

Data Structures & Algorithms

(PCC-CS 301)

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Topics Covered

1. Linear Data Structure
 - a. Circular Queue

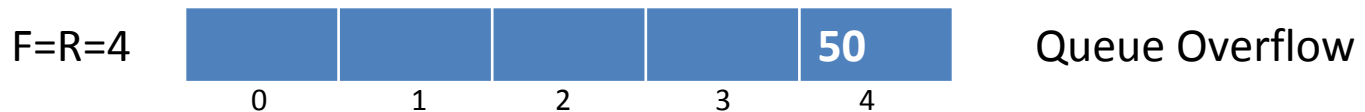
Circular Queue

- Why necessary?

- Problem in simple Queue implementation

- Memory utilization is poor

- Wastage of memory in following case where new data cannot be inserted although maximum cells are vacant



- Solution in Circular Queue

- Utilization of the unused spaces



After inserting new data: 60, 70, 80, 90

Circular Queue

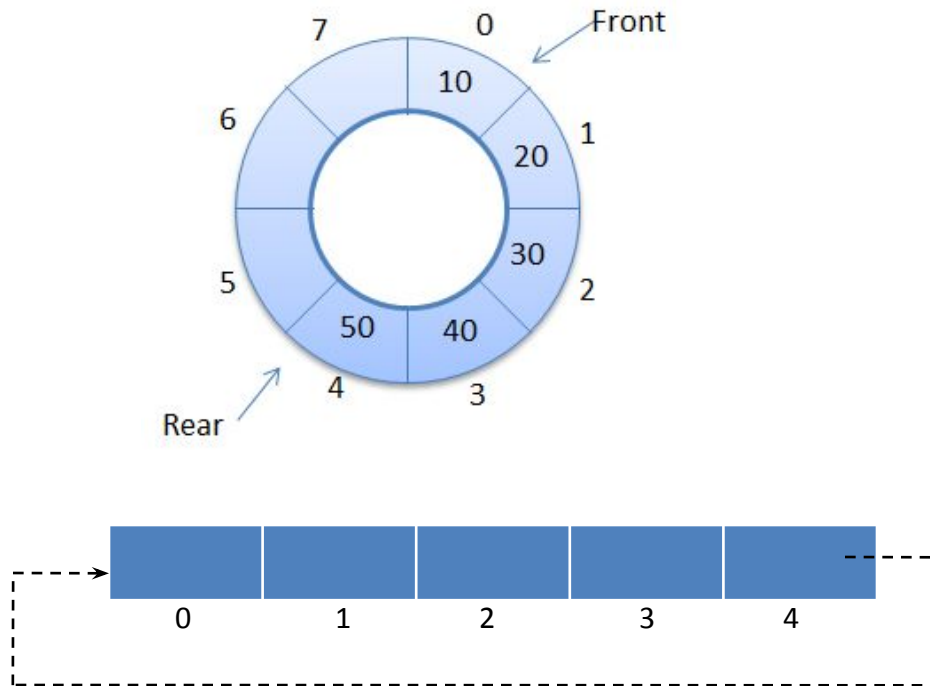
- Circular Queue

- Properties

- It is defined as a **First In First Out (FIFO)** data structure
 - The first data inserted into the Queue to be deleted first
 - The **first element** of the Queue is pointed by **FRONT** pointer
 - The **last element** of the Queue is pointed by **REAR** pointer
 - New element is inserted through **REAR** pointer
 - An element is accessed or deleted through **FRONT** pointer
 - **REAR** pointer can rotate circularly to insert new element into the queue if the initial positions are found vacant

Circular Queue

- Circular Queue
 - Representation

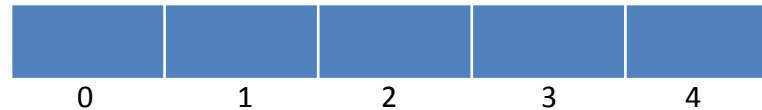


Circular Queue

- Circular Queue

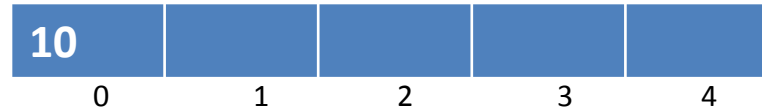
- Different cases

F=R=null



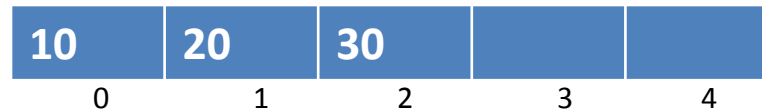
Empty Queue

F=R=0

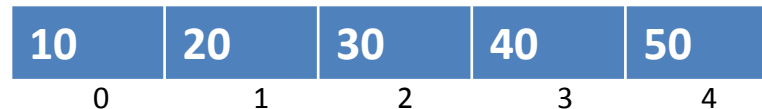


F=FRONT
R=REAR

F=0 , R=2

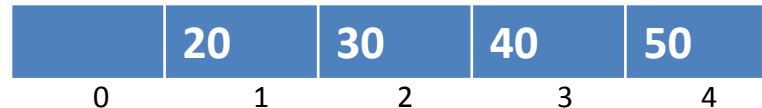


F=0 , R=4



Queue Overflow

F=1 , R=4



F=1 , R=0



Queue Overflow

Circular Queue

- Circular Queue

- Operations

- ENQUEUE (data insertion into queue)
 - DEQUEUE (data deletion from queue)

Primary operation

- Front / Display (showing element of queue)
 - QueueSize (returns the total element)
 - IsFullQueue (checks if Queue is overflow)
 - IsEmptyQueue (checks if Queue is underflow)

Auxiliary operation

Circular Queue

- Operation

- ENQUEUE

- This function inserts one element at the REAR position of the Queue if it is not full

```
void ENQUEUE(data)
{
    if IsFullQueue = TRUE
        print Q is full
    else
        if IsEmptyQueue = TRUE
            F := 0 and R:= 0
        else
            if F > 0 and R = Max_Size
                R:= 0
            else
                R:=R+1
            Q(R) := data
}
```

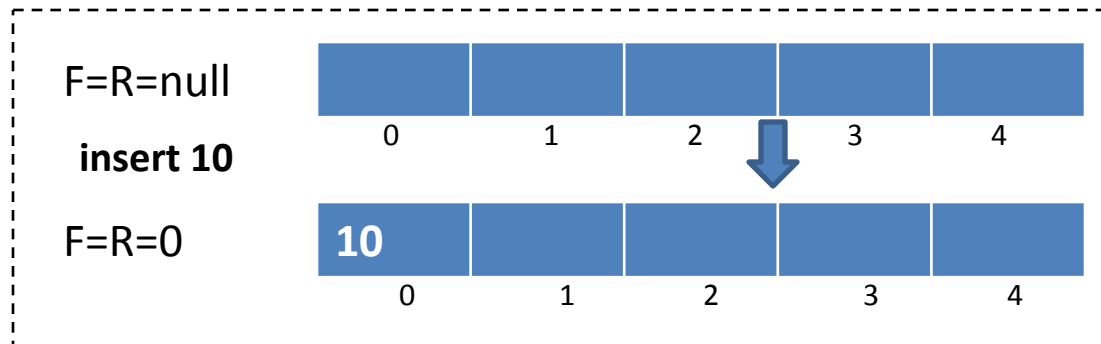


```
void ENQUEUE(data)
{
    if IsFullQueue = TRUE
        print Q is full
    else
        if IsEmptyQueue = TRUE
            F := 0 and R:= 0
        else
            R:= (R+1) mod (Max_Size)
        Q(R) := data
}
```


Circular Queue

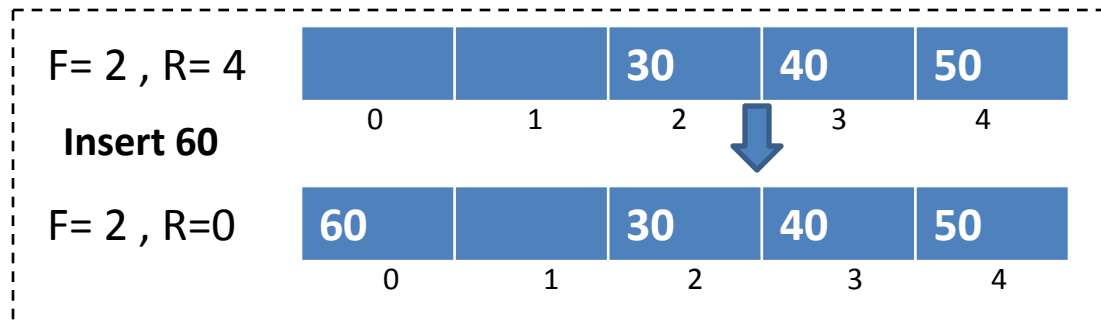
- Operation

- ENQUEUE (example)



insert 20 20

$$\begin{aligned}
 R &= (0+1) \bmod (\text{Max_Size}) \\
 &= (0+1) \bmod (5) \\
 &= 1 \bmod 5 \\
 &= 1
 \end{aligned}$$



$$\begin{aligned}
 R &= (R+1) \bmod (\text{Max_Size}) \\
 &= (4+1) \bmod (5) \\
 &= 5 \bmod 5 \\
 &= 0
 \end{aligned}$$

Circular Queue

- Operation

- DEQUEUE

- This operation deletes the front element of the Queue if it is not empty

```
int DEQUEUE()
{
    if IsEmptyQueue = TRUE
        return NULL
    else
        data := Q(F)
        if F = R
            F := null and R:= null
        else
            if F = Max_Size
                F := 0
            else
                F := F+1
        return data
}
```

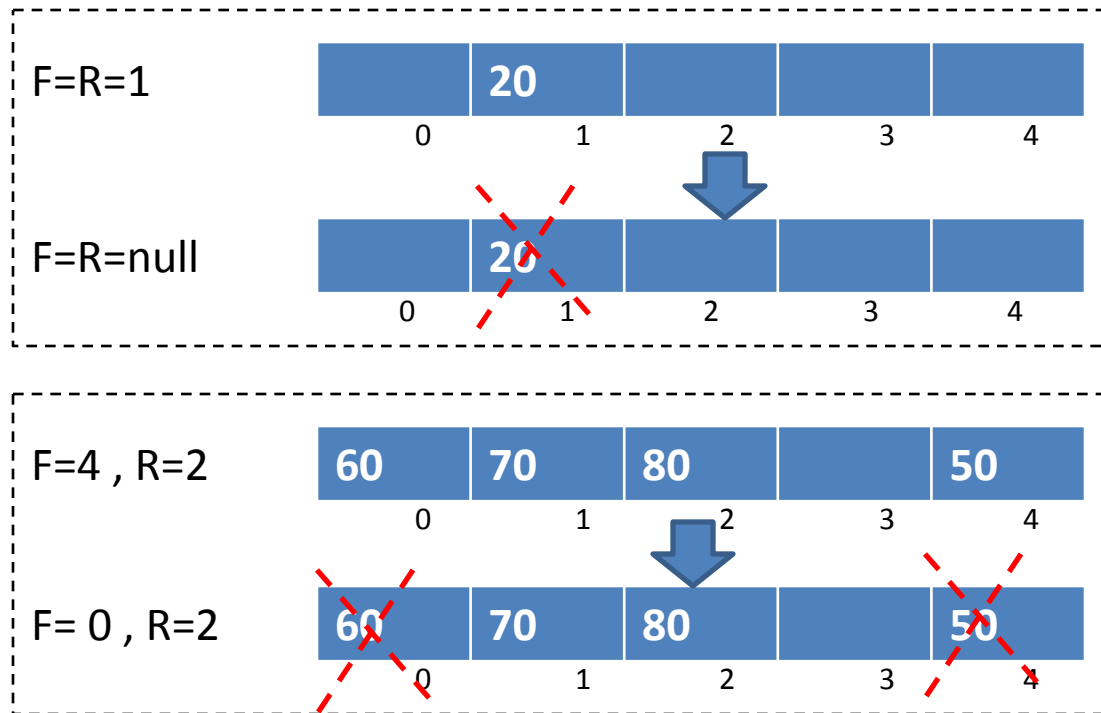


```
int DEQUEUE()
{
    if IsEmptyQueue = TRUE
        return NULL
    else
        data := Q(F)
        if F = R
            F := null and R:= null
        else
            F := (F+1) mod (Max_Size)
        return data
}
```

Circular Queue

- Operation

- DEQUEUE (example)



$$\begin{aligned}
 F &= (F+1) \bmod (\text{Max_Size}) \\
 &= (4+1) \bmod (5) \\
 &= 5 \bmod 5 \\
 &= 0
 \end{aligned}$$

Dequeue()

$$\begin{aligned}
 F &= (F+1) \bmod (\text{Max_Size}) \\
 &= (0+1) \bmod (5) \\
 &= 1
 \end{aligned}$$

$F=1, R=2$

Circular Queue

- Operation

- Front / Display

- Front function displays the front element of the Queue
 - All elements can also be displayed through an auxiliary pointer without shifting FRONT or REAR

```
int Front()
{
    if IsEmptyQueue = TRUE
        return NULL
    else
        return Q(F)
}
```

```
void Display()
{
    if IsEmptyQueue = TRUE
        print Q is empty
    else
        for i= F to R
            print Q(i)
}
```

Circular Queue

- Operation

- QueueSize

- This function returns the counting of elements present in the current queue

```
int QueueSize()
{
    if F = null and R = NULL
        return 0
    else
        for i = F to R
            count := count +1
        return count
}
```

Circular Queue

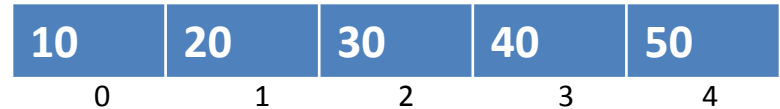
- Operation

- IsFullQueue

- This function checks whether the Queue is full or not
 - We cannot insert data into Queue if it is full

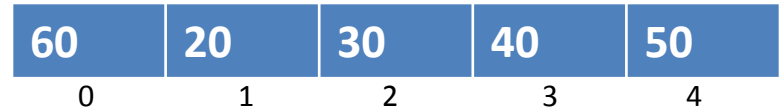
```
Boolean IsFullQueue()  
{  
    if R = Max_Size or F = R+1  
        return TRUE  
    else  
        return FALSE  
}
```

F=0 , R=4



Queue Overflow

F=1 , R=0



Circular Queue

- Operation

- IsEmptyQueue

- This function checks whether the Queue is empty or not
 - We cannot delete or display the Queue if it is empty

```
Boolean IsEmptyQueue()
{
    if F = null and R = null
        return TRUE
    else
        return FALSE
}
```

Circular Queue

- Operation: complexity

Operation	Time Complexity
Enqueue()	$O(1)$
DeQueue()	$O(1)$
Display()	$O(n)$
QueueSize()	$O(n)$
IsFullQueue()	$O(1)$
IsEmptyQueue()	$O(1)$

Circular Queue

- Circular Queue

- Applications

- Memory management
 - To maintain the list of unused memory. As soon as any memory gets free by any process, it is added at rear end in the circular queue
 - Computer controlled traffic system
 - Circular queue is used to switch on the traffic lights one-by-one repeatedly
 - CPU scheduling (in operating system)
 - Operating system maintains a circular queue to store the ready (or waiting for some event to occur) processes to be executed

Queries?