

# Theory of Computation: [7M-10M]

## 1) Basics

- \*\*\* 2) Regular Languages : —
- Regular Expression
  - FA
  - RG
  - Regulars & Non-Regulars
  - Closure properties
  - P.L. & FA with o/p

3) DCFLs & CFLs

4) TM & Undecidability

## Basics:

- 1) What is TDC?
- 2) TDC Applications?
- 3) Chomsky Hierarchy
- 4) Symbol, Alphabet, String, Language, Automata, Grammat
- 5) Operations on strings
- 6) Operations on languages

TOC



Solving Problems



Computable ?



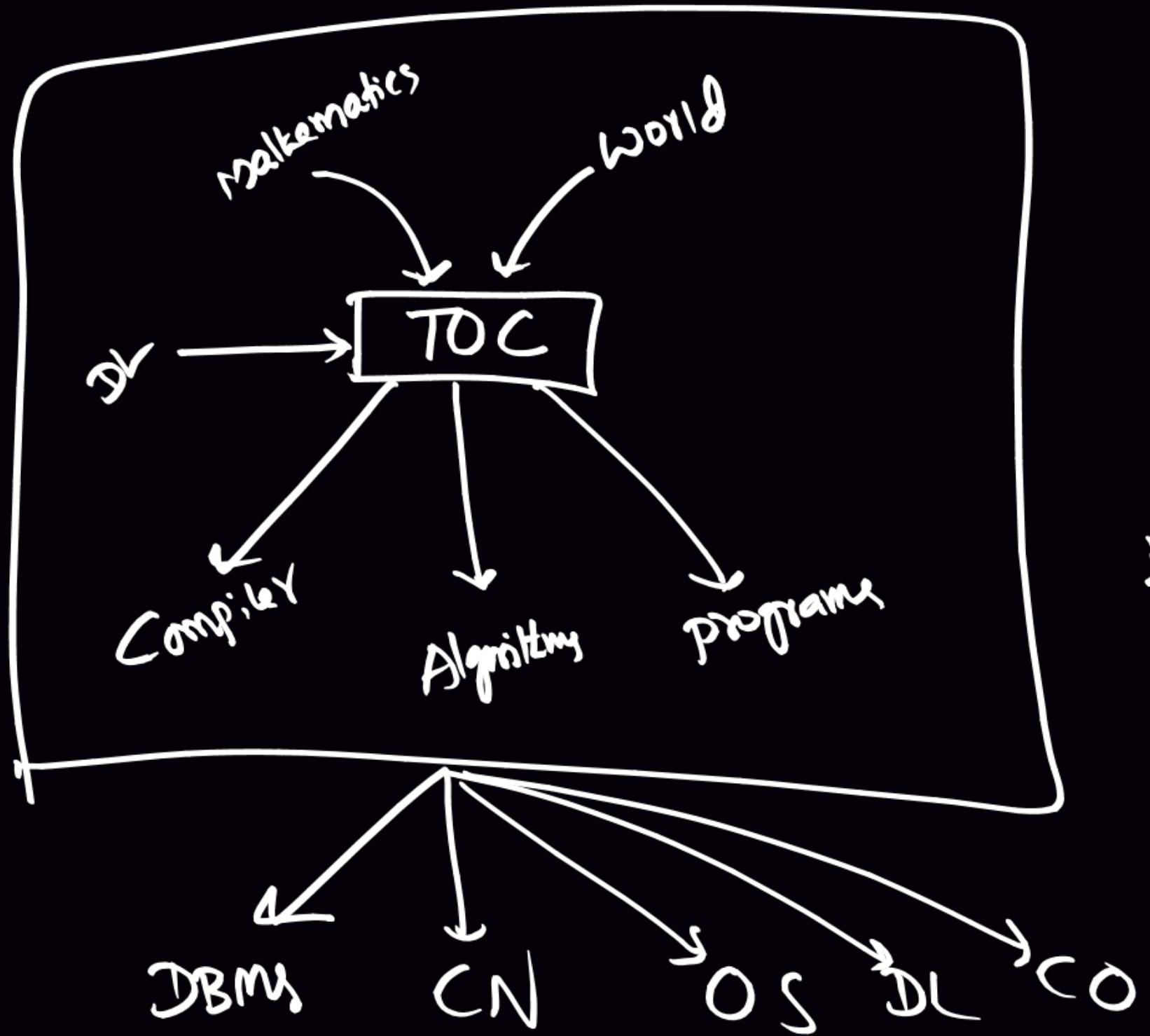
If Computable , complexity ?



## Applications :

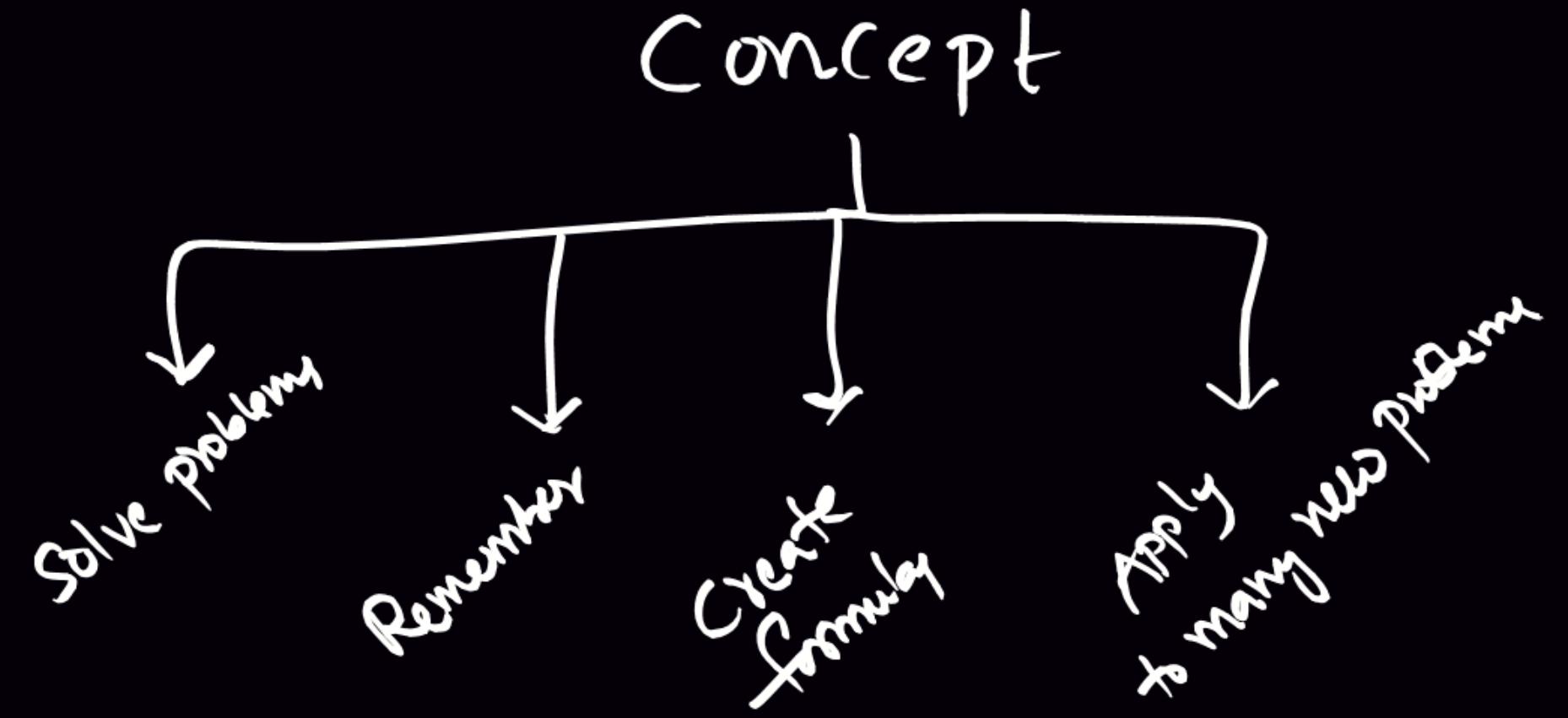
- Compiler Design
- Spell checker
- Traffic Signal
- Designing Digital Circuit
- AI
- :

[ is comp, 2's comp, Adder,  
Subtractors, sequential detectors, ... ]



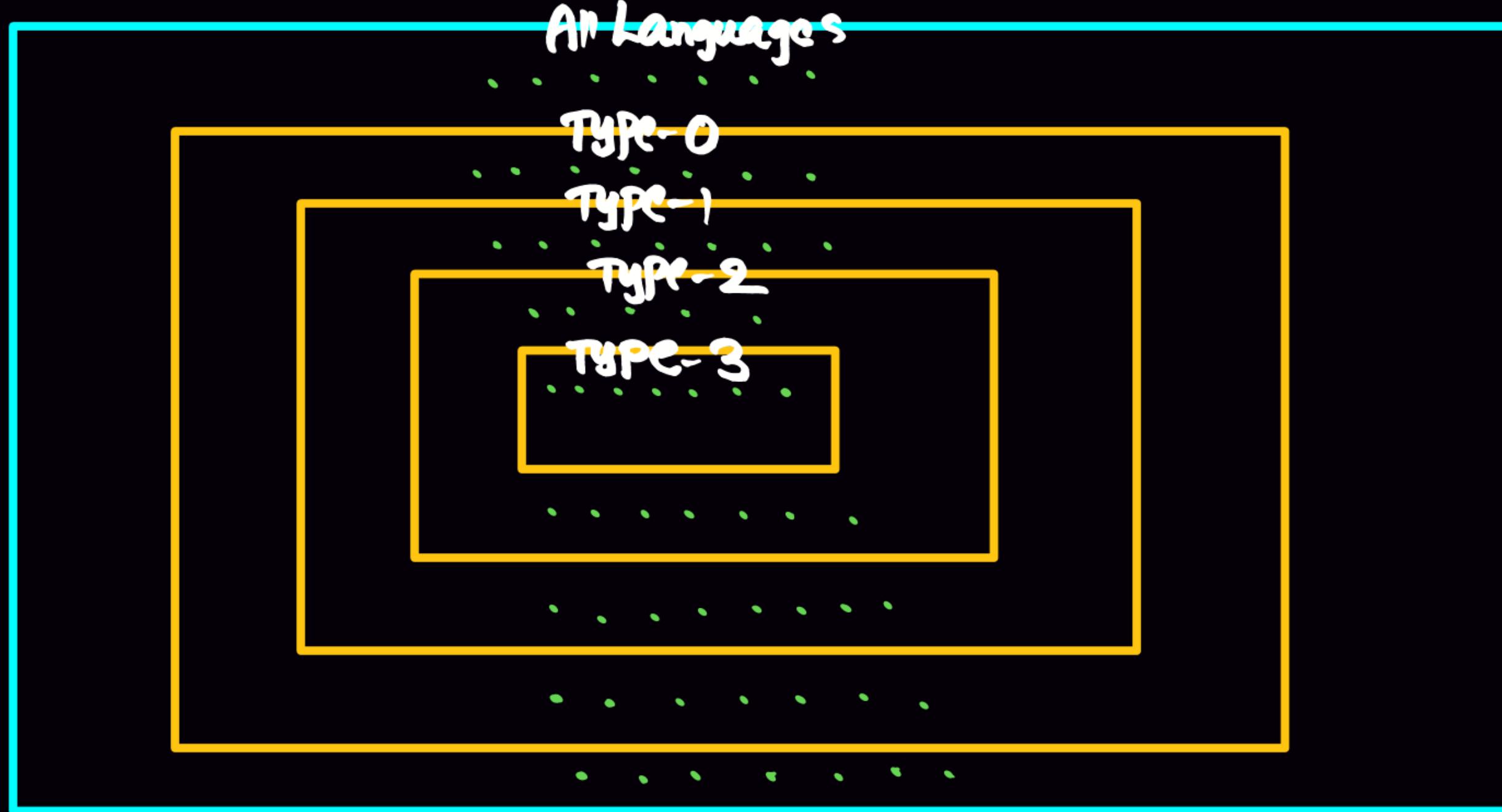
1<sup>st</sup>: Concept ?  
 ↓  
 2<sup>nd</sup>: Formula ?

90-95 Lectures



# Chomsky Hierarchy :

---



Type-3 class = Set of all regular languages

Type-2 class = Set of all CFLs

Type-1 class = Set of all CSLs

Type-0 class = Set of all Recursively Enumerable languages

classes:

$$\boxed{\text{Type-3} \subset \text{Type-2} \subset \text{Type-1} \subset \text{Type-0}}$$

Type-3 class :

- Regular language  $\in$  Type-3 class
- Finite Automata
- Regular Expression
- Regular Grammar

Class: Type-3

Language: Regular

Automata: FA

Grammar: RG

Type-2

CFL  
(Context free)

PDA

CFG

Type-1

CSL  
(Context sensitive)

LBA

CSG

Type-0

REL

TM

UG

(Recursively Enumerable)

## Basics:

TOC :

Symbol

Alphabet ( $\Sigma$ ) ( $\Delta$ )

Word/String

Language

C Language

Characters

Character set

Tokens

program

syntax  
semantics  
logic?

English Language:

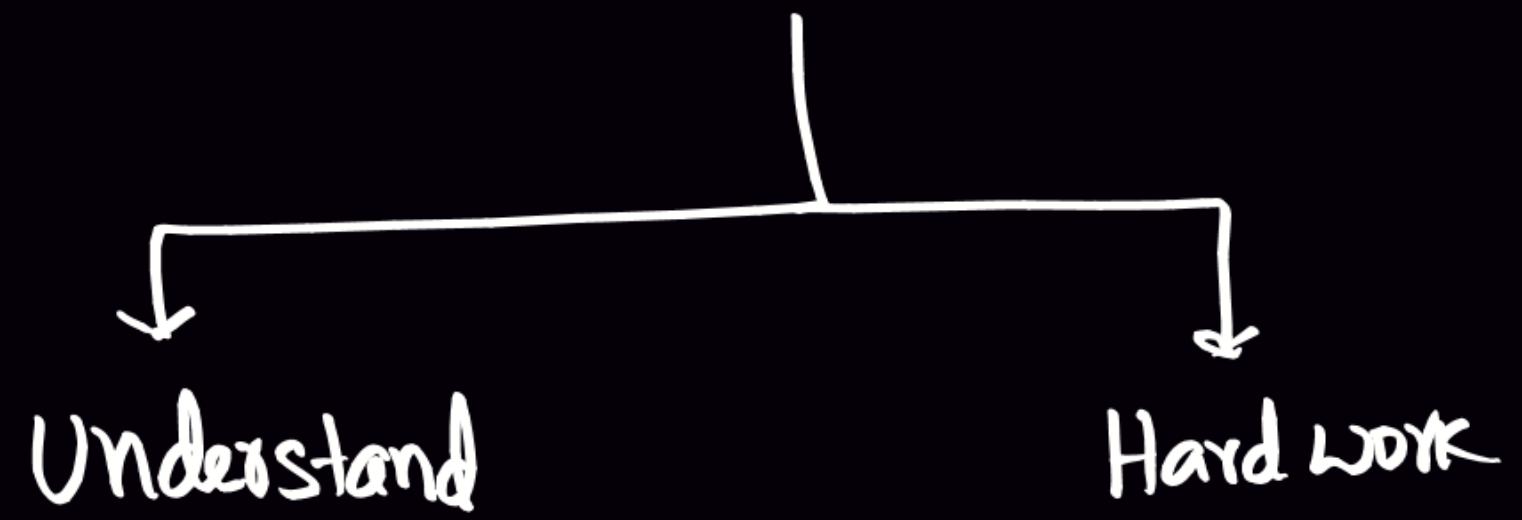
Letters (a, b, c, ..., z)  
symbols

Alphabet = {a, b, c, ..., z}  
(Set)

Words: Apple  
Ball  
Cat  
:

Sentence:

Learn ?



## Symbol :

- Smallest unit
- It can be any
- It should be given
- It is one

abc

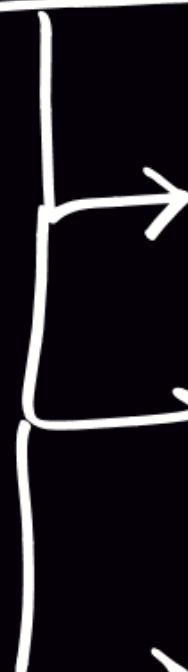
Symbols: a, b, c  
 $|a| = 1$   
 $|b| = 1$   
 $|c| = 1$   
 $|\underline{abc}| = 3$

Symbols: ab, c, def  
 $|ab| = \text{no meaning}$   
 $|c| = 1$   
 $|def| = 1$   
 $|\underline{abc}| = 2$

Symbols: abc, de, fgh  
 $|\underline{abc}| = 1$   
 $|\underline{def}| = 1$

a /

## Alphabet :



$$\Sigma = \{a, b\}$$

$$|a|=1$$

$$|b|=1$$

$$\Sigma = \{\text{gate, exam}\}$$

$$|\text{gate}|=1$$

$$|\text{exam}|=1$$

$$\Sigma = \{a, b, c, \dots, z\}$$

$$|\text{gate}|=4$$

$$|\text{rank}|=4$$

$$|\text{topper}|=6$$

$$\Sigma = \{(0,0), (0,1), (1,0), (1,1)\}$$

$$\left| \begin{array}{ccccc} (0,0) & (1,0) & (1,1) & (0,0) & (0,1) \\ \underline{0,0} & \underline{1,0} & \underline{1,1} & \underline{0,0} & \underline{0,1} \end{array} \right| = 5$$



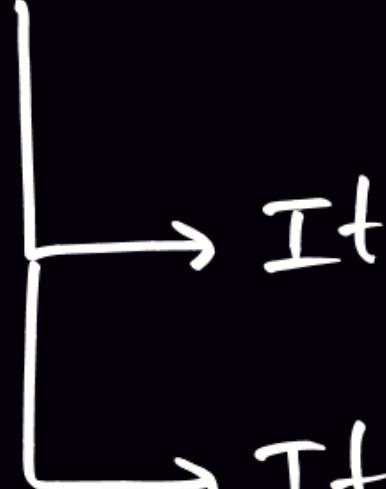
$$\Sigma = \{\text{Q}, \text{S}, \text{D}\}$$

$$\left| \begin{array}{ccc} \text{Q} & \text{Q} & \text{D} \end{array} \right| = 3$$

$$\Sigma = \{abc, 01, +- \}$$

$$\left| \begin{array}{cccc} a & b & c & a & b & c \\ \underline{a} & \underline{b} & \underline{c} & \underline{a} & \underline{b} & \underline{c} \\ 0 & 1 & + & - & 0 & 1 \end{array} \right| = 5$$

String [word]:



→ It is a sequence of symbols

→ It is a finite sequence

$$\Sigma = \{a, b\}$$

zero length  
:  $\epsilon$

one sequence:  
(one length)

a  
b

two length:

aa  
ab  
ba  
bb

3 length

Strings:

aaa  
aab  
aba  
abb  
baa  
bab  
baq  
b9b  
b9a  
bbb

How many k-length

strings over  $\Sigma = \{a, b\}$ ?

2 choices  
2 choices

$2 \times 2 \times 2 \times \dots \times 2$  times  
 $= 2^k$  strings

$$\Sigma = \{a, b, c, d\}$$

How many 7 length strings?

4 choices  
4 choices

$$4 \times 4 \times 4 \times \dots \times 4 \text{ times} = 4^7$$

## Zero length string (Empty string) (Null strings)

- It is special string with zero no. of symbols.
- Denoted using  $\epsilon$  or  $\lambda$

$\Sigma = \{a, b\}$

$$|\epsilon| = | \ | = 0$$

a is symbol

b is symbol

IS  $\epsilon$  symbol?

- NO
- It is empty string

$\Sigma = \{a\} \Rightarrow$  Strings upto 3 length?  
 $(\leq 3)$

$\epsilon$

a

aa

aaa

$\Sigma = \{0, 1, 2\}$   $\Rightarrow$  write strings upto 2 length.

$\epsilon$	$^0 3$
0	$^1 3$
1	$^2 3$
2	
00	$^2 3^2$
01	
02	
10	
11	
12	
20	
21	
22	

How many strings upto 2 length?

$$= 3^0 + 3^1 + 3^2$$

$$= a^0 + a^1 + a^2 + \dots + a^n$$

$$= \frac{n+1}{a-1}$$

$$= \frac{3^3 - 1}{3 - 1} = \frac{26}{2} = 13$$

Language [Set] [collection]

↳ Set of strings over  $\Sigma$ .

$$\Sigma = \{a, b\}$$

$$L_1 = \{\} = \emptyset = \text{Empty language}$$

$$L_2 = \{\epsilon\}$$

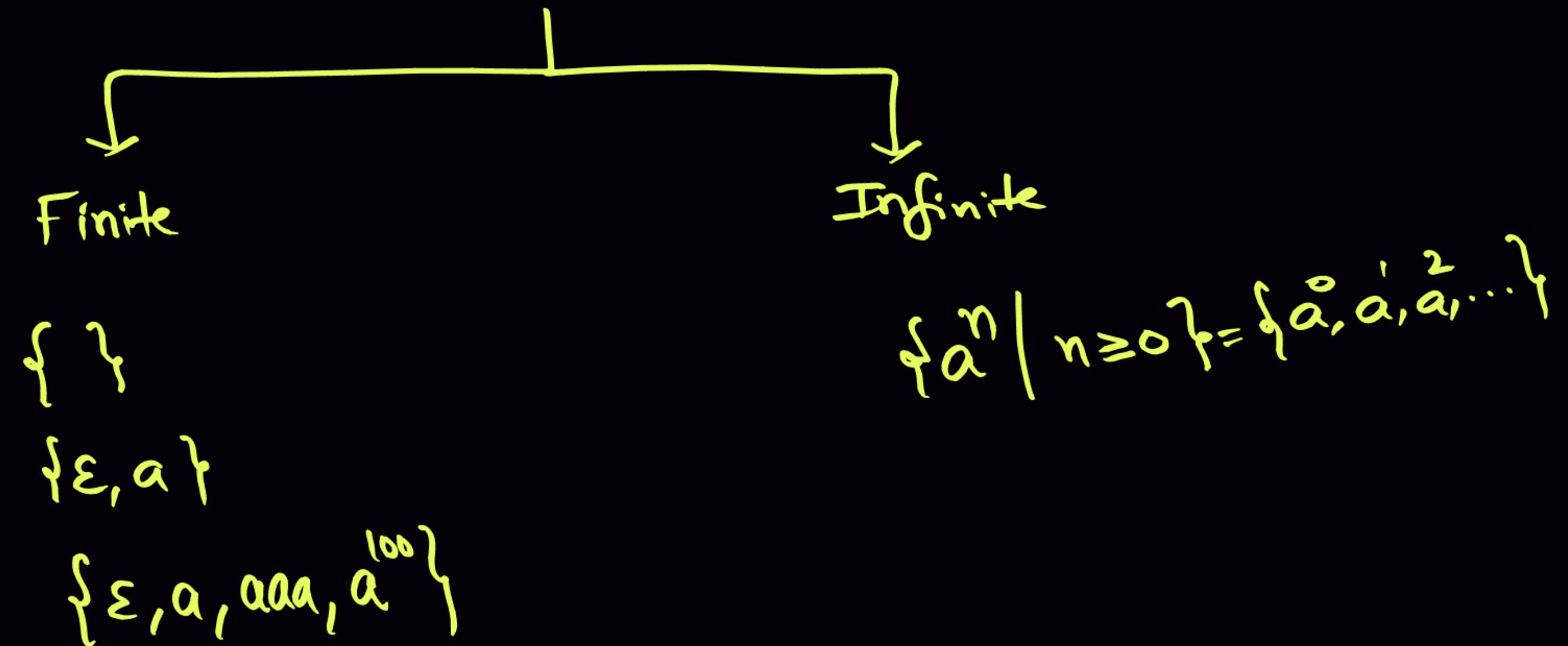
$$L_3 = \{\epsilon, a, abbb\}$$

$\epsilon$  string  
 $\emptyset$  lang

$$|\epsilon| = 0$$

$$|\{\epsilon\}| = 1$$

# Language



$\epsilon$   
empty string

$\{\} = \phi$   
empty set

$\{\epsilon\}$   
non empty set  
which has one string.

$$|\epsilon| = 0$$

|String|  
Length of String

$$|\phi| = |\{\} = 0$$

|set|  
Size of Set  
No. of objects in Set

$$|\{\epsilon\}| = 1$$

Automata

↳ m/c

Grammar

↳ collection of rules

I want to find even.

problem

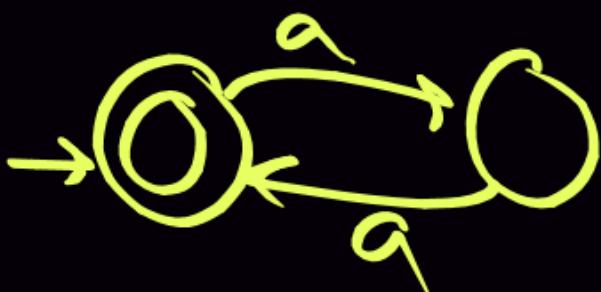
In real world

Even Language

$\{\epsilon, aa, a^4, a^6, \dots\}$

Language

In TOL



If Computable, we will show model  
(automata/grammar|...)

## H.W.:

I) Let  $w = aaaa$ .

1) No. of prefixes of  $w$  =

2) " Suffixes " =

3) " Substrings " =

II) Let  $w = abcd$

1) No. of prefixes =

2) No. of suffixes =

3) No. of Substring =

|String|

Length of string

|\underline{abc}| = 3

|Spt|

Site of xt

|\{1, \underline{5}, \underline{3}, 8\}| = 4

Symbol → any

Alphabet → collection of all symbols

String → sequence of symbols

Language → collection of strings