Assignment 8 - SGD using linear Regression

```
In [1]: ▶ 1 ## Lets import Packages from the required libraries
             2 from sklearn.datasets import load_boston
             3 from sklearn.model_selection import train_test_split
             4 from sklearn.preprocessing import StandardScaler
             5 from sklearn.linear_model import SGDRegressor
             6 from sklearn.linear_model import LinearRegression
             7 from sklearn.metrics import mean_squared_error
             8 import pandas as pd
             9 import seaborn as sns
            10 import matplotlib.pyplot as plt
            11 import numpy as np
In [2]: ► 1 ## Loading our dataset
             2 boston=load_boston()
In [3]: № 1 # Shape of the dataset
             2 boston.data.shape
   Out[3]: (506, 13)
In [4]: | 1 | print(boston.feature_names)
           ['CRIM' 'ZN' 'INDUS' 'CHAS' 'NOX' 'RM' 'AGE' 'DIS' 'RAD' 'TAX' 'PTRATIO'
```

'B' 'LSTAT']

```
In [5]:
             1 ## Description of each feature
              2 print(boston.DESCR)
            .. _boston_dataset:
            Boston house prices dataset
            _____
            **Data Set Characteristics:**
                :Number of Instances: 506
                :Number of Attributes: 13 numeric/categorical predictive. Median Value (attribute 14) is usually the target.
                :Attribute Information (in order):
                    - CRIM
                               per capita crime rate by town
                    - ZN
                               proportion of residential land zoned for lots over 25,000 sq.ft.
                              proportion of non-retail business acres per town
                               Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)
                    - CHAS
                    - NOX
                               nitric oxides concentration (parts per 10 million)
                               average number of rooms per dwelling
                    - RM
                    - AGE
                               proportion of owner-occupied units built prior to 1940
                    - DIS
                               weighted distances to five Boston employment centres
                    - RAD
                               index of accessibility to radial highways
                               full-value property-tax rate per $10,000
                    - TAX
                    - PTRATIO pupil-teacher ratio by town
                               1000(Bk - 0.63)^2 where Bk is the proportion of blacks by town
                    - B
                    - LSTAT
                              % lower status of the population
                    - MEDV
                               Median value of owner-occupied homes in $1000's
                :Missing Attribute Values: None
                :Creator: Harrison, D. and Rubinfeld, D.L.
            This is a copy of UCI ML housing dataset.
            https://archive.ics.uci.edu/ml/machine-learning-databases/housing/ (https://archive.ics.uci.edu/ml/machine-learning-databases/housing/)
            This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.
            The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic
            prices and the demand for clean air', J. Environ. Economics & Management,
            vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics
            ...', Wiley, 1980. N.B. Various transformations are used in the table on
            pages 244-261 of the latter.
            The Boston house-price data has been used in many machine learning papers that address regression
            problems.
            .. topic:: References
               - Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influential Data and Sources of Collinearity', Wiley, 1980. 244-261.
               - Quinlan, R. (1993). Combining Instance-Based and Model-Based Learning. In Proceedings on the Tenth International Conference of Machine Learning, 236-243, University of Mass
            achusetts, Amherst. Morgan Kaufmann.
```

In [6]:

boston_data=pd.DataFrame(data=boston.data,columns=boston.feature_names)

0.0 0.469 6.421 78.9 4.9671 2.0 242.0

```
In [7]: N | 1 | boston_data['price']=boston.target | boston_data.head(2) |

Out[7]: | CRIM | ZN | INDUS | CHAS | NOX | RM | AGE | DIS | RAD | TAX | PTRATIO | B | LSTAT | price |

O | 0.00632 | 18.0 | 2.31 | 0.0 | 0.538 | 6.575 | 65.2 | 4.0900 | 1.0 | 296.0 | 15.3 | 396.9 | 4.98 | 24.0
```

17.8 396.9

Train Test Split

1 0.02731 0.0

9.14 21.6

Standardize the Train set

7.07

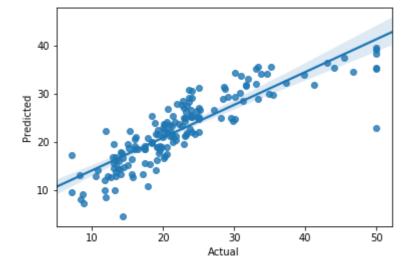
Write custom SGD for linear Regression

```
In [10]:
              1 class SGD scratch :
                      '''The class contains various functions to perform Schocastic Gradient Descent on Linear regression
              3
                         Class includes 2 functions primarily
                        1.find w b function : To find best (W,b) that fits the data giving minimum loss using SGD.
              4
               5
                        Note: Some important parameters from sklearn.SGDRegressor have also been implemented
               6
                         2.Predict Function: that predicts y label given (w,b) '''
              7
                     def __init__(self,dataset,learning_rate,k,no_iterations,shuffle=False,divide=None):
              8
                          # initiating values
              9
                          self.data=dataset
              10
                          self.learning_rate=learning_rate
              11
                          self.k=k
              12
                          self.divide=divide
              13
                          self.no_iterations=no_iterations
              14
                          self.shuffle=shuffle
              15
              16
                     def find w b(self):
              17
                          from sklearn.utils import shuffle
              18
                          k,no_iter=self.k,self.no_iterations
              19
                         w=np.random.randn(1,13)
              20
                         b=0
              21
                          lr_rate=self.learning_rate
              22
              23
                         for i in range(no_iter):
              24
                             w_vector,b_vector=np.zeros(shape=(1,13)),0
              25
                             if shuffle:
              26
                                  self.data=shuffle(self.data) #Shuffle the dataframe when shuffle=True for every iterations
              27
                             else:
              28
                                  pass
              29
              30
              31
                             #take sample of size k and store the data and target seprately
              32
                             sampled_data=self.data.sample(k,replace=False)
              33
                             x=np.array(sampled_data.drop('price',axis=1))
              34
                             y=np.array(sampled_data['price'])
              35
                             residual_sum_square=0
              36
                             for pt in range(k):
              37
                                  actual_=y[pt] ## actual value y[i]
              38
                                  predicts_ = np.dot(w,x[pt]) + b ## predicted value w.T.x[pt] + intercept
              39
                                  w_{\text{vector}} = (-2) * x[pt] * (y[pt] - (np.dot(w,x[pt]) + b) )
              40
                                  b_{vector} = (-2) * (y[pt] - (np.dot(w,x[pt]) + b))
              41
                                  error = (predicts_ - actual_) ** 2 # square( actual(y[i]) - predicted(y[i]) )
              42
                                  residual_sum_square += error # sum of square of all the residue
              43
              44
                             print("-"*20)
              45
                             print('Iteration {0}: mean squared error : {1} '.format(i,residual_sum_square/k))
              46
              47
                             previous state b=b # storing the previous intercept value
              48
                             previous_state_w=w #storing the previous weights values
              49
              50
                             w=w-lr_rate*(w_vector/k)
              51
                             b=b-lr_rate*(b_vector/k)
              52
              53
                             diff_vec= previous_state_w - w #calculate the difference between the vectors
              54
                             if abs(previous_state_b -b) < 0.0008 and np.sqrt(np.sum(diff_vec**2)) < 0.0008 : # exit loop if w,b value is almost same, set random threshold 0.008
              55
                                  print('*'*20)
              56
                                  print('State wj :', previous_state_w)
              57
                                  print('State wj+1 :', w)
              58
                                  print('State bj :', previous_state_b)
              59
                                  print('State bj+1 :', b)
              60
                                  print('Iteration terminated at :',i)
```

```
print('Iteration terminated at :',i)
61
62
                    break
63
                if self.divide:
64
65
                    lr_rate = lr_rate / pow((i+1),0.05)
66
                    print('lr_rate: ',lr_rate)
67
                print("-"*10)
68
69
            return w,b
70
71
       def predict_func(self,w,b,test_set):
72
            predict_set=[]
73
            test_set=np.array(test_set)
74
            for pt in range(len(test_set)):
75
                predictions=(np.dot(w,test_set[pt])+b)
76
                predict_set.append(predictions[0])
77
            return predict_set
```

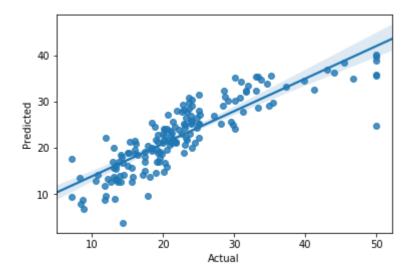
Sklearn SGD Regressor

Mean Squared Error : 22.2971947293



Sklearn Linear Regression

Mean Squared Error : 22.1950284502

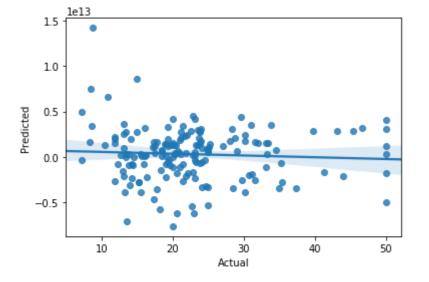


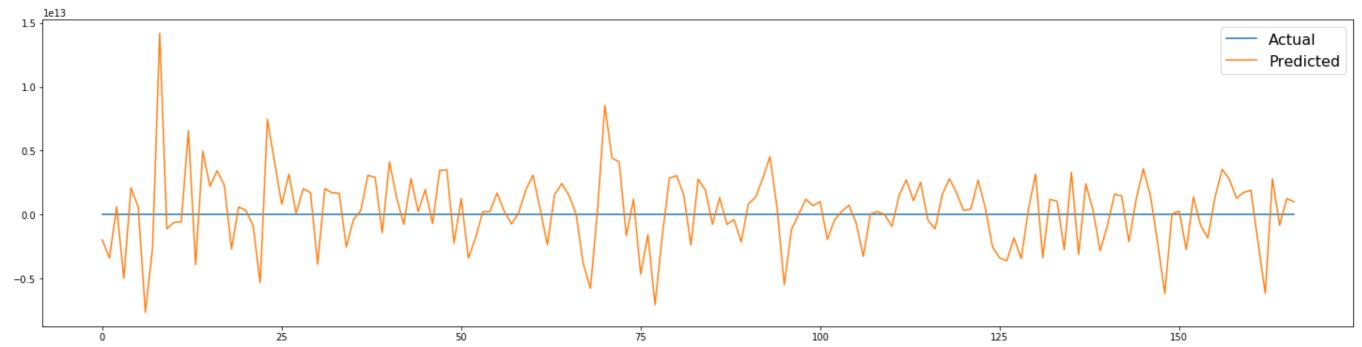
Custom SGD regressor : Trial 1

- 1. Initially implementing with learning rate =1 and iterations=100
- 2. For every iteration set learning rate = learning rate /2
- 3. Shuffle the dataset per iteration

```
2 w,b=model.find_w_b()
           3 predictions=model.predict_func(w,b,x_test)
           4 weights['Custom SGD (Trial 1)'] = pd.DataFrame(w.T)
          1r rate: 0.6529478154043212
          -----
          -----
          Iteration 7 : mean squared error : [ 8.57695860e+15]
          lr_rate: 0.5884695206938755
          -----
          -----
          Iteration 8 : mean squared error : [ 2.98338967e+17]
          lr_rate: 0.5272442454241162
          -----
          -----
          Iteration 9 : mean squared error : [ 1.02650061e+19]
          lr rate: 0.46990692835986236
          -----
          Iteration 10 : mean squared error : [ 4.48201807e+20]
          lr_rate: 0.41681391978913523
          -----
          -----
          Iteration 11 : mean squared error : [ 9.33673670e+21]
In [14]: ► 1 ## Plotting functions
           2 #Scatter plot
           3 predict_data=pd.DataFrame(data= {'Actual' : y_test,'Predicted' :predictions})
           4 sns.regplot(x='Actual', y='Predicted', data=predict_data)
           5 print('Mean Squared Error :', mean_squared_error(y_test, predictions))
```

Mean Squared Error: 8.36279966769e+24





Mean Squared Error: 8.36279966769e+24

Observations:

1. We see that the model does not perform well and gives a MSE of 8.36 e+24, with the above set parameters

Custom SGD regressor : Trial 2

- 1. Implementing with learning rate =0.2 and iterations=500
- 2. Shuffle the dataset per iteration

```
2 w,b=model.find_w_b()
           3 predictions=model.predict_func(w,b,x_test)
           4 weights['Custom SGD (Trial 2)'] = pd.DataFrame(w.T)
          Iteration 0 : mean squared error : [ 700.84819584]
          lr rate: 0.2
          -----
          _____
          Iteration 1 : mean squared error : [ 316.38821338]
          lr_rate: 0.19318726578496911
          -----
          -----
          Iteration 2 : mean squared error : [ 441.89517938]
          lr_rate: 0.18286156535236558
          -----
          -----
          Iteration 3 : mean squared error : [ 629.41243007]
          lr rate: 0.17061587335782108
          _____
          Iteration 4 : mean squared error : [ 1002.15283167]
          lr_rate: 0.15742399642419647
          -----
          -----
          Iteration 5 : mean squared error : [ 936.9914339]
          lr_rate: 0.14393399205076884
          -----
          -----
          Iteration 6 : mean squared error : [ 467.33421729]
          lr_rate: 0.13058956308086425
          -----
          -----
          Iteration 7 : mean squared error : [ 187.10058905]
          lr_rate: 0.1176939041387751
          -----
          -----
          Iteration 8 : mean squared error : [ 105.94217708]
          lr rate: 0.10544884908482326
          -----
          -----
          Iteration 9 : mean squared error : [ 51.12823438]
          lr_rate: 0.09398138567197249
          -----
          Iteration 10 : mean squared error : [ 31.43511732]
          lr_rate: 0.08336278395782706
          -----
          -----
          Iteration 11 : mean squared error : [ 25.61902904]
          lr_rate: 0.07362293851363488
          -----
          -----
          Iteration 12 : mean squared error : [ 34.78255225]
          lr rate: 0.06476136289387929
          -----
          _____
          Iteration 13 : mean squared error : [ 32.92859496]
          lr_rate: 0.05675571223453064
```

-----Iteration 14 : mean squared error : [18.10594608] lr rate: 0.04956841305788922 ----------Iteration 15 : mean squared error : [17.81742436] lr_rate: 0.04315180990924041 ----------Iteration 16 : mean squared error : [52.10837854] lr_rate: 0.03745213411452443 -----Iteration 17 : mean squared error : [54.09439634] lr_rate: 0.03241253096307968 ----------Iteration 18 : mean squared error : [23.48152295] lr_rate: 0.02797533298812906 ----------Iteration 19 : mean squared error : [24.45075207] lr_rate: 0.024083730836508242 -----Iteration 20 : mean squared error : [28.34336721] lr_rate: 0.020682965145182638 ----------Iteration 21 : mean squared error : [28.70609073] lr_rate: 0.017721140385663577 ----------Iteration 22 : mean squared error : [33.12278788] lr_rate: 0.015149743303671968 -----Iteration 23 : mean squared error : [17.14495377] lr rate: 0.012923933424513973 ----------Iteration 24 : mean squared error : [13.78995902] lr_rate: 0.011002660480289505 -----Iteration 25 : mean squared error : [15.31844472] lr_rate: 0.009348653091118545 -----Iteration 26 : mean squared error : [27.17433044] lr_rate: 0.007928314257640278 ----------Iteration 27 : mean squared error : [20.48470372] lr_rate: 0.006711551925354233 ----------Iteration 28 : mean squared error : [13.99175996] lr_rate: 0.005671566840000688

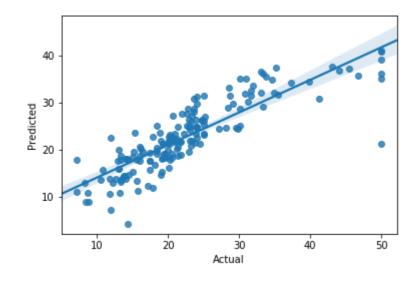
-----Iteration 29 : mean squared error : [15.27902335] lr rate: 0.004784614938798966 ----------Iteration 30 : mean squared error : [20.8187387] lr rate: 0.004029757453381585 ----------Iteration 31 : mean squared error : [19.11246344] lr_rate: 0.0033886085968905127 -----Iteration 32 : mean squared error : [13.30765294] lr rate: 0.002845088048680407 ----------Iteration 33 : mean squared error : [30.13956293] lr_rate: 0.002385183330304127 ----------Iteration 34 : mean squared error : [22.7648264] lr_rate: 0.001996725495132476 _____ Iteration 35 : mean squared error : [33.75817345] lr rate: 0.00166918025298942 ----------Iteration 36 : mean squared error : [19.68642721] lr rate: 0.001393455653778815 -----Iteration 37 : mean squared error : [40.08183626] lr_rate: 0.001161726703474252 -----Iteration 38 : mean squared error : [22.5424867] lr_rate: 0.0009672767341122829 ----------Iteration 39 : mean squared error : [19.71794527] lr_rate: 0.0008043549563845681 ----------Iteration 40 : mean squared error : [19.30155866] lr_rate: 0.0006680493556141013 ----------Iteration 41 : mean squared error : [10.77947171] lr_rate: 0.0005541739216873886 ----------Iteration 42 : mean squared error : [41.22611897] lr_rate: 0.0004591691082456614 -----Iteration 43 : mean squared error : [14.04456581] lr rate: 0.00038001437770191166 ---------localhost:8888/notebooks/Documents/appleidai/SGD%2CLinearR%2CGD/SGD Assignment8.ipynb

8/11/2020

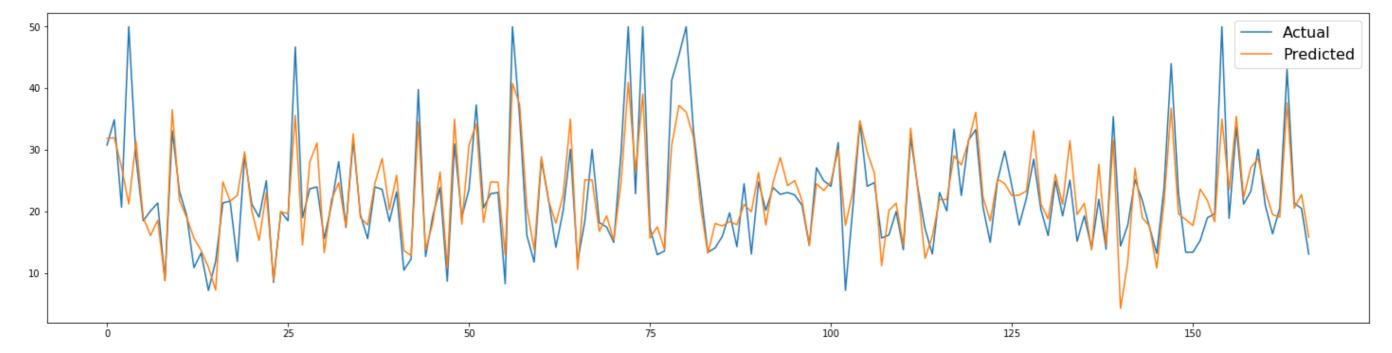
Iteration 44 : mean squared error : [27.34772574] lr_rate: 0.00031415169161586796 ----------Iteration 45 : mean squared error : [25.92401596] lr_rate: 0.0002594188387963494 ----------Iteration 46 : mean squared error : [24.32942131] lr rate: 0.00021399154687634468 ----------Iteration 47 : mean squared error : [18.12495464] lr_rate: 0.00017633338974736067 -----Iteration 48 : mean squared error : [33.92756921] lr_rate: 0.0001451525775591791 ----------Iteration 49 : mean squared error : [43.50212676] lr rate: 0.00011936479377123923 -----Iteration 50 : mean squared error : [13.43127502] ******** -0.50619766 -2.86436668 0.98714701 -0.70267729 -1.45645257 0.56144044 -3.45457129]] State wj+1 : [[-0.62514733 1.07999767 -1.3900024 1.28460618 -0.40767812 2.93881272 -0.50603737 -2.86438383 0.98706158 -0.70279323 -1.45648774 0.56146142 -3.45412598]] State bj : [22.49808336] State bj+1 : [22.49809334] Iteration terminated at: 50 Iteration terminated at: 50

```
In [56]: ▶
             1 ## Plotting functions
              2 #Scatter plot
              3 predict_data=pd.DataFrame(data= {'Actual' : y_test,'Predicted' :predictions})
              4 sns.regplot(x='Actual', y='Predicted', data=predict_data)
              5 print('Mean Squared Error :',mean_squared_error(y_test, predictions))
```

Mean Squared Error : 22.5748669474



```
1 plt.figure(figsize=(25,6))
In [57]: ▶
              2 plt.plot(y_test, label='Actual')
              3 plt.plot(predictions, label='Predicted')
              4 plt.legend(prop={'size': 16})
              5 plt.show()
              6 print('Mean Squared Error :',mean_squared_error(y_test, predictions))
```



Mean Squared Error : 22.5748669474

Observations:

1. We see that the model performs well and gives a MSE of 29.3 as close as sklearn's SGDREgressor, with the above set parameters

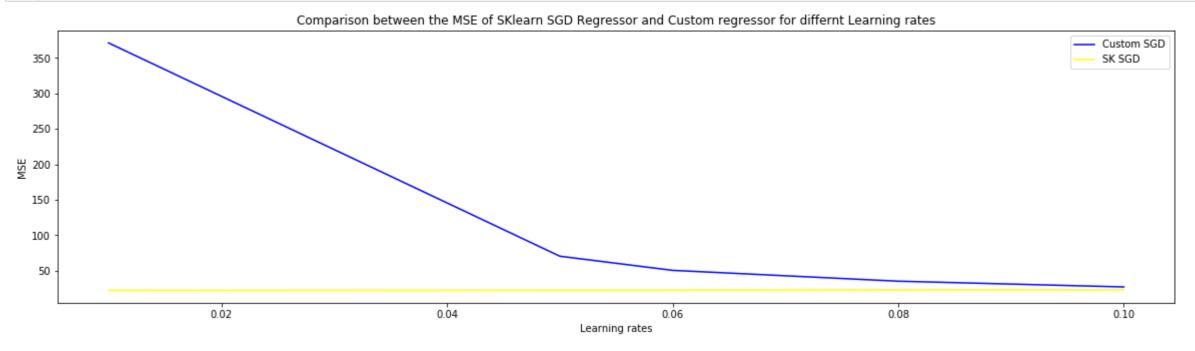
Effect of learning rate on model performance

1. Considering a set of learning rate and check the model performance of each with constant iteration 100

```
In [40]: | 1 | alpha_set = [0.1,0.08,0.06,0.05,0.01]
             2 custom_sgd_mse=[]
             3 sk_sgd_mse=[]
             4 for i in alpha_set:
                  # train custom model
                   model=SGD_scratch(transformed_train_set,i,40,500,shuffle=True,divide=1)
                   w,b=model.find_w_b()
             8
                   predictions=model.predict_func(w,b,x_test)
             9
                   custom_sgd_mse.append(mean_squared_error(y_test, predictions))
            10
            11
                   ##train SGDregressor
            12
                   sklearn_model = SGDRegressor(max_iter=500,alpha=i)
            13
                   sklearn_model.fit(x_train, y_train)
            14
                   y_pred=sklearn_model.predict(x_test)
            15
                   sk_sgd_mse.append(mean_squared_error(y_test, y_pred))
           lr_rate: 0.007574871651835984
           -----
           Iteration 23 : mean squared error : [ 19.99525915]
           lr_rate: 0.0064619667122569864
           -----
           Iteration 24 : mean squared error : [ 29.64388956]
           lr rate: 0.005501330240144753
           -----
           Iteration 25 : mean squared error : [ 45.95801426]
           lr_rate: 0.004674326545559273
           -----
           -----
           Iteration 26 : mean squared error : [ 9.25083364]
           lr_rate: 0.003964157128820139
           -----
           -----
```

Plotting MSE for custom SGD vs Sklearn SGD

```
In [41]: N | 1 plt.figure(figsize=(20,5))
plt.plot(alpha_set, custom_sgd_mse, color='blue', label='Custom SGD')
plt.plot(alpha_set, sk_sgd_mse, color='yellow', label='SK SGD')
4 plt.xlabel('Learning rates')
5 plt.ylabel('MSE')
6 plt.title("Comparison between the MSE of SKlearn SGD Regressor and Custom regressor for differnt Learning rates")
7 plt.legend()
8 plt.show()
```



Observations

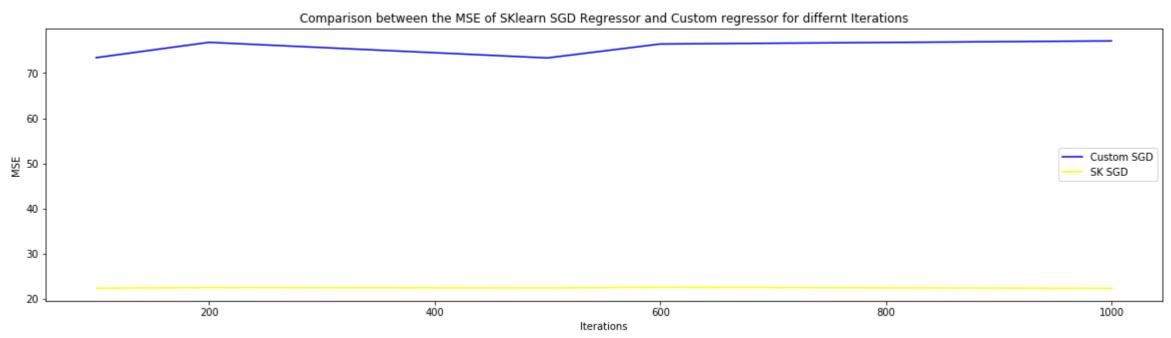
- 1.We can observe that our custom model has effect/fluctuations of learning rate to a greater extent than sklearn SGD.
- 2.With lower values of learning rate tends to decrease MSE (i.e learning rate < 0.06)

Effect of number of iterations on model performance

1. Considering a set of iterations rate and check the model performance of each with constant learning rate 0.05

```
In [42]: | 1 | iter_set = [100,200,500,600,1000]
             2 custom_sgd_mse=[]
             3 sk_sgd_mse=[]
             4 for i in iter set:
                   # train custom model
                   model=SGD_scratch(transformed_train_set,0.05,40,i,shuffle=True,divide=1)
                   w,b=model.find_w_b()
             8
                   predictions=model.predict_func(w,b,x_test)
             9
                   custom_sgd_mse.append(mean_squared_error(y_test, predictions))
            10
            11
                   ##train SGDregressor
            12
                   sklearn_model = SGDRegressor(max_iter=i,alpha=0.05,shuffle=True)
            13
                   sklearn_model.fit(x_train, y_train)
            14
                   y_pred=sklearn_model.predict(x_test)
            15
                   sk_sgd_mse.append(mean_squared_error(y_test, y_pred))
           Iteration 5 : mean squared error : [ 235.62347647]
            lr_rate: 0.03598349801269221
            -----
            -----
            Iteration 6 : mean squared error : [ 195.01186375]
            lr_rate: 0.03264739077021606
            -----
           Iteration 7 : mean squared error : [ 163.57443764]
            lr rate: 0.029423476034693776
            -----
            Iteration 8 : mean squared error : [ 149.84551938]
            lr_rate: 0.026362212271205814
            -----
            -----
            Iteration 9 : mean squared error : [ 125.73590188]
           lr_rate: 0.023495346417993123
            -----
            -----
```

Plotting MSE for custom SGD vs Sklearn SGD



Observations

1.We can observe that our custom model has effect/fluctuations of iterations to a greater extent than sklearn SGD.

2.As number of iterations increase it converges to optimumum better.

Comparing Weights and MSE

Out[44]:

	Sklearn SGD	Sklearn Linear Regression	Custom SGD (Trial 1)	Custom SGD (Trial 2)
0	-0.712181	-0.863947	1.652214e+12	0.088773
1	0.548530	0.743271	-1.479200e+12	0.999658
2	-0.709605	-0.412015	-1.618272e+12	-0.749712
3	1.082881	1.000662	-2.599226e+11	0.912983
4	-1.573638	-2.252131	-9.759675e+11	-0.076970
5	2.437577	2.217033	-3.254227e+10	3.052044
6	-0.056164	0.065871	-9.869387e+11	0.302897
7	-2.604154	-3.255986	-7.281176e+11	-1.504199
8	1.513546	2.875749	6.985335e+11	-0.798913
9	-0.917969	-1.996244	-1.128136e+12	-0.229589
10	-1.927254	-2.152966	-1.426380e+12	-2.003892
11	0.756422	0.751297	-6.406850e+11	0.738550
12	-3.610867	-3.884441	1.531544e+12	-2.944202

```
In [58]: ▶ 1 ##http://zetcode.com/python/prettytable/
              3 from prettytable import PrettyTable
              4 x = PrettyTable()
              5 x.field_names = [ "Model", "MSE"]
              6 print('MSE comparisons ')
              7 x.add_row(["Sklearn SGD",22.2])
              8 | x.add_row(["Sklearn Linear Regression",22.1])
              9 x.add_row(["Custom SGD (Trial 1)",8.9e+24])
             10 x.add_row(["Custom SGD (Trial 2)",22.5])
             11 print(x)
```

MSE comparisons

Model	MSE
Sklearn SGD	22.2
Sklearn Linear Regression	22.1
Custom SGD (Trial 1)	8.9e+24
Custom SGD (Trial 2)	22.5

Conclusion:

1. After applying custom SGD to our dataset with learning rate 0.2 and iterations of 500 we see that MSE is closer to the SKlearn SGD MSE 22.2.

Ref: https://www.kaggle.com/premvardhan/stocasticgradientdescent-implementation-lr-python (https://www.kaggle.com/premvardhan/stocasticgradientdescent-implementation-lr-python), https://www.kaggle.com/tentotheminus9/linear-regression-from-scratch-gradient-descent (https://www.kaggle.com/tentotheminus9/linear-regression-from-scratch-gradient-descent)

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