

# Data Structures & Algorithms

## (PCC-CS 301)

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# Topics Covered

1. Linear Data Structure
  - a. Stack (continued)
  - b. Queue

# Stack: Abstract Data Type

- Stack

- Operations

- PUSH (data insertion into stack)
    - POP (data deletion from stack)
    - Display (showing element of stack)

Primary operation

- IsFullStack (checks if stack is overflow)
    - IsEmptyStack (checks if stack is underflow)

Auxiliary operation

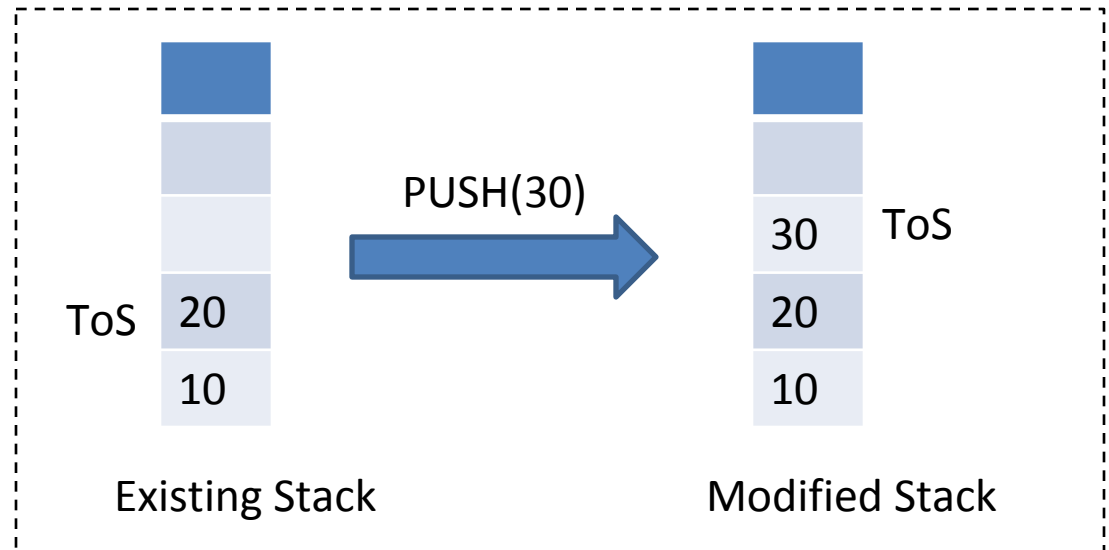
# Stack: Abstract Data Type

- Stack Operation

- PUSH

- This function inserts one element at the top most position of the stack if the stack is not full
    - The newly inserted data is pointed by ToS

```
void PUSH(element)
{
    if IsFullStack = TRUE
        return
    else
        tos := tos+1
        Stack(tos) := element
}
```



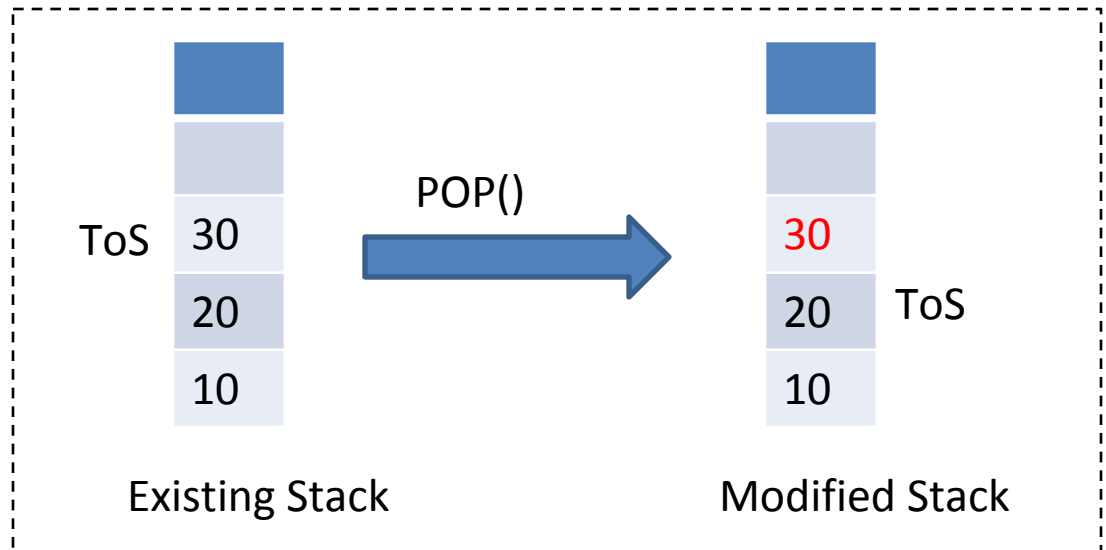
# Stack: Abstract Data Type

- Stack Operation

- POP

- This operation deletes the top most element of the stack if it is not empty
    - The current top most element will be pointed by ToS

```
int POP()
{
    if IsEmptyStack = TRUE
        return NULL
    else
        data := Stack(tos)
        tos := tos-1
        return data
}
```



# Stack: Abstract Data Type

- Stack Operation

- Display (or PEEK)

- This function displays the top most element of the stack.
    - It does not change the ToS pointer
    - All elements can also be displayed through an auxiliary pointer without shifting ToS

```
int PEEK()
{
    if IsEmptyStack = TRUE
        return NULL
    else
        return Stack(ToS)
}
```

```
void Display()
{
    if IsEmptyStack = TRUE
        print "stack empty"
    else
        for i= ToS to 0
            print Stack(i)
}
```

# Stack: Abstract Data Type

- Stack Operation

- IsFullStack

- This function checks whether the stack is full or not
    - We cannot push data into stack if it is full

```
Boolean IsFullStack()
{
    if ToS = Max_Size
        return TRUE
    else
        return FALSE
}
```

# Stack: Abstract Data Type

- Stack Operation

- IsEmptyStack

- This function checks whether the stack is empty or not
    - We cannot pop or display the stack if it is empty

```
Boolean IsEmptyStack()  
{  
    if ToS = NULL  
        return TRUE  
    else  
        return FALSE  
}
```



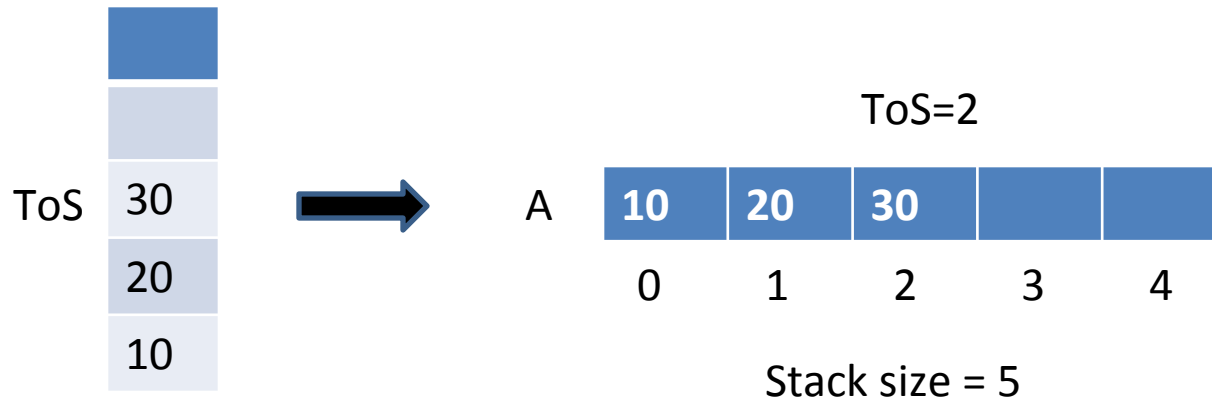
# Stack: Abstract Data Type

- Stack Operation: complexity

Operation	Time Complexity
PUSH()	$O(1)$
POP()	$O(1)$
Display()	$O(1)$
IsFullStack()	$O(1)$
IsEmptyStack()	$O(1)$
* Display all elements	$O(n)$

# Stack: Abstract Data Type

- Stack
  - Implementation
    - Using array
    - Using Linked-list (will be described later)
  - Array implementation



For an empty  
Stack, ToS is  
set at -1

# Stack: Abstract Data Type

- Stack

- Disadvantage

- Stack size is fixed
    - Stack size may be increased dynamically but it is very cost effective (for array implementation)
    - Data insertion, deletion and accessing is restricted (can be performed one by one and from one end of the stack)

# Stack: Abstract Data Type

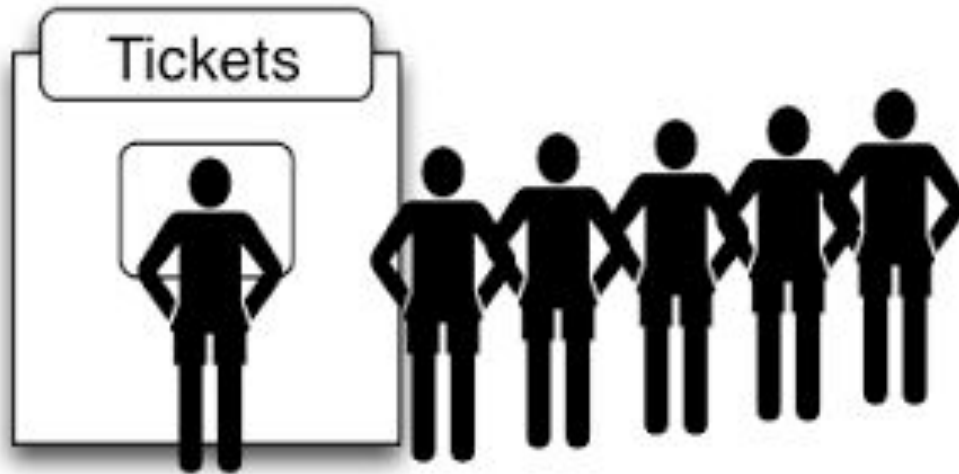
- Stack
  - Applications
    - In-fix to post-fix expression conversion
    - Evaluation of mathematical expression (post-fix)
    - Implementing function calls including recursion
    - Page visiting history in web browser
    - Undo sequence in a text editor
    - Implementing operations of other data structures
      - Traversal in Tree data structure
      - Traversal in Graph data structure

# Queue

(Abstract Data Type)

# Queue

□ Real Scenario to Data Structure



# Queue: Abstract Data Type

- Queue

- Properties

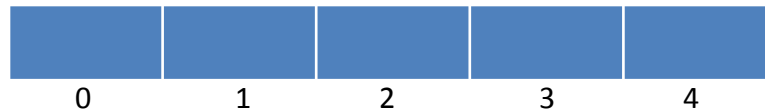
- Queue is defined as a **First In First Out (FIFO)** data structure
      - The first data inserted into the Queue to be deleted first
    - The associated operations of a Queue are also defined with the data structure that is why it is considered as an **ADT**
    - The **first element** of the Queue is pointed by **FRONT** pointer
    - The **last element** of the Queue is pointed by **REAR** pointer
    - New element is inserted at **REAR** end
    - An element is accessed or deleted from **FRONT** end

# Queue: Abstract Data Type

- Queue

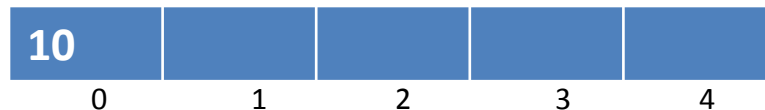
- Representation

F=R=null



Empty Queue

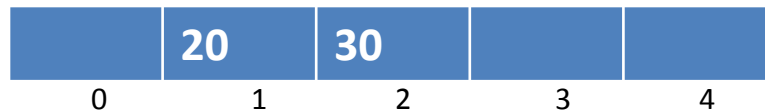
F=R=0



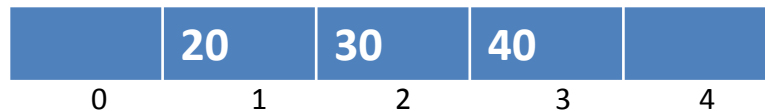
F=0 , R=1



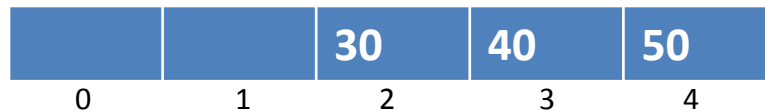
F=1 , R=2



F=1 , R=3



F=2 , R=4



Queue Overflow

F=FRONT  
R=REAR



# Queue: Abstract Data Type

- Queue

- Operations

- ENQUEUE (data insertion into queue)
    - DEQUEUE (data deletion from queue)

Primary operation

- Front / Display (showing element of queue)
    - QueueSize ( returns the total element)
    - IsFullQueue (checks if Queue is overflow)
    - IsEmptyQueue (checks if Queue is underflow)

Auxiliary operation

# Queue: Abstract Data Type

- Queue variations

- Simple Queue

- Data can be inserted at one end, deleted from the other end
    - Rear pointer will always be in right side of front pointer

- Circular Queue

- Data can be inserted circularly if front end is vacant
    - Rear pointer can come, circularly, before front pointer

- Double Ended Queue (Deque)

- Data can be inserted or removed from either end of the queue

- Priority Queue

- Each element is associated with a priority, based on which it is processed (accessed or deleted)

# Queue: Abstract Data Type

- Queue Operation: simple queue

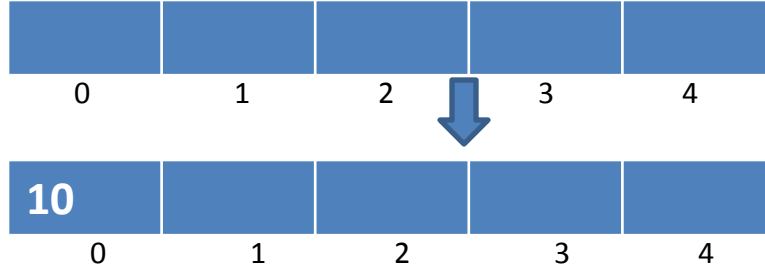
- ENQUEUE

- This function inserts one element at the REAR position of the Queue if it is not full

F=R=null

insert 10

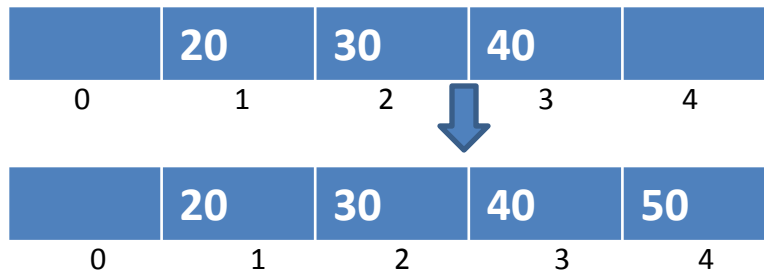
F=R=0



F= 1 , R= 3

insert 50

F= 1 , R=4



```
void ENQUEUE(data)
```

```
{
```

```
  if IsFullQueue = TRUE
```

```
    print Q is full
```

```
  else
```

```
    if IsEmptyQueue = TRUE
```

```
      F := 0 and R:= 0
```

```
    else
```

```
      R:= R+1
```

```
      Q(R) := data
```

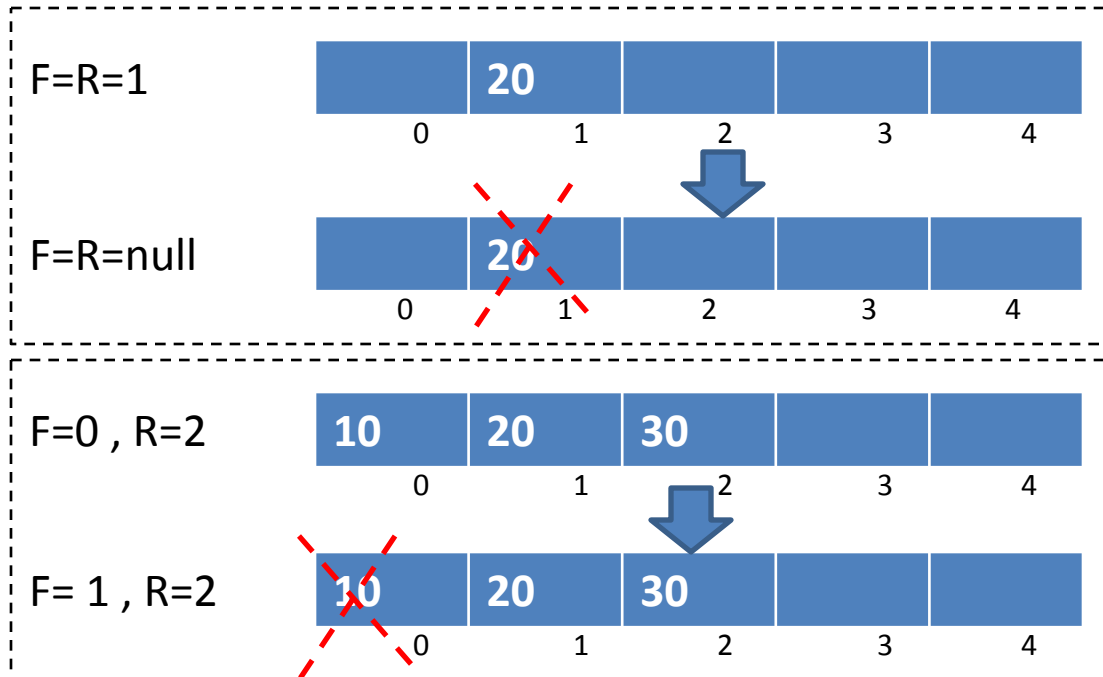
```
}
```

# Queue: Abstract Data Type

- Queue Operation: simple queue

- DEQUEUE

- This operation deletes the front element of the Queue if it is not empty



```
int DEQUEUE()
{
    if IsEmptyQueue = TRUE
        return NULL
    else
        if F = R
            data := Q(F)
            F := null and R:= null
        else
            data := Q(F)
            F:= F+1
        return data
}
```

# Queue: Abstract Data Type

- Queue Operation: simple queue

- Front / Display

- Front function displays the front element of the Queue
    - All elements can also be displayed through an auxiliary pointer without shifting FRONT or REAR

```
int Front()
{
    if IsEmptyQueue = TRUE
        return NULL
    else
        return Q(F)
}
```

```
void Display()
{
    if IsEmptyQueue = TRUE
        print Q is empty
    else
        for i= F to R
            print Q(i)
}
```

# Queue: Abstract Data Type

- Queue Operation: simple queue
  - QueueSize
    - This function returns the counting of elements present in the current queue

```
int QueueSize()
{
    if F = null and R = NULL
        return 0
    else
        for i = F to R
            count := count +1
        return count
}
```

# Queue: Abstract Data Type

- Queue Operation: simple queue
  - IsFullQueue
    - This function checks whether the Queue is full or not
    - We cannot insert data into Queue if it is full

```
Boolean IsFullQueue()  
{  
    if R = Max_Size  
        return TRUE  
    else  
        return FALSE  
}
```

# Queue: Abstract Data Type

- Queue Operation: simple queue
  - IsEmptyQueue
    - This function checks whether the Queue is empty or not
    - We cannot delete or display the Queue if it is empty

```
Boolean IsEmptyQueue()
{
    if F = null and R = null
        return TRUE
    else
        return FALSE
}
```



# Queue: Abstract Data Type

- Queue Operation: complexity

Operation	Time Complexity
Enqueue()	$O(1)$
DeQueue()	$O(1)$
Display()	$O(n)$
QueueSize()	$O(n)$
IsFullQueue()	$O(1)$
IsEmptyQueue()	$O(1)$

# Queue: Abstract Data Type

- Queue

- Disadvantage

- Queue size is fixed
    - Queue size may be increased dynamically but it is very cost effective (for array implementation)
    - Data insertion, deletion and accessing is restricted

# Queue: Abstract Data Type

- Queue

- Applications

- Job scheduling by Operating System for same priority jobs
    - Handling multiprocessing in computing devices
    - Implementing first-come-first-serve based real-life operations
    - Waiting time of a customers at call centre
    - Implementing operations of other data structures
      - Various Graph operations (shortest path finding, finding MST)
      - Traversal in Graph data structure

# Queries?