D.  $\frac{5}{4}$
68. Solve for  $\theta$ :  $4 \sin^2 \theta - 3 = 0$ , where  $0^\circ \leq \theta \leq 360^\circ$ .  
 A.  $30^\circ, 150^\circ, 210^\circ, 330^\circ$   
 B.  $45^\circ, 135^\circ, 225^\circ, 315^\circ$   
 C.  $60^\circ, 120^\circ, 240^\circ, 300^\circ$   
 D.  $90^\circ, 270^\circ$
69. A boat sails 40 km on a bearing of  $070^\circ$ , then 30 km on a bearing of  $160^\circ$ . How far is it from its starting point?  
 A.  $10\sqrt{13}$  km  
 B. 50 km  
 C.  $\sqrt{2500 - 2400 \cos 90^\circ}$  km  
 D. 70 km
70. If  $\tan A = \frac{3}{4}$  and  $\tan B = \frac{5}{12}$  where  $A$  and  $B$  are acute, find  $\tan(A + B)$ .  
 A.  $\frac{63}{16}$   
 B.  $\frac{56}{33}$   
 C.  $\frac{16}{63}$   
 D.  $\frac{33}{56}$
71. The area of an equilateral triangle is  $16\sqrt{3}$  cm<sup>2</sup>. Find the length of each side.  
 A. 4 cm  
 B. 8 cm  
 C. 12 cm  
 D. 16 cm
72. From a point  $P$ , the bearing of point  $Q$  is  $050^\circ$  and the bearing of point  $R$  is  $140^\circ$ . If  $PQ = PR = 100$  m, find the distance  $QR$ .  
 A. 100 m  
 B.  $100\sqrt{2}$  m  
 C.  $100\sqrt{3}$  m  
 D. 200 m
73. Solve for  $\theta$ :  $\cos \theta + \sin \theta = 1$ , where  $0^\circ \leq \theta \leq 360^\circ$ .  
 A.  $0^\circ, 90^\circ$   
 B.  $0^\circ, 180^\circ$   
 C.  $90^\circ, 270^\circ$   
 D.  $0^\circ, 90^\circ, 360^\circ$
74. In triangle  $PQR$ ,  $p = 13$  cm,  $q = 14$  cm, and  $\angle P = 55^\circ$ . Find  $\angle Q$  using the sine rule.  
 A.  $\sin^{-1} \left( \frac{14 \sin 55^\circ}{13} \right)$   
 B.  $\sin^{-1} \left( \frac{13 \sin 55^\circ}{14} \right)$   
 C.  $55^\circ$   
 D.  $\cos^{-1} \left( \frac{13}{14} \right)$
75. A vertical tower stands at the center of a circular field of radius 50 m. From a point on the circumference, the angle of elevation to the top of the tower is  $35^\circ$ . Find the height of the tower.  
 A.  $50 \sin 35^\circ$  m  
 B.  $50 \cos 35^\circ$  m  
 C.  $50 \tan 35^\circ$  m  
 D.  $\frac{50}{\tan 35^\circ}$  m
76. If  $\sin \theta = k$  where  $-1 \leq k \leq 1$ , find  $\sin(180^\circ - \theta)$ .  
 A.  $-k$   
 B.  $k$   
 C.  $1 - k$   
 D.  $\sqrt{1 - k^2}$



77. Two angles of a triangle are  $40^\circ$  and  $65^\circ$ . If the side opposite the  $40^\circ$  angle is 8 cm, find the side opposite the  $65^\circ$  angle.
- $\frac{8 \sin 65^\circ}{\sin 40^\circ}$  cm
  - $\frac{8 \sin 40^\circ}{\sin 65^\circ}$  cm
  - $8 \sin 65^\circ$  cm
  - $8 \cos 40^\circ$  cm
78. A parallelogram has adjacent sides of lengths 12 cm and 16 cm, with an included angle of  $70^\circ$ . Find the length of the longer diagonal.
- $\sqrt{544 - 384 \cos 70^\circ}$  cm
  - $\sqrt{544 + 384 \cos 70^\circ}$  cm
  - $\sqrt{544 - 384 \cos 110^\circ}$  cm
  - $\sqrt{544 + 384 \cos 110^\circ}$  cm
79. Solve for  $\theta$ :  $2 \sin \theta = \cos \theta$ , where  $0^\circ \leq \theta \leq 180^\circ$ .
- $\tan^{-1}(2)$
  - $\tan^{-1}\left(\frac{1}{2}\right)$
  - $30^\circ$
  - $60^\circ$
80. From a lighthouse 100 m above sea level, two boats are observed at angles of depression of  $20^\circ$  and  $35^\circ$  on the same side. Find the distance between the boats.
- $100 \left( \frac{1}{\tan 20^\circ} - \frac{1}{\tan 35^\circ} \right)$  m
  - $100 \left( \frac{1}{\tan 35^\circ} - \frac{1}{\tan 20^\circ} \right)$  m
  - $100(\tan 35^\circ - \tan 20^\circ)$  m
  - $\frac{100}{\tan 20^\circ + \tan 35^\circ}$  m
81. If  $\cos \theta = -\frac{3}{5}$  and  $180^\circ < \theta < 270^\circ$ , find  $\cot \theta$ .
- $\frac{3}{4}$
  - $-\frac{3}{4}$
  - $\frac{4}{3}$
  - $-\frac{4}{3}$
82. In triangle  $ABC$ ,  $a = 17$  cm,  $b = 15$  cm, and  $c = 8$  cm. Find  $\cos C$  using the cosine rule.
- $\frac{15}{17}$
  - $\frac{8}{17}$
  - $\frac{17}{15}$
  - $\frac{240}{255}$
83. A ship travels 60 km on a bearing of  $S40^\circ E$ . How far south has it traveled?
- $60 \sin 40^\circ$  km
  - $60 \cos 40^\circ$  km
  - $60 \sin 50^\circ$  km
  - $60 \cos 50^\circ$  km
84. Solve for  $\theta$ :  $\sin 2\theta = \sin \theta$ , where  $0^\circ \leq \theta \leq 180^\circ$ .
- $0^\circ, 60^\circ, 180^\circ$
  - $0^\circ, 90^\circ, 180^\circ$
  - $0^\circ, 120^\circ, 180^\circ$
  - $30^\circ, 150^\circ$
85. Two towers of heights 30 m and 50 m stand on level ground. If the distance between them is 60 m, find the angle of elevation from the top of the shorter tower to the top of the taller tower.
- $\tan^{-1}\left(\frac{1}{3}\right)$
  - $\tan^{-1}\left(\frac{1}{2}\right)$
  - $\tan^{-1}\left(\frac{2}{3}\right)$
  - $\tan^{-1}\left(\frac{3}{4}\right)$
86. If  $\tan \theta = -\frac{4}{3}$  and  $90^\circ < \theta < 180^\circ$ , find  $\sin \theta + \cos \theta$ .
- $\frac{1}{5}$
  - $-\frac{1}{5}$
  - $\frac{7}{5}$
  - $-\frac{7}{5}$
87. In triangle  $XYZ$ ,  $\angle X = 30^\circ$ ,  $\angle Y = 45^\circ$ , and  $z = 10$  cm. Find side  $x$ .
- 5 cm
  - $5\sqrt{2}$  cm
  - $10 \sin 30^\circ$  cm
  - $\frac{10 \sin 30^\circ}{\sin 105^\circ}$  cm
88. A ladder reaches a window 12 m above the ground when inclined at  $65^\circ$  to the horizontal. Find the length of the ladder.
- $\frac{12}{\sin 65^\circ}$  m
  - $\frac{12}{\cos 65^\circ}$  m
  - $12 \sin 65^\circ$  m
  - $12 \tan 65^\circ$  m
89. Find all values of  $\theta$  satisfying  $\cos 2\theta = 0$ , where  $0^\circ \leq \theta \leq 180^\circ$ .
- $45^\circ, 135^\circ$
  - $30^\circ, 150^\circ$
  - $60^\circ, 120^\circ$
  - $90^\circ$
90. Two sides of a triangle are 9 cm and 12 cm. If the area is  $27 \text{ cm}^2$ , find the included angle.
- $30^\circ$  or  $150^\circ$
  - $45^\circ$  or  $135^\circ$
  - $60^\circ$  or  $120^\circ$
  - $\sin^{-1}\left(\frac{1}{2}\right)$  or  $180^\circ - \sin^{-1}\left(\frac{1}{2}\right)$
91. A plane flies from city  $A$  on a bearing of  $310^\circ$  for 150 km to city  $B$ . What is the northward displacement?
- $150 \sin 50^\circ$  km
  - $150 \cos 50^\circ$  km
  - $150 \sin 40^\circ$  km
  - $150 \cos 40^\circ$  km
92. If  $\sec \theta = \frac{13}{5}$  and  $\theta$  is acute, find  $\csc \theta$ .
- $\frac{13}{12}$

- B.  $\frac{12}{13}$   
 C.  $\frac{5}{12}$   
 D.  $\frac{12}{5}$
93. In triangle  $ABC$ ,  $a = 6$  cm,  $b = 8$  cm, and  $c = 10$  cm. Find the area of the triangle.  
 A.  $24 \text{ cm}^2$   
 B.  $30 \text{ cm}^2$   
 C.  $40 \text{ cm}^2$   
 D.  $48 \text{ cm}^2$
94. Solve for  $\theta$ :  $\tan \theta + \cot \theta = 2$ , where  $0^\circ < \theta < 90^\circ$ .  
 A.  $30^\circ$   
 B.  $45^\circ$   
 C.  $60^\circ$   
 D.  $75^\circ$
95. Two observation posts are 8 km apart. A fire is spotted from both posts with bearings of  $045^\circ$  and  $315^\circ$  respectively from the posts. How far is the fire from the first post?  
 A. 4 km  
 B.  $4\sqrt{2}$  km  
 C. 8 km  
 D.  $8\sqrt{2}$  km
96. If  $\sin A = \frac{1}{3}$  and  $\cos B = \frac{1}{4}$  where  $A$  and  $B$  are acute, find  $\sin(A - B)$ .  
 A.  $\frac{1}{12}(4 - \sqrt{30})$   
 B.  $\frac{1}{12}(\sqrt{30} - 4)$   
 C.  $\frac{1}{12}(4\sqrt{2} - \sqrt{15})$   
 D.  $\frac{1}{12}(4 + \sqrt{30})$
97. A rhombus has side length 10 cm and one angle of  $60^\circ$ . Find the length of the shorter diagonal.  
 A. 5 cm  
 B. 10 cm  
 C.  $10\sqrt{3}$  cm  
 D. 20 cm
98. Solve for  $\theta$ :  $3 \tan^2 \theta = 1$ , where  $0^\circ \leq \theta \leq 360^\circ$ .  
 A.  $30^\circ, 150^\circ, 210^\circ, 330^\circ$   
 B.  $45^\circ, 135^\circ, 225^\circ, 315^\circ$   
 C.  $60^\circ, 120^\circ, 240^\circ, 300^\circ$   
 D.  $90^\circ, 270^\circ$
99. If  $\tan \theta = 3/4$  and  $\theta$  is acute, find  $\cos \theta$ .  
 A.  $3/5$   
 B.  $4/5$   
 C.  $5/4$   
 D.  $5/3$
100. Find the value of  $\sin^2 30^\circ + \cos^2 30^\circ$ .  
 A.  $1/2$   
 B.  $\sqrt{3}/2$   
 C. 1  
 D. 0

## 3.5 Co-ordinate Geometry

### 3.5.1 Questions

- Find the distance between points  $A(3, 4)$  and  $B(6, 8)$ .  
 A. 3  
 B. 4  
 C. 5  
 D. 7
- What is the midpoint of the line joining  $(-2, 5)$  and  $(4, -3)$ ?  
 A.  $(1, 1)$   
 B.  $(2, 2)$   
 C.  $(3, 4)$   
 D.  $(-1, -1)$
- Find the gradient of the line passing through  $(2, 3)$  and  $(5, 9)$ .  
 A. 1  
 B. 2  
 C. 3  
 D. 4
- The gradient of the line joining  $(-2, 0)$  and  $(0, -4)$  is  
 A.  $-2$   
 B.  $-1$   
 C. 2  
 D. 4
- Find the distance between points  $(0, 0)$  and  $(3, 4)$ .  
 A. 3  
 B. 4  
 C. 5  
 D. 7
- What is the midpoint between  $(6, 8)$  and  $(2, 4)$ ?  
 A.  $(4, 6)$   
 B.  $(8, 12)$

- C. (2, 2)  
D. (3, 5)
7. Find the gradient of the line  $2y = 4x + 6$   
A. 1  
B. 2  
C. 3  
D. 4
8. The distance between (1, 2) and (4, 6) is  
A. 3  
B. 4  
C. 5  
D. 7
9. Find the equation of a line with gradient 3 passing through (0, 2)  
A.  $y = 3x + 2$   
B.  $y = 2x + 3$   
C.  $y = 3x - 2$   
D.  $y = x + 5$
10. What is the midpoint of (10, 14) and (6, 2)?  
A. (8, 8)  
B. (16, 16)  
C. (4, 6)  
D. (2, 3)
11. Find the gradient of the line passing through (0, 5) and (3, 11)  
A. 1  
B. 2  
C. 3  
D. 6
12. The distance between (-3, 4) and (3, 4) is  
A. 0  
B. 3  
C. 6  
D. 8
13. Find the gradient of the line  $3y + 6x = 9$   
A. -2  
B. -1  
C. 2  
D. 3
14. What is the midpoint between (5, 7) and (9, 11)?  
A. (7, 9)  
B. (14, 18)  
C. (4, 4)  
D. (2, 2)
15. Find the distance between (2, 1) and (5, 5)  
A. 3  
B. 4  
C. 5  
D. 6
16. The gradient of a line parallel to  $y = 4x + 1$  is  
A. 1  
B. 2  
C. 4  
D. -4
17. Find the midpoint of (0, 0) and (8, 6)  
A. (4, 3)  
B. (8, 6)  
C. (2, 1.5)  
D. (16, 12)
18. What is the gradient of the line passing through (1, 1) and (4, 7)?  
A. 1  
B. 2  
C. 3  
D. 6
19. Find the distance between (-1, -1) and (2, 3)  
A. 3  
B. 4  
C. 5  
D. 6
20. The equation of a line with gradient 2 and y-intercept -3 is  
A.  $y = 2x - 3$   
B.  $y = -3x + 2$   
C.  $y = 2x + 3$   
D.  $y = 3x - 2$
21. Find the midpoint between (-4, 6) and (10, -2)

- A. (3, 2)  
B. (6, 4)  
C. (7, 4)  
D. (14, 8)
22. What is the gradient of the line  $y = -3x + 7$ ?  
A. -3  
B. 3  
C. 7  
D. -7
23. Find the distance between (5, 0) and (0, 12)  
A. 11  
B. 12  
C. 13  
D. 17
24. The gradient of a line perpendicular to  $y = 2x + 5$  is  
A. 2  
B. -2  
C.  $\frac{1}{2}$   
D.  $-\frac{1}{2}$
25. Find the midpoint of (7, 9) and (3, 5)  
A. (5, 7)  
B. (10, 14)  
C. (4, 4)  
D. (2, 2)
26. What is the gradient of the line passing through (2, 5) and (2, 9)?  
A. 0  
B. 1  
C. undefined  
D. 4
27. Find the distance between (6, 8) and (6, 2)  
A. 0  
B. 4  
C. 6  
D. 10
28. The equation of a line passing through (3, 4) with gradient -1 is  
A.  $y = -x + 7$   
B.  $y = x + 1$   
C.  $y = -x - 1$   
D.  $y = x + 7$
29. Find the midpoint between (12, 8) and (4, 16)  
A. (8, 12)  
B. (16, 24)  
C. (6, 6)  
D. (4, 4)
30. What is the gradient of a horizontal line?  
A. 0  
B. 1  
C. -1  
D. undefined
31. Find the distance between (8, 15) and (8, 3)  
A. 0  
B. 8  
C. 12  
D. 18
32. The gradient of the line  $4y = 8x - 12$  is  
A. 1  
B. 2  
C. 4  
D. 8
33. Find the midpoint of (-5, -3) and (7, 9)  
A. (1, 3)  
B. (2, 6)  
C. (6, 6)  
D. (12, 12)
34. What is the gradient of the line passing through (3, 2) and (7, 2)?  
A. 0  
B. 1  
C. 4  
D. undefined
35. Find the distance between (0, 5) and (12, 0)  
A. 11  
B. 12  
C. 13

- D. 17
36. The equation of a line with gradient  $\frac{1}{2}$  passing through (4, 3) is
- A.  $y = \frac{1}{2}x + 1$   
 B.  $y = 2x - 5$   
 C.  $y = \frac{1}{2}x - 1$   
 D.  $y = x + 1$
37. Find the midpoint between (9, 12) and (15, 4)
- A. (12, 8)  
 B. (24, 16)  
 C. (6, 8)  
 D. (3, 4)
38. What is the gradient of a vertical line?
- A. 0  
 B. 1  
 C. -1  
 D. undefined
39. Find the distance between (-2, -3) and (4, 5)
- A. 8  
 B. 9  
 C. 10  
 D. 11
40. The gradient of the line  $5y - 10x = 15$  is
- A. -2  
 B. 2  
 C. 5  
 D. 10
41. Find the midpoint of (20, 30) and (10, 10)
- A. (15, 20)  
 B. (30, 40)  
 C. (10, 20)  
 D. (5, 10)
42. What is the gradient of the line passing through (-1, 4) and (2, 10)?
- A. 1  
 B. 2  
 C. 3  
 D. 6
43. Find the distance between (7, 24) and (0, 0)
- A. 24  
 B. 25  
 C. 31  
 D. 7
44. The gradient of a line perpendicular to  $y = -\frac{1}{3}x + 4$  is
- A. -3  
 B.  $-\frac{1}{3}$   
 C.  $\frac{1}{3}$   
 D. 3
45. Find the midpoint between (8, 14) and (12, 6)
- A. (10, 10)  
 B. (20, 20)  
 C. (4, 8)  
 D. (2, 4)
46. What is the gradient of the line  $y - 3x = 6$ ?
- A. -3  
 B. 3  
 C. 6  
 D. -6
47. Find the distance between (9, 40) and (0, 0)
- A. 40  
 B. 41  
 C. 49  
 D. 9
48. The equation of a line passing through the origin with gradient 5 is
- A.  $y = 5x$   
 B.  $y = x + 5$   
 C.  $y = 5x + 1$   
 D.  $y = -5x$
49. Find the midpoint of (-6, 8) and (14, -4)
- A. (4, 2)  
 B. (8, 4)  
 C. (10, 6)  
 D. (20, 12)

50. What is the gradient of the line passing through (5, 1) and (1, 5)?
- A. 1  
B. -1  
C. 4  
D. -4
51. Find the distance between (3, 7) and (6, 11)
- A. 3  
B. 4  
C. 5  
D. 7
52. The gradient of a line parallel to  $y = -5x + 2$  is
- A. -5  
B. 5  
C. 2  
D. -2
53. Find the midpoint between (18, 24) and (6, 8)
- A. (12, 16)  
B. (24, 32)  
C. (6, 8)  
D. (3, 4)
54. What is the gradient of the line  $6y + 12x = 18$ ?
- A. -2  
B. 2  
C. 6  
D. -6
55. Find the distance between (10, 24) and (10, 4)
- A. 0  
B. 10  
C. 20  
D. 28
56. The equation of a line with gradient -3 and y-intercept 5 is
- A.  $y = -3x + 5$   
B.  $y = 3x + 5$   
C.  $y = -3x - 5$   
D.  $y = 5x - 3$
57. Find the midpoint of (25, 35) and (15, 15)
- A. (20, 25)  
B. (40, 50)  
C. (10, 20)  
D. (5, 10)
58. What is the gradient of the line passing through (0, 3) and (4, 11)?
- A. 1  
B. 2  
C. 3  
D. 4
59. Find the distance between (8, 6) and (2, -2)
- A. 6  
B. 8  
C. 10  
D. 14
60. The gradient of a line perpendicular to  $y = \frac{2}{3}x - 1$  is
- A.  $\frac{2}{3}$   
B.  $-\frac{2}{3}$   
C.  $\frac{3}{2}$   
D.  $-\frac{3}{2}$
61. Find the midpoint between (5, 13) and (11, 7)
- A. (8, 10)  
B. (16, 20)  
C. (6, 6)  
D. (3, 3)
62. What is the gradient of the line  $2y = -6x + 10$ ?
- A. -3  
B. 3  
C. -6  
D. 2
63. Find the distance between (15, 20) and (15, 8)
- A. 0  
B. 12  
C. 15  
D. 28

64. The equation of a line passing through (2, 1) with gradient 4 is
- $y = 4x - 7$
  - $y = 4x + 7$
  - $y = 4x - 1$
  - $y = 2x + 4$
65. Find the midpoint of (30, 40) and (10, 20)
- (20, 30)
  - (40, 60)
  - (15, 15)
  - (10, 10)
66. What is the gradient of the line passing through (6, 2) and (10, 10)?
- 1
  - 2
  - 4
  - 8
67. Find the distance between (5, 12) and (0, 0)
- 12
  - 13
  - 17
  - 5
68. The gradient of a line parallel to  $y = \frac{1}{4}x - 3$  is
- $\frac{1}{4}$
  - $-\frac{1}{4}$
  - 4
  - 4
69. Find the midpoint between (22, 18) and (14, 10)
- (18, 14)
  - (36, 28)
  - (8, 8)
  - (4, 4)
70. What is the gradient of the line  $3y + 9x = 12$ ?
- 3
  - 3
  - 9
  - 9
71. Find the distance between (20, 21) and (20, 5)
- 0
  - 16
  - 20
  - 26
72. The equation of a line with gradient  $\frac{3}{4}$  passing through (8, 5) is
- $y = \frac{3}{4}x - 1$
  - $y = \frac{3}{4}x + 1$
  - $y = \frac{4}{3}x - 1$
  - $y = 3x + 4$
73. Find the midpoint of (16, 22) and (8, 14)
- (12, 18)
  - (24, 36)
  - (8, 8)
  - (4, 4)
74. What is the gradient of the line passing through (7, 5) and (7, 15)?
- 0
  - 1
  - 10
  - undefined
75. Find the distance between (9, 12) and (0, 0)
- 12
  - 15
  - 21
  - 9
76. The gradient of a line perpendicular to  $y = 4x + 7$  is
- 4
  - 4
  - $\frac{1}{4}$
  - $-\frac{1}{4}$
77. Find the midpoint between (28, 36) and (12, 20)
- (20, 28)
  - (40, 56)

- C. (16, 16)  
D. (8, 8)
78. What is the gradient of the line  $y + 5x = 15$ ?  
A. -5  
B. 5  
C. 15  
D. -15
79. Find the distance between (24, 7) and (0, 0)  
A. 24  
B. 25  
C. 31  
D. 7
80. The equation of a line passing through (5, 6) with gradient -2 is  
A.  $y = -2x + 16$   
B.  $y = 2x - 4$   
C.  $y = -2x - 4$   
D.  $y = -2x + 6$
81. Find the midpoint of (35, 45) and (25, 25)  
A. (30, 35)  
B. (60, 70)  
C. (10, 20)  
D. (5, 10)
82. What is the gradient of the line passing through (1, 8) and (5, 20)?  
A. 2  
B. 3  
C. 4  
D. 12
83. Find the distance between (6, 8) and (1, -4)  
A. 11  
B. 12  
C. 13  
D. 17
84. The gradient of a line parallel to  $y = -7x + 3$  is  
A. -7  
B. 7  
C. 3  
D. -3
85. Find the midpoint between (40, 50) and (20, 30)  
A. (30, 40)  
B. (60, 80)  
C. (20, 20)  
D. (10, 10)
86. What is the gradient of the line  $4y - 8x = 20$ ?  
A. -2  
B. 2  
C. 4  
D. -4
87. Find the distance between (13, 84) and (13, 0)  
A. 0  
B. 13  
C. 84  
D. 97
88. The equation of a line with gradient 6 and y-intercept -2 is  
A.  $y = 6x - 2$   
B.  $y = -6x + 2$   
C.  $y = 6x + 2$   
D.  $y = 2x - 6$
89. Find the midpoint of (50, 60) and (30, 40)  
A. (40, 50)  
B. (80, 100)  
C. (20, 20)  
D. (10, 10)
90. What is the gradient of the line passing through (3, 10) and (9, 22)?  
A. 1  
B. 2  
C. 3  
D. 4
91. Find the distance between (11, 60) and (0, 0)  
A. 60  
B. 61  
C. 71  
D. 11
92. The gradient of a line perpendicular to  $y = -\frac{5}{2}x + 1$  is



- A.  $-\frac{5}{2}$   
 B.  $\frac{5}{2}$   
 C.  $-\frac{2}{5}$   
 D.  $\frac{2}{5}$
93. Find the midpoint between (45, 55) and (35, 35)  
 A. (40, 45)  
 B. (80, 90)  
 C. (10, 20)  
 D. (5, 10)
94. What is the gradient of the line  $7y + 14x = 21$ ?  
 A. -2  
 B. 2  
 C. 7  
 D. -7
95. Find the coordinate of the midpoint of the line joining  $P(-3, 5)$  and  $Q(5, -3)$ .  
 A. (1, 2)  
 B. (2, 1)  
 C. (1, 1)  
 D. (2, 2)
96. Find the gradient of the line joining (2, 7) and (5, 1).  
 A. 2  
 B. -2  
 C. 3  
 D. -3
97.  $P(-6, 1)$  and  $Q(6, 6)$  are the two ends of the diameter of a given circle. Calculate the radius.  
 A. 6.5 units  
 B. 13.0 units  
 C. 3.5 units  
 D. 7.0 units
98. Find the distance between the points (4, 3) and (1, -1).  
 A. 3  
 B. 4  
 C. 5  
 D. 6
99. Find the equation of the line passing through (2, 3) with gradient -2.  
 A.  $y = -2x + 7$   
 B.  $y = -2x - 7$   
 C.  $y = 2x + 7$   
 D.  $y = 2x - 7$
100. Calculate the area of a triangle with vertices at 0, 0, 5, 0 and 0, 8.  
 A. square units  
 B. square units  
 C. square units  
 D. square units

# Chapter 4

## Calculus

### 4.1 Differentiation

#### 4.1.1 Questions

- The minimum point on the curve  $y = x^2 - 6x + 5$  is at:  
A. (1,5)  
B. (2,3)  
C. (3,4)  
D. (-3,4)  
E. (3,-4)
- At what value of  $x$  is the function  $y = x^2 + x + 1$  minimum?  
A. -1  
B.  $-\frac{1}{2}$   
C.  $\frac{1}{2}$   
D. 1
- At what value of  $x$  is the function  $y = x^2 - 2x - 3$  minimum?  
A. 1  
B. -1  
C. -4  
D. 4
- Find the maximum value of  $y = -x^2 + 2x + 3$ .  
A. -4  
B. -1  
C. 1  
D. 4
- Find the maximum value of  $y = 3x^2 - x^3$ .  
A. 2  
B. 4  
C. 6  
D. 0
- Find the minimum value of  $y = x^3 - 3x + 1$ .  
A. -1  
B. 1  
C. 2  
D. -2
- Find the value of  $x$  for which the function  $f(x) = 2x^3 - x^2 - 4x + 4$  has a maximum value.  
A.  $\frac{2}{3}$   
B. 1  
C. -1  
D.  $-\frac{2}{3}$
- Find the value of  $x$  for which the function  $f(x) = 3x^3 - 9x^2$  is minimum.  
A. 2  
B. 0  
C. 5  
D. 3
- Find the maximum value of the function  $f(x) = 2 + x - x^2$ .  
A.  $\frac{9}{4}$   
B.  $\frac{7}{4}$

- C.  $\frac{3}{2}$   
D.  $\frac{1}{2}$
10. Find the maximum value of  $y$  in the equation  $y = 1 - 2x - 3x^2$ .  
A.  $\frac{4}{3}$   
B.  $\frac{5}{4}$   
C.  $\frac{3}{4}$   
D.  $\frac{5}{3}$
11. The minimum value of  $y$  in the equation  $y = x^2 - 6x + 8$  is:  
A. 8  
B. 3  
C. 0  
D. -1
12. Obtain the maximum value of the function  $f(x) = x^3 - 12x + 11$ .  
A. -5  
B. -2  
C. 2  
D. 27
13. Find the value of  $h$  if the maximum value of  $y = 1 + hx - 3x^2$  is 13.  
A. 10  
B. 11  
C. 12  
D. 13
14. A trader realizes  $10x - x^2$  naira profit from the sale of  $x$  bags of corn. How many bags will give him the maximum profit?  
A. 4  
B. 5  
C. 6  
D. 7
15. Find the value of  $x$  for which the function  $y = x^3 - x$  has a minimum value.  
A.  $\frac{\sqrt{3}}{3}$   
B.  $-\frac{\sqrt{3}}{3}$   
C.  $\sqrt{3}$   
D.  $-\sqrt{3}$
16. If  $f(x) = x^2 - 2x - 3$ , find the least value of  $f(x)$  and the corresponding value of  $x$ .  
A.  $f(x) = -3, x = 1$   
B.  $f(x) = -3, x = 3$   
C.  $f(x) = -4, x = 1$   
D.  $f(x) = 1, x = -4$
17. If  $y = 3 \cos\left(\frac{x}{3}\right)$ , find  $\frac{dy}{dx}$  when  $x = \frac{3\pi}{2}$ .  
A. -1  
B. 1  
C. 2  
D. 3
18. What is the rate of change of the volume  $v$  of a hemisphere with respect to its radius  $r$  when  $r = 2$ ? ( $V = \frac{2}{3}\pi r^3$ )  
A.  $2\pi$   
B.  $4\pi$   
C.  $8\pi$   
D.  $16\pi$
19. If  $y = (1 - 2x)^3$ , find the value of  $\frac{dy}{dx}$  at  $x = -1$ .  
A. 22  
B. 57  
C. -6  
D. -54
20. Find the derivative of  $y = \sin(2x^3 + 3x - 4)$ .  
A.  $\cos(2x^3 + 3x - 4)$   
B.  $-\cos(2x^3 + 3x - 4)$   
C.  $-(6x^2 + 3) \cos(2x^3 + 3x - 4)$   
D.  $(6x^2 + 3) \cos(2x^3 + 3x - 4)$
21. The radius  $r$  of a circular disc is increasing at the rate of 0.5 cm/sec. At what rate is the area of the disc increasing when its radius is 6 cm?  
A.  $3\pi \text{ cm}^2/\text{sec}$   
B.  $18\pi \text{ cm}^2/\text{sec}$   
C.  $6\pi \text{ cm}^2/\text{sec}$   
D.  $36\pi \text{ cm}^2/\text{sec}$
22. Find  $\frac{dy}{dx}$ , if  $y = \cos x$ .

- A.  $\sin x$   
 B.  $-\sin x$   
 C.  $\tan x$   
 D.  $-\tan x$
23. Differentiate:  $(\cos \theta - \sin \theta)^2$  with respect to  $\theta$ .  
 A.  $1 - 2 \cos 2\theta$   
 B.  $-2 \sin 2\theta$   
 C.  $-2 \cos 2\theta$   
 D.  $1 - 2 \sin 2\theta$
24. Differentiate:  $\left(x^2 - \frac{1}{x}\right)^2$  with respect to  $x$ .  
 A.  $4x^3 - 2 + \frac{2}{x^3}$   
 B.  $4x^3 - 2 - \frac{2}{x^3}$   
 C.  $4x^3 - 4x - \frac{2}{x}$   
 D.  $4x^3 - 3x + \frac{2}{x}$
25. Find the point  $(x, y)$  on the Euclidean plane where the curve  $y = 2x^2 - 2x + 3$  has 2 as the gradient.  
 A.  $(1, 3)$   
 B.  $(2, 2)$   
 C.  $(3, 4)$   
 D.  $(3, 2)$
26. For what value of  $x$  is the tangent to the curve  $y = x^2 - 4x + 3$  parallel to the  $x$ -axis?  
 A. 0  
 B. 1  
 C. 2  
 D. 3
27. Differentiate  $\frac{6x^3 - 5x^2 + 1}{3x^2}$  with respect to  $x$ .  
 A.  $2 - \frac{2}{3x^3}$   
 B.  $2 + \frac{1}{6x}$   
 C.  $2x - \frac{5}{3}$   
 D.  $2 - \frac{1}{3x^2}$
28. If  $y = (1 + x)^2$ , find  $\frac{dy}{dx}$ .  
 A.  $x + 1$   
 B.  $2x - 1$   
 C.  $2 + 2x$   
 D.  $1 + 2x$
29. Differentiate  $3x^3 + 2x^2 + 3x + 1$  with respect to  $x$ .  
 A.  $9x^2 + 4x + 3$   
 B.  $9x^2 + 4x - 3$   
 C.  $9x^2 - 4x - 3$   
 D.  $9x^2 - 4x + 3$
30. Differentiate  $\frac{2}{3}x^3 - \frac{4}{x}$ .  
 A.  $2x^2 + \frac{4}{x^2}$   
 B.  $2x^2 - \frac{4}{x}$   
 C.  $3x^2 - \frac{4}{x}$   
 D.  $3x^2 + \frac{4}{x^2}$
31. Find the derivative of  $\frac{\sin x}{\cos x}$ .  
 A.  $\tan x \cos x$   
 B.  $\csc x \sec x$   
 C.  $\sec^2 x$   
 D.  $\cot^2 x$
32. If  $y = x^2 - 3x + 4$ , find  $\frac{dy}{dx}$  at  $x = 5$ .  
 A. 9  
 B. 7  
 C. 5  
 D. 3
33. If  $y = 2x \cos 2x - \sin 2x$ , find  $\frac{dy}{dx}$  when  $x = \frac{\pi}{2}$ .  
 A. 0  
 B.  $-\pi$   
 C.  $\pi$   
 D.  $-2\pi$
34. If  $y = 3 \cos 4x$ , find  $\frac{dy}{dx}$ .  
 A.  $-24 \sin 4x$   
 B.  $12 \sin 4x$   
 C.  $-12 \sin 4x$   
 D.  $6 \sin 8x$
35. Find the derivative of  $(2 + 3x)(1 - x)$  with respect to  $x$ .

- A.  $6x - 1$   
B.  $1 - 6x$   
C.  $-3$   
D.  $6$
36. Find  $\frac{dy}{dx}$ , if  $y = -3x^3 + 2x^2 - 3x + 1$ .  
A.  $-9x^2 + 4x + 3$   
B.  $-9x^2 + 4x - 3$   
C.  $-9x^2 - 4x + 3$   
D.  $-9x^2 - 4x - 3$
37. If  $y = 2x^3 + 6x^2 + 6x + 1$ , find  $\frac{dy}{dx}$ .  
A.  $6x^2 + 12x + 1$   
B.  $6x^2 - 12x + 1$   
C.  $6x^2 + 12x + 6$   
D.  $6x^2 + 6x + 6$
38. Find the derivative of  $y = \left(\frac{1}{3}x + 6\right)^2$ .  
A.  $2\left(\frac{1}{3}x + 6\right)$   
B.  $\frac{2}{3}\left(\frac{1}{3}x + 6\right)$   
C.  $\frac{1}{3}\left(\frac{1}{3}x + 6\right)^2$   
D.  $\frac{2}{3}\left(\frac{1}{3}x + 6\right)^2$
39. If  $y = x^2 - 3x + 4$ , find  $\frac{dy}{dx}$  at  $x = 2$ .  
A.  $-1$   
B.  $1$   
C.  $2$   
D.  $-2$
40. If  $y = x^2 + \sqrt{x}$ , find  $\frac{dy}{dx}$ .  
A.  $2x - \frac{1}{2}x^{\frac{1}{2}}$   
B.  $2x - \frac{1}{2}x^{-\frac{1}{2}}$   
C.  $2x + x^{-\frac{1}{2}}$   
D.  $2x + \frac{1}{2}x^{-\frac{1}{2}}$
41. Find  $\frac{dy}{dx}$ , if  $y = \frac{2}{3}x^3 - \frac{4}{x}$ .  
A.  $3x^2 - \frac{4}{x}$   
B.  $3x^2 + \frac{4}{x^2}$   
C.  $2x^2 - \frac{4}{x}$   
D.  $2x^2 + \frac{4}{x^2}$
42. If  $y = \cos 3x$ , find  $\frac{dy}{dx}$ .  
A.  $\frac{1}{3} \sin 3x$   
B.  $3 \sin 3x$   
C.  $-\frac{1}{3} \sin 3x$   
D.  $-3 \sin 3x$
43. Find  $\frac{dy}{dx}$ , if  $y = \cos x$ .  
A.  $\sin x$   
B.  $-\sin x$   
C.  $\tan x$   
D.  $-\tan x$
44. Find the slope of the curve  $y = 2x^2 + 5x - 3$  at  $(1, 4)$ .  
A.  $4$   
B.  $6$   
C.  $7$   
D.  $9$
45. Find the derivative of  $y = \sin^2(5x)$  with respect to  $x$ .  
A.  $5 \sin 5x \cos 5x$   
B.  $2 \sin 5x \cos 5x$   
C.  $15 \sin 5x \cos 5x$   
D.  $10 \sin 5x \cos 5x$
46. The slope of the tangent to the curve  $y = 3x^2 - 2x + 5$  at the point  $(1, 6)$  is:  
A.  $1$   
B.  $4$   
C.  $5$   
D.  $6$
47. If the gradient of the curve  $y = 2kx^2 + x + 1$  at  $x = 1$  is  $9$ , find the value of  $k$ .  
A.  $2$   
B.  $-2$   
C.  $4$   
D.  $-4$

48. The distance travelled by a particle from a fixed point is given as  $s = (t^3 - t^2 - t + 5)$  cm. Find the minimum distance that the particle can cover from the fixed point (for  $t \geq 0$ ).
- 2.3 cm
  - 4.0 cm
  - 5.2 cm
  - 6.0 cm
49. Differentiate  $(2x + 5)^2(x - 4)$  with respect to  $x$ .
- $4(2x + 5)(x - 4)$
  - $4(2x + 5)(4x - 3)$
  - $(2x + 5)(6x - 11)$
  - $(2x + 5)(2x - 13)$
50. Find the rate of change of the volume  $v$  of a sphere with respect to its radius  $r$  when  $r = 1$ . ( $V = \frac{4}{3}\pi r^3$ )
- $24\pi$
  - $12\pi$
  - $4\pi$
  - $8\pi$
51. If  $y = 2x \cos 2x - \sin 2x$ , find  $\frac{dy}{dx}$  when  $x = \frac{\pi}{4}$ .
- $\frac{\pi}{4}$
  - $\frac{\pi}{2}$
  - $-\pi$
  - $-\frac{\pi}{2}$
52. Differentiate  $\frac{x}{\cos x}$  with respect to  $x$ .
- $1 + \sec^2 x$
  - $1 + x \tan x \sec x$
  - $\cos x + x \tan x$
  - $\sec x + x \tan x \sec x$
53. If  $y = 243(4x + 5)^{-2}$ , find  $\frac{dy}{dx}$  when  $x = 1$ .
- $-\frac{8}{9}$
  - $\frac{9}{8}$
  - $-\frac{8}{3}$
  - $\frac{3}{8}$
54. What is the derivative of  $t^2 \sin(3t - 5)$  with respect to the variable  $t$ ?
- $2t \sin(3t - 5) + 3t^2 \cos(3t - 5)$
  - $2t \sin(3t - 5) - 3t^2 \cos(3t - 5)$
  - $6t \cos(3t - 5)$
  - $2t \sin(3t - 5) + t^2 \cos(3t)$
55. A circle with radius 5 cm has its radius increasing at the rate of 0.2 cm/s. What will be the corresponding increase in area?
- $\pi$
  - $2\pi$
  - $4\pi$
  - $5\pi$
56. Find the dimensions of the rectangle of greatest area which has a fixed perimeter  $p$ .
- Square of sides  $\frac{p}{2}$
  - Square of sides  $p$
  - Square of sides  $\frac{p}{4}$
  - Square of sides  $2p$
57. The gradient of a curve is  $2x + 7$  and the curve passes through the point  $(2, 0)$ . Find the equation of the curve.
- $y = x^2 + 7x - 18$
  - $y = x^2 + 7x + 18$
  - $y = x^2 + 7x - 9$
  - $y = x^2 + 7x + 9$
58. Differentiate  $y = \sqrt[3]{x^2}(2x - x^2)$ .
- $\frac{10x^{\frac{5}{3}}}{3} - \frac{8x^{\frac{5}{3}}}{3}$
  - $\frac{10x^{\frac{2}{3}}}{3} - \frac{8x^{\frac{5}{3}}}{3}$
  - $\frac{10x^{\frac{5}{3}}}{3} - \frac{8x^{\frac{2}{3}}}{3}$
  - $\frac{10x^{\frac{2}{3}}}{3} - \frac{8x^{\frac{2}{3}}}{3}$
59. The slope of the tangent to the curve  $y = 5x^2 - 3x + 5$  at the point  $(1, 6)$  is:
- 19
  - 7
  - 4
  - 3
60. Find the derivative of the function  $y = 2x^2(2x - 1)$  at the point  $x = -1$ .

- A. 18  
B. -4  
C. 16  
D. -6
61. Find the derivative of  $y = \ln(4x^3 - 2x)$  (assuming natural logarithm).
- A.  $\frac{4x^2 - 2}{7x + 6}$   
B.  $\frac{12x - 2}{4x^2}$   
C.  $\frac{43x^2 - 2x}{7x}$   
D.  $\frac{12x^2 - 2}{4x^3 - 2x}$
62. Find the derivative of  $y = e^x \sin x$ .
- A.  $e^x(\sin x + \cos x)$   
B.  $e^x(\sin x - \cos x)$   
C.  $e^x \cos x$   
D.  $xe^x \sin x$
63. Find the second derivative of  $y = 8x^3 - 3x^2 + 7x - 1$ .
- A.  $11x^2 + 6x - 7$   
B.  $24x^2 - 6x + 7$   
C.  $48x - 6$   
D.  $32x + 7$
64. For what value of  $x$  is the tangent to the curve  $y = x^2 + 6x + 8$  parallel to the  $x$ -axis?
- A. -3  
B. 3  
C. 4  
D. -4
65. Find the second derivative of  $y = x \sin(x)$ .
- A.  $2 \cos(x) - x \sin(x)$   
B.  $\sin(x) - x \cos(x)$   
C.  $\sin(x) + x \cos(x)$   
D.  $x \sin(x) - 2 \cos(x)$
66. Differentiate  $\frac{2x}{\sin(x)}$  with respect to  $x$ .
- A.  $2 \cot x \sec x(1 + \tan x)$   
B.  $2 \csc x - x \cot x$   
C.  $2x \csc x + \tan x$   
D.  $2 \csc x(1 - x \cot x)$
67. Find the point  $(x, y)$  on the Euclidean plane where the curve  $y = 2x^2 - 2x + 3$  has 2 as gradient.
- A. (1, 3)  
B. (2, 7)  
C. (3, 15)  
D. (0, 3)
68. Find the equation of the tangent at the point (2, 0) to the curve  $y = x^2 - 2x$ .
- A.  $y = 2x - 4$   
B.  $y = 2x + 4$   
C.  $y = 2x + 2$   
D.  $y = 2x - 2$
69. Differentiate  $y = 20x^{-4} + 9$ .
- A.  $-80x^{-5}$   
B.  $-80x^5$   
C.  $80x^{-5}$   
D.  $80x^5$
70. Differentiate  $y = x^2 \ln x$ .
- A.  $x(2 \ln x + 1)$   
B.  $2x \ln x$   
C.  $x + \ln x$   
D.  $2x + 1/x$
71. If  $f(x) = 3x^3 + 4x^2 + x - 8$ , what is the value of  $f(-2)$ ?
- A. -24  
B. 30  
C. -18  
D. -50
72. Find the derivative of  $y = \sqrt{1 - x^2}$ .
- A.  $\frac{x}{\sqrt{1 - x^2}}$   
B.  $\frac{-x}{\sqrt{1 - x^2}}$   
C.  $\frac{1}{2\sqrt{1 - x^2}}$   
D.  $\frac{-1}{\sqrt{1 - x^2}}$
73. If  $y = \arctan(x)$ , find  $\frac{dy}{dx}$ .
- A.  $\frac{1}{1 + x^2}$   
B.  $\frac{-1}{1 + x^2}$

- C.  $\sec^2 x$   
 D.  $\frac{1}{\sqrt{1-x^2}}$
74. Differentiate  $y = \frac{e^x}{x}$  with respect to  $x$ .  
 A.  $\frac{e^x(x-1)}{x^2}$   
 B.  $\frac{e^x(x+1)}{x^2}$   
 C.  $e^x$   
 D.  $\frac{e^x}{x^2}$
75. The slope of the normal to the curve  $y = x^2 - 5x + 2$  at  $x = 1$  is:  
 A.  $-3$   
 B.  $1/3$   
 C.  $3$   
 D.  $-1/3$
76. Find  $\frac{dy}{dx}$  if  $y = (x^2 + 1)^3$ .  
 A.  $3x(x^2 + 1)^2$   
 B.  $6x(x^2 + 1)^2$   
 C.  $2x(x^2 + 1)^3$   
 D.  $(x^2 + 1)^2$
77. Given  $f(x) = \frac{1}{x}$ , find  $f''(x)$ .  
 A.  $-\frac{1}{x^2}$   
 B.  $\frac{1}{x^3}$   
 C.  $\frac{2}{x^3}$   
 D.  $-\frac{2}{x^3}$
78. A function  $f(x) = x^3 - 6x^2 + 5$ . Find the interval where the function is decreasing.  
 A.  $x < 0$  or  $x > 4$   
 B.  $0 < x < 4$   
 C.  $x < 2$  or  $x > 6$   
 D.  $2 < x < 6$
79. Find the derivative of  $y = \sin(\sqrt{x})$ .  
 A.  $\frac{\cos(\sqrt{x})}{2\sqrt{x}}$   
 B.  $\cos(\sqrt{x})$   
 C.  $2\sqrt{x} \cos(\sqrt{x})$   
 D.  $\frac{-\cos(\sqrt{x})}{2\sqrt{x}}$
80. If  $y = \sec x$ , find  $\frac{dy}{dx}$ .  
 A.  $\tan^2 x$   
 B.  $\sec x \tan x$   
 C.  $-\sec x \tan x$   
 D.  $\csc x \cot x$
81. Find the gradient of the curve  $y = \ln(x^2)$  at  $x = 2$ .  
 A.  $1/2$   
 B.  $1$   
 C.  $2$   
 D.  $\ln 4$
82. The position of a particle is given by  $s(t) = t^3 - 3t^2 + 3t + 7$ . What is its acceleration when velocity is zero?  
 A.  $0$   
 B.  $6$   
 C.  $-6$   
 D.  $1$
83. Differentiate  $y = 5^{2x}$ .  
 A.  $5^{2x} \ln 5$   
 B.  $2 \cdot 5^{2x} \ln 5$   
 C.  $2x \cdot 5^{2x-1}$   
 D.  $2 \cdot 5^{2x}$
84. Find the critical points of  $f(x) = x + \frac{1}{x}$ .  
 A.  $x = 0, x = 1$   
 B.  $x = 1, x = -1$   
 C.  $x = 0$  only  
 D.  $x = 1$  only
85. If  $y = \cos^2(3x)$ , find  $\frac{dy}{dx}$ .  
 A.  $-3 \sin(6x)$   
 B.  $6 \cos(3x) \sin(3x)$   
 C.  $-2 \sin(3x)$   
 D.  $-6 \sin(3x)$
86. The derivative of  $y = \arcsin(2x)$  is:  
 A.  $\frac{1}{\sqrt{1-4x^2}}$   
 B.  $\frac{2}{\sqrt{1-4x^2}}$



- C.  $\frac{2}{\sqrt{1-x^2}}$   
 D.  $\frac{1}{1+4x^2}$
87. Find the equation of the tangent to  $y = e^x$  at  $x = 0$ .
- A.  $y = x + 1$   
 B.  $y = x - 1$   
 C.  $y = x$   
 D.  $y = ex$
88. If  $f(x) = (x + 1)^2(x - 1)$ , find  $f'(0)$ .
- A.  $-1$   
 B.  $1$   
 C.  $0$   
 D.  $2$
89. Differentiate  $y = \log_{10}(x)$ .
- A.  $\frac{1}{x}$   
 B.  $\frac{\ln 10}{x}$   
 C.  $\frac{1}{x \ln 10}$   
 D.  $\frac{x}{\ln 10}$
90. For the curve  $y = x^2 e^{-x}$ , find the  $x$ -coordinates of the turning points.
- A.  $(0, -2)$   
 B.  $(0, 2)$   
 C.  $(1, 2)$   
 D.  $(-1, 0)$
91. If  $y = \frac{\sin x}{1 + \cos x}$ , find  $\frac{dy}{dx}$ .
- A.  $\frac{1}{1 + \cos x}$   
 B.  $\frac{\cos x}{(1 + \cos x)^2}$   
 C.  $\frac{1}{(1 + \cos x)^2}$   
 D.  $\frac{-\sin x}{(1 + \cos x)^2}$
92. Find the derivative of  $y = \sqrt{x^2 + a^2}$ , where  $a$  is a constant.
- A.  $\frac{x}{\sqrt{x^2 + a^2}}$   
 B.  $\frac{1}{2\sqrt{x^2 + a^2}}$   
 C.  $\frac{2x}{\sqrt{x^2 + a^2}}$   
 D.  $\frac{ax}{\sqrt{x^2 + a^2}}$
93. The minimum value of  $f(x) = x^2 + \frac{16}{x}$  for  $x > 0$  is:
- A.  $8$   
 B.  $12$   
 C.  $16$   
 D.  $4$
94. Differentiate  $y = x^x$  with respect to  $x$ .
- A.  $xx^{x-1}$   
 B.  $x^x \ln x$   
 C.  $x^x(1 + \ln x)$   
 D.  $x^x$
95. If  $y = \frac{1}{x^n}$ , find  $\frac{dy}{dx}$ .
- A.  $\frac{n}{x^{n+1}}$   
 B.  $\frac{-n}{x^{n-1}}$   
 C.  $\frac{-n}{x^{n+1}}$   
 D.  $nx^{n-1}$
96. What is the slope of the tangent to the curve  $y = \sqrt{x}$  at  $x = 4$ ?
- A.  $1/4$   
 B.  $1/2$   
 C.  $2$   
 D.  $4$
97. Find the second derivative of  $y = \ln(x)$ .
- A.  $1/x^2$   
 B.  $-1/x^2$   
 C.  $1/x$   
 D.  $-1/x$
98. If the radius of a sphere is increasing at  $2 \text{ cm/s}$ , find the rate of increase of its volume when the radius is  $3 \text{ cm}$ . ( $V = \frac{4}{3}\pi r^3$ )
- A.  $24\pi \text{ cm}^3/\text{s}$   
 B.  $36\pi \text{ cm}^3/\text{s}$   
 C.  $72\pi \text{ cm}^3/\text{s}$   
 D.  $12\pi \text{ cm}^3/\text{s}$

99. The function  $y = |x - 2|$  is not differentiable at:

- A.  $x = 0$
- B.  $x = 1$
- C.  $x = 2$
- D. All points

100. Differentiate  $y = \tan(3x + 2)$  with respect to  $x$ .

- A.  $3 \sec^2(3x + 2)$
- B.  $\sec^2(3x + 2)$
- C.  $3 \cot(3x + 2)$
- D.  $-3 \sec^2(3x + 2)$

## 4.2 Integration

### 4.2.1 Questions

1. Find the integral of  $y = 3x^2 - 2x - 1$  with respect to  $x$ .

- A.  $x^3 - x^2 - x + C$
- B.  $x^3 + x^2 - x + C$
- C.  $x^3 + x^2 + x + C$
- D.  $x^3 - x^2 + x + C$

2. Integrate the expression  $6x^2 - 2x + 1$  with respect to  $x$ .

- A.  $3x^3 - 2x^2 + x + c$
- B.  $2x^3 - x^2 + x + c$
- C.  $2x^3 - 3x^2 + c$
- D.  $x^3 + x^2 - x + c$

3. Integrate  $x^{-2} + \cos x$  with respect to  $x$ .

- A.  $\frac{1}{x} + \sin x + k$
- B.  $-\frac{1}{x} + \sin x + k$
- C.  $-\frac{1}{x} - \sin x + k$
- D.  $\ln |x| + \sin x + k$

4. The expression  $ax^2 + bx + c$  equals 5 at  $x = 1$ . If its derivative is  $2x + 1$ , what are the values of  $a$ ,  $b$ ,  $c$  respectively?

- A. 1, 1, 3
- B. 1, 3, 1
- C. 1, 2, 1
- D. 2, 1, 1

5. Integrate the expression  $(2x + 1)^3$  with respect to  $x$ .

- A.  $\frac{(2x + 1)^3}{8} + k$
- B.  $\frac{(2x + 1)^4}{8} + k$
- C.  $\frac{(2x + 1)^4}{6} + k$

D.  $\frac{(2x + 1)^2}{8} + k$

6. Evaluate  $\int (4x^{-3} - 7x^2 + 5x - 6) dx$ .

- A.  $-2x^{-2} - \frac{7}{3}x^3 + \frac{5}{2}x^2 - 6x + C$
- B.  $2x^2 + \frac{7}{3}x^3 + 5x^2 - 6 + C$
- C.  $12x^2 + 14x - 5 + C$
- D.  $-12x^{-4} - 14x + 5 + C$

7. Evaluate  $\int_{-1}^2 (2x^2 + x) dx$ .

- A.  $4\frac{1}{2}$
- B.  $3\frac{1}{2}$
- C.  $7\frac{1}{2}$
- D.  $5\frac{1}{4}$

8. Integrate  $\frac{x^2 - \sqrt{x}}{x}$  with respect to  $x$ .

- A.  $\frac{x^2}{2} - 2\sqrt{x} + k$
- B.  $\frac{2(x^2 - x)}{3x} + k$
- C.  $\frac{x^2}{2} - \sqrt{x} + k$
- D.  $\frac{x^2 - x}{3x} + k$

9. Evaluate  $\int_{-1}^1 (2x + 1)^2 dx$ .

- A.  $3\frac{2}{3}$
- B. 4
- C.  $4\frac{1}{3}$
- D.  $4\frac{2}{3}$

10. Evaluate  $\int (\cos 4x + \sin 3x) dx$ .

- A.  $\sin 4x - \cos 3x + k$   
B.  $\sin 4x + \cos 3x + k$   
C.  $\frac{1}{4}\sin 4x - \frac{1}{3}\cos 3x + k$   
D.  $\frac{1}{4}\sin 4x + \frac{1}{3}\cos 3x + k$
11. Evaluate  $\int_0^{\frac{\pi}{2}} \sin x \, dx$ .  
A. -2  
B. -1  
C. 1  
D. 2
12. Evaluate  $\int_1^2 \frac{5}{x} \, dx$ .  
A. 1.47  
B. 2.67  
C. 3.23  
D. 3.47
13. Evaluate the integral  $\int_{\frac{\pi}{12}}^{\frac{\pi}{4}} 2 \cos 2x \, dx$ .  
A.  $-\frac{1}{2}$   
B. -1  
C.  $\frac{1}{2}$   
D. 1
14. Evaluate  $\int (2x + 3)^{\frac{1}{2}} \, dx$ .  
A.  $\frac{1}{12}(2x + 3)^6 + k$   
B.  $\frac{1}{3}(2x + 3)^{\frac{1}{2}} + k$   
C.  $\frac{1}{3}(2x + 3)^{\frac{3}{2}} + k$   
D.  $\frac{1}{12}(2x + 3)^{\frac{3}{4}} + k$
15. Evaluate  $\int (\sin x - 5x^2) \, dx$ .  
A.  $-\cos x - 10x + k$   
B.  $\cos x - \frac{5x^3}{3} + k$   
C.  $-\cos x - \frac{5x^3}{3} + k$   
D.  $\cos x - 10x + k$
16. Evaluate  $\int \sin 2x \, dx$ .  
A.  $\cos 2x + k$   
B.  $\frac{1}{2}\cos 2x + k$   
C.  $-\frac{1}{2}\cos 2x + k$   
D.  $-\cos 2x + k$
17. If  $y = x(x^4 + x + 1)$ , evaluate  $\int_0^1 y \, dx$ .  
A.  $\frac{11}{12}$   
B. 1  
C.  $\frac{5}{6}$   
D. 0
18. Evaluate  $\int_2^{\pi} (\sec^2 x - \tan^2 x) \, dx$ .  
A.  $\frac{\pi}{2}$   
B.  $\frac{\pi}{3}$   
C.  $\pi - 2$   
D.  $\pi + 2$
19. Evaluate  $\int_0^{\frac{\pi}{4}} (\sin x - \cos x) \, dx$ .  
A.  $\sqrt{2} + 1$   
B.  $\sqrt{2} - 1$   
C.  $1 - \sqrt{2}$   
D.  $-\sqrt{2} - 1$
20. Evaluate  $\int_{-2}^1 (x - 1)^2 \, dx$ .  
A.  $-\frac{10}{3}$   
B. 7  
C. 9  
D. 11
21. A function  $f(x)$  passes through the origin and its first derivative is  $3x + 2$ . What is  $f(x)$ ?  
A.  $f(x) = \frac{3x^2}{2} + 2x$   
B.  $f(x) = \frac{3x^2}{2} + x$   
C.  $f(x) = 3x^2 + \frac{x}{2}$

D.  $f(x) = 3x^2 + 2x$

22. Evaluate  $\int_2^3 (x^2 - 2x) \, dx$ .

A. 4

B. 2

C.  $\frac{4}{3}$

D.  $\frac{1}{3}$

23. Evaluate  $\int_{-4}^0 (1 - 2x) \, dx$ .

A. -20

B. -16

C. 10

D. 20

24. Evaluate  $\int_1^2 (6x^2 - 2x) \, dx$ .

A. 11

B. 12

C. 13

D. 16

25. Evaluate  $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos x \, dx$ .

A. 0

B. 1

C. 2

D. 3

26. Evaluate  $\int_0^2 (x^3 + x^2) \, dx$ .

A.  $4\frac{5}{6}$

B.  $6\frac{2}{3}$

C.  $1\frac{5}{6}$

D.  $2\frac{5}{6}$

27. Evaluate  $\int_1^2 2 \, dx$ .

A. 3

B. 5

C. 2

D. 6

28. Evaluate  $\int_1^2 (x^2 - 4x) \, dx$ .

A.  $\frac{11}{3}$

B.  $\frac{3}{11}$

C.  $-\frac{3}{11}$

D.  $-\frac{11}{3}$

29. Evaluate  $\int (\sin x + 2) \, dx$ .

A.  $\cos x + x^2 + k$

B.  $\cos x + 2x + k$

C.  $-\cos x + x^2 + k$

D.  $-\cos x + 2x + k$

30. Evaluate  $\int \cos 4x \, dx$ .

A.  $\frac{3}{4} \sin 4x + k$

B.  $-\frac{1}{4} \sin 4x + k$

C.  $-\frac{3}{4} \sin 4x + k$

D.  $\frac{1}{4} \sin 4x + k$

31. Integrate  $\frac{1+x}{x^3}$  with respect to  $x$ .

A.  $2x^2 - \frac{1}{x} + k$

B.  $x^2 - \frac{1}{x} + k$

C.  $-\frac{x^2}{2} - \frac{1}{x} + k$

D.  $-\frac{1}{2x^2} - \frac{1}{x} + k$

32. Evaluate  $\int (x^2 + 3x - 5) \, dx$ .

A.  $\frac{x^3}{3} - \frac{3x^2}{2} - 5x + k$

B.  $\frac{x^3}{3} - \frac{3x^2}{2} + 5x + k$

C.  $\frac{x^3}{3} + \frac{3x^2}{2} - 5x + k$

D.  $\frac{x^3}{3} + \frac{3x^2}{2} + 5x + k$

33. Integrate  $\frac{2x^3 + 2x}{x}$  with respect to  $x$ .
- A.  $\frac{2x^3}{3} - 2x + k$   
 B.  $\frac{2x^3}{3} + 2x + k$   
 C.  $x^3 - 2x + k$   
 D.  $x^3 + 2x + k$
34. Evaluate  $\int (5x^3 + 7x^2 - 2x + 5) dx$ .
- A.  $\frac{5x^4}{4} + \frac{7x^3}{3} + 2x + C$   
 B.  $\frac{5x^4}{4} + \frac{7x^3}{3} - x^2 + 5x + C$   
 C.  $\frac{5x^3}{3} + \frac{7x^2}{2} - x + C$   
 D.  $\frac{2x^2}{3} + \frac{x}{5} - C$
35. Find the value of  $\int_0^\pi \frac{\cos^2 \theta - 1}{\sin^2 \theta} d\theta$ .
- A.  $\pi$   
 B.  $-\pi$   
 C.  $\frac{\pi}{2}$   
 D.  $-\frac{\pi}{2}$
36. The area enclosed by  $y = x^2 - 1$ ,  $y = 3$ , and  $x \geq 0$  is revolved around the  $y$ -axis. If the volume is  $K\pi$ , find  $K$ .
- A. 7  
 B.  $\frac{15}{2}$   
 C. 8  
 D.  $\frac{17}{2}$
37. Evaluate  $\int (2x - 5)^4 dx$ .
- A.  $\frac{(2x - 5)^5}{5} + C$   
 B.  $\frac{(2x - 5)^5}{10} + C$   
 C.  $8(2x - 5)^3 + C$   
 D.  $\frac{(2x - 5)^3}{6} + C$
38. Find  $\int e^{3x} dx$ .
- A.  $3e^{3x} + C$   
 B.  $e^{3x} + C$   
 C.  $\frac{1}{3}e^{3x} + C$   
 D.  $\frac{1}{3}e^x + C$
39. Evaluate  $\int_0^1 (x^2 - x + 1) dx$ .
- A.  $\frac{1}{6}$   
 B.  $\frac{5}{6}$   
 C. 1  
 D.  $\frac{7}{6}$
40. Find  $\int \sec^2(3x) dx$ .
- A.  $\tan(3x) + C$   
 B.  $\frac{1}{3} \tan(3x) + C$   
 C.  $3 \tan(3x) + C$   
 D.  $\sec(3x) \tan(3x) + C$
41. Evaluate  $\int_1^e \frac{1}{x} dx$ .
- A. 0  
 B. 1  
 C.  $e$   
 D.  $e - 1$
42. Find the area under the curve  $y = x^2$  from  $x = 0$  to  $x = 3$ .
- A. 3  
 B. 6  
 C. 9  
 D. 27
43. Evaluate  $\int \frac{2}{x+1} dx$ .
- A.  $2 \ln |x + 1| + C$   
 B.  $\ln |x + 1| + C$   
 C.  $\frac{-2}{(x+1)^2} + C$   
 D.  $2 \arctan(x) + C$
44. If  $\frac{dy}{dx} = 2x - 3$  and  $y = 2$  when  $x = 1$ , find  $y$  in terms of  $x$ .

- A.  $y = x^2 - 3x + 2$   
 B.  $y = x^2 - 3x + 4$   
 C.  $y = 2x^2 - 3x + 3$   
 D.  $y = x^2 - 3x$
45. Evaluate  $\int_0^{\pi} \cos x dx$ .  
 A. 0  
 B. 1  
 C. -1  
 D. 2
46. Find  $\int (3 - 4x)^{-2} dx$ .  
 A.  $\frac{(3 - 4x)^{-1}}{-4} + C$   
 B.  $\frac{(3 - 4x)^{-1}}{4} + C$   
 C.  $\frac{(3 - 4x)^{-3}}{-12} + C$   
 D.  $-4(3 - 4x)^{-3} + C$
47. What is the area bounded by the curve  $y = 4 - x^2$  and the x-axis?  
 A.  $\frac{8}{3}$   
 B.  $\frac{16}{3}$   
 C.  $\frac{32}{3}$   
 D. 16
48. Evaluate  $\int_0^2 (3x^2 + 4x - 5) dx$ .  
 A. 2  
 B. 4  
 C. 6  
 D. 8
49. Find  $\int (x + 1)(x - 2) dx$ .  
 A.  $\frac{x^3}{3} - \frac{x^2}{2} - 2x + C$   
 B.  $\frac{x^3}{3} + \frac{x^2}{2} - 2x + C$   
 C.  $x^2 - x - 2 + C$   
 D.  $\frac{(x + 1)^2(x - 2)^2}{4} + C$
50. Evaluate  $\int_1^4 \sqrt{x} dx$ .
- A.  $\frac{7}{3}$   
 B.  $\frac{14}{3}$   
 C. 2  
 D. 3
51. The gradient of a curve is given by  $4x + 3$ . If the curve passes through the point  $(1, 5)$ , find its equation.  
 A.  $y = 2x^2 + 3x$   
 B.  $y = 2x^2 + 3x + 5$   
 C.  $y = 2x^2 + 3x - 0$   
 D.  $y = 4x^2 + 3x - 2$
52. Evaluate  $\int e^{-x/2} dx$ .  
 A.  $-2e^{-x/2} + C$   
 B.  $-\frac{1}{2}e^{-x/2} + C$   
 C.  $2e^{-x/2} + C$   
 D.  $e^{-x/2} + C$
53. Find the area enclosed by the curve  $y = x^3$ , the x-axis, and the lines  $x = 1$  and  $x = 2$ .  
 A.  $\frac{7}{4}$   
 B.  $\frac{15}{4}$   
 C. 4  
 D. 7
54. Evaluate  $\int_0^{\pi/6} \sec x \tan x dx$ .  
 A.  $\frac{2\sqrt{3}}{3} - 1$   
 B.  $1 - \frac{2\sqrt{3}}{3}$   
 C.  $\frac{\sqrt{3}}{3}$   
 D.  $2 - \sqrt{3}$
55. If  $\int_0^a (2x + 1) dx = 4$ , find the positive value of  $a$ .  
 A. 1  
 B.  $\frac{3}{2}$   
 C. 2  
 D. 3
56. Find  $\int \frac{x^2 + 1}{x^2} dx$ .

- A.  $x - \frac{1}{x} + C$   
B.  $x + \frac{1}{x} + C$   
C.  $1 - \frac{2}{x^3} + C$   
D.  $2x + C$
57. Evaluate  $\int (1-x)^3 dx$ .  
A.  $\frac{(1-x)^4}{4} + C$   
B.  $-\frac{(1-x)^4}{4} + C$   
C.  $-3(1-x)^2 + C$   
D.  $3(1-x)^2 + C$
58. The area bounded by the curve  $y = x$ , the  $x$ -axis,  $x = 0$  and  $x = 2$  is revolved around the  $x$ -axis. Find the volume of the solid generated.  
A.  $\frac{2\pi}{3}$   
B.  $\frac{4\pi}{3}$   
C.  $\frac{8\pi}{3}$   
D.  $4\pi$
59. Evaluate  $\int_0^{\pi/3} \sin(3x) dx$ .  
A. 0  
B.  $\frac{1}{3}$   
C.  $\frac{2}{3}$   
D. 1
60. Evaluate  $\int (x^2 + 1)^2 dx$ .  
A.  $\frac{x^5}{5} + \frac{2x^3}{3} + x + C$   
B.  $\frac{(x^2 + 1)^3}{3} + C$   
C.  $\frac{x^5}{5} + x^3 + x + C$   
D.  $\frac{(x^2 + 1)^3}{6x} + C$
61. If  $\int_1^k \frac{1}{x^2} dx = \frac{1}{2}$ , find the value of  $k$ .  
A. 1  
B. 2  
C.  $\frac{1}{2}$   
D. 4
62. Find the indefinite integral of  $\sec^2 x e^{\tan x}$ .  
A.  $e^{\tan x} + C$   
B.  $\tan x e^{\tan x} + C$   
C.  $\sec x e^{\tan x} + C$   
D.  $e^{\sec^2 x} + C$
63. Evaluate  $\int \frac{\ln x}{x} dx$ .  
A.  $\ln |\ln x| + C$   
B.  $(\ln x)^2 + C$   
C.  $\frac{1}{2}(\ln x)^2 + C$   
D.  $\frac{1}{x^2} + C$
64. The area of the region bounded by  $y = e^x$ , the  $x$ -axis,  $x = 0$  and  $x = 1$  is:  
A.  $e$   
B.  $e - 1$   
C.  $1 - e$   
D. 1
65. Evaluate  $\int 2^x dx$ .  
A.  $2^x + C$   
B.  $\frac{2^x}{\ln 2} + C$   
C.  $2^x \ln 2 + C$   
D.  $x2^{x-1} + C$
66. Evaluate  $\int_0^1 (e^x + e^{-x}) dx$ .  
A.  $e - \frac{1}{e}$   
B.  $e + \frac{1}{e}$   
C.  $e - \frac{1}{e} - 2$   
D. 0
67. Find  $\int \frac{1}{2x+3} dx$ .  
A.  $\ln |2x+3| + C$   
B.  $2 \ln |2x+3| + C$   
C.  $\frac{1}{2} \ln |2x+3| + C$   
D.  $\frac{-1}{(2x+3)^2} + C$

68. Find the area bounded by  $y = \sin x$ , the  $x$ -axis, from  $x = 0$  to  $x = \pi$ .
- A. 0  
B. 1  
C. 2  
D.  $\pi$
69. Evaluate  $\int x e^{x^2} dx$ .
- A.  $e^{x^2} + C$   
B.  $x^2 e^{x^2} + C$   
C.  $\frac{1}{2} e^{x^2} + C$   
D.  $2e^{x^2} + C$
70. Evaluate  $\int_0^{\pi/4} \tan x \sec^2 x dx$ .
- A.  $\frac{1}{4}$   
B.  $\frac{1}{2}$   
C. 1  
D. 2
71. Find  $\int \cos^2 x dx$  (Hint:  $\cos 2x = 2 \cos^2 x - 1$ )
- A.  $\frac{x}{2} + \frac{\sin 2x}{4} + C$   
B.  $\frac{x}{2} - \frac{\sin 2x}{4} + C$   
C.  $x + \sin 2x + C$   
D.  $\frac{\cos^3 x}{3} + C$
72. If  $\int_0^b x dx = 8$ , find  $b > 0$ .
- A. 2  
B. 4  
C. 8  
D. 16
73. Evaluate  $\int \frac{1}{\sqrt{1-x^2}} dx$ .
- A.  $\arcsin x + C$   
B.  $\arccos x + C$   
C.  $\ln |\sqrt{1-x^2}| + C$   
D.  $2\sqrt{1-x^2} + C$
74. The volume generated by revolving the area under  $y = \sqrt{x}$  from  $x = 0$  to  $x = 4$  about the  $x$ -axis is:
- A.  $4\pi$   
B.  $8\pi$   
C.  $16\pi$   
D.  $\frac{8\pi}{3}$
75. Evaluate  $\int_{-1}^1 x^3 dx$ .
- A. 0  
B.  $\frac{1}{4}$   
C.  $\frac{1}{2}$   
D. 1
76. Find  $\int \frac{e^x}{1+e^x} dx$ .
- A.  $e^x \ln |1+e^x| + C$   
B.  $\ln(1+e^x) + C$   
C.  $\frac{e^{2x}}{2+e^x} + C$   
D.  $\arctan(e^x) + C$
77. Evaluate  $\int_1^2 (x + \frac{1}{x})^2 dx$ .
- A.  $\frac{29}{6}$   
B.  $\frac{17}{3}$   
C. 5  
D.  $\frac{10}{3}$
78. If  $\frac{dy}{dx} = \sin x + x$  and  $y(0) = 1$ , find  $y$ .
- A.  $y = \cos x + \frac{x^2}{2}$   
B.  $y = -\cos x + \frac{x^2}{2} + 1$   
C.  $y = -\cos x + \frac{x^2}{2} + 2$   
D.  $y = \cos x + \frac{x^2}{2} + 1$
79. Evaluate  $\int 5 dx$ .
- A.  $5 + C$   
B.  $5x + C$   
C.  $\frac{x^2}{2} + 5x + C$   
D.  $C$



80. Evaluate  $\int_0^2 |x - 1| dx$ .
- A. 0  
B.  $\frac{1}{2}$   
C. 1  
D. 2
81. Find  $\int \frac{1}{x \ln x} dx$ .
- A.  $(\ln x)^2 + C$   
B.  $\ln |\ln x| + C$   
C.  $\frac{1}{(\ln x)^2} + C$   
D.  $\ln x^2 + C$
82. The area bounded by  $y = 2x$ , the x-axis,  $x = 1$  and  $x = 3$  is:
- A. 4  
B. 6  
C. 8  
D. 10
83. Evaluate  $\int \sin^2 x \cos x dx$ .
- A.  $\frac{\sin^3 x}{3} + C$   
B.  $\frac{\cos^3 x}{3} + C$   
C.  $\sin x \cos x + C$   
D.  $2 \sin x \cos x + C$
84.  $\int_e^{e^2} \frac{dx}{x \ln x}$ .
- A. 1  
B.  $\ln 2$   
C. 2  
D.  $e$
85. Find  $\int (x + 1)^5 dx$ .
- A.  $5(x + 1)^4 + C$   
B.  $\frac{(x + 1)^6}{6} + C$   
C.  $(x + 1)^6 + C$   
D.  $\frac{x^6}{6} + x^5 + \cdots + C$
86. Evaluate  $\int_0^{\pi/2} \cos^3 x \sin x dx$ .
- A.  $\frac{1}{4}$   
B.  $\frac{1}{3}$   
C. 0  
D. 1
87. The value of  $\int_0^1 \frac{dx}{1 + x^2}$  is:
- A.  $\pi$   
B.  $\frac{\pi}{2}$   
C.  $\frac{\pi}{4}$   
D. 1
88. Integrate  $\sqrt{ax + b}$  with respect to  $x$ .
- A.  $\frac{1}{2a\sqrt{ax + b}} + C$   
B.  $\frac{2}{3a}(ax + b)^{3/2} + C$   
C.  $\frac{1}{a}(ax + b)^{3/2} + C$   
D.  $\frac{2}{a}(ax + b)^{1/2} + C$
89. If  $f'(x) = x - \frac{1}{x^2}$  and  $f(1) = \frac{1}{2}$ , find  $f(x)$ .
- A.  $\frac{x^2}{2} + \frac{1}{x} + 1$   
B.  $\frac{x^2}{2} - \frac{1}{x} + 1$   
C.  $\frac{x^2}{2} + \frac{1}{x} - 1$   
D.  $\frac{x^2}{2} - \frac{1}{x} - \frac{1}{2}$
90. Evaluate  $\int_{-2}^2 (x^3 + \sin x) dx$ .
- A. 0  
B. 4  
C. 8  
D.  $16/3$
91. Find  $\int x\sqrt{x^2 + 1} dx$ .
- A.  $\frac{1}{2}(x^2 + 1)^{3/2} + C$   
B.  $\frac{1}{3}(x^2 + 1)^{3/2} + C$   
C.  $(x^2 + 1)^{1/2} + C$

- D.  $x^2\sqrt{x^2+1} + C$
92. What is  $\int_a^b f(x)dx + \int_b^c f(x)dx$ ?
- A.  $\int_a^c f(x)dx$   
 B.  $\int_c^a f(x)dx$   
 C.  $\int_b^a f(x)dx + \int_c^b f(x)dx$   
 D. 0
93. Evaluate  $\int (e^{2x} + e^{-2x})^2 dx$ .
- A.  $\frac{1}{4}e^{4x} + 2x - \frac{1}{4}e^{-4x} + C$   
 B.  $\frac{1}{2}e^{4x} + 2x - \frac{1}{2}e^{-4x} + C$   
 C.  $e^{4x} + 2 + e^{-4x} + C$   
 D.  $\frac{(e^{2x} + e^{-2x})^3}{3} + C$
94. Find the area between the curves  $y = x^2$  and  $y = x$ .
- A.  $\frac{1}{3}$   
 B.  $\frac{1}{6}$   
 C.  $\frac{1}{2}$   
 D. 1
95.  $\int \tan^2 x dx$ .
- A.  $\sec^2 x - x + C$   
 B.  $\tan x - x + C$   
 C.  $\frac{\tan^3 x}{3} + C$   
 D.  $\ln |\sec x| + C$
96. Evaluate  $\int_0^{\ln 2} e^x dx$ .
- A. 1  
 B. 2  
 C.  $2 - \ln 2$   
 D.  $\ln 2$
97. Find  $\int \frac{\cos x}{1 + \sin^2 x} dx$ .
- A.  $\ln(1 + \sin^2 x) + C$   
 B.  $\arctan(\sin x) + C$   
 C.  $\arcsin(\cos x) + C$   
 D.  $\frac{-\sin x}{(1 + \sin^2 x)^2} + C$
98. Find the volume of the solid generated by revolving the region bounded by  $y = \frac{1}{x}$ , the x-axis, from  $x = 1$  to  $x = 2$ .
- A.  $\pi$   
 B.  $\frac{\pi}{2}$   
 C.  $\frac{\pi}{3}$   
 D.  $2\pi$
99. Evaluate  $\int \frac{2x+3}{x^2+3x+5} dx$ .
- A.  $2 \ln |x^2 + 3x + 5| + C$   
 B.  $\ln |x^2 + 3x + 5| + C$   
 C.  $\frac{1}{2} \ln |x^2 + 3x + 5| + C$   
 D.  $\arctan(x^2 + 3x + 5) + C$
100. Evaluate  $\int_0^1 x(x^2 + 1)^3 dx$ .
- A.  $\frac{15}{8}$   
 B.  $\frac{7}{4}$   
 C. 22  
 D.  $\frac{17}{8}$

## Chapter 5

# Combinatorics

### 5.1 Combination & Permutation

#### 5.1.1 Questions

1. Ralia has 7 different posters to be hung in her bedroom, living room, and kitchen. Assuming she has plans to plant at least a poster in each of the 3 rooms, how many choices does she have?  
A. 49  
B. 170  
C. 210  
D. 21
2. In how many ways can a committee of 2 women and 3 men be chosen from 6 men and 5 women?  
A. 200  
B. 100  
C. 50  
D. 30
3. In how many ways can the letters of the word MATHEMATICS be arranged?  
A.  $\frac{11!}{9!2!}$   
B.  $\frac{11!}{9!2!2!}$   
C.  $\frac{11!}{2!2!2!}$   
D.  $\frac{11!}{2!2!}$
4. In how many ways can the letters of the word ACCEPTANCE be arranged?  
A.  $\frac{10!}{2!2!3!}$   
B.  $\frac{10!}{2!2!}$   
C.  $10!$   
D.  $\frac{10!}{2!3!}$
5. Five people are to be arranged in a row for a group photograph. How many arrangements are there if a married couple in the group insist on sitting next to each other?  
A. 48  
B. 12  
C. 7  
D. 10
6. In how many ways can 6 subjects be selected from 10 subjects for an examination  
A. 215  
B. 218  
C. 216  
D. 210
7. In how many ways can a delegation of 3 be chosen from 5 men and 3 women, if atleast 1 man and 1 woman must be included?  
A. 28  
B. 30  
C. 15  
D. 45
8. Find the number of ways of selecting 6 out of 10 subjects for an examination  
A. 218  
B. 216

- C. 210  
D. 215
9. In how many ways can the letters of the word ELATION be arranged?
- A.  $6!$   
B.  $7!$   
C.  $5!$   
D.  $8!$
10. In how many ways can the letters of the word CALCULUS be arranged?
- A. 1680  
B. 2100  
C. 5040  
D. 1760
11. In how many ways can the letters of the word COMBINATION be arranged?
- A. 4989600  
B. 39916800  
C. 19958400  
D. 9979200
12. In how many ways can 7 directors sit round a table?
- A. 24  
B. 5040  
C. 120  
D. 120
13. In how many ways can the letters of the word TOTALITY be arranged?
- A. 6720  
B. 6270  
C. 6207  
D. 6027
14. How many numbers greater than 1000 can be made from the digits 1, 2, 3, 4, and 5 without repeating any one of them?
- A. 152  
B. 210  
C. 216  
D. 144
15. In how many ways can a team of 3 girls be selected from 7 girls?
- A.  $\frac{7!}{5!2!}$   
B.  $\frac{7!}{3!}$   
C.  $\frac{7!}{3!4!}$   
D.  $\frac{7!}{4!}$
16. In how many ways can a student select 2 subjects from 5 subjects?
- A.  $\frac{5!}{3!2!}$   
B.  $\frac{5!}{2!2!}$   
C.  $\frac{5!}{2!3!}$   
D.  $\frac{5!}{2!}$
17. In how many ways can five people sit round a circular table?
- A. 24  
B. 60  
C. 12  
D. 120
18. How many two-digit numbers can be formed from the digits 0, 1, 2, and 3 if a digit can be repeated and no number may begin with 0?
- A. 4  
B. 12  
C. 16  
D. 20
19. In how many ways can 9 people be seated if 3 chairs are available?
- A. 720  
B. 504  
C. 336  
D. 210
20. A final examination requires that a student answer any 4 out of 6 questions. In how many ways can this be done?
- A. 15  
B. 20  
C. 45  
D. 30

21. In how many ways can 6 coloured chalks be arranged if 2 are of the same colour?
- A. 60
  - B. 240
  - C. 120
  - D. 360
22. How many possible ways are there of seating seven people  $P, Q, R, S, T, U$ , and  $V$  at a circular table?
- A. 720
  - B. 2520
  - C. 5040
  - D. 360
23. A committee of six is to be formed by a state governor from nine state commissioners and three members of the State House of Assembly. In how many ways can the members of the committee be chosen so as to include one member of the House of the Assembly?
- A. 924 ways
  - B. 524 ways
  - C. 462 ways
  - D. 378 ways
24. How many two-digit numbers can be formed from the digits 0, 1, 2, and 3 if a digit can be repeated and no number may begin with 0?
- A. 4
  - B. 12
  - C. 16
  - D. 20
25. Find the number of committees of three that can be formed consisting of two men and one woman from four men and three women
- A. 3
  - B. 6
  - C. 18
  - D. 24
26. In how many ways can 8 people be arranged in a straight line if 2 particular people must not be next to each other?
- A. 30240
  - B. 25200
  - C. 10080
  - D. 5040
27. How many 3-digit numbers can be formed from the digits 1, 2, 3, 4, 5, 6 if no digit is repeated?
- A. 120
  - B. 216
  - C. 720
  - D. 180
28. In how many ways can a president, vice-president, and secretary be chosen from a group of 10 people?
- A. 720
  - B. 120
  - C. 210
  - D. 1000
29. How many different 4-letter arrangements can be made from the word PEPPER?
- A. 60
  - B. 72
  - C. 84
  - D. 96
30. In how many ways can 4 boys and 3 girls be arranged in a row if the girls must sit together?
- A. 720
  - B. 1440
  - C. 2880
  - D. 144
31. A committee of 5 is to be selected from 6 men and 4 women. In how many ways can this be done if there must be exactly 3 men?
- A. 120
  - B. 100
  - C. 80
  - D. 60
32. How many odd 3-digit numbers can be formed from the digits 1, 2, 3, 4, 5 without repetition?
- A. 36
  - B. 48
  - C. 60
  - D. 24
33. In how many ways can 10 books be arranged on a shelf if 3 particular books must always be together?
- A. 241920
  - B. 120960

- C. 604800  
D. 43200
34. A team of 4 people is to be selected from 5 couples. In how many ways can this be done if no couple is selected together?
- A. 80  
B. 100  
C. 120  
D. 60
35. In how many ways can the letters of the word PROPORTION be arranged?
- A. 907200  
B. 1814400  
C. 453600  
D. 604800
36. How many 5-digit even numbers can be formed using the digits 0, 1, 2, 3, 4 without repetition?
- A. 42  
B. 48  
C. 54  
D. 36
37. In how many ways can 5 keys be arranged on a circular key ring?
- A. 12  
B. 24  
C. 60  
D. 120
38. A box contains 5 red balls, 4 blue balls, and 3 green balls. In how many ways can 3 balls be selected if all must be of different colors?
- A. 60  
B. 120  
C. 180  
D. 240
39. How many numbers between 3000 and 4000 can be formed from the digits 1, 2, 3, 4, 5, 6 if no digit is repeated?
- A. 60  
B. 120  
C. 180  
D. 240
40. In how many ways can 8 people sit around a circular table if 2 particular people must sit together?
- A. 1440  
B. 720  
C. 2880  
D. 5040
41. A student must answer 5 questions out of 8 in an examination. In how many ways can this be done if the first 3 questions are compulsory?
- A. 10  
B. 15  
C. 20  
D. 25
42. In how many ways can the letters of the word STATISTICS be arranged?
- A. 50400  
B. 100800  
C. 25200  
D. 151200
43. How many 4-digit numbers divisible by 5 can be formed from the digits 0, 1, 2, 3, 4, 5 without repetition?
- A. 120  
B. 96  
C. 108  
D. 84
44. In how many ways can 3 prizes be distributed among 10 students if each student can receive at most one prize?
- A. 720  
B. 1000  
C. 120  
D. 210
45. A committee of 6 members is to be formed from 8 men and 5 women. How many committees can be formed with at least 4 men?
- A. 1050  
B. 980  
C. 1120  
D. 896
46. In how many ways can 4 different mathematics books and 3 different physics books be arranged on a shelf if books of the same subject must be together?

- A. 288  
B. 144  
C. 576  
D. 1152
47. How many 3-letter words (with or without meaning) can be formed from the letters of the word DAUGHTER if no letter is repeated?
- A. 336  
B. 168  
C. 504  
D. 252
48. In how many ways can 9 students be divided into 3 groups of 3 each?
- A. 280  
B. 560  
C. 1680  
D. 840
49. A password must contain 4 digits. How many different passwords can be formed if the first digit cannot be 0 and repetition is allowed?
- A. 9000  
B. 10000  
C. 5040  
D. 6561
50. In how many ways can a captain and vice-captain be selected from a cricket team of 11 players?
- A. 110  
B. 55  
C. 22  
D. 121
51. How many diagonals does a decagon (10-sided polygon) have?
- A. 35  
B. 45  
C. 55  
D. 65
52. In how many ways can 5 couples be seated in a row if each couple must sit together?
- A. 3840  
B. 7680  
C. 1920  
D. 15360
53. A class has 12 students. In how many ways can 4 students be selected to represent the class in a competition?
- A. 495  
B. 11880  
C. 1485  
D. 220
54. How many 4-digit numbers greater than 5000 can be formed from the digits 3, 4, 5, 6, 7 if repetition is not allowed?
- A. 72  
B. 48  
C. 60  
D. 120
55. In how many ways can the letters of the word EXAMINATION be arranged so that the vowels always occur together?
- A. 120960  
B. 241920  
C. 60480  
D. 181440
56. A committee of 7 is to be formed from 5 teachers and 4 students. In how many ways can this be done if there must be more teachers than students?
- A. 80  
B. 70  
C. 60  
D. 90
57. In how many ways can 6 beads of different colors be arranged to form a necklace?
- A. 60  
B. 120  
C. 720  
D. 30
58. How many 5-digit numbers can be formed from the digits 1, 2, 3, 4, 5, 6 if the number must be divisible by 4 and no digit is repeated?
- A. 120  
B. 144  
C. 168  
D. 96

59. In how many ways can 4 boys and 4 girls be seated alternately in a row?
- A. 1152  
B. 576  
C. 2304  
D. 288
60. A bag contains 6 identical red balls and 4 identical blue balls. In how many ways can 5 balls be selected?
- A. 6  
B. 5  
C. 4  
D. 7
61. In how many ways can 10 different books be divided equally between 2 students?
- A. 252  
B. 126  
C. 504  
D. 63
62. How many 3-digit numbers less than 500 can be formed from the digits 1, 2, 3, 4, 5, 6 if no digit is repeated?
- A. 80  
B. 100  
C. 120  
D. 60
63. In how many ways can a team of 11 players be selected from 15 players if 2 particular players must be included?
- A. 715  
B. 286  
C. 364  
D. 455
64. In how many ways can the letters of the word MISSISSIPPI be arranged?
- A. 34650  
B. 69300  
C. 17325  
D. 138600
65. A multiple choice test has 10 questions with 4 options each. In how many ways can a student answer all questions?
- A. 1048576  
B. 40  
C. 5040  
D. 3628800
66. In how many ways can 5 different flags be displayed on 3 poles if each pole must have at least one flag?
- A. 150  
B. 120  
C. 180  
D. 90
67. How many 4-letter arrangements can be made from the letters of the word SUCCESSFUL if all letters are distinct in the arrangement?
- A. 840  
B. 1260  
C. 420  
D. 1680
68. In how many ways can 8 identical balls be distributed among 3 different boxes if each box must contain at least one ball?
- A. 21  
B. 28  
C. 15  
D. 36
69. A committee of 5 members is to be formed from 4 men and 6 women. In how many ways can this be done if there must be at least 2 men and at least 2 women?
- A. 186  
B. 210  
C. 120  
D. 156
70. In how many ways can 7 people be arranged in a circle if 3 particular people must not sit together?
- A. 576  
B. 432  
C. 288  
D. 144
71. How many 5-digit palindromic numbers can be formed using the digits 1, 2, 3, 4, 5?
- A. 125  
B. 120  
C. 25



- D. 625
72. In how many ways can 6 men and 4 women be seated in a row such that no two women sit together?
- A. 604800  
B. 1209600  
C. 302400  
D. 151200
73. A committee of 4 is to be selected from 6 doctors and 5 engineers. In how many ways can this be done if the committee must have equal numbers of doctors and engineers?
- A. 150  
B. 200  
C. 100  
D. 180
74. In how many ways can 5 red balls, 4 blue balls, and 3 green balls be arranged in a row if balls of the same color are identical?
- A. 27720  
B. 55440  
C. 13860  
D. 110880
75. How many numbers between 4000 and 5000 can be formed from the digits 2, 3, 4, 5, 6, 7 if no digit is repeated?
- A. 60  
B. 120  
C. 240  
D. 180
76. In how many ways can a group of 12 people be divided into three groups of 4 each for three different tasks?
- A. 34650  
B. 5775  
C. 11550  
D. 23100
77. How many 6-digit numbers can be formed from the digits 1, 2, 3, 4, 5, 6 if the even digits must occupy even positions?
- A. 36  
B. 72  
C. 18
- D. 48
78. In how many ways can 10 students be arranged in a row if 3 particular students must be separated by at least 2 other students?
- A. 2419200  
B. 1814400  
C. 1209600  
D. 604800
79. A box contains 5 different English books, 4 different Mathematics books, and 3 different Science books. In how many ways can 3 books be selected if exactly one book of each subject is selected?
- A. 60  
B. 120  
C. 180  
D. 220
80. In how many ways can the letters of the word PARALLEL be arranged such that all L's are not together?
- A. 3360  
B. 2520  
C. 6720  
D. 1680
81. How many 4-digit even numbers greater than 4000 can be formed from the digits 1, 2, 3, 4, 5, 6 if no digit is repeated?
- A. 156  
B. 120  
C. 144  
D. 108
82. In how many ways can 8 people be seated around a circular table if 4 particular people must sit in alternate positions?
- A. 144  
B. 288  
C. 576  
D. 72
83. A committee of 6 is to be formed from 7 men and 6 women such that the committee contains at least 3 men and at least 2 women. In how many ways can this be done?
- A. 1596  
B. 1386  
C. 1191

- D. 1716
84. In how many ways can 4 different rings be worn on the fingers of one hand (excluding the thumb)?
- A. 256  
B. 1024  
C. 64  
D. 16
85. How many 5-letter words can be formed from the letters of the word MONDAY if each word must contain exactly 2 vowels?
- A. 720  
B. 360  
C. 480  
D. 240
86. In how many ways can 5 Indian and 4 American delegates be seated at a round table so that all Americans sit together?
- A. 2880  
B. 5760  
C. 1440  
D. 720
87. A code consists of 3 letters followed by 2 digits. How many different codes can be formed if the first letter must be a vowel, repetition is allowed, and the digits must be different?
- A. 29250  
B. 32500  
C. 16900  
D. 35100
88. In how many ways can 7 different colored beads be arranged on a bracelet?
- A. 360  
B. 720  
C. 2520  
D. 180
89. A team of 5 is to be selected from 7 boys and 6 girls. In how many ways can this be done if the team must contain more boys than girls?
- A. 1071  
B. 756  
C. 861
- D. 966
90. In how many ways can the letters of the word COMMITTEE be arranged if all vowels must be together and all consonants must be together?
- A. 2880  
B. 1440  
C. 5760  
D. 720
91. How many 6-digit numbers can be formed using the digits 0, 1, 2, 3, 4, 5 if the number must be even, greater than 300000, and no digit is repeated?
- A. 156  
B. 132  
C. 144  
D. 168
92. In how many ways can 10 identical apples and 6 identical oranges be distributed among 4 children such that each child gets at least one fruit?
- A. 252  
B. 378  
C. 210  
D. 504
93. A student must answer 8 questions out of 12 in an examination. In how many ways can this be done if questions 1 and 2 cannot both be omitted?
- A. 489  
B. 462  
C. 495  
D. 429
94. In how many ways can 9 different books be distributed equally among 3 students?
- A. 1680  
B. 280  
C. 5040  
D. 840
95. How many triangles can be formed by joining the vertices of an octagon?
- A. 56  
B. 84  
C. 28  
D. 120

96. In how many ways can 6 students be divided into 2 groups of 3 each for a debate competition?
- A. 10  
B. 20  
C. 30  
D. 40
97. In how many ways can 4 red flags, 3 blue flags, and 2 green flags be arranged in a row if flags of the same color are identical?
- A. 1260  
B. 2520  
C. 630  
D. 5040
98. A password must contain 2 letters followed by 3 digits. How many different passwords can be formed if the letters must be different and the digits must be odd?
- A. 32500  
B. 81250  
C. 65000  
D. 16250
99. In how many ways can a team of 11 cricket players be selected from 8 batsmen and 6 bowlers if the team must include at least 5 batsmen and at least 4 bowlers?
- A. 294  
B. 336  
C. 378  
D. 420
100. How many 7-digit telephone numbers can be formed if the first digit cannot be 0 or 1, and repetition of digits is allowed?
- A. 8000000  
B. 9000000  
C. 7000000  
D. 10000000

## 5.2 Probability

### 5.2.1 Questions

1. A bag contains 5 red balls and 3 blue balls. What is the probability of selecting a red ball?
- A.  $\frac{5}{8}$   
B.  $\frac{3}{8}$   
C.  $\frac{5}{3}$   
D.  $\frac{3}{5}$
2. Two dice are thrown together. What is the probability that the sum of the numbers is 7?
- A.  $\frac{1}{6}$   
B.  $\frac{1}{12}$   
C.  $\frac{5}{36}$   
D.  $\frac{7}{36}$
3. A box contains 4 red, 3 white, and 5 black balls. If one ball is drawn at random, what is the probability that it is not red?
- A.  $\frac{2}{3}$   
B.  $\frac{1}{3}$   
C.  $\frac{1}{2}$   
D.  $\frac{3}{4}$
4. A card is drawn at random from a standard deck of 52 cards. What is the probability of drawing a king?
- A.  $\frac{1}{13}$   
B.  $\frac{1}{52}$   
C.  $\frac{4}{52}$   
D.  $\frac{1}{4}$
5. If  $P(A) = 0.6$  and  $P(B) = 0.4$ , and A and B are mutually exclusive events, find  $P(A \text{ or } B)$ .
- A. 1.0  
B. 0.24  
C. 0.8

- D. 0.5
6. A bag contains 6 white and 4 black balls. Two balls are drawn at random without replacement. What is the probability that both are white?
- A.  $\frac{1}{3}$   
B.  $\frac{2}{5}$   
C.  $\frac{1}{2}$   
D.  $\frac{3}{10}$
7. The probability that it will rain tomorrow is 0.7. What is the probability that it will not rain?
- A. 0.3  
B. 0.7  
C. 1.0  
D. 0.5
8. Three coins are tossed simultaneously. What is the probability of getting at least two heads?
- A.  $\frac{1}{2}$   
B.  $\frac{1}{4}$   
C.  $\frac{3}{8}$   
D.  $\frac{5}{8}$
9. A die is rolled. What is the probability of getting an even number?
- A.  $\frac{1}{2}$   
B.  $\frac{1}{3}$   
C.  $\frac{2}{3}$   
D.  $\frac{1}{6}$
10. A bag contains 8 red and 5 blue marbles. If two marbles are drawn at random with replacement, what is the probability that both are red?
- A.  $\frac{64}{169}$   
B.  $\frac{8}{13}$   
C.  $\frac{56}{169}$   
D.  $\frac{40}{169}$
11. From a deck of 52 cards, what is the probability of drawing a heart or a king?
- A.  $\frac{4}{13}$   
B.  $\frac{17}{52}$   
C.  $\frac{13}{52}$   
D.  $\frac{16}{52}$
12. A bag contains 5 red, 4 blue, and 3 green balls. What is the probability of drawing a blue ball?
- A.  $\frac{1}{3}$   
B.  $\frac{1}{4}$   
C.  $\frac{5}{12}$   
D.  $\frac{1}{2}$
13. Two cards are drawn from a deck without replacement. What is the probability that both are aces?
- A.  $\frac{1}{221}$   
B.  $\frac{4}{663}$   
C.  $\frac{1}{169}$   
D.  $\frac{2}{221}$
14. A coin is tossed three times. What is the probability of getting exactly two tails?
- A.  $\frac{3}{8}$   
B.  $\frac{1}{4}$   
C.  $\frac{1}{2}$   
D.  $\frac{1}{8}$
15. If  $P(A) = 0.5$ ,  $P(B) = 0.4$ , and  $P(A \cap B) = 0.2$ , find  $P(A \cup B)$ .
- A. 0.7  
B. 0.9  
C. 0.6  
D. 0.8

16. A box contains 7 red and 5 white balls. Three balls are drawn at random. What is the probability that all are red?
- A.  $\frac{7}{44}$   
B.  $\frac{35}{264}$   
C.  $\frac{1}{12}$   
D.  $\frac{7}{22}$
17. A die is rolled twice. What is the probability that the sum is 10?
- A.  $\frac{1}{12}$   
B.  $\frac{1}{9}$   
C.  $\frac{1}{18}$   
D.  $\frac{5}{36}$
18. A card is drawn from a deck of 52 cards. What is the probability that it is either a spade or a face card?
- A.  $\frac{11}{26}$   
B.  $\frac{25}{52}$   
C.  $\frac{13}{26}$   
D.  $\frac{22}{52}$
19. In a class of 30 students, 18 play football and 12 play basketball. If 8 play both games, what is the probability that a randomly selected student plays at least one game?
- A.  $\frac{11}{15}$   
B.  $\frac{2}{3}$   
C.  $\frac{3}{5}$   
D.  $\frac{4}{5}$
20. A bag contains 4 red, 5 blue, and 6 green balls. Two balls are drawn at random. What is the probability that they are of different colors?
- A.  $\frac{37}{70}$   
B.  $\frac{74}{105}$   
C.  $\frac{31}{70}$   
D.  $\frac{33}{70}$
21. What is the probability of getting at least one head when a coin is tossed four times?
- A.  $\frac{15}{16}$   
B.  $\frac{1}{2}$   
C.  $\frac{7}{8}$   
D.  $\frac{3}{4}$
22. A number is selected at random from the numbers 1 to 20. What is the probability that it is divisible by 3 or 5?
- A.  $\frac{9}{20}$   
B.  $\frac{1}{2}$   
C.  $\frac{11}{20}$   
D.  $\frac{2}{5}$
23. Two dice are rolled. What is the probability that at least one shows a 6?
- A.  $\frac{11}{36}$   
B.  $\frac{1}{3}$   
C.  $\frac{5}{18}$   
D.  $\frac{1}{6}$
24. A bag contains 3 red, 4 white, and 5 black balls. If three balls are drawn at random, what is the probability that they are of the same color?
- A.  $\frac{3}{44}$   
B.  $\frac{7}{44}$   
C.  $\frac{1}{11}$   
D.  $\frac{5}{44}$
25. If the probability of an event is  $\frac{3}{7}$ , what is the probability of its complement?
- A.  $\frac{4}{7}$

- B.  $\frac{3}{7}$   
 C.  $\frac{1}{7}$   
 D.  $\frac{10}{7}$
26. A letter is chosen at random from the word "MATHEMATICS". What is the probability that it is a vowel?
- A.  $\frac{4}{11}$   
 B.  $\frac{5}{11}$   
 C.  $\frac{3}{11}$   
 D.  $\frac{6}{11}$
27. Three cards are drawn from a deck without replacement. What is the probability that all three are diamonds?
- A.  $\frac{11}{850}$   
 B.  $\frac{13}{204}$   
 C.  $\frac{1}{64}$   
 D.  $\frac{1}{52}$
28. A box contains 6 defective and 14 non-defective items. If 3 items are drawn at random, what is the probability that at least one is defective?
- A.  $\frac{73}{95}$   
 B.  $\frac{22}{95}$   
 C.  $\frac{3}{10}$   
 D.  $\frac{91}{190}$
29. A die is rolled. What is the probability of getting a prime number?
- A.  $\frac{1}{2}$   
 B.  $\frac{1}{3}$   
 C.  $\frac{2}{3}$   
 D.  $\frac{5}{6}$
30. If two events A and B are independent with  $P(A) = 0.6$  and  $P(B) = 0.5$ , find  $P(A \text{ and } B)$ .
- A. 0.3  
 B. 0.5  
 C. 0.8  
 D. 0.25
31. A bag contains 5 red, 6 blue, and 4 green balls. What is the probability of drawing either a red or green ball?
- A.  $\frac{3}{5}$   
 B.  $\frac{2}{5}$   
 C.  $\frac{1}{3}$   
 D.  $\frac{9}{15}$
32. Four coins are tossed simultaneously. What is the probability of getting exactly three heads?
- A.  $\frac{1}{4}$   
 B.  $\frac{3}{16}$   
 C.  $\frac{1}{8}$   
 D.  $\frac{1}{2}$
33. A number is chosen at random from 1 to 50. What is the probability that it is a multiple of 7?
- A.  $\frac{7}{50}$   
 B.  $\frac{1}{7}$   
 C.  $\frac{3}{25}$   
 D.  $\frac{2}{25}$
34. Two events A and B are such that  $P(A) = 0.4$ ,  $P(B) = 0.5$ , and  $P(A \cup B) = 0.7$ . Find  $P(A \cap B)$ .
- A. 0.2  
 B. 0.3  
 C. 0.1  
 D. 0.6
35. A bag contains 7 white and 8 black balls. If two balls are drawn at random, what is the probability that one is white and one is black?
- A.  $\frac{56}{105}$   
 B.  $\frac{8}{15}$   
 C.  $\frac{7}{15}$

- D.  $\frac{1}{2}$
36. A die is rolled three times. What is the probability of getting three different numbers?
- A.  $\frac{5}{9}$   
B.  $\frac{20}{27}$   
C.  $\frac{2}{3}$   
D.  $\frac{25}{36}$
37. From a group of 5 men and 4 women, a committee of 3 is selected at random. What is the probability that it contains at least one woman?
- A.  $\frac{5}{6}$   
B.  $\frac{37}{42}$   
C.  $\frac{2}{3}$   
D.  $\frac{3}{4}$
38. A card is drawn from a deck and replaced. This is done three times. What is the probability of getting exactly two spades?
- A.  $\frac{9}{64}$   
B.  $\frac{3}{16}$   
C.  $\frac{27}{256}$   
D.  $\frac{1}{8}$
39. In a single throw of two dice, what is the probability of getting a doublet?
- A.  $\frac{1}{6}$   
B.  $\frac{1}{12}$   
C.  $\frac{1}{36}$   
D.  $\frac{5}{36}$
40. A box contains 4 red, 3 blue, and 5 green marbles. Three marbles are drawn at random without replacement. What is the probability that all three are green?
- A.  $\frac{1}{22}$
- B.  $\frac{5}{66}$   
C.  $\frac{10}{132}$   
D.  $\frac{1}{11}$
41. If  $P(A) = 0.7$ ,  $P(B) = 0.6$ , and  $P(A \cap B) = 0.4$ , find  $P(A' \cap B')$ .
- A. 0.1  
B. 0.2  
C. 0.3  
D. 0.4
42. A letter is chosen at random from the word "PROBABILITY". What is the probability that it is the letter B?
- A.  $\frac{2}{11}$   
B.  $\frac{1}{11}$   
C.  $\frac{3}{11}$   
D.  $\frac{1}{5}$
43. Three dice are thrown simultaneously. What is the probability that the sum is 10?
- A.  $\frac{1}{8}$   
B.  $\frac{25}{216}$   
C.  $\frac{27}{216}$   
D.  $\frac{1}{12}$
44. A bag contains 5 white, 7 red, and 8 black balls. If three balls are drawn at random, what is the probability that they are of different colors?
- A.  $\frac{7}{19}$   
B.  $\frac{280}{1140}$   
C.  $\frac{14}{57}$   
D.  $\frac{140}{570}$
45. A number is selected at random from 1 to 100. What is the probability that it is divisible by both 3 and 5?
- A.  $\frac{1}{15}$   
B.  $\frac{2}{25}$

- C.  $\frac{3}{50}$   
D.  $\frac{7}{100}$
46. Two cards are drawn from a deck with replacement. What is the probability that both are hearts?
- A.  $\frac{1}{16}$   
B.  $\frac{1}{4}$   
C.  $\frac{13}{204}$   
D.  $\frac{1}{8}$
47. A box contains 10 items, 3 of which are defective. If 2 items are selected at random without replacement, what is the probability that both are defective?
- A.  $\frac{1}{15}$   
B.  $\frac{3}{45}$   
C.  $\frac{2}{15}$   
D.  $\frac{1}{10}$
48. A coin is tossed 5 times. What is the probability of getting at least 4 heads?
- A.  $\frac{3}{16}$   
B.  $\frac{1}{8}$   
C.  $\frac{5}{32}$   
D.  $\frac{6}{32}$
49. From a pack of 52 cards, two cards are drawn at random. What is the probability that both are red?
- A.  $\frac{25}{102}$   
B.  $\frac{1}{4}$   
C.  $\frac{13}{51}$   
D.  $\frac{26}{51}$
50. A die is rolled. Given that an even number appears, what is the probability that it is 4?
- A.  $\frac{1}{3}$   
B.  $\frac{1}{2}$   
C.  $\frac{1}{6}$   
D.  $\frac{2}{3}$
51. A bag contains 6 red, 5 blue, and 4 green balls. If two balls are drawn at random with replacement, what is the probability that both are of the same color?
- A.  $\frac{77}{225}$   
B.  $\frac{1}{3}$   
C.  $\frac{37}{105}$   
D.  $\frac{61}{225}$
52. Three students A, B, and C have probabilities  $\frac{1}{2}$ ,  $\frac{1}{3}$ , and  $\frac{1}{4}$  of solving a problem independently. What is the probability that the problem will be solved?
- A.  $\frac{3}{4}$   
B.  $\frac{2}{3}$   
C.  $\frac{11}{12}$   
D.  $\frac{5}{6}$
53. A box contains 8 balls numbered 1 to 8. Two balls are drawn at random. What is the probability that their sum is odd?
- A.  $\frac{4}{7}$   
B.  $\frac{1}{2}$   
C.  $\frac{3}{7}$   
D.  $\frac{16}{28}$
54. A card is drawn from a deck of 52 cards. What is the probability that it is a black card or a queen?
- A.  $\frac{7}{13}$   
B.  $\frac{1}{2}$   
C.  $\frac{28}{52}$   
D.  $\frac{15}{26}$



55. Four persons are chosen at random from a group of 3 men, 2 women, and 4 children. What is the probability that exactly two of them are children?
- A.  $\frac{10}{21}$   
B.  $\frac{3}{7}$   
C.  $\frac{1}{2}$   
D.  $\frac{2}{5}$
56. A number is chosen at random from the first 30 natural numbers. What is the probability that it is a perfect square?
- A.  $\frac{1}{6}$   
B.  $\frac{1}{5}$   
C.  $\frac{1}{10}$   
D.  $\frac{2}{15}$
57. Two dice are thrown. What is the probability that the difference of numbers shown is 2?
- A.  $\frac{2}{9}$   
B.  $\frac{1}{6}$   
C.  $\frac{1}{9}$   
D.  $\frac{7}{36}$
58. A bag contains 4 white, 5 black, and 6 red balls. Three balls are drawn at random. What is the probability that at least one is white?
- A.  $\frac{37}{91}$   
B.  $\frac{69}{91}$   
C.  $\frac{54}{91}$   
D.  $\frac{22}{91}$
59. If  $P(A) = 0.3$ ,  $P(B) = 0.4$ , and A and B are independent, find  $P(A' \cap B')$ .
- A. 0.42  
B. 0.58  
C. 0.28  
D. 0.12
60. A letter is selected at random from the word "ARRANGEMENT". What is the probability that it is a consonant?
- A.  $\frac{6}{11}$   
B.  $\frac{5}{11}$   
C.  $\frac{7}{11}$   
D.  $\frac{4}{11}$
61. Three cards are drawn from a deck with replacement. What is the probability that all three are aces?
- A.  $\frac{1}{2197}$   
B.  $\frac{64}{140608}$   
C.  $\frac{1}{169}$   
D.  $\frac{8}{2197}$
62. A box contains 5 red, 4 blue, and 3 yellow marbles. Two marbles are drawn without replacement. What is the probability that the first is red and the second is blue?
- A.  $\frac{5}{33}$   
B.  $\frac{20}{132}$   
C.  $\frac{10}{66}$   
D.  $\frac{1}{6}$
63. A die is thrown twice. What is the probability that the product of the numbers is even?
- A.  $\frac{3}{4}$   
B.  $\frac{1}{2}$   
C.  $\frac{5}{12}$   
D.  $\frac{2}{3}$
64. From 10 boys and 8 girls, a committee of 5 is selected. What is the probability that it contains exactly 3 boys?
- A.  $\frac{3360}{8568}$   
B.  $\frac{1}{3}$   
C.  $\frac{120}{357}$

- D.  $\frac{280}{714}$
65. A number is chosen at random from 1 to 60. What is the probability that it is divisible by 4 or 6?
- A.  $\frac{1}{2}$   
 B.  $\frac{13}{30}$   
 C.  $\frac{7}{15}$   
 D.  $\frac{2}{5}$
66. Two events A and B are such that  $P(A) = 0.5$ ,  $P(B) = 0.6$ , and  $P(A \cap B) = 0.3$ . Find  $P(A|B)$ .
- A. 0.5  
 B. 0.6  
 C. 0.3  
 D. 0.8
67. A bag contains 7 red, 5 white, and 6 blue balls. If one ball is drawn at random, what is the probability that it is either red or white?
- A.  $\frac{2}{3}$   
 B.  $\frac{7}{18}$   
 C.  $\frac{5}{9}$   
 D.  $\frac{12}{18}$
68. Four coins are tossed. What is the probability of getting at least two tails?
- A.  $\frac{11}{16}$   
 B.  $\frac{5}{8}$   
 C.  $\frac{3}{4}$   
 D.  $\frac{1}{2}$
69. A number is selected at random from integers 1 to 25. What is the probability that it is prime?
- A.  $\frac{9}{25}$   
 B.  $\frac{2}{5}$   
 C.  $\frac{8}{25}$   
 D.  $\frac{1}{3}$
70. Two dice are rolled. What is the probability that the sum is greater than 9?
- A.  $\frac{1}{6}$   
 B.  $\frac{5}{36}$   
 C.  $\frac{1}{4}$   
 D.  $\frac{7}{36}$
71. A bag contains 6 identical red balls and 4 identical blue balls. If 3 balls are drawn at random, what is the probability of getting 2 red and 1 blue?
- A.  $\frac{1}{2}$   
 B.  $\frac{3}{5}$   
 C.  $\frac{2}{5}$   
 D.  $\frac{60}{120}$
72. If events A and B are independent with  $P(A) = 0.7$  and  $P(B) = 0.5$ , find  $P(A \cup B)$ .
- A. 0.85  
 B. 0.9  
 C. 1.2  
 D. 0.35
73. A card is drawn from a deck. What is the probability that it is a red face card?
- A.  $\frac{3}{26}$   
 B.  $\frac{1}{13}$   
 C.  $\frac{6}{52}$   
 D.  $\frac{1}{4}$
74. Three students attempt a problem independently. Their probabilities of solving it are  $\frac{1}{2}$ ,  $\frac{1}{3}$ , and  $\frac{1}{5}$ . What is the probability that exactly one solves it?
- A.  $\frac{7}{15}$   
 B.  $\frac{13}{30}$   
 C.  $\frac{1}{2}$   
 D.  $\frac{3}{10}$

75. A box contains 9 tickets numbered 1 to 9. Two tickets are drawn at random. What is the probability that the sum is even?
- A.  $\frac{4}{9}$   
B.  $\frac{5}{9}$   
C.  $\frac{1}{2}$   
D.  $\frac{20}{36}$
76. A die is rolled four times. What is the probability of getting at least one six?
- A.  $\frac{671}{1296}$   
B.  $\frac{625}{1296}$   
C.  $\frac{2}{3}$   
D.  $\frac{1}{2}$
77. From a group of 6 men and 5 women, two people are selected at random. What is the probability that both are women?
- A.  $\frac{2}{11}$   
B.  $\frac{10}{55}$   
C.  $\frac{5}{22}$   
D.  $\frac{1}{6}$
78. A bag contains 5 white and 7 black balls. If two balls are drawn at random with replacement, what is the probability that at least one is white?
- A.  $\frac{95}{144}$   
B.  $\frac{49}{144}$   
C.  $\frac{5}{12}$   
D.  $\frac{2}{3}$
79. Two cards are drawn from a deck without replacement. What is the probability that the first is a king and the second is a queen?
- A.  $\frac{4}{663}$   
B.  $\frac{16}{2652}$   
C.  $\frac{1}{169}$   
D.  $\frac{8}{663}$
80. A number is chosen at random from 1 to 40. What is the probability that it is divisible by 2 and 3?
- A.  $\frac{1}{6}$   
B.  $\frac{3}{20}$   
C.  $\frac{7}{40}$   
D.  $\frac{1}{5}$
81. Three dice are thrown simultaneously. What is the probability of getting the same number on all three?
- A.  $\frac{1}{36}$   
B.  $\frac{1}{216}$   
C.  $\frac{6}{216}$   
D.  $\frac{1}{6}$
82. A bag contains 4 red, 3 blue, and 5 green marbles. Three marbles are drawn at random. What is the probability that no two are of the same color?
- A.  $\frac{3}{11}$   
B.  $\frac{60}{220}$   
C.  $\frac{2}{11}$   
D.  $\frac{30}{110}$
83. If  $P(A) = 0.4$ ,  $P(B) = 0.5$ , and  $P(A \cap B) = 0.2$ , find  $P(B|A)$ .
- A. 0.5  
B. 0.4  
C. 0.2  
D. 0.25
84. A coin is biased such that heads is twice as likely as tails. What is the probability of getting tails?
- A.  $\frac{1}{3}$   
B.  $\frac{1}{2}$   
C.  $\frac{2}{3}$

D.  $\frac{1}{4}$

85. A letter is chosen at random from the word "SUCCESS". What is the probability that it is the letter S?

A.  $\frac{3}{7}$

B.  $\frac{4}{7}$

C.  $\frac{2}{7}$

D.  $\frac{1}{2}$

86. Two dice are rolled. What is the probability that at least one die shows a number greater than 4?

A.  $\frac{5}{9}$

B.  $\frac{2}{3}$

C.  $\frac{20}{36}$

D.  $\frac{4}{9}$

87. A box contains 8 red, 6 blue, and 4 green balls. If three balls are drawn at random without replacement, what is the probability that all are blue?

A.  $\frac{5}{204}$

B.  $\frac{20}{816}$

C.  $\frac{1}{34}$

D.  $\frac{6}{204}$

88. If events A and B are mutually exclusive with  $P(A) = 0.3$  and  $P(B) = 0.5$ , find  $P(A' \cap B')$ .

A. 0.2

B. 0.8

C. 0.35

D. 0.15

89. A number is selected at random from integers 10 to 30. What is the probability that it is divisible by 3?

A.  $\frac{1}{3}$

B.  $\frac{7}{21}$

C.  $\frac{8}{21}$

D.  $\frac{2}{7}$

90. Three cards are drawn from a deck without replacement. What is the probability that at least one is a spade?

A.  $\frac{133}{204}$

B.  $\frac{71}{204}$

C.  $\frac{2}{3}$

D.  $\frac{39}{68}$

91. A bag contains 10 balls numbered 1 to 10. If two balls are drawn at random, what is the probability that their product is odd?

A.  $\frac{2}{9}$

B.  $\frac{10}{45}$

C.  $\frac{1}{3}$

D.  $\frac{5}{18}$

92. A bag contains 7 red, 5 blue, and 3 yellow balls. If three balls are drawn at random without replacement, what is the probability that exactly two are red?

A.  $\frac{21}{65}$

B.  $\frac{168}{455}$

C.  $\frac{42}{91}$

D.  $\frac{3}{13}$

93. Two friends agree to meet between 2:00 PM and 3:00 PM. Each arrives at a random time and waits for 15 minutes. What is the probability that they meet?

A.  $\frac{7}{16}$

B.  $\frac{1}{4}$

C.  $\frac{1}{2}$

D.  $\frac{3}{8}$

94. Two events A and B are independent with  $P(A) = 0.4$  and  $P(A \cup B) = 0.7$ . Find  $P(B)$ .

A. 0.5

B. 0.6

- C. 0.3  
D. 0.4
95. A die is rolled. What is the probability of getting a number less than 5?
- A.  $\frac{2}{3}$   
B.  $\frac{1}{2}$   
C.  $\frac{5}{6}$   
D.  $\frac{3}{4}$
96. From a deck of 52 cards, three cards are drawn with replacement. What is the probability that all three are kings?
- A.  $\frac{1}{2197}$   
B.  $\frac{64}{140608}$   
C.  $\frac{8}{2197}$   
D.  $\frac{1}{169}$
97. A box contains 5 red, 4 blue, and 6 green balls. Two balls are drawn without replacement. What is the probability that both are of the same color?
- A.  $\frac{16}{105}$   
B.  $\frac{31}{105}$   
C.  $\frac{1}{3}$   
D.  $\frac{37}{105}$
98. A coin is tossed 6 times. What is the probability of getting exactly 4 heads?
- A.  $\frac{15}{64}$   
B.  $\frac{5}{16}$   
C.  $\frac{3}{8}$   
D.  $\frac{1}{4}$
99. A number is chosen at random from 1 to 80. What is the probability that it is a multiple of both 4 and 6?
- A.  $\frac{1}{20}$   
B.  $\frac{3}{40}$   
C.  $\frac{7}{80}$   
D.  $\frac{1}{16}$
100. Two dice are thrown. What is the probability that the product of the numbers is a perfect square?
- A.  $\frac{1}{4}$   
B.  $\frac{11}{36}$   
C.  $\frac{7}{36}$   
D.  $\frac{5}{18}$

# Chapter 6

## Statistics

### 6.1 Measures of Central Tendency

#### 6.1.1 Questions

- Find the mean of the numbers 3, 5, 7, 9, and 11.
  - 7
  - 6
  - 8
  - 5
- The median of the data set 2, 5, 8, 11, 14 is
  - 8
  - 5
  - 11
  - 7
- Find the mode of the following data: 3, 5, 3, 7, 3, 9, 5.
  - 3
  - 5
  - 7
  - 9
- The mean of five numbers is 12. If four of the numbers are 10, 11, 13, and 15, find the fifth number.
  - 11
  - 12
  - 10
  - 9
- Find the median of 15, 20, 18, 12, 25, 22, 16.
  - 18
  - 20
  - 16
  - 19
- The data set 4, 7, 7, 10, 10, 10, 13 has a mode of
  - 10
  - 7
  - 13
  - 4
- If the mean of 8, 10,  $x$ , 14, and 16 is 12, find the value of  $x$ .
  - 12
  - 11
  - 10
  - 13
- Find the mean of the first five prime numbers.
  - 5.6
  - 6
  - 5
  - 6.5
- The median of 3, 7, 5, 9, 11, 13 is
  - 8
  - 7
  - 9
  - 7.5
- Which measure of central tendency is most affected by extreme values?
  - Mean
  - Median

- C. Mode  
D. Range
11. Find the mode of 12, 15, 12, 18, 20, 12, 15, 18, 12.  
A. 12  
B. 15  
C. 18  
D. 20
12. The mean of 6, 8, 10, 12, and  $x$  is 10. Find  $x$ .  
A. 14  
B. 12  
C. 10  
D. 16
13. Find the median of 2, 4, 6, 8, 10, 12, 14, 16.  
A. 8  
B. 9  
C. 10  
D. 7
14. The ages of five students are 15, 16, 14, 17, and 18 years. Find their mean age.  
A. 16  
B. 15  
C. 17  
D. 14
15. If the mean of 7 numbers is 15 and the mean of 3 of them is 12, find the mean of the remaining 4 numbers.  
A. 17.25  
B. 16.5  
C. 18  
D. 15.75
16. Find the mode of the data: 5, 7, 5, 8, 5, 9, 7, 7, 5.  
A. 5  
B. 7  
C. 8  
D. 9
17. The median of 21, 15, 18, 12, 24, 27 is  
A. 19.5  
B. 18  
C. 21  
D. 20
18. Find the mean of 20, 25, 30, 35, 40.  
A. 30  
B. 25  
C. 35  
D. 28
19. The data set 2, 4, 6, 8 has no mode. What can be said about this data?  
A. All values occur with equal frequency  
B. The data is bimodal  
C. The median is 5  
D. Both A and C
20. If the mean of 5, 7, 9,  $x$ , and 11 is 8, find  $x$ .  
A. 8  
B. 7  
C. 9  
D. 6
21. Find the median of 40, 35, 50, 45, 30, 55, 60.  
A. 45  
B. 50  
C. 40  
D. 47.5
22. The mode of 3, 5, 7, 5, 9, 5, 11, 7 is  
A. 5  
B. 7  
C. 9  
D. 3
23. Calculate the mean of 12, 18, 24, 30, 36.  
A. 24  
B. 22  
C. 26  
D. 20
24. The median of an even number of observations is  
A. The middle value  
B. The average of the two middle values  
C. The most frequent value  
D. The sum of all values
25. Find the mean of the squares of the first four natural numbers.

- A. 7.5  
B. 10  
C. 5  
D. 8
26. If the mean of 10 numbers is 20 and one number 25 is removed, what is the new mean?  
A. 19.44  
B. 20  
C. 18.5  
D. 21
27. Find the mode of 8, 10, 12, 10, 8, 14, 10, 8, 10.  
A. 10  
B. 8  
C. Both 8 and 10  
D. 12
28. The median of 5, 10, 15, 20, 25, 30, 35, 40, 45 is  
A. 25  
B. 20  
C. 30  
D. 22.5
29. Find the mean of all multiples of 5 between 1 and 30.  
A. 17.5  
B. 15  
C. 20  
D. 12.5
30. The mean of 4, 6, 8, 10, 12 is increased by 3 when each number is increased by  
A. 3  
B. 15  
C. 6  
D. 9
31. Find the median of 100, 90, 80, 110, 120, 95, 105.  
A. 100  
B. 105  
C. 95  
D. 110
32. The mode of a data set with all different values is  
A. Zero
- B. Does not exist  
C. The mean  
D. The median
33. If the mean of  $x$ ,  $x+2$ ,  $x+4$ ,  $x+6$ , and  $x+8$  is 10, find  $x$ .  
A. 6  
B. 7  
C. 8  
D. 5
34. Find the median of 2.5, 3.5, 4.5, 5.5, 6.5, 7.5.  
A. 5  
B. 5.5  
C. 4.5  
D. 6
35. The mean of 15 observations is 32. If two observations 40 and 50 are added, what is the new mean?  
A. 33.29  
B. 34  
C. 35  
D. 32.5
36. Find the mode of 1, 2, 2, 3, 3, 3, 4, 4, 4, 4.  
A. 4  
B. 3  
C. 2  
D. 1
37. The median of 7, 14, 21, 28, 35 is  
A. 21  
B. 14  
C. 28  
D. 20
38. Calculate the mean of the first 10 even natural numbers.  
A. 11  
B. 10  
C. 12  
D. 9
39. If the mean of 20 observations is 15 and that of another 30 observations is 20, find the mean of all 50 observations.  
A. 18  
B. 17.5  
C. 19



- D. 16.5
40. Find the mode of the data where all frequencies are equal.
- A. Does not exist
  - B. Zero
  - C. The mean
  - D. All values
41. The median of 1, 3, 5, 7, 9, 11, 13, 15, 17 is
- A. 9
  - B. 8
  - C. 10
  - D. 7
42. Find the mean of 2.5, 3.0, 3.5, 4.0, 4.5, 5.0.
- A. 3.75
  - B. 4
  - C. 3.5
  - D. 4.25
43. If the median of a data set is 25 and the mean is 30, the data is
- A. Positively skewed
  - B. Negatively skewed
  - C. Symmetric
  - D. Normal
44. Find the mode of 50, 60, 70, 60, 80, 60, 90, 70.
- A. 60
  - B. 70
  - C. 50
  - D. 80
45. The mean of three numbers is 20. If two of them are 15 and 18, find the third number.
- A. 27
  - B. 25
  - C. 22
  - D. 20
46. Find the median of 0.5, 1.5, 2.5, 3.5, 4.5, 5.5, 6.5, 7.5.
- A. 4
  - B. 3.5
  - C. 4.5
- D. 5
47. The mode is most useful when data is
- A. Categorical
  - B. Continuous
  - C. Symmetric
  - D. Normally distributed
48. Calculate the mean of 1, 4, 9, 16, 25.
- A. 11
  - B. 10
  - C. 12
  - D. 13
49. If each observation in a data set is multiplied by 5, the mean is
- A. Multiplied by 5
  - B. Divided by 5
  - C. Increased by 5
  - D. Remains the same
50. Find the median of 11, 22, 33, 44, 55, 66, 77, 88, 99.
- A. 55
  - B. 44
  - C. 50
  - D. 60
51. The mean of 8 numbers is 25. If 5 is subtracted from each number, the new mean is
- A. 20
  - B. 25
  - C. 30
  - D. 15
52. Find the mode of 15, 20, 25, 20, 30, 25, 20, 35.
- A. 20
  - B. 25
  - C. 15
  - D. 30
53. The median of 6, 12, 18, 24, 30, 36 is
- A. 21
  - B. 18
  - C. 24
  - D. 20
54. Find the mean of the first 7 odd natural numbers.

- A. 7  
B. 8  
C. 6  
D. 9
55. If the mean of 10, 15, 20,  $x$ , 30 is 20, find  $x$ .  
A. 25  
B. 20  
C. 22  
D. 18
56. The median is always  
A. A value in the data set  
B. The middle value when data is ordered  
C. Equal to the mean  
D. The most frequent value
57. Find the mode of 100, 200, 200, 300, 300, 300, 400.  
A. 300  
B. 200  
C. 100  
D. 400
58. The mean of 5 consecutive odd numbers is 21. Find the largest number.  
A. 25  
B. 23  
C. 27  
D. 21
59. Find the median of 50, 55, 60, 65, 70, 75, 80, 85, 90, 95.  
A. 72.5  
B. 70  
C. 75  
D. 65
60. Calculate the mean of 3, 6, 9, 12, 15, 18.  
A. 10.5  
B. 12  
C. 9  
D. 11
61. The mode of a bimodal distribution has  
A. Two values  
B. One value  
C. Three values  
D. No value
62. If the mean of  $x$ ,  $2x$ ,  $3x$ ,  $4x$ , and  $5x$  is 30, find  $x$ .  
A. 10  
B. 5  
C. 15  
D. 20
63. Find the median of 17, 23, 19, 21, 25, 20, 22.  
A. 21  
B. 20  
C. 22  
D. 19
64. The mean of 12 observations is 15. If each observation is doubled, the new mean is  
A. 30  
B. 15  
C. 27  
D. 18
65. Find the mode of 2, 4, 6, 2, 8, 2, 10, 4, 6, 2.  
A. 2  
B. 4  
C. 6  
D. 8
66. The median of 9, 18, 27, 36, 45, 54, 63, 72 is  
A. 40.5  
B. 36  
C. 45  
D. 42
67. Find the mean of all two-digit multiples of 10.  
A. 55  
B. 50  
C. 60  
D. 45
68. If the mean of  $a$ ,  $b$ ,  $c$  is 15 and the mean of  $a$ ,  $b$ ,  $c$ ,  $d$  is 20, find  $d$ .  
A. 35  
B. 30  
C. 25

- D. 40
69. Find the median of integers from 1 to 9.
- A. 5  
B. 4  
C. 6  
D. 4.5
70. The mode of the data 5, 10, 15, 10, 20, 15, 10, 25 is
- A. 10  
B. 15  
C. 20  
D. 5
71. Calculate the mean of 0, 5, 10, 15, 20, 25, 30.
- A. 15  
B. 12.5  
C. 17.5  
D. 20
72. If every value in a data set is the same, then
- A. Mean = Median = Mode  
B. Mean  $\neq$  Median  
C. Mode does not exist  
D. Median  $\neq$  Mode
73. Find the median of 1.2, 3.4, 2.3, 4.5, 3.2, 5.1.
- A. 3.3  
B. 3.4  
C. 3.2  
D. 2.85
74. The mean of 6 numbers is 18. If one number 24 is replaced by 18, the new mean is
- A. 17  
B. 18  
C. 19  
D. 16
75. Find the mode of 7, 14, 21, 14, 28, 21, 14, 35.
- A. 14  
B. 21  
C. 7  
D. 28
76. The median of 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 is
- A. 6  
B. 5  
C. 7  
D. 5.5
77. Find the mean of 16, 18, 20, 22, 24, 26, 28.
- A. 22  
B. 20  
C. 24  
D. 21
78. If the median is greater than the mean, the data is likely
- A. Negatively skewed  
B. Positively skewed  
C. Symmetric  
D. Uniform
79. Find the mode of 33, 44, 55, 44, 66, 55, 44, 77.
- A. 44  
B. 55  
C. 33  
D. 66
80. The mean of the first  $n$  natural numbers is
- A.  $\frac{n+1}{2}$   
B.  $\frac{n}{2}$   
C.  $n+1$   
D.  $\frac{n-1}{2}$
81. Find the median of 5, 15, 25, 35, 45, 55, 65, 75, 85.
- A. 45  
B. 40  
C. 50  
D. 35
82. Calculate the mean of 7, 14, 21, 28, 35, 42.
- A. 24.5  
B. 21  
C. 28  
D. 25
83. The mode is preferred over the mean when
- A. Data is qualitative  
B. Data has extreme values

- C. Quick calculation is needed  
D. All of the above
84. Find the median of 8, 16, 24, 32, 40, 48, 56.  
A. 32  
B. 28  
C. 36  
D. 24
85. If the mean of 4, 8, 12, x, 20 is 12, find x.  
A. 16  
B. 14  
C. 12  
D. 18
86. The median of 3, 6, 9, 12, 15, 18, 21, 24, 27, 30 is  
A. 16.5  
B. 15  
C. 18  
D. 15.5
87. Find the mean of 2, 4, 8, 16, 32.  
A. 12.4  
B. 10  
C. 14  
D. 16
88. Which measure of central tendency can have more than one value?  
A. Mode  
B. Mean  
C. Median  
D. None
89. Find the median of 13, 26, 39, 52, 65, 78, 91.  
A. 52  
B. 39  
C. 45.5  
D. 65
90. The mean of 5 consecutive even numbers is 16. Find the smallest number.  
A. 12  
B. 10  
C. 14  
D. 16
91. Find the mode of 1, 3, 5, 3, 7, 5, 9, 5, 11.  
A. 5  
B. 3  
C. 7  
D. 1
92. The median is less affected by outliers than the mean because it  
A. Depends only on position  
B. Is always smaller  
C. Is always larger  
D. Uses all data values
93. Find the mean of 11, 22, 33, 44, 55, 66, 77, 88, 99.  
A. 55  
B. 50  
C. 60  
D. 44
94. The sum of deviations of observations from their mean is always  
A. Zero  
B. Positive  
C. Negative  
D. One
95. The mean of 9 numbers is 40. If 4 is added to each number, the new mean is  
A. 44  
B. 40  
C. 36  
D. 45
96. Find the median of 1.5, 2.5, 3.5, 4.5, 5.5, 6.5, 7.5, 8.5.  
A. 5  
B. 4.5  
C. 5.5  
D. 6
97. For a symmetric distribution, which relationship holds?  
A. Mean = Median = Mode  
B. Mean > Median  
C. Median > Mean  
D. Mode > Mean

98. If each value in a data set is increased by  $k$ , the mean increases by
- A.  $k$
  - B.  $2k$
  - C.  $k^2$
  - D.  $\frac{k}{n}$
99. The mode of a trimodal distribution has
- A. Three values
  - B. Two values
  - C. One value
  - D. No value
100. The median divides the data into
- A. Two equal parts
  - B. Three equal parts
  - C. Four equal parts
  - D. Unequal parts

# Chapter 7

## Values To Memorize

### 7.1 Square Roots

- $\sqrt{1} = 1$
- $\sqrt{2} = 1.4142$
- $\sqrt{3} = 1.7321$
- $\sqrt{4} = 2$
- $\sqrt{5} = 2.2361$
- $\sqrt{6} = 2.4495$
- $\sqrt{7} = 2.6458$
- $\sqrt{8} = 2.8284$
- $\sqrt{9} = 3$
- $\sqrt{10} = 3.1623$

- $14^2 = 196$
- $15^2 = 225$
- $16^2 = 256$
- $17^2 = 289$
- $18^2 = 324$
- $19^2 = 361$
- $20^2 = 400$
- $21^2 = 441$

### 7.2 Squares

- $1^2 = 1$
- $2^2 = 4$
- $3^2 = 9$
- $4^2 = 16$
- $5^2 = 25$
- $6^2 = 36$
- $7^2 = 49$
- $8^2 = 64$
- $9^2 = 81$
- $10^2 = 100$
- $11^2 = 121$
- $12^2 = 144$
- $13^2 = 169$

- $22^2 = 484$
- $23^2 = 529$
- $24^2 = 576$
- $25^2 = 625$
- $26^2 = 676$
- $27^2 = 729$
- $28^2 = 784$
- $29^2 = 841$
- $30^2 = 900$

### 7.3 Cubes

- $1^3 = 1$
- $2^3 = 8$
- $3^3 = 27$
- $4^3 = 64$
- $5^3 = 125$
- $6^3 = 216$
- $7^3 = 343$
- $8^3 = 512$
- $9^3 = 729$
- $10^3 = 1000$
- $11^3 = 1331$
- $12^3 = 1728$
- $13^3 = 2197$
- $14^3 = 2744$
- $15^3 = 3375$
- $16^3 = 4096$
- $17^3 = 4913$
- $18^3 = 5832$
- $19^3 = 6859$
- $20^3 = 8000$
- $21^3 = 9261$
- $22^3 = 10648$
- $23^3 = 12167$
- $24^3 = 13824$
- $25^3 = 15625$
- $26^3 = 17576$
- $27^3 = 19683$
- $28^3 = 21952$
- $29^3 = 24389$
- $30^3 = 27000$

### 7.4 Logarithms

- $\log_{10} 1 = 0$
- $\log_{10} 2 = 0.3010$
- $\log_{10} 3 = 0.4771$
- $\log_{10} 4 = 0.6020$
- $\log_{10} 5 = 0.699$
- $\log_{10} 6 = 0.778$
- $\log_{10} 7 = 0.845$
- $\log_{10} 8 = 0.903$
- $\log_{10} 9 = 0.954$
- $\log_{10} 10 = 1$