Assignment 1

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Download all python codes from

https://github.com/ayush−2321/AI1103/blob/main/
  assignment1/problem(a).py

and latex-tikz codes from

https://github.com/ayush−2321/AI1103/blob/main/
  assignment1/asignment1.txt

PROBLEM(A)(PROB. MISC. 5.8)

On a multiple choice examination with 3 possible answers of each of the five questions, what is the probability that the candidate would get four or more correct answers just by guessing

SOLUTION

Let $X_i \in (0, 1)$ be a random variable where $X_i = 1$ represents a successful guess and $X_i = 0$ represents unsuccessful guess on the ith question.

$$p = \frac{1}{3}$$

$$X = \sum_{i=1}^{n} X_i \qquad (0.0.1)$$

where n is the total number of questions. So, X has a binomial distribution.

$$pr(X \geq r) = \sum_{k=r}^{n} \binom{n}{r} p^k (1-p)^{n-k}$$

Now, in this case n=5 and r=4

$$Pr_x(4) = \frac{10}{243}$$

$$Pr_x(5) = \frac{1}{243}$$

Hence, required probability$= \frac{11}{243}$

PROBLEM(B)

Five cards are drawn successively from a well shuffled deck of 52 cards. What is the probability that

  i. All the five cards are spades.
  ii. only 3 cards are spade.
  iii. no cards are spade.

SOLUTION

Let $X_i \in (0, 1)$ be a random variable which denotes whether spade is drawn at the ith draw.

$$X = \sum_{i=1}^{i=5} X_i$$

where X denotes the number of spades obtained.

  i. $X = 5$

$$Pr_x(5) = \frac{\binom{13}{5}}{\binom{52}{5}}$$

$$\implies Pr_x(5) = 0.0049$$

  ii. $X = 3$

$$Pr_x(5) = \frac{\binom{13}{3}\binom{39}{2}}{\binom{52}{5}}$$

$$\implies Pr_x(3) = 0.081$$

  iii. $X = 0$

$$Pr_x(5) = \frac{\binom{39}{5}}{\binom{52}{5}}$$

$$\implies Pr_x(5) = 0.221$$