

Final Project Seminar

4/6/2021, CS 3510

Itinerary

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Project Overview



Project Introduction

- We will be designing algorithms for solving Minesweeper puzzles.
 - Board with squares
 - Some squares have mines
 - Other squares show the number of nearby mines
 - Don't click on the mines
- Naively guessing solutions is an exponential-time search



Only 2000's kids will remember this!

Our Algorithm Specifications

- Input:
 - size: $\langle m, n \rangle$
 - bombs: $\langle b \rangle$
 - safe: $\langle x, y \rangle$ (Guaranteed safe start)
 - grid: $\langle \text{string of length } m \cdot n \text{ with domain } [0-9] \rangle$
 - $[0 - 8]$ is the number of nearby bombs
 - $[9]$ is a bomb
 - $\text{Tile}[x][y] = \text{grid}[y \cdot n + x]$
- Output:
 - Bitstring of length $m \cdot n$
 - 0 represents no bomb
 - 1 represents bomb
 - Same access rules as input string
- Testing: $\text{diff}(\text{input_grid}, \text{output})$
 - Same \Rightarrow 
 - Different \Rightarrow 

Example Input

size: 10,10

bombs: 20

safe: 5,5

grid:

```
99311929293992123221139201921001110129100
00000112100000011291211001921929101221024
432392001999299200
```

| | | | | | | | | | |
|-----|-----|-----|-----|---|-----|-----|-----|---|-----|
| 1.0 | 1.0 | 3 | 1 | 1 | 1.0 | 2 | 1.0 | 2 | 1.0 |
| 3 | 1.0 | 1.0 | 2 | 1 | 2 | 3 | 2 | 2 | 1 |
| 1 | 3 | 1.0 | 2 | | 1 | 1.0 | 2 | 1 | |
| | 1 | 1 | 1 | | 1 | 2 | 1.0 | 1 | |
| | | | | | | 1 | 1 | 2 | 1 |
| | | | | | | 1 | 1 | 2 | 1.0 |
| 1 | 2 | 1 | 1 | | | 1 | 1.0 | 2 | 1 |
| 1.0 | 2 | 1.0 | 1 | | 1 | 2 | 2 | 1 | |
| 2 | 4 | 4 | 3 | 2 | 3 | 1.0 | 2 | | |
| 1 | 1.0 | 1.0 | 1.0 | 2 | 1.0 | 1.0 | 2 | | |

size: 10,10

bombs: 20

safe: 5,5

grid:

00011102920001921392122213942119910299201232

11392011291011101922210011122292223901922399

590111193399

| | | | | | | | | | |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| | | | 1 | 1 | 1 | | 2 | 1.0 | 2 |
| | | | 1 | 1.0 | 2 | 1 | 3 | 1.0 | 2 |
| 1 | 2 | 2 | 2 | 1 | 3 | 1.0 | 4 | 2 | 1 |
| 1 | 1.0 | 1.0 | 1 | | 2 | 1.0 | 1.0 | 2 | |
| 1 | 2 | 3 | 2 | 1 | 1 | 3 | 1.0 | 2 | |
| 1 | 1 | 2 | 1.0 | 1 | | 1 | 1 | 1 | |
| 1 | 1.0 | 2 | 2 | 2 | 1 | | | 1 | 1 |
| 1 | 2 | 2 | 2 | 1.0 | 2 | 2 | 2 | 3 | 1.0 |
| | 1 | 1.0 | 2 | 2 | 0.6 | 0.4 | 1.0 | 0.6 | 0.4 |
| | 1 | 1 | 1 | 1 | 0.4 | | | | |

Deliverables

- 2 implemented algorithms
- Accompanying project report
 - For each algorithm:
 - Algorithm explanation and analysis
 - Performance plots
- Details in project description

Team Formation

- Make a post on Piazza
- Pinned team forming feature

Constraint Satisfaction Problems

What is a CSP

A set of variable objects and constraints

- Triple $\langle X, D, C \rangle$
 - X: variables
 - D: domain of values for each X
 - C: constraints
- Example: Crossword Puzzle
 - X: Words
 - D: $[A-Z]^+$, Words
 - C: $\text{Word}_1[i] = \text{Word}_2[j]$,
 $\text{len}(\text{Word}_1) = 7$
... and so on

Solving a CSP

CSPs are usually approached as search problems

Backtracking

Constraint Propagation

Local Search

Backtracking

- “Depth-first search” in the problem domain

```
prefix = ""
def backtrack(proposed_suffix):
    potential_solution = prefix + proposed_suffix

    if is_answer(potential_solution):
        submit_answer(potential_solution)
    if breaks_constraint(potential_solution):
        return

    while s := next_possible_suffix(potential_solution):
        backtrack(s)

backtrack("")
```

Constraint Propagation

Modify the constraints into an equivalent simpler set of constraints.

- Can prove solvability
 - $\{A + B = 1, A + B = 2\} \Rightarrow \text{Impossible}$
- Can simplify constraints
 - $\{A + B = 1, A + B + C = 3\} \Rightarrow \{C = 2, A + B = 1\}$

Local Optimization

- Propose a (probably incorrect) solution, then try to change the proposed solution incrementally until it's as correct as possible

```
algorithm MIN-CONFLICTS is
  input: csp, A constraint satisfaction problem.
         max_steps, The number of steps allowed before giving up.
         current_state, An initial assignment of values for the variables in the csp.
  output: A solution set of values for the variable or failure.

  for i ← 1 to max_steps do
    if current_state is a solution of csp then
      return current_state
    set var ← a randomly chosen variable from the set of conflicted variables CONFLICTED[csp]
    set value ← the value v for var that minimizes CONFLICTS(var,v,current_state,csp)
    set var ← value in current_state

  return failure
```


Q&A