INTEGRATION QUESTIONS

NUTM Nexus Writing Team

May 2, 2025

1 Differentiation of Integrals

1. Use the theorem of integration as inverse of differentiation (FTC) to find $\frac{dy}{dx}$ if:

(a)
$$y = \int_{a}^{x} (t^3 + 1) dt$$

(b)
$$y = \int_{1+3x^2}^4 \frac{1}{2+e^t} dt$$

2. Find the derivatives:

(a)
$$\frac{d}{dt} \int_0^{t^4} \sqrt{u} \, du$$

(b)
$$\frac{d}{dx} \int_0^{x^3} e^{-t} dt$$

2 Evaluation of Definite Integrals

Evaluate the following definite integrals (numbering follows original presentation order):

1

1.
$$\int_{-2}^{0} (2x+5) \, \mathrm{d}x$$

2.
$$\int_{-3}^{1} \left(5 - \frac{x}{2}\right) dx$$

$$3. \qquad \int_0^2 x(x-3) \, \mathrm{d}x$$

4.
$$\int_{-1}^{1} (x^2 - 2x + 3) \, \mathrm{d}x$$

5.
$$\int_0^4 \left(3x - \frac{x^3}{4}\right) dx$$

6.
$$\int_{-2}^{2} (x^3 - 2x + 3) \, \mathrm{d}x$$

7.
$$\int_0^1 (x^2 + \sqrt{x}) \, \mathrm{d}x$$

8.
$$\int_{1}^{32} x^{-6/5} \, \mathrm{d}x$$

- 9. $\int_{1}^{-1} (r+1)^2 \, \mathrm{d}r$
- **10.** $\int_{-\sqrt{3}}^{\sqrt{3}} (t+1)(t^2+4) \, dt$
- 11. $\int_{\sqrt{2}}^{1} \left(\frac{u^7}{2} \frac{1}{u^5} \right) du$
- 12. $\int_{-3}^{-1} \frac{y^5 2y}{y^3} \, \mathrm{d}y$
- 13. $\int_{1}^{\sqrt{2}} \frac{s^2 + \sqrt{s}}{s^2} ds$
- **14.** $\int_1^8 \frac{(x^{1/3} + 1)(2 x^{2/3})}{x^{1/3}} \, \mathrm{d}x$