



DSC NSEC

08

Chapter

NEURAL NETWORK : A MATHEMATICAL MODEL

UNIT THREE

SEP 23, 2019

AYUSH THAKUR

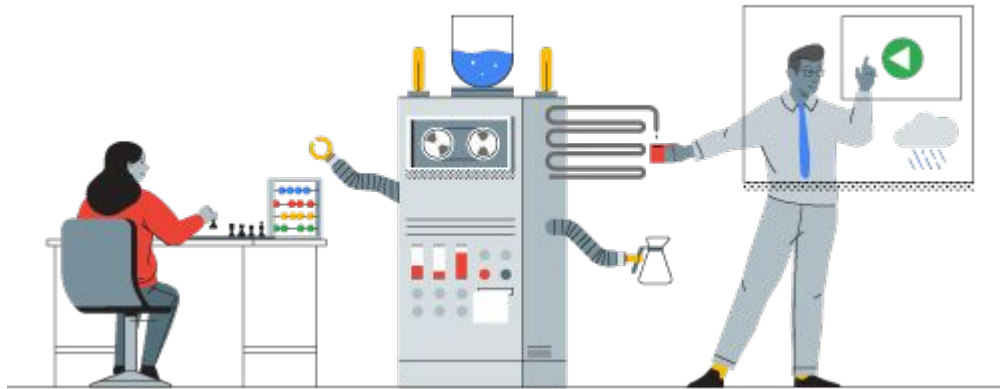
Intro to ML with DSC NSEC

About Me

- Deep Learning for Computer Vision
- Chair, IEEE EDS Student Branch Chapter, NSEC
- Winner of few competitions.
- Human <3



Chapter 8: Neural Network: A Mathematical Model (Peekaboo)



Agenda

- Mathematical Modeling
 - What?
 - How?
 - Example
- Intelligence
 - ! Human
 - Modelling Brain- Artificial Neuron
 - Learning

Disclaimers

“Stay with me.”

Biology Ahead

Some Maths Too

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Modeling is a process that uses
Math
to represent, analyze, make predictions
or otherwise provide insight into
real-world phenomenon.

It's an abstraction of **Real life scenario**,
system or event that uses
mathematical **language** to **predict** the
behaviour, dynamics and evolution of
said scenario, system or event.

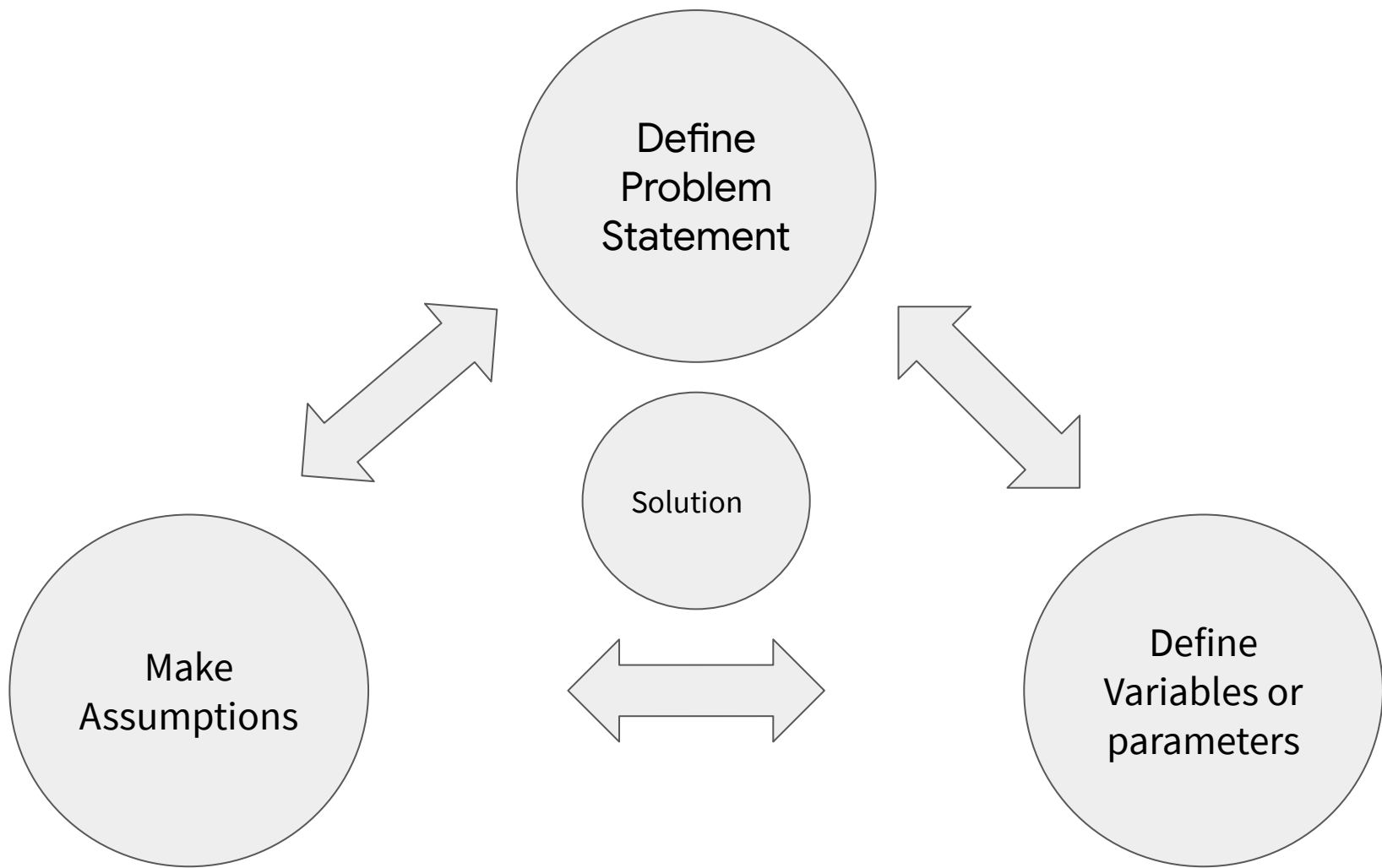
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- Mathematical Modeling

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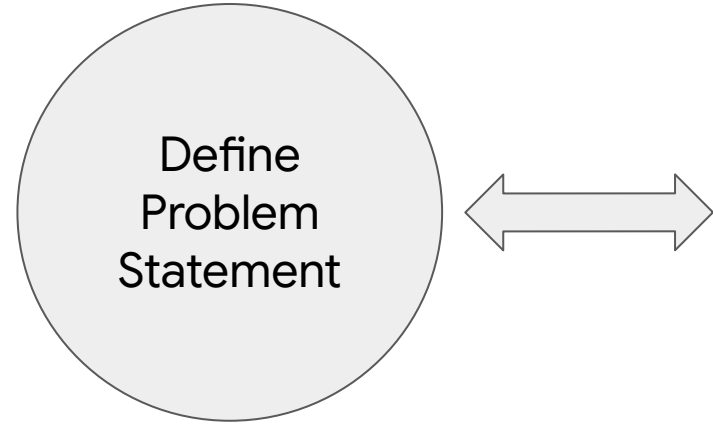
Let's Leave Earth's Gravity

Defining problem statement: #1

- What is Gravity?
- How to leave earth's gravity?

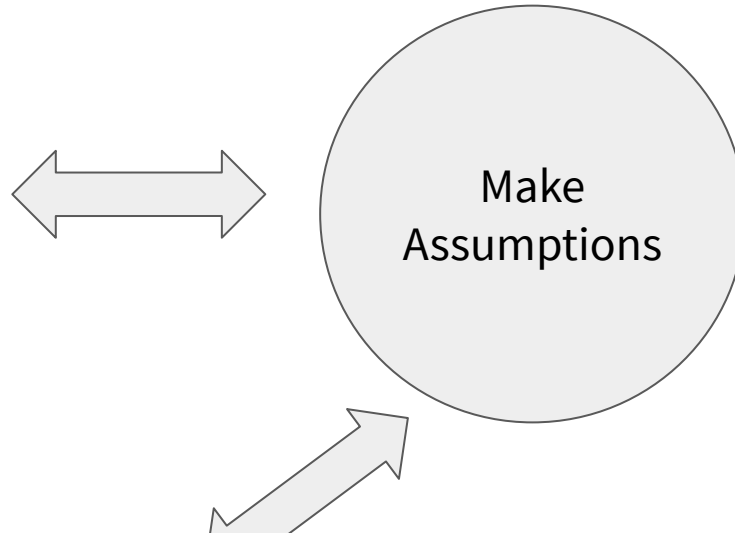
Defining problem statement: #2

- Escape Velocity: Enough velocity to overcome gravitational pull.



Assumptions

- If minimum escape velocity is computed, any object with more velocity can leave earth.
- Factors like drag by air is not considered in the modelling process.
- Won't bother about achieving that velocity. Let's just find out the velocity.



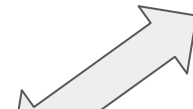
Defining Parameters

- We have a mathematical model for gravity (Courtesy: Sir Newton). Hence related parameters are known and defined. For Ex: Gravitational constant or G .
- Since velocity is to be computed let's call it V_{esp} .
- The object to leave earth will have mass. Let's call it m .
- While defining gravity of earth we must have defined the parameters like radius of earth(R) and mass of earth (M)



Define
Variables or
parameters

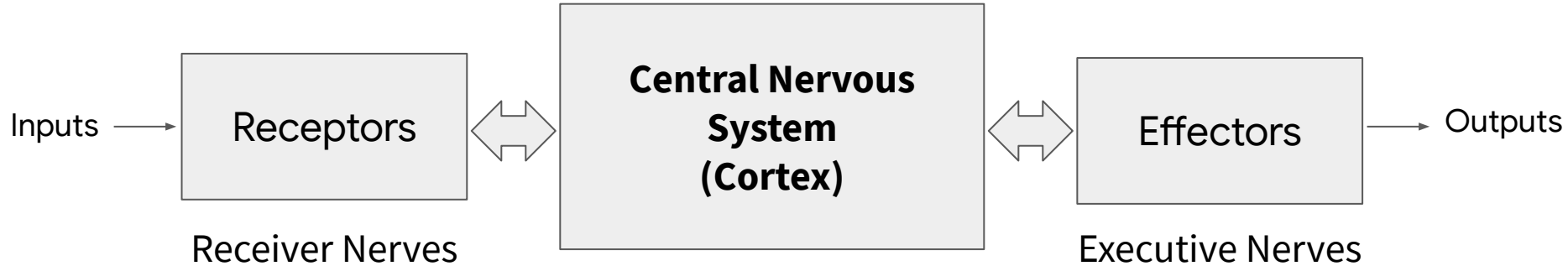
SOLUTION: <https://www.wikihow.com/Calculate-Escape-Velocity>



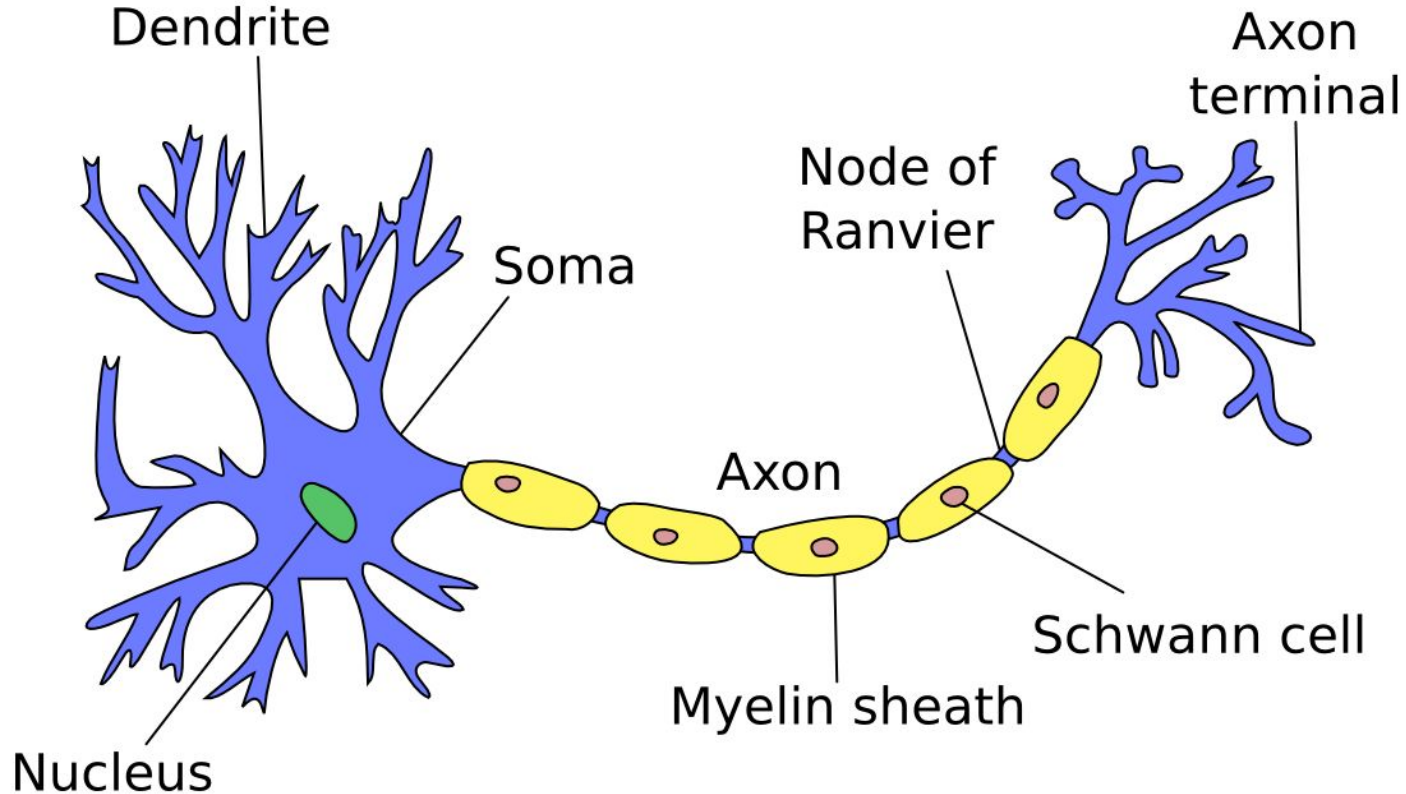
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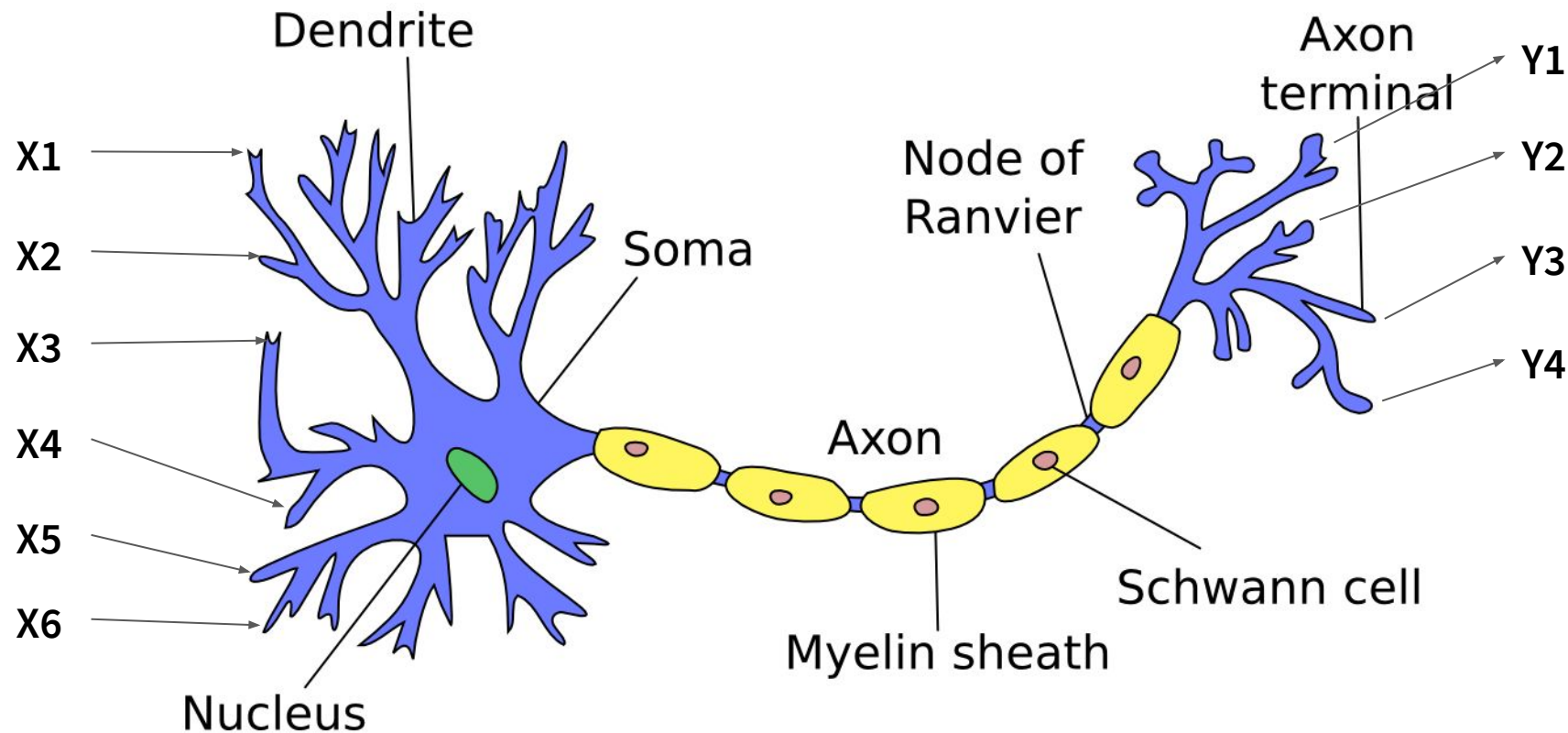
Human Nervous System



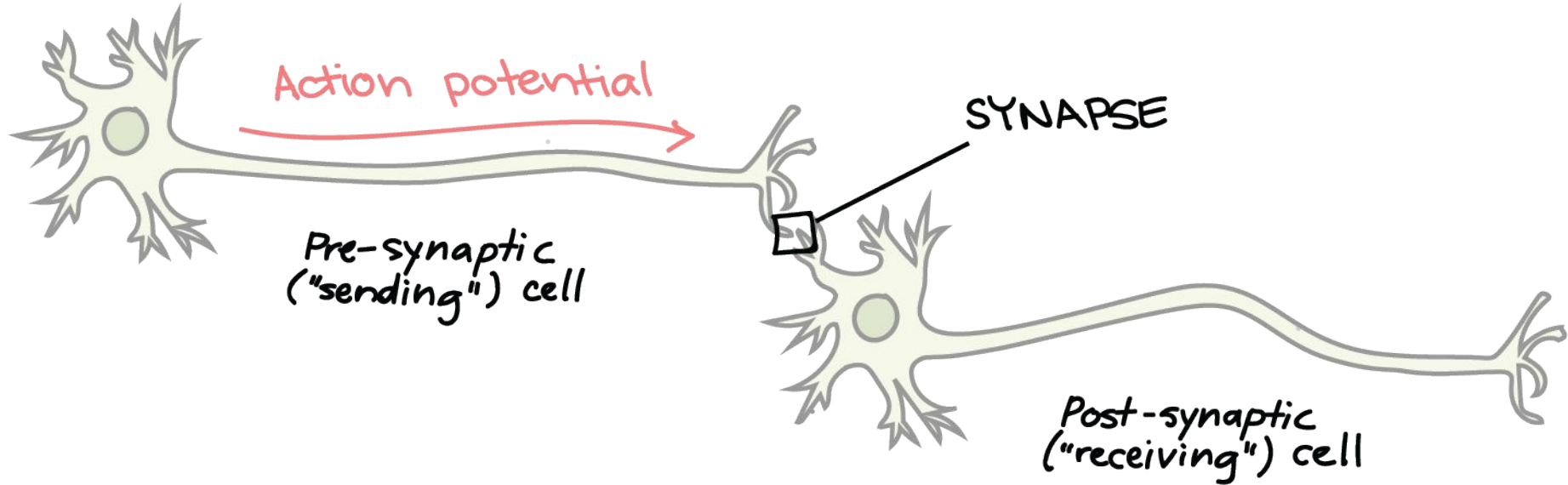
Biological Neurons



Biological Neurons



Connection Between Neurons



A **synapse** serves as a unique inter-neuron interface to transfer the information.

At the **early stage** of the human brain development (the first two years from birth) about 1 million synapses (**hard-wired connections**) are formed per second.

Synapses are then **modified** through the **learning process**.

Summary

- Input
- Neurons
- Connected neurons via synapses
- Modification of synapses through learning process
- Output

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Mathematical Model of Single Neuron

Defining problem:

Dynamic generation of dynamic output based on dynamic input.

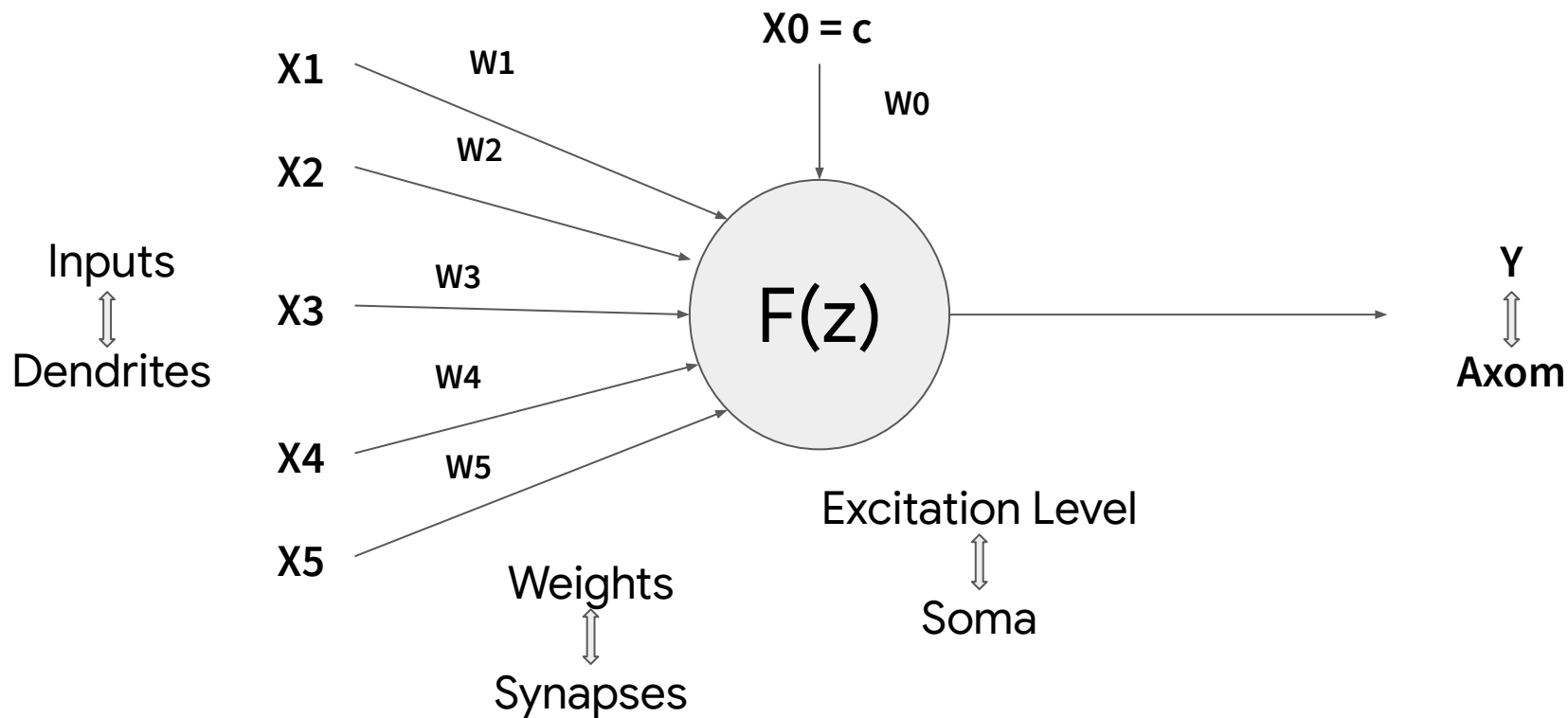
Assumptions:

- Output is dependent variable.
- Input is independent variable.

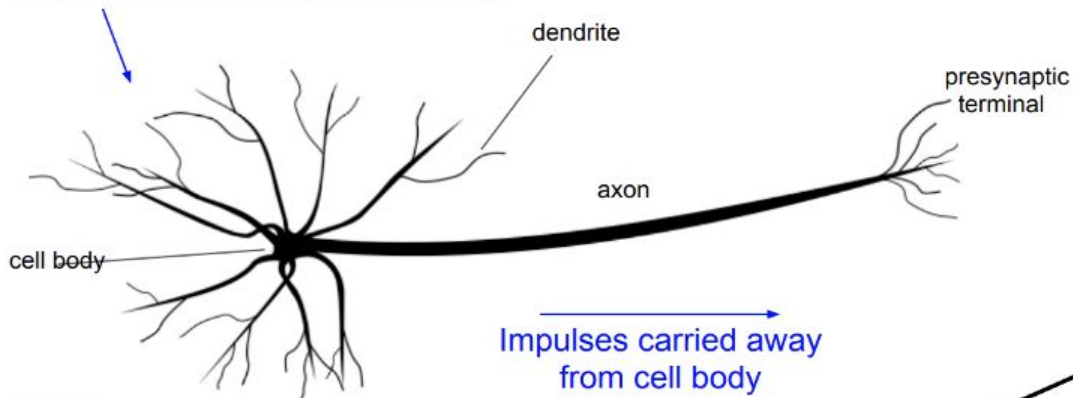
Define Variables:

- Inputs as x_1, x_2, x_3 and so on.
- Outputs as y_1, y_2, y_3 and so on.

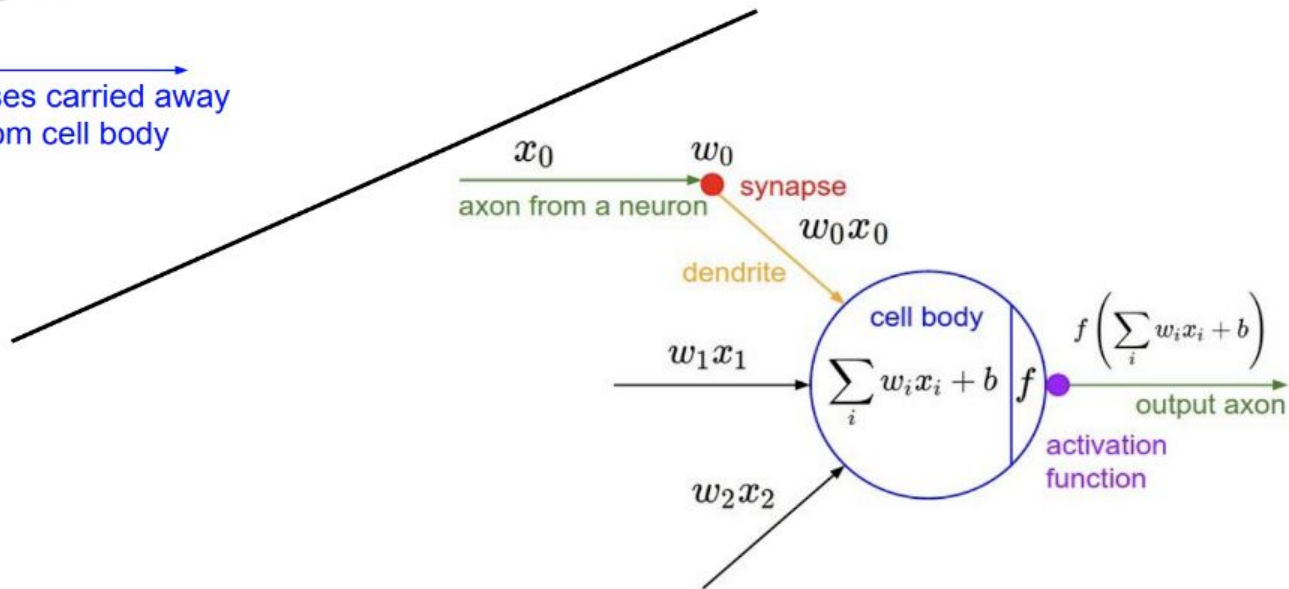
Inspiration from Biological Neuron



Impulses carried toward cell body

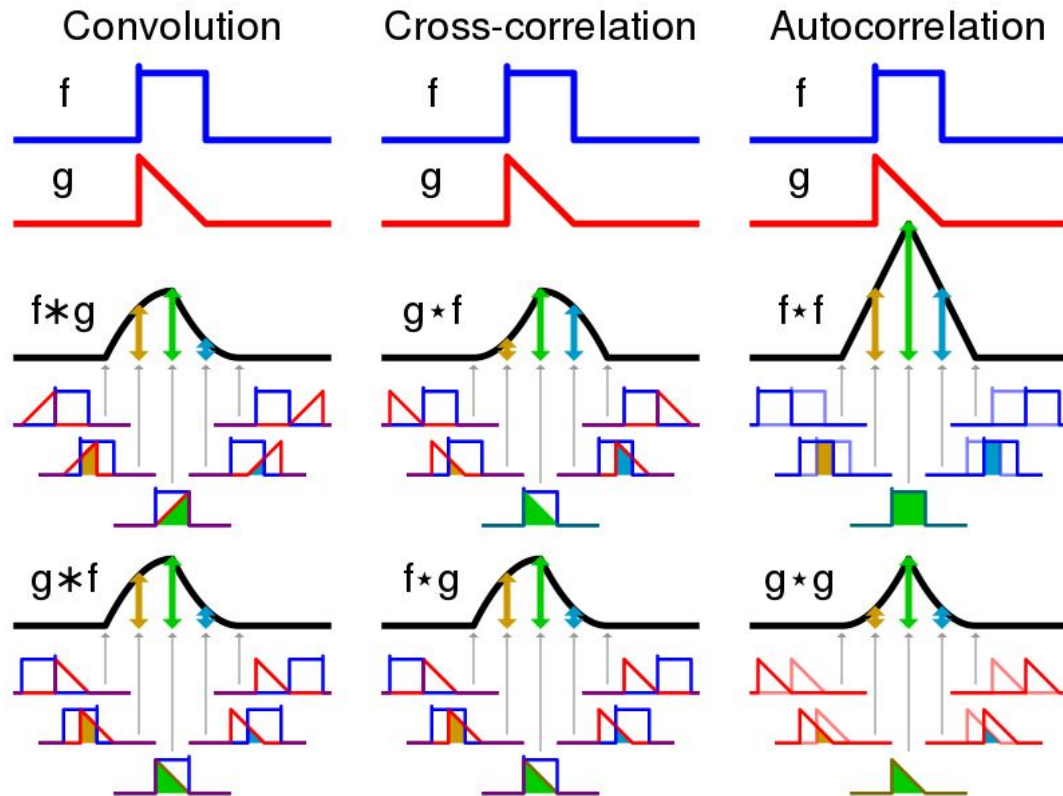


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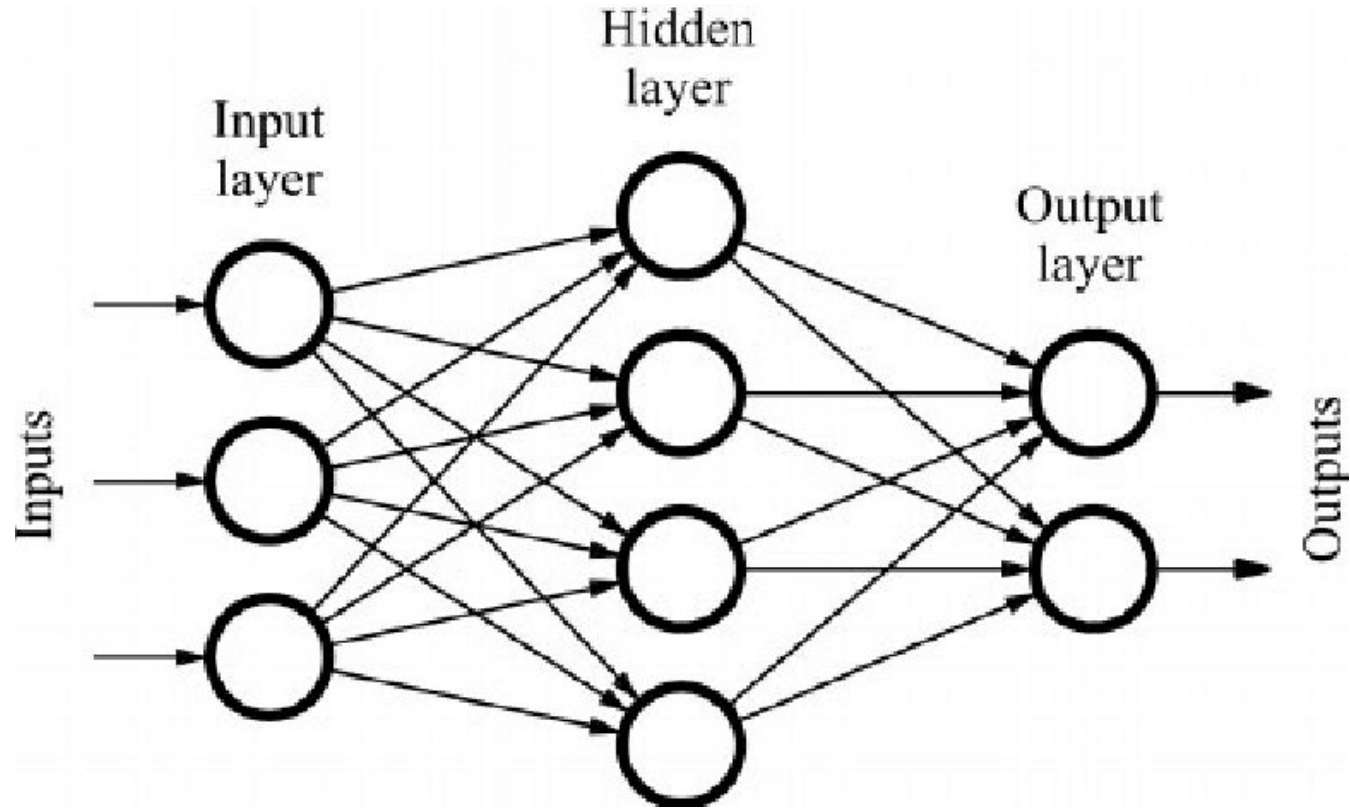
Head over to Colab: <https://tinyurl.com/prelu>

AutoCorrelation - An Analogy



- We started with random weights.
- This is an approximation of the inputs.
- Autocorrelation gives the similarity between same signals.
- Decrease dissimilarity.
- Hence weights are approximating better.
- Learning happened.

Feed Forward Network - Topology



Activations

- Let's see some polynomials.
- Linearity: Limited by complexity.
- Non-Linearity: Able to capture complex features.

Famous activations:

- Sigmoid
- Tanh
- Relu

Up for Questions

! Humans

Thank You

Connect me on:

Mail to: mein2work@gmail.com

Connect: [Linkedin](#)

Find slide on github: [ayulockin/talks](https://github.com/ayulockin/talks)