

# **Ace Your UTME Mathematics**

A Comprehensive Guide with Past Questions and Solutions

**By**

**Ayodeji Adesegun and Chimobi Nwafor**

March 2024



# Dedication and Acknowledgements

This work is dedicated to our families, whose unwavering support has been our greatest strength throughout this journey. Their constant encouragement and belief in our abilities have fueled our passion and perseverance in creating this resource.

We would also like to express our sincere gratitude to the following individuals and institutions for their invaluable contributions:

- Our mentors and teachers, who instilled in us a love for mathematics and equipped us with the knowledge and skills needed to succeed.
- The examiners and administrators of the UTME, whose dedication to educational standards ensures a fair and effective assessment process.
- Our colleagues and friends, who provided feedback and support throughout the development of this book.
- The wider academic community, whose research and publications have laid the foundation for our understanding of mathematics.

We are truly grateful for the collective effort that has made this book possible. We hope that it will be a valuable resource for students preparing for the UTME and beyond.

## How We Wrote This Book

This book was written using the  $\text{\LaTeX}$  document processing package. Specifically, this book was prepared using the MikTeX installation of pdf $\text{\LaTeX}$  on a PC running Windows 11. We must thank the authors of the various packages we used. The diagrams were prepared using METAPOST, a graphics programming language based on Donald Knuth's METAFONT.

## About the Authors

**Ayodeji Adesegun:** He is a teenager. In his spare time, he enjoys solving mathematical problems from various contests not excluding the Olympiads. You can find more about him [here](#).

**Chimobi Nwafor:** He is a software engineer trainee at INITS.

# Contents

<b>1</b>	<b>Number and Numeration</b>	<b>1</b>
1.1	Number Bases	1
1.1.1	Questions	1
<b>2</b>	<b>Fraction and Decimals</b>	<b>7</b>
2.1	Percentage Error and Approximation	7
2.1.1	Questions	7
2.1.2	Solution	15
<b>3</b>	<b>Algebra</b>	<b>19</b>
3.1	Factorization and Remainder Theorem	19
3.1.1	Questions	19
3.1.2	Solution	25
3.2	Indices and Standard Form	28
3.2.1	Questions	28
<b>4</b>	<b>Geometry</b>	<b>33</b>
4.1		33
4.1.1	Questions	33
4.1.2	Solution	39
4.2	Co-ordinate Geometry	42
4.2.1	Questions	42
4.2.2	Solution	47
<b>5</b>	<b>Calculus</b>	<b>51</b>
5.1	Differentiation	51
5.1.1	Questions	51
5.1.2	Solution	58
5.2	Integration	61
5.2.1	Questions	61
5.2.2	Solution	66
<b>6</b>	<b>Combinatorics</b>	<b>69</b>
6.1	Combination & Permutation	69
6.1.1	Questions	69
6.1.2	Solution	75
<b>7</b>	<b>Statistics</b>	<b>79</b>
7.1	Measures of Central Tendency	79
7.1.1	Questions	79
7.1.2	Solution	85

<b>8</b>	<b>Values To Memorize</b>	<b>89</b>
8.1	Square Roots	89
8.2	Squares	89
8.3	Cubes	90
8.4	Logarithms	90



# Preface

Welcome to "Ace Your UTME Mathematics," a comprehensive guide designed to help you conquer the upcoming UTME Mathematics exam. This book provides you with a wealth of past questions, detailed solutions, and insightful strategies to enhance your understanding and preparation.

This book is organized into chapters that follow the official UTME Mathematics syllabus, covering all key topics and subtopics. Each chapter includes a variety of past questions carefully selected to reflect the types and difficulty levels encountered in the actual exam.

In addition to past questions, we have provided detailed solutions that explain the reasoning behind each step and highlight common mistakes to avoid. We encourage you to work through these solutions carefully and utilize them as learning tools to improve your problem-solving skills.

Furthermore, we have incorporated valuable strategies throughout the book, offering tips and techniques to maximize your efficiency and performance on the exam. These strategies will help you manage your time effectively, approach different question types confidently, and overcome any challenges you may encounter.

We are confident that "Ace Your UTME Mathematics" will be your ultimate companion on your journey to success. By diligently working through the material and utilizing the resources provided, you will gain the knowledge, skills, and confidence needed to achieve your desired score on the UTME Mathematics exam.

Best of luck!

Ayodeji Adesegun and Chimobi Nwafor





# Chapter 1

## Number and Numeration

### 1.1 Number Bases

#### 1.1.1 Questions

1. The number 25 when converted from the tens and units base to the binary base (base 2) is one of the following
  - A. 10011
  - B. 1111011
  - C. 111000
  - D. 11001
  - E. 110011
2. The currency used in a country bought 4 bags of rice at  $N56$  per bag and 3 tins of milk at  $N4$  per tin. What is the total cost of the items she bought?
  - A.  $N245$
  - B.  $N242$
  - C.  $N236$
  - D.  $N341$
  - E.  $N338$
3. Evaluate  $212_3 - 121_3 + 222_3$ .
  - A.  $313_3$
  - B.  $1000_3$
  - C.  $1020_3$
  - D.  $1222_3$
  - E.  $1213_3$
4. A trader in a country where their currency 'MONT' ( $M$ ) is in base five bought  $103_5$  oranges at  $M14_5$  each. If he sold the oranges at  $M24_5$  each, what would be his gain?
  - A.  $M103_5$
  - B.  $M1030_5$
  - C.  $M102_5$
  - D.  $M2002_5$
  - E.  $M3024_5$
5. Find  $x$  if  $(x_4)^2 = (100100)_2$ 
  - A. 6
  - B. 12
  - C. 100
  - D. 210
  - E. 10042
6. Convert  $241_5$  to base 8.
  - A.  $71_8$
  - B.  $107_8$
  - C.  $176_8$
  - D.  $241_8$
7. In the equation  $\frac{11_2}{x_2} = \frac{1000_2}{x_2 + 101_2}$ , solve for  $x$ .
  - A. 101
  - B. 11
  - C. 110
  - D. 111
  - E. 10
8.  $4243_5 - 12x4_5 = y344$ . What is the difference between  $x$  and  $y$ ?
  - A. 4
  - B. 2
  - C. 1
  - D. 3
  - E. 5
9. In base ten, the number  $101101_2$  equals.
  - A. 15

- B. 45  
C. 23  
D. 12  
E. 46
10. Convert the number 39 to base 2.  
A. 100111  
B. 111001  
C. 110111  
D. 111111  
E. 100101
11. Find  $n$  if  $34_n = 100112$ .  
A. 5  
B. 6  
C. 7  
D. 8  
E. 9
12. If  $2_9 \times (Y3)_9 = 3_5 \times (Y3)_5$ . Find the value of  $Y$   
A. 4  
B. 3  
C. 2  
D. 1  
E. 5
13. Simplify  $213_4 \times 23_4$ .  
A.  $10321_4$   
B.  $12231_4$   
C.  $13221_4$   
D.  $10311_4$   
E.  $13021_4$
14.  $55_x + 52_x = 77_{10}$ , find  $x$ .  
A. 5  
B. 6  
C. 7  
D. 8  
E. 10
15. If  $x_{10} = 23_5$ , find  $x$ .  
A. 15  
B. 12  
C. 14  
D. 13  
E. 16
16. Find the sum of  $25_6, 52_6, 43_6$  in base 8.  
A. 411  
B. 141  
C. 114  
D. 417
17.  $2A3_3 = 77_8$ , find  $A$ .  
A. 1  
B. 2  
C. 0  
D. 4
18. Evaluate  $(202_3)^2 - (112_3)^2$   
A. 21112  
B. 21121  
C. 21011  
D. 21120
19. If  $321_4$  is divided by  $23_4$  and leaves a remainder  $r$ , what is the value of  $r$ ?  
A. 4  
B. 2  
C. 3  
D. 0  
E. 1
20. Convert  $521_{10}$  to a number in base 5  
A.  $1404_5$   
B.  $4041_5$   
C.  $4140_5$   
D.  $4014_5$   
E.  $4104_5$
21. If  $6R7_8 = 511_9$ , find  $R$ .  
A. 6  
B. 5  
C. 3  
D. 2  
E. 8
22. Find the value of  $x$  if  $121_x + 112_x = 30_{10}$ .  
A. 5  
B. 7  
C.  $-\frac{9}{2}$   
D. 3  
E. 4
23. Evaluate  $(1011_2)^2 - 1012_2$ .  
A.  $110000_2$   
B.  $110000_2$   
C.  $101011_2$

- D.  $110110_2$
24. Add  $1101_2$ ,  $11011_2$  and  $111_2$ .
- A.  $110110_2$
- B.  $101011_2$
- C.  $111011_2$
- D.  $101010_2$
- E.  $110011_2$
25. Find the value of  $m$  if  $13_m + 24_m = 41_m$
- A. 8
- B. 5
- C. 4
- D. 6
- E. 3
26. If  $125_x = 20_10$ , find  $x$ .
- A. 2
- B. 3
- C. 4
- D. 6
- E. 5
27. If  $(K2)_6 \times 3_6 = 3_5(K4)_5$ , what is the value of  $k$ ?
- A. 2
- B. 1
- C. 3
- D. 4
- E. 5
28. Find P, if  $451_6 - P_7 = 305_6$
- A.  $116_7$
- B.  $62_7$
- C.  $611_7$
- D.  $142_7$
29. The sum of four numbers is  $1214_5$ . What is the average expressed in base 5?
- A. 141
- B. 411
- C. 417
- D. 114
- E. 471
30.  $(1P03)_4 = 115_{10}$ , find P.
- A. 2
- B. 0
- C. 1
- D. 4
- E. 3
31.  $(P344)_6 - (23P2)_6 = (2PP2)_6$ , find the digit P.
- A. 1
- B. 2
- C. 3
- D. 4
- E. 5
32.  $4243_5 - (12X4)_5 = Y344$ . what is the difference between X and Y?
- A. 1
- B. 2
- C. 3
- D. 4
- E. 5
33. A.
- B.
- C.
- D.
34. A.
- B.
- C.
- D.
35. A.
- B.
- C.
- D.
36. A.
- B.
- C.
- D.
37. A.
- B.
- C.
- D.
38. A.
- B.
- C.
- D.
39. A.
- B.
- C.
- D.

- |     |    |     |
|-----|----|-----|
| 40. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 51. |
| 41. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 52. |
| 42. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 53. |
| 43. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 54. |
| 44. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 55. |
| 45. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 56. |
| 46. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 57. |
| 47. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 58. |
| 48. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 59. |
| 49. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 60. |
| 50. | A. | B.  |

- |     |    |     |    |
|-----|----|-----|----|
|     | C. |     | C. |
|     | D. |     | D. |
| 61. | A. | 71. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 62. | A. | 72. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 63. | A. | 73. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 64. | A. | 74. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 65. | A. | 75. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 66. | A. | 76. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 67. | A. | 77. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 68. | A. | 78. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 69. | A. | 79. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 70. | A. | 80. | A. |
|     | B. |     | B. |
|     |    |     | C. |
|     |    |     | D. |

81. A.  
B.  
C.  
D.

82. A.  
B.  
C.  
D.

83. A.  
B.  
C.  
D.

84. A.  
B.  
C.  
D.

85. A.  
B.  
C.  
D.

86. A.  
B.  
C.  
D.

87. A.  
B.  
C.  
D.

88. A.  
B.  
C.  
D.

89. A.  
B.  
C.  
D.

90. A.  
B.  
C.  
D.

91. A.  
B.  
C.  
D.

92. A.  
B.  
C.  
D.

93. A.  
B.  
C.  
D.

94. A.  
B.  
C.  
D.

95. A.  
B.  
C.  
D.

96. A.  
B.  
C.  
D.

97. A.  
B.  
C.  
D.

98. A.  
B.  
C.  
D.

99. A.  
B.  
C.  
D.

100. A.  
B.  
C.  
D.

## Chapter 2

# Fraction and Decimals

### 2.1 Percentage Error and Approximation

#### 2.1.1 Questions

1. The sum of  $3\frac{7}{8}$  and  $1\frac{1}{3}$  is greater than the difference between  $\frac{3}{8}$  and  $1\frac{2}{3}$  by.  
A.  $3\frac{2}{3}$   
B.  $1\frac{1}{2}$   
C.  $8\frac{1}{8}$   
D.  $3\frac{11}{12}$   
E.  $5\frac{1}{4}$
2. After getting a rise of 15%, a man's new monthly salary is N 345. How much per month did he earn before the increase?  
A. N360  
B. N300  
C. N293.25  
D. N330  
E. N396.75
3. Find correct to 3 significant figures, the value of  $\sqrt{41830}$   
A. 647  
B. 2050  
C. 205  
D. 647  
E. 6470
4. 12 men complete a job in 9 days. How many men working at the same rate, would be required to complete the job in 6 days?.  
A. 24  
B. 9  
C. 8  
D. 12  
E. 18
5. Simplify  $2\frac{5}{12} - 1\frac{7}{8} \times \frac{6}{5}$ .  
A.  $\frac{11}{30}$   
B.  $\frac{9}{4}$   
C.  $\frac{1}{6}$   
D.  $\frac{5}{3}$   
E.  $\frac{13}{20}$
6. By selling an article for N45.00 a man makes a profit of 8%. For how much should he have sold it in order to make a profit of 32%?  
A. N59.00  
B. N55.00  
C. N180.00  
D. N63.00  
E. N42.00
7. Which of the following fractions is less than one-third?  
A.  $\frac{4}{11}$   
B.  $\frac{122}{383}$   
C.  $\frac{15}{46}$   
D.  $\frac{22}{63}$

- E.  $\frac{6}{25}$
8. The ratio of the price of loaf of bread to the price of a packet of sugar in 1975 was  $a : x$ . In 1980, the price of a loaf of bread went up by 25% and that of a packet of sugar by 10%. Their new ratio is now ?
- A.  $50a : 44x$   
 B.  $44a : 50x$   
 C.  $40a : 44x$   
 D.  $55a : 44x$   
 E.  $44a : 55x$
9. Simplify:  $1 + \frac{2}{3 + \frac{4}{5 + \frac{6}{7}}}$
- A.  $\frac{7}{95}$   
 B.  $\frac{177}{95}$   
 C.  $\frac{233}{151}$   
 D.  $\frac{17}{10}$   
 E.  $\frac{3}{10}$
10. Evaluate and correct to 4 decimal places  $827.51 \times 0.015$ .
- A. 124.1265  
 B. 8.8415  
 C. 12.4127  
 D. 12.4120  
 E. 124.1265
11. A micrometer is defined as one millionth of a millimeter. A length of 12,000 micrometer may be represented as
- A. 0.000012m  
 B. 0.12m  
 C. 0.00000012m  
 D. 0.0000000012m  
 E. 0.0000012m
12. The difference between  $4\frac{5}{7}$  and  $2\frac{1}{4}$  is greater than the sum of  $\frac{1}{14}$  and  $1\frac{1}{2}$  by.
- A.  $\frac{27}{28}$   
 B.  $\frac{23}{28}$   
 C.  $\frac{50}{56}$   
 D.  $\frac{48}{56}$   
 E.  $\frac{24}{48}$
13. When a dealer sells a bicycle for N81, he makes a profit of 8%. What did he pay for the bicycle.
- A. N75  
 B. N75.52  
 C. N74.52  
 D. N87.48  
 E. N73
14. A man and wife went to buy an article costing N400. The woman had 10% of the cost and the man 40% of the remainder. How much did they have altogether?
- A. N186  
 B. N184  
 C. N200  
 D. N144  
 E. N100
15. A sum of money invested at 5% per annum simple interest amount to N285.20 after 3 years. How long will it take the same sum to amount to N434.00 at  $7\frac{1}{2}\%$  per annum simple interest?
- A. 10 years  
 B. 12 years  
 C.  $7\frac{1}{2}$  years  
 D. 14 years  
 E. 5 years
16. A construction company is owned by two partners A and B and it is agreed that their profit will be divided in ratio 4:5, at the end of the year, B received N5,000 more than A. What is the total profit of the company for the year?
- A. N45,000  
 B. N30,000  
 C. N150,000  
 D. N25,000  
 E. N30,000
17. The diameter of metal rod is measured as 23.40cm to 4 significant figures. What is the maximum error in the measurement?
- A. 0.0004cm  
 B. 0.05cm  
 C. 0.005cm



- D. 0.5cm  
E. 0.45cm
18. Simplify:  $3 - \frac{2}{\frac{4}{5} + \frac{1}{2}}$
- A.  $1\frac{9}{10}$   
B.  $1\frac{3}{10}$   
C.  $1\frac{3}{4}$   
D. -1  
E. 1
19. Given that  $x : y = \frac{1}{3} : \frac{1}{2}$  and  $\psi : \theta = \frac{2}{5} : \frac{4}{7}$ , find  $x : \theta$ .
- A. 20 : 21  
B. 7 : 15  
C. 3 : 20  
D. 2 : 35  
E. 4 : 105
20. If N560 is shared in the ratio 7 : 2 : 1, what is the smallest share?
- A. N392  
B. N113.40  
C. N56.70  
D. N87.48  
E. N126.41
21. Simplify:  $\frac{1}{2} + \frac{1}{2 + \frac{1}{2 - \frac{1}{4 + \frac{1}{5}}}}$
- A.  $\frac{169}{190}$   
B.  $-\frac{1}{3}$   
C.  $\frac{13}{15}$   
D.  $-\frac{3}{4}$   
E.  $-\frac{14}{27}$
22.  $22\frac{1}{2}\%$  of the Nigerian Naira equals  $17\frac{1}{10}\%$  of a foreign currency  $M$ . What is the conversion rate of  $M$  to Naira?
- A.  $2\frac{11}{57}$  Naria  
B.  $1\frac{18}{57}$  Naria  
C.  $\frac{15}{59}$  Naria  
D.  $\frac{15}{57}$  Naria  
E.  $38\frac{1}{4}$  Naria
23. Divide the LCM of 48, 64, and 80 by their HCF.
- A. 30  
B. 48  
C. 52  
D. 20  
E. 60
24. A sum of money was invested at 8% per annum simple interest. If after 4 years the money amounts to N330.00, find the amount originally invested.
- A. N150  
B. N200  
C. N165  
D. N180  
E. N250
25.  $P$  sold his bicycle to  $Q$  at a profit of 10%.  $Q$  sold to  $R$  for N209 at a loss of 5%. How much did the bicycle cost  $P$ ?
- A. N150  
B. N205  
C. N180  
D. N196  
E. N200
26. Find the smallest number by which 252 can be multiplied to obtain a perfect square.
- A. 2  
B. 3  
C. 5  
D. 7  
E. 9
27. Find the reciprocal of:  $\frac{\frac{2}{3}}{\frac{1}{2} + \frac{1}{3}}$
- A.  $\frac{4}{5}$   
B.  $\frac{2}{5}$   
C.  $\frac{6}{9}$   
D.  $\frac{5}{4}$

- E.  $\frac{3}{4}$
28. Three boys shared some oranges, the first received  $\frac{1}{3}$  of the oranges, the second received  $\frac{2}{3}$  of the remainder, if the third boy
- 48
  - 72
  - 54
  - 42
  - 60
29. Udoh deposited N150.00 in the bank. At the end of 5 years, the simple interest on the principal was N55.00. At what rate per annum was the interest paid
- $7\frac{1}{3}\%$
  - 5%
  - 11%
  - $3\frac{1}{2}\%$
  - $4\frac{2}{5}\%$
30. A number of pencil were shared among Desmond, Florence, and Kevin in ratio 2 : 3 : 5 respectively. If Desmond got 5, how many were shared out?
- 30
  - 15
  - 25
  - 20
  - 35
31. Find the least length of a rod which can be cut into exactly equal strips, each of 40 cm or 48 cm in length.
- 240 cm
  - 480 cm
  - 360 cm
  - 120 cm
  - 480 cm
32. A rectangular lawn has an area of 1815 square yards. If its length is 50 metres, find its width in meters. Given that 1 metre equals 1.1 yard.
- 30.00 m
  - 33.00 m
  - 32.00 m
  - 39.93 m
  - 36.45 m
33. Reduce each number to two significant figures and then evaluate  $\frac{0.021741 \times 1.2047}{0.023789}$
- 0.8
  - 1.2
  - 1.1
  - 0.9
  - 0.6
34. A cinema hall contains a certain number of people. If  $27\frac{1}{2}\%$  are children,  $47\frac{1}{2}\%$  are men and 84 are women, find the number of men in the hall
- 133
  - 84
  - 63
  - 113
35. A woman buys 270 oranges for N1,800 and sells at 5 for N40. What is her profit?
- N 1,620
  - N 630
  - N 360
  - N 2,160
36. If a car travels 120km on 45 litres of petrol, how much petrol is needed for a journey of 600km?
- 720 litres
  - 225 litres
  - 960 litres
  - 160 litres
37. Simplify  $1 - \left(\frac{1}{7} \times 3\frac{1}{2}\right) / \frac{3}{4}$
- 2
  - 1
  - $\frac{1}{3}$
  - $\frac{2}{3}$
38. Evaluate:  $\frac{12.02 \times 20.06}{26.04 \times 60.06}$ , correct to 3 significant figures
- 0.154
  - 0.155
  - 0.158
  - 0.157
39. Evaluate:  $\frac{0.8 \times 0.43 \times 0.031}{0.05 \times 0.72 \times 0.021}$ , correct to 3 significant figures
- 14.1
  - 14.09
  - 14.12

- D. 14.11
40. A man bought a car for N500,000 and was able to sell it for N350,000, what was his percentage loss?
- A. 50%
- B. 30%
- C. 70%
- D. 60%
41. Simplify:  $1\frac{2}{3} + 4\frac{1}{4} + 1\frac{5}{12}$
- A.  $4\frac{1}{3}$
- B.  $4\frac{2}{3}$
- C.  $4\frac{12}{17}$
- D.  $4\frac{3}{17}$
42. A man donates 16% of his monthly net earning to the church, if it amounts to N4,500, what is his monthly income?
- A. N40,500
- B. N52,000
- C. N52,500
- D. N45,000
43. If a student measured the length of a table to be 2.30 m instead of 2.50m. What was his percentage error in measuring the length?
- A. 7%
- B. 10%
- C. 9%
- D. 8%
44. A man bought a second-hand photocopy machine for 34,000. He serviced it at a cost of N2,000 and then sold it at a profit of 15%. What was the selling price?
- A. 37,550
- B. 40,000
- C. 41,400
- D. 42,400
45. A student spent  $\frac{1}{5}$  of his allowance on books,  $\frac{1}{3}$  of the remainder on food and kept the rest for contingencies. What fraction was kept?
- A.  $\frac{8}{15}$
- B.  $\frac{4}{5}$
- C.  $\frac{2}{3}$
- D.  $\frac{7}{15}$
46. If  $p : q = \frac{2}{3} : \frac{5}{6}$  and  $\frac{3}{4} : \frac{1}{2}$ , find  $p : q : r$
- A. 12 : 15 : 10
- B. 10 : 15 : 24
- C. 9 : 10 : 15
- D. 12 : 15 : 16
47. Simplify:  $\frac{3\frac{2}{3} \times \frac{5}{6} \times \frac{2}{3}}{\frac{11}{25} \times \frac{3}{4} \times \frac{2}{27}}$
- A.  $4\frac{1}{3}$
- B. 30
- C.  $5\frac{2}{3}$
- D. 50
48. A man earns N3,500 per month out of which he spends 15% on his children's education. If he spends additional N1,950 on food, how much does he have left?
- A. N2,975
- B. N1,950
- C. N525
- D. N1025
49. Evaluate  $\frac{21}{9}$  to 3 significant figures
- A. 2.30
- B. 2.31
- C. 2.32
- D. 2.33
50. A girl share a number of apples in the ratio 5:3:2. if the highest share is 40. find the smallest share.
- A. 74
- B. 38
- C. 36
- D. 16
51. Calculate the time taken for N3,000 to earn N600 at 8% simple interest.
- A. 3 years
- B.  $2\frac{1}{2}$  years
- C.  $1\frac{1}{2}$  years
- D.  $3\frac{1}{2}$  years

52. Find the tax on an income of N20, 000 if no tax is paid on the first N10, 000 and tax is paid at N50 and in N1, 000 on the next N5, 000 and at N55 and N1000 on the remainder.
- A. N225  
B. N525  
C. N552  
D. N500
53. The time taken to do a piece of work is inversely proportional to the number of men employed. If it takes 30 men to do a piece of work in 6 days, how many men are required to do the work in 4 days?
- A. 35  
B. 45  
C. 25  
D. 60
54. Three boys shared oranges. The first received  $\frac{1}{3}$  of the oranges and the second received  $\frac{2}{3}$  of the remainder. If the third boy received the remaining 12 oranges, how much oranges did they share?
- A. 42  
B. 60  
C. 54  
D. 48
55. A farmer planted 5,000 grains of maize and harvests 5,000 cobs, each bearing 500 grains. What is the ratio of the number of grains sowed to the number harvested?
- A. 1 : 5,000  
B. 1 : 25,000  
C. 1 : 500  
D. 1 : 250,000
56. Evaluate:  $\frac{0.21 \times 0.072 \times 0.00054}{0.006 \times 1.68 \times 0.063}$
- A. 0.1286  
B. 0.01285  
C. 0.01286  
D. 0.1285
57. A man's initial salary is N540 a month and increases after a period of six months by N36 a month. Find his salary in the eighth month of the third year.
- A. 828  
B. 756  
C. 720  
D. 684
58. Find correct to 3 decimal places:  $\left(\frac{1}{0.05}\right) \div \left(\frac{1}{5.005}\right) - 0.05 \times 2.05$
- A.  
B.  
C.  
D.
59. A.  
B.  
C.  
D.
60. A.  
B.  
C.  
D.
61. A.  
B.  
C.  
D.
62. A.  
B.  
C.  
D.
63. A.  
B.  
C.  
D.
64. A.  
B.  
C.  
D.
65. A.  
B.  
C.  
D.
66. A.  
B.  
C.  
D.
67. A.  
B.  
C.

- |     |    |     |    |
|-----|----|-----|----|
|     | D. |     | D. |
| 68. | A. | 78. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 69. | A. | 79. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 70. | A. | 80. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 71. | A. | 81. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 72. | A. | 82. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 73. | A. | 83. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 74. | A. | 84. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 75. | A. | 85. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 76. | A. | 86. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 77. | A. | 87. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     |    |     | D. |
|     |    | 88. | A. |

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | D. |
|     | C. | 93. | A. |
|     | D. |     | B. |
| 89. | A. |     | C. |
|     | B. |     | D. |
|     | C. | 94. | A. |
|     | D. |     | B. |
| 90. | A. |     | C. |
|     | B. |     | D. |
|     | C. | 95. | A. |
|     | D. |     | B. |
| 91. | A. |     | C. |
|     | B. |     | D. |
|     | C. | 96. | A. |
|     | D. |     | B. |
| 92. | A. |     | C. |
|     | B. |     | D. |
|     | C. |     |    |

## 2.1.2 Solution

1. We begin by converting the mixed fractions to improper fractions,  
 $3\frac{7}{8} = \frac{31}{8}$  and  $1\frac{1}{3} = \frac{4}{3}$  and add them up.  
 Taking LCM of 8 and 3 we get 24,

$$\frac{31}{8} + \frac{4}{3} = \frac{(31 \times 3) + (8 \times 4)}{24} = \frac{93 + 32}{24} = \frac{125}{24}$$

Similarly,

$$1\frac{2}{3} - \frac{3}{8} \Rightarrow \frac{5}{3} - \frac{3}{8} = \frac{(5 \times 8) - (3 \times 3)}{24} = \frac{31}{24}$$

Now subtract  $\frac{31}{24}$  from  $\frac{125}{24}$

$$\frac{125}{24} - \frac{31}{24} = \frac{125 - 31}{24} = \frac{94}{24} = 3\frac{11}{12} \text{ (D)}$$

2. **Amount he earned before the increase** i.e his Initial Salary  
 Let initial Salary =  $x$  new salary = N345  
 So, listen He had 15% of his initial salary ( $x$ ) added to his initial earn ( $x$ )

initial salary + 15% of initial = new salary

$$x + \frac{15}{100}x = 345 \Rightarrow \frac{100x + 15x}{100} = 345$$

$$115x = 345 \times 100 \Rightarrow x = \left(\frac{345}{115}\right) \times 100$$

$$\therefore 3 \times 100 = 300 \text{ (B)}$$

**Note:** when give this:  $\frac{x \times 100}{y}$  its advisable to group in the form  $\left(\frac{x}{y}\right) \times 100$ , incase the fraction part becomes decimal the 100 only shift the decimal point.

3.

4. The **time taken (t)** to complete a job is inversely proportional to **numbers of men (n)** i.e as the number of men increase the job is done faster.

$$\text{time taken} \propto \frac{1}{\text{number of men}} \Rightarrow t \propto \frac{1}{n} \quad (2.1)$$

Removing proportionality sign

$$t = \frac{k}{n} \Rightarrow tn = k$$

Generally:  $t_1 n_1 = t_2 n_2 = \dots = t_k n_k$   
 given  $t_1 = 9, n_1 = 12, t_2 = 6$  and  $n_2 = ?$   
 Using:  $t_1 n_1 = t_2 n_2 \Rightarrow 9 \times 12 = 6 \times n_2$   
 taking the advantage that  $6 \mid 12$

$$n_2 = \left(\frac{12}{6}\right) \times 9 = 18 \text{ men (E)}$$

5. We begin by converting the mixed fractions to improper fractions,

$$2\frac{5}{12} - 1\frac{7}{8} \times \frac{6}{5} \Rightarrow \frac{29}{12} - \frac{15}{8} \times \frac{6}{5}$$

Applying BODMAS, multiplication comes before subtraction,

$$\begin{aligned} \therefore \frac{29}{12} - \left(\frac{6 \times 15}{8 \times 5}\right) &= \frac{29}{12} - \frac{90}{40} \\ &\Rightarrow \frac{29}{12} - \frac{9}{4} = \frac{29 - (9 \times 3)}{12} \\ &\Rightarrow \frac{29 - 27}{12} = \frac{2}{12} = \frac{1}{6} \text{ (C)} \end{aligned}$$

6. Given: Selling price = N45.00, Profit% = 8%.  
 Let the cost price be  $x$ .

$$\% \text{profit} = \frac{\text{Selling Price} - \text{Cost Price}}{\text{Cost Price}} \times 100$$

$$8 = \frac{45 - x}{x} \times 100 \Rightarrow 8x = 4500 - 100x$$

$$108x = 4500 \Rightarrow x = \frac{4500}{108}$$

$$\therefore \text{cost price} = \frac{4500}{108}$$

Now, the question says he had made a %profit of 32%, how much did he sell it?

Using formula, We have:

$$32 = \frac{SP - \frac{4500}{108}}{\frac{4500}{108}} \times 100 = \frac{108 \left( SP - \frac{4500}{108} \right)}{4500} \times 100$$

$$\Rightarrow 32 = \frac{108SP - 4500}{4500} \times 100$$

$$\Rightarrow \frac{32 \times 4500}{100} = 108SP - 4500$$

$$\Rightarrow SP = \frac{(32 \times 45) + 4500}{108} = \frac{5940}{108} = 55$$

$$\therefore N55.00 \text{ (B)}$$

7.

8. **In 1980:** The intial price  $a : x$  rose by 25% and 10% respectively, hence:

$$a : x \Rightarrow a + \frac{25}{100}a : x + \frac{10}{100}x$$

$$\text{Which reduces to } \frac{125}{100}a : \frac{110}{100}x \Rightarrow 125a : 110x$$

$$\text{dividing by 5 } \frac{125}{20}a : \frac{110}{20}x \Rightarrow 25a : 22x$$

$$\text{Multiplying by 2 } 50a : 44x \quad \text{(A)}$$

9. For questions of this type, it's best to start from the bottom of the continued fraction,
- Step 1:**  $5 + \frac{6}{7} \Rightarrow \frac{41}{7}$
- Step 2:**  $4 \div \frac{41}{7} \Rightarrow \frac{28}{41}$
- Step 3:**  $3 + \frac{28}{41} \Rightarrow \frac{151}{41}$
- Step 4:**  $2 \div \frac{151}{41} \Rightarrow \frac{82}{151}$
- Step 5:**  $1 + \frac{82}{151} \Rightarrow \frac{233}{151}$
- Option (C)
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.
- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.
- 74.
- 75.
- 76.



- |     |      |
|-----|------|
| 77. | 90.  |
| 78. | 91.  |
| 79. | 92.  |
| 80. | 93.  |
| 81. | 94.  |
| 82. | 95.  |
| 83. | 96.  |
| 84. | 97.  |
| 85. | 98.  |
| 86. | 99.  |
| 87. | 100. |
| 88. | 101. |
| 89. |      |



# Chapter 3

## Algebra

### 3.1 Factorization and Remainder Theorem

#### 3.1.1 Questions

1. If the function  $f$  is defined by  $f(x+2) = 2x^2 + 7x - 5$ , find  $f(-1)$ 
  - A.  $-8$
  - B.  $4$
  - C.  $10$
  - D.  $-10$
2. Factorize  $a^2x - b^2y - b^2x + a^2y$ 
  - A.  $(y-x)(a-b)(a+b)$
  - B.  $(a-b)(x+y)$
  - C.  $(x-y)(a-b)$
  - D.  $(x+y)(a-b)(a+b)$
3. if  $x-1$  and  $x+1$  are both factors of the equation:  $x^3 + px^2 + qx + 6 = 0$ , evaluate  $p$  and  $q$ 
  - A.  $-6, -1$
  - B.  $1, -1$
  - C.  $6, 1$
  - D.  $6, -6$
4. if  $f(x) = \frac{1}{x-1} + \frac{x-1}{x^2-1}$ , find  $f(1-x)$ 
  - A.  $\frac{1}{x} + \frac{1}{x-2}$
  - B.  $-\frac{1}{x} - \frac{1}{x-2}$
  - C.  $x + \frac{1}{2x-1}$
  - D.  $\frac{1}{x} + \frac{1}{x^2-1}$
  - E.  $-\frac{1}{x} - \frac{1}{2x-1}$
5. Multiply  $(x+3y+5)$  by  $(2x^2+5y+2)$ 
  - A.  $2x^3+3x^2y+10xy^2+13y+10x^2+2x+10$
  - B.  $2x^3+2x^2y+10xy+10y^2+31y+5x^2+2x+10$
  - C.  $2x^3+6x^2y+5xy+10y^2+13y+5x^2+2x+10$
  - D.  $2x^3+6x^2y+5xy+15y^2+31y+5x^2+2x+10$
  - E.  $2x^3+3x^2y+5xy+10y^2+13y+5x^2+2x+10$
6. If  $kx^3+10x^2+lx-3$  is divisible by  $(x-1)$  and if when it is divided by  $(x+2)$  the remainder is  $27$ , find the constant  $k$  and  $l$ .
  - A.
  - B.
  - C.
  - D.
7. Factorize  $3x^3+4x^2-13x+6$  completely, given that  $x-1$  is a factor
  - A.  $(x-1)(x-3)(x+2)$
  - B.  $(x-1)(x-3)(3x+2)$
  - C.  $(x-1)(x-2)(x+3)$
  - D.  $(x-1)(x+3)(3x+2)$
  - E.  $(x-1)(x+3)(3x-2)$
8. Multiply  $x^2+x+1$  by  $x^2-x+1$ 
  - A.  $x^4+3x^2+x+1$
  - B.  $x^4+4x^2-6x+1$
  - C.  $x^4+4x^2+1$
  - D.  $x^4-x^3-x^2+x+1$
  - E.  $x^4-6x^2-4x+1$
9. If  $x=1$  is a root of the equation:  $x^3-2x^2-5x+6$ , find the other roots.
  - A.  $-3$  and  $2$
  - B.  $1$  and  $3$
  - C.  $-2$  and  $2$

- D. 3 and -2  
E. -3 and 1
10. If  $x + 2$  and  $x - 1$  are factors of the expression:  $lx^3 + 2kx^2 + 24$ , find the values of  $l$  and  $k$   
A.  $l = -6, k = -9$   
B.  $l = -2, k = -1$   
C.  $l = -2, k = 1$   
D.  $l = 0, k = 1$   
E.  $l = 6, k = 0$
11. Factorize completely:  $81a^4 - 16b^4$   
A.  $(3a + 2b)(2a - 3b)(9a^2 + 4b^2)$   
B.  $(3a - 2b)(2a - 3b)(9a^2 - 4b^2)$   
C.  $(3a - 2b)(3a - 2b)(9a^2 + 4b^2)$   
D.  $(3a - 2b)(2a - 3b)(4a^2 - 9b^2)$   
E.  $(3a - 2b)(3a + 2b)(9a^2 + 4b^2)$
12. The factor which is common to all three binomial expressions:  $4a^2 - 9b^2, 8a^2 + 27b^3, (4a + 6b)^2$   
A.  $4a - 6b$   
B.  $4a + 6b$   
C.  $2a - 3b$   
D.  $2a + 3b$   
E.  $3a - 2b$
13. If  $x - 2$  and  $x + 1$  are factors of the expression:  $x^3 + px^2 + qx + 1$   
A. -3  
B. 0  
C.  $-\frac{17}{3}$   
D.  $-\frac{2}{3}$   
E. 3
14. The factors of  $9 - (x^2 - 3x - 1)^2$  are.  
A.  $(x - 4)(x - 1)(x - 1)(x + 2)$   
B.  $(x - 4)(x + 1)(x - 2)(x - 1)$   
C.  $(x - 2)(x + 2)(x + 1)(x + 4)$   
D.  $(x - 2)(x + 2)(x + 1)(x - 1)$   
E.  $(x - 4)(x - 3)(x - 2)(x + 1)$
15. If  $f(x - 2) = 4x^2 + x + 7$  find  $f(1)$   
A. 27  
B. 7  
C. 17  
D. 46  
E. 12
16. If  $g(y) = \frac{y - 3}{11} + \frac{11}{y^2 - 9}$  what is  $g(y + 3)$   
A.  $\frac{y}{11} + \frac{11}{y(y + 5)}$   
B.  $\frac{y + 30}{11} + \frac{11}{y(y + 3)}$   
C.  $\frac{y}{11} + \frac{11}{y(y + 3)}$   
D.  $\frac{y + 3}{11} + \frac{11}{y(y - 6)}$
17. Factorize completely  $3a + 125a^3$   
A.  $(2a + 5x)(4 + 10ax + 25ax^2)$   
B.  $(2a + 5x^2)(4 + 25ax)$   
C.  $a(2 + 5x)(4 - 10x + 25ax^2)$   
D.  $a(2 + 5x)(4 + 10ax + 25ax^2)$
18. Factorize  $x^2 + 2a + ax + 2x$   
A.  $(x^2 - 1)(x + a)$   
B.  $(x + 2)(x + a)$   
C.  $(x + 2a)(x + 3)$   
D.  $(x + 2a)(x - 1)$
19. The graphical method of solving the equation:  $x^3 + 3x^2 + 4x - 28 = 0$  is by drawing the graphs of the curves  
A.  $y = x^3$  and  $y = 3x^2 + x - 28$   
B.  $y = x^3 + 3x^2 + 4x$  and  $y$   
C.  $y = x^3 + 3x^2 + 4x - 28$  and the line  $y = \frac{28}{x}$   
D.  $y = x^2 + 3x + 4$  and  $y = \frac{28}{x}$   
E.  $y = x^2 + 3x + 4$  and line  $y = 28x$
20. Factorize  $(4a + 3)^2 - (3a - 2)^2$   
A.  $(x + 2a)(x - 1)$   
B.  $(x + 1)(x + 2a)$   
C.  $(x + 2)(x + a)$   
D.  $(x^2 - 1)(x + a)$
21. If  $x^3 - 12x - 16 = 0$  has  $x - 2$  as a solution, then the equation has  
A. 3 roots all different  
B.  $x - 4$  as a solution also  
C. 3 roots all equal  
D. 3 roots with two equal and the third different  
E. only one root
22. The expression:  $x^3 - 4x^2 + cx + d$  is such that  $x + 1$  is a factor and its value is 1 when  $x$  is -2. find  $c$  and  $d$   
A.  $c = -4$  and  $d = 9$   
B.  $c = 20$  and  $d = 9$

- C.  $c = -20$  and  $d = 15$   
 D.  $c = -20$  and  $d = -15$   
 E.  $c = 20$  and  $d = -15$
23. What factor is common to all the expressions:  
 $x + 1$ ,  $2x^2 + x + 1$  and  $x^2 - 1$   
 A.  $x + 1$   
 B. 1  
 C. No common factor  
 D.  $2x - 1$   
 E.  $x$
24. Factorize completely:  $(x^2 + x)^2 - (2x + 2)^2$   
 A.  $(x + y)(x + 2)(x - 2)$   
 B.  $(x + 1)^2(x + 2)(x - 2)$   
 C.  $(x + y)^2(y - 2)^2$   
 D.  $(x + 1)^2(x + 2)^2$
25. if  $f(x) = 2x^2 + 5x + 3$ , find  $f(x + 1)$   
 A.  $2x^2 - x + 10$   
 B.  $2x^2 - x$   
 C.  $4x^2 + 3x + 12$   
 D.  $4x^2 + 3x + 2$
26. If one factor of  $x^3 - 8^{-1}$  is  $x - 2^{-1}$ , the other factor is  
 A.  $x^2 + 2^{-1}x - 4^{-1}$   
 B.  $x^2 + 2^{-1}x - 4^{-1}$   
 C.  $x^2 - 2^{-1}x - 4^{-1}$   
 D.  $x^2 + 4^{-1}x - 2^{-1}$
27. Factorize  $9(x + y)^2 - 4(x - y)^2$   
 A.  $(x + y)(5x + y)$   
 B.  $(x + y)^2$   
 C.  $(5(x + y)^2)$   
 D.  $(x + 5y)(5x + y)$
28. Factorize  $4a^2 - 12ab - c^2 + 9b^2$   
 A.  $(2a + 3b - c)(2a + 3b + c)$   
 B.  $4a(a - 3b) + (3b - c)^2$   
 C.  $(2a - 3b - c)(2a - 3b + c)$   
 D.  $4a(a - 3b) + (3b + c)^2$
29. What are  $k$  and  $l$  respectively if:  $\frac{1}{2}(3y - 4x)^2 = (8x^2 + kxy + ly^2)$   
 A. 12,  $\frac{9}{2}$   
 B. -12,  $\frac{9}{2}$   
 C. 6, 9  
 D. -6, 9
30. if  $f(x - 4) = x^2 + 2x + 3$ , find  $f(2)$   
 A. 11  
 B. 6  
 C. 51  
 D. 27
31. Factorize completely:  $y^3 - 4xy + xy^3 - 4y$   
 A.  $y(1 - x)(y + 2)(y - 2)$   
 B.  $y(1 + x)(y - 2)(y - 2)$   
 C.  $(y + xy)(y + 2)(y - 2)$   
 D.  $(y + xy)(y + 2)(y - 2)$
32. If  $g(x) = x^2 + 3x + 4$ , find  $g(x + 1) - g(x)$   
 A.  $2(x + 2)$   
 B.  $(x + 2)$   
 C.  $(2x + 1)$   
 D.  $x^2 + 4$
33. Factorize:  $m^3 - 2m^2 - m + 2$   
 A.  $(m + 1)(m + 1)(m + 2)$   
 B.  $(m^2 + 1)(m - 2)$   
 C.  $(m^2 + 2)(m - 1)$   
 D.  $(m - 2)(m + 1)(m - 1)$
34. Which of the following is a factor of  $rs + tr - pt - ps$   
 A.  $(p - s)$   
 B.  $(r - p)$   
 C.  $(s - p)$   
 D.  $(r + p)$
35. If  $x + 1$  is a factor of:  $x^3 + 3x^2 + kx + 4$ , find the value of  $k$   
 A. -6  
 B. 6  
 C. 8  
 D. -8
36. Factorize:  $9p^2 - q^2 + 6pr - 9r^2$   
 A.  $(3p - 3q + r)(3p - q)$   
 B.  $(6p - 3q - 3r)(3p - q - 4r)$   
 C.  $(3p - 3q + r)(3p - q - 3r)$   
 D.
37. A.  
 B.  
 C.  
 D.
38. A.

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 39. | A. | 49. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 40. | A. | 50. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 41. | A. | 51. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 42. | A. | 52. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 43. | A. | 53. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 44. | A. | 54. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 45. | A. | 55. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 46. | A. | 56. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 47. | A. | 57. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 48. | A. | 58. | A. |
|     |    |     | B. |
|     |    |     | C. |

- |     |    |     |    |
|-----|----|-----|----|
|     | D. |     | D. |
| 59. | A. | 69. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 60. | A. | 70. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 61. | A. | 71. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 62. | A. | 72. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 63. | A. | 73. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 64. | A. | 74. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 65. | A. | 75. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 66. | A. | 76. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 67. | A. | 77. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 68. | A. | 78. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     |    |     | D. |
|     |    | 79. | A. |

- B.  
C.  
D.  
80. A.  
B.  
C.  
D.  
81. A.  
B.  
C.  
D.  
82. A.  
B.  
C.  
D.  
83. A.  
B.  
C.  
D.  
84. A.  
B.  
C.  
D.  
85. A.  
B.  
C.  
D.  
86. A.  
B.  
C.  
D.  
87. A.  
B.  
C.  
D.  
88. A.  
B.  
C.  
D.  
89. A.  
B.  
C.
- D.  
90. A.  
B.  
C.  
D.  
91. A.  
B.  
C.  
D.  
92. A.  
B.  
C.  
D.  
93. A.  
B.  
C.  
D.  
94. A.  
B.  
C.  
D.  
95. A.  
B.  
C.  
D.  
96. A.  
B.  
C.  
D.  
97. A.  
B.  
C.  
D.  
98. A.  
B.  
C.  
D.  
99. A.  
B.  
C.  
D.



**3.1.2 Solution**

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.

- 74.
- 75.
- 76.
- 77.
- 78.
- 79.
- 80.
- 81.
- 82.
- 83.
- 84.
- 85.
- 86.
- 87.
- 88.
- 89.
- 90.
- 91.
- 92.
- 93.
- 94.
- 95.
- 96.
- 97.
- 98.
- 99.
- 100.

## 3.2 Indices and Standard Form

### 3.2.1 Questions

1. A.  
B.  
C.  
D.
2.  $\frac{1.28 * 10^4}{6.4 * 10^2}$  equals  
A.  
B.  
C.  
D.
3. A.  
B.  
C.  
D.
4. A.  
B.  
C.  
D.
5. A.  
B.  
C.  
D.
6. A.  
B.  
C.  
D.
7. A.  
B.  
C.  
D.
8. A.  
B.  
C.  
D.
9. A.  
B.  
C.  
D.
10. A.  
B.  
C.  
D.
11. A.  
B.  
C.  
D.
12. A.  
B.  
C.  
D.
13. A.  
B.  
C.  
D.
14. A.  
B.  
C.  
D.
15. A.  
B.  
C.  
D.
16. A.  
B.  
C.  
D.
17. A.  
B.  
C.  
D.
18. A.  
B.  
C.  
D.
19. A.  
B.

- |     |    |     |    |
|-----|----|-----|----|
|     | C. |     | C. |
|     | D. |     | D. |
| 20. | A. | 30. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 21. | A. | 31. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 22. | A. | 32. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 23. | A. | 33. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 24. | A. | 34. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 25. | A. | 35. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 26. | A. | 36. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 27. | A. | 37. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 28. | A. | 38. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 29. | A. | 39. | A. |
|     | B. |     | B. |
|     |    |     | C. |
|     |    |     | D. |

- |     |    |     |
|-----|----|-----|
| 40. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 51. |
| 41. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 52. |
| 42. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
| 43. | A. | 53. |
|     | B. | A.  |
|     | C. | B.  |
|     | D. | C.  |
| 44. | A. | D.  |
|     | B. | 54. |
|     | C. | A.  |
|     | D. | B.  |
| 45. | A. | C.  |
|     | B. | D.  |
|     | C. | 55. |
|     | D. | A.  |
| 46. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 56. |
| 47. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
| 48. | A. | 57. |
|     | B. | A.  |
|     | C. | B.  |
|     | D. | C.  |
| 49. | A. | D.  |
|     | B. | 58. |
|     | C. | A.  |
|     | D. | B.  |
| 50. | A. | C.  |
|     |    | D.  |
|     |    | 59. |
|     |    | A.  |
|     |    | B.  |
|     |    | C.  |
|     |    | D.  |
|     |    | 60. |
|     |    | A.  |
|     |    | B.  |

- |     |    |     |    |
|-----|----|-----|----|
|     | C. |     | C. |
|     | D. |     | D. |
| 61. | A. | 71. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 62. | A. | 72. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 63. | A. | 73. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 64. | A. | 74. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 65. | A. | 75. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 66. | A. | 76. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 67. | A. | 77. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 68. | A. | 78. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 69. | A. | 79. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 70. | A. | 80. | A. |
|     | B. |     | B. |
|     |    |     | C. |
|     |    |     | D. |

81. A.  
B.  
C.  
D.

82. A.  
B.  
C.  
D.

83. A.  
B.  
C.  
D.

84. A.  
B.  
C.  
D.

85. A.  
B.  
C.  
D.

86. A.  
B.  
C.  
D.

87. A.  
B.  
C.  
D.

88. A.  
B.  
C.  
D.

89. A.  
B.  
C.  
D.

90. A.  
B.  
C.  
D.

91. A.  
B.  
C.  
D.

92. A.  
B.  
C.  
D.

93. A.  
B.  
C.  
D.

94. A.  
B.  
C.  
D.

95. A.  
B.  
C.  
D.

96. A.  
B.  
C.  
D.

97. A.  
B.  
C.  
D.

98. A.  
B.  
C.  
D.

99. A.  
B.  
C.  
D.

100. A.  
B.  
C.  
D.



# Chapter 4

## Geometry

### 4.1

#### 4.1.1 Questions

- |       |        |
|-------|--------|
| 1. A. | D.     |
| B.    | 8. A.  |
| C.    | B.     |
| D.    | C.     |
| 2. A. | D.     |
| B.    | 9. A.  |
| C.    | B.     |
| D.    | C.     |
| 3. A. | D.     |
| B.    | 10. A. |
| C.    | B.     |
| D.    | C.     |
| 4. A. | D.     |
| B.    | 11. A. |
| C.    | B.     |
| D.    | C.     |
| 5. A. | D.     |
| B.    | 12. A. |
| C.    | B.     |
| D.    | C.     |
| 6. A. | D.     |
| B.    | 13. A. |
| C.    | B.     |
| D.    | C.     |
| 7. A. | D.     |
| B.    | 14. A. |
| C.    | B.     |
|       | C.     |

- |     |    |     |    |
|-----|----|-----|----|
|     | D. |     | D. |
| 15. | A. | 25. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 16. | A. | 26. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 17. | A. | 27. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 18. | A. | 28. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 19. | A. | 29. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 20. | A. | 30. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 21. | A. | 31. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 22. | A. | 32. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 23. | A. | 33. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 24. | A. | 34. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     |    |     | D. |
|     |    | 35. | A. |

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 36. | A. | 46. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 37. | A. | 47. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 38. | A. | 48. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 39. | A. | 49. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 40. | A. | 50. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 41. | A. | 51. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 42. | A. | 52. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 43. | A. | 53. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 44. | A. | 54. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 45. | A. | 55. | A. |
|     |    |     | B. |
|     |    |     | C. |

- D.
56. A.  
B.  
C.  
D.
57. A.  
B.  
C.  
D.
58. A.  
B.  
C.  
D.
59. A.  
B.  
C.  
D.
60. A.  
B.  
C.  
D.
61. A.  
B.  
C.  
D.
62. A.  
B.  
C.  
D.
63. A.  
B.  
C.  
D.
64. A.  
B.  
C.  
D.
65. A.  
B.  
C.
- D.
66. A.  
B.  
C.  
D.
67. A.  
B.  
C.  
D.
68. A.  
B.  
C.  
D.
69. A.  
B.  
C.  
D.
70. A.  
B.  
C.  
D.
71. A.  
B.  
C.  
D.
72. A.  
B.  
C.  
D.
73. A.  
B.  
C.  
D.
74. A.  
B.  
C.  
D.
75. A.  
B.  
C.  
D.
76. A.

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 77. | A. | 87. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 78. | A. | 88. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 79. | A. | 89. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 80. | A. | 90. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 81. | A. | 91. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 82. | A. | 92. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 83. | A. | 93. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 84. | A. | 94. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 85. | A. | 95. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 86. | A. | 96. | A. |
|     |    |     | B. |
|     |    |     | C. |

- D.
97. A.  
B.  
C.  
D.
98. A.  
B.  
C.  
D.
99. A.  
B.  
C.  
D.
100. A.  
B.  
C.  
D.

**4.1.2 Solution**

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.



- 74.
- 75.
- 76.
- 77.
- 78.
- 79.
- 80.
- 81.
- 82.
- 83.
- 84.
- 85.
- 86.
- 87.
- 88.
- 89.
- 90.
- 91.
- 92.
- 93.
- 94.
- 95.
- 96.
- 97.
- 98.
- 99.
- 100.

## 4.2 Co-ordinate Geometry

### 4.2.1 Questions

1. A.  
B.  
C.  
D.
2. A.  
B.  
C.  
D.
3. A.  
B.  
C.  
D.
4. A.  
B.  
C.  
D.
5. A.  
B.  
C.  
D.
6. A.  
B.  
C.  
D.
7. A.  
B.  
C.  
D.
8. A.  
B.  
C.  
D.
9. A.  
B.  
C.  
D.
10. A.
- B.
- C.
- D.
11. A.  
B.  
C.  
D.
12. A.  
B.  
C.  
D.
13. A.  
B.  
C.  
D.
14. A.  
B.  
C.  
D.
15. A.  
B.  
C.  
D.
16. A.  
B.  
C.  
D.
17. A.  
B.  
C.  
D.
18. A.  
B.  
C.  
D.
19. A.  
B.  
C.  
D.

- |     |    |     |
|-----|----|-----|
| 20. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 31. |
| 21. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 32. |
| 22. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
| 23. | A. | 33. |
|     | B. | A.  |
|     | C. | B.  |
|     | D. | C.  |
| 24. | A. | D.  |
|     | B. | 34. |
|     | C. | A.  |
|     | D. | B.  |
| 25. | A. | C.  |
|     | B. | D.  |
|     | C. | 35. |
|     | D. | A.  |
| 26. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 36. |
| 27. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
| 28. | A. | 37. |
|     | B. | A.  |
|     | C. | B.  |
|     | D. | C.  |
| 29. | A. | D.  |
|     | B. | 38. |
|     | C. | A.  |
|     | D. | B.  |
| 30. | A. | C.  |
|     |    | D.  |
|     |    | 39. |
|     |    | A.  |
|     |    | B.  |
|     |    | C.  |
|     |    | D.  |
|     |    | 40. |
|     |    | A.  |
|     |    | B.  |

- |     |    |     |    |
|-----|----|-----|----|
|     | C. |     | C. |
|     | D. |     | D. |
| 41. | A. | 51. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 42. | A. | 52. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 43. | A. | 53. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 44. | A. | 54. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 45. | A. | 55. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 46. | A. | 56. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 47. | A. | 57. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 48. | A. | 58. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 49. | A. | 59. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 50. | A. | 60. | A. |
|     | B. |     | B. |
|     |    |     | C. |
|     |    |     | D. |

- |     |    |     |
|-----|----|-----|
| 61. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 72. |
| 62. | A. | B.  |
|     | B. | C.  |
|     | C. | D.  |
|     | D. | 73. |
| 63. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 74. |
| 64. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 75. |
| 65. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 76. |
| 66. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 77. |
| 67. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 78. |
| 68. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 79. |
| 69. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 80. |
| 70. | A. | A.  |
|     | B. | B.  |
|     | C. | C.  |
|     | D. | D.  |
|     |    | 81. |
| 71. | A. | A.  |
|     |    | B.  |

- C.  
D.
82. A.  
B.  
C.  
D.
83. A.  
B.  
C.  
D.
84. A.  
B.  
C.  
D.
85. A.  
B.  
C.  
D.
86. A.  
B.  
C.  
D.
87. A.  
B.  
C.  
D.
88. A.  
B.  
C.  
D.
89. A.  
B.  
C.  
D.
90. A.  
B.  
C.  
D.
91. A.
- B.  
C.  
D.
92. A.  
B.  
C.  
D.
93. A.  
B.  
C.  
D.
94. A.  
B.  
C.  
D.
95. A.  
B.  
C.  
D.
96. A.  
B.  
C.  
D.
97. A.  
B.  
C.  
D.
98. A.  
B.  
C.  
D.
99. A.  
B.  
C.  
D.
100. A.  
B.  
C.  
D.

**4.2.2 Solution**

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.



- 74.
- 75.
- 76.
- 77.
- 78.
- 79.
- 80.
- 81.
- 82.
- 83.
- 84.
- 85.
- 86.
- 87.
- 88.
- 89.
- 90.
- 91.
- 92.
- 93.
- 94.
- 95.
- 96.
- 97.
- 98.
- 99.
- 100.



# Chapter 5

## Calculus

### 5.1 Differentiation

#### 5.1.1 Questions

1. The minimum point on the curve  $y = x^2 - 6x + 5$  is at?  
A. (1,5)  
B. (2,3)  
C. (3,4)  
D. (-3,4)  
E. (3,-4)
2. At what value of  $x$  is the function  $y = x^2 + x + 1$  minimum?  
A. -1  
B.  $-\frac{1}{2}$   
C.  $\frac{1}{2}$   
D. 1
3. At what value of  $x$  is the function  $y = x^2 - 2x - 3$  minimum?  
A. 1  
B. -1  
C. -4  
D. 4
4. Find the maximum value of  $y = x^2 - 2x - 3$   
A. -4  
B. -1  
C. 1  
D. 4
5. Find the maximum value of  $y = 3x^2 - x^3$   
A. 2  
B. 4  
C. 6  
D. 0
6. Find the minimum value of  $y = x^3 + x^2 - x + 1$   
A. -1  
B. 1  
C. 2  
D. -2
7. Find the value of  $x$  for which the function  $f(x) = 2x^3 - x^2 - 4x + 4$  has a maximum value.  
A.  $\frac{2}{3}$   
B. 1  
C. -1  
D.  $-\frac{2}{3}$
8. Find the value of  $x$  for which the function  $f(x) = 3x^3 - 9x^2$  is minimum  
A. 2  
B. 0  
C. 5  
D. 3
9. Find the maximum value of the function  $f(x) = 2 + x - x^2$   
A.  $\frac{9}{4}$   
B.  $\frac{7}{4}$   
C.  $\frac{3}{2}$   
D.  $\frac{1}{2}$
10. Find the maximum value of  $y$  in the equation:  
 $y = 1 - 2 - 3x^2$

- A.  $\frac{4}{3}$   
 B.  $\frac{5}{4}$   
 C.  $\frac{3}{4}$   
 D.  $\frac{5}{3}$
11. The minimum value of  $y$  in the equation:  $y = x^2 - 6x + 8$  is  
 A. 8  
 B. 3  
 C. 0  
 D. -1
12. Obtain the maximum value of the function:  
 $f(x) = x^3 - 12x + 11$   
 A. -5  
 B. -2  
 C. 2  
 D. 27
13. Find the value of  $h$  if the maximum value of  $y = 1 + hx - 3x^2$  is 13.  
 A. 10  
 B. 11  
 C. 12  
 D. 13
14. A trader realizes  $10x - x^2$  naira profit from the sale of  $x$  bags of corn. How many bags will give him the maximum profit?  
 A. 4  
 B. 5  
 C. 6  
 D. 7
15. Find the value of  $x$  for which the function  $y = x^3 - x$  has a minimum value.  
 A.  $\frac{\sqrt{3}}{3}$   
 B.  $-\frac{\sqrt{3}}{3}$   
 C.  $\sqrt{3}$   
 D.  $-\sqrt{3}$
16. If  $f(x) = x^2 - 2x - 3$ , find the least value of  $f(x)$  and the corresponding value of  $x$ .  
 A.  $f(x) = -3, x = 1$   
 B.  $f(x) = -3, x = 3$   
 C.  $f(x) = 1, x = -4$   
 D.  $f(x) = 1, x = -4$
17. If  $y = 3 \cos\left(\frac{x}{3}\right)$ , find  $\frac{dy}{dx}$  when  $x = \frac{3\pi}{2}$ .  
 A. -1  
 B. 1  
 C. 2  
 D. 3
18. What is the rate of change of the volume  $v$  of a hemisphere with respect to its radius  $r$  when  $r = 2$ ?  
 A.  $2\pi$   
 B.  $4\pi$   
 C.  $8\pi$   
 D.  $16\pi$
19. If  $y = (1 - 2x)^3$ , find the value of  $\frac{dy}{dx}$  at  $x = -1$ .  
 A. 22  
 B. 57  
 C. -6  
 D. -54
20. Find the derivative of  $y = \sin(2x^3 + 3x - 4)$ .  
 A.  $\cos(2x^2 + 3x - 4)$   
 B.  $-\cos(2x^2 + 3x - 4)$   
 C.  $-(6x^2 + 3)\cos(2x^2 + 3x - 4)$   
 D.  $(6x^2 + 3)\cos(2x^2 + 3x - 4)$
21. The radius  $r$  of a circular disc is increasing at the rate of 0.5 cm/sec. At what rate is the area of the disc increasing when its radius is 6 cm?  
 A.  $3\pi \text{ cm}^2/\text{sec}$   
 B.  $18\pi \text{ cm}^2/\text{sec}$   
 C.  $6\pi \text{ cm}^2/\text{sec}$   
 D.  $36\pi \text{ cm}^2/\text{sec}$
22. Find  $\frac{dy}{dx}$ , if  $y = \cos x$ .  
 A.  $\sin x$   
 B.  $-\sin x$   
 C.  $\tan x$   
 D.  $-\tan x$
23. Differentiate:  $(\cos \theta - \sin \theta)^2$  with respect to  $\theta$ .  
 A.  $1 - 2 \cos 2\theta$   
 B.  $-2 \sin 2\theta$   
 C.  $-2 \cos 2\theta$   
 D.  $1 - 2 \sin 2\theta$
24. Differentiate:  $\left(x^2 + \frac{1}{x}\right)^2$  with respect to  $x$ .  
 A.  $4x^3 - 2 + \frac{2}{x^3}$

- B.  $4x^3 - 2 - \frac{2}{x^3}$   
 C.  $4x^3 - 4x - \frac{2}{x}$   
 D.  $4x^3 - 3x + \frac{2}{x}$
25. Find the point  $x, y$  on the Euclidean plane where the curve  $y = 2x^2 - 2x + 3$  has 2 as the gradient.  
 A. (1, 4)  
 B. (2, 2)  
 C. (3, 4)  
 D. (3, 2)
26. For what value of  $x$  is the tangent to the curve  $y = x^2 - 4x + 3$  parallel to the  $x$ -axis?  
 A. 0  
 B. 1  
 C. 2  
 D. 3
27. If  $y = x \sin x$ , find  $\frac{d^2y}{dx^2}$ .  
 A.  $2 \cos x - \sin x$   
 B.  $\sin x + \cos x$   
 C.  $\sin x - \cos x$   
 D.  $\cos x - 2 \sin x$
28. Differentiate:  $\frac{6x^3 - 5x^2 + 1}{3x^2}$  with respect to  $x$   
 A.  $2 + \frac{2}{3x^3}$   
 B.  $2 + \frac{1}{6x}$   
 C.  $\sin x - \cos x$   
 D.  $\cos x - 2 \sin x$
29. If  $y = (1 + x)^2$ , find  $\frac{dy}{dx}$ .  
 A.  $x + 1$   
 B.  $2x - 1$   
 C.  $2 + 2x$   
 D.  $1 + 2x$
30. Differentiate:  $3x^3 + 2x^2 + 3x + 1$  with respect to  $x$   
 A.  $9x^2 + 4x + 3$   
 B.  $9x^2 + 4x - 3$   
 C.  $9x^2 - 4x - 3$   
 D.  $9x^2 - 4x + 3$
31. Differentiate:  $\frac{2}{3}x^3 - \frac{4}{x}$   
 A.  $2x^2 + \frac{4}{x^2}$
- B.  $2x^2 - \frac{4}{x}$   
 C.  $3x^2 - \frac{4}{x}$   
 D.  $3x^2 + \frac{4}{x^2}$
32. Find the derivative of  $\frac{\sin x}{\cos x}$   
 A.  $\tan x \cos x$   
 B.  $\csc x \sec x$   
 C.  $\sec^2 x$   
 D.  $\cot^2 x$
33. If  $y = x^2 - 3x + 4$ , find  $\frac{dy}{dx}$  at  $x = 5$ .  
 A. 9  
 B. 7  
 C. 5  
 D. 3
34. If  $y = 2x \cos 2x - \sin 2x$ , find  $\frac{dy}{dx}$  when  $x = \frac{\pi}{4}$ .  
 A. 9  
 B. 7  
 C. 5  
 D. 3
35. If  $y = 3 \cos 4x$ , find  $\frac{dy}{dx}$   
 A.  $-24 \sin 4x$   
 B.  $12 \sin 4x$   
 C.  $-12 \sin 4x$   
 D.  $6 \sin 8x$
36. Find the derivative of  $(2 + 3x)(1 - x)$  with respect to  $x$ .  
 A.  $6x - 1$   
 B.  $1 - 6x$   
 C.  $-3$   
 D. 6
37. Find  $\frac{dy}{dx}$ , if  $y = 3x^3 + 2x^2 + 3x + 1$ .  
 A.  $9x^2 + 4x + 3$   
 B.  $9x^2 + 4x - 3$   
 C.  $9x^2 - 4x + 3$   
 D.  $9x^2 - 4x - 3$
38. If  $y = 2x^3 + 6x^2 + 6x + 1$ , find  $\frac{dy}{dx}$ .  
 A.  $6x^2 + 12x + 1$   
 B.  $6x^2 - 12x + 1$   
 C.  $6x^2 + 12x + 6$   
 D.  $6x^2 + 6x + 6$
39. Find the derivative of  $y = \left(\frac{1}{3}x + 6\right)^2$ .

- A.  $2\left(\frac{1}{3}x + 6\right)$   
 B.  $\frac{2}{3}\left(\frac{1}{3}x + 6\right)$   
 C.  $\frac{1}{3}\left(\frac{1}{3}x + 6\right)^2$   
 D.  $\frac{2}{3}\left(\frac{1}{3}x + 6\right)^2$
40. If  $y = x^2 - 3x + 4$ , find  $\frac{dy}{dx}$  at  $x = 5$ .  
 A. 9  
 B. 7  
 C. 5  
 D. 3
41. If  $y = x^2 + \sqrt{x}$ , find  $\frac{dy}{dx}$ .  
 A.  $2x - \frac{1}{2}x^{\frac{1}{2}}$   
 B.  $2x - \frac{1}{2}x^{-\frac{1}{2}}$   
 C.  $2x + x^{-\frac{1}{2}}$   
 D.  $2x + \frac{1}{2}x^{-\frac{1}{2}}$
42. Find  $\frac{dy}{dx}$ , if  $y = \frac{2}{3}x^3 - \frac{4}{x}$   
 A.  $3x^2 - \frac{4}{x}$   
 B.  $3x^2 + \frac{4}{x^2}$   
 C.  $2x^2 - \frac{4}{x}$   
 D.  $2x^2 + \frac{4}{x^2}$
43. If  $y = \cos(3x)$ , find  $\frac{dy}{dx}$ .  
 A.  $\frac{1}{3} \sin(3x)$   
 B.  $3 \sin(3x)$   
 C.  $-\frac{1}{3} \sin(3x)$   
 D.  $-3 \sin(3x)$
44. Find  $\frac{dy}{dx}$ , if  $y = \cos x$   
 A.  $\sin x$   
 B.  $-\sin x$   
 C.  $\tan x$   
 D.  $-\tan x$
45. Find the slope of the curve:  $y = 2x^3 + 5x - 3$  at  $(1, 4)$ .  
 A. 4  
 B. 6  
 C. 7  
 D. 9
46. Find the derivative of  $y = \sin^2(5x)$  with respect to  $x$ .  
 A.  $5 \sin(5x) \cos(5x)$   
 B.  $2 \sin(5x) \cos(5x)$   
 C.  $15 \sin(5x) \cos(5x)$   
 D.  $10 \sin(5x) \cos(5x)$
47. The slope of the tangent to the curve:  $y = 3x^2 - 2x + 5$  at the point  $(1, 6)$  is  
 A. 1  
 B. 4  
 C. 5  
 D. 6
48. If the gradient of the curve  $y = 2kx^2 + x + 1$  at  $x = 1$  is 9, find the value of  $k$   
 A. 2  
 B. -2  
 C. 4  
 D. -4
49. The distance travelled by a particle from a fixed point is given as  $s = t^3 - t^2 - t + 5$  cm. Find the minimum distance that the particle can cover from the fixed point.  
 A. 2.3 cm  
 B. 4.0 cm  
 C. 5.2 cm  
 D. 6.0 cm
50. Differentiate  $(2x + 5)^2(x - 4)$  with respect to  $x$ .  
 A.  $4(2x + 5)(x - 4)$   
 B.  $4(2x + 5)(4x - 3)$   
 C.  $(2x + 5)(6x - 11)$   
 D.  $(2x + 5)(2x - 13)$
51. Find the rate of change of the volume of  $v$  of a sphere with respect to its radius  $r$  when  $r = 1$   
 A.  $24\pi$   
 B.  $12\pi$   
 C.  $4\pi$   
 D.  $8\pi$
52. If  $y = 2x \cos(2x) - \sin(2x)$ , find  $\frac{dy}{dx}$  when  $x = \frac{\pi}{4}$   
 A.  $\frac{\pi}{4}$   
 B.  $\frac{\pi}{2}$   
 C.  $-\pi$   
 D.  $-\frac{\pi}{2}$

53. Differentiate  $\frac{x}{\cos x}$  with respect to  $x$
- A.  $1 + \sec^2 x$   
 B.  $1 + x \tan x \sec x$   
 C.  $\cos x + x \tan x$   
 D.  $\sec x + x \tan x \sec x$
54. If  $y = 243(4x + 5)^{-2}$ , find  $\frac{dy}{dx}$  when  $x = 1$
- A.  $-\frac{8}{9}$   
 B.  $\frac{9}{8}$   
 C.  $-\frac{8}{3}$   
 D.  $\frac{3}{8}$
55. What is the derivative of  $t^2 \sin(3t - 5)$  with respect to the variable  $t$ ?
- A.  $2t \sin(2t - 5) + 3t^2 \cos(3t - 5)$   
 B.  $2t \sin(2t - 5) - 3t^2 \cos(3t - 5)$   
 C.  $6t \cos(2t - 5)$   
 D.  $2t \sin(2t - 5) + t^2 \cos(3t)$
56. A circle with radius 5 cm has its radius increasing at the rate of  $0.2 \text{ cm}^2$ . What will be the corresponding increase in area?
- A.  $\pi$   
 B.  $2\pi$   
 C.  $4\pi$   
 D.  $5\pi$
57. Find the dimensions of the rectangle of greatest area which has a fixed perimeter  $p$ .
- A. Square of sides  $\frac{p}{2}$   
 B. Square of sides  $p$   
 C. Square of sides  $\frac{p}{4}$   
 D. Square of sides  $2p$
58. The gradient of a curve is  $2x + 7$  and the curve passes through the point  $(2, 0)$ . Find the equation of the curve.
- A.  $y = x^2 + 7x - 18$   
 B.  $y = x^2 + 7x + 18$   
 C.  $y = x^2 + 7x - 9$   
 D.  $y = x^2 + 7x + 9$
59. Differentiate  $y = \sqrt[3]{x^2}(2x - x^2)$
- A.  $\frac{10x^{\frac{5}{3}}}{3} - \frac{8x^{\frac{5}{3}}}{3}$   
 B.  $\frac{10x^{\frac{2}{3}}}{3} - \frac{8x^{\frac{2}{3}}}{3}$   
 C.  $\frac{10x^{\frac{5}{3}}}{3} - \frac{8x^{\frac{2}{3}}}{3}$   
 D.  $\frac{10x^{\frac{2}{3}}}{3} - \frac{8x^{\frac{5}{3}}}{3}$
60. The slope of the tangent to the curve:  $y = 5x^2 - 3x + 5$  at the point  $(1, 6)$  is
- A. 19  
 B. 7  
 C. 4  
 D. 3
61. Find the derivative of the function  $y = 2x^2(2x - 1)$  at the point  $x = -1$
- A. 18  
 B.  $-4$   
 C. 16  
 D.  $-6$
62. Find the derivative of  $y = \log(4x^3 - 2x)$
- A.  $\frac{4x^2 - 2}{7x + 6}$   
 B.  $\frac{12x - 2}{4x^2}$   
 C.  $\frac{43x^2 - 2x}{7x}$   
 D.  $\frac{12x^2 - 2}{4x^3 - 2x}$
63. If  $f'(x) = \sqrt{x} - \frac{1}{\sqrt{x}}$ , find the value of  $f''(4)$
- A.  $\frac{15}{128}$   
 B.  $\frac{21}{128}$   
 C.  $\frac{7}{128}$   
 D.  $\frac{11}{128}$
64. Find the second derivative of  $y = 8x^3 - 3x^2 + 7x - 1$
- A.  $11x^2 + 6x - 7$   
 B.  $24x^2 - 6x + 7$   
 C.  $48x - 6$   
 D.  $32x + 7$
65. For what value of  $x$  is the tangent to the curve  $y = x^2 + 6x + 8$  parallel to the  $x$ -axis?
- A.  $-3$   
 B. 3  
 C. 4  
 D.  $-4$

66. Find the second derivative of  $y = x \sin(x)$  D.  
 A.  $2 \cos(x) - x \sin(x)$   
 B.  $\sin(x) - x \cos(x)$   
 C.  $\sin(x) + x \cos(x)$   
 D.  $x \sin(x) - 2 \cos(x)$
67. Differentiate  $\frac{2x}{\sin(x)}$  with respect to  $x$  74. A.  
 A.  $2 \cot x \sec x(1 + \tan x)$  B.  
 B.  $2 \csc x - x \cot x$  C.  
 C.  $2x \csc x + \tan x$  D.  
 D.  $2 \csc x(1 - x \cot x)$  75. A.
68. Find the point  $(x, y)$  on the Euclidean plane where the curve  $y = 2x^2 - 2x + 3$  has 2 as gradient B.  
 A.  $(1, 3)$  C.  
 B.  $(2, 7)$  D.  
 C.  $(3, 15)$  76. A.  
 D.  $(0, 3)$  77. A.
69. Find the equation of the tangent at the point  $(2, 0)$  to the curve  $y = x^2 - 2x$  B.  
 A.  $y = 2x - 4$  C.  
 B.  $y = 2x + 4$  D.  
 C.  $y = 2x + 2$  78. A.  
 D.  $y = 2x - 2$  79. A.
70. Differentiate  $y = 20x^{-4} + 9$ . B.  
 A.  $-80x^{-5}$  C.  
 B.  $-80x^5$  D.  
 C.  $80x^{-5}$  80. A.  
 D.  $80x^5$  B.
71. Differentiate  $y = \log_7(2x - 3)$  C.  
 A.  $\frac{2}{\log_7(2x - 3)}$  D.  
 B.  $\frac{1}{\log_7(2x - 3)}$  81. A.  
 C.  $\frac{7}{\log_7(2x - 3)}$  B.  
 D.  $\frac{2x}{\log_7(2x - 3)}$  C.
72. A. D.  
 B. C.  
 C. D.  
 D. 82. A.
73. A. B.  
 B. C.  
 C. D.
83. A.  
 B.  
 C.  
 D.



84. A.  
B.  
C.  
D.
85. A.  
B.  
C.  
D.
86. A.  
B.  
C.  
D.
87. A.  
B.  
C.  
D.
88. A.  
B.  
C.  
D.
89. A.  
B.  
C.  
D.
90. A.  
B.  
C.  
D.
91. A.  
B.  
C.  
D.
92. A.  
B.  
C.  
D.
93. A.  
B.  
C.  
D.
94. A.  
B.  
C.  
D.
95. A.  
B.  
C.  
D.
96. A.  
B.  
C.  
D.
97. A.  
B.  
C.  
D.
98. Find the derivative of  
A.  
B.  
C.  
D.
99. Find the derivative of  
A.  
B.  
C.  
D.
100. The derivative of  
A.  
B.  
C.  
D.

**5.1.2 Solution**

1. The minimum point can be gotten by
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.

74.

75.

76.

77.

78.

79.

80.

81.

82.

83.

84.

85.

86.

87.

88.

89.

90.

91.

92.

93.

94.

95.

96.

97.

98.

99.

100.

## 5.2 Integration

### 5.2.1 Questions

1. Find the integral of  $y = 3x^2 - 2x - 1$ 
  - A.  $x^3 - x^2 - x$
  - B.  $x^3 + x^2 - x$
  - C.  $x^3 + x^2 + x$
  - D.  $x^3 - x^2 + x$
2. Integrate the expression  $6x^2 - 2x + 1$ 
  - A.  $3x^3 - 2x^2 + x + c$
  - B.  $2x^3 - x^2 + x + c$
  - C.  $2x^3 - 3x^2 + c$
  - D.  $x^3 + x^2 - x + c$
3. Integrate  $\frac{1}{x} + \cos x$  with respect to  $x$ 
  - A.  $x - \sin x + k$
  - B.  $x + \sin x - k$
  - C.  $-\frac{1}{x^2} + \sin x + k$
  - D.  $-\frac{1}{x^2} - \sin x + k$
4. If the expression  $ax^2 + bx + c$  equals 5 at  $x = 1$ . If its derivative is  $2x + 1$ , what are the values of  $a, b, c$  respectively?
  - A. 1, 1, 3
  - B. 1, 3, 1
  - C. 1, 2, 1
  - D. 2, 1, 1
5.
  - A.
  - B.
  - C.
  - D.
6.
  - A.
  - B.
  - C.
  - D.
7.
  - A.
  - B.
  - C.
  - D.
8.
  - A.
  - B.
  - C.
9.
  - A.
  - B.
  - C.
  - D.
10.
  - A.
  - B.
  - C.
  - D.
11.
  - A.
  - B.
  - C.
  - D.
12.
  - A.
  - B.
  - C.
  - D.
13.
  - A.
  - B.
  - C.
  - D.
14.
  - A.
  - B.
  - C.
  - D.
15.
  - A.
  - B.
  - C.
  - D.
16.
  - A.
  - B.
17.
  - A.
  - B.
  - C.
  - D.
18.
  - A.

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 19. | A. | 29. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 20. | A. | 30. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 21. | A. | 31. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 22. | A. | 32. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 23. | A. | 33. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 24. | A. | 34. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 25. | A. | 35. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 26. | A. | 36. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 27. | A. | 37. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 28. | A. | 38. | A. |
|     |    |     | B. |
|     |    |     | C. |

- D.
39. A.  
B.  
C.  
D.
40. A.  
B.  
C.  
D.
41. A.  
B.  
C.  
D.
42. A.  
B.  
C.  
D.
43. A.  
B.  
C.  
D.
44. A.  
B.  
C.  
D.
45. A.  
B.  
C.  
D.
46. A.  
B.  
C.  
D.
47. A.  
B.  
C.  
D.
48. A.  
B.  
C.
- D.
49. A.  
B.  
C.  
D.
50. A.  
B.  
C.  
D.
51. A.  
B.  
C.  
D.
52. A.  
B.  
C.  
D.
53. A.  
B.  
C.  
D.
54. A.  
B.  
C.  
D.
55. A.  
B.  
C.  
D.
56. A.  
B.  
C.  
D.
57. A.  
B.  
C.  
D.
58. A.  
B.  
C.  
D.
59. A.

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 60. | A. | 70. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 61. | A. | 71. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 62. | A. | 72. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 63. | A. | 73. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 64. | A. | 74. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 65. | A. | 75. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 66. | A. | 76. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 67. | A. | 77. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 68. | A. | 78. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 69. | A. | 79. | A. |
|     |    |     | B. |
|     |    |     | C. |



80. D.  
A.  
B.  
C.  
D.
81. A.  
B.  
C.  
D.
82. A.  
B.  
C.  
D.
83. A.  
B.  
C.  
D.
84. A.  
B.  
C.  
D.
85. A.  
B.  
C.  
D.
86. A.  
B.  
C.  
D.
87. A.  
B.  
C.  
D.
88. A.  
B.  
C.  
D.
89. A.  
B.  
C.  
D.
90. A.  
B.
- C.  
D.
91. A.  
B.  
C.  
D.
92. A.  
B.  
C.  
D.
93. A.  
B.  
C.  
D.
94. A.  
B.  
C.  
D.
95. A.  
B.  
C.  
D.
96. A.  
B.  
C.  
D.
97. A.  
B.  
C.  
D.
98. A.  
B.  
C.  
D.
99. A.  
B.  
C.  
D.
100. A.  
B.  
C.  
D.

**5.2.2 Solution**

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.

74.

75.

76.

77.

78.

79.

80.

81.

82.

83.

84.

85.

86.

87.

88.

89.

90.

91.

92.

93.

94.

95.

96.

97.

98.

99.

100.

## Chapter 6

# Combinatorics

### 6.1 Combination & Permutation

#### 6.1.1 Questions

1. Ralia has 7 different posters to be hung in her bedroom, living room, and kitchen. Assuming she has plans to plant at least a poster in each of the 3 rooms, how many choices does she have?  
A. 49  
B. 170  
C. 210  
D. 21
2. In how many ways can a committee of 2 women and 3 men be chosen from 6 men and 5 women?  
A. 200  
B. 100  
C. 50  
D. 30
3. In how many ways can the letters of the word MATHEMATICS be arranged?  
A.  $\frac{11!}{9!2!}$   
B.  $\frac{11!}{9!2!2!}$   
C.  $\frac{11!}{2!2!2!}$   
D.  $\frac{11!}{2!2!}$
4. In how many ways can the letters of the word ACCEPTANCE be arranged?  
A.  $\frac{10!}{2!2!3!}$   
B.  $\frac{10!}{2!2!}$   
C.  $10!$   
D.  $\frac{10!}{2!3!}$
5. Five people are to be arranged in a row for a group photograph. How many arrangements are there if a married couple in the group insist on sitting next to each other?  
A. 48  
B. 12  
C. 7  
D. 10
6. In how many ways can 6 subjects be selected from 10 subjects for an examination  
A. 215  
B. 218  
C. 216  
D. 210
7. In how many ways can a delegation of 3 be chosen from 5 men and 3 women, if atleast 1 man and 1 woman must be included?  
A. 28  
B. 30  
C. 15  
D. 45
8. Find the number of ways of selecting 6 out of 10 subjects for an examination  
A. 218  
B. 216  
C. 210  
D. 215
9. In how many ways can the letters of the word ELATION be arranged?  
A.  $6!$

- B.  $7!$   
 C.  $5!$   
 D.  $8!$
10. In how many ways can the letters of the word CALCULUS be arranged?  
 A. 1680  
 B. 2100  
 C. 5040  
 D. 1760
11. In how many ways can the letters of the word COMBINATION be arranged?  
 A.  
 B.  
 C.  
 D.
12. In how many ways can 7 directors sit round a table?  
 A. 24  
 B. 5040  
 C. 120  
 D. 120
13. In how many ways can the letters of the word TOTALITY be arranged?  
 A. 6720  
 B. 6270  
 C. 6207  
 D. 6027
14. How many numbers greater than 1000 can be made from the digits 1, 2, 3, 4, and 5 without repeating any one of them?  
 A. 152  
 B. 210  
 C. 216  
 D. 144
15. In how many ways can a team of 3 girls be selected from 7 girls?  
 A.  $\frac{7!}{5!2!}$   
 B.  $\frac{7!}{3!}$   
 C.  $\frac{7!}{3!4!}$   
 D.  $\frac{7!}{4!}$
16. In how many ways can a student select 2 subjects from 5 subjects?  
 A.  $\frac{5!}{3!2!}$   
 B.  $\frac{5!}{2!2!}$   
 C.  $\frac{5!}{2!3!}$   
 D.  $\frac{5!}{2!}$
17. In how many ways can five people sit round a circular table?  
 A. 24  
 B. 60  
 C. 12  
 D. 120
18. How many two-digit numbers can be formed from the digits 0, 1, 2, and 3 if a digit can be repeated and no number may begin with 0?  
 A. 4  
 B. 12  
 C. 16  
 D. 20
19. In how many ways can 9 people be seated if 3 chairs are available?  
 A. 720  
 B. 504  
 C. 336  
 D. 210
20. A final examination requires that a student answer any 4 out of 6 questions. In how many ways can this be done?  
 A. 15  
 B. 20  
 C. 45  
 D. 30
21. In how many ways can 6 coloured chalks be arranged if 2 are of the same colour?  
 A. 60  
 B. 240  
 C. 120  
 D. 360
22. How many possible ways are there of seating seven people  $P, Q, R, S, T, U$ , and  $V$  at a circular table?  
 A. 720  
 B. 2520  
 C. 5040  
 D. 360

23. A committee of six is to be formed by a state governor from nine state commissioners and three members of the State House of Assembly. In how many ways can the members of the committee be chosen so as to include one member of the House of the Assembly?
- A. 924 ways  
B. 524 ways  
C. 462 ways  
D. 378 ways
24. How many two-digit numbers can be formed from the digits 0,1, 2, and 3 if a digit can be repeated and no number may begin with 0?
- A. 4  
B. 12  
C. 16  
D. 20
25. Find the number of committees of three that can be formed consisting of two men and one woman from four men and three women
- A. 3  
B. 6  
C. 18  
D. 24
26. A.  
B.  
C.  
D.
27. A.  
B.  
C.  
D.
28. A.  
B.  
C.  
D.
29. A.  
B.  
C.  
D.
30. A.  
B.  
C.  
D.
31. A.  
B.  
C.  
D.
32. A.  
B.  
C.  
D.
33. A.  
B.  
C.  
D.
34. A.  
B.  
C.  
D.
35. A.  
B.  
C.  
D.
36. A.  
B.  
C.  
D.
37. A.  
B.  
C.  
D.
38. A.  
B.  
C.  
D.
39. A.  
B.  
C.  
D.
40. A.  
B.  
C.  
D.
41. A.

- B.  
C.  
D.
42. A.  
B.  
C.  
D.
43. A.  
B.  
C.  
D.
44. A.  
B.  
C.  
D.
45. A.  
B.  
C.  
D.
46. A.  
B.  
C.  
D.
47. A.  
B.  
C.  
D.
48. A.  
B.  
C.  
D.
49. A.  
B.  
C.  
D.
50. A.  
B.  
C.  
D.
51. A.
- B.  
C.  
D.
52. A.  
B.  
C.  
D.
53. A.  
B.  
C.  
D.
54. A.  
B.  
C.  
D.
55. A.  
B.  
C.  
D.
56. A.  
B.  
C.  
D.
57. A.  
B.  
C.  
D.
58. A.  
B.  
C.  
D.
59. A.  
B.  
C.  
D.
60. A.  
B.  
C.  
D.
61. A.  
B.  
C.



- D.
62. A.  
B.  
C.  
D.
63. A.  
B.  
C.  
D.
64. A.  
B.  
C.  
D.
65. A.  
B.  
C.  
D.
66. A.  
B.  
C.  
D.
67. A.  
B.  
C.  
D.
68. A.  
B.  
C.  
D.
69. A.  
B.  
C.  
D.
70. A.  
B.  
C.  
D.
71. A.  
B.  
C.
- D.
72. A.  
B.  
C.  
D.
73. A.  
B.  
C.  
D.
74. A.  
B.  
C.  
D.
75. A.  
B.  
C.  
D.
76. A.  
B.  
C.  
D.
77. A.  
B.  
C.  
D.
78. A.  
B.  
C.  
D.
79. A.  
B.  
C.  
D.
80. A.  
B.  
C.  
D.
81. A.  
B.  
C.  
D.
82. A.

- B.  
C.  
D.
83. A.  
B.  
C.  
D.
84. A.  
B.  
C.  
D.
85. A.  
B.  
C.  
D.
86. A.  
B.  
C.  
D.
87. A.  
B.  
C.  
D.
88. A.  
B.  
C.  
D.
89. A.  
B.  
C.  
D.
90. A.  
B.  
C.  
D.
91. A.  
B.  
C.
- D.
92. A.  
B.  
C.  
D.
93. A.  
B.  
C.  
D.
94. A.  
B.  
C.  
D.
95. A.  
B.  
C.  
D.
96. A.  
B.  
C.  
D.
97. A.  
B.  
C.  
D.
98. A.  
B.  
C.  
D.
99. A.  
B.  
C.  
D.
100. A.  
B.  
C.  
D.

**6.1.2 Solution**

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.

- 74.
- 75.
- 76.
- 77.
- 78.
- 79.
- 80.
- 81.
- 82.
- 83.
- 84.
- 85.
- 86.
- 87.
- 88.
- 89.
- 90.
- 91.
- 92.
- 93.
- 94.
- 95.
- 96.
- 97.
- 98.
- 99.
- 100.



# Chapter 7

## Statistics

### 7.1 Measures of Central Tendency

#### 7.1.1 Questions

- |       |        |
|-------|--------|
| 1. A. | D.     |
| B.    | 8. A.  |
| C.    | B.     |
| D.    | C.     |
| 2. A. | D.     |
| B.    | 9. A.  |
| C.    | B.     |
| D.    | C.     |
| 3. A. | D.     |
| B.    | 10. A. |
| C.    | B.     |
| D.    | C.     |
| 4. A. | D.     |
| B.    | 11. A. |
| C.    | B.     |
| D.    | C.     |
| 5. A. | D.     |
| B.    | 12. A. |
| C.    | B.     |
| D.    | C.     |
| 6. A. | D.     |
| B.    | 13. A. |
| C.    | B.     |
| D.    | C.     |
| 7. A. | D.     |
| B.    | 14. A. |
| C.    | B.     |
|       | C.     |

- |     |    |     |    |
|-----|----|-----|----|
|     | D. |     | D. |
| 15. | A. | 25. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 16. | A. | 26. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 17. | A. | 27. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 18. | A. | 28. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 19. | A. | 29. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 20. | A. | 30. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 21. | A. | 31. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 22. | A. | 32. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 23. | A. | 33. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 24. | A. | 34. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     |    |     | D. |
|     |    | 35. | A. |



- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 36. | A. | 46. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 37. | A. | 47. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 38. | A. | 48. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 39. | A. | 49. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 40. | A. | 50. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 41. | A. | 51. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 42. | A. | 52. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 43. | A. | 53. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 44. | A. | 54. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 45. | A. | 55. | A. |
|     |    |     | B. |
|     |    |     | C. |

- D.
56. A.  
B.  
C.  
D.
57. A.  
B.  
C.  
D.
58. A.  
B.  
C.  
D.
59. A.  
B.  
C.  
D.
60. A.  
B.  
C.  
D.
61. A.  
B.  
C.  
D.
62. A.  
B.  
C.  
D.
63. A.  
B.  
C.  
D.
64. A.  
B.  
C.  
D.
65. A.  
B.  
C.
- D.
66. A.  
B.  
C.  
D.
67. A.  
B.  
C.  
D.
68. A.  
B.  
C.  
D.
69. A.  
B.  
C.  
D.
70. A.  
B.  
C.  
D.
71. A.  
B.  
C.  
D.
72. A.  
B.  
C.  
D.
73. A.  
B.  
C.  
D.
74. A.  
B.  
C.  
D.
75. A.  
B.  
C.  
D.
76. A.

- |     |    |     |    |
|-----|----|-----|----|
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 77. | A. | 87. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 78. | A. | 88. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 79. | A. | 89. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 80. | A. | 90. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 81. | A. | 91. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 82. | A. | 92. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 83. | A. | 93. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 84. | A. | 94. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 85. | A. | 95. | A. |
|     | B. |     | B. |
|     | C. |     | C. |
|     | D. |     | D. |
| 86. | A. | 96. | A. |
|     |    |     | B. |
|     |    |     | C. |

- D.
97. A.  
B.  
C.  
D.
98. A.  
B.  
C.  
D.
99. A.  
B.  
C.  
D.
100. A.  
B.  
C.  
D.

**7.1.2 Solution**

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.
- 11.
- 12.
- 13.
- 14.
- 15.
- 16.
- 17.
- 18.
- 19.
- 20.
- 21.
- 22.
- 23.
- 24.
- 25.
- 26.
- 27.
- 28.
- 29.
- 30.
- 31.
- 32.
- 33.
- 34.
- 35.
- 36.

- 37.
- 38.
- 39.
- 40.
- 41.
- 42.
- 43.
- 44.
- 45.
- 46.
- 47.
- 48.
- 49.
- 50.
- 51.
- 52.
- 53.
- 54.
- 55.
- 56.
- 57.
- 58.
- 59.
- 60.
- 61.
- 62.
- 63.
- 64.
- 65.
- 66.
- 67.
- 68.
- 69.
- 70.
- 71.
- 72.
- 73.

- 74.
- 75.
- 76.
- 77.
- 78.
- 79.
- 80.
- 81.
- 82.
- 83.
- 84.
- 85.
- 86.
- 87.
- 88.
- 89.
- 90.
- 91.
- 92.
- 93.
- 94.
- 95.
- 96.
- 97.
- 98.
- 99.
- 100.





# Chapter 8

## Values To Memorize

### 8.1 Square Roots

- $\sqrt{1} = 1$
- $\sqrt{2} = 1.4142$
- $\sqrt{3} = 1.7321$
- $\sqrt{4} = 2$
- $\sqrt{5} = 2.2361$
- $\sqrt{6} = 2.4495$
- $\sqrt{7} = 2.6458$
- $\sqrt{8} = 2.8284$
- $\sqrt{9} = 3$
- $\sqrt{10} = 3.1623$
- $13^2 = 169$
- $14^2 = 196$
- $15^2 = 225$
- $16^2 = 256$
- $17^2 = 289$
- $18^2 = 324$
- $19^2 = 361$
- $20^2 = 400$
- $21^2 = 441$

### 8.2 Squares

- $1^2 = 1$
- $2^2 = 4$
- $3^2 = 9$
- $4^2 = 16$
- $5^2 = 25$
- $6^2 = 36$
- $7^2 = 49$
- $8^2 = 64$
- $9^2 = 81$
- $10^2 = 100$
- $11^2 = 121$
- $12^2 = 144$
- $22^2 = 484$
- $23^2 = 529$
- $24^2 = 576$
- $25^2 = 625$
- $26^2 = 676$
- $27^2 = 729$
- $28^2 = 784$
- $29^2 = 841$
- $30^2 = 900$

### 8.3 Cubes

- $1^3 = 1$
- $2^3 = 8$
- $3^3 = 27$
- $4^3 = 64$
- $5^3 = 125$
- $6^3 = 216$
- $7^3 = 343$
- $8^3 = 512$
- $9^3 = 729$
- $10^3 = 1000$
- $11^3 = 1331$
- $12^3 = 1728$
- $13^3 = 2197$
- $14^3 = 2744$
- $15^3 = 3375$
- $16^3 = 4096$
- $17^3 = 4913$
- $18^3 = 5832$
- $19^3 = 6859$
- $20^3 = 8000$
- $21^3 = 9261$
- $22^3 = 10648$
- $23^3 = 12167$
- $24^3 = 13824$
- $25^3 = 15625$
- $26^3 = 17576$
- $27^3 = 19683$
- $28^3 = 21952$
- $29^3 = 24389$
- $30^3 = 27000$

### 8.4 Logarithms

- $\log_{10} 1 = 0$
- $\log_{10} 2 = 0.3010$
- $\log_{10} 3 = 0.4771$
- $\log_{10} 4 = 0.6020$
- $\log_{10} 5 = 0.699$
- $\log_{10} 6 = 0.778$
- $\log_{10} 7 = 0.845$
- $\log_{10} 8 = 0.903$
- $\log_{10} 9 = 0.954$
- $\log_{10} 10 = 1$