PARTIAL FRACTIONS AND ITS INTEGRATION

NUTM Nexus Writing Team

April 29, 2025

1 Examples: Partial Fraction Decomposition

- 1. (Example 1) Write the partial fraction decomposition for $\frac{x+7}{x^2-x-6}$.
- 2. (Example 2) Write the partial fraction decomposition for $\frac{x+8}{x^2+7x+12}$.
- 3. (Example 3) Write the form of the partial fraction decomposition for $\frac{5x^2 + 20x + 6}{x(x+1)^2}$.
- 4. (Example 4) Write the form of the partial fraction decomposition for $\frac{3x^2 + 7x + 4}{x^3 + 4x^2 + 4x}$.

2 ClassWork: Partial Fraction Decomposition

Write the partial fraction decomposition for the following expressions:

5.
$$\frac{2(x+20)}{x^2-25}$$

6.
$$\frac{3x+11}{x^2-2x-3}$$

7.
$$\frac{8x+3}{x^2-3x}$$

8.
$$\frac{10x+3}{x^2+x}$$

9.
$$\frac{4x - 13}{x^2 - 3x - 10}$$

$$10. \ \frac{7x+5}{6(2x^2+3x+1)}$$

11.
$$\frac{3x^2 - 2x - 5}{x^3 + x^2}$$

12.
$$\frac{3x^2 - x + 1}{x(x+1)^2}$$

13.
$$\frac{x+1}{3(x-2)^2}$$

14.
$$\frac{3x-4}{(x-5)^2}$$

15.
$$\frac{8x^2 + 15x + 9}{(x+1)^3}$$

16.
$$\frac{6x^2 - 5x}{(x+2)^3}$$

3 ClassWork: Integration by Partial Fractions

Use partial fractions to find the indefinite integral:

17.
$$\int \frac{1}{x^2 - 1} \, \mathrm{d}x$$

18.
$$\int \frac{4}{x^2 - 4} \, \mathrm{d}x$$

19.
$$\int \frac{-2}{x^2 - 16} \, \mathrm{d}x$$

20.
$$\int \frac{-4}{x^2 - 4} \, \mathrm{d}x$$

21.
$$\int \frac{1}{2x^2 - x} \, \mathrm{d}x$$

$$22. \int \frac{2}{x^2 - 2x} \, \mathrm{d}x$$

23.
$$\int \frac{10}{x^2 - 10x} \, \mathrm{d}x$$

24.
$$\int \frac{5}{x^2 + x - 6} \, \mathrm{d}x$$

25.
$$\int \frac{3}{x^2 + x - 2} \, \mathrm{d}x$$

26.
$$\int \frac{1}{4x^2 - 9} \, \mathrm{d}x$$

27.
$$\int \frac{5-x}{2x^2+x-1} \, dx$$

28.
$$\int \frac{x+1}{x^2 + 4x + 3} \, \mathrm{d}x$$

29.
$$\int \frac{x^2 - 4x - 4}{x^3 - 4x} \, \mathrm{d}x$$

30.
$$\int \frac{x^2 + 12x + 12}{x^3 - 4x} \, \mathrm{d}x$$

31.
$$\int \frac{x+2}{x^2-4x} \, \mathrm{d}x$$

32.
$$\int \frac{4x^2 + 2x - 1}{x^3 + x^2} \, \mathrm{d}x$$

33.
$$\int \frac{2x-3}{(x-1)^2} \, \mathrm{d}x$$

34.
$$\int \frac{x^4}{(x-1)^3} \, \mathrm{d}x$$

35.
$$\int \frac{3x^2 + 3x + 1}{x(x^2 + 2x + 1)} \, \mathrm{d}x$$

36.
$$\int \frac{3x}{x^2 - 6x + 9} \, \mathrm{d}x$$